

Is the PTA stochastic gravitational wave background originating from Supermassive Black Hole mergers or from the Early Universe?

Francesco Shankar

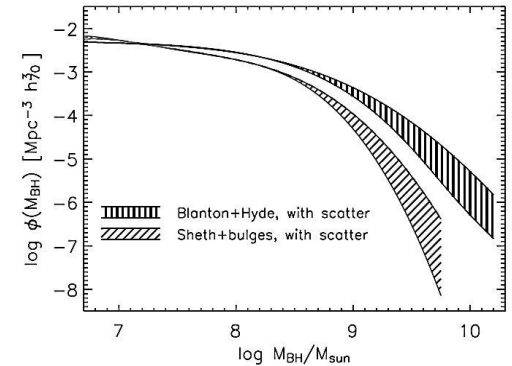
With: D. Roberts, Hao Fu, A. Smith, M. Bernardi, C. Marsden,
A. Lapi, N. Menci, V. Allevato, A. V. Alonso Tetilla, F.
Fontanot, L. Boco, and many more...

22/05/2025 – Round Table on New Avenues in Particle Cosmology

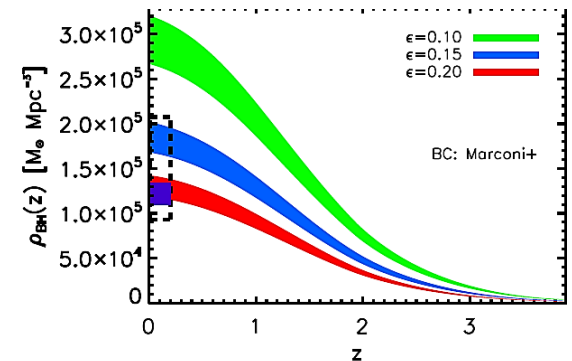
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WHAT I WILL DISCUSS:

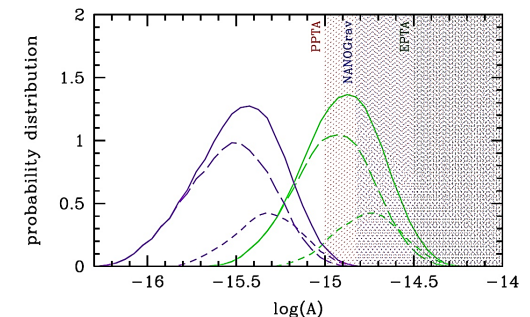
Introduction to SMBHs:
Relations and Demography



Evolution of SMBHs:
SMBH growth and feedback



Physical implications:
Mergers and GWs

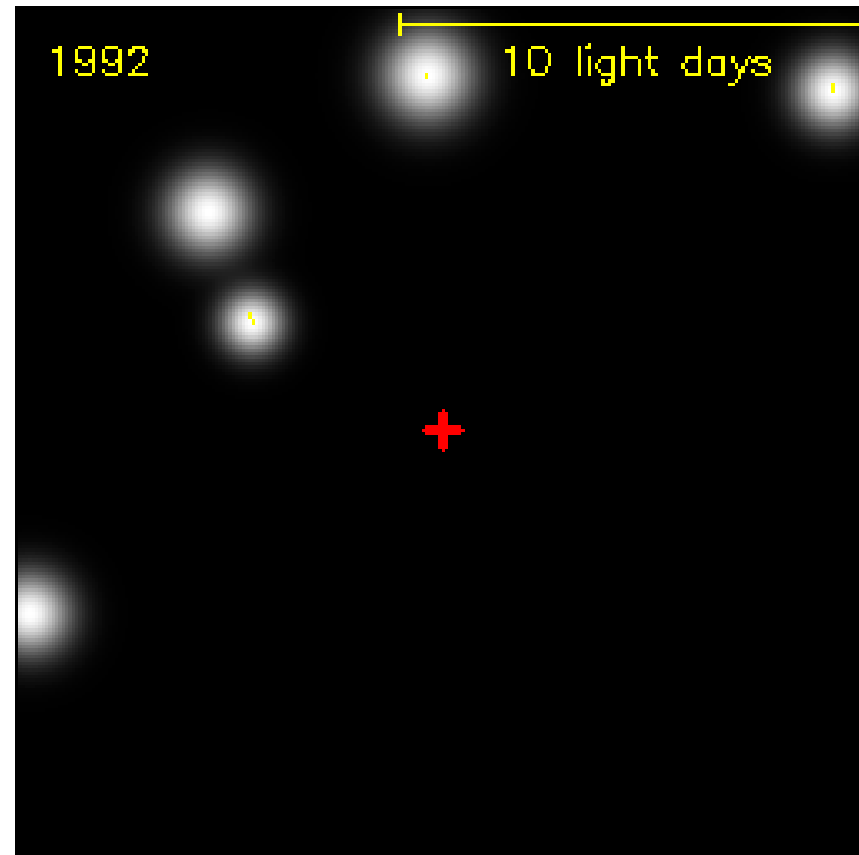


Introduction to SMBHs:

Relations and Demography

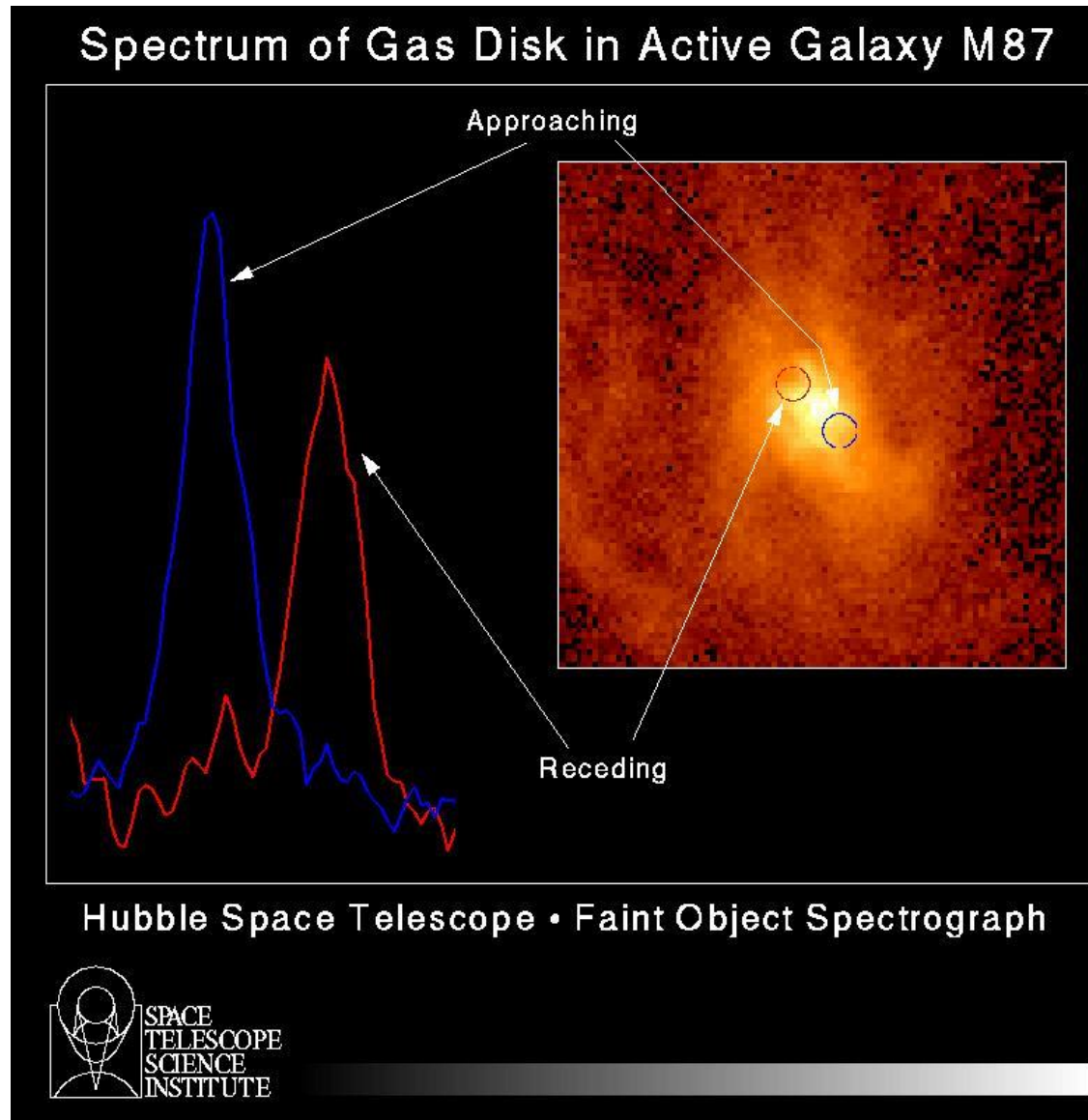
Evidence for central supermassive black hole in normal/inactive galaxies

- Orbits of luminous giant stars around the location of Sgr A*
- Derived mass $\sim 4 \times 10^6 M_{\odot}$

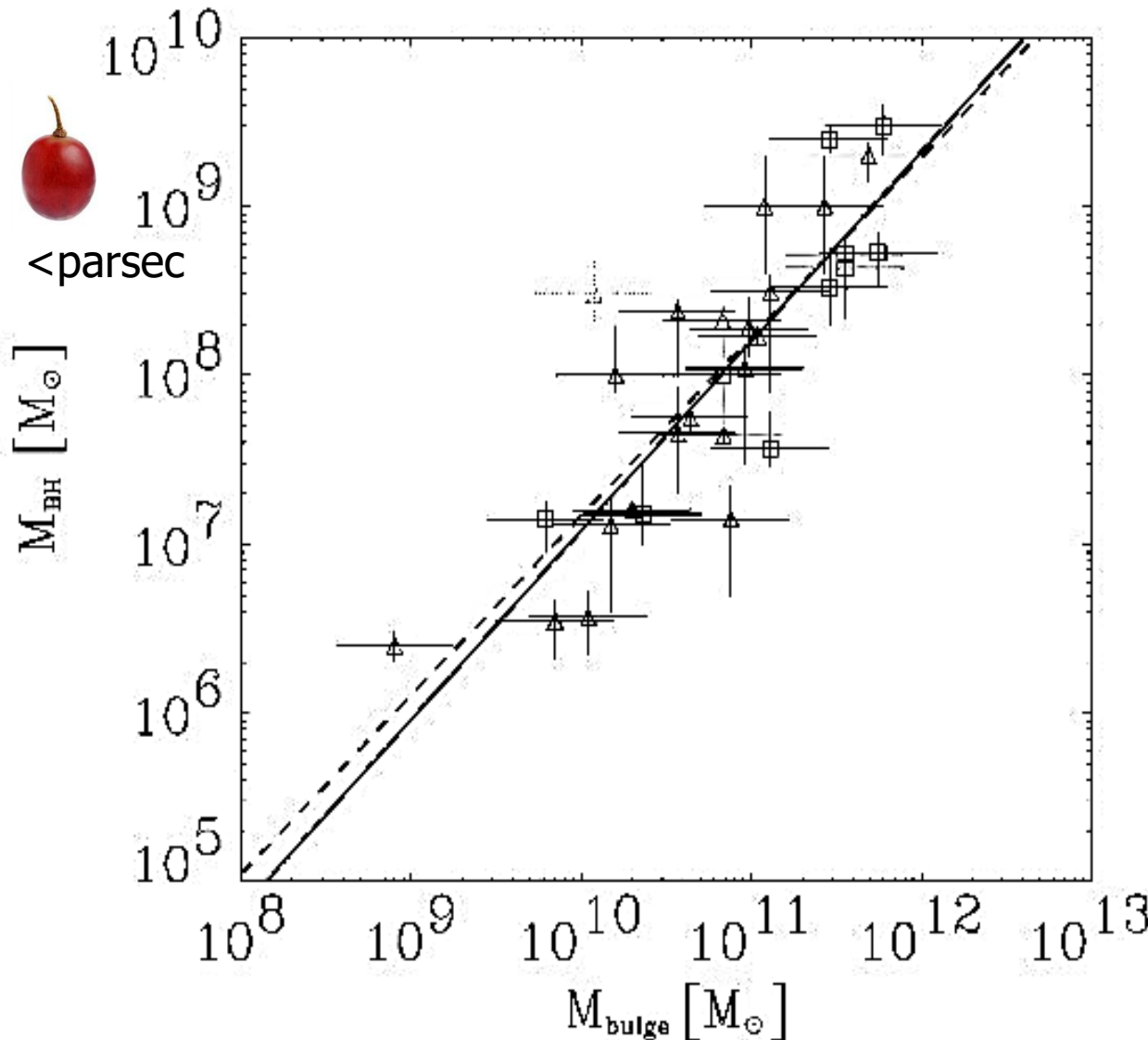


Evidence for SMBH in M87

- Velocity change of almost 500 km/s within 0.25" of nucleus
- $m v^2 / r = G M m / r^2$
- $\rightarrow M = v^2 r / G$
- $\rightarrow M \sim 1 \text{ billion } M_{\odot} !$



The «Magorrian» relation: $M_{\text{BH}}-M_{\text{bulge}}$



Marconi&Hunt 03
Haering&Rix 04

Thousands and
thousands of papers on
the **co-evolution**
of black holes and
galaxies

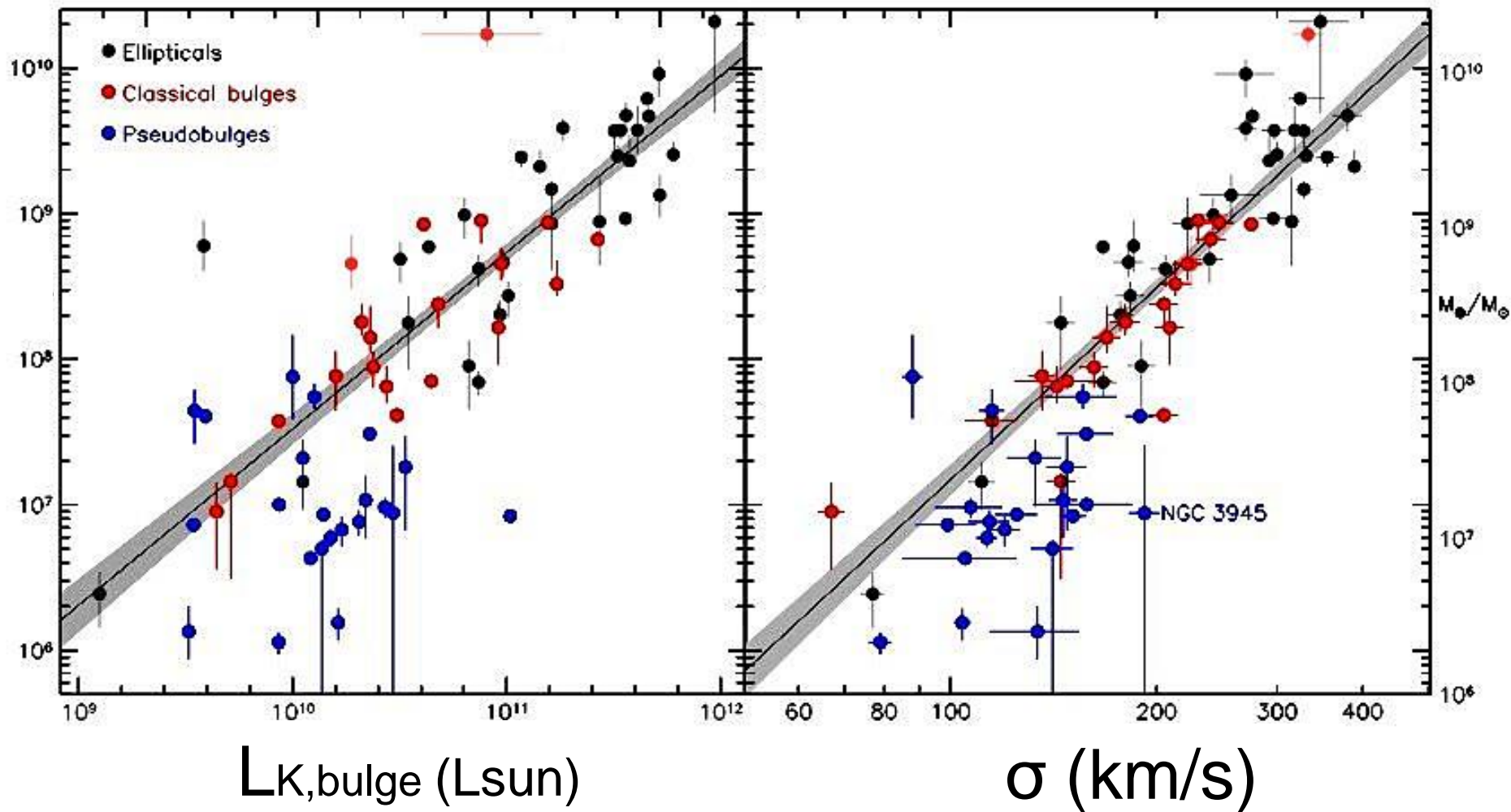


> kilo-parsec

Which is the most fundamental?

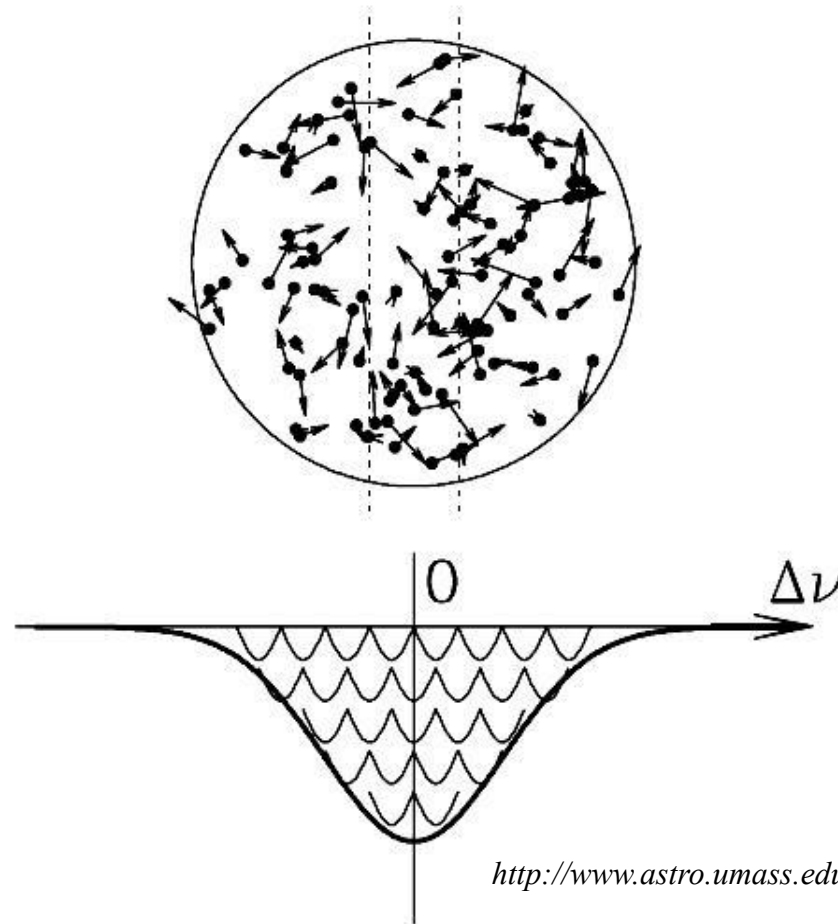
$M_{\text{BH}} \sim M_{\text{star}}$

$M_{\text{BH}} \sim \sigma^{4-5}$



Kormendy & Ho 13

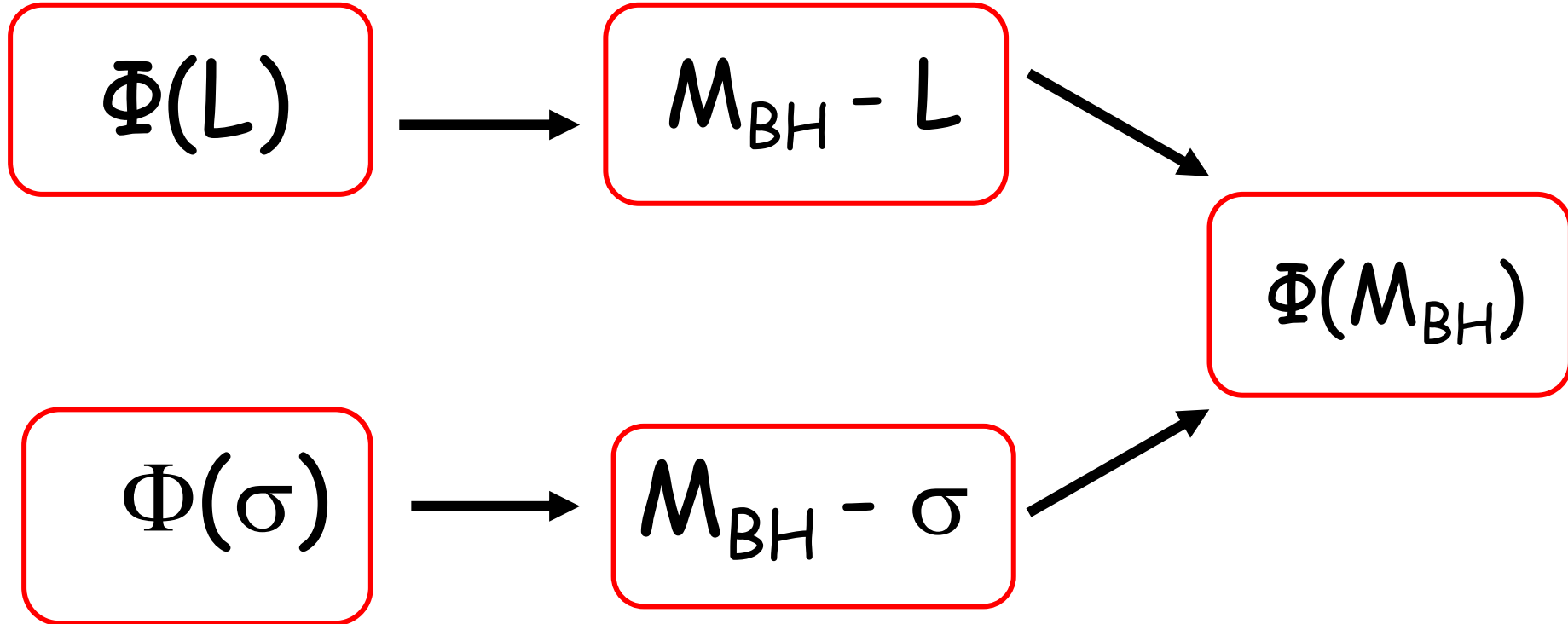
Radial velocity dispersion



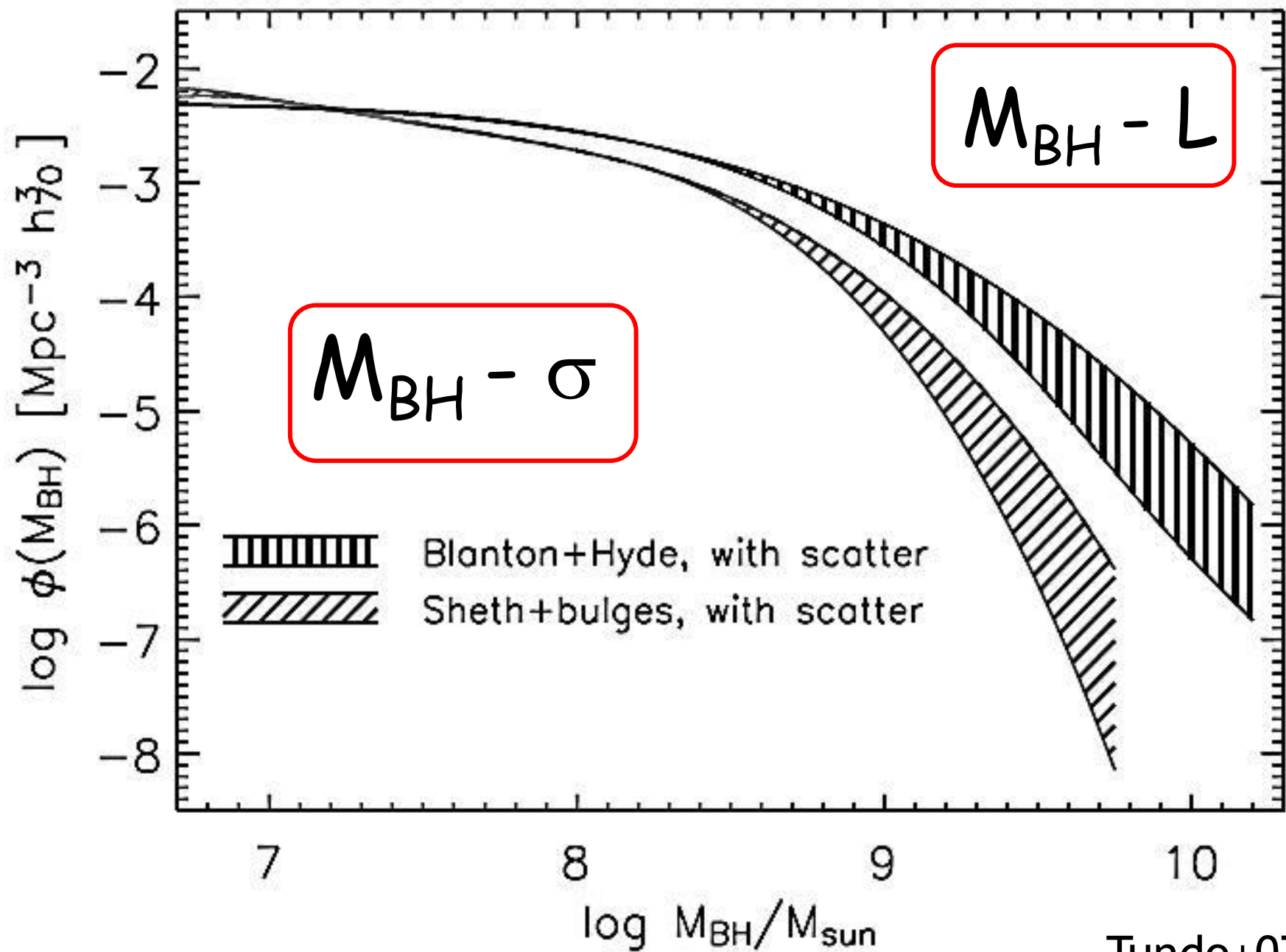
<http://www.astro.umass.edu/~hjmo/astro330/html/dir/reading.pdf>

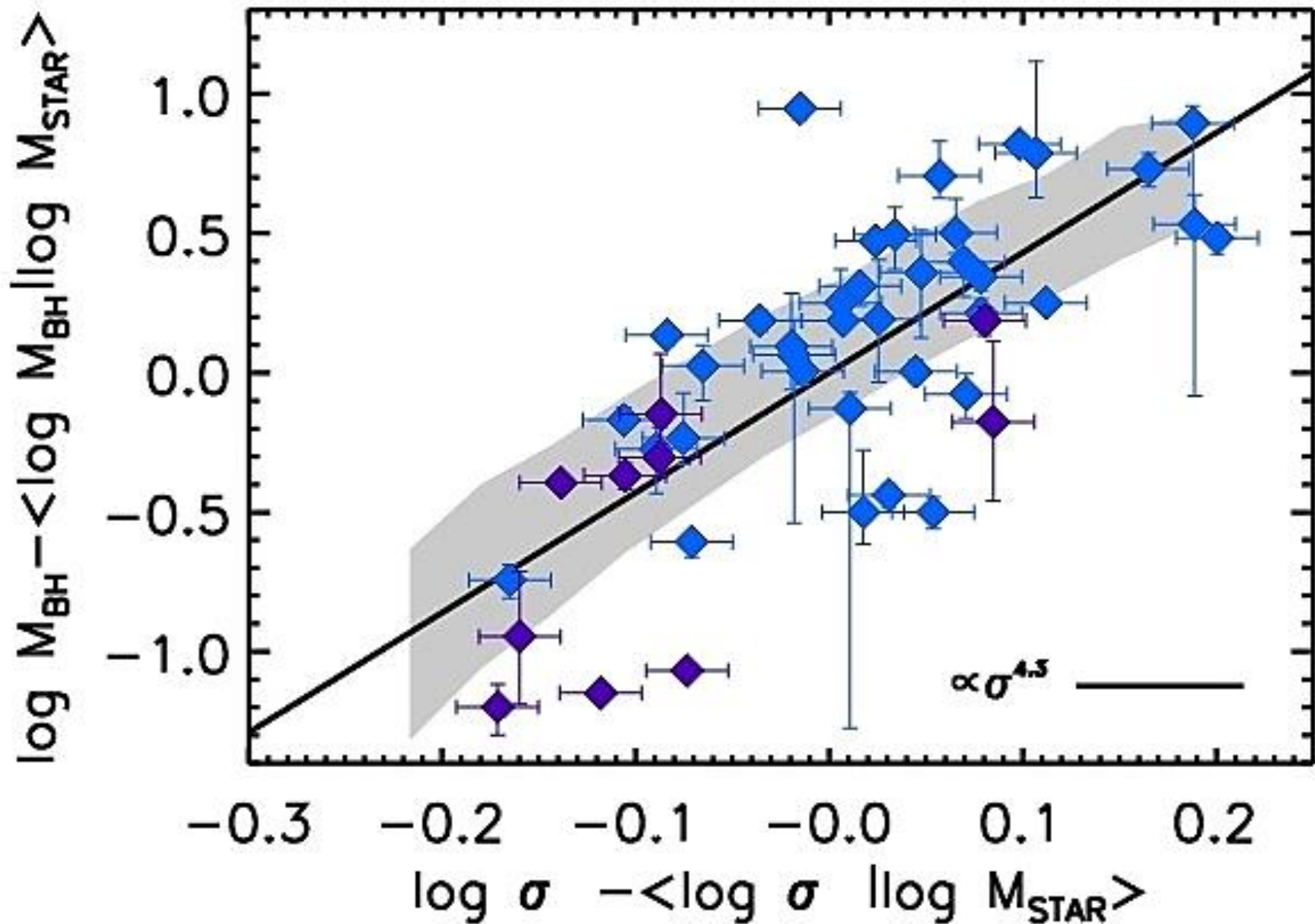
In a galaxy, each star produces a small Doppler shift with respect to the rest frame of the galaxy. The **superposition of many absorption lines** produces a broadening of the observed line. In mathematical terms, it is the convolution of the original stellar spectral line with the velocity distribution of the stars in the galaxy along the line-of-sight.

How many SMBH? How Massive?



Several caveats: scatter, colour change, bulge fractions, etc...





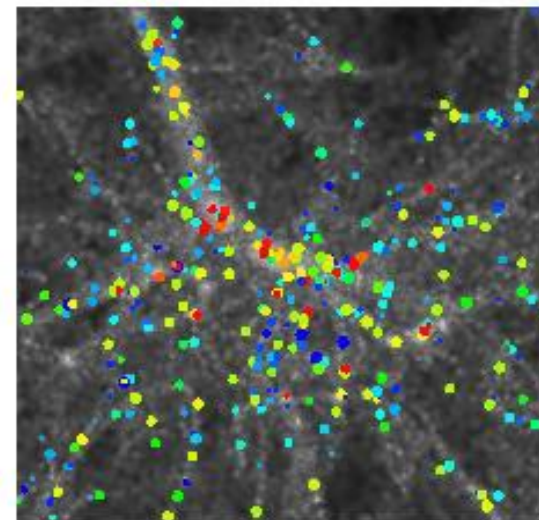
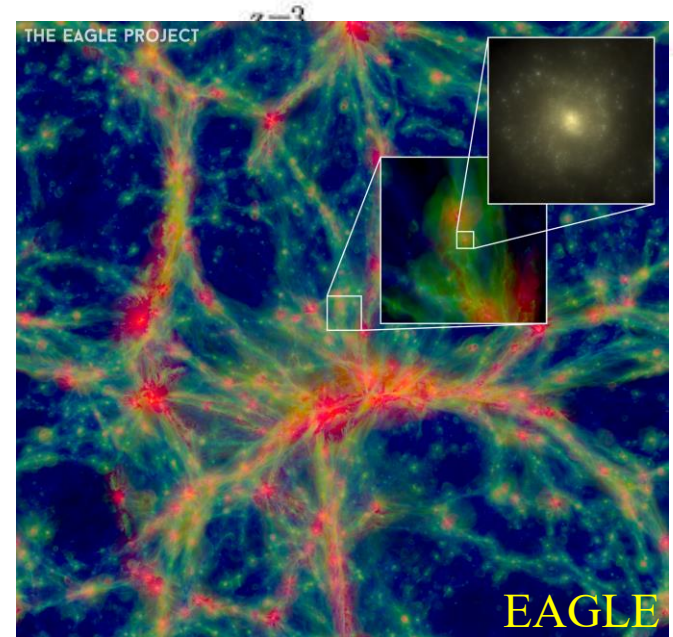
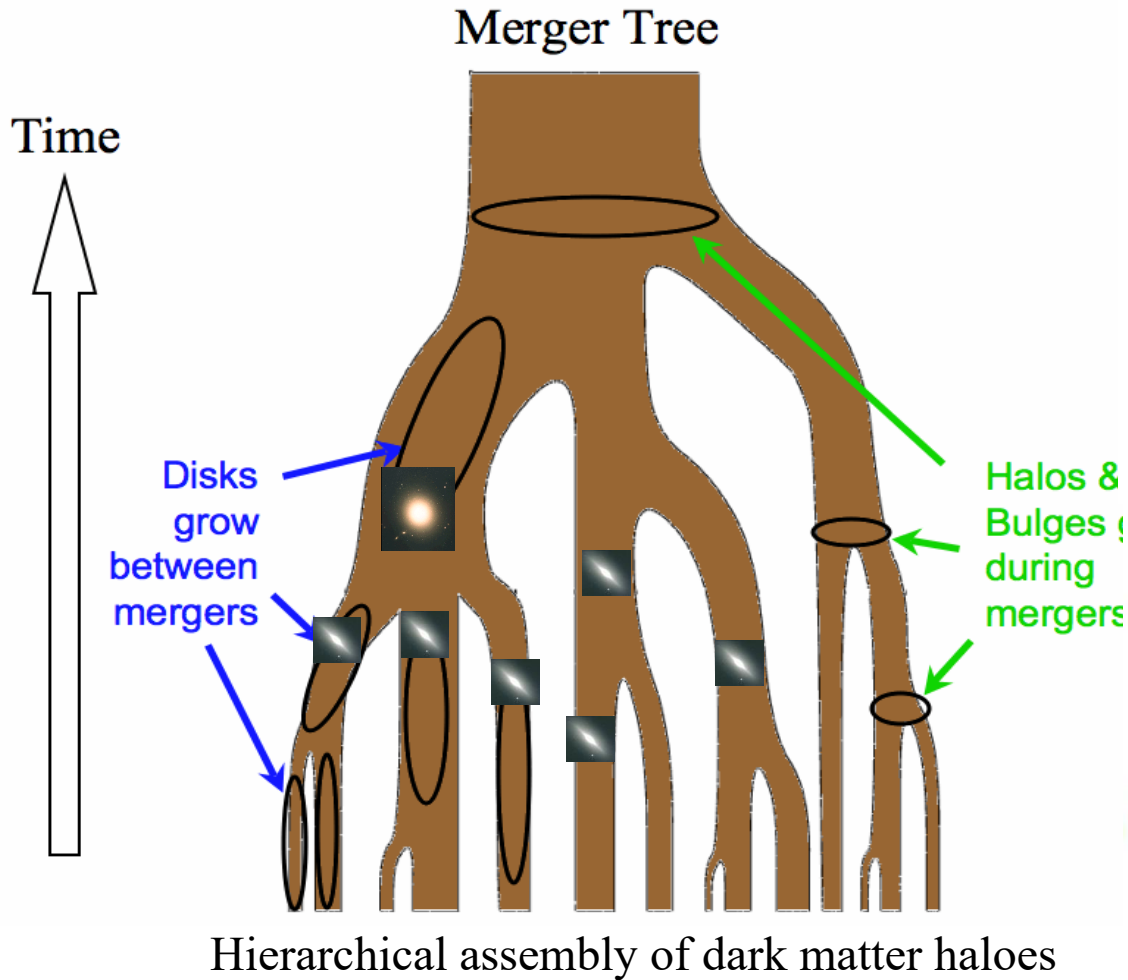
Take-home message I:

SMBHs are as common as galaxies but their average masses are uncertain

Evolution of SMBHs:

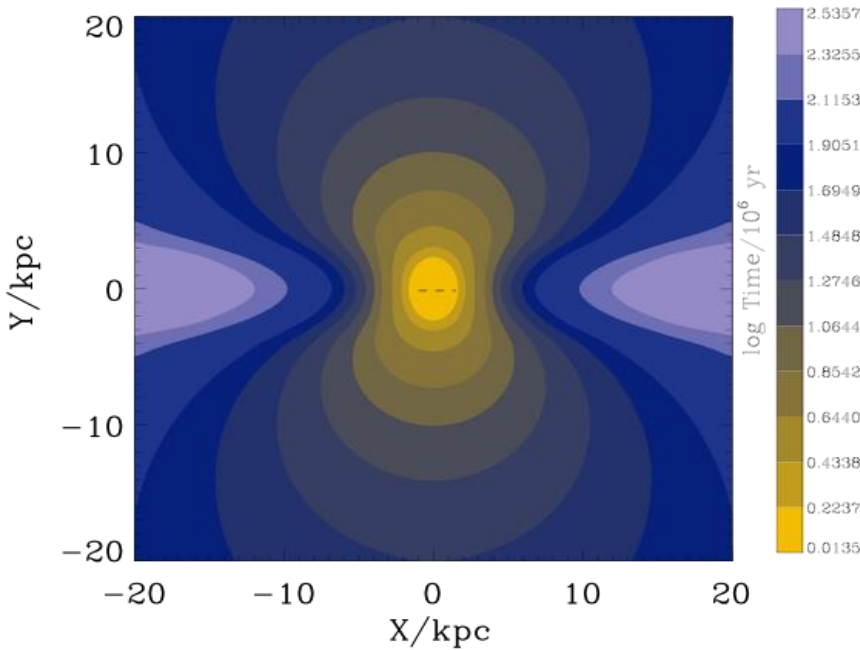
SMBH growth and feedback

GALAXIES and SMBHs LIVE AND GROW WITHIN DARK MATTER HALOES IN Λ CDM



MPA-SAM (Kauffmann+)

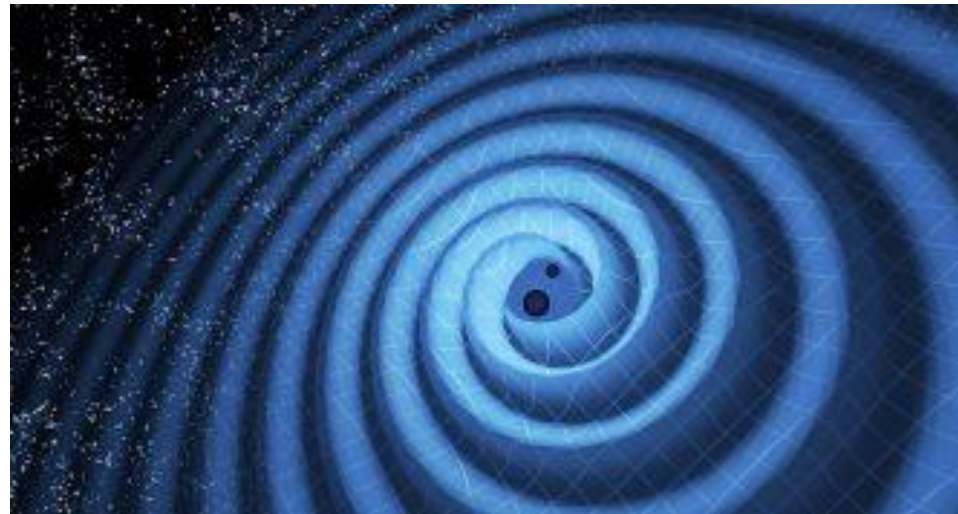
Why do we care about supermassive black holes?



N. Menci, ...FS, et al. 2019

SMBHs might have shaped galaxies via their energetic/kinetic outputs halting and/or promoting star formation and supporting morphological transformations

SMBH binaries are considered among the loudest sources of gravitational waves



T.
PYLE/LIGO

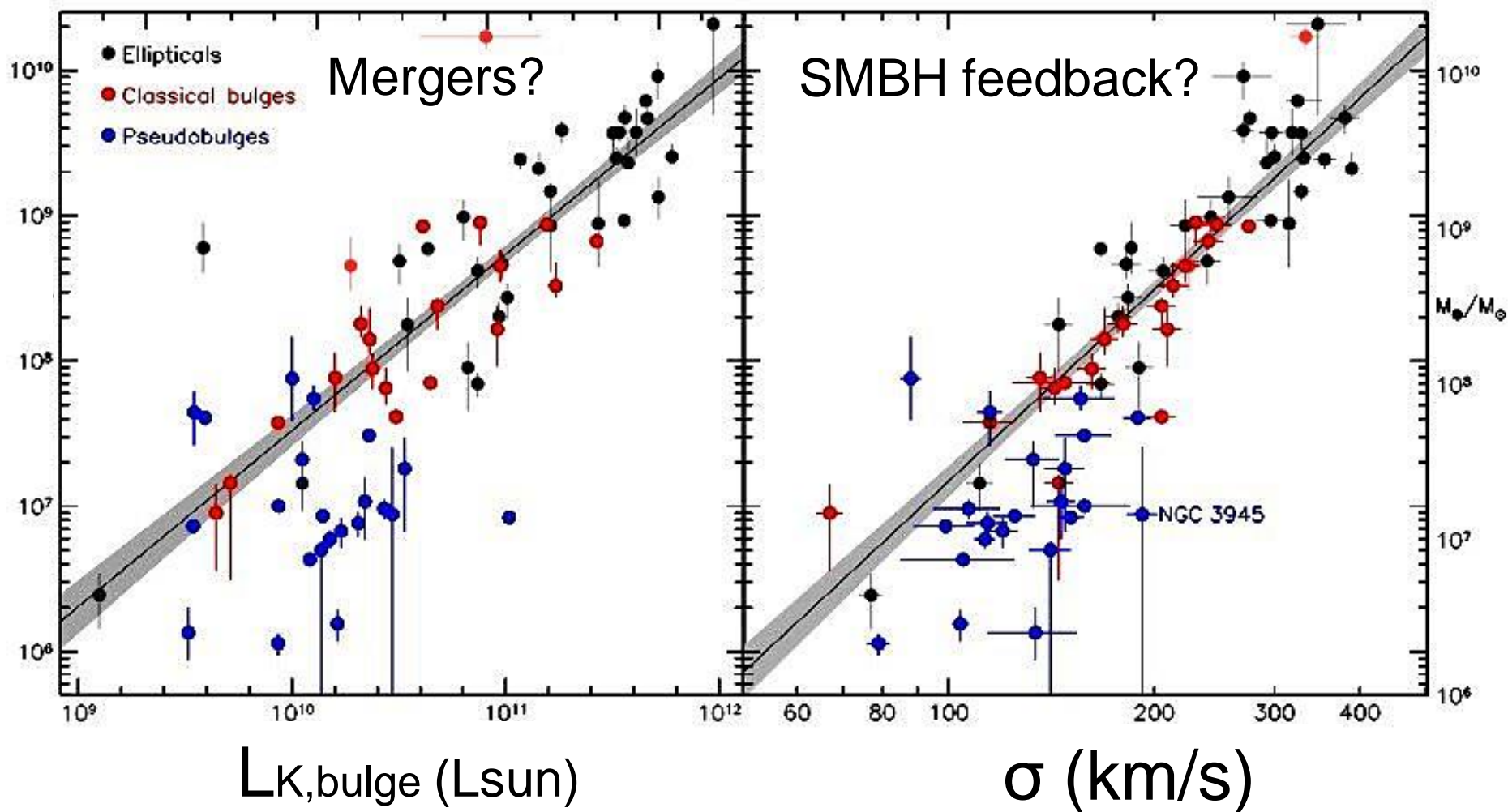
Which is the most fundamental?

$M_{\text{BH}} \sim M_{\text{star}}$

$M_{\text{BH}} \sim \sigma^{4-5}$

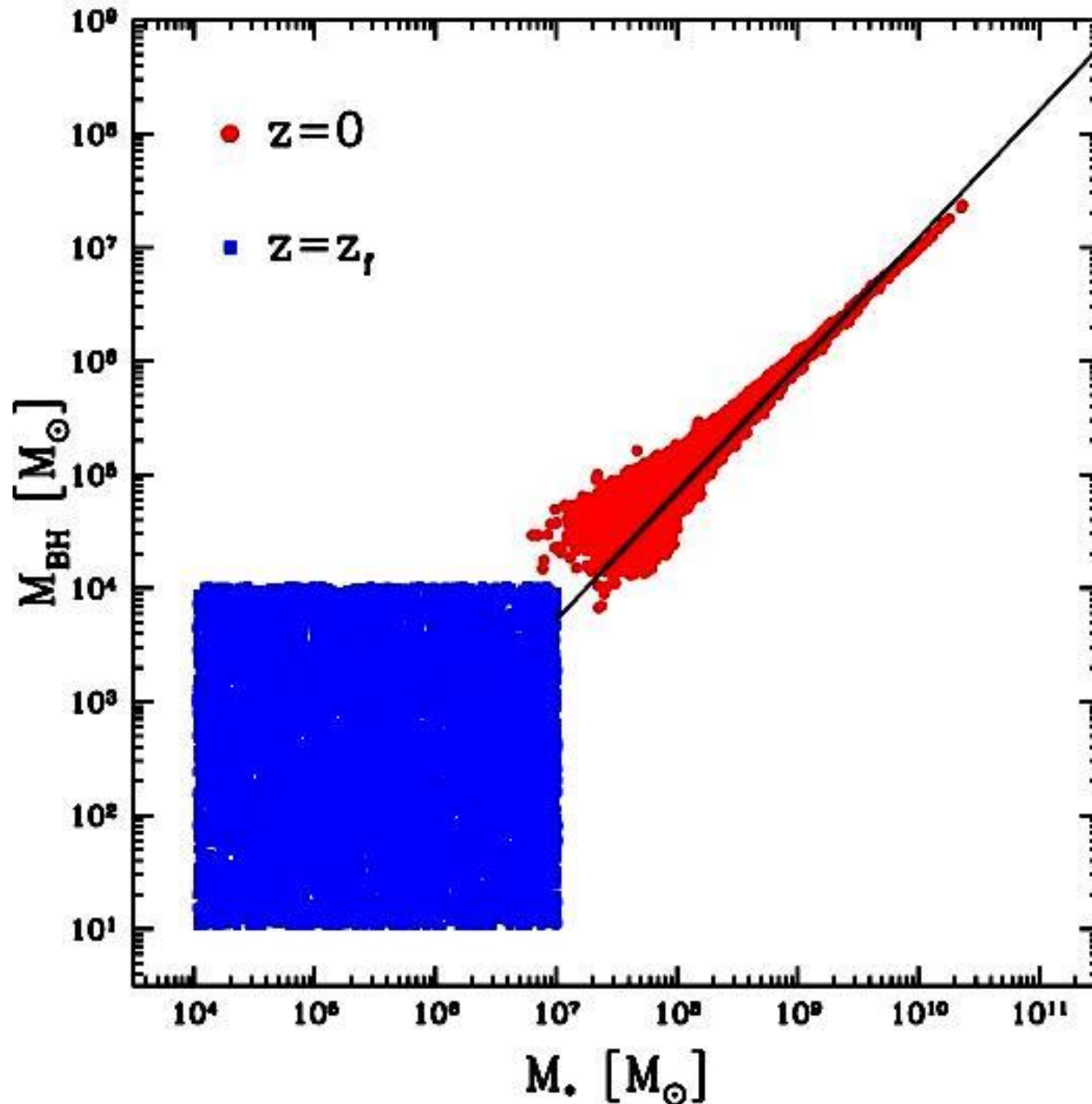
Mergers?

SMBH feedback?



Kormendy & Ho 13

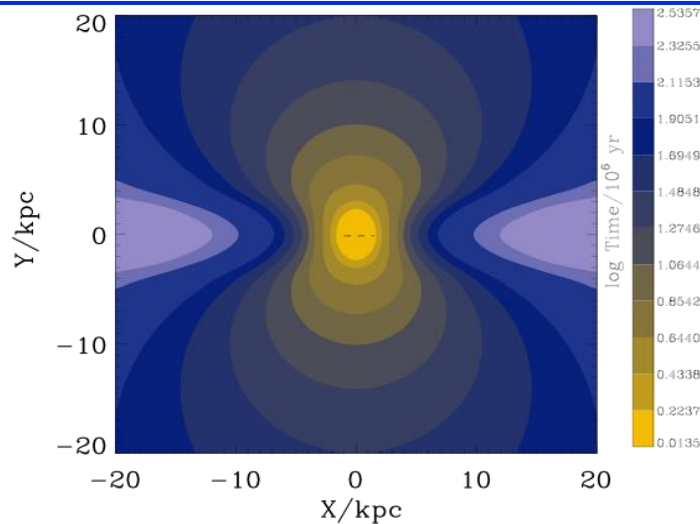
SMBH MERGERS?



Even with NO gas accretion, **ONLY mergers** at the rate predicted by Λ CDM can already predict a linear relation!

Jahnke+Maccio 11

SMBH feedback?



N. Menci,..FS, et al.
2019

$$\dot{M}_{BH} c^2 \tau_{dyn} \sim M_{star} \sigma^2$$

$$\tau_{dyn} \sim R / \sigma$$

$$M_{BH} \sim \dot{M}_{BH} \sim M_{star} \sigma^3 / R$$

$$GM_{star} / R \sim \sigma^2$$

$$M_{BH} \sim \sigma^5$$

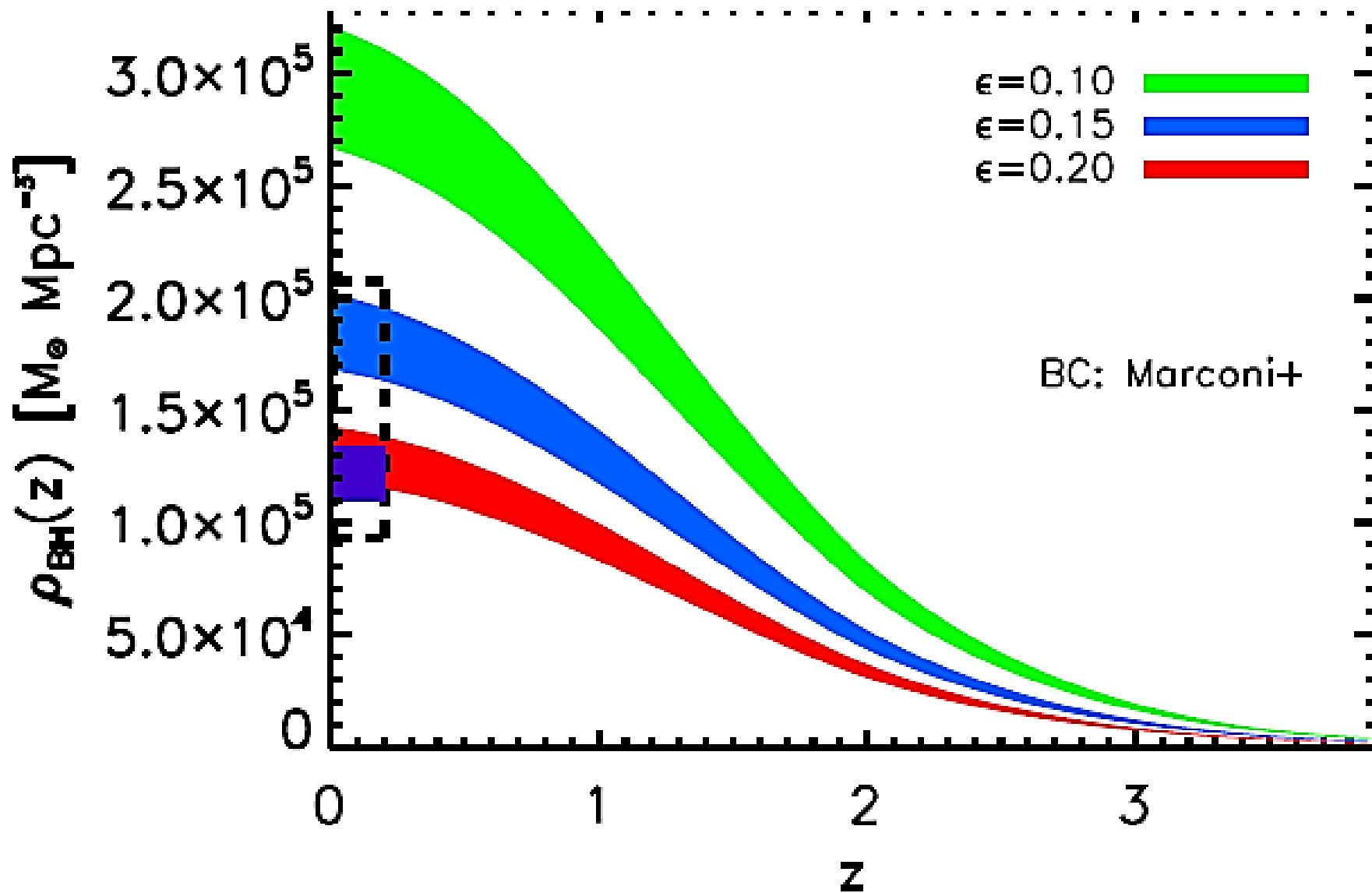
Silk&Rees98

The “Soltan-Paczynski (1982) argument”

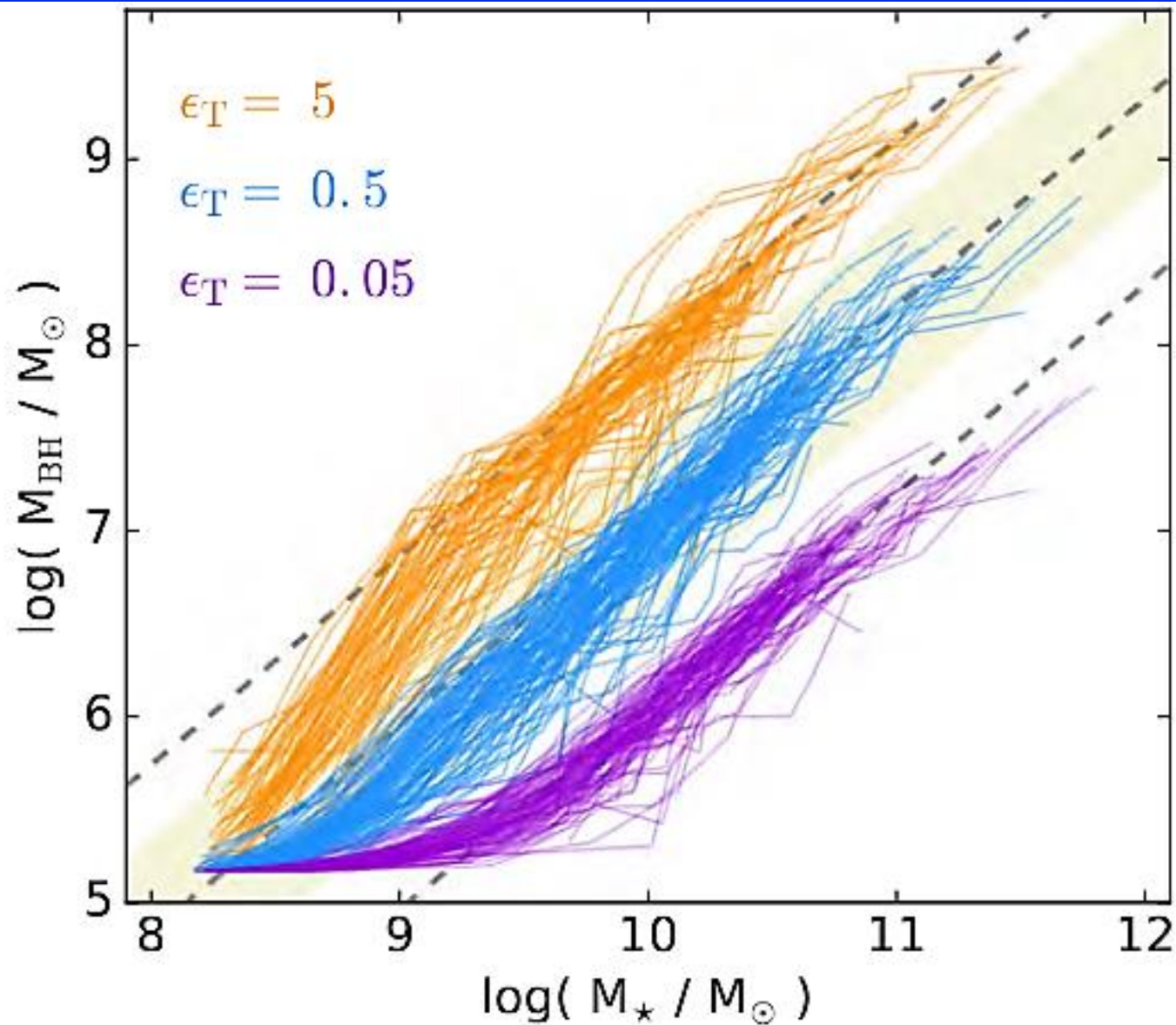
$$L = \varepsilon \frac{d(mc^2)}{dt}$$

$$\frac{1 - \varepsilon}{\varepsilon c^2} \int L \Phi(L, t) dt = \rho_{BH, relic}$$

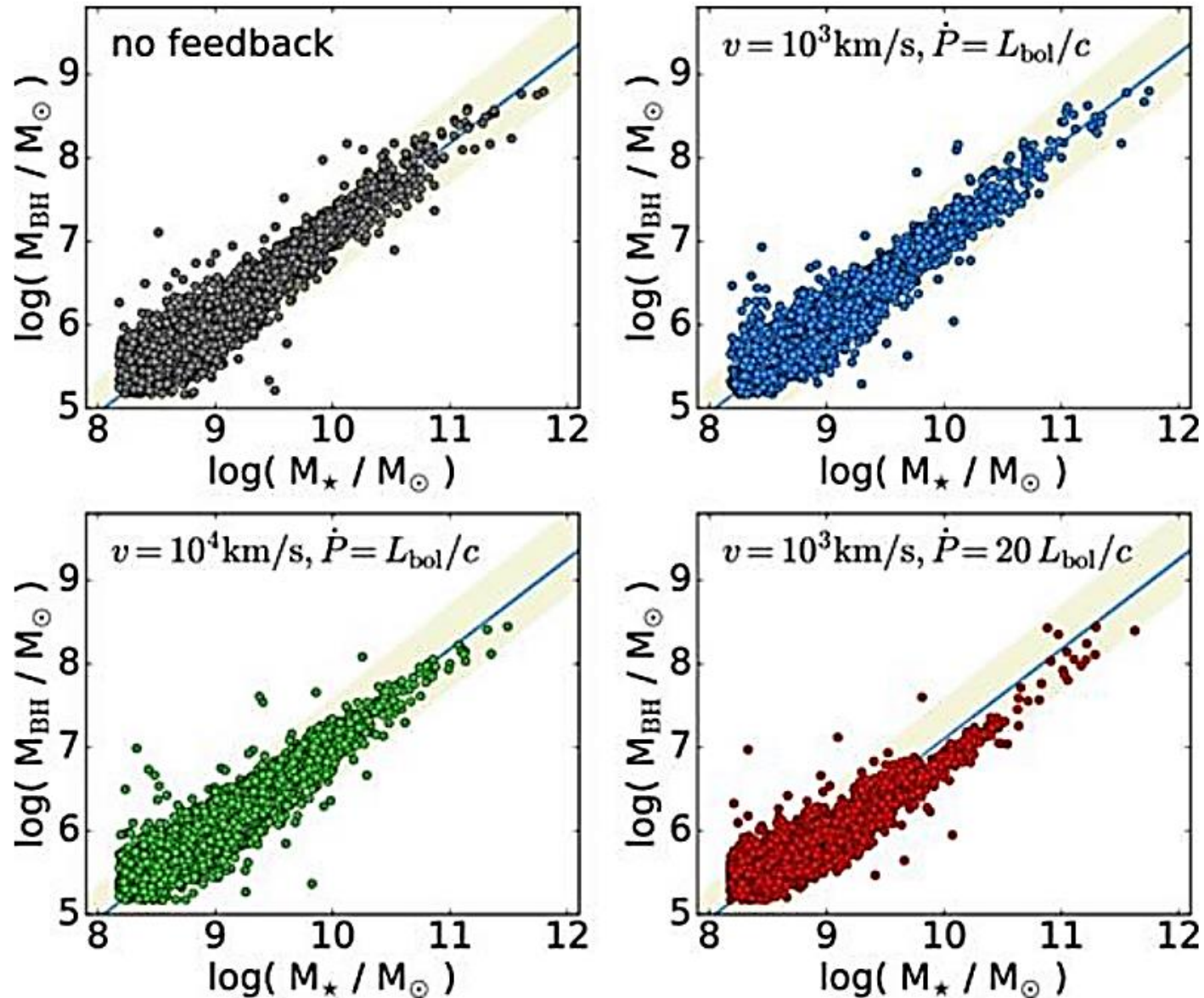
$$\rho_{BH, relic} \Leftrightarrow \rho_{BH, local} \Rightarrow \varepsilon$$



Accretion is connecting SMBHs and galaxies



Weak effect of AGN feedback on scaling relations

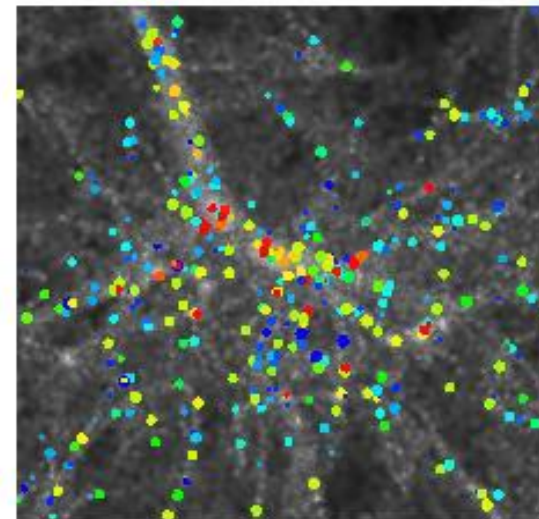
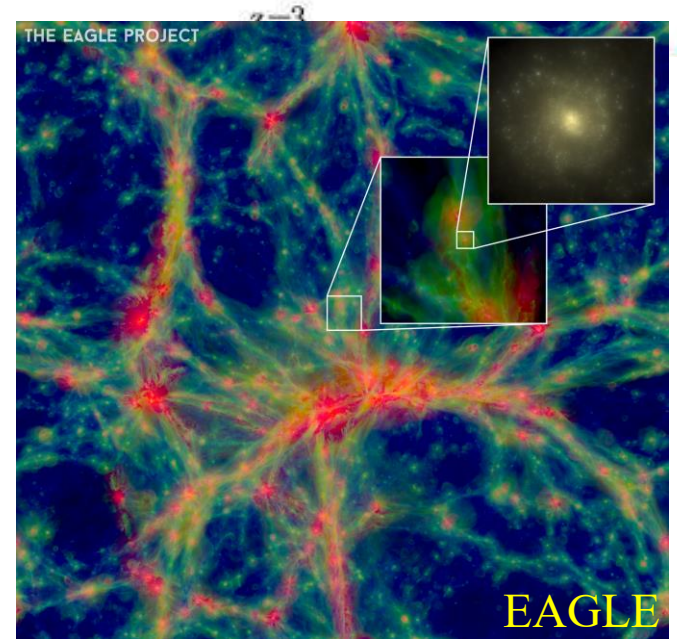
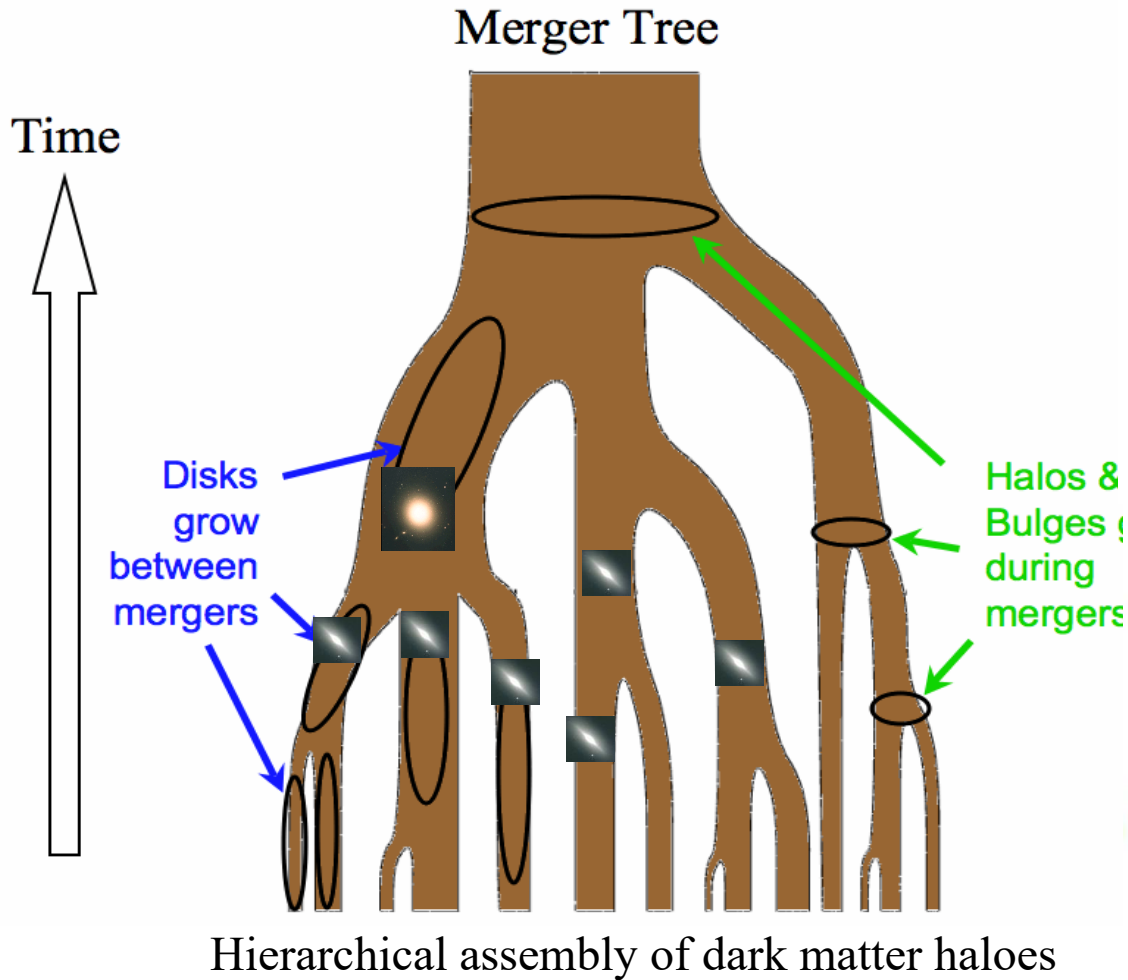


Take-home message II:
**SMBHs grow primarily via
gas accretion!**

Physical implications:

Mergers and GWs

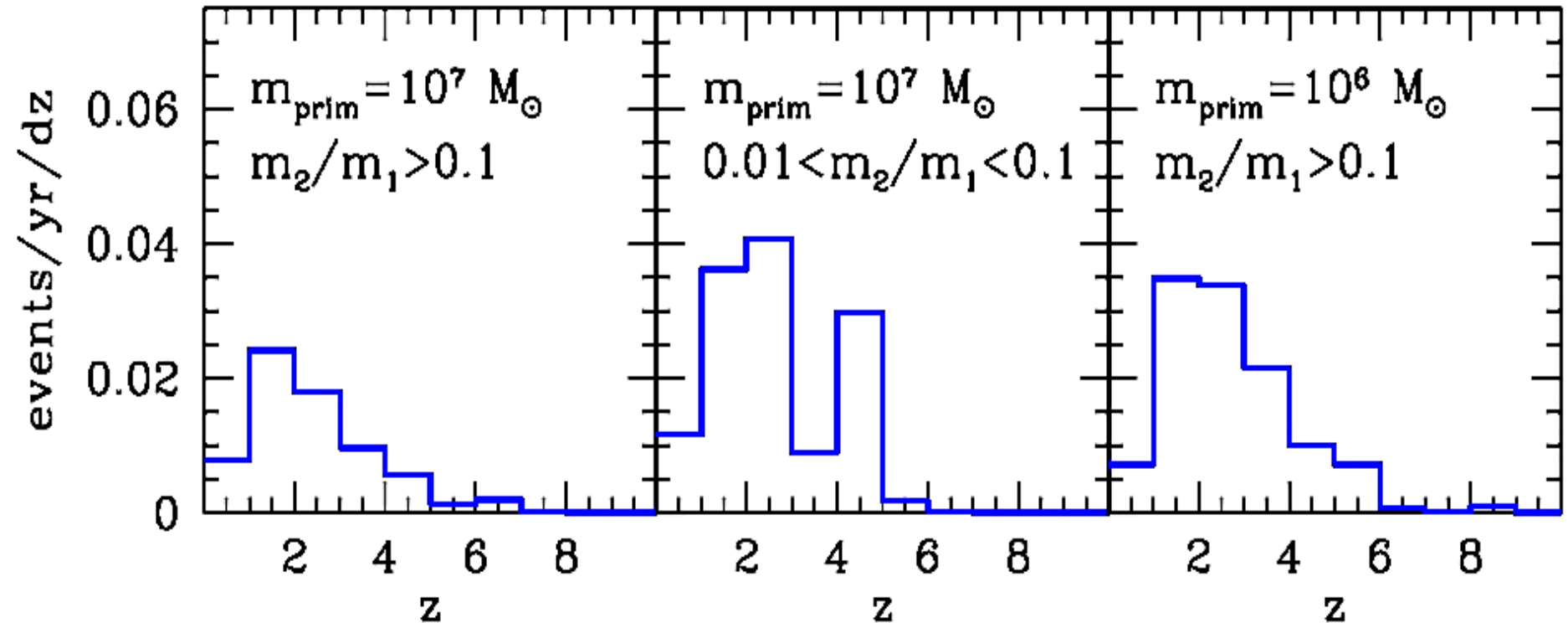
GALAXIES and SMBHs LIVE AND GROW WITHIN DARK MATTER HALOES IN Λ CDM



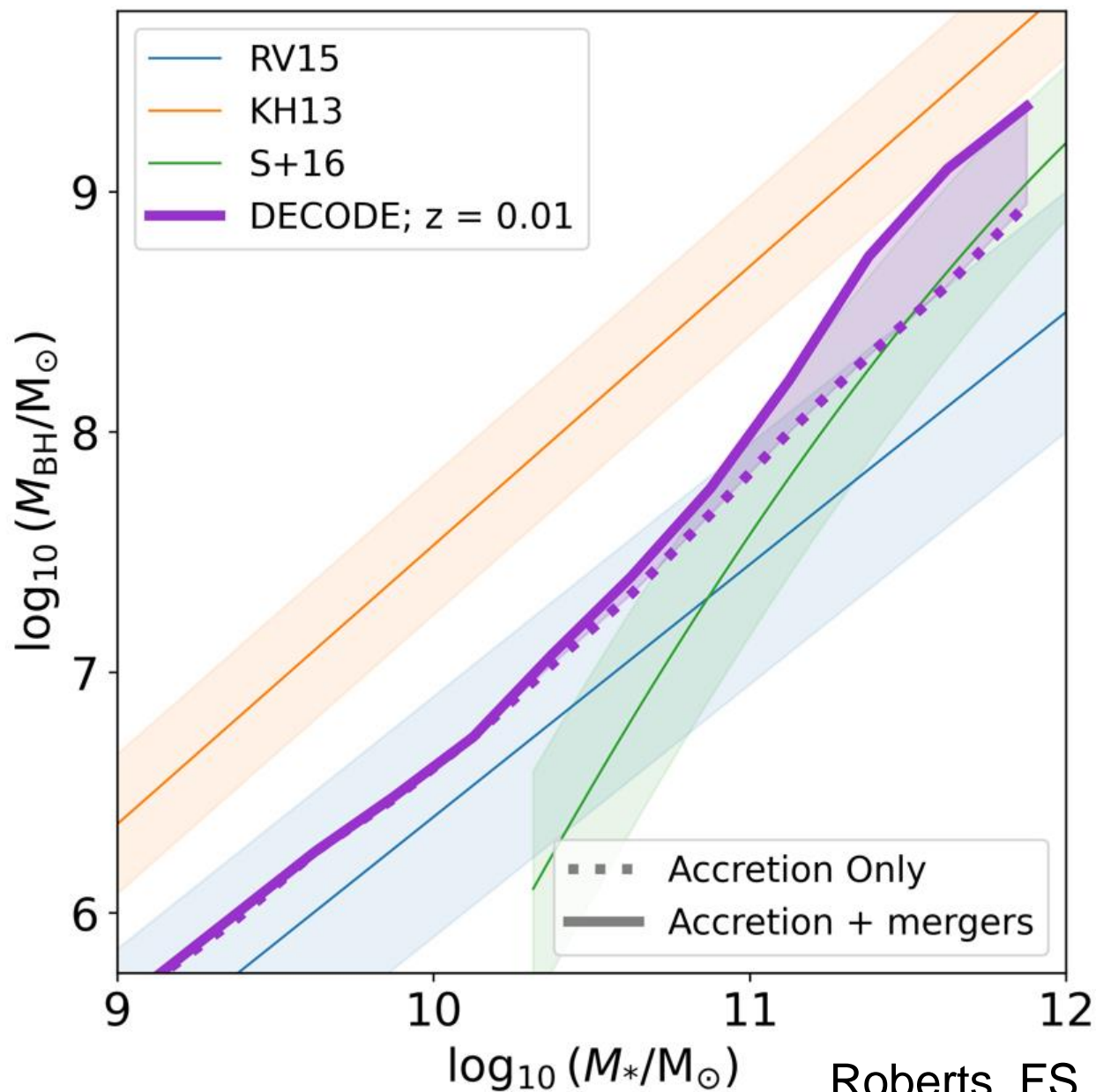
MPA-SAM (Kauffmann+)

Example of galaxy (bulge) merger rates that may favour supermassive black hole binaries and mergers

Haehnelt+03

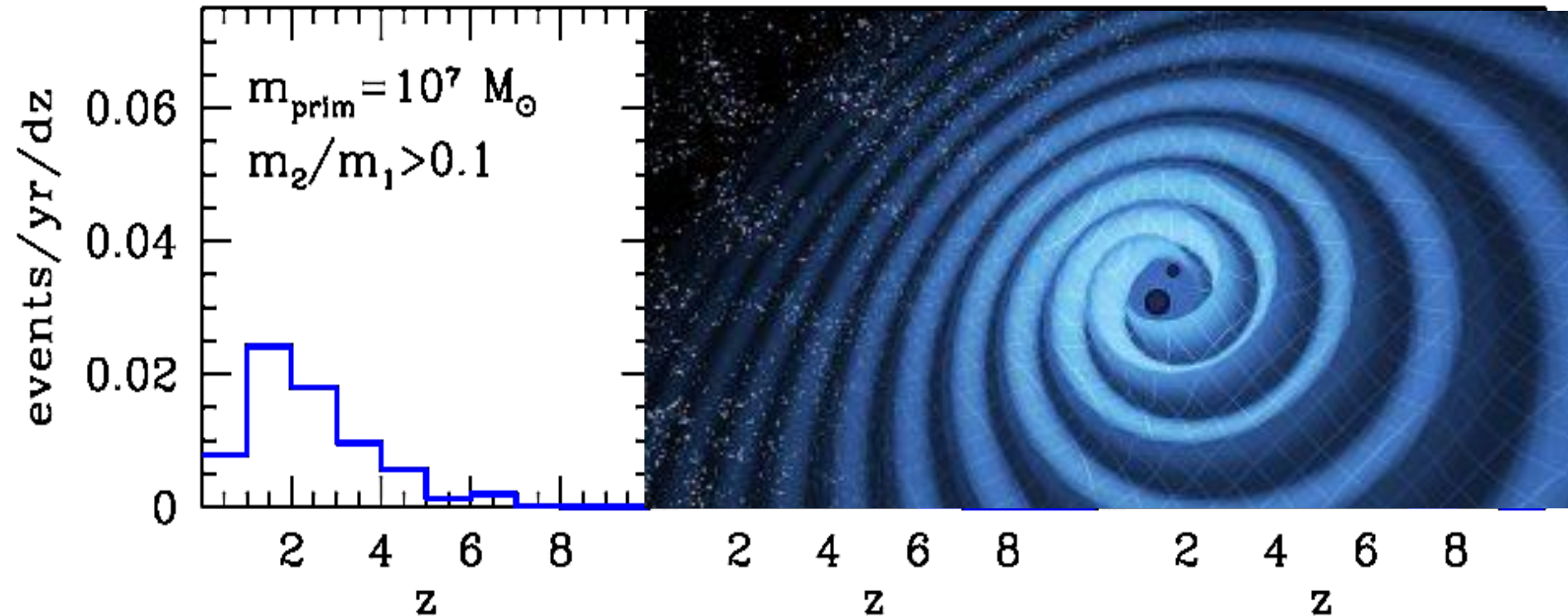


Effect of mergers is modest



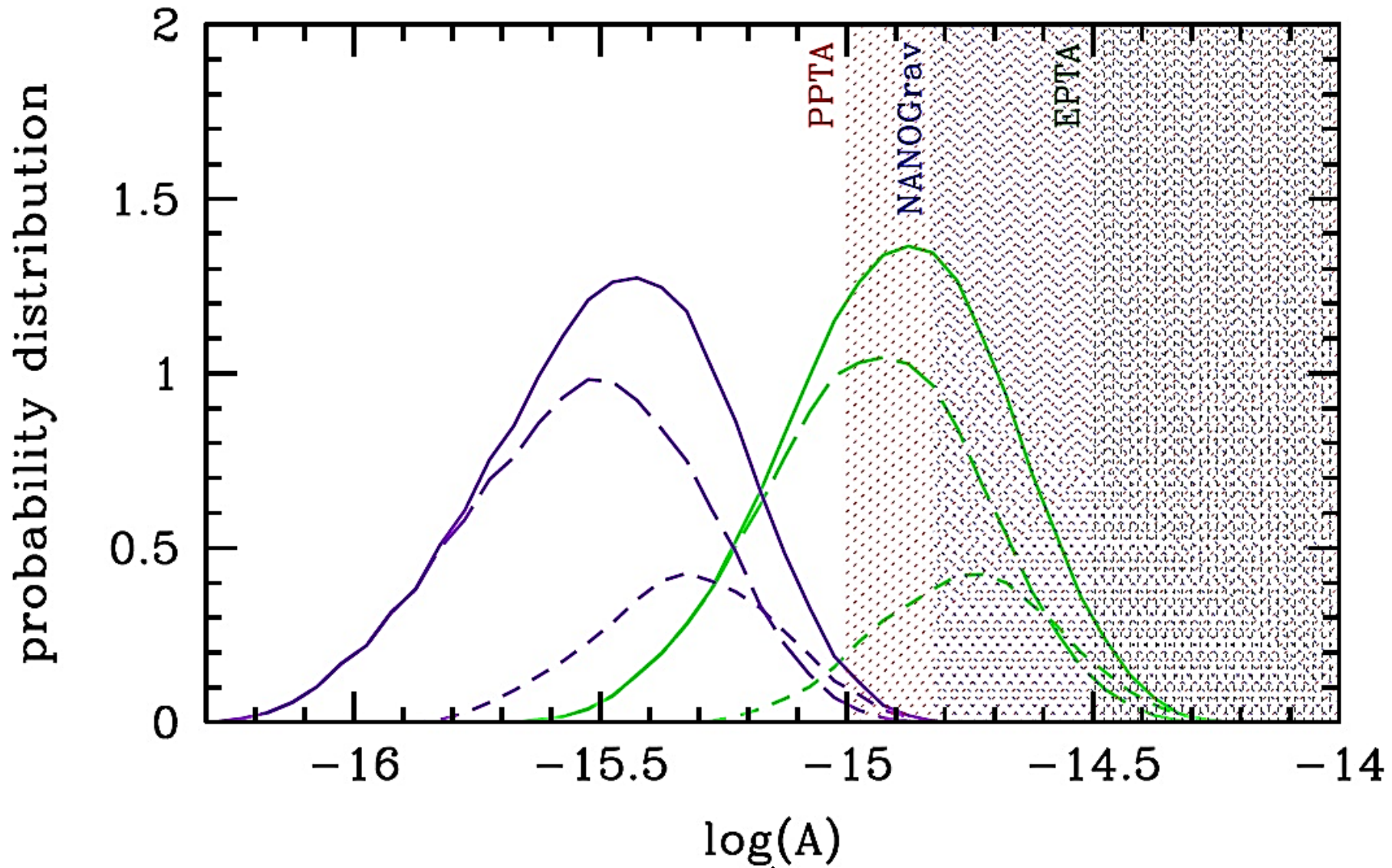
Example of galaxy (bulge) merger rates that may favour supermassive black hole binaries and mergers

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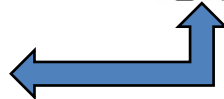


$$h_c^2(f) = \frac{4 G^{5/3}}{3 \pi^{1/3} c^2 f^{4/3}} \int \frac{dt}{(1+z)^{1/3}} \int dM_{\bullet} M_{\bullet}^{5/3} \int dq \frac{q}{(1+q)^2} \frac{d^2 \mathcal{R}_{\bullet \rightarrow \bullet}}{dM_{\bullet} dq}$$

How much Gravitational Waves?

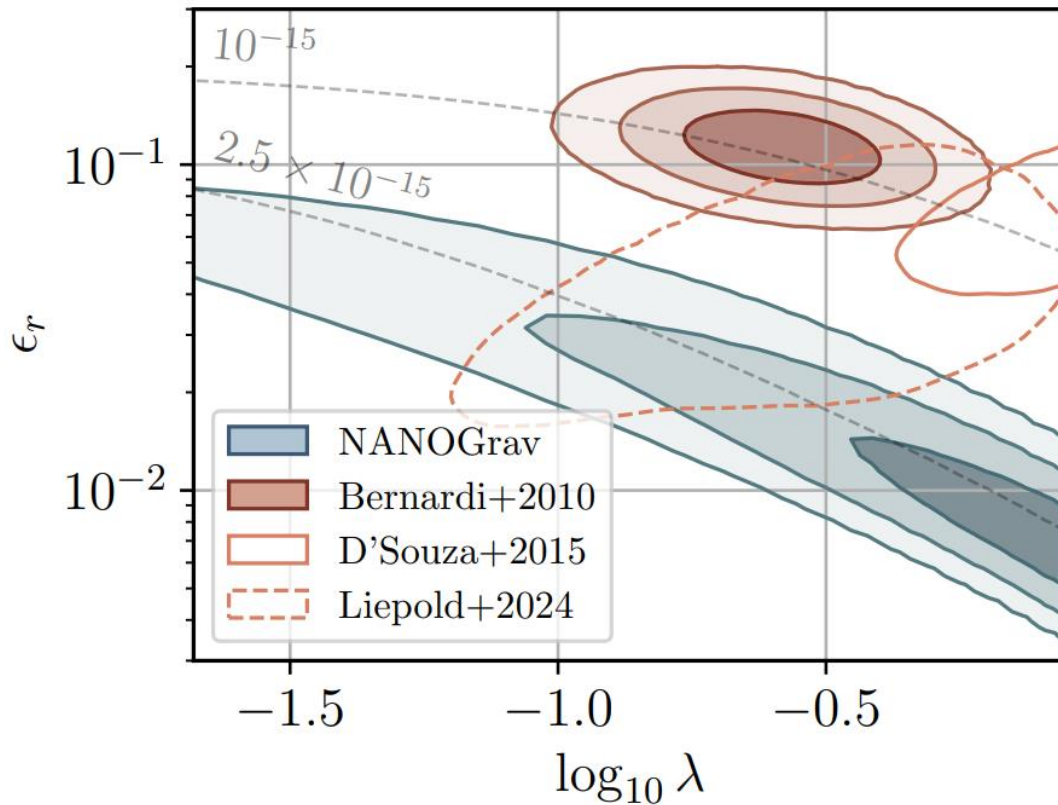


characteristic Amplitude GWs at $f=1/\text{yr}$



Sesana, FS, et al. 2016

How much Gravitational Waves?



Red shaded region
uses $M_{\text{BH}}-\sigma$ relation

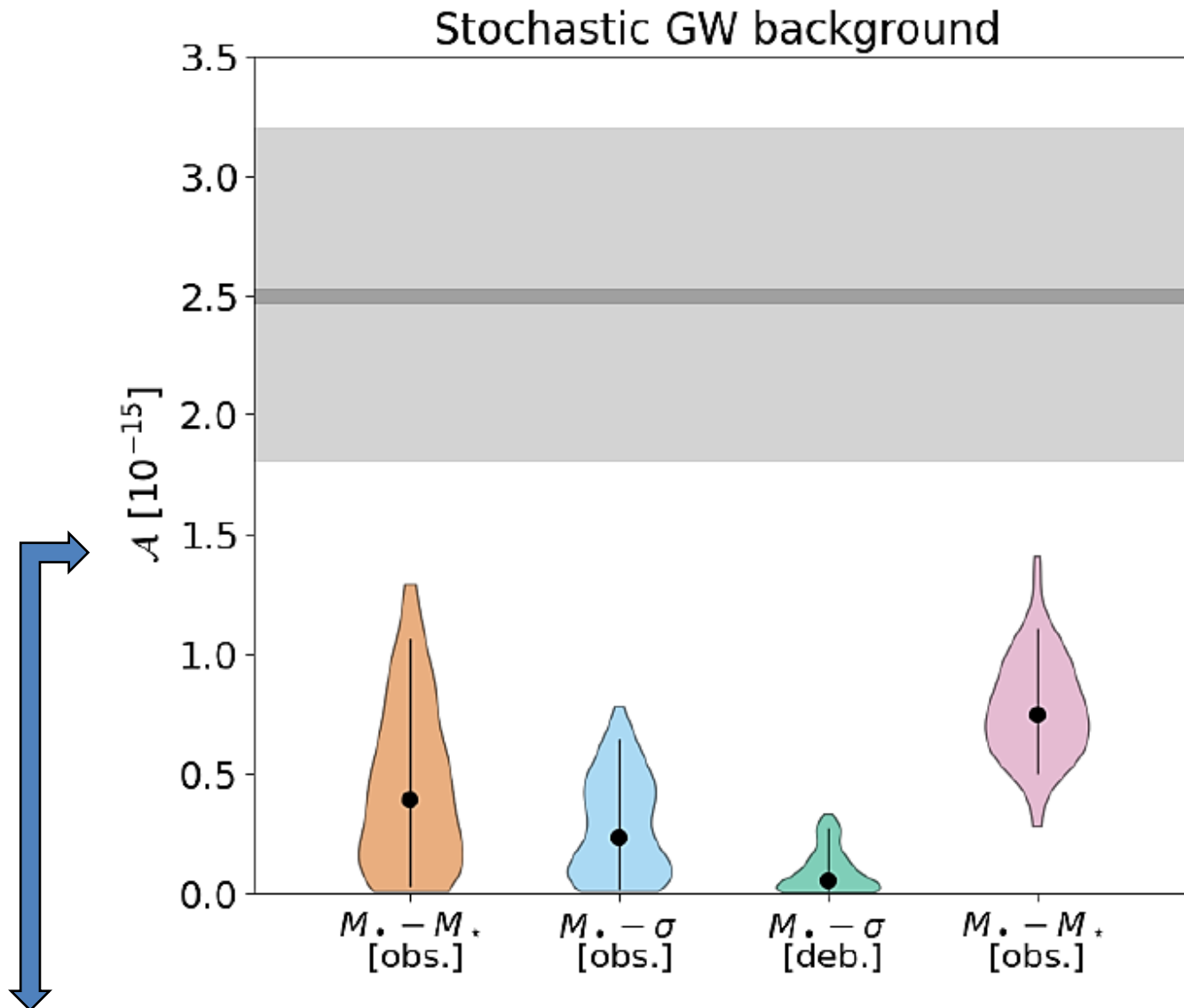
Dashed-line region
uses $M_{\text{BH}}-M^*$
relation

Blue shaded region
is from NANOGrav

Merger rates using a full semi-empirical model

G. Sato-Polito, M. Zaldarriaga, and E. Quataert, 2025

How much Gravitational Waves?

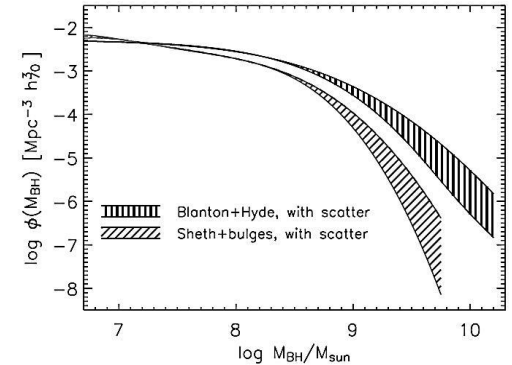


Take-home message III:

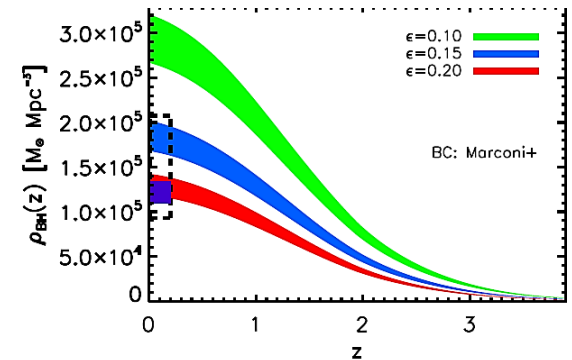
**The predicted GW
cumulative contribution
of SMBH mergers to PTA
may be subdominant**

WHAT I DISCUSSED:

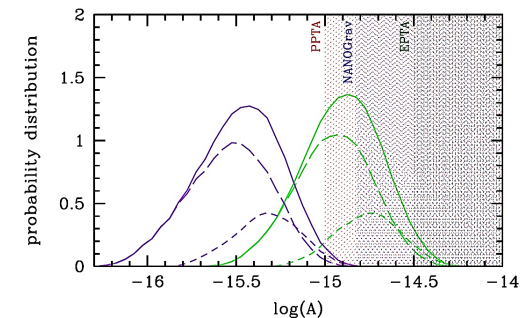
SMBH demography:
Unclear average masses



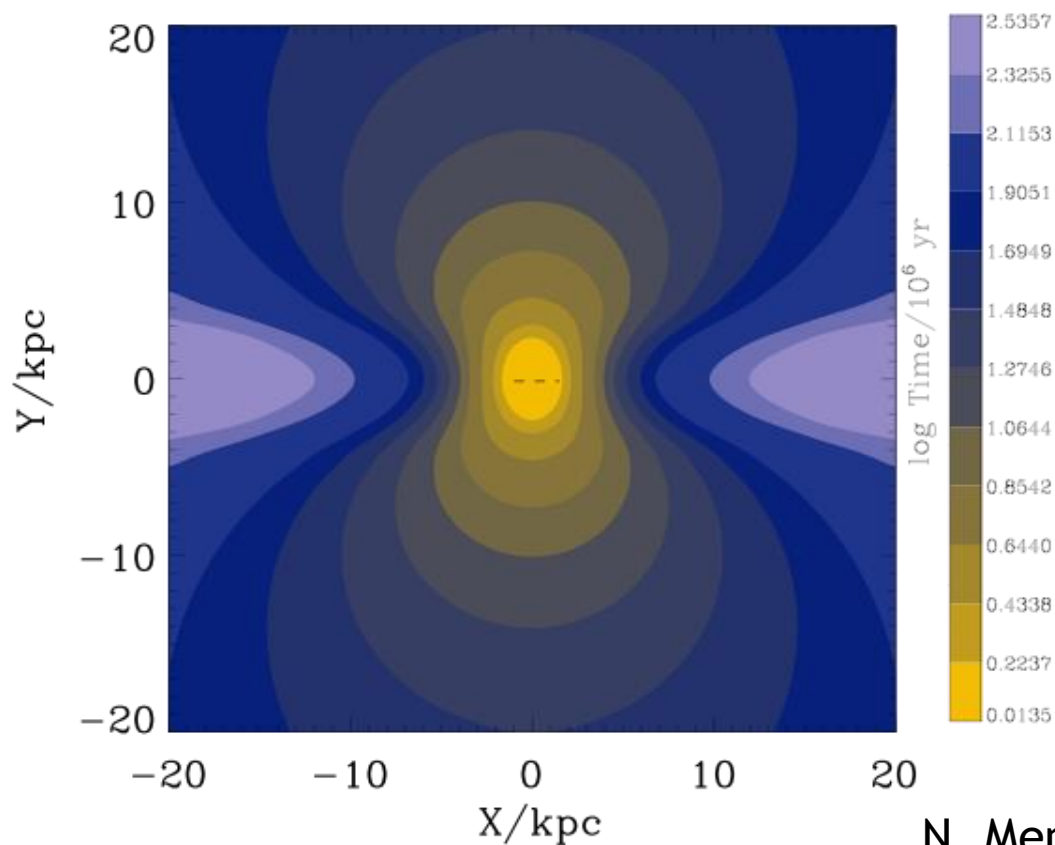
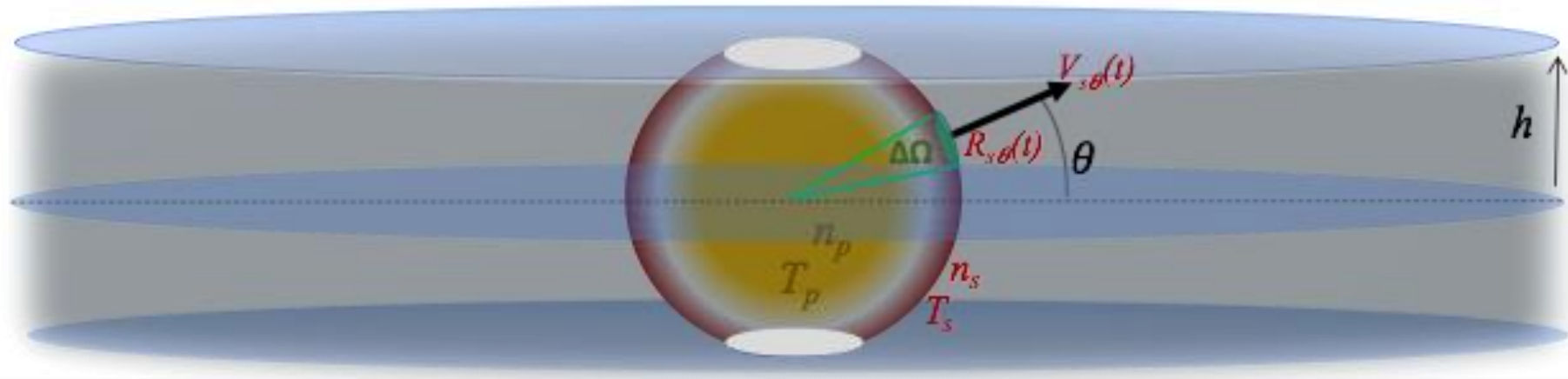
Evolution of SMBHs:
Accretion dominant



Physical implications:
Tension with PTA



Example of kinetic AGN feedback: Expansion of outflows at different azimuthal angles



HOW EFFICIENT IS ACCRETION?

IT DEPENDS ON HOW CLOSE WE GET...

$$L = \frac{dU}{dt} = \frac{GM}{r} \frac{dm}{dt}$$

$$r = R_s = \frac{2GM}{c^2}$$

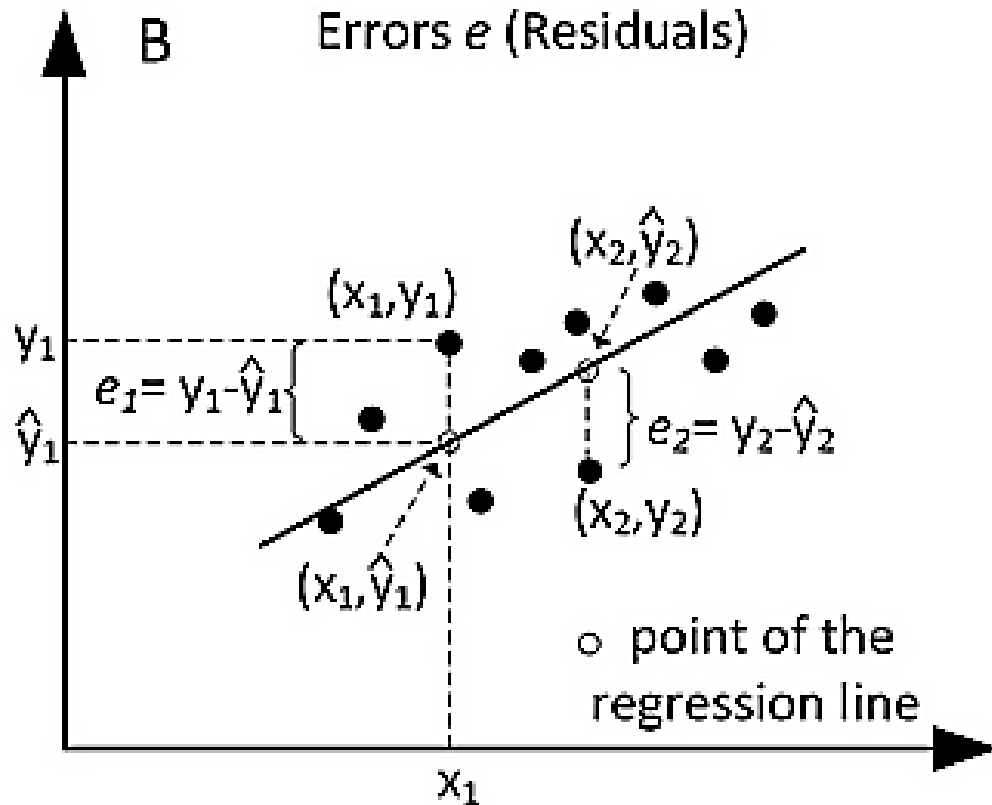
We can extract
light/energy only for $R > R_s$

$$\Rightarrow L = \frac{GM}{2GM} \times c^2 \times \frac{dm}{dt} = \frac{1}{2} \frac{d(mc^2)}{dt}$$

$$\varepsilon = 0.1 - 0.4 \gg \gg \gg \varepsilon_{STAR} \sim 0.008!!!!$$

**SMALL r BIG M -> VERY
HIGH EFFICIENCY!!!**

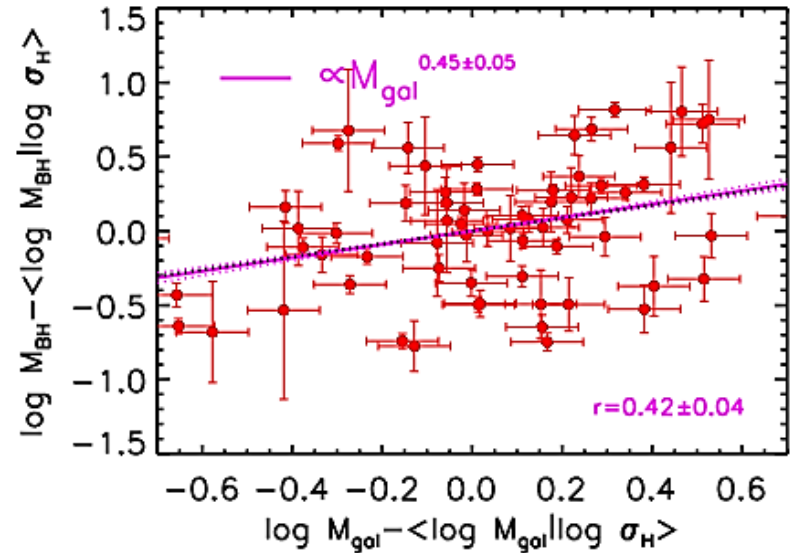
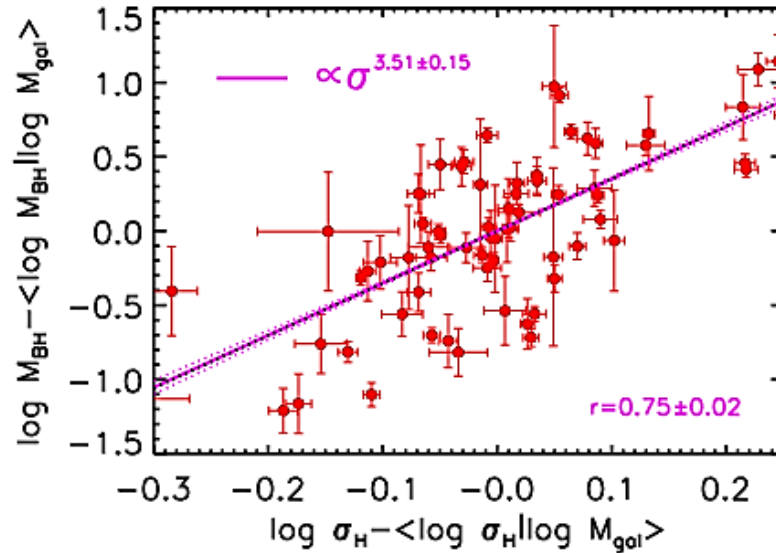
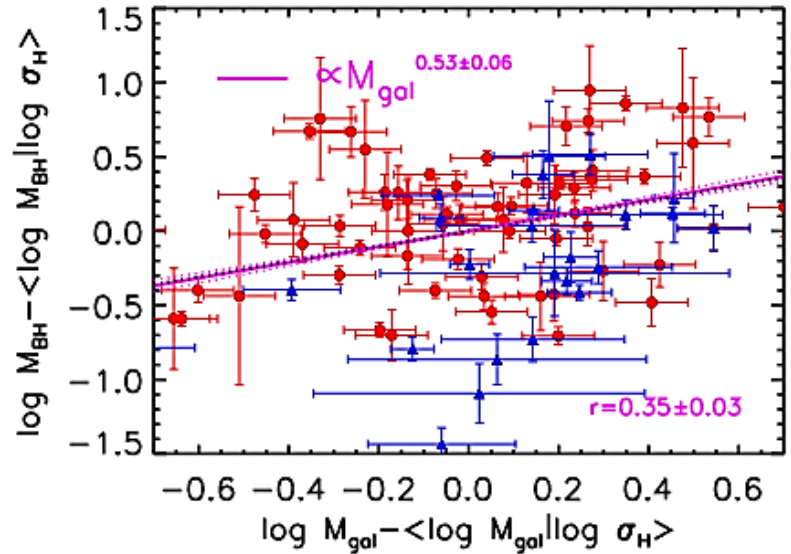
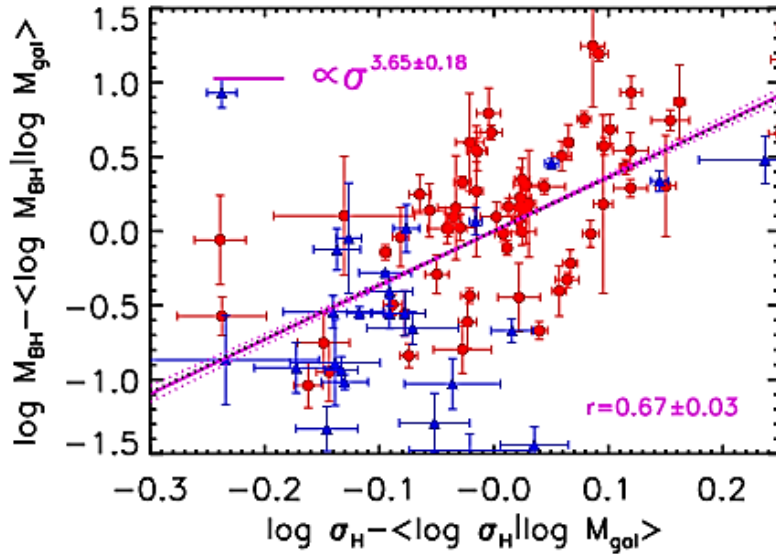
How do residuals work?



- 1) Calculate residuals of $y(x) - y_{\text{fit}}(x)$
- 2) Calculate residuals of $z(x) - z_{\text{fit}}(x)$
- 3) Calculate correlation coefficient between the two residuals, if strong then NO underlying correlation with x !

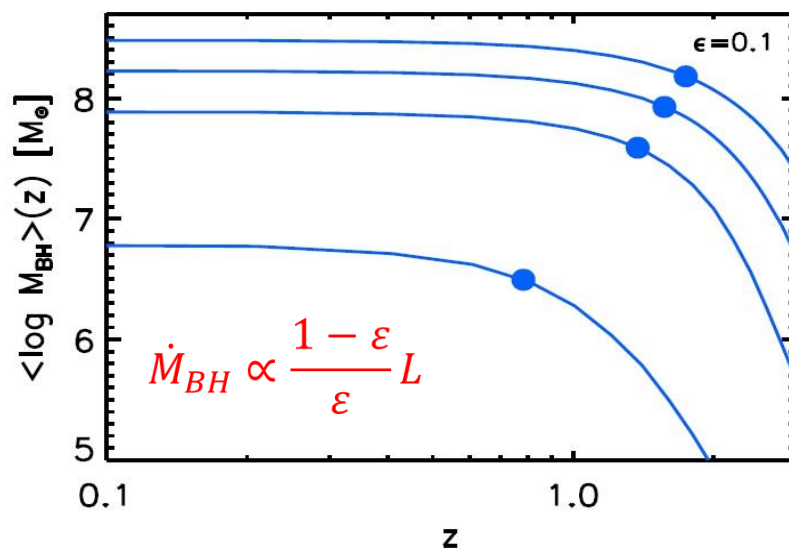
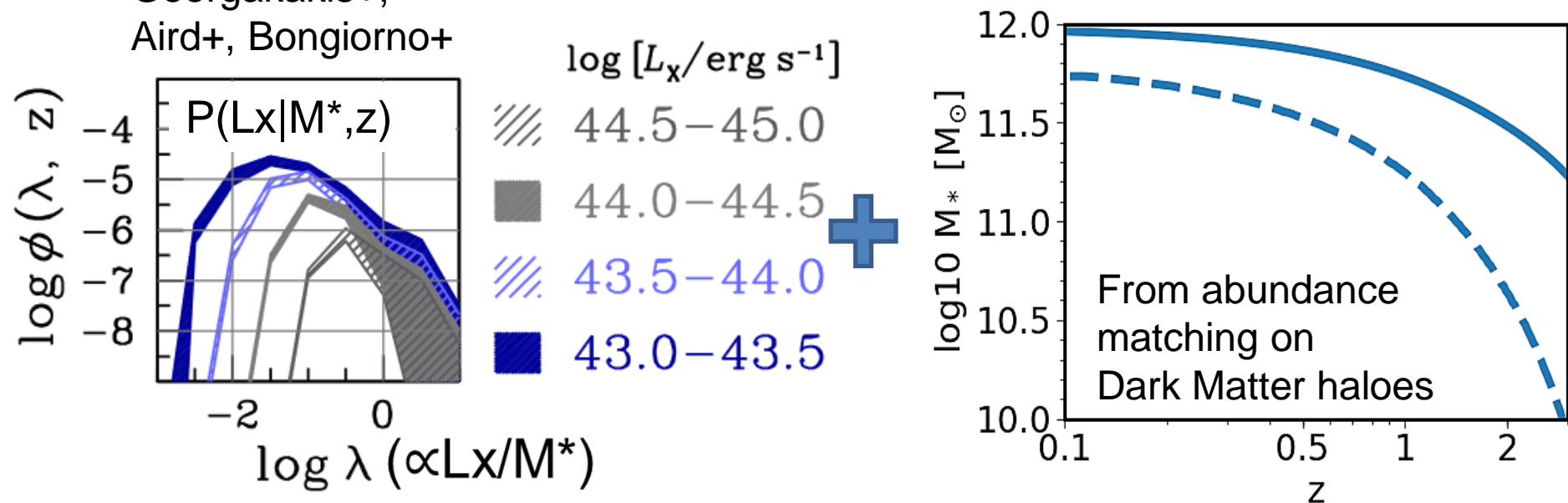
George Grekousis 2020

σ more fundamental than M_{gal}

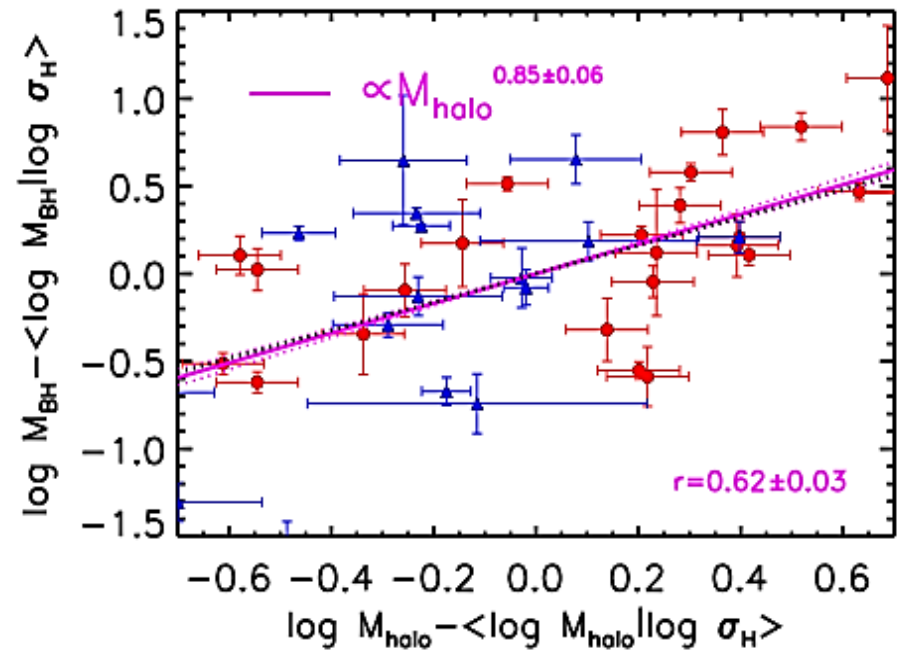
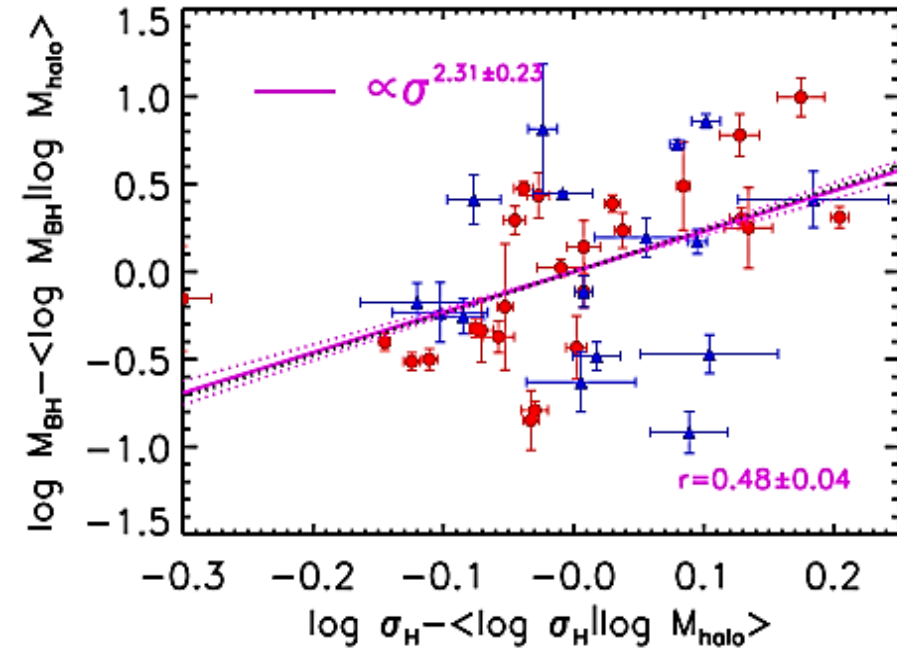


From $P(L_x|M^*,z)$ relation to SMBH scaling relations

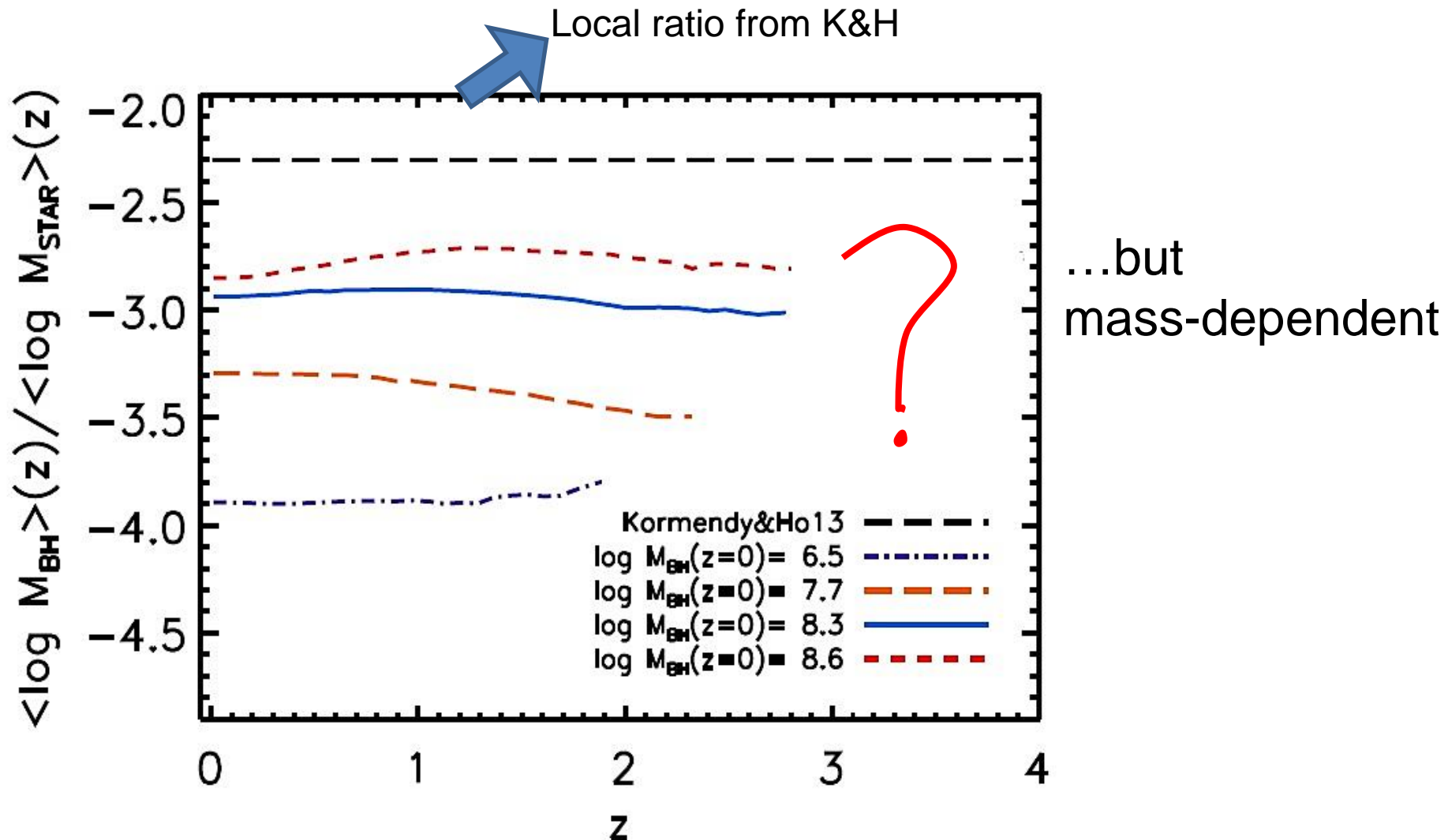
Georgakakis+,
Aird+, Bongiorno+



M_{halo} more fundamental than σ ?

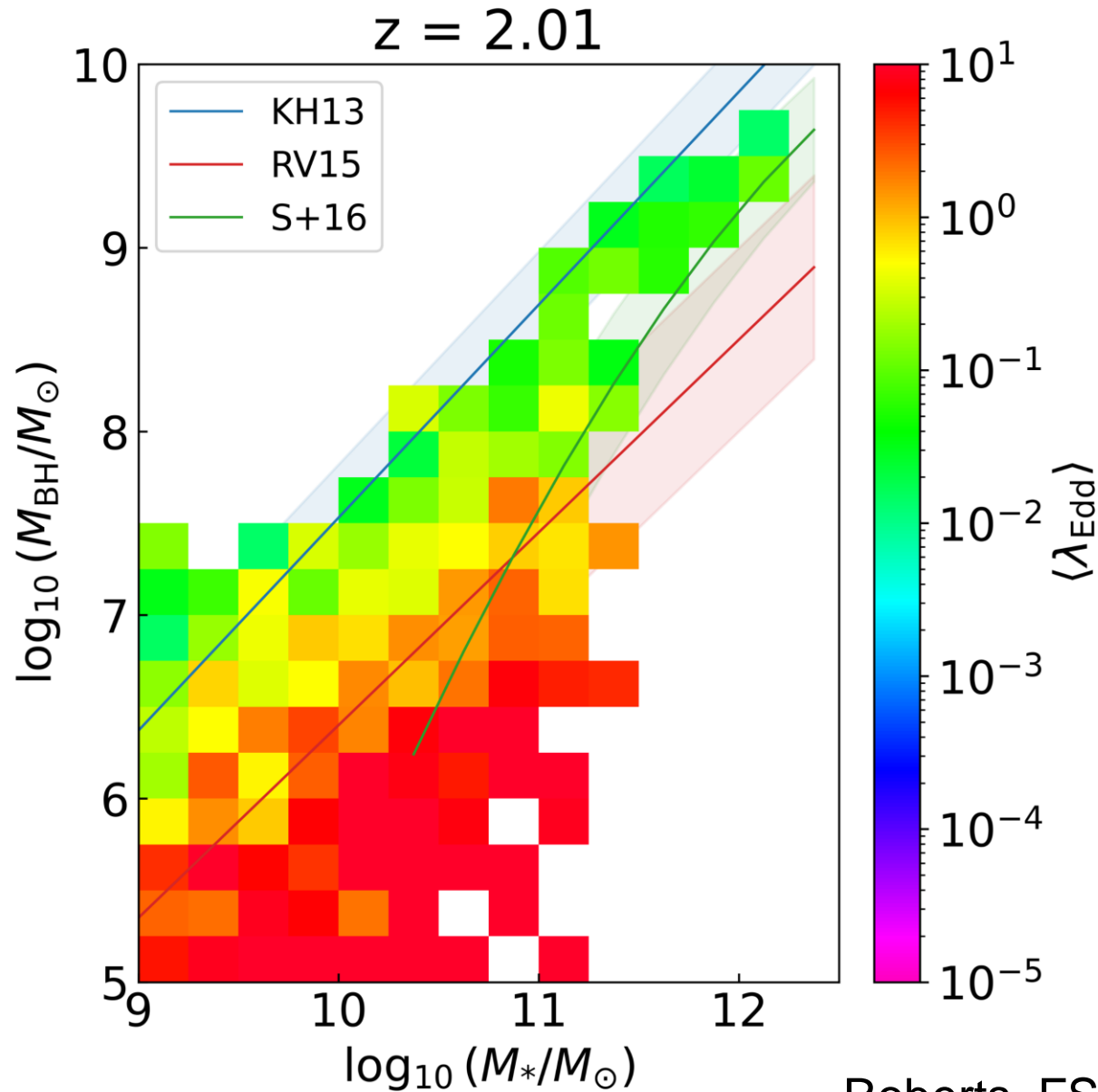


Almost constant evolution of M_{BH}-M_{gal} relation

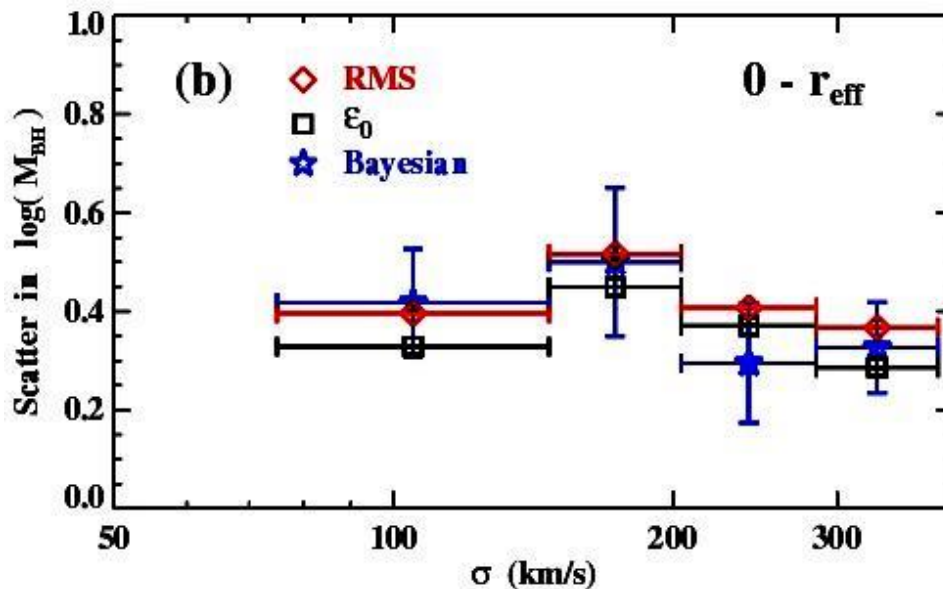


FS+20, as in direct observations from, e.g.,
Suh+20, Carraro+20, Tanaka+24...

Scatter depends on Eddington ratio!

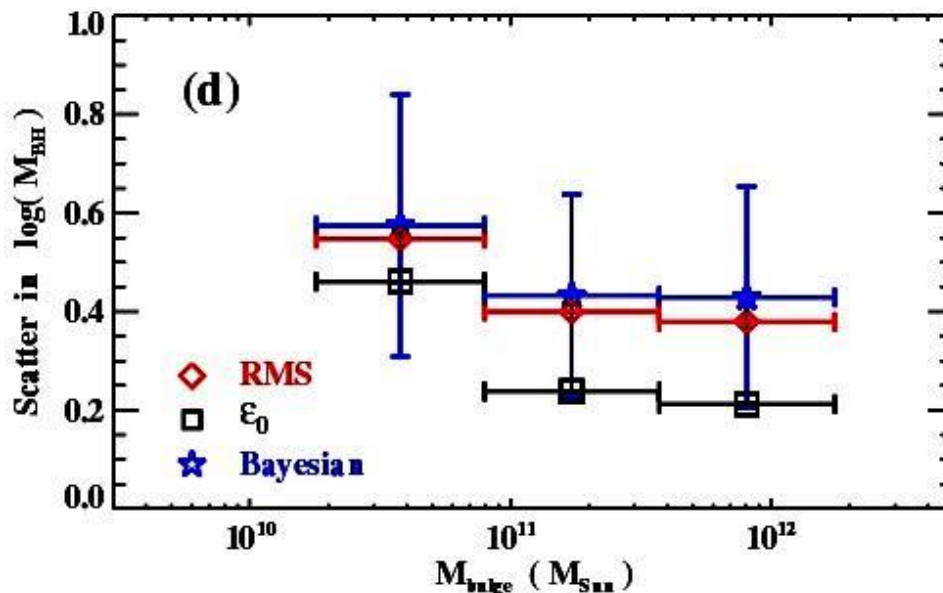


Is the M_{bh}-σ the most fundamental?

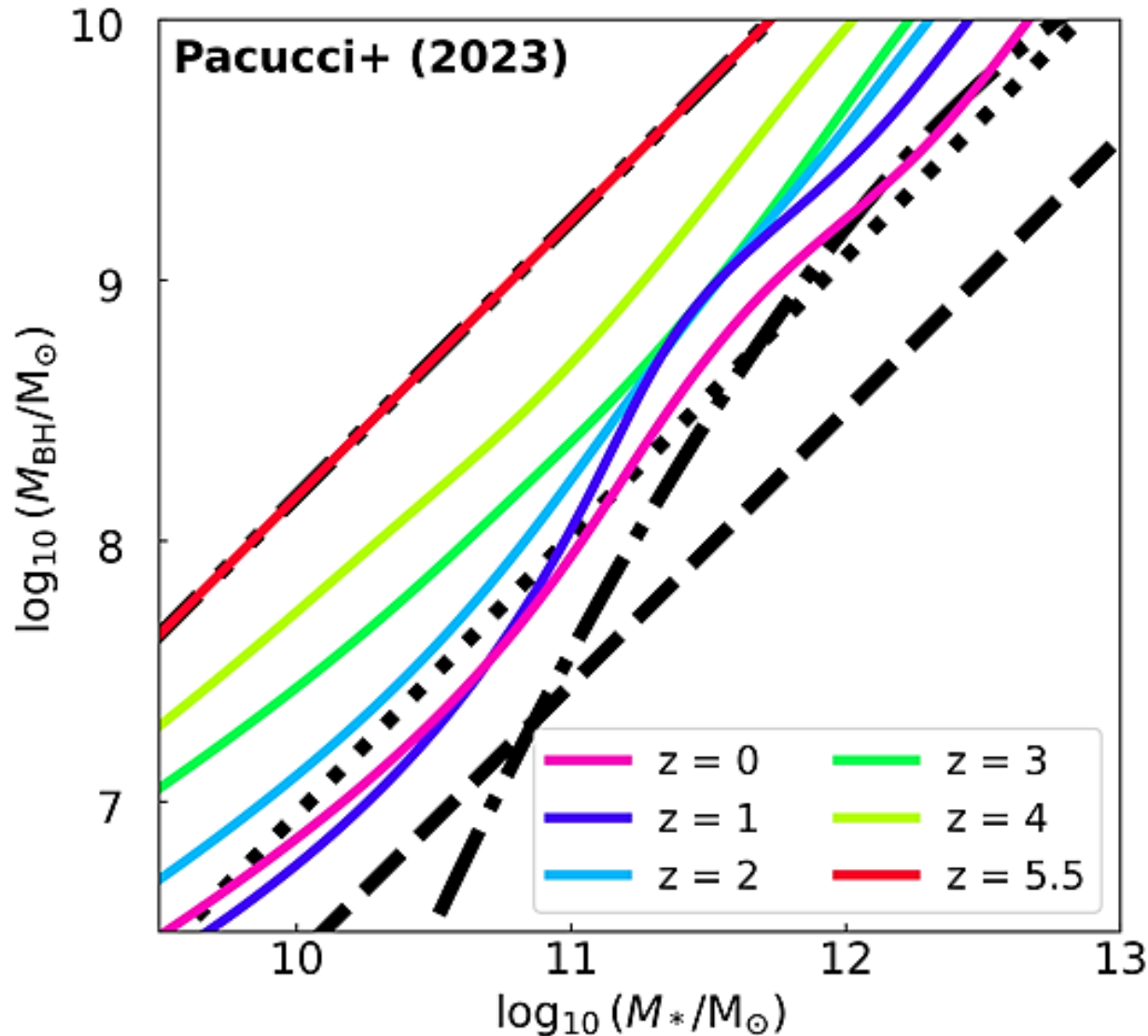


Scatter always ranging within 0.3-0.5 dex

RESIDUALS!

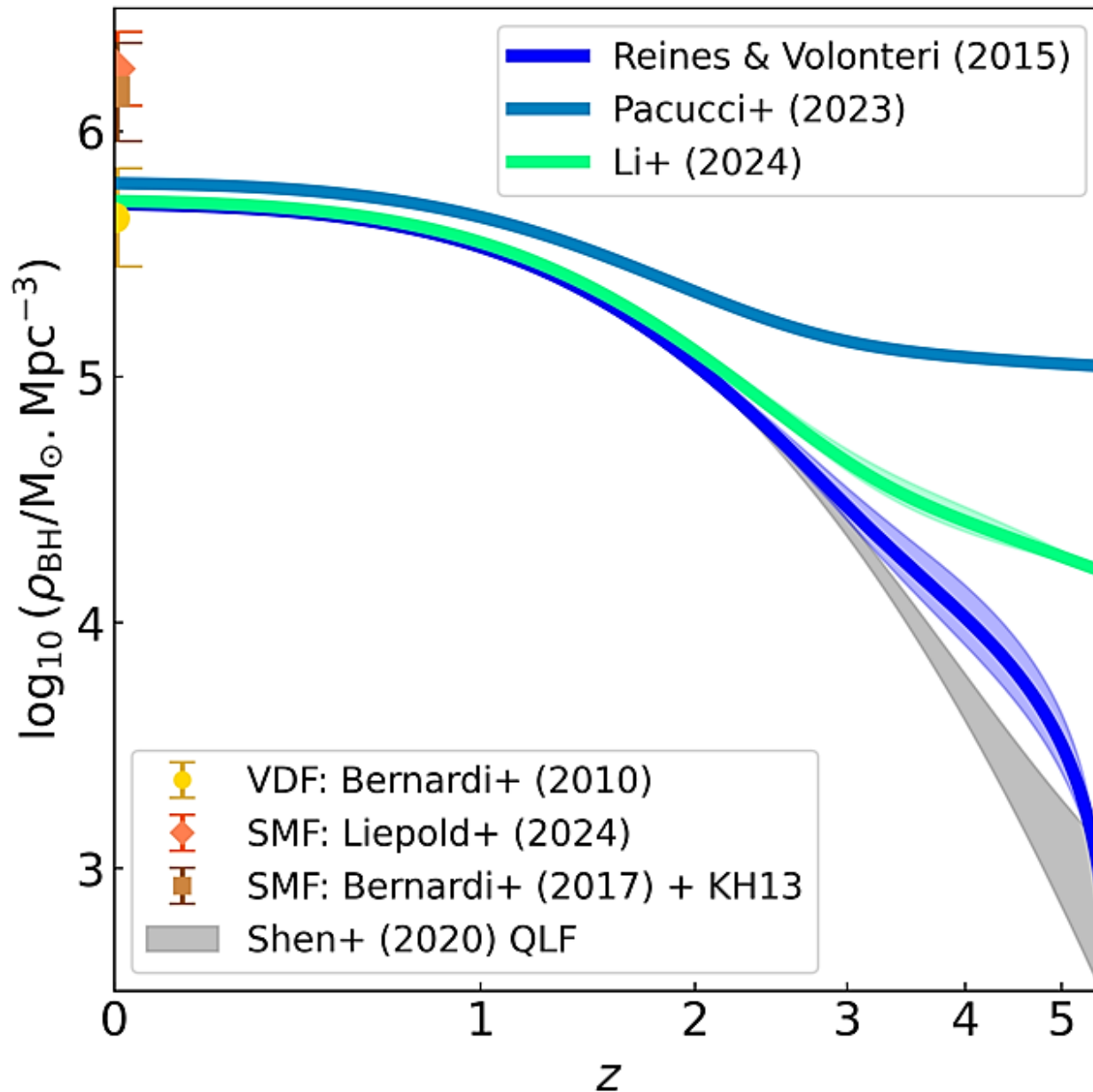


High-z conditions little effect on local demography



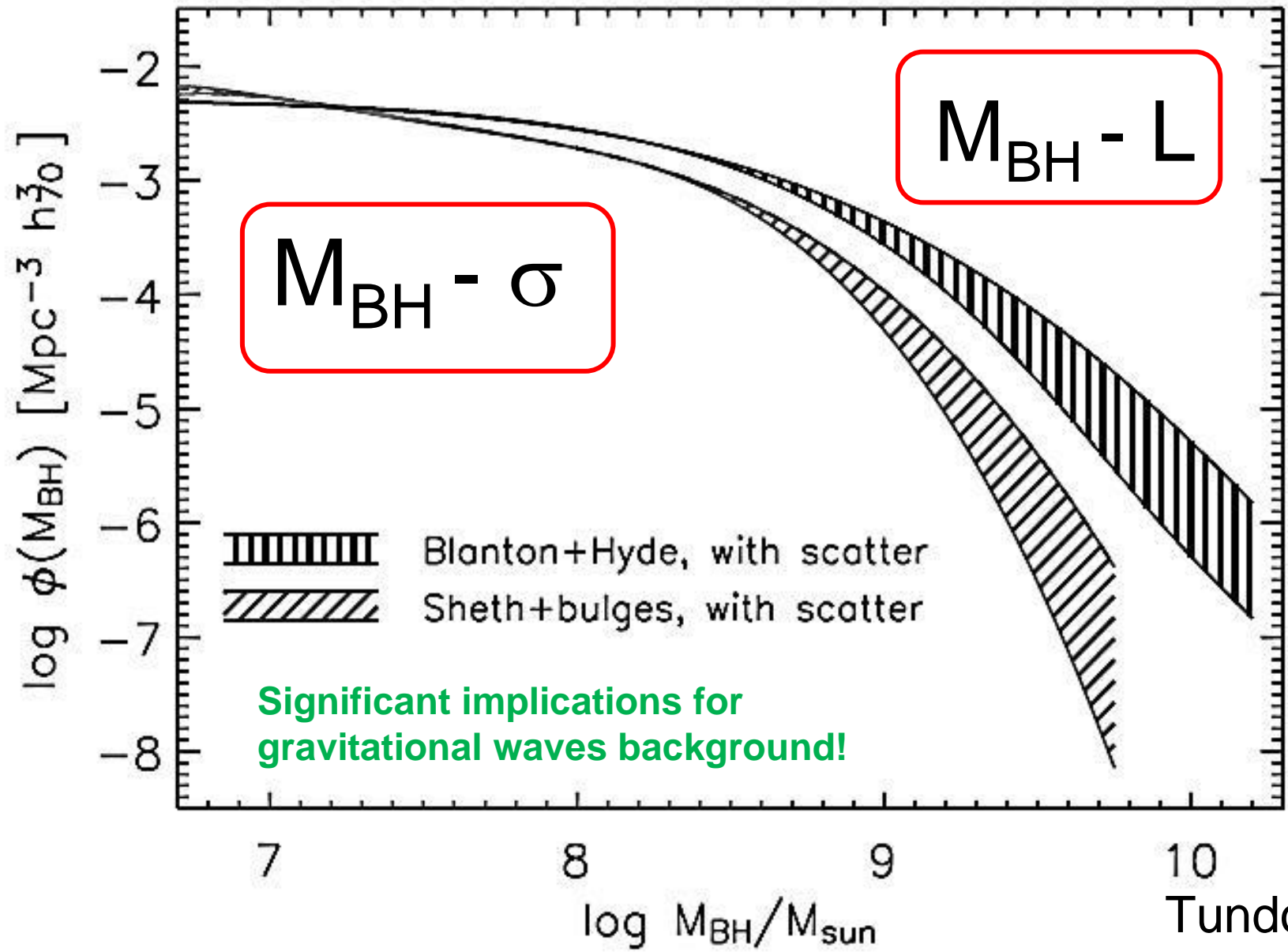
Accretion models predict that even starting from very high ICs, the $z=0$ tends to line up with the local relation

High-z conditions little effect on local demography

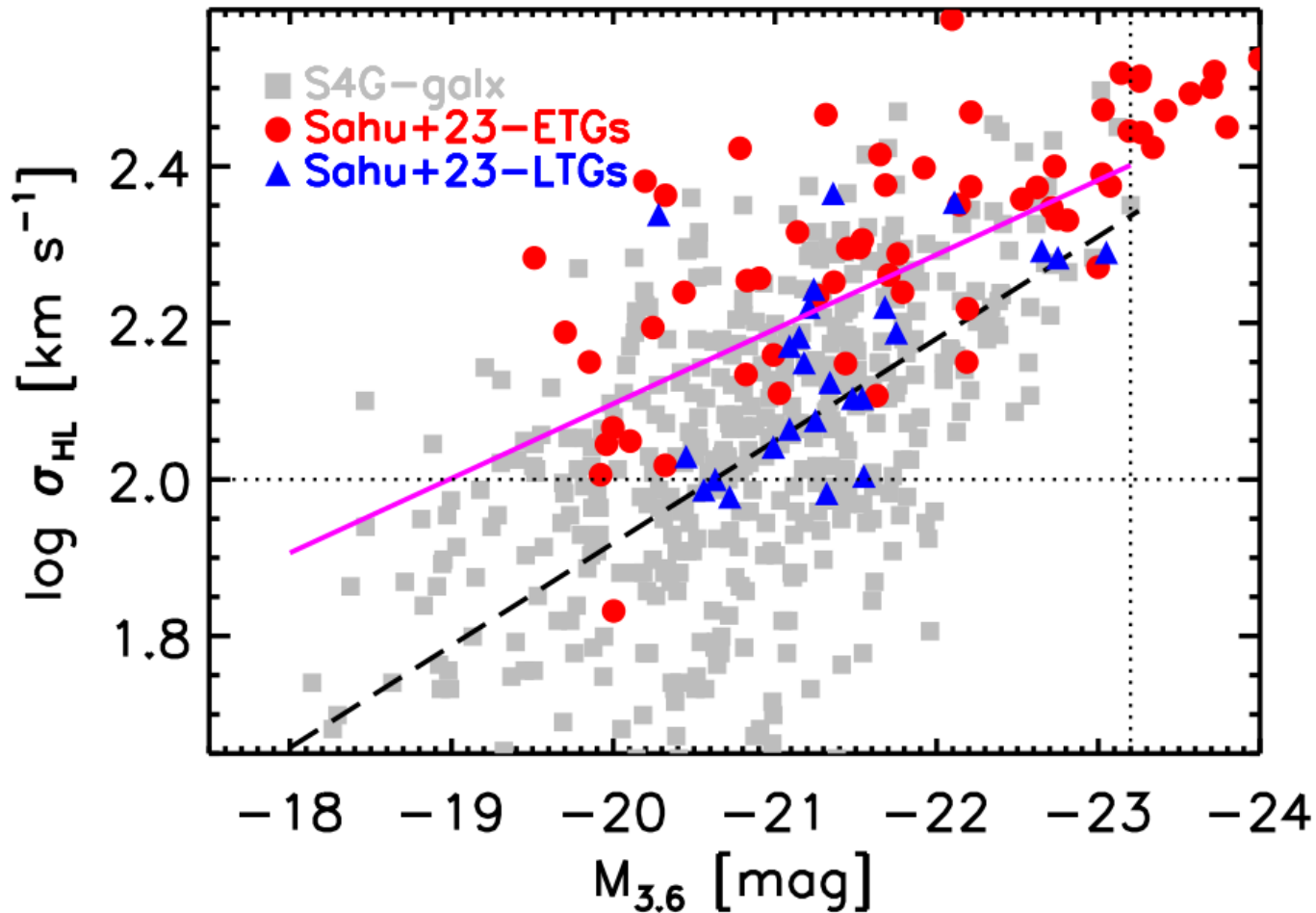


High Initial Conditions necessarily imply mild evolution in the integrated SMBH mass density!

Two SMBH mass functions?



Beware of bias!



SMBH local sample biased high compared to all local galaxies?
Observational or physical bias?