

Dark Matters 2022

Co-genesis in a dark sector

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ULB, Belgium

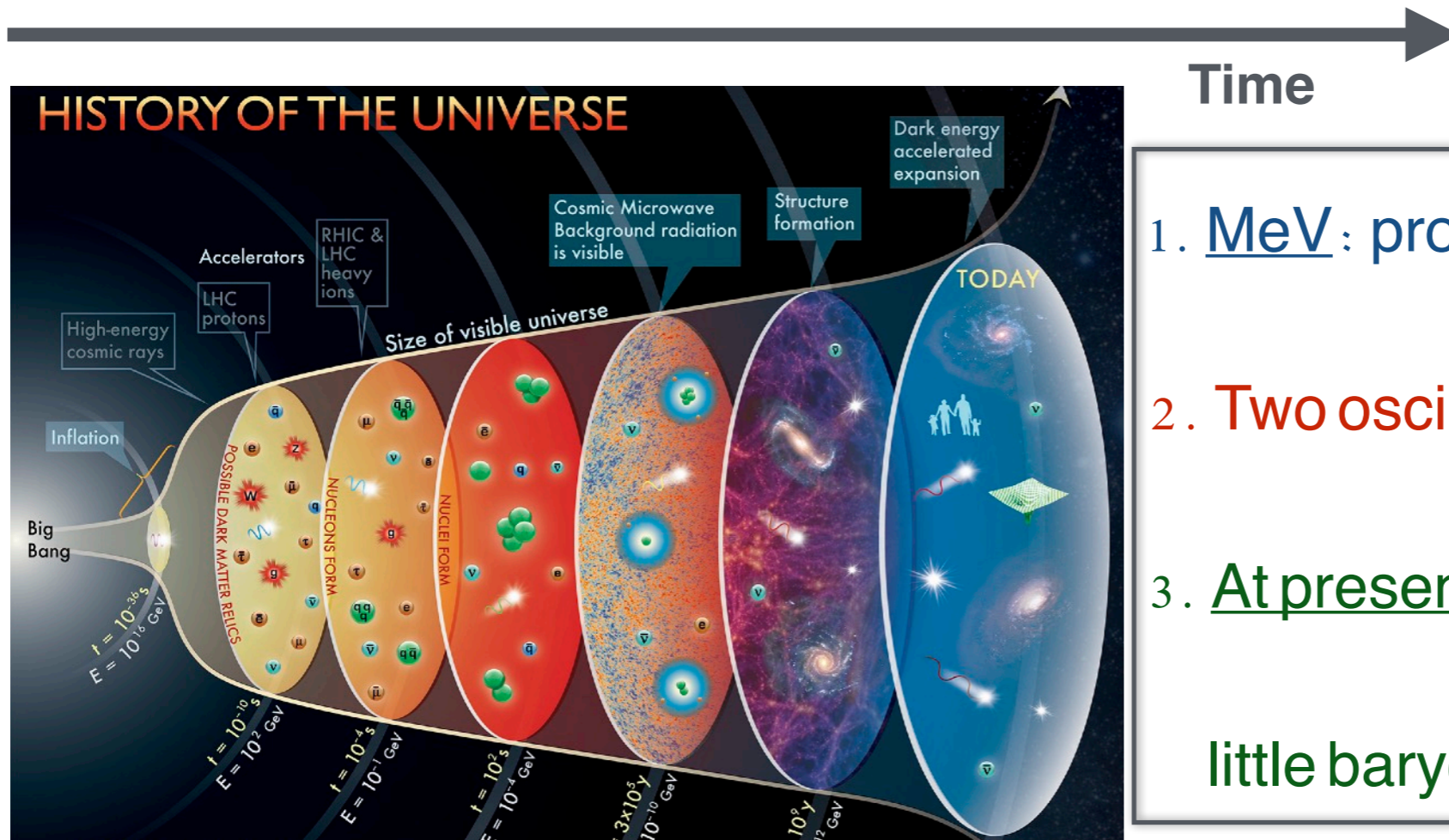


HEPHY

Xiaoyong Chu

I. Motivations

Standard Cosmology, with remaining puzzles

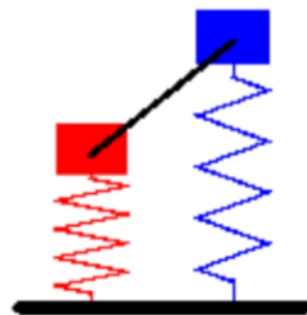


1. MeV: proton /neutron in equilibrium;
2. Two oscillating modes in T~eV;
3. At present: dark gravity potentials
&
little baryon-antibaryon annihilation



1. nucleosynthesis
2. background radiation
3. structure formation
&
cosmic rays

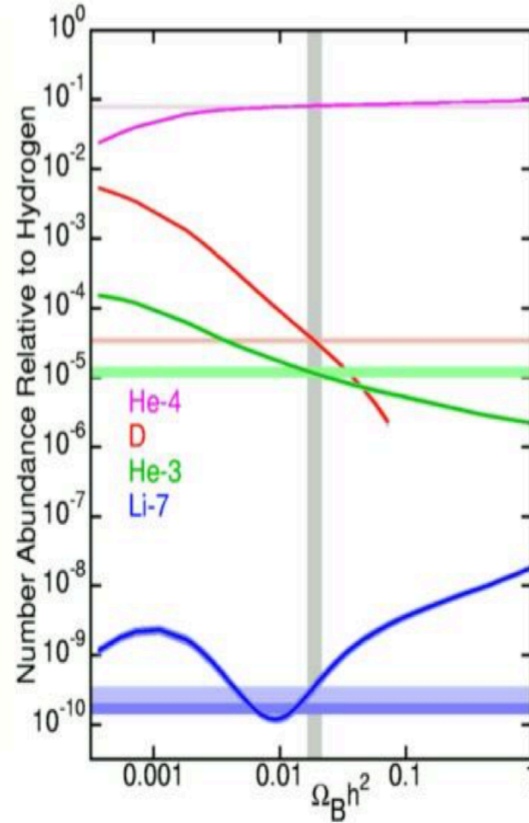
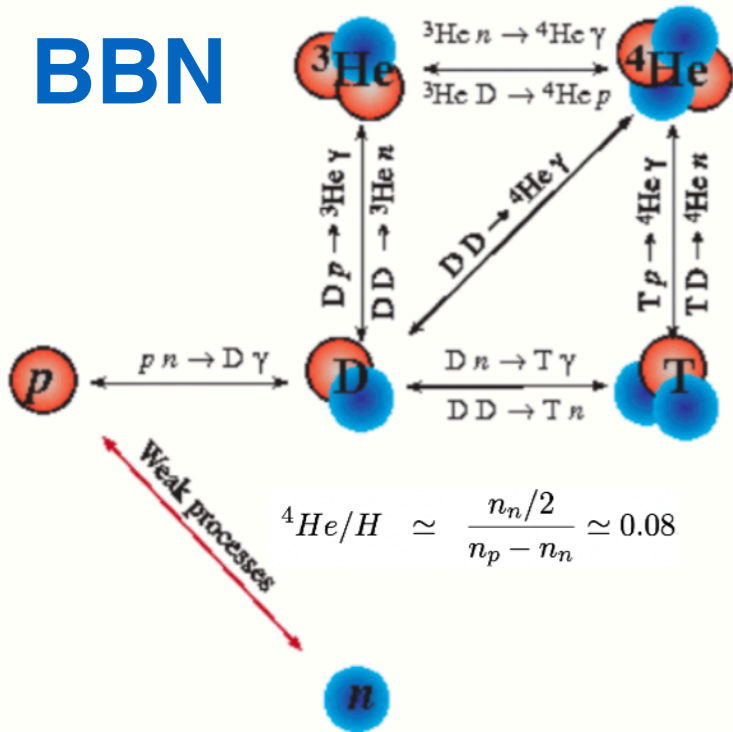
New physics
before MeV



Visible Dark Matter

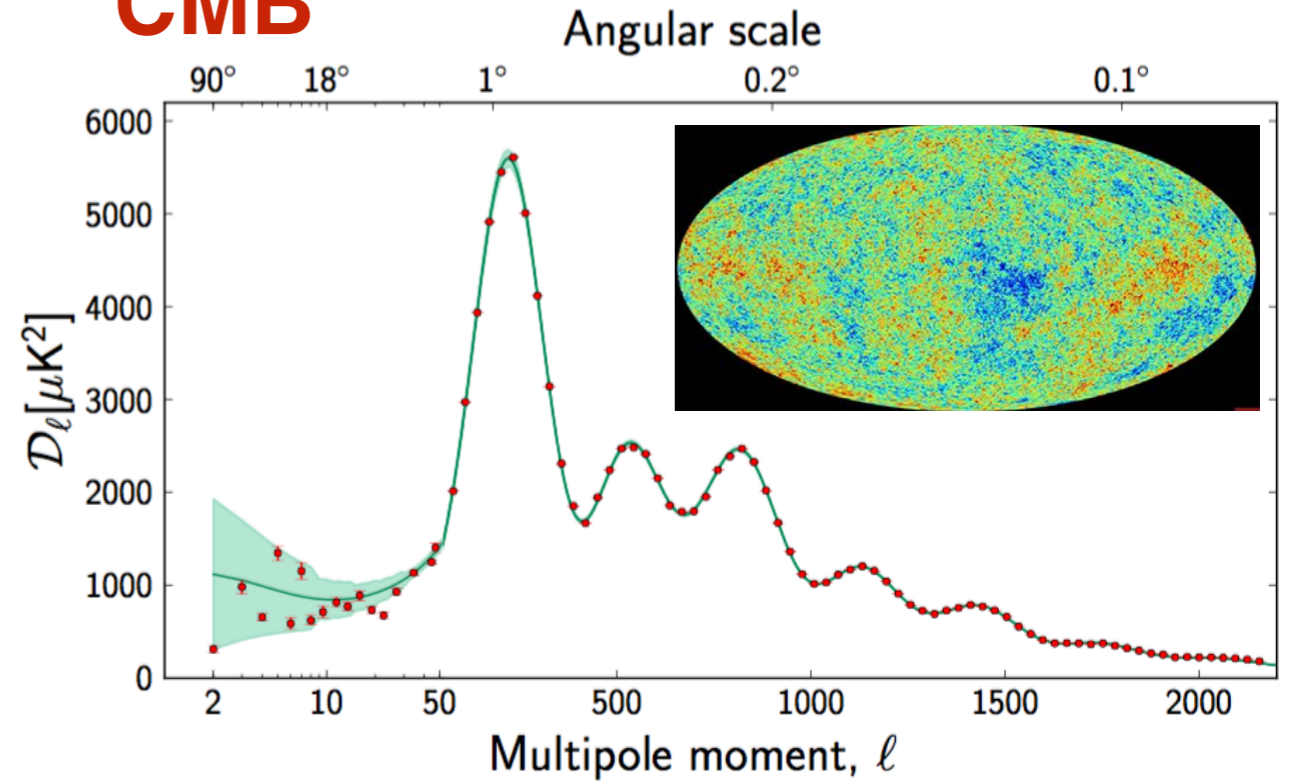
Measurements of precision cosmology

BBN



$$\Omega_b h^2 = 0.020 \pm 0.0015$$

CMB



$$\Omega_b h^2 = 0.02205 \pm 0.00028,$$

$$\Omega_{\text{DM}} h^2 = 0.1199 \pm 0.0027.$$

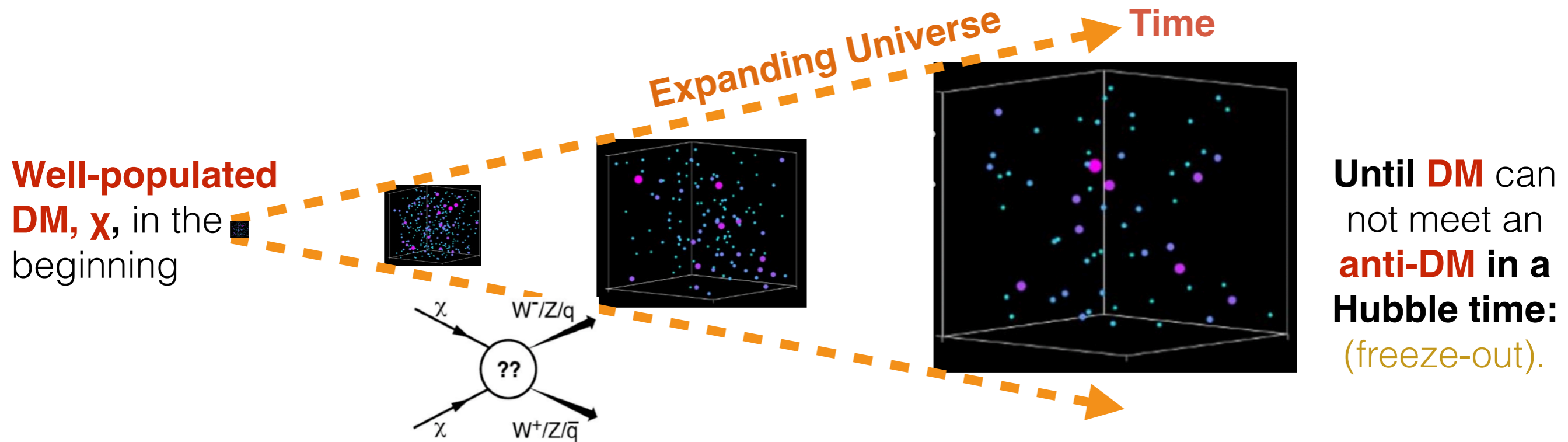
That is, $\Omega_b / \Omega_{\text{DM}} \sim 1/5$

a coincidence, **or not?**  **Co-genesis**

II. To co-generate
**dark matter (DM) &
baryon asymmetry (BAU)**

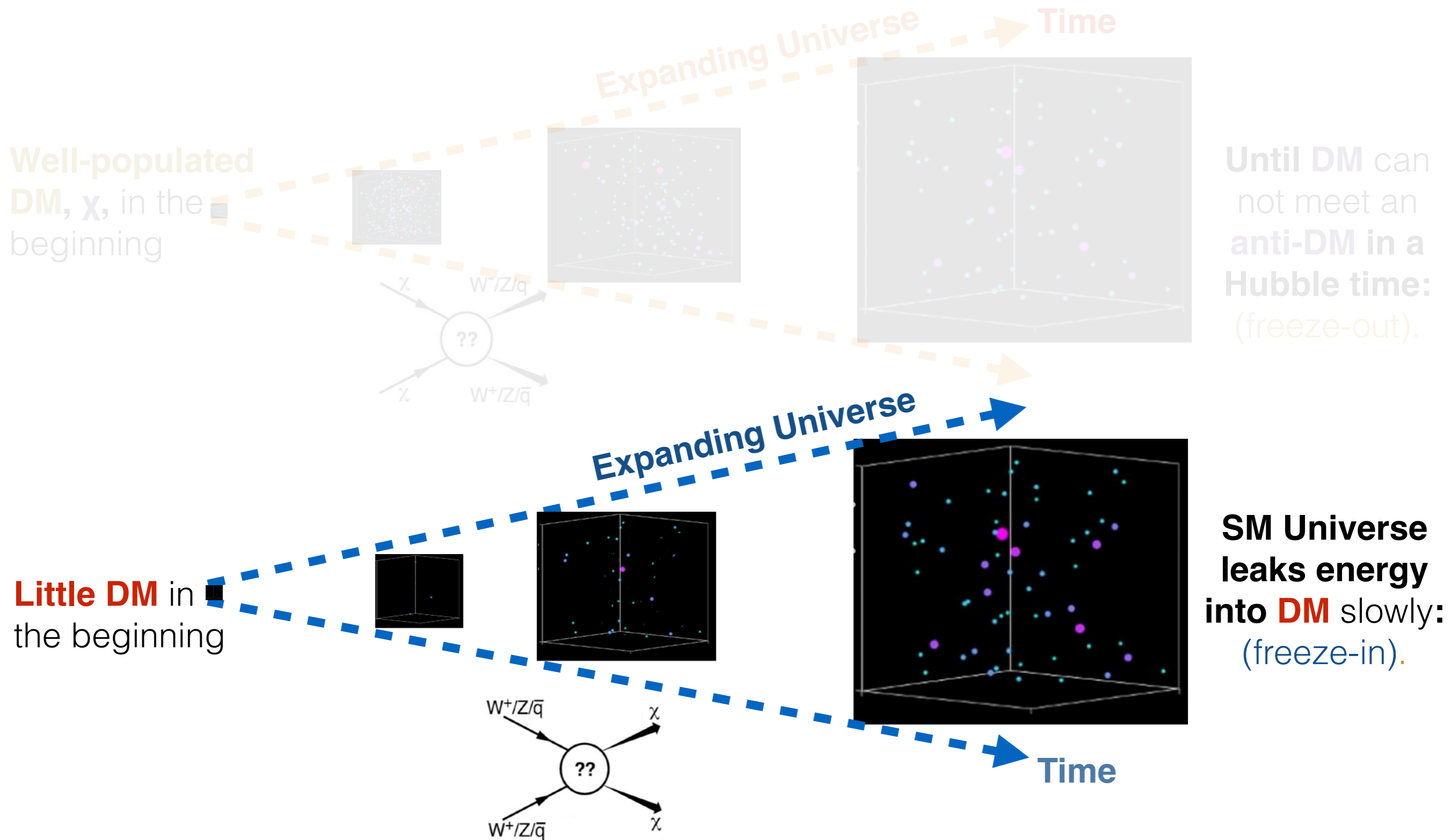
For DM generation: **freeze-out**/in and so on.

The conventional expectation: **Weakly-Interacting Massive Particles (WIMP)**



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The conventional expectation: **Weakly-Interacting Massive Particles (WIMP)**



For BAU generation: Sakharov conditions

$$\frac{n_B}{n_\gamma} \sim 6.1_{-0.5}^{+0.7} \times 10^{-10}$$

1. **C**, **CP** symmetry violation;
2. **Baryon** number violation;
3. Out of equilibrium.*

*Third condition may not be necessary as Universe **expansion violates CPT**: [spontaneous baryogenesis](#) [*Cohen&Kaplan 1987, 1988*].

One may use axion/curvature. e.g. [gravitational baryogenesis](#) [Davoudiasl et al, hep-ph/0403019]

$$\mathcal{L} \supset \int dx^4 \sqrt{-g} \lambda \frac{\partial_\mu \mathcal{R}}{M_p^2} J_{B-L}^\mu$$

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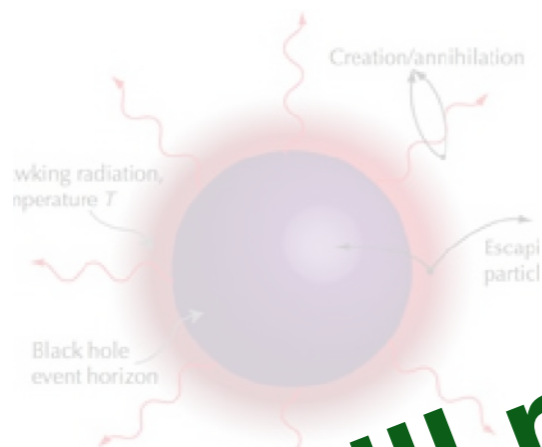
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$$\mathcal{L} \supset \int dx^4 \sqrt{-g} \lambda \frac{\partial_\mu \mathcal{R}}{M_p^2} J_{B-L}^\mu$$

Generalised to **reheating by local defects** in early Universe

e.g. primordial black hole evaporation [A. Hook 1404.0113]



$$\mathcal{L} \supset \int dx^4 \sqrt{-g} \frac{\partial_\mu \phi}{M_*} J_{B-L}^\mu$$

violating different "thermal mass" for B and Bbar.

Emission, decay of such defects also **produce DM**, leading to **co-genesis**

will not be discussed here!

(C=balls, locally reheated sphere, cosmic strings, axion quark nuggets, filtered brane, ...)

[or axion-like DM and/or Affleck-Dine baryogenesis].

Co-genesis, more globally:

$$\Omega_b/\Omega_{\text{DM}} \sim 1/5$$

A. Opposite asymmetry

$$\Delta_B + \Delta_{\text{DM}} = 0$$

conserves a $U(1)_{\text{B-L+X}}$ number, requiring only **one new process** and

$$m_{\text{DM}} \approx 5 \text{ GeV}^*$$

*DM may still vary after decoupled.

Models that **conserve a $U(1)_{\text{B-L+X}}$ number**, naturally arise in unified models [Nussinov 1985, Barr, Chivukula & Farhi 1990, ...]:

e.g. Spontaneous co-genesis [March-Russell&McCullough 1106.4319]

$$\mathcal{L} \supset \frac{\partial_\mu \phi}{f} J_X^\mu \Rightarrow U_X(T)(n_X - n_{\bar{X}})$$

with $W_X = M_X \bar{X} X + \frac{1}{M_S^2} X^2 U^c D^c D'$ satisfy $2\mu_X = \mu_{u_R} + 2\mu_{d_R}$

Co-genesis, more globally:

$$\Omega_b / \Omega_{\text{DM}} \sim 1/5$$

B. Converted asymmetry

$$\Delta_B \sim \Delta_{\text{DM}}$$

Generated then leaked. **One process** for **Δ -production**, the **other** for **Δ -conversion**.

(dark) Sphalerons [e.g. Shelton & Zurek 1008.1997, Blennow et al. 1009.3159]

Xogenesis via effective operators [Buckley&Randall 1009.0270], and so on..

$$B = -\frac{4}{13} \sum_{i=1}^N L_i \left(1 + \frac{1}{\pi^2} \frac{m_{l_i}^2}{T^2} \right)$$

[Kuzmin, Rubakov & Shaposhnikov PLB191 171(1987)]

If total ΔL vanishes

$$\Delta_\tau = B/3 - L_\tau$$

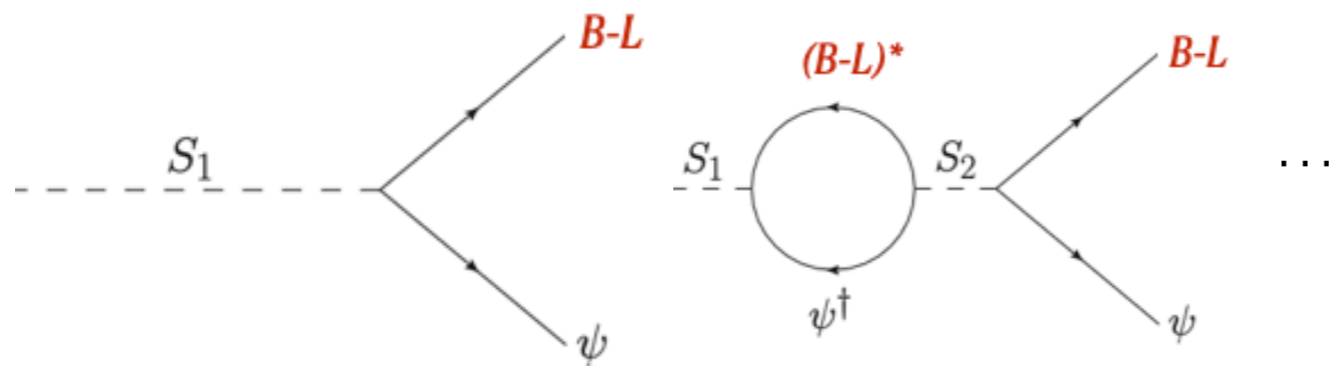
Asymmetry generated by the **secondary contributions of sphaleron** via out-of-equilibrium **flavor violation** [e.g. leptoflavorgenesis, Mukaida, Schmitz & Yamada 2111.03082]

Suitable for **multi-component DM**, similar to L-flavors, but easier to have **large CPV**.

Co-genesis, more globally:

$$\Omega_b / \Omega_{\text{DM}} \sim 1/5$$

While both may share the **out-of-equilibrium** processes / background (**S**), only **B-L asymmetry** relies on the **CP parameter** via loop interferences:



- Zero-T (or thermal) Feynman diagrams;
- If **S** is out-of-equilibrium mesons, no new CP needed
[**mesogenesis**, *Aitken, McKeen et al. 1708.01259, 1810.00880, ...*].

C. Symmetric DM

$$\epsilon_{CP} \ll 1 \rightarrow n_B / n_\gamma \ll 1$$

Correlation is not obvious, so

- **analytical DM solutions**
- **predicting exact ϵ_{CP}**

important for quantitative study.

The out-of-equilibrium processes can be DM **freeze-in** or **freeze-out**.

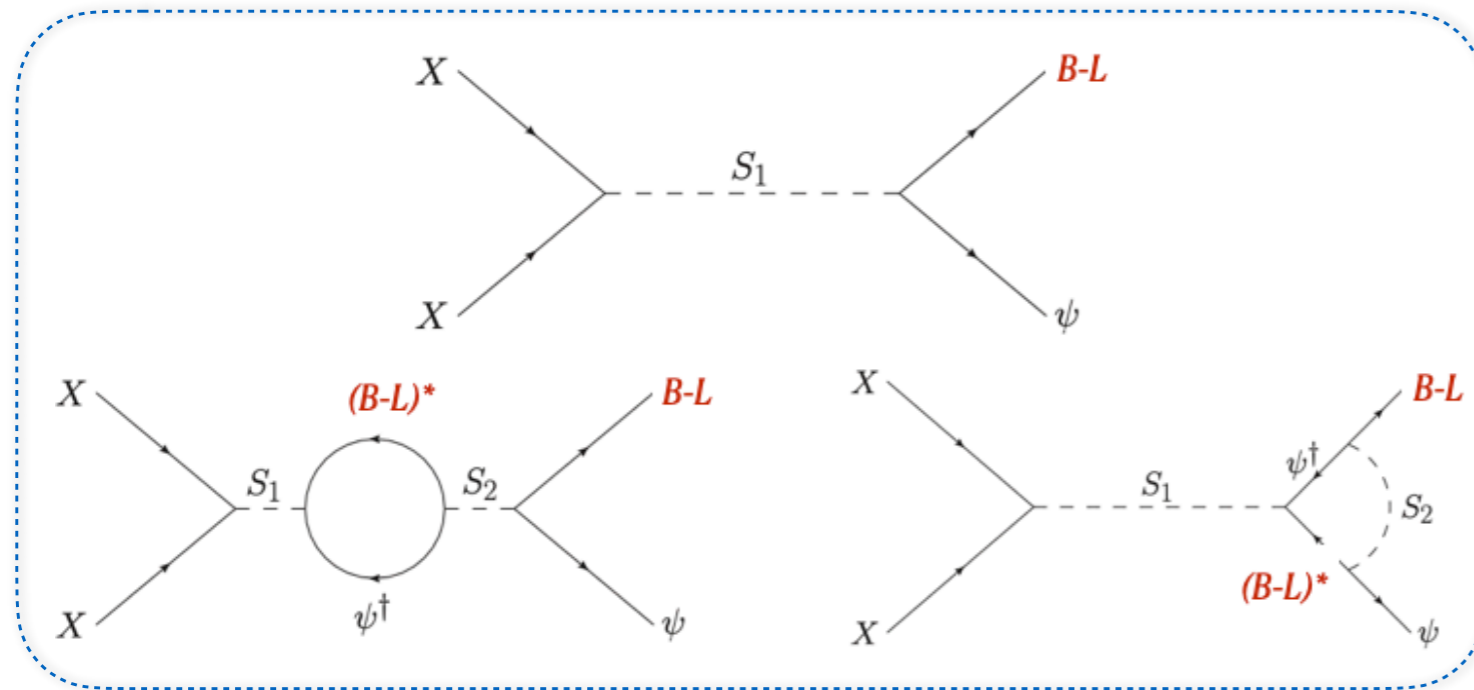
- Freeze-in, e.g. vMSM-like [*Asaka&Shaposhnikov 2005, Shuve&Tucker-Smith 2004.00636...*];
- Freeze-out: **to be discussed below**:

III. Co-genesis for symmetric freeze-out

Case I: WIMP_y (thermal) freeze-out

[McDonald 1009.3227, Cui, Randall & Shuve 1112.2704, etc.]

DM freeze-out via intermediate (B-L) violating states [Cui's review 1510.04298]



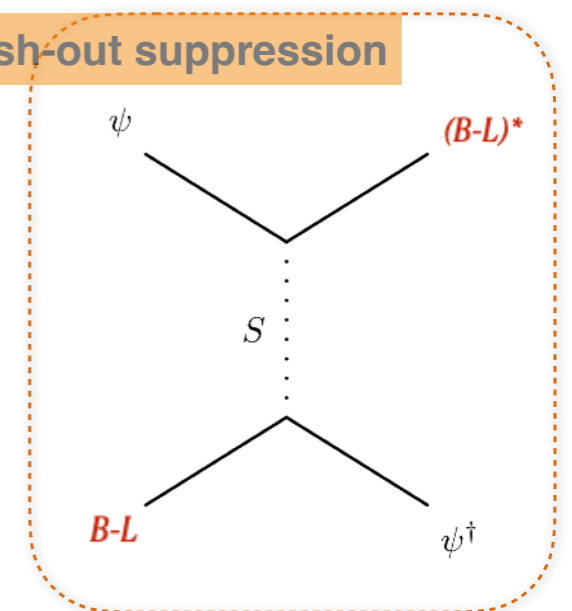
source term

Freeze-out: out-of-equilibrium

$$\frac{dY_X}{dx} = -\frac{2s(x)}{xH(x)} \langle \sigma_{\text{ann}} v \rangle [Y_X^2 - (Y_X^{\text{eq}})^2]$$

At the same time, intermediate states also induce **wash-out**, e.g.

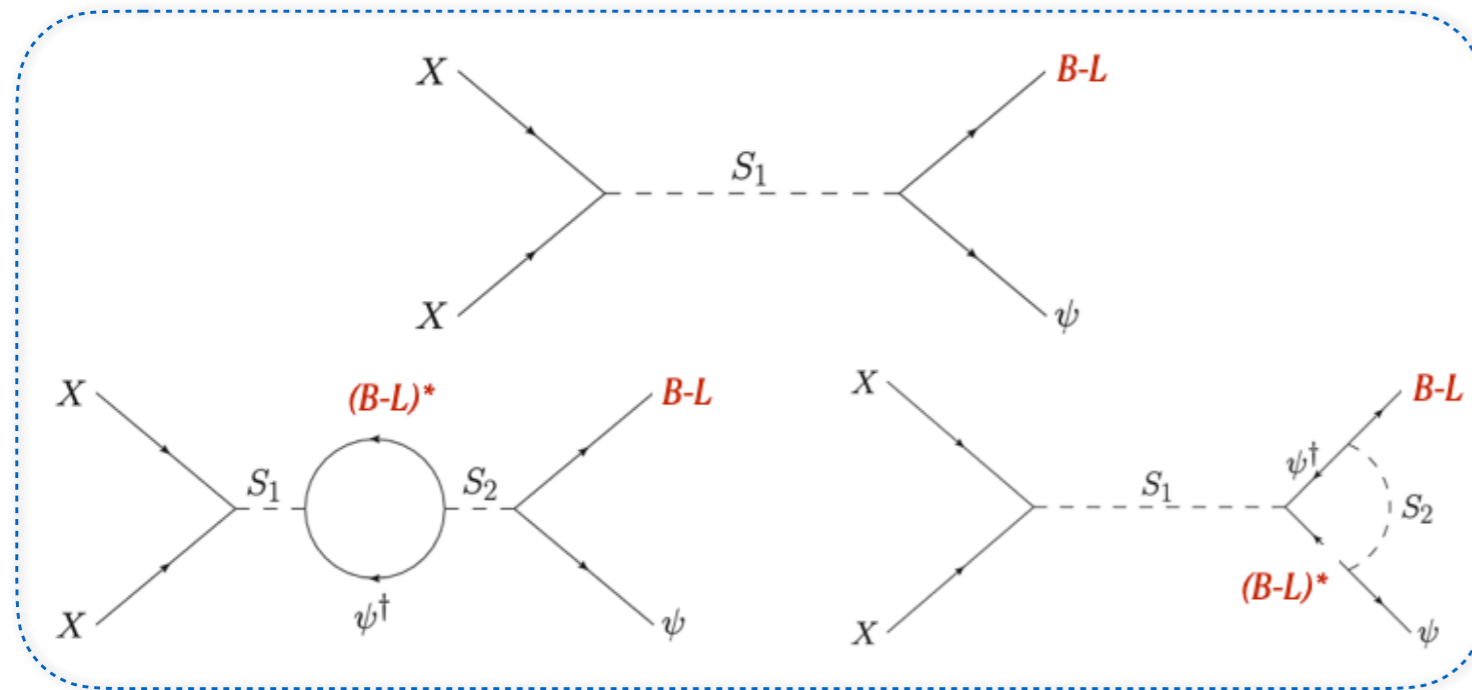
wash-out suppression



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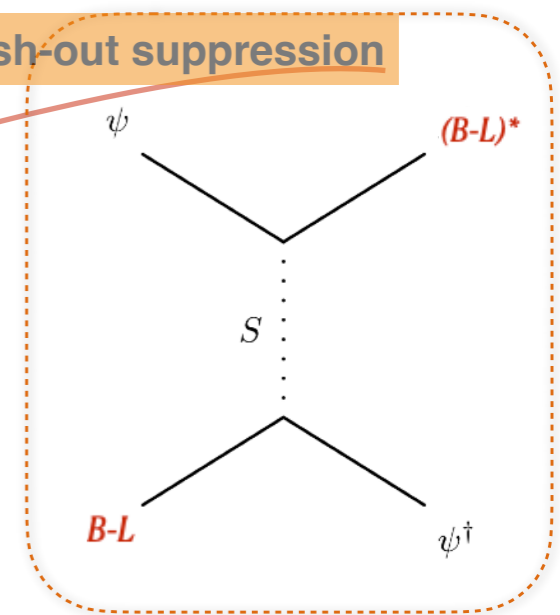
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At the same time, intermediate states also induce **wash-out**, e.g.

$$Y_B(0) = \epsilon_{\text{CP}} \int_0^{T_D} \frac{dY_{\chi_B}}{dT} \exp\left(-\int_0^T \frac{\Gamma_W(T')}{H(T')} \frac{dT'}{T'}\right) dT$$

wash-out suppression

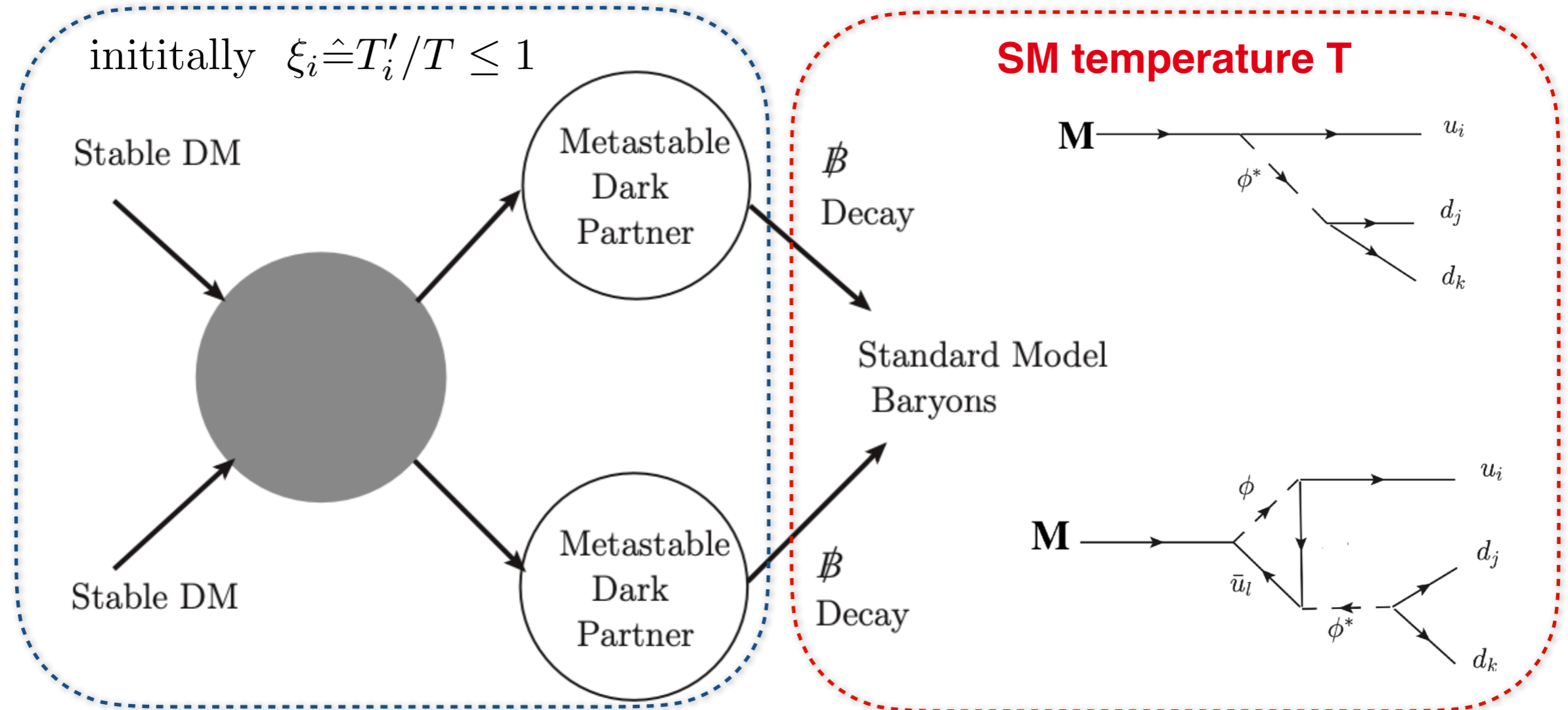


Strongly coupled S: typically important wash-out suppression

Case II: WIMPy dark freeze-out

[**xc**, Cui, Pradler & Shamma 2112.10784]

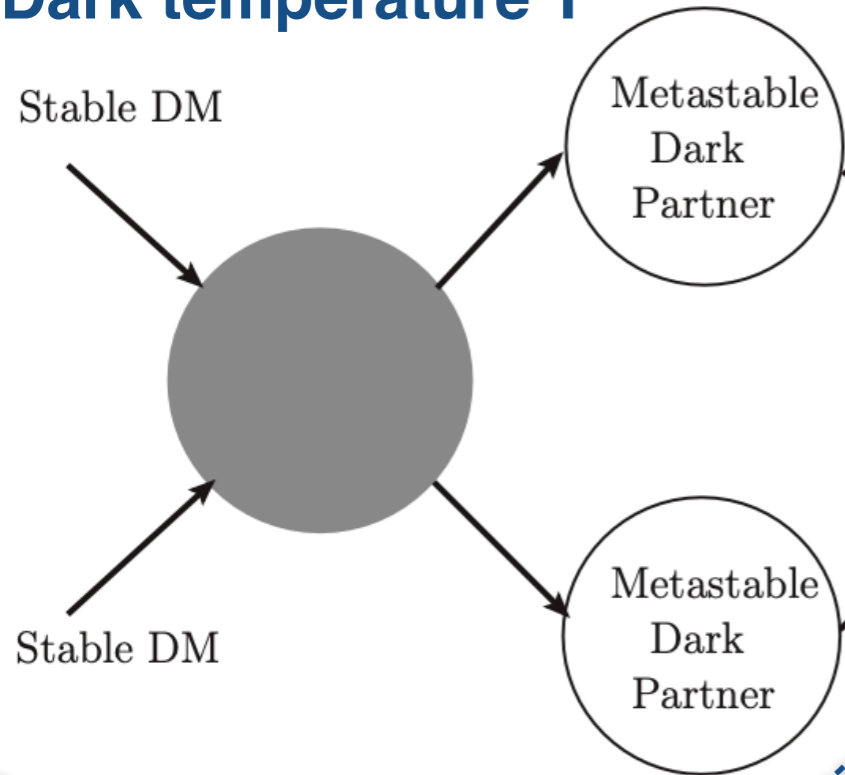
Simply assume **final states, M**, are not in equilibrium with SM particles:



$$\dot{n}_{\text{DM}} + 3Hn_{\text{DM}} = -\langle\sigma_{\text{DM}v}\rangle n_{\text{anni.}}^2 + \langle\sigma_{\text{creat.}v}\rangle n_{\text{M}}^2 \quad Y_B = \epsilon_{\text{CP}} Y_{\text{M}} \simeq \left(\frac{\text{Im}[\alpha_j \alpha_m \beta_j^* \beta_m^*]}{|\alpha_j|^2} \frac{m_{\chi_2}^2}{20\pi m_\phi^2} \right) Y_{\text{M}}$$

Analytical solutions are possible & Absence of wash-out.

Dark temperature T'



a) If total dark **particle number is conserved**.

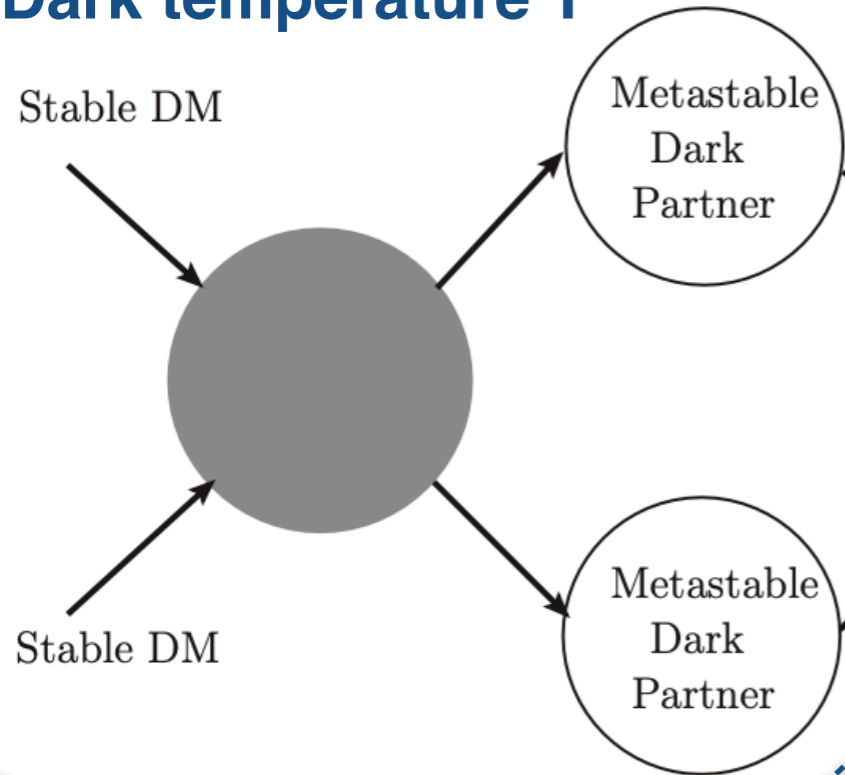
e.g. nearly degenerate $m_{DM} \geq m_M \gg T'_{f.o.}$

$$T' \simeq (3\xi_i T)^2 / m_M \quad (\hat{=} \beta T^2 / m_{DM})$$

$$\delta = (m_{DM} - m_M) / m_{DM} \ll 1$$

Quasi-static solution:
$$Y_M = \frac{1}{1 + (1 - \delta)^{-3/2} e^{-\delta m_{DM} / T'}} (Y_{DM} + Y_M)$$

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Allowing analytical results:

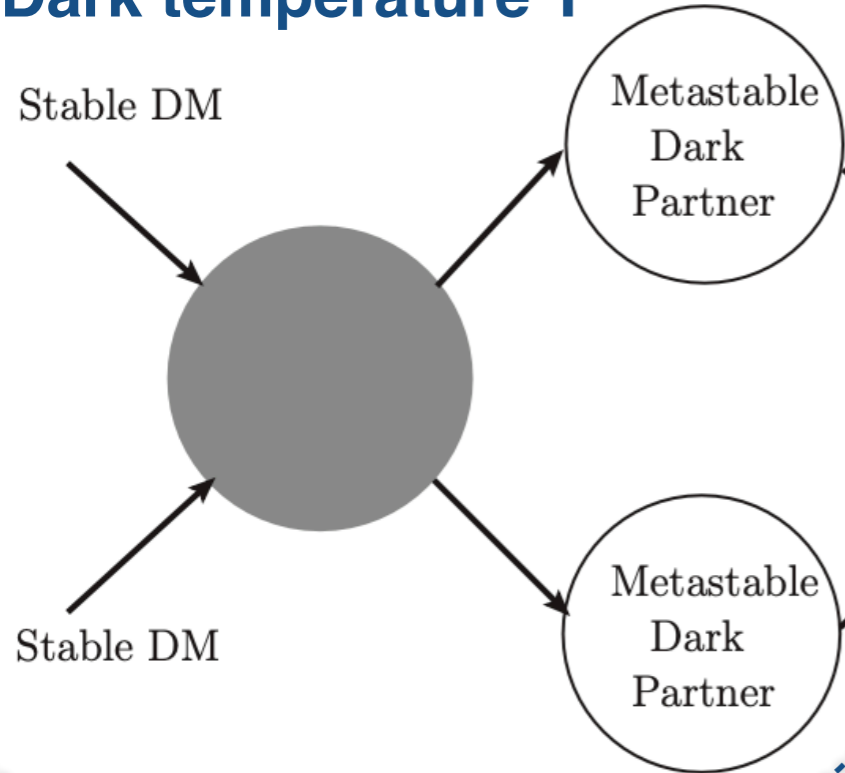
→
$$Y_{DM} \simeq \frac{1}{\lambda} \left(\frac{1}{\delta \beta} \ln \left[\frac{0.15 \lambda \xi_i^3 \beta^{1/2} \delta^{1/2}}{(1 - \delta)^{3/2}} \frac{g_\chi}{g_{*S}} \right] \right)^{1/2} \quad \text{for s-wave.}$$

$$\lambda = 0.264 g_{*S} / g_*^{1/2} m_{PI} m_{DM} \sigma_0$$

Case II: WIMPy dark freeze-out

[**xc**, Cui, Pradler & Shamma 2112.10784]

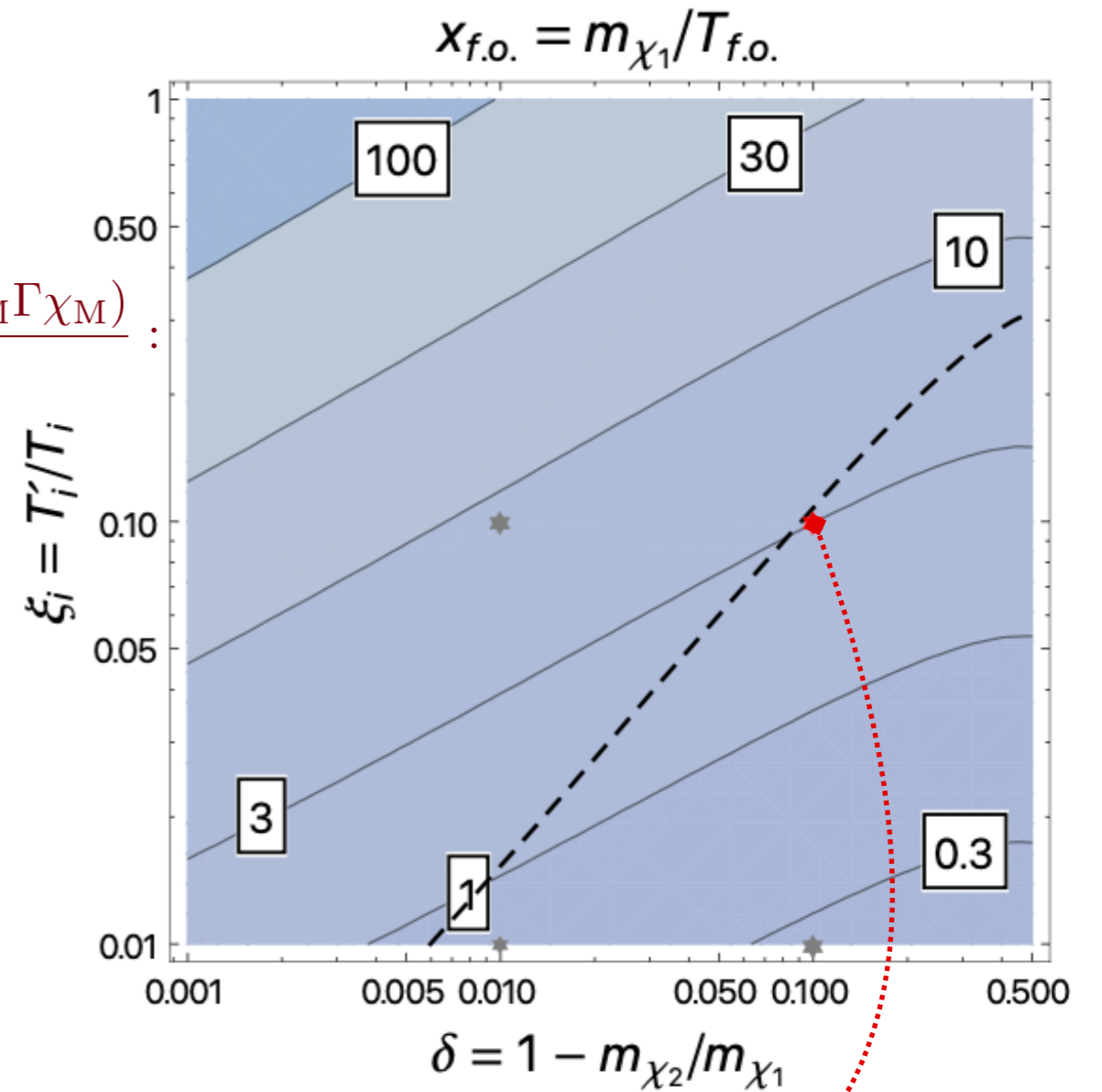
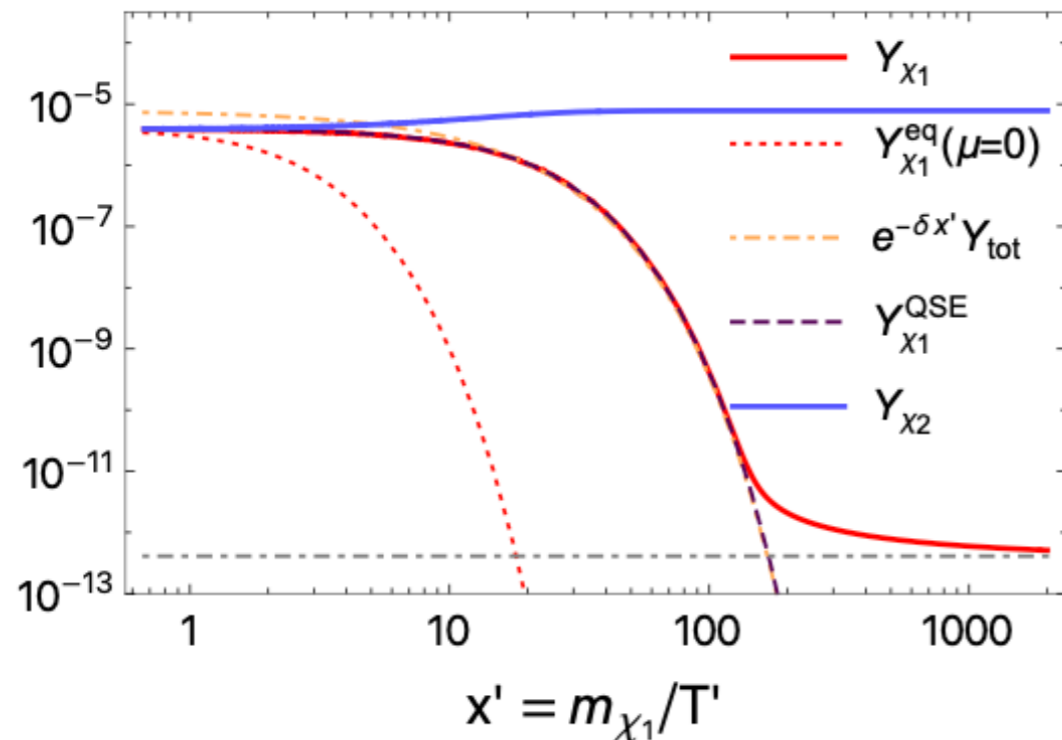
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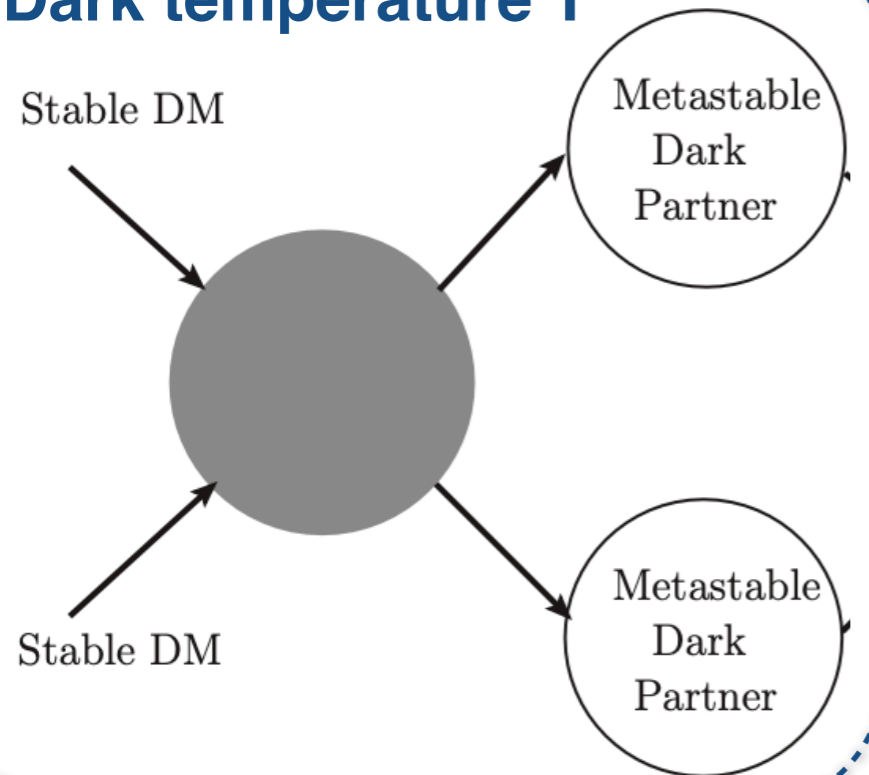
For **1 TeV DM**

via $\frac{(\bar{\chi}_{\text{DM}}\Gamma_{\chi_{\text{DM}}})(\bar{\chi}_{\text{M}}\Gamma_{\chi_{\text{M}}})}{(4\text{ TeV})^2}$



Agree with numerical calculations well.

Dark temperature T'



b) if allows **number-changing** of dark partner M:

$$m_{DM} \gg T'_{f.o.} \gg m_M$$

A dark freeze-out, with $\xi \equiv T'/T \simeq \text{const.}$

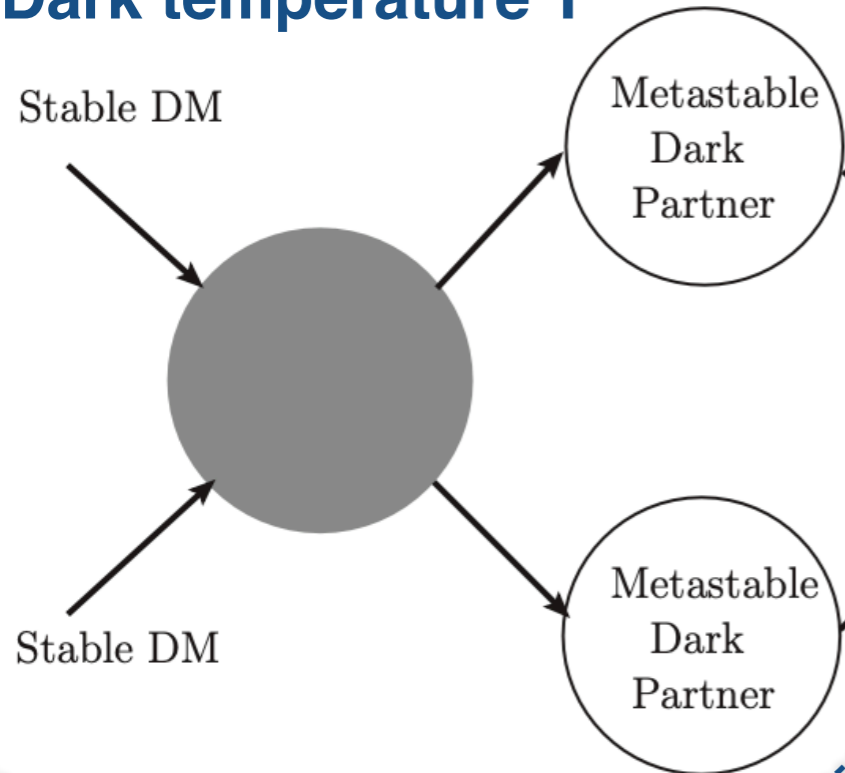
$$Y_{DM} \simeq \frac{\xi}{\lambda} x_{f.o.} \propto \frac{\xi}{\langle \sigma_{\text{anni.}} v \rangle} \text{ for s-wave freeze-out}$$

It converges to conventional WIMP results with $\xi=1$, as shown in the literature

[Ackerman et al. 0810.5126, Feng et al.0808.2318, **XC**, Hambye & Tytgat 1112.0493].

$$Y_M \propto \xi^3 \text{ (or given by SIMP-like freeze-out)}$$

Dark temperature T'



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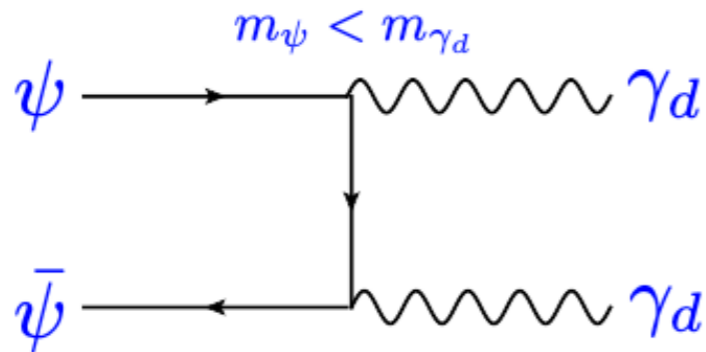
To combine a & b:

$$\frac{\Omega_B}{\Omega_{DM}} = \epsilon_{CP} \frac{m_p}{m_{DM}} \times \begin{cases} 0.42 \frac{g_X}{g_*} \frac{\xi_i^3 \lambda}{(2n+1)\beta^n} \frac{1}{x_{f.o.}^{2n+1}} - 1 & \text{near-degenerate} \\ 0.42 \frac{g_X}{g_*} \frac{\xi_i^3 \lambda}{(n+1)\xi_{f.o.}^{-n}} \frac{1}{x_{f.o.}^{n+1}} - 1 & \text{hierarchical} \end{cases}$$

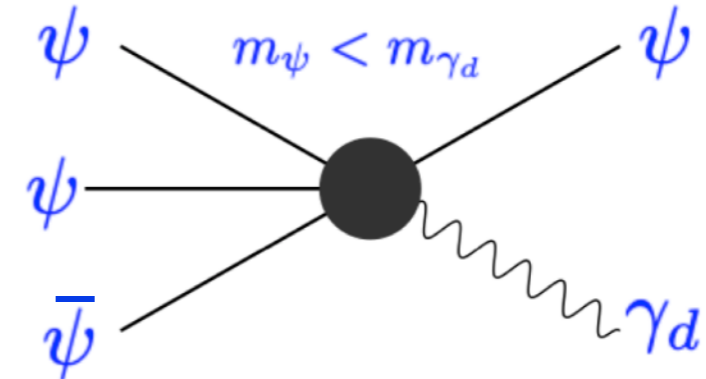
To **suppress wash-out** in DM freeze-out:

Many models contains a **heavy partner** (may be **heavier than DM**).

- (Enabled) **forbidden annihilation**

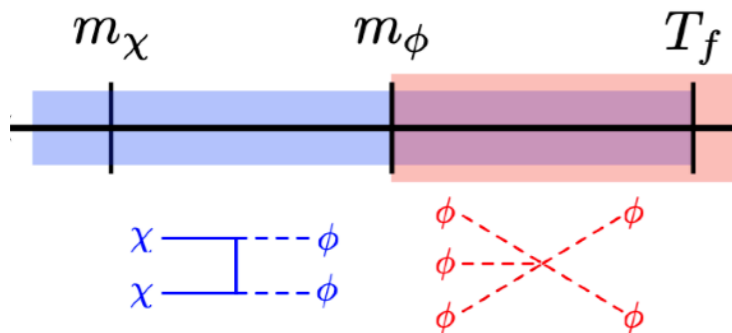


[Griest & Seckel PRD43, 3191(1991), D'Agnolo & Ruderman 1505.07107]



[Cline, Liu, Slatyer & Xue 1702.07716]

- **Cannibal annihilation**

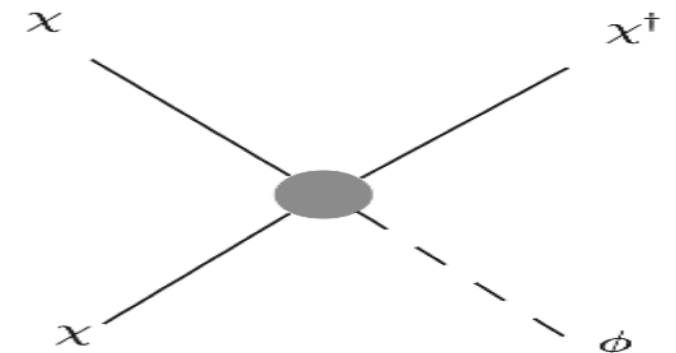


[Carlson, Machacek & Hall, ApJ398, 43(1992), Pappadopulo, Ruderman & Trevisan 1602.04219, etc.]

- **Meta-stable bound states** [see Petraki's talk]

- Also *semi-annihilation/catalysed/inverse-decay/multi-step+ freeze-out*

[1003.5912, 1705.08450, 1803.02901, 1906.00981, 2003.04900, 2004.07705, 2102.02447, 2111.14857, ...]



Symmetric DM in a **general BAU set-up**:

1. **C**, **CP** symmetry violation;
2. **Baryon** number violation;
3. Out of equilibrium.

$$\frac{dY_{B-L}}{dt} = (\epsilon_{CP} \Gamma_V) (Y_N - Y_N^{\text{eq}}) - \Gamma_{\text{wash-out}} Y_{B-L}$$

source term wash-out suppression

Sufficient BAU abundance can be obtained from:

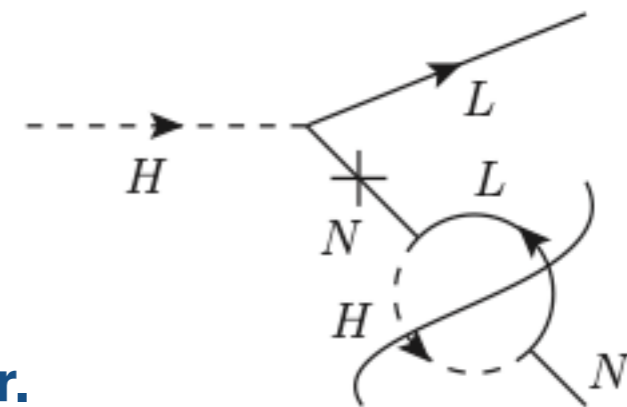
- **Early decoupling** of wash-out: a naive example above

To suppress wash-out, one may alternatively **stop EW sphaleron**

processes when ΔB reaches its maximum:

[e.g. *Hambye & Teresi 1606.00017*, where the BEH scalar may decay to generates ΔL due to thermal corrections]

More freedom to have phase transition in a dark sector.



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source term wash-out suppression

Sufficient BAU abundance can be obtained from:

- **Strong deviation** from chemical equilibrium

Simplest: **thermal** leptogenesis

N - heavy Majorana neutrino

$$Y_N - Y_N^{\text{eq}} = \frac{1}{\Gamma_{\text{tot}}} \frac{dY_N}{dt} \simeq \frac{1}{\Gamma_{\text{tot}}} \frac{dY_N^{\text{eq}}}{dt} \ll 1$$

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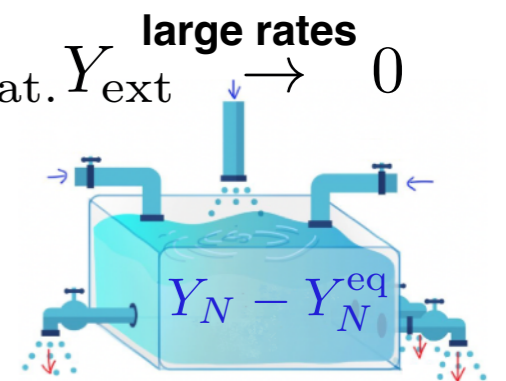
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New: **quasi-static equilibrium (QES)**
 [instead of thermal equilibrium]

$$\frac{dY_N}{dt} = -\Gamma_{\text{tot}} (Y_N - Y_N^{\text{eq}}) + \Gamma_{\text{creat.}} Y_{\text{ext}} \xrightarrow{\text{large rates}} 0$$

$$\rightarrow (Y_N - Y_N^{\text{eq}}) \simeq \frac{\Gamma_{\text{creat.}}}{\Gamma_{\text{tot}}} Y_{\text{ext}}$$



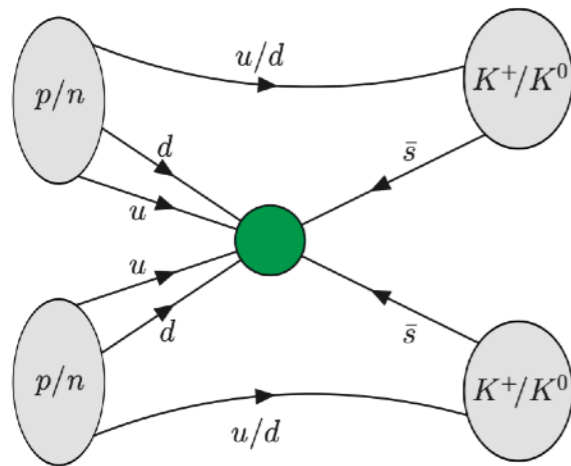
Dark sector naturally serves as external sources!

IV. Relevant **experimental searches**

A meta-stable **B-violating** particle [χ_M -like particle]

Set it to be a Majorana fermion χ_M with $\mathcal{L}_{|\Delta B|=1} \supset \frac{\alpha_j}{\Lambda^2} (\bar{u}_j P_L \chi_M) (\bar{d}_k P_L d_l^c) + h.c.$

1. Strong constraints from **di-nucleon decay & n-nbar oscillation**:



[Aitken, MaKeen et al. 1708.01259]

e.g. for (uds): $\frac{\alpha_j^2}{m_M \Lambda^4} \lesssim \frac{10^{-10}}{\text{TeV}^5}$

→ To have successful **baryogenesis** and **nucleosynthesis**, we choose **heavy quarks**, e.g. (c ds), (u db).

A meta-stable **B-violating** particle [χ_M -like particle]

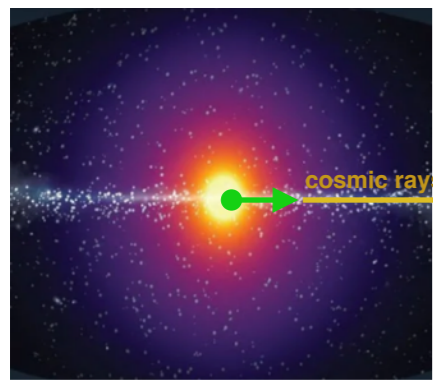
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1. Strong constraints from **di-nucleon decay & n-nbar oscillation:**

—————> **heavy quarks**, e.g. (cds), (udb).

2. **On-shell χ_M from DM annihilations:**

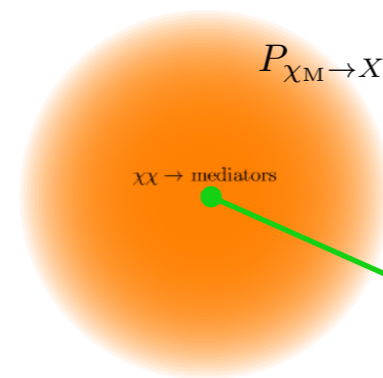
at **Galactic centre**: indirect detection



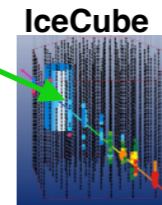
typically $\tau_M \sim 10^{-7} - 10^{-2}$ sec

—————> $m_{DM} \geq \mathcal{O}(10^2)$ GeV

inside **the Sun**: DM (in)direct detection



$$P_{\chi_M \rightarrow X} |_{\text{detector}} = \frac{V_{\text{detector}}}{l_M \cdot 4\pi r_{\text{Earth}}^2} \approx 0.8 \times 10^{-13} \left(\frac{0.02 \text{ sec}}{\tau \sqrt{m_{DM}^2/m_M^2 - 1}} \right)$$



assuming one event per year:

—————> $\sigma_{\chi N}^{\text{SI}} \sim 10^{-45} - 10^{-46} \text{ cm}^2$

Weak even in this best scenario.

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1. Strong constraints from **di-nucleon decay & n-nbar oscillation:**

→ **heavy quarks**, e.g. (c d s), (u d b).

2. **On-shell χ_M from DM annihilations:**

→ $m_{\text{DM}} \geq \mathcal{O}(10^2) \text{ GeV}$

→ $\sigma_{\chi N}^{\text{SI}} \sim 10^{-45} - 10^{-46} \text{ cm}^2$

Weak even in this best scenario.

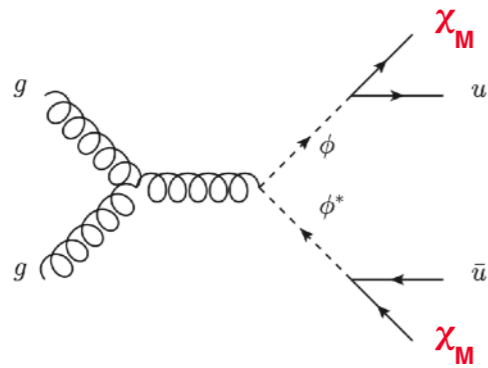
3. **Neutron electric dipole moment** bounds on CP-violations:

→ use only **right-handed quarks** and left-handed anti-quarks

(to have further Yukawa suppression [see e.g. *N.Yamanaka et al. 1703.01570*])

A meta-stable B-violating particle [χ_M -like particle]

- **Collider:** displaced vertices & missing ET



$$\mathcal{L}_{UV} \supset \alpha_j \phi(\bar{u}_j P_L \chi_M) + h.c.$$

coloured heavy scalar

Meta-stable fermion

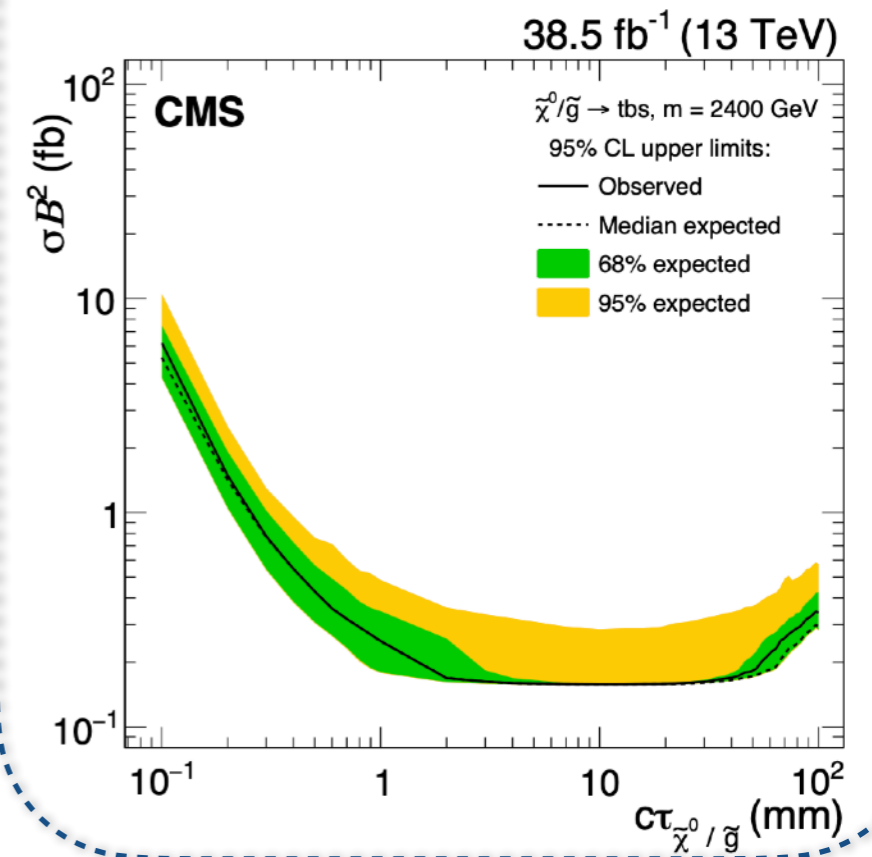
With 10 TeV scalar, production is suppressed: $\sigma_M \sim \left(\frac{|\alpha|}{10^{-2}}\right)^4 \text{ fb.}$

Small coupling to create visible displaced vertices:

$$c\gamma\tau_M = 4 \text{ cm} \left(\frac{\gamma}{10}\right) \left(\frac{10^{-4}}{|\alpha|}\right)^2 \left(\frac{1 \text{ TeV}}{m_M}\right)^5 \left(\frac{m_\phi}{10 \text{ TeV}}\right)^4$$

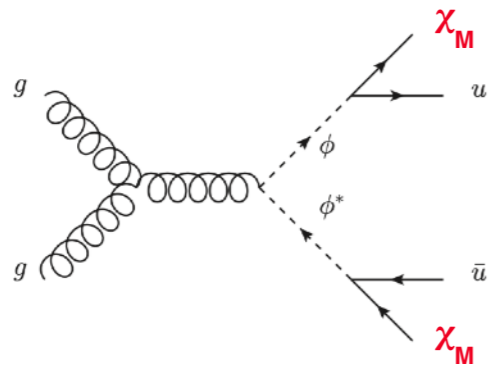
➔ **Undetectable in LHC**, maybe possible in HL-LHC.

Displaced vertices search in multijet events [CMS 1803.03078]:



A **meta-stable** B-violating particle [χ_M -like particle]

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coloured heavy scalar

Meta-stable fermion

- **A early matter-dominated (EMD) Universe?**

TeV dark freeze-out at $t \sim 10^{-10}$ sec, and χ_M **may dominate** later before BBN.

(leading to density dilution, which conserves Ω_B/Ω_{DM})

During EMD, the **sub-horizon density perturbations grow** linearly, at most:

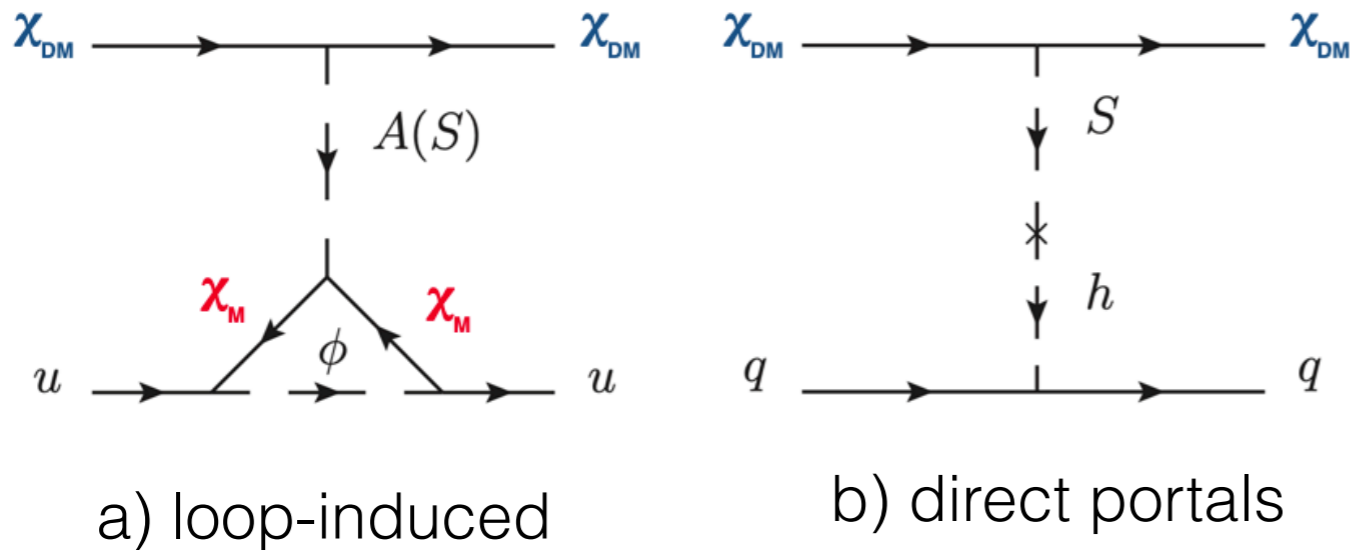
$$L_{\text{co-moving}} = \tau_M \left(\frac{s(T_{\text{EDM}})}{s(T_0)} \right)^{1/3} \approx 10^{-5} \sqrt{\frac{\tau_M}{0.02 \text{ s}}} \text{ Mpc},$$

which corresponds to $10^{-4} M_\odot$, and future Pulsar Timing Arrays may reach it [K.

Zurek et al 2005. 03030, 2012.09857, ...].

DM signals within concrete models

- DM direct detection:



a) suppressed by large intermediate scales

$$\sigma_{\chi N}^{\text{SI}} \sim \frac{f_N^2}{256\pi^5} \left[\frac{\alpha^2 m_M m_\chi m_N^2}{m_\phi^2 m_S^2 (m_\chi + m_N)} \right]^2$$

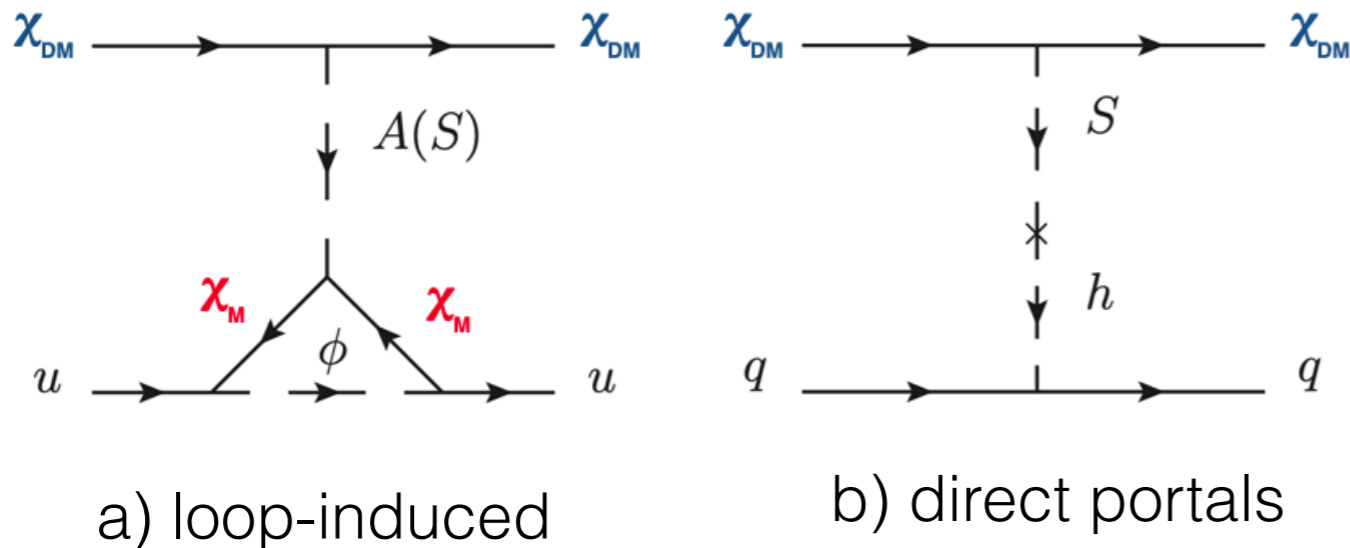
b) suppressed by small mixing

$$\sigma_{\chi N}^{\text{SI}} \sim 10^{-42} \theta_{Sh}^2 \text{ cm}^2$$

➡ **unlikely** for a decoupled sector.

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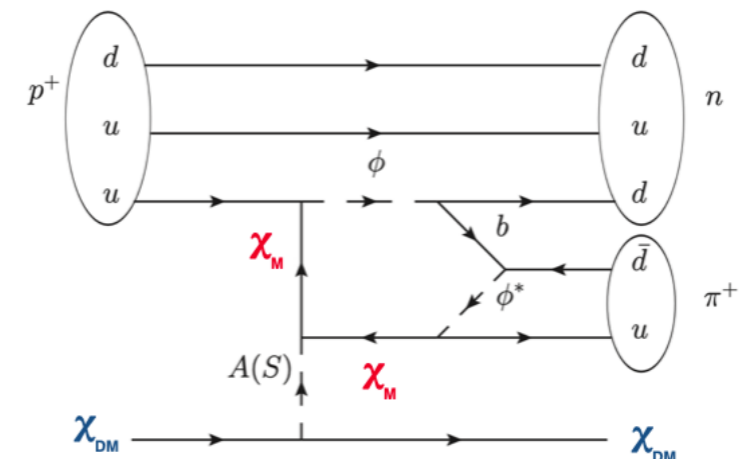
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➡ **unlikely** for a decoupled sector.

- Exotic signatures:

e.g. DM-induced **proton decay**

➡ Unlikely in the Local Group, maybe in neutron star, to be investigated [Huang&Zhao 1312.0011].



V. Conclusions

Conclusions

- **Standard cosmology**, including DM&BAU, is well established;
- The similar DM&BAU abundances: shared origin, coincidence, or anthropic principle?
- **For asymmetric DM, a shared origin** could be theoretically natural;
- **Symmetric DM** within co-genesis needs to be quantitatively explored.
- **Dark sector** naturally provides **suppressed wash-out** and/or **strong deviation** from SM thermal equilibrium.

Discovery of new physics will help 😊 [*+ muonic g-2, cosmic ray excesses, H0 tension, ...*].

Backup

Flavor violation [2111.03082]:

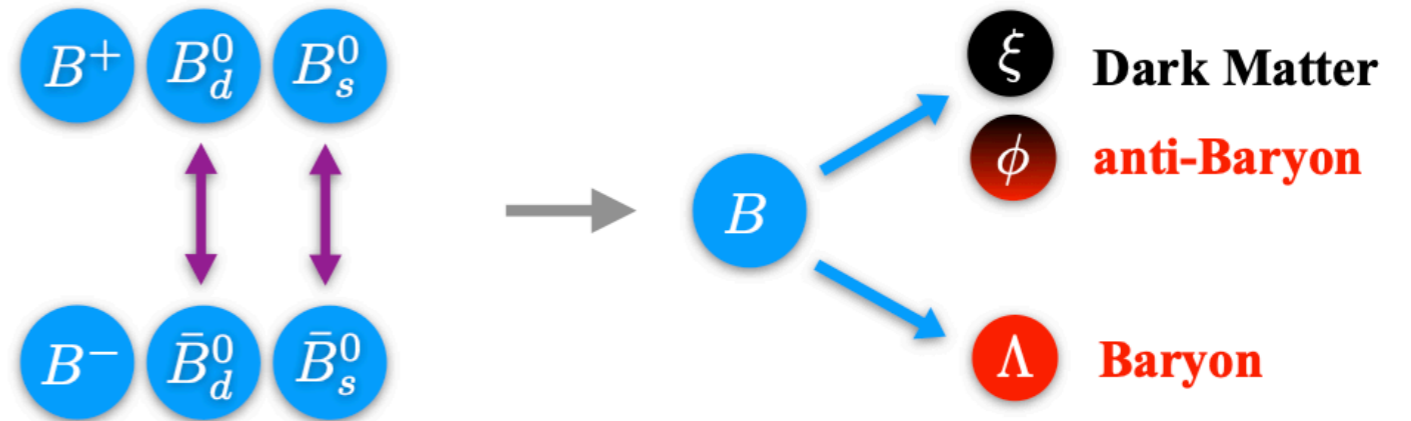
baryon asymmetry after sphaleron decoupling is given

$$Y_B \simeq \frac{3A(x_{\text{Sp}})}{13\pi^2} \sum_{f=e,\mu,\tau} y_f^2 Y_{\Delta_f},$$

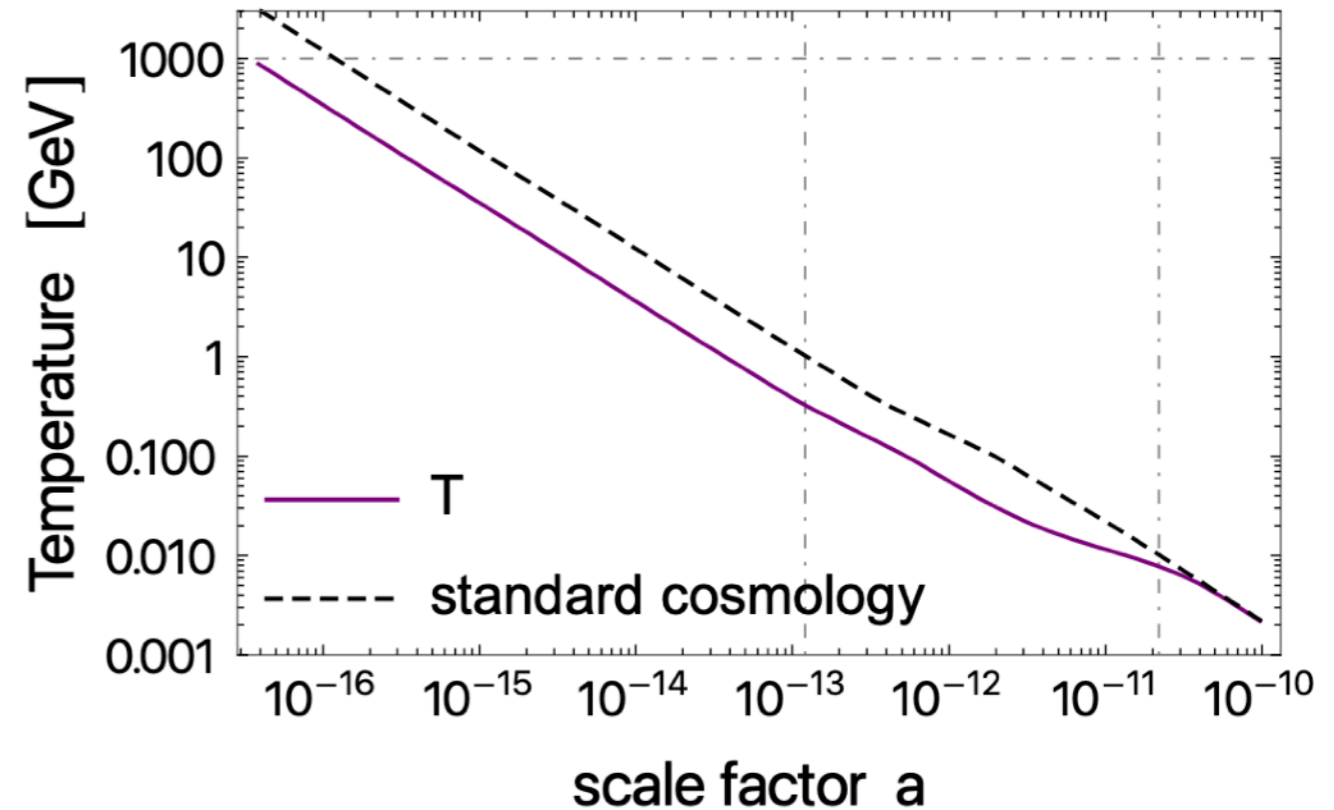
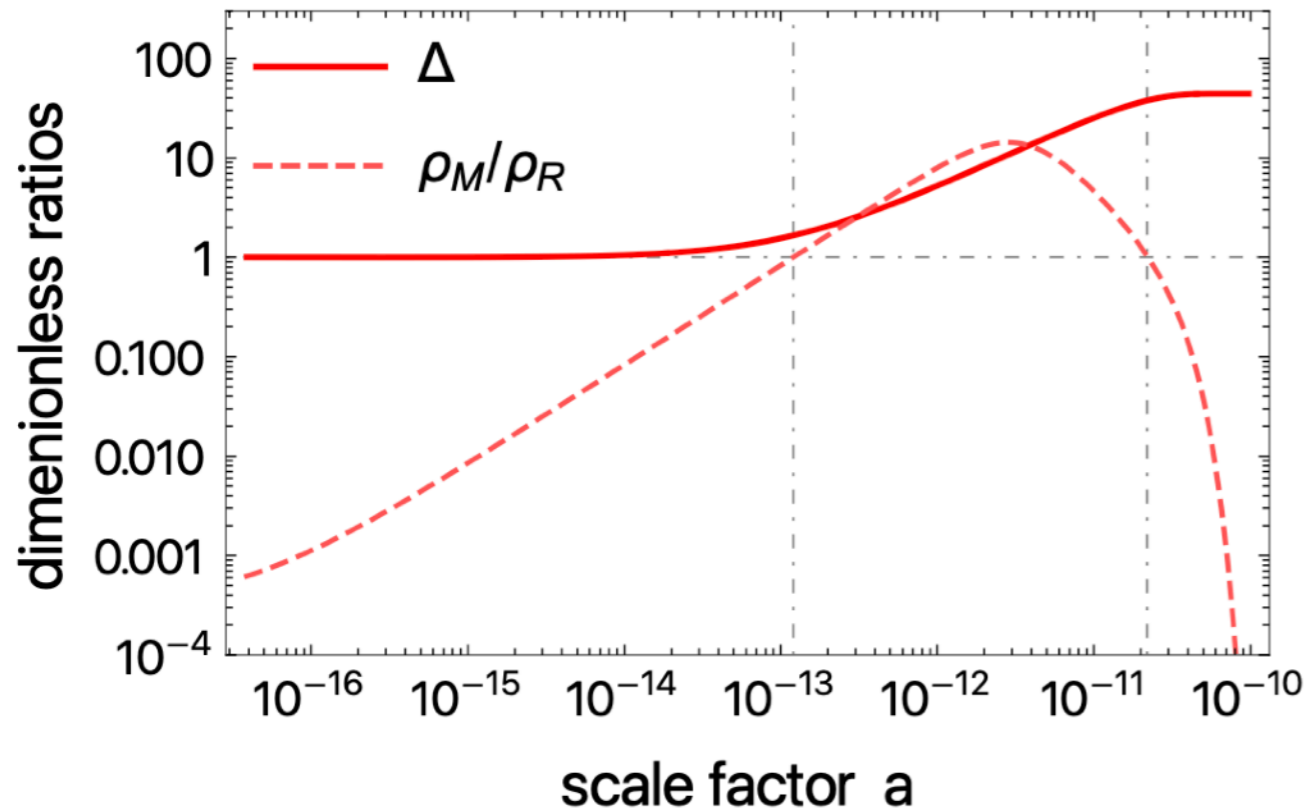
for vanishing total $B - L$, where

$$A(x) \equiv \frac{13(1034 + 2473x^2 + 792x^4)}{48(869 + 333x^2)}, \quad A(x_{\text{Sp}}) \simeq 1.3.$$

Mesogenesis [1810.00880, 2101.02706, 2109.09751,...]



Entropy dilution:

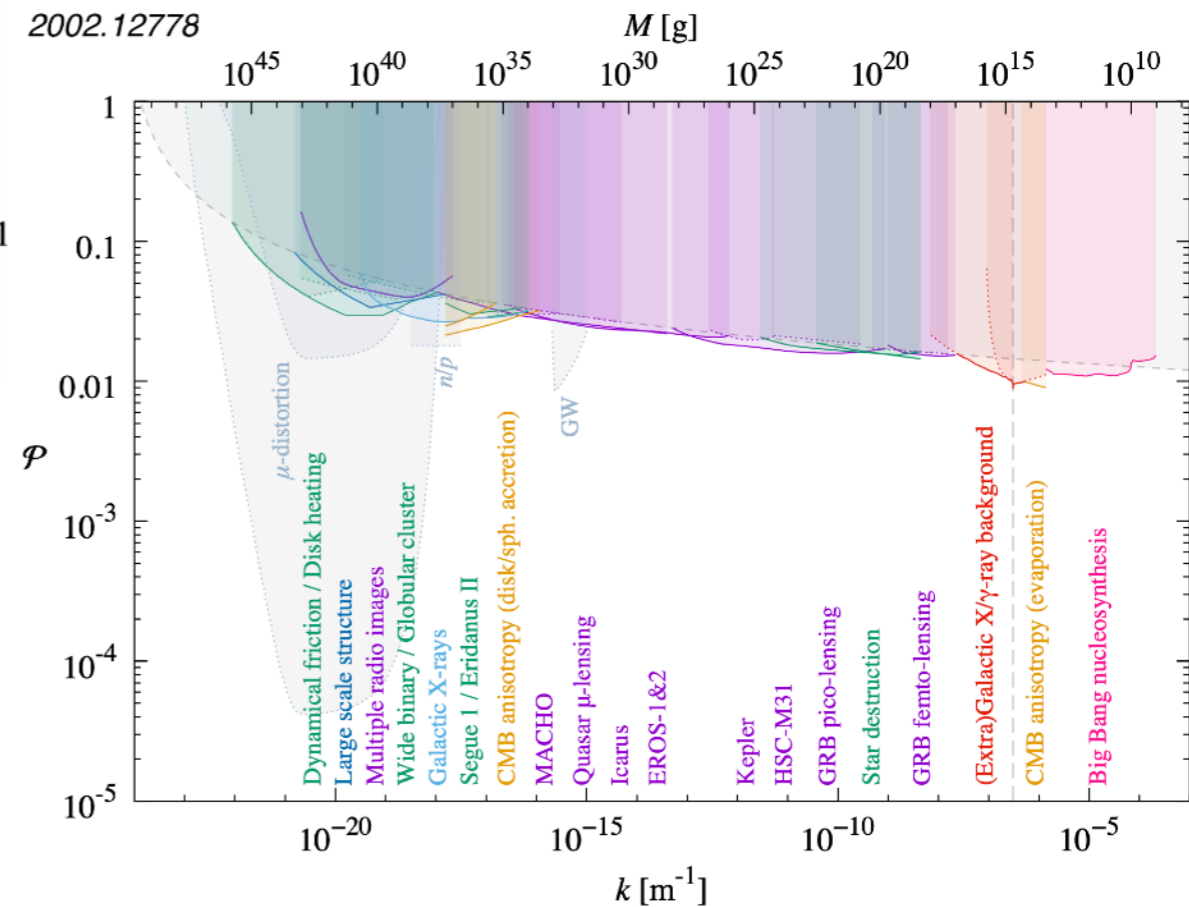
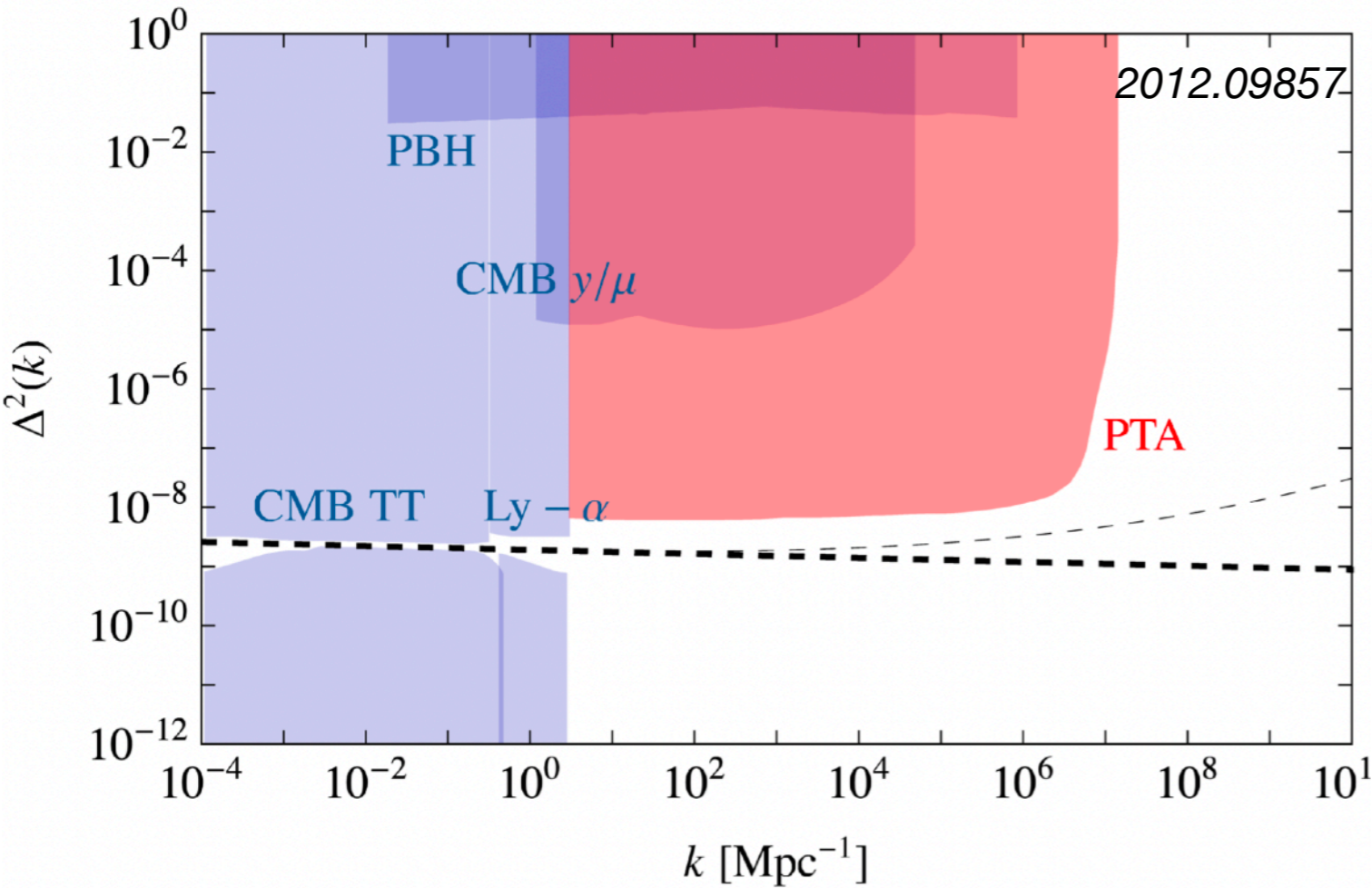


Sub-halo scale detection?

Still need the **halo-mass distributions** from *PTA, CTA, lensing, astrometry, stellar streams, ...*

Also probed by distortions in primordial GW in the far future.

[1804.01991, 1903.04218, 2002.08962, 2005.03030, 2009.06639, 2012.09857]



- **Astrometry** from Nancy Grace Roman Space Telescope [2108.10886]