

# Quantization of Constantly Curved Tetrahedron

*Monday 6 May 2024 17:00 (15 minutes)*

In this talk, we develop a quantum theory of homogeneously curved tetrahedron geometry, by applying the combinatorial quantization to the phase space of tetrahedron shapes defined in arXiv:1506.03053. Our method is based on the relation between this phase space and the moduli space of  $SU(2)$  flat connections on a 4-punctured sphere. The quantization results in the physical Hilbert space as the solution of the quantum closure constraint, which quantizes the classical closure condition  $M_4 M_3 M_2 M_1 = 1$ ,  $M_i \in SU(2)$ , for the homogeneously curved tetrahedron. The quantum group  $U_q(\mathfrak{su}(2))$  emerges as the gauge symmetry of a quantum tetrahedron. The physical Hilbert space of the quantum tetrahedron coincides with the Hilbert space of 4-valent intertwiners of  $U_q(\mathfrak{su}(2))$ . In addition, we define the area operators quantizing the face areas of the tetrahedron and compute the spectrum. The resulting spectrum is consistent with the usual Loop-Quantum-Gravity area spectrum in the large spin regime but is different for small spins. This work closely relates to 3+1 dimensional Loop Quantum Gravity in presence of cosmological constant and provides a justification for the emergence of quantum group in the theory.

**Author:** HSIAO, Chen Hung (FAU - Florida)

**Presenter:** HSIAO, Chen Hung (FAU - Florida)

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