

# Lessons from the bygone anomalies: From Data to Models to Theories

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The Joint International Workshop on SM and Beyond 2024 &  
The 3rd Gordon Godfrey Workshop on Astroparticle Physics  
UNSW, Sydney, Dec 9-13 (2024)

# Two Ways to Interpret the Data

**EFT & Simplified Models vs.  
(The Simplest) UV Completions**

# Many Bygone Anomalies

- Large FCNC ~ FCCC Weak Interactions before GIM
- Muon  $g-2$ , ATOMKI, MiniBooNE, ....
- CDF  $W_{jj}$ , Top FBA, 750 GeV diphoton,
- DM related ones: 511 keV  $\gamma$  ray excess, PAMELA  $e^+$  excess, Galactic Center  $\gamma$  ray excess, XENON1T, ....

# Reappraisal of SM

# Current Status of SM

- Only Higgs ( $\sim$ SM) and Nothing Else so far at the LHC
- Yukawa & Higgs self couplings to be measured and tested
- Nature is described by Quantum Local Gauge Theories
- Unitarity and gauge invariance played key roles in development of the SM

# Building Blocks of SM

- Lorentz/Poincare Symmetry
- Local Gauge Symmetry : Gauge Group + Matter Representations from Exp's
- Higgs mechanism for masses of weak gauge bosons and SM chiral fermions
- These principles lead to unsurpassed success of the SM in particle physics

# Accidental Sym's of SM

- Renormalizable parts of the SM Lagrangian conserve baryon #, lepton # : broken only by dim-6 and dim-5 op's  $\longrightarrow$  "longevity of proton" and "lightness of neutrinos" becoming Natural Consequences of the SM (with conserved color in QCD)
- QCD and QED at low energy conserve P and C, and flavors
- In retrospect, it is strange that P and C are good symmetries of QCD and QED at low energy, since the LH and the RH fermions in the SM are independent objects
- What is the correct question ? "P and C to be conserved or not ?" Or "LR sym or not ?"

# How to do Model Building

- Specify local gauge sym, matter contents and their representations w/o any global sym
- Write down all the operators upto dim-4
- Check anomaly cancellation
- Consider accidental global symmetries
- Look for nonrenormalizable operators that break/conserves the accidental symmetries of the model

- If there are spin-1 particles, extra care should be paid : need an agency which provides mass to the spin-1 object
- Check if you can write Yukawa couplings to the observed fermion
- You may have to introduce additional Higgs doublets with new gauge interaction if you consider new chiral gauge symmetry (Ko, Omura, Yu on chiral U(1)' model for top FB asymmetry)
- Impose various constraints and study phenomenology

# Usual Approaches

- Introduce a minimal set of particles to explain anomalies
- Very often symmetry issues (SM gauge symmetry or new gauge/global symmetry) are ignored
- Very often nonrenormalizable operators are used, ignoring unitarity issues  $\longrightarrow$  can produce incorrect results, especially for DM productions at high energy colliders
- **Unitarity and Gauge invariance: most important**

# Motivations for BSM

# Pheno'cal Motivations

- Neutrino masses and mixings

Leptogenesis

- Baryogenesis

- Inflation (inflaton)

Starobinsky & Higgs Inflation

?

- **Nonbaryonic DM**

Many candidates

- Origin of EWSB and Cosmological Const ?

Can we attack these problems ?

# Theoretical Motivations

- Fine tuning problem of Higgs mass parameter : SUSY, RS, ADD, etc.
- Critical comments in the Les Houches Lecture by Aneesh Manohar (arXiv:1804.05863)
- Standard arguments :
  - Electron self-energy in classical E&M vs. QED
  - $\Delta m_K$  without/with charm quark
  - $\Delta m^2 = m_{\pi^\pm}^2 - m_{\pi^0}^2$  without/with  $\rho$  mesons
  - These arguments are simply wrong !

# My Personal Viewpoints

- Traditionally Fine Tuning or Naturalness problem was the driving force for many BSM, and predicted many signatures @ LHC
- No signatures @ LHC means that the traditional motivation is not that well motivated
- Mathematical and Theoretical Consistency : more important for BSM model buildings
- Unitarity is one of the Holy Grails in EFT approach

**Anomaly Free :  
before/after GIM**

# Before GIM

- Weinberg Model for u,d,s :  
 $(u_L, d_L \cos \theta_c + s_L \sin \theta_c)^T, u_R, d_R, s_R,$
- Predicts FCNC  $\sim$  FCCC :  
 $\Gamma(K^+ \rightarrow \mu^+ \nu_\mu) \sim \Gamma(K^0 \rightarrow \mu^+ \mu^-)$  , in  
contradiction to the exp data. What is going on ?
- Where is another combination,  
 $(-d_L \sin \theta_c + s_L \cos \theta_c)$  ?

# GIM (1970)

- GIM proposed to introduce the 4th quark, “charm”, as the SU(2) partner of the 2nd combination
- FCNC=0 @ tree level, and induced at loops
- $m_c \sim 1.5$  GeV explains  $\Delta m_K$  (Gaillard, Lee, Rosner, 1974), and confirmed by discovery of  $J/\psi$  in 1974 !
- In retrospect, large FCNC is a wrong prediction of anomalous gauge theory for 3 quark flavors, which is not a healthy theory

**Extra spin-1 requires extensions  
of the Higgs sector :  
Top FBA as an example**

# Contents

- EFT approach for Top FBA
- Phenomenological top FCNC from extra  $Z'$  with chiral interaction + Local gauge invariance : Multi-Higgs doublet models with chiral  $U(1)'$  : Ko-Omura-Yu Model
- Details of top FCNC, B decays and related issues
- EFT : Reappraisal and Caution

- In the usual EFT approach, one imposes only the SM gauge invariance (full or unbroken)
- If there are new spin-1 particle around, then one has to impose a new gauge symmetry on EFT operators
- Within EFT, some observables cannot be described without introducing additional sets of effective operators
- If we consider renormalizable and unitary models with local gauge invariance, one can study many different observables, although the results are model-dependent
- This approach is discussed in this talk in the context of top forward-backward asymmetry

**Top FBA@Tevatron and Top CA@LHC  
in chiral U(1)' models  
with flavored Higgs fields**

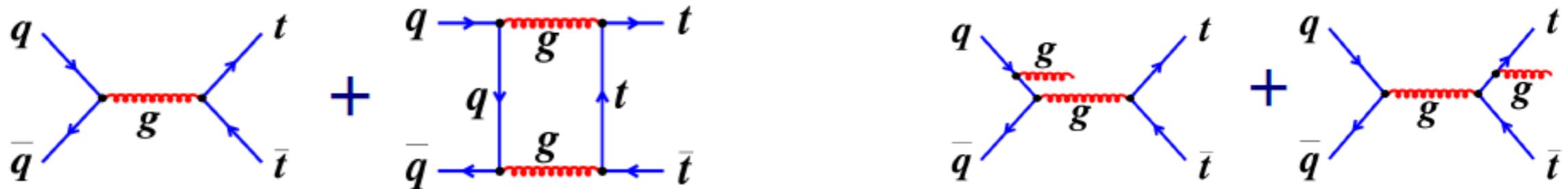
# Contents

- SM Prediction vs. Data
- Z' model for Top FBA
- Flavor dependent U(1)' model
- Conclusion & General Remarks

# Top Charge Asym in QCD (Muller@ICHEP2012)

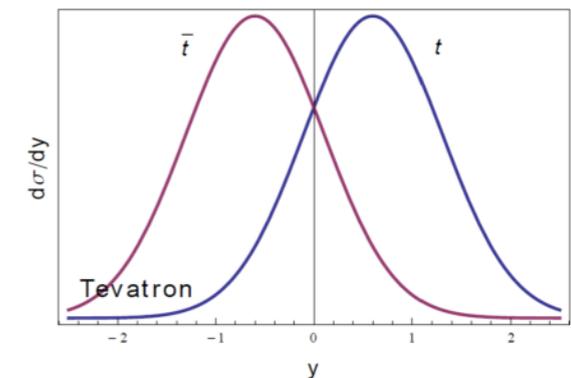
NLO QCD: interference of higher order diagrams leads to asymmetry for  $t\bar{t}$  produced through  $q\bar{q}$  annihilation:

- Top quark is emitted preferentially in direction of the incoming quark
- Antitop quark opposite
- Production through new processes may lead to different asymmetries



- At Tevatron: define forward-backward asymmetry

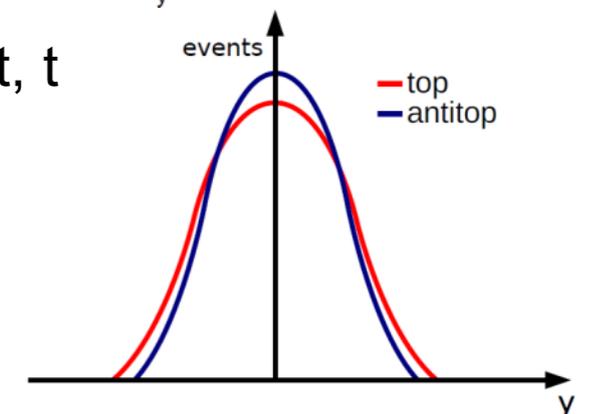
$$A^{t\bar{t}} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)}$$



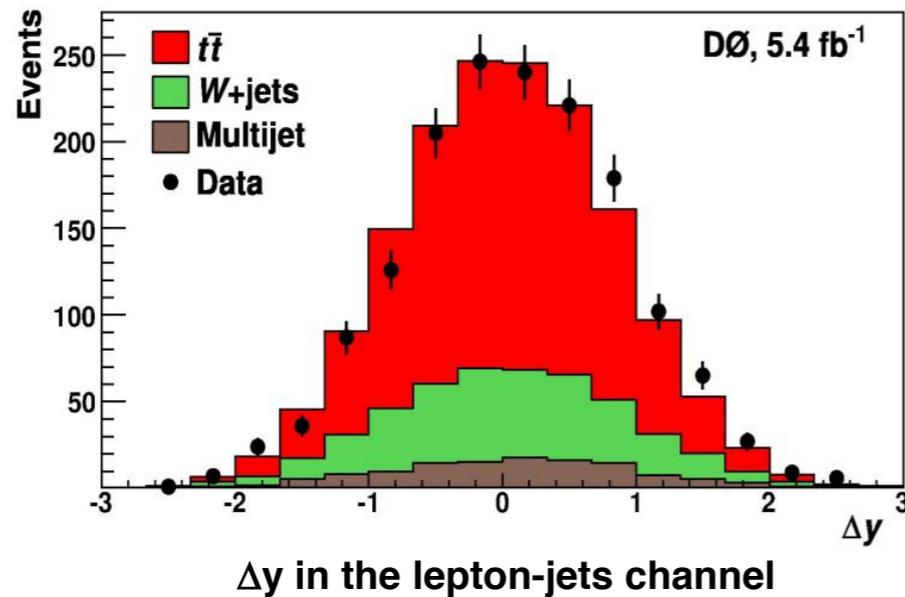
- At LHC: define asymmetry in the widths of rapidity distributions of  $t$ ,  $\bar{t}$

$$A_C = \frac{N(\Delta |y| > 0) - N(\Delta |y| < 0)}{N(\Delta |y| > 0) + N(\Delta |y| < 0)}$$

$$\Delta |y| = |y_t| - |y_{\bar{t}}|$$



# ICHEP 2012 : Top FBA (Muller's talk)



Measured asymmetry on detector level after bkg subtraction:

$$A_{FB} \text{ det} = 0.092 \pm 0.037 \text{ (stat+syst)}$$

$$\text{MC@NLO: } A_{FB} \text{ det} = 0.024 \pm 0.007$$

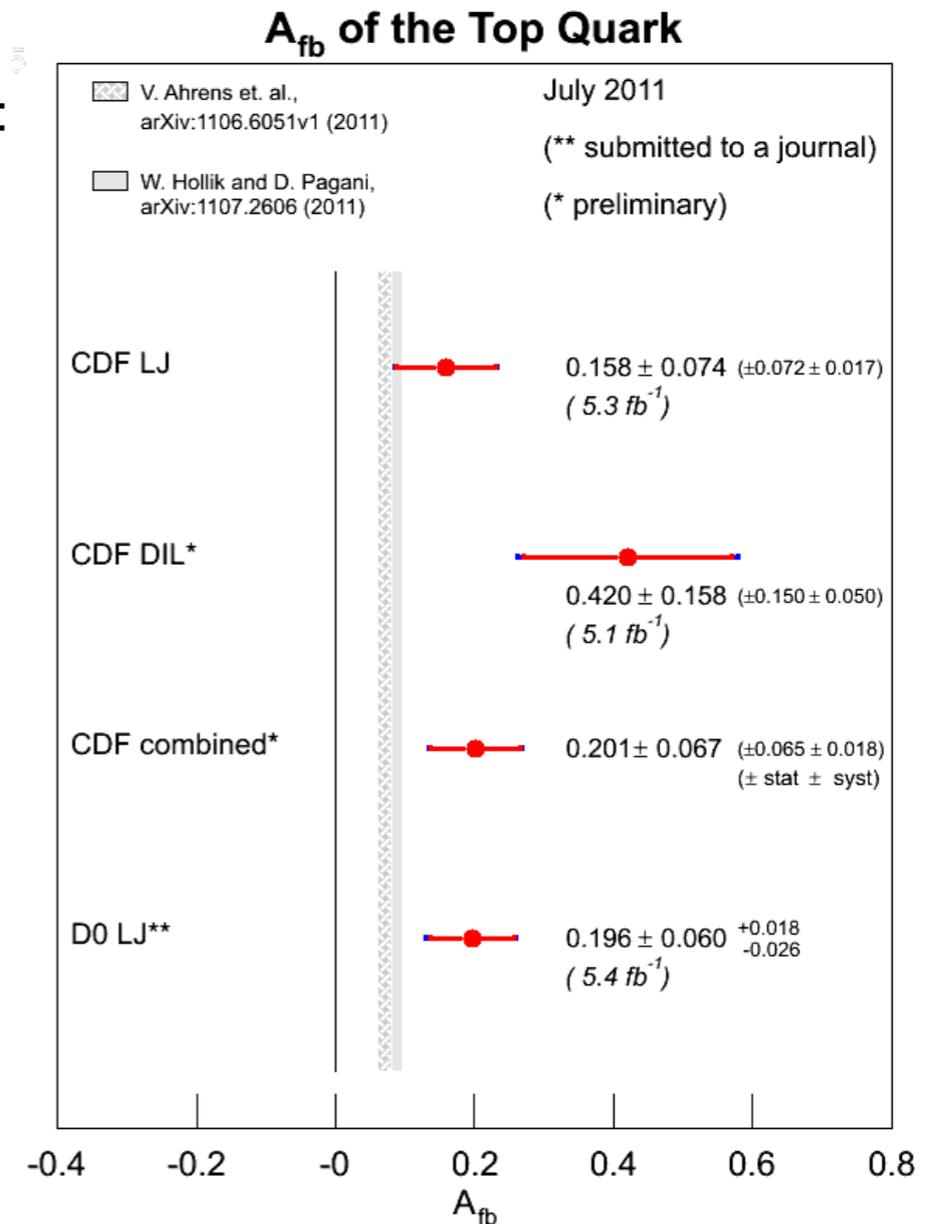
Measured asymmetry on parton level:

$$A_{FB} = 0.196 \pm 0.065 \text{ (stat+syst)}$$

D0 results in the di-lepton channel:

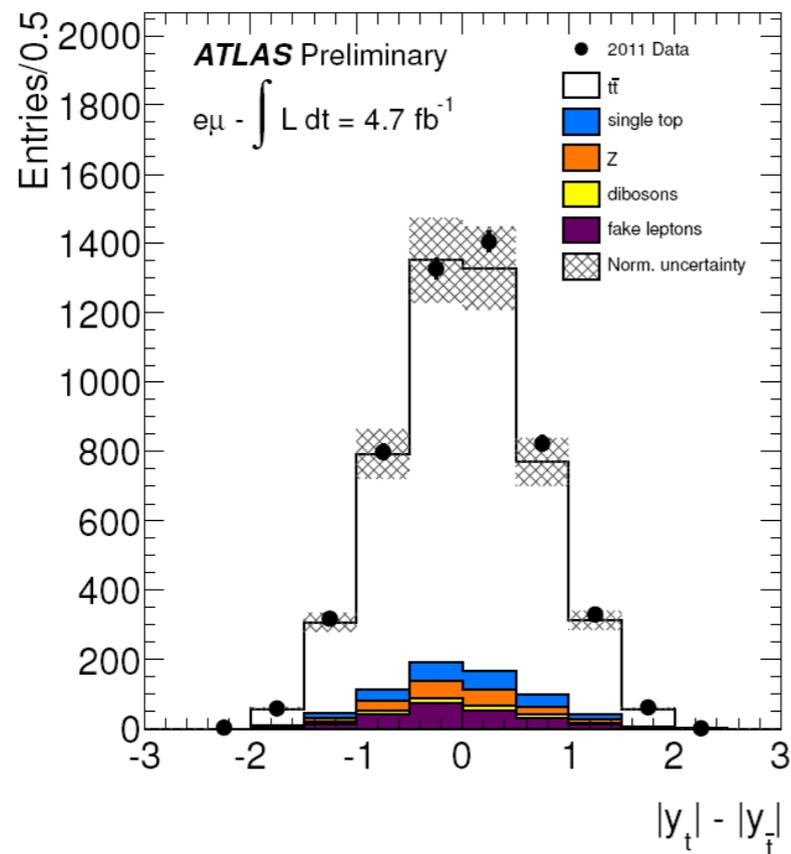
$$A_{FB} = 0.118 \pm 0.032$$

Summary:

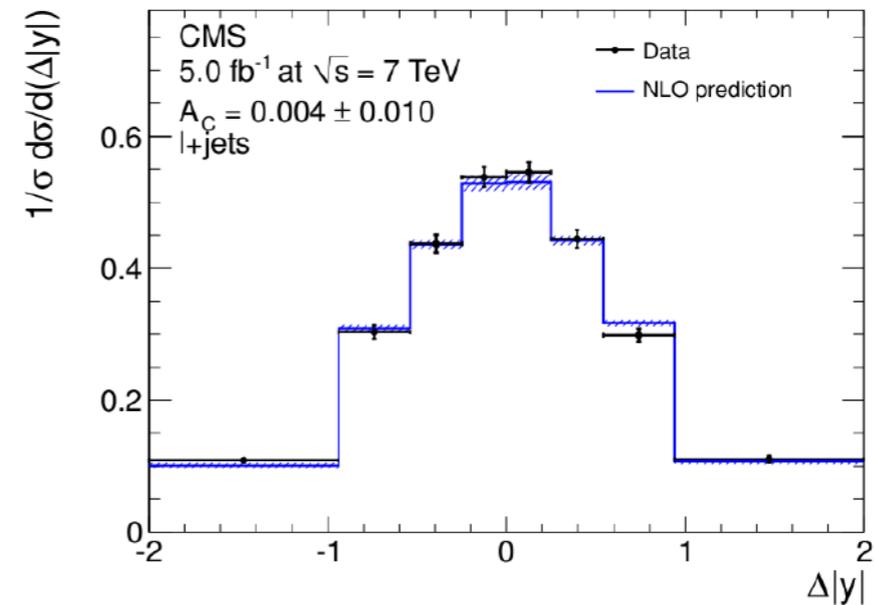


Both CDF and D0 see significant asymmetry in  $t\bar{t}$  production in all channels with strong dependence on  $m_{t\bar{t}}$ , in conflict with the SM

# ICHEP 2012 : Top C Asym (Muller's talk)



**ATLAS-CONF-2012-057**



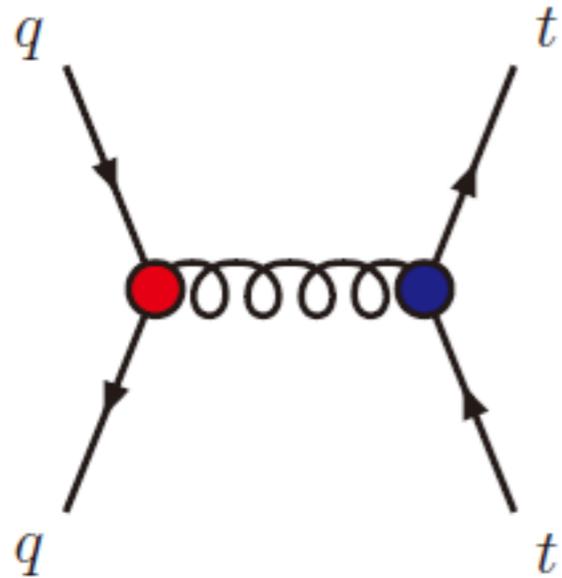
**CMS PAPER TOP-11-030**

● ATLAS:  $A_C = 0.029 \pm 0.018 \text{ (stat.)} \pm 0.014 \text{ (syst.)}$

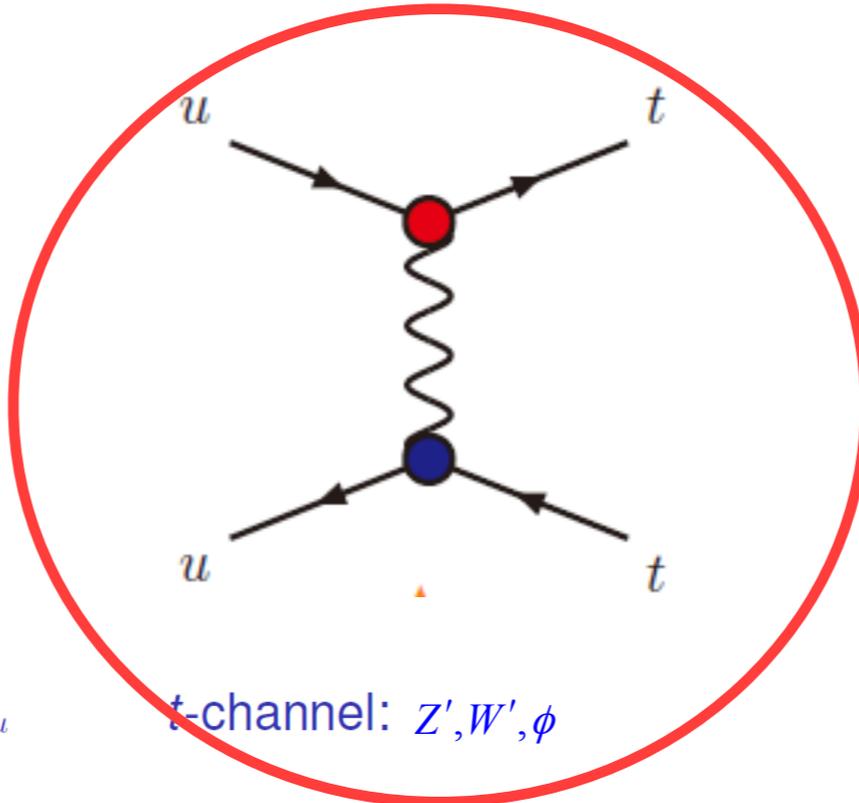
● CMS: Corrected:  $A_C = 0.004 \pm 0.010 \text{ (stat.)} \pm 0.011 \text{ (syst.)}$

● Theory (Kühn, Rodrigo):  $A_C = 0.0115 \pm 0.0006$

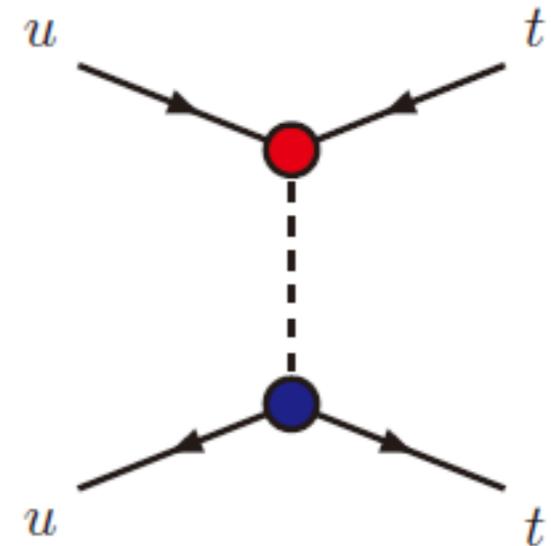
# New physics models for top $A_{FB}$



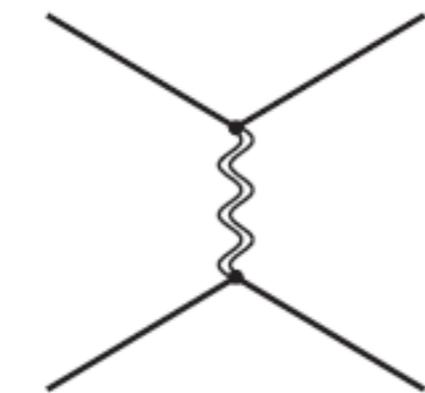
s-channel: coloured resonance  $\mathcal{G}_\mu$



t-channel:  $Z', W', \phi$

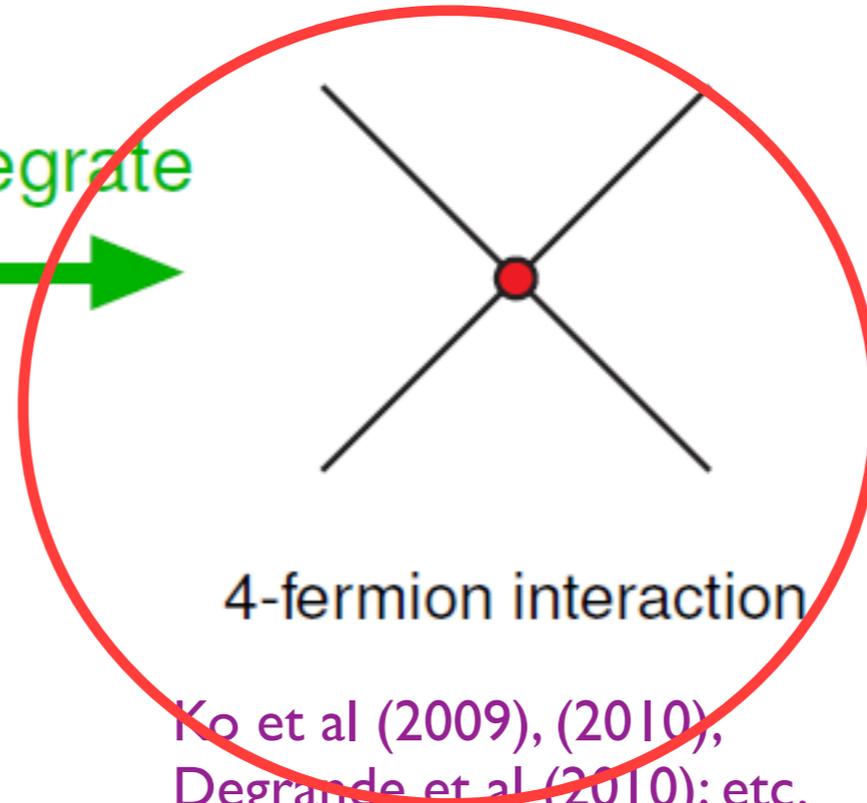


u-channel: exotic scalars



(new) heavy VB

Integrate



4-fermion interaction

Ko et al (2009), (2010),  
Degrande et al (2010); etc.

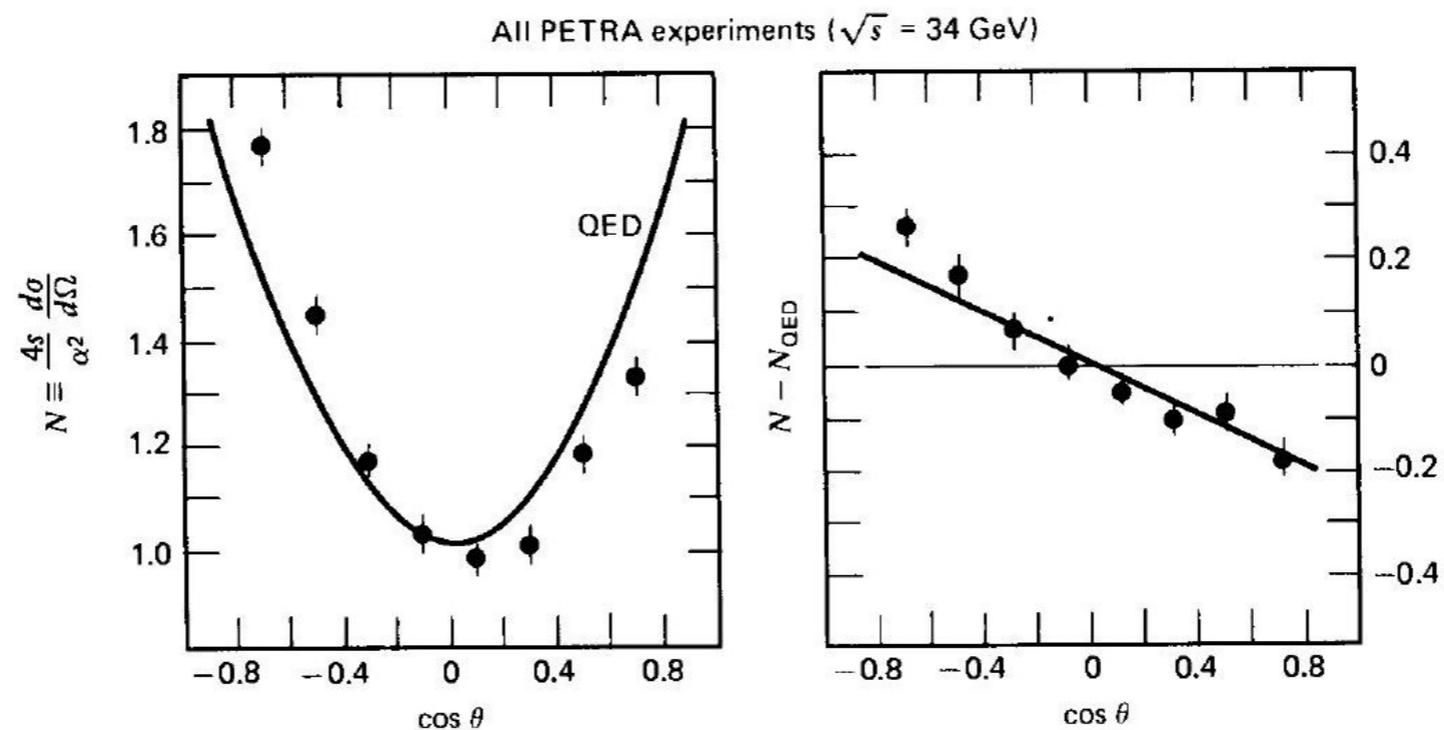
- flavor dependent.
- challenging to construct a realistic model.
  - anomaly free, renormalizable, and realistic Yukawa couplings.

# EFT Approaches

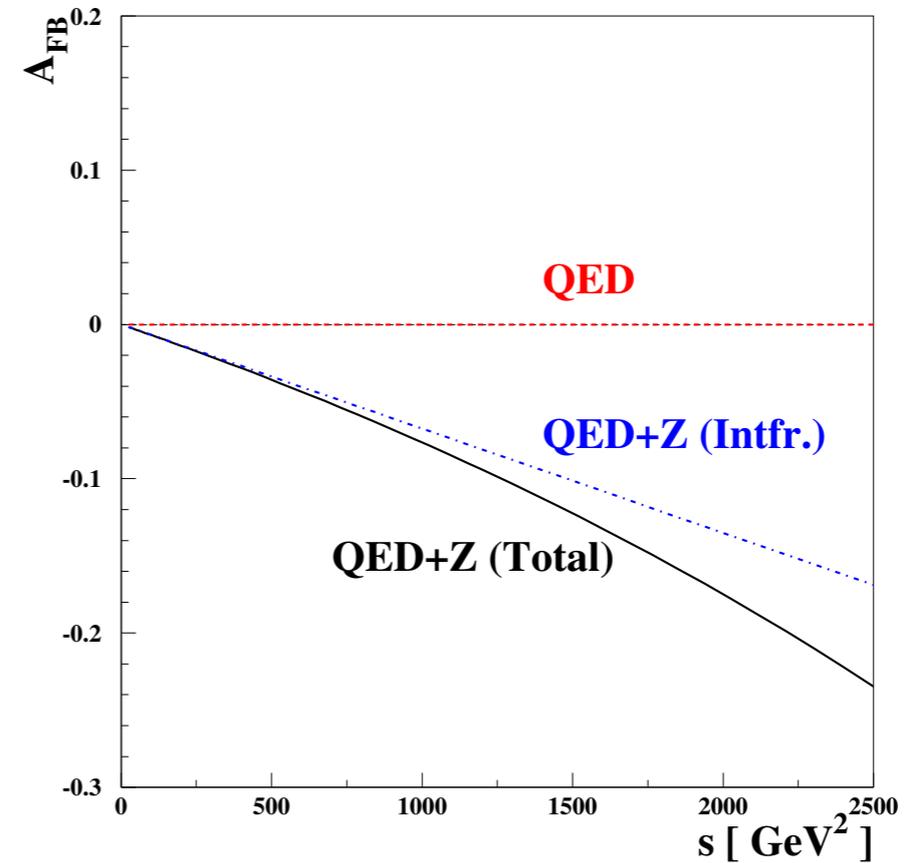
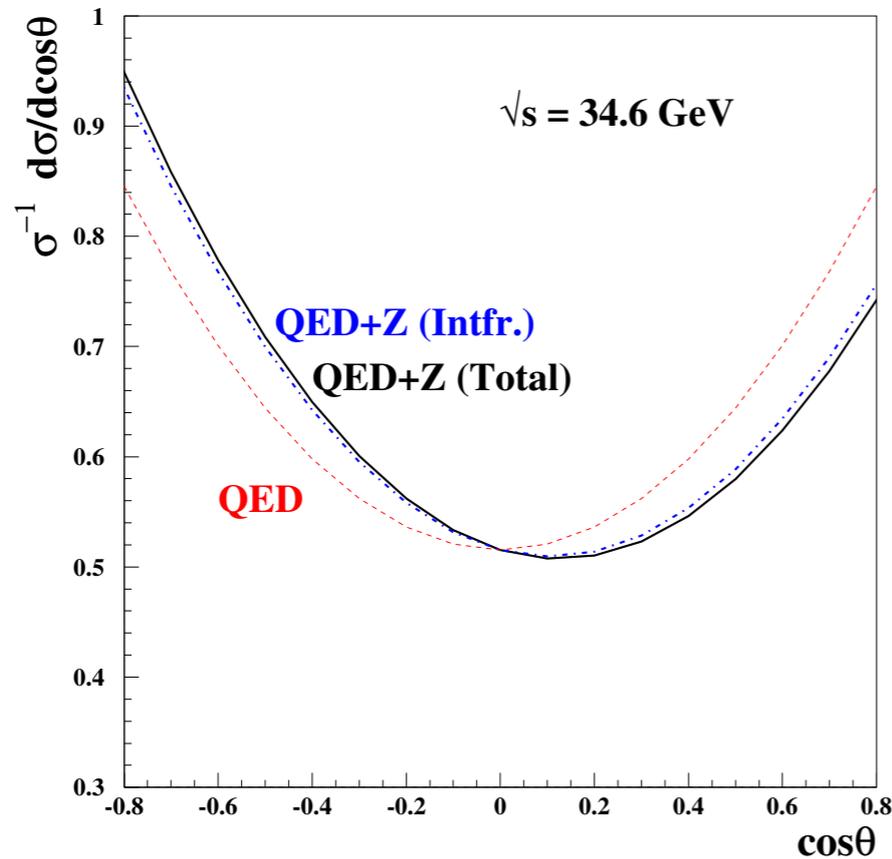
Based on arXiv:0912.1105 (PLB)  
arXiv:1011.5976 (PLB)  
arXiv:1104.4443 (PRD)  
with Dong Won Jung, Jae Sik Lee  
(and Su Hyun Nam)

# Wisdom from EW Physics

- The first evidence of asymmetry was found in angular distribution of muons from  $e^+e^-$  collisions at PETRA in the 80's ( $\sqrt{s} \sim 30$  GeV, well below the  $Z^0$  pole)



- Source of  $A_{FB}$  is a term linear in  $\cos \theta$  from interference between  $\gamma$  or  $Z$  vector coupling and the axial vector  $Z$  coupling.



- Since  $\sqrt{s} \ll M_Z$ , good approx. to assume 4 fermion interactions by integrating out  $Z$  boson
- $A_{\text{FB}} \simeq -\frac{3G_F}{\sqrt{2}} \frac{s}{4\pi\alpha} (g_L - g_R)^2 \equiv kG_F s$
- $k \simeq -7$  from EFT, whereas  $k = -5.78$  from the full expression

# Dim-6 Effective Op's

- $t\bar{t}$  production at the Tevatron dominated by  $q\bar{q}$  channel
- Enough to consider dimension-6 four-quark operators **assuming new physics scale is high enough**:

$$\mathcal{L}_6 = \frac{g_s^2}{\Lambda^2} \sum_{A,B} \left[ C_{1q}^{AB} (\bar{q}_A \gamma_\mu q_A) (\bar{t}_B \gamma^\mu t_B) + C_{8q}^{AB} (\bar{q}_A T^a \gamma_\mu q_A) (\bar{t}_B T^a \gamma^\mu t_B) \right]$$

where

$$T^a = \lambda^a / 2, \quad \{A, B\} = \{L, R\}, \quad L, R \equiv (1 \mp \gamma_5) / 2 \quad (q = u, d, s, c, b)$$

- Other d=6 operators are all reducible to the above operators after Fierzing (Hill and Parke 1994)
- We ignore flavor changing dim-6 operators such as  $\bar{d}_R \gamma^\mu s_R \bar{t}_R \gamma_\mu t_R$ , since those contributions to the  $t\bar{t}$  production cross section will be of a order  $1/\Lambda^4$

# (Helicity Amp)<sup>2</sup>

- The squared helicity amplitude is given by

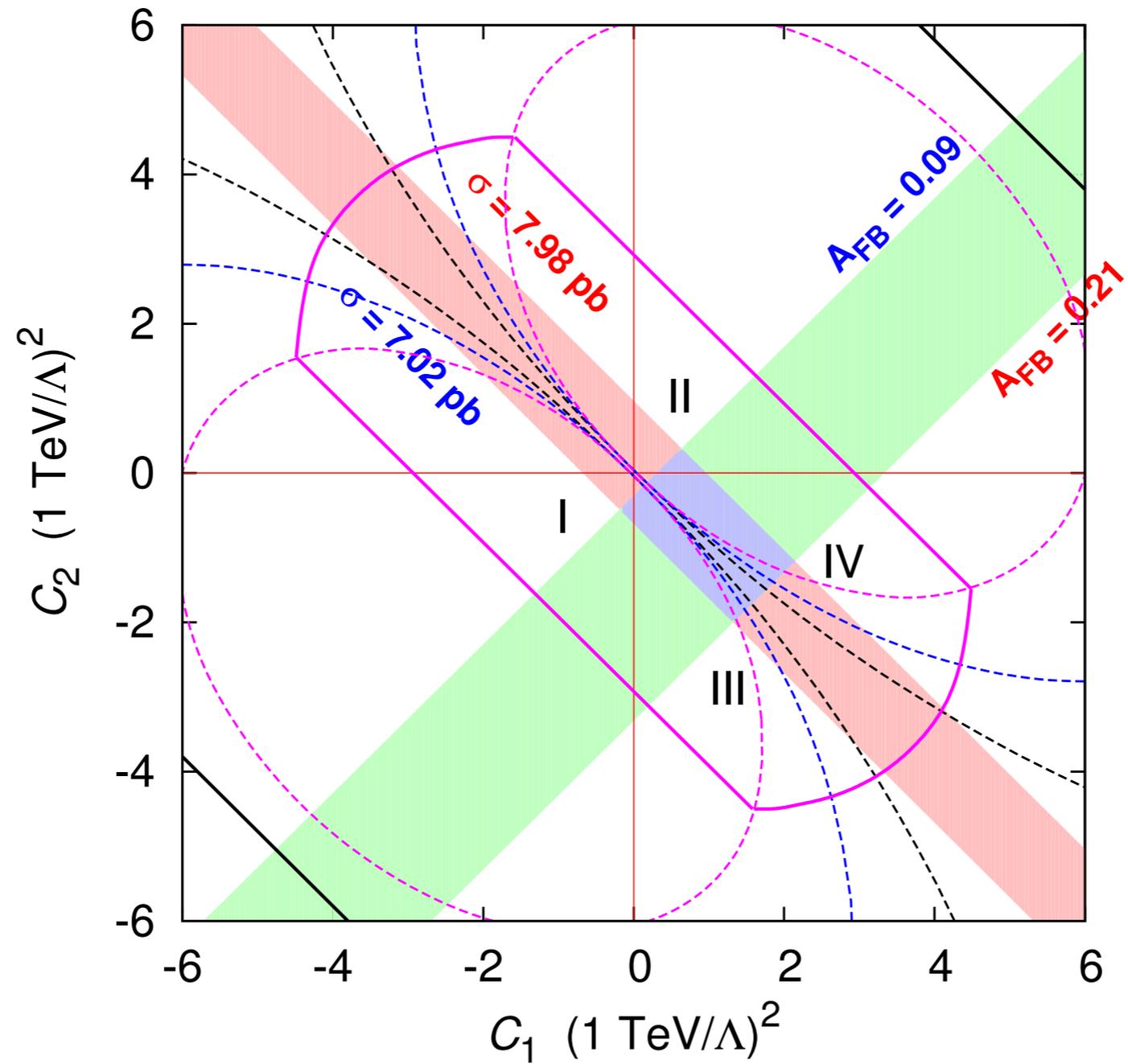
$$\begin{aligned} \overline{|\mathcal{M}(t_L \bar{t}_L + t_R \bar{t}_R)|^2} &= \frac{4 g_s^4}{9 \hat{s}} m_t^2 \left[ 2 + \frac{\hat{s}}{\Lambda^2} (C_1 + C_2) \right] s_{\hat{\theta}}^2 \\ \overline{|\mathcal{M} t_L \bar{t}_R + t_R \bar{t}_L|^2} &= \frac{2 g_s^4}{9} \left[ \left( 1 + \frac{\hat{s}}{2\Lambda^2} (C_1 + C_2) \right) (1 + c_{\hat{\theta}}^2) \right. \\ &\quad \left. + \hat{\beta}_t \left( \frac{\hat{s}}{\Lambda^2} (C_1 - C_2) \right) c_{\hat{\theta}} \right] \end{aligned}$$

where

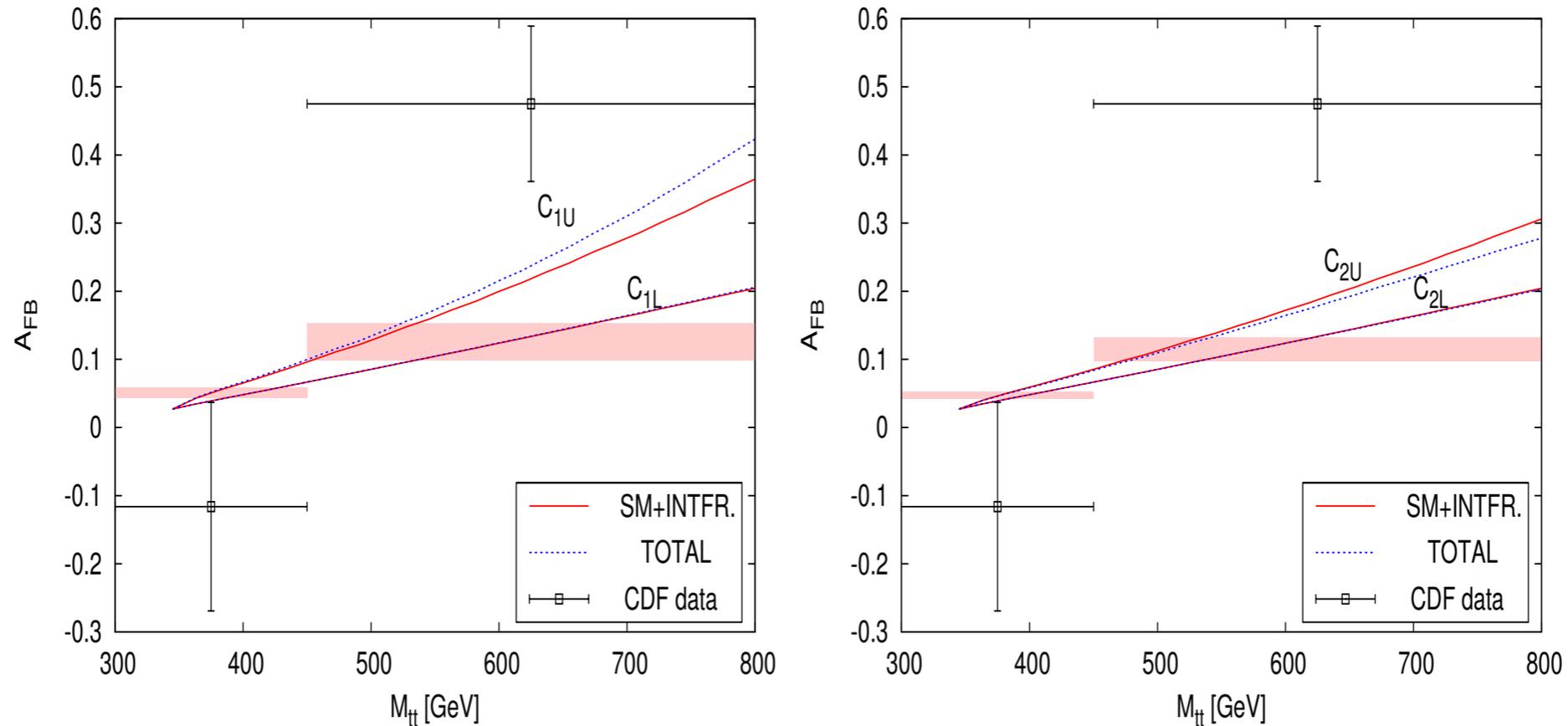
$$\begin{aligned} C_1 &\equiv C_{8q}^{LL} + C_{8q}^{RR}, & C_2 &\equiv C_{8q}^{LR} + C_{8q}^{RL} \\ \hat{\beta}_t^2 &= 1 - 4m_t^2/\hat{s}, & s_{\hat{\theta}} &\equiv \sin \hat{\theta}, & c_{\hat{\theta}} &\equiv \cos \hat{\theta} \end{aligned}$$

- The term linear in  $\cos \hat{\theta}$  could generate the forward-backward asymmetry which is proportional to  $\Delta C \equiv C_1 - C_2$ .

# Favored Region



# AFB as functions of $M(t\bar{t})$



**Figure:** Top FB asymmetry as functions of  $M_{t\bar{t}}$ . In the left frames we are taking  $C_1$  in the range between  $C_{1L} = 0.15$  and  $C_{1U} = 0.97$  with  $C_2 = 0$ . In the right frames, we vary  $C_2$  in the range between  $C_{2L} = -0.15$  and  $C_{2U} = -0.67$  with  $C_1 = 0$ .

# Spin-1 Resonances

- One can consider the following interactions of quarks with spin-1 flavor-conserving (changing) color-singlet  $V_1$  ( $\tilde{V}_1$ ) and color-octet  $V_8^a$  ( $\tilde{V}_8^a$ ) vectors ( $A = L, R$ ) relevant to  $A_{FB}^t$ :

$$\begin{aligned}
 \mathcal{L}_V = & g_s V_1^\mu \sum_A \left[ g_{1q}^A (\bar{q}_A \gamma_\mu q_A) + g_{1t}^A (\bar{t}_A \gamma_\mu t_A) \right] \\
 & + g_s V_8^{a\mu} \sum_A \left[ g_{8q}^A (\bar{q}_A \gamma_\mu T^a q_A) + g_{8t}^A (\bar{t}_A \gamma_\mu T^a t_A) \right] \\
 & + g_s \left[ \tilde{V}_1^\mu \sum_A \tilde{g}_{1q}^A (\bar{t}_A \gamma_\mu q_A) + \tilde{V}_8^{a\mu} \sum_A \tilde{g}_{8q}^A (\bar{t}_A \gamma_\mu T^a q_A) + \text{h.c.} \right]
 \end{aligned}$$

# Spin-0 resonance

- Following interactions of quarks with spin-0 flavor-changing color-singlet  $\tilde{S}_1$  and color-octet  $\tilde{S}_8^a$  scalars could also contribute to  $A_{FB}^t$ :

$$\mathcal{L}_{\tilde{S}} = g_s \left[ \tilde{S}_1 \sum_A \tilde{\eta}_{1q}^A (\bar{t} A q) + \tilde{S}_8^a \sum_A \tilde{\eta}_{8q}^A (\bar{t} A T^a q) + \text{h.c.} \right]$$

- One can also consider color-triplet  $S_k^\gamma$  and color-sextet scalars  $S_{ij}^{\alpha\beta}$  with minimal flavor violating interactions with the SM quarks (Arnold, Pospelov, Trott, Wise):

$$\mathcal{L}_S = g_s \left[ \frac{\eta_3}{2} \epsilon_{\alpha\beta\gamma} \epsilon^{ijk} u_{iR}^\alpha u_{jR}^\beta S_k^\gamma + \eta_6 u_{iR}^\alpha u_{jR}^\beta S_{ij}^{\alpha\beta} + \text{h.c.} \right]$$

# Wilson Coefficients

- After integrating out the heavy vectors and scalars, we obtain the Wilson coefficients as follows:

$$\begin{aligned}
 \frac{C_{8q}^{LL}}{\Lambda^2} &= -\frac{1}{m_V^2} g_{8q}^L g_{8t}^L - \frac{1}{m_{\tilde{V}}^2} \left[ 2|\tilde{g}_{1q}^L|^2 - \frac{1}{N_c} |\tilde{g}_{8q}^L|^2 \right] \\
 \frac{C_{8q}^{RR}}{\Lambda^2} &= -\frac{1}{m_V^2} g_{8q}^R g_{8t}^R - \frac{1}{m_{\tilde{V}}^2} \left[ 2|\tilde{g}_{1q}^R|^2 - \frac{1}{N_c} |\tilde{g}_{8q}^R|^2 \right] - \frac{|\eta_3|^2}{m_{S_3}^2} + \frac{2|\eta_6|^2}{m_{S_6}^2} \\
 \frac{C_{8q}^{LR}}{\Lambda^2} &= -\frac{1}{m_V^2} g_{8q}^L g_{8t}^R - \frac{1}{m_{\tilde{S}}^2} \left[ |\tilde{\eta}_{1q}^L|^2 - \frac{1}{2N_c} |\tilde{\eta}_{8q}^L|^2 \right] \\
 \frac{C_{8q}^{RL}}{\Lambda^2} &= -\frac{1}{m_V^2} g_{8q}^R g_{8t}^L - \frac{1}{m_{\tilde{S}}^2} \left[ |\tilde{\eta}_{1q}^R|^2 - \frac{1}{2N_c} |\tilde{\eta}_{8q}^R|^2 \right]
 \end{aligned}$$

# Scoreboard

New particle	couplings	$C_1$	$C_2$	1 $\sigma$ favor
$V_8$ (spin-1 FC octet)	$g_{8q,8t}^{L,R}$	indefinite	indefinite	✓
$\tilde{V}_1$ (spin-1 FV singlet)	$\tilde{g}_{1q}^{L,R}$	−	0	×
$\tilde{V}_8$ (spin-1 FV octet)	$\tilde{g}_{8q}^{L,R}$	+	0	✓
$\tilde{S}_1$ (spin-0 FV singlet)	$\tilde{\eta}_{1q}^{L,R}$	0	−	✓
$\tilde{S}_8$ (spin-0 FV octet)	$\tilde{\eta}_{8q}^{L,R}$	0	+	×
$S_3^\alpha$ (spin-0 FV triplet)	$\eta_3$	−	0	×
$S_6^{\alpha\beta}$ (spin-0 FV sextet)	$\eta_6$	+	0	✓

# Constraints

- 1- $\sigma$  favored values of the couplings **Updated data:**

$$\tilde{V}_8 : \frac{1}{N_c} \left( \frac{1 \text{ TeV}}{m_{\tilde{V}}} \right)^2 \left( |\tilde{g}_{8q}^L|^2 + |\tilde{g}_{8q}^R|^2 \right) \simeq 0.76(0.64),$$

$$\tilde{S}_1 : \left( \frac{1 \text{ TeV}}{m_{\tilde{S}}} \right)^2 \left( |\tilde{\eta}_{1q}^L|^2 + |\tilde{\eta}_{1q}^R|^2 \right) \simeq 0.62(0.49),$$

$$S_{13}^{\alpha\beta} : 2 \left( \frac{1 \text{ TeV}}{m_{S_6}} \right)^2 |\eta_6|^2 \simeq 0.76(0.64)$$

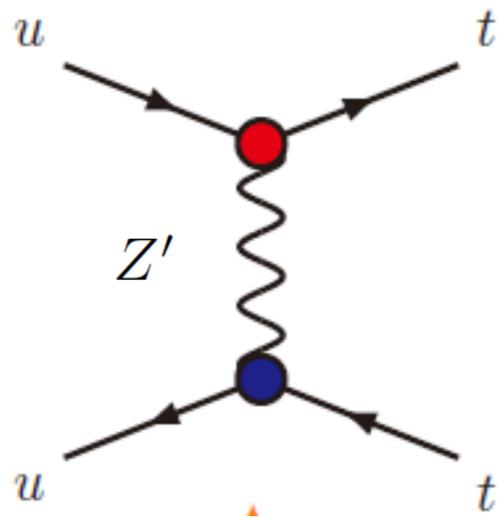
These could be discovered and tested at the LHC, by measuring the mass and the couplings

RG running effect studied in arXiv:1406.4570  
w/ S.Jung, YWYoon, C.Yu (2014)

# **Beyond EFT : Simplified (Pheno) Model**

# Z' model

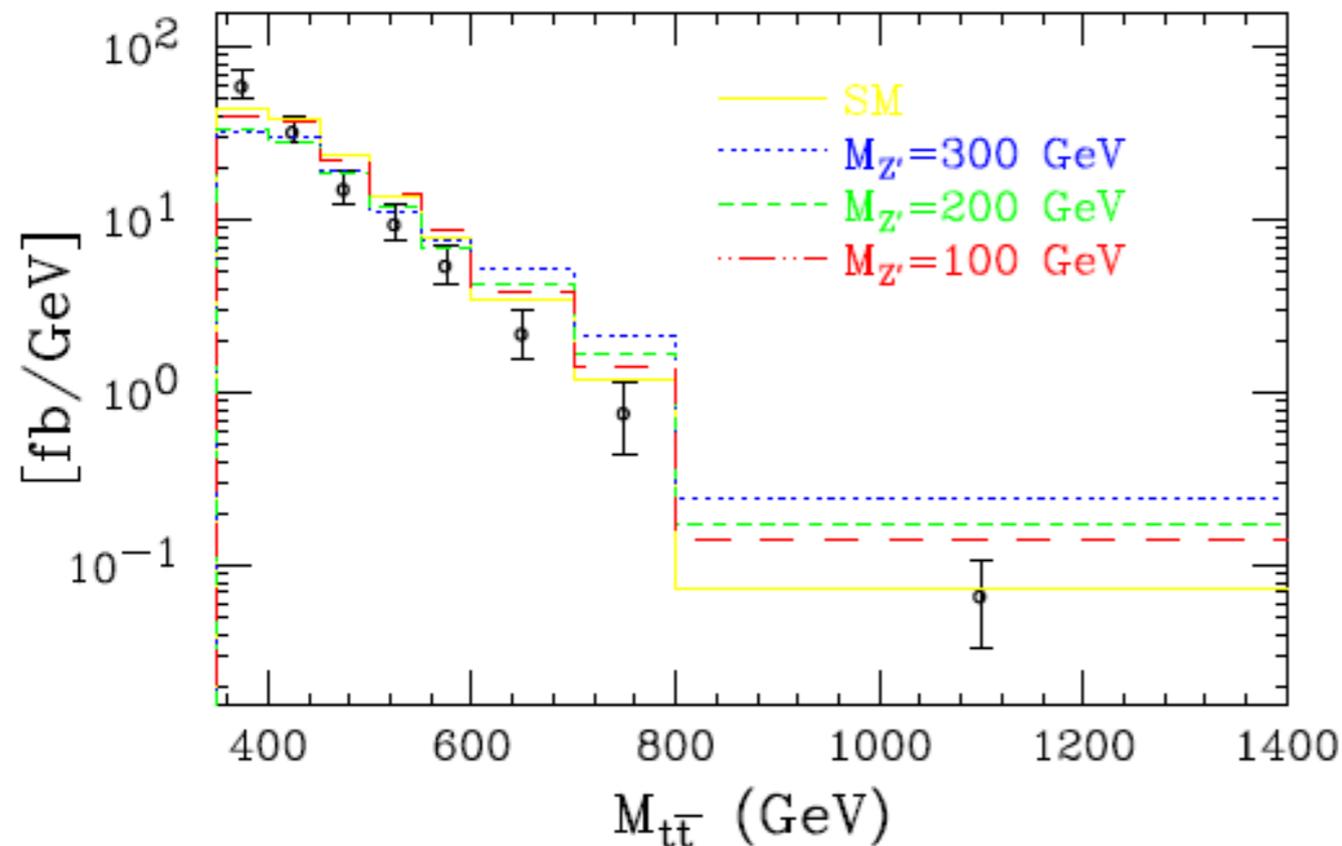
Jung, Murayama, Pierce, Wells, PRD81



- assume large flavor-offdiagonal coupling and small diagonal couplings.

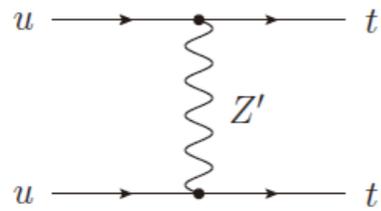
$$\mathcal{L} \ni g_X Z'_\mu \bar{u} \gamma^\mu P_R t + h.c.$$

- In general, could have different couplings to the top and antitop quarks.

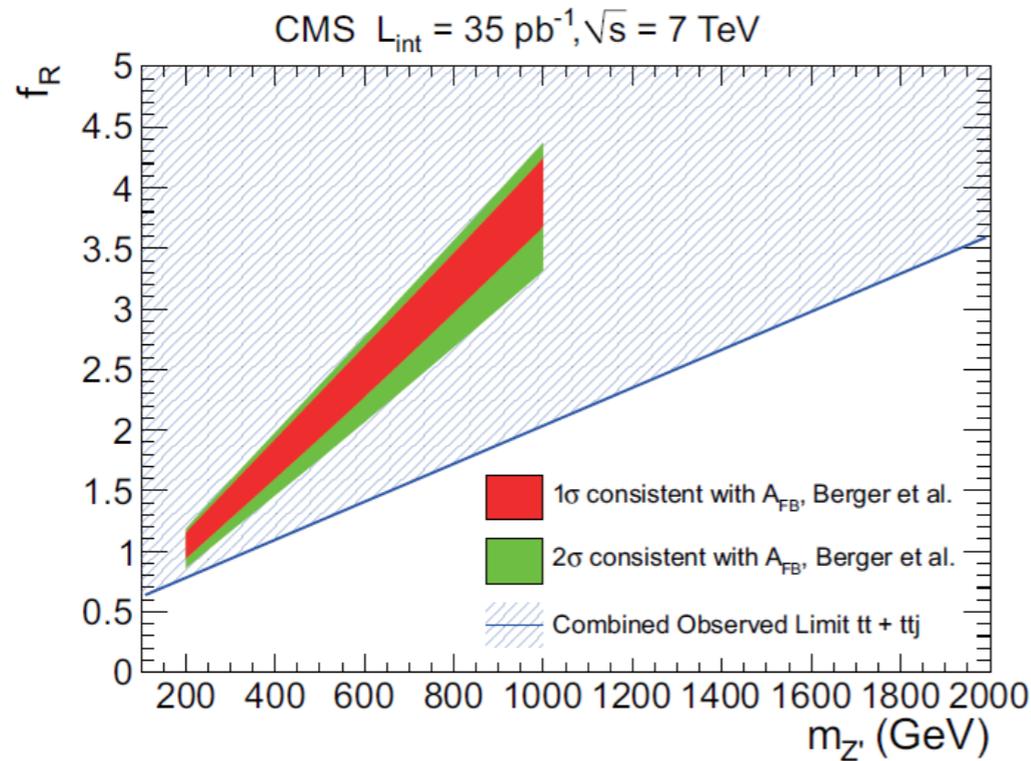


- light Z' is favored from the  $M_{t\bar{t}}$  distribution.
- severely constrained by the same sign top pair production.
  - the t-channel scalar exchange model has a similar constraint.

# Same sign top pair production at LHC



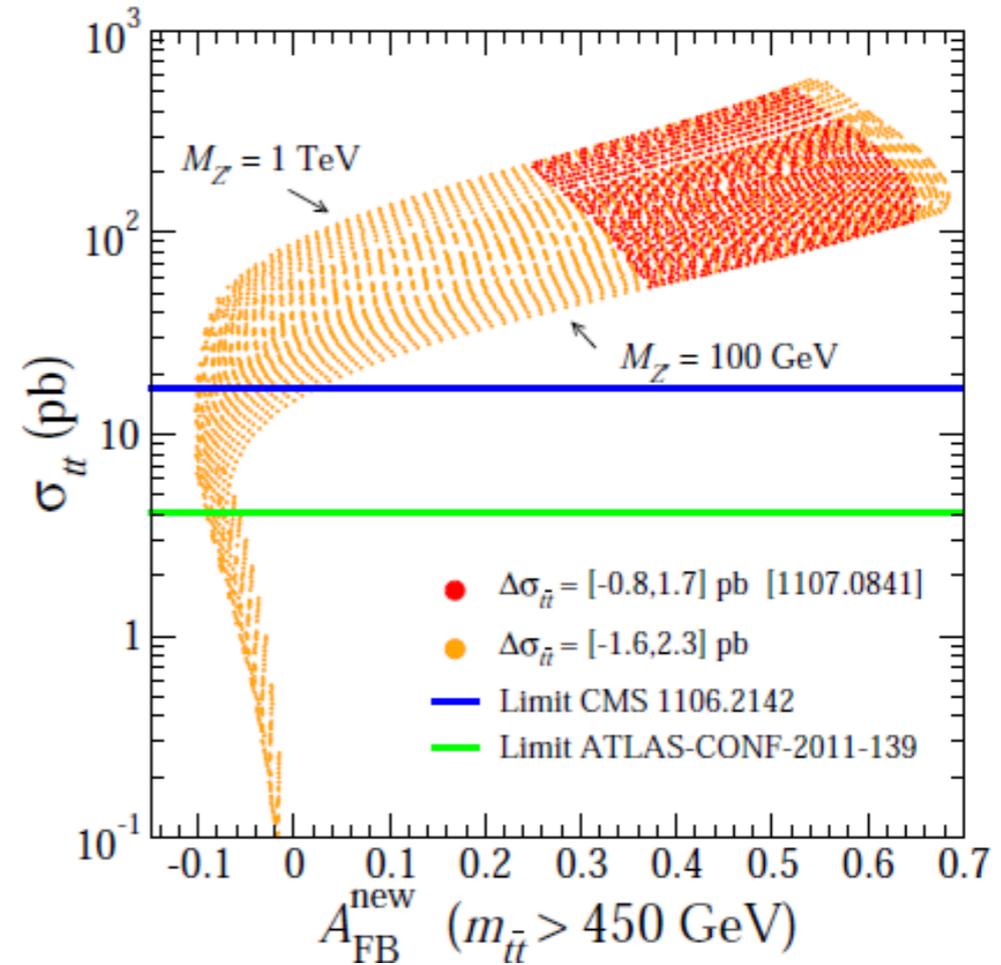
$$\mathcal{L} = g_W \bar{u} \gamma^\mu (f_L P_L + f_R P_R) t Z'_\mu + \text{h.c.},$$



CMS:  $\sigma(pp \rightarrow tt(j)) < 17 \text{ pb}$  at 95C.L.  
 ATLAS:  $\sigma(pp \rightarrow tt(j)) < 4 \text{ pb}$  at 95C.L.

CMS, JHEP1108; ATLAS-CONF-2011-169

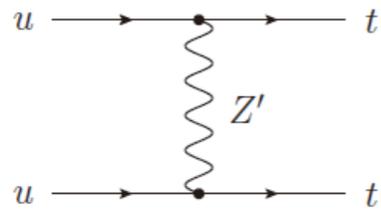
## General exclusion plot



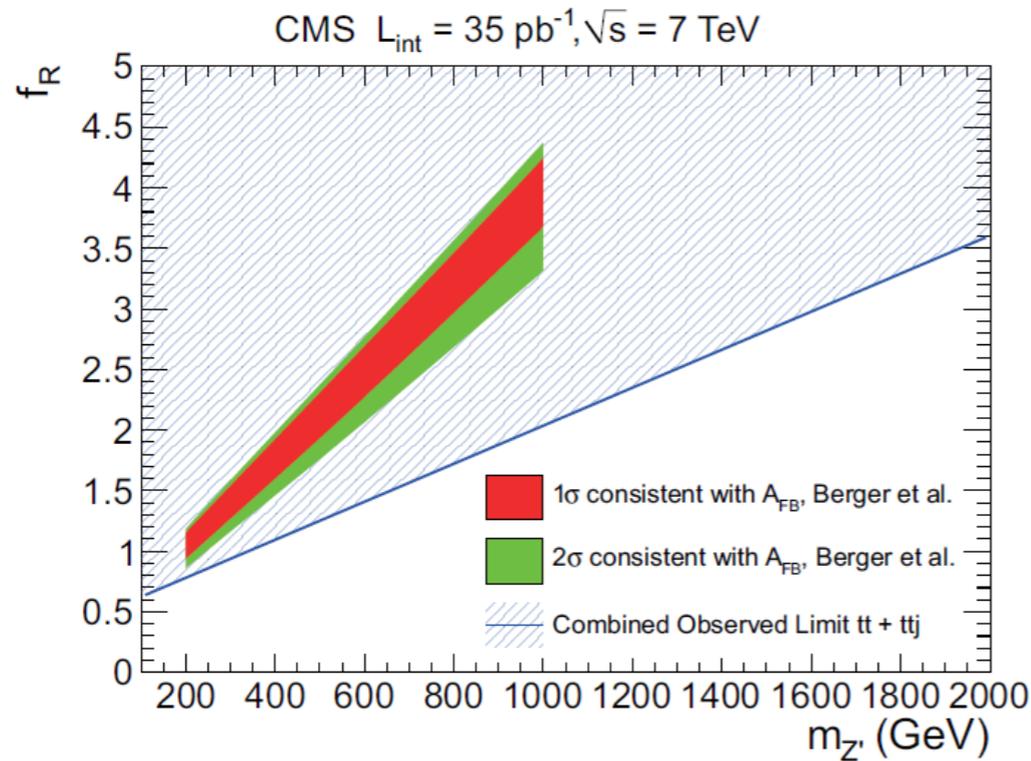
Aguilar-Saavedra, TOP2011

- the t-channel  $Z'$  or scalar exchange models are excluded?

# Same sign top pair production at LHC



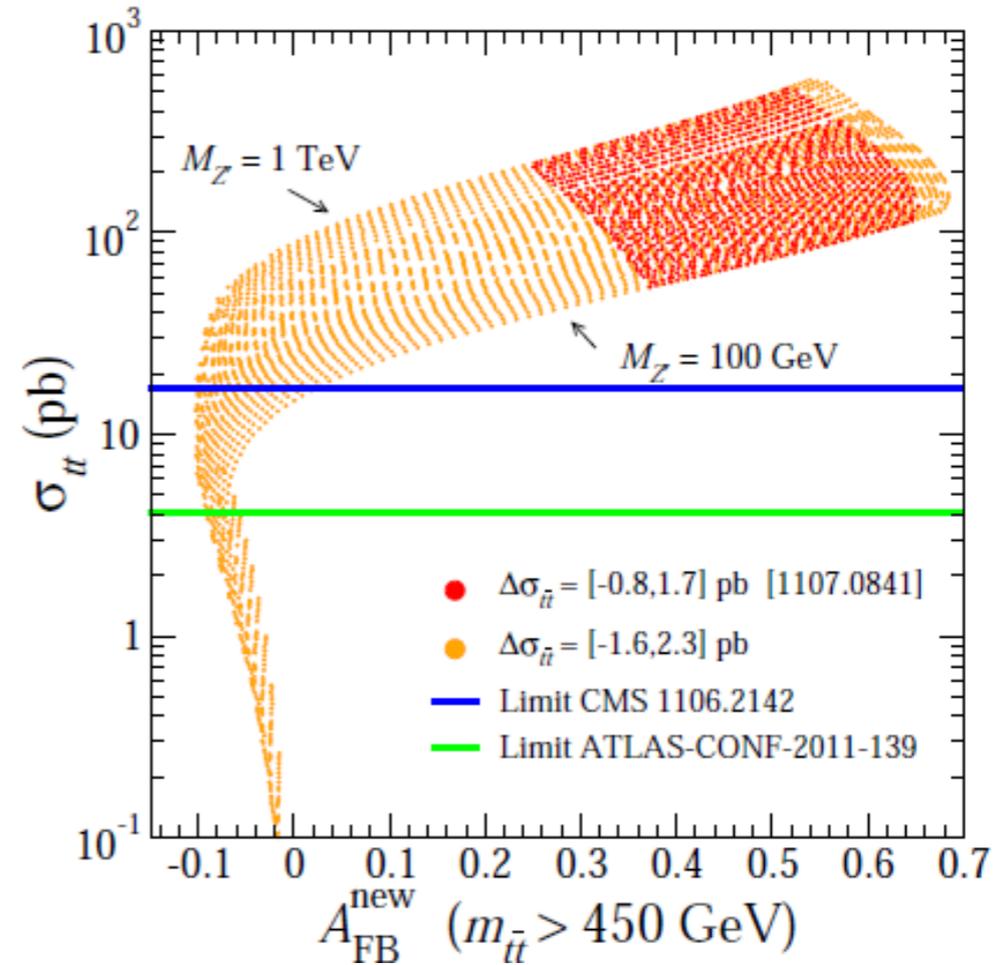
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CMS, JHEP1108; ATLAS-CONF-2011-169

## General exclusion plot



Aguilar-Saavedra, TOP2011

- the t-channel  $Z'$  or scalar exchange models are excluded?
- the answer is NO.

Is the  $Z'$  model for top FB  
asym excluded by the same  
sign top pair production ?

Is the  $Z'$  model for top FB  
asym excluded by the same  
sign top pair production ?

**NO !**

**NOT YET !**

However, the story is not so simple for models with vector bosons that have chiral couplings with the SM fermions !

Chiral  $U(1)$ ' model (Ko, Omura, Yu)

- (1) arXiv:1108.0350, PRD (2012)
- (2) arXiv:1108.4005, JHEP 1201 (2012) 147
- (3) arXiv:1205.0407, EPJC 73 (2013) 2269
- (4) arXiv:1212.4607, JHEP 1303 (2013) 151

# What is the problem of the original $Z'$ model ?

- $Z'$  couples to the RH up type quarks : leptophobic and chiral : **ANOMALY ?**
- No Yukawa couplings for up-type quarks : **MASSLESS TOP QUARK ?**
- Origin of  $Z'$  mass
- Origin of flavor changing couplings of  $Z'$

# What is the problem of the original Z' model ?

$$\mathcal{L}_Y = -Y_{ij}^U \overline{Q_{Li}} \tilde{H} U_{Rj} - Y_{ij}^D \overline{Q_{Li}} H D_{Rj} + H.c.$$

Not gauge invariant

Gauge invariant : OK!

No Yukawa's for up-type quarks:  
**MASSLESS TOP QUARK !**

How to cure this problem ?

This problem is independent of top FCNC

# Answer : Extend Higgs sector

$$\mathcal{L}_Y = -Y_{ij}^U \overline{Q_{Li}} \tilde{H} U_{Rj} - Y_{ij}^D \overline{Q_{Li}} H D_{Rj} + H.c.$$

Not gauge invariant

Gauge invariant : OK!

$$\mathcal{L}_Y = -Y_{ijk}^U \overline{Q_{Li}} \tilde{H}_k U_{Rj} - Y_{ij}^D \overline{Q_{Li}} H D_{Rj} + H.c.$$

$H_k : U(1)$  charged

**Mandatory to extend Higgs sector!**  
 **$Z'$  only model does not exist!**

# of  $U(1)$ '-charged new Higgs doublets depend on  $U(1)$ ' charge assignments to the RH up quarks

# Flavor-dependent $U(1)'$ model

- Charge assignment : SM fermions

	$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)'$
$Q_1$	3	2	1/6	$q_L$
$Q_2$	3	2	1/6	$q_L$
$Q_3$	3	2	1/6	$q_L$
$\overline{D}_1$	$\overline{3}$	1	1/3	$-q_L$
$\overline{D}_2$	$\overline{3}$	1	1/3	$-q_L$
$\overline{D}_3$	$\overline{3}$	1	1/3	$-q_L$
$\overline{U}_1$	$\overline{3}$	1	$-2/3$	$u_1$
$\overline{U}_2$	$\overline{3}$	1	$-2/3$	$u_2$
$\overline{U}_3$	$\overline{3}$	1	$-2/3$	$u_3$
$H$	1	2	1/2	0

LH quarks and RH down-type quarks have universal couplings.

Flavor-dependent

Higgs

# Flavor-dependent $U(1)'$ model

- Charge assignment : Higgs fields

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)'$
$H_1$	1	2	1/2	$-q_L - u_1$
$H_2$	1	2	1/2	$-q_L - u_2$
$H_3$	1	2	1/2	$-q_L - u_3$
$\Phi$	1	1	1	$-q_\Phi$

- introduce three Higgs doublets charged under  $U(1)'$  in addition to the SM Higgs which is not charged under  $U(1)'$ .

$$\begin{aligned}
 V_y = & y_{i1}^u H_1 \bar{U}_1 Q_i + y_{i2}^u H_2 \bar{U}_2 Q_i + y_{i3}^u H_3 \bar{U}_3 Q_i \\
 & + y_{ij}^d \bar{D}_j Q_i i\tau_2 H^\dagger \\
 & + y_{ij}^e \bar{E}_j L_i i\tau_2 H^\dagger + y_{ij}^n H \bar{N}_j L_i.
 \end{aligned}$$

- The  $U(1)'$  is spontaneously broken by  $U(1)'$  charged complex scalar  $\Phi$ .

# Anomaly Cancellation : Sol. I

- Anomaly cancellation requires extra fermions I:  $SU(2)$  doublets

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)'$
$Q'$	3	2	1/6	$-(q_1 + q_2 + q_3)$
$D'_R$	3	1	-1/3	$-(d_1 + d_2 + d_3)$
$U'_R$	3	1	2/3	$-(u_1 + u_2 + u_3)$
$L'$	1	2	-1/2	0
$E'$	1	1	-1	0
$l_{L1}$	1	2	-1/2	$Q_L$
$l_{R1}$	1	2	-1/2	$Q_R$
$l_{L2}$	1	2	-1/2	$-Q_L$
$l_{R2}$	1	2	-1/2	$-Q_R$

one extra generation

$SU(2)_L^2 \cdot U(1)'$

vector-like pairs

$U(1)'^2 \cdot U(1)$

a candidate for CDM

# Anomaly Cancellation : Sol. II

- Anomaly cancellation requires extra fermions II:  $SU(3)_c$  triplets

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)'$
$q_{L1}$	3	1	$-1/3$	$Q_L$
$q_{R1}$	3	1	$-1/3$	$Q_R$
$q_{L2}$	3	1	$-1/3$	$-Q_L$
$q_{R2}$	3	1	$-1/3$	$-Q_R$

- introduce the singlet scalar  $X$  to the SM in order to allow the decay of the extra colored particles.

$$V_m = \lambda_i X^\dagger \overline{D_{Ri} q_{L1}} + \lambda_i X \overline{D_{Ri} q_{L2}}$$

a candidate for CDM

# Flavor-dependent U(1)' model

- Gauge coupling in the mass base

- Z' interacts only with the right-handed up-type quarks

$$g' Z'^{\mu} \sum_{i,j=1,2,3} (g_R^u)_{ij} \overline{U}_R^i \gamma_{\mu} U_R^j \quad \leftarrow \quad g' Z'^{\mu} \sum_{i=1,2,3} u_i \overline{U}'_{Ri} \gamma_{\mu} U'_{Ri}$$

- The 3 X 3 coupling matrix  $g_R^u$  is defined by

$$(g_R^u)_{ij} = (U_R^u)_{ik} u_k (U_R^u)_{kj}^{\dagger}$$

biunitary matrix diagonalizing the up-type quark mass matrix

mass base:  $g' Z'^{\mu} \left[ (g_L^u)_{ij} \overline{\hat{U}}_L^i \gamma_{\mu} \hat{U}_L^j + (g_L^d)_{ij} \overline{\hat{D}}_L^i \gamma_{\mu} \hat{D}_L^j + (g_R^u)_{ij} \overline{\hat{U}}_R^i \gamma_{\mu} \hat{U}_R^j + (g_R^d)_{ij} \overline{\hat{D}}_R^i \gamma_{\mu} \hat{D}_R^j \right]$

tree-level contributions to FCNC

$$D^0 - \overline{D}^0$$

$A_{FB}$

$$K^0 - \overline{K}^0$$

$$B^0 - \overline{B}^0$$

$$B_s - \overline{B}_s$$

$$D^0 - \overline{D}^0$$

$A_{FB}$

$$K^0 - \overline{K}^0$$

$$B^0 - \overline{B}^0$$

$$B_s - \overline{B}_s$$

# Flavor-dependent $U(1)'$ model

- 2 Higgs doublet model :  $(u_1, u_2, u_3) = (0, 0, 1)$

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)'$
$H$	1	2	1/2	0
$H_3$	1	2	1/2	1
$\Phi$	1	1	1	$q_\Phi$

$$V_y = y_{i1}^u \overline{Q}_i \tilde{H} U_{R1} + y_{i2}^u \overline{Q}_i \tilde{H} U_{Rj} + y_{i3}^u \overline{Q}_i \tilde{H}_3 U_{Rj} \\ + y_{ij}^d \overline{Q}_i H D_{Rj} + y_{ij}^e \overline{L}_i H \overline{E}_j + y_{ij}^n \overline{L}_i \tilde{H} N_j.$$

$$V_h = Y_{ij}^u \overline{\hat{U}}_{Li} \hat{U}_{Rj} \hat{h}_0 + Y_{ij}^d \overline{\hat{D}}_{Li} \hat{D}_{Rj} \hat{h}_0,$$

$$Y_{ij}^u = \frac{m_i^u \cos \alpha}{v \cos \beta} \delta_{ij} + \frac{2m_i^u}{v \sin 2\beta} (g_R^u)_{ij} \sin(\alpha - \beta),$$

$$Y_{ij}^d = \frac{m_i^d \cos \alpha}{v \cos \beta} \delta_{ij},$$

}  $\propto$  the fermion mass

# Flavor-dependent $U(1)'$ model

- 3 Higgs doublet model:  $(u_1, u_2, u_3) = (-q, 0, q)$

	$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)'$
$H_1$	1	2	1/2	$q$
$H_2$	1	2	1/2	0
$H_3$	1	2	1/2	$-q$
$\Phi$	1	1	0	$-1$

$$\begin{aligned} \mathcal{L}_Y = & y_{i1}^u H_1 \bar{U}_1 Q_i + y_{i2}^u H_2 \bar{U}_2 Q_i + y_{i3}^u H_3 \bar{U}_3 Q_i \\ & + y_{ij}^d H_2^\dagger \bar{D}_j Q_i + y_{ij}^e H_2^\dagger \bar{E}_j L_i + y_{ij}^n H_2 \bar{N}_j L_i. \end{aligned}$$

# Flavor-dependent U(1)' model

- Yukawa coupling in the mass base (2HDM)

- lightest Higgs h:  $V_h = Y_{ij}^u \overline{\hat{U}}_{Li} \hat{U}_{Rj} h + Y_{ij}^d \overline{\hat{D}}_{Li} \hat{D}_{Rj} h + Y_{ij}^e \overline{\hat{E}}_{Li} \hat{E}_{Rj} h + h.c.,$

$$Y_{ij}^u = \frac{m_i^u \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij} + \frac{2m_i^u}{v \sin 2\beta} (g_R^u)_{ij} \sin(\alpha - \beta) \cos \alpha_\Phi,$$

$$Y_{ij}^d = \frac{m_i^d \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij},$$

$$Y_{ij}^e = \frac{m_i^l \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij},$$

- lightest charged Higgs h<sup>±</sup>:  $V_{h^\pm} = -Y_{ij}^{u-} \overline{\hat{D}}_{Li} \hat{U}_{Rj} h^- + Y_{ij}^{d+} \overline{\hat{U}}_{Li} \hat{D}_{Rj} h^+ + h.c.,$

$$Y_{ij}^{u-} = \sum_l (V_{\text{CKM}})_{li}^* \left\{ \frac{\sqrt{2} m_l^u \tan \beta}{v} \delta_{lj} - \frac{2\sqrt{2} m_l^u}{v \sin 2\beta} (g_R^u)_{lj} \right\},$$

$$Y_{ij}^{d+} = (V_{\text{CKM}})_{ij} \frac{\sqrt{2} m_j^d \tan \beta}{v},$$

- lightest pseudoscalar Higgs a:  $V_a = -iY_{ij}^{au} \overline{\hat{U}}_{Li} \hat{U}_{Rj} a + iY_{ij}^{ad} \overline{\hat{D}}_{Li} \hat{D}_{Rj} a + iY_{ij}^{ae} \overline{\hat{E}}_{Li} \hat{E}_{Rj} a + h.c.,$

$$Y_{ij}^{au} = \frac{m_i^u \tan \beta}{v} \delta_{ij} - \frac{2m_i^u}{v \sin 2\beta} (g_R^u)_{ij},$$

$$Y_{ij}^{ad} = \frac{m_i^d \tan \beta}{v} \delta_{ij},$$

$$Y_{ij}^{ae} = \frac{m_i^l \tan \beta}{v} \delta_{ij}.$$

# Flavor-dependent U(1)' model

- Yukawa coupling in the mass base (2HDM)

- lightest Higgs h:  $V_h = Y_{ij}^u \overline{\hat{U}}_{Li} \hat{U}_{Rj} h + Y_{ij}^d \overline{\hat{D}}_{Li} \hat{D}_{Rj} h + Y_{ij}^e \overline{\hat{E}}_{Li} \hat{E}_{Rj} h + h.c.,$

$$Y_{ij}^u = \frac{m_i^u \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij} + \frac{2m_i^u}{v \sin 2\beta} (g_R^u)_{ij} \sin(\alpha - \beta) \cos \alpha_\Phi,$$

$$Y_{ij}^d = \frac{m_i^d \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij},$$

$$Y_{ij}^e = \frac{m_i^l \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij},$$

- lightest charged Higgs h<sup>±</sup>:  $V_{h^\pm} = -Y_{ij}^{u-} \overline{\hat{D}}_{Li} \hat{U}_{Rj} h^- + Y_{ij}^{d+} \overline{\hat{U}}_{Li} \hat{D}_{Rj} h^+ + h.c.,$

$$Y_{ij}^{u-} = \sum_l (V_{\text{CKM}})_{li}^* \left\{ \frac{\sqrt{2} m_l^u \tan \beta}{v} \delta_{lj} - \frac{2\sqrt{2} m_l^u}{v \sin 2\beta} (g_R^u)_{lj} \right\},$$

$$Y_{ij}^{d+} = (V_{\text{CKM}})_{ij} \frac{\sqrt{2} m_j^d \tan \beta}{v},$$

- lightest pseudoscalar Higgs a:  $V_a = -iY_{ij}^{au} \overline{\hat{U}}_{Li} \hat{U}_{Rj} a + iY_{ij}^{ad} \overline{\hat{D}}_{Li} \hat{D}_{Rj} a + iY_{ij}^{ae} \overline{\hat{E}}_{Li} \hat{E}_{Rj} a + h.c.,$

$$Y_{ij}^{au} = \frac{m_i^u \tan \beta}{v} \delta_{ij} - \frac{2m_i^u}{v \sin 2\beta} (g_R^u)_{ij},$$

$$Y_{ij}^{ad} = \frac{m_i^d \tan \beta}{v} \delta_{ij},$$

$$Y_{ij}^{ae} = \frac{m_i^l \tan \beta}{v} \delta_{ij}.$$

# Top-antitop pair production

## 1. Z' dominant scenario

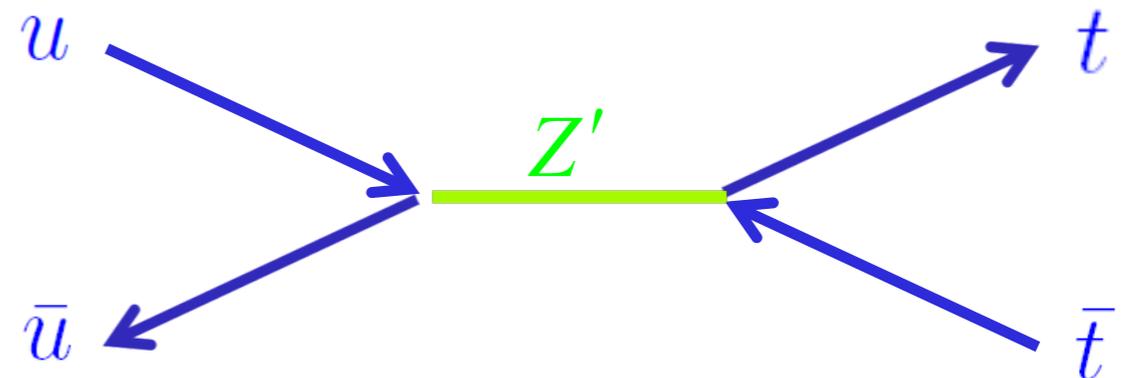
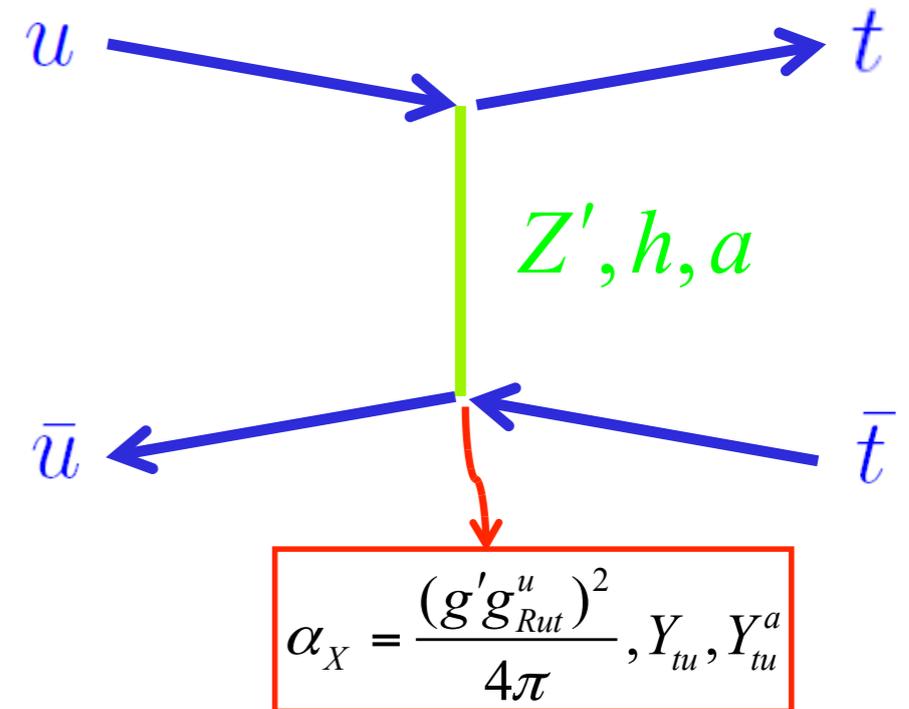
cf. Jung, Murayama, Pierce, Wells, PRD81(2010)♪

## 2. Higgs dominant scenario

cf. Babu, Frank, Rai, PRL107(2011)♪

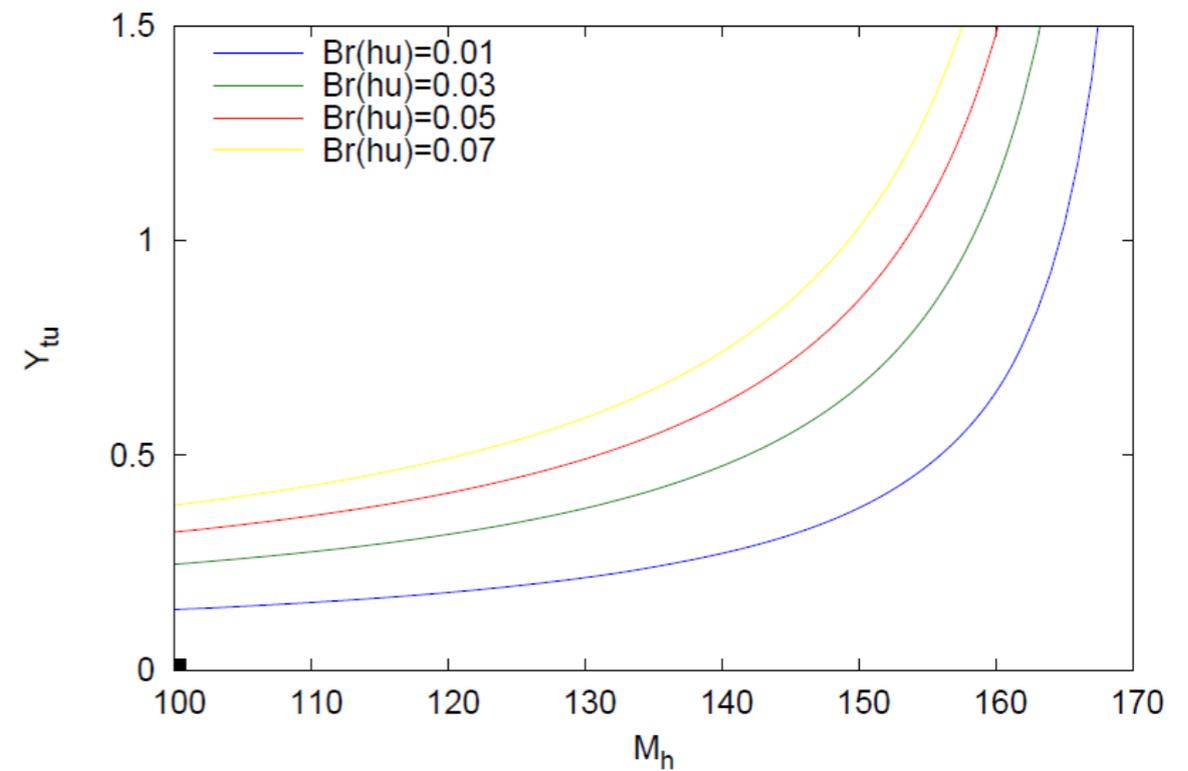
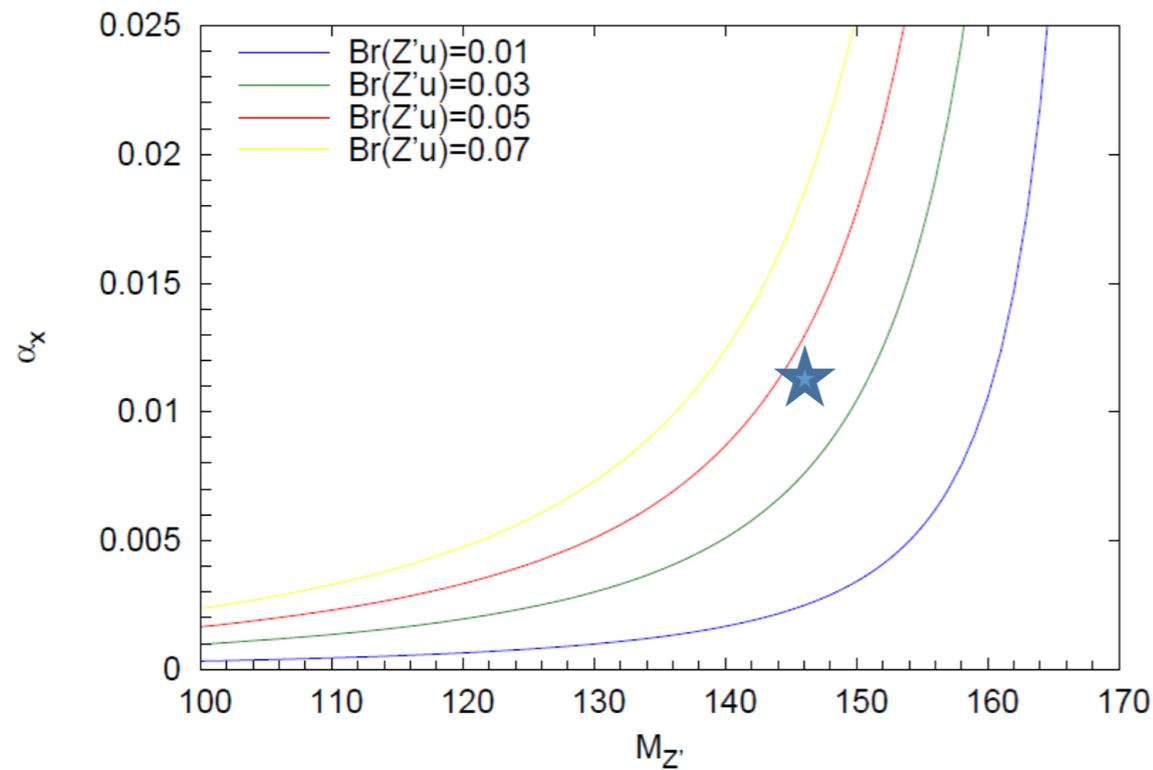
## 3. Mixed scenario

Destructive interference between Z' and h,a for the same sign pair production (Ko, Omura, Yu)



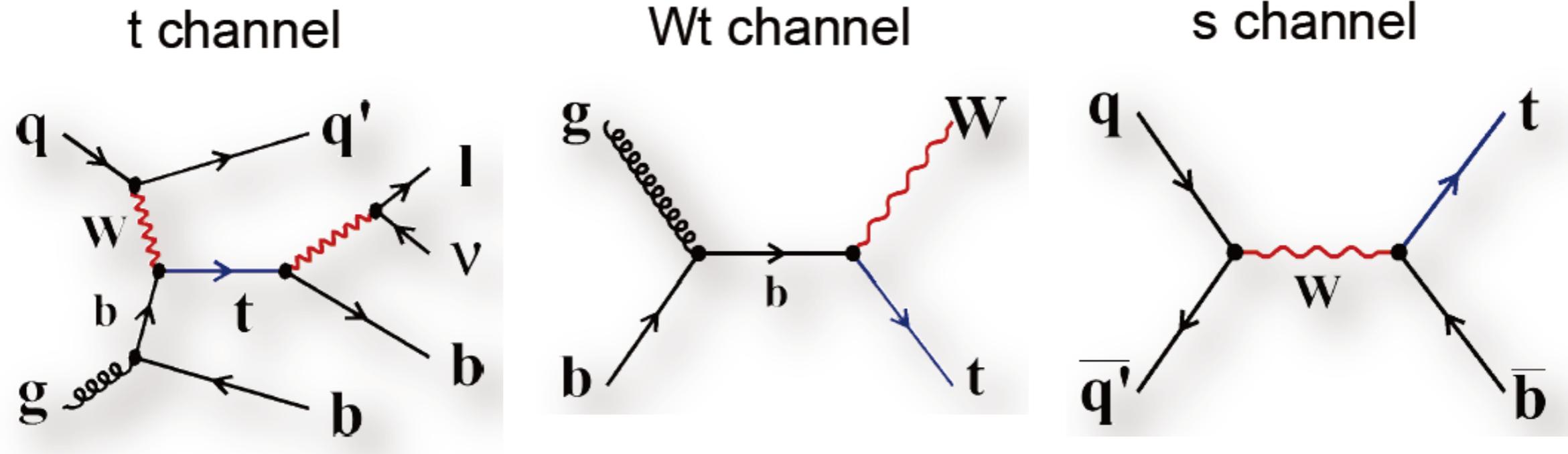
# Top quark decay

- decay into  $W+b$  in SM :  $\text{Br}(t \rightarrow Wb) \sim 100\%$ .
- If the top quark decays to  $Z' + u$  or  $h + u$  ,  $\text{Br}(t \rightarrow Wb)$  might significantly be changed.



- requires  $\text{Br}(t \rightarrow \text{non-SM}) < 5\%$  .
- choose either  $m_{Z'} < m_t$  or  $m_h < m_t$  .

# Single top quark production



- **D0** [D0, 1105.2788](#)

$$\sigma(p\bar{p} \rightarrow tbq) = 2.90 \pm 0.59 \text{ pb}$$

In the SM,

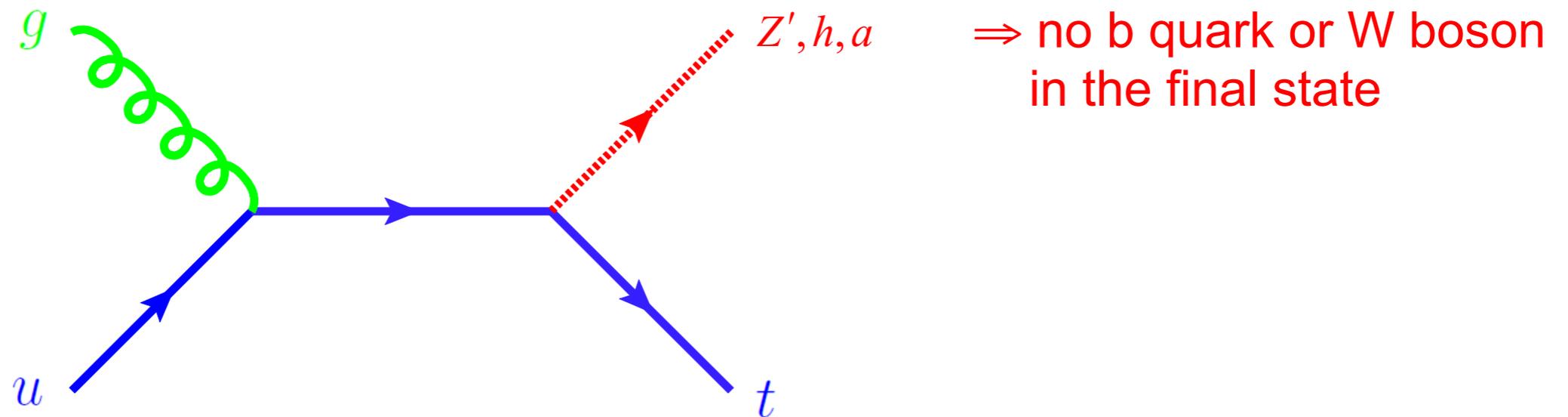
$$\sigma(p\bar{p} \rightarrow tbq) = 2.26 \pm 0.12 \text{ pb}$$

- **CMS** [CMS, 1106.3052](#)

$$\sigma(pp \rightarrow tbq) = 83.6 \pm 29.8 \pm 3.3 \text{ pb}$$

$$\sigma(pp \rightarrow tbq) = 64.3^{+2.1+1.5}_{-0.7-1.7} \text{ pb}$$

# Single top quark production



- **D0** [D0, 1105.2788](#)

$$\sigma(p\bar{p} \rightarrow tbq) = 2.90 \pm 0.59 \text{ pb}$$

In the SM,

$$\sigma(p\bar{p} \rightarrow tbq) = 2.26 \pm 0.12 \text{ pb}$$

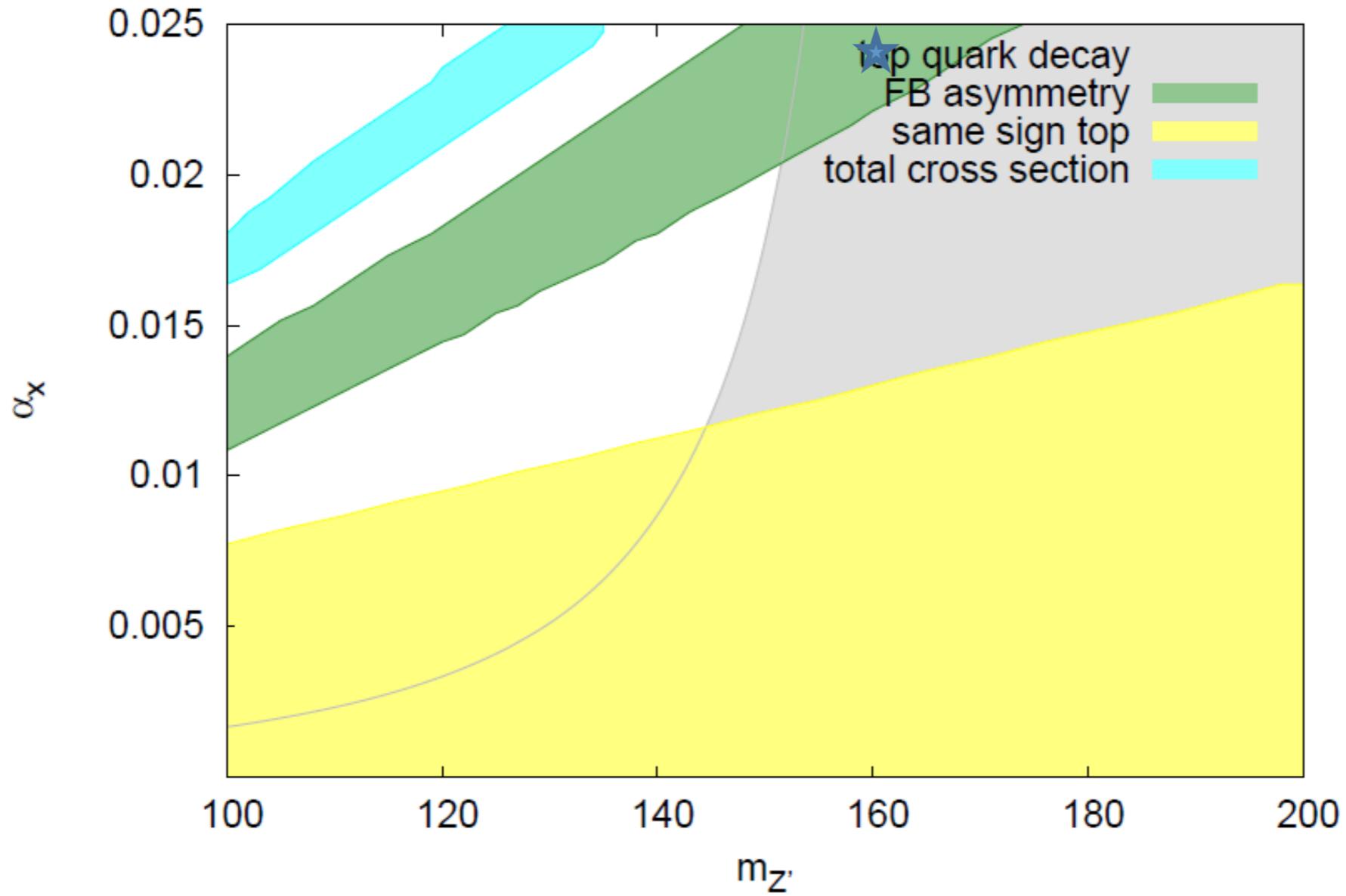
- **CMS** [CMS, 1106.3052](#)

$$\sigma(pp \rightarrow tbq) = 83.6 \pm 29.8 \pm 3.3 \text{ pb}$$

$$\sigma(pp \rightarrow tbq) = 64.3_{-0.7-1.7}^{+2.1+1.5} \text{ pb}$$

# Favored region

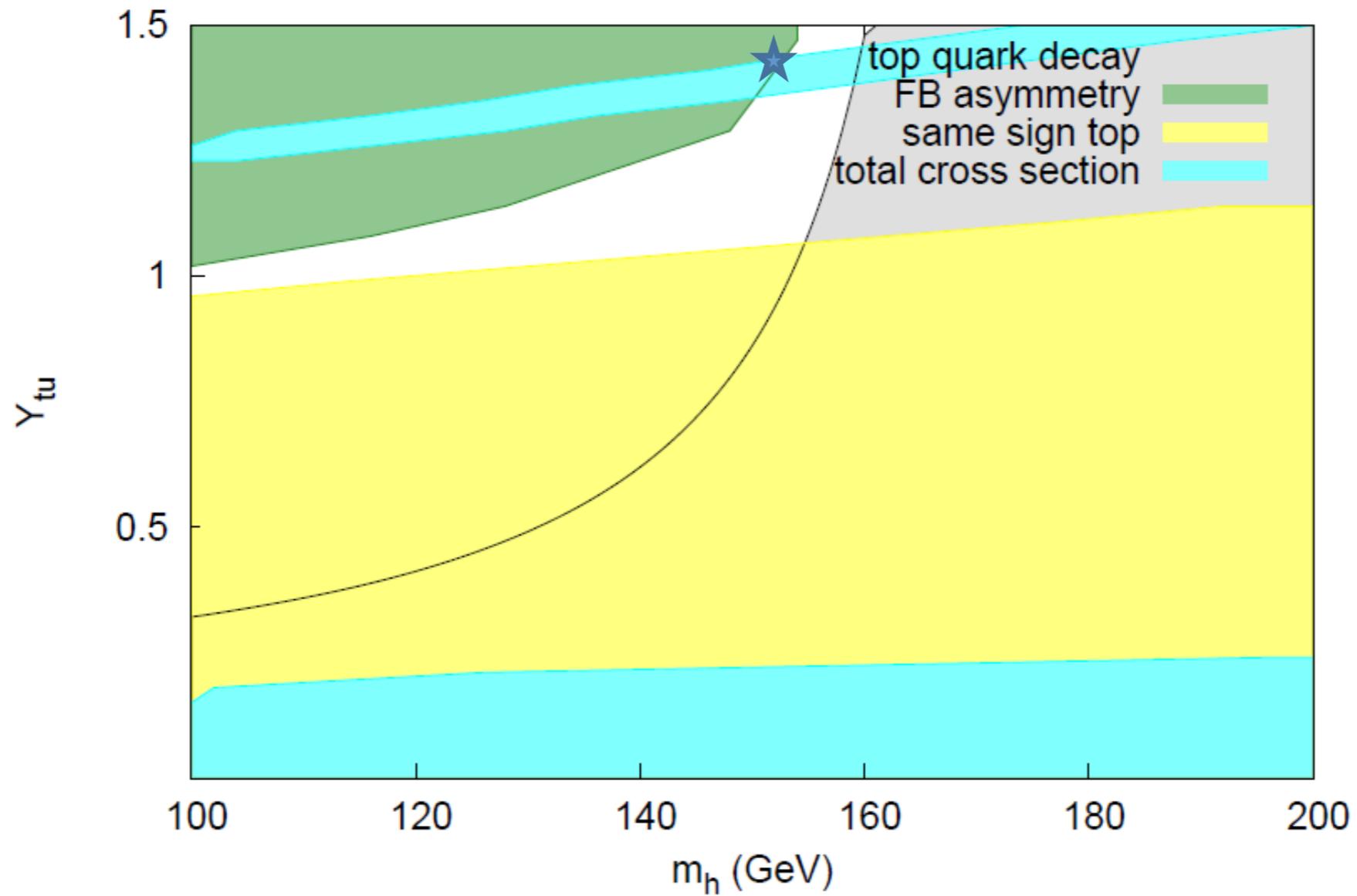
Z' dominant case



★ = similar to Jung, Murayama, Pierce, Wells' model (PRD81)

# Favored region

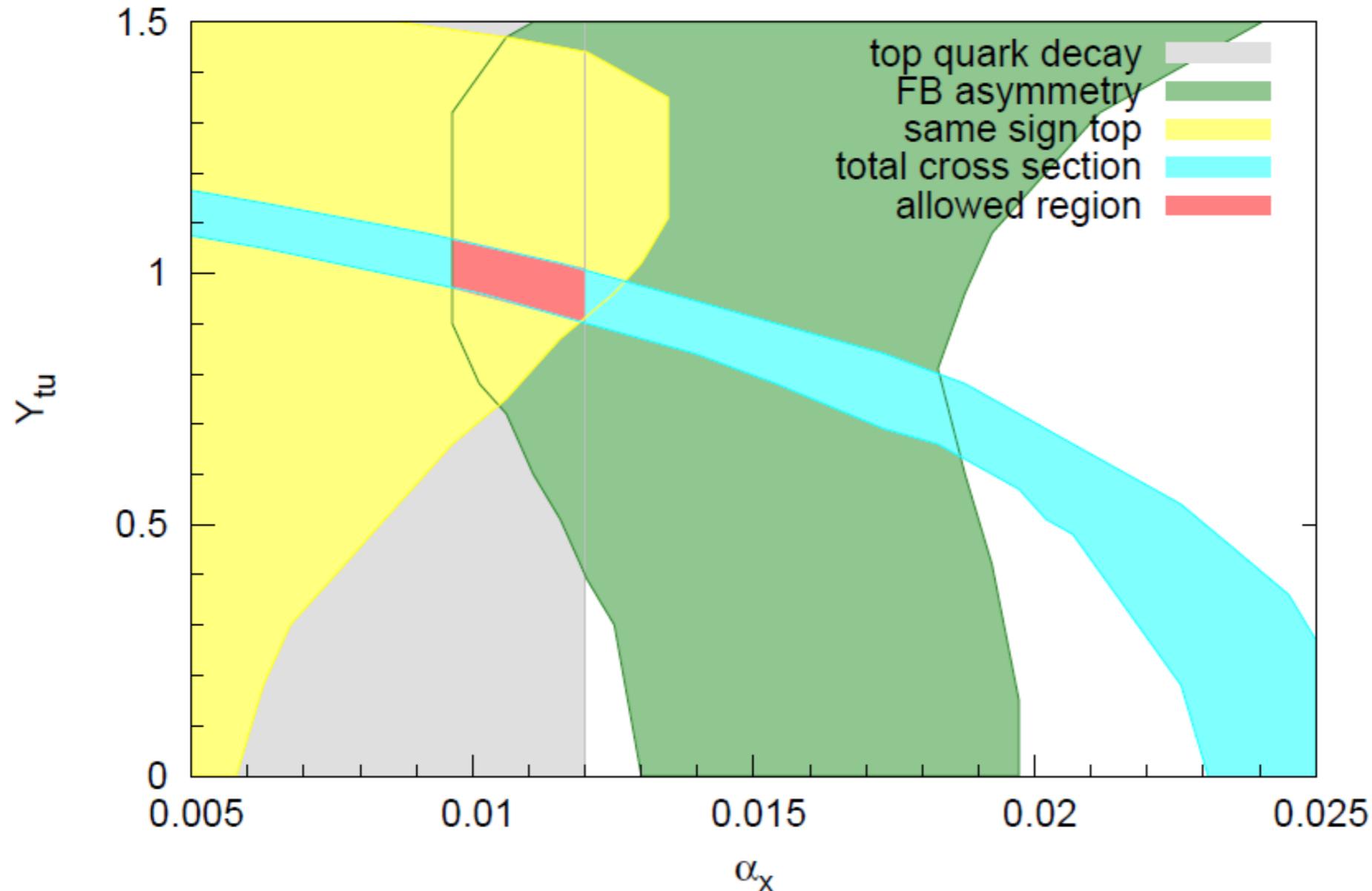
Scalar Higgs (h) dominant case



★ = similar to Babu, Frank, Rai's model (PRL107)

# Favored region

Z'+h+a case



$$m_{Z'} = 145 \text{ GeV}$$

$$m_h = 180 \text{ GeV}$$

$$m_a = 300 \text{ GeV}$$

$$Y_{tu}^a = 1.1$$

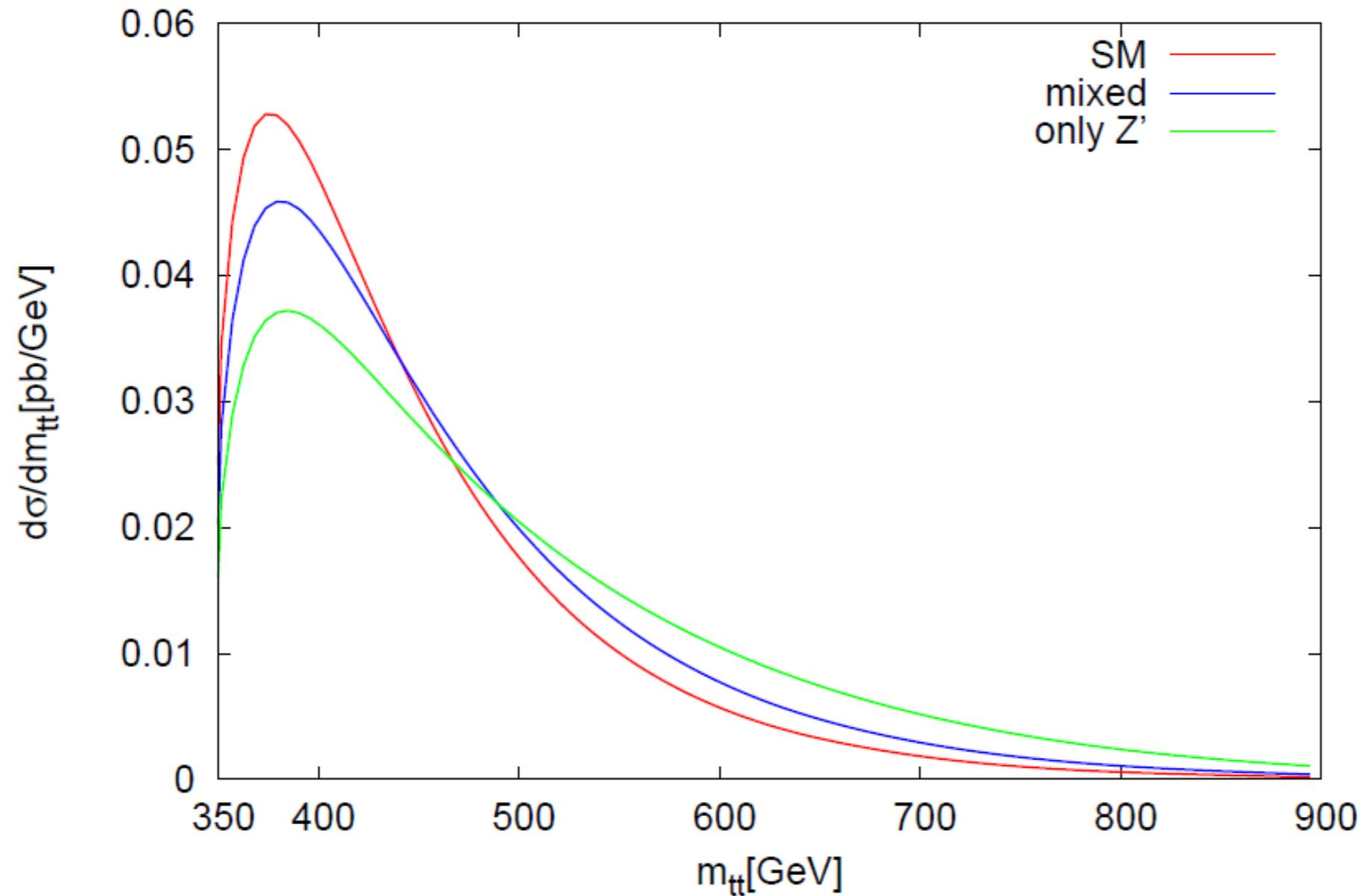
- **destructive interference** between Z and Higgs bosons in the same sign top pair production.
- consistent with the CMS bound, but not with the ATLAS bound.

# Invariant mass distribution

Only Z' case

$$m_{Z'} = 145 \text{ GeV}$$

$$\alpha_x = 0.029$$



mixed case

$$m_{Z'} = 145 \text{ GeV}$$

$$m_h = 180 \text{ GeV}$$

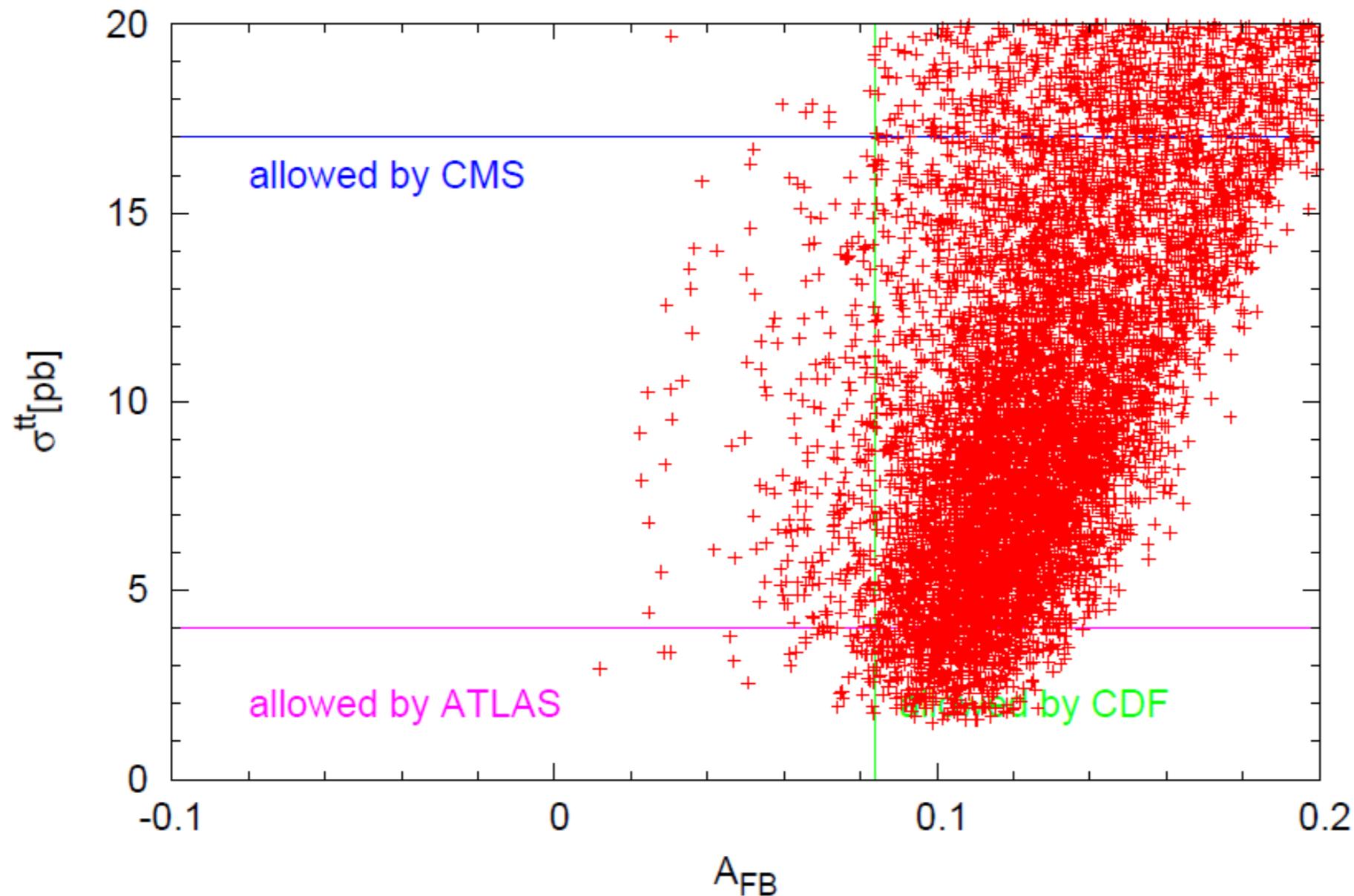
$$m_a = 300 \text{ GeV}$$

$$\alpha_x = 0.01$$

$$Y_{tu} = 1.0$$

$$Y_{tu}^a = 1.1$$

# $A_{\text{FB}}$ versus $\sigma_{t\bar{t}}$



$$m_{Z'} = 145 \text{ GeV}$$

$$180 \text{ GeV} < m_h < 1 \text{ TeV}$$

$$180 \text{ GeV} < m_a < 1 \text{ TeV}$$

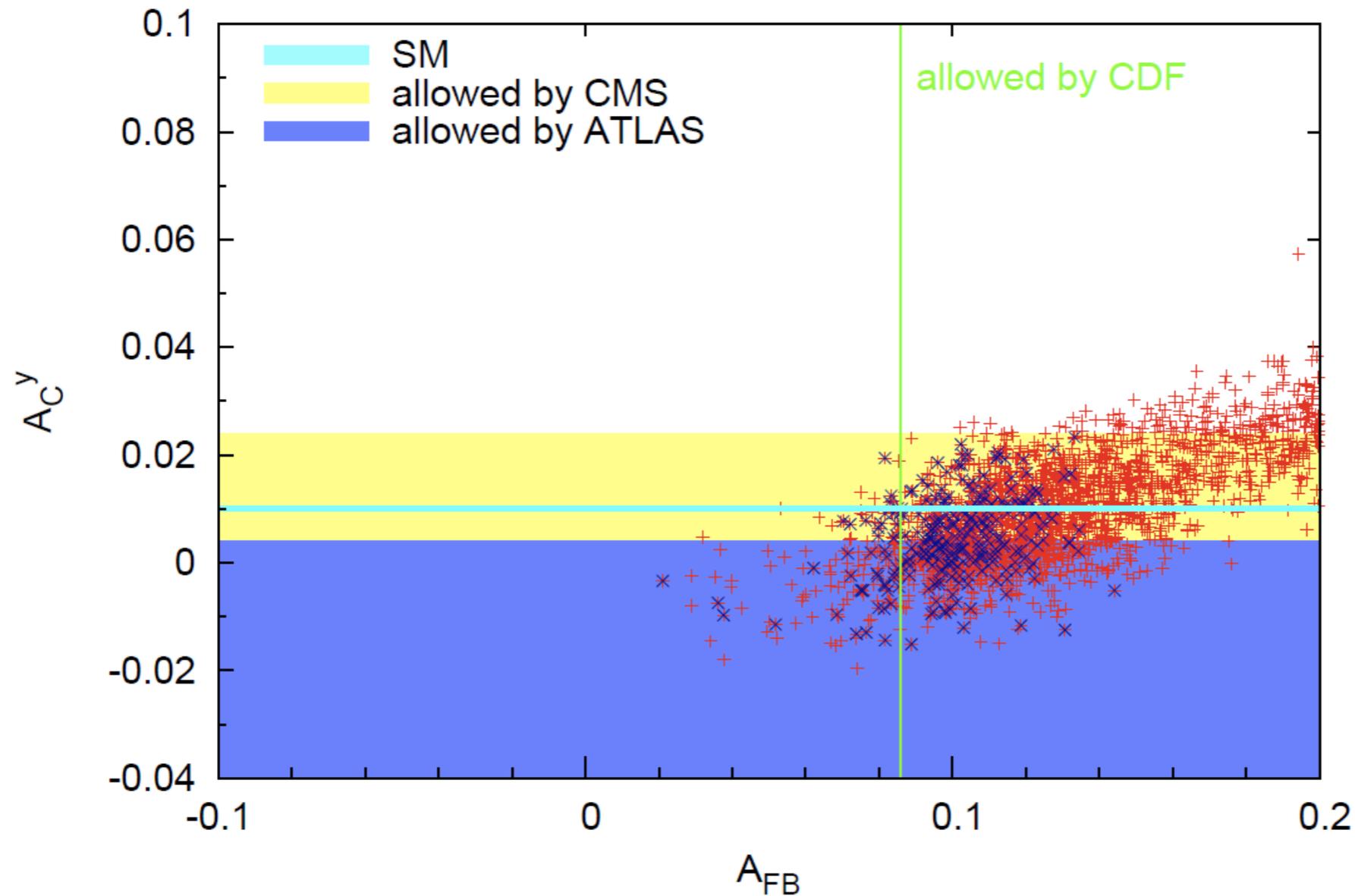
$$0.005 < \alpha_X < 0.025$$

$$0.5 < Y_{tu} < 1.5$$

$$0.5 < Y_{tu}^a < 1.5$$

Have a trouble with new CMS data  $< 0.39$  pb

# $A_{\text{FB}}$ versus $A_{\text{C}}^y$



$$m_{Z'} = 145 \text{ GeV}$$

$$180 \text{ GeV} < m_h < 1 \text{ TeV}$$

$$180 \text{ GeV} < m_a < 1 \text{ TeV}$$

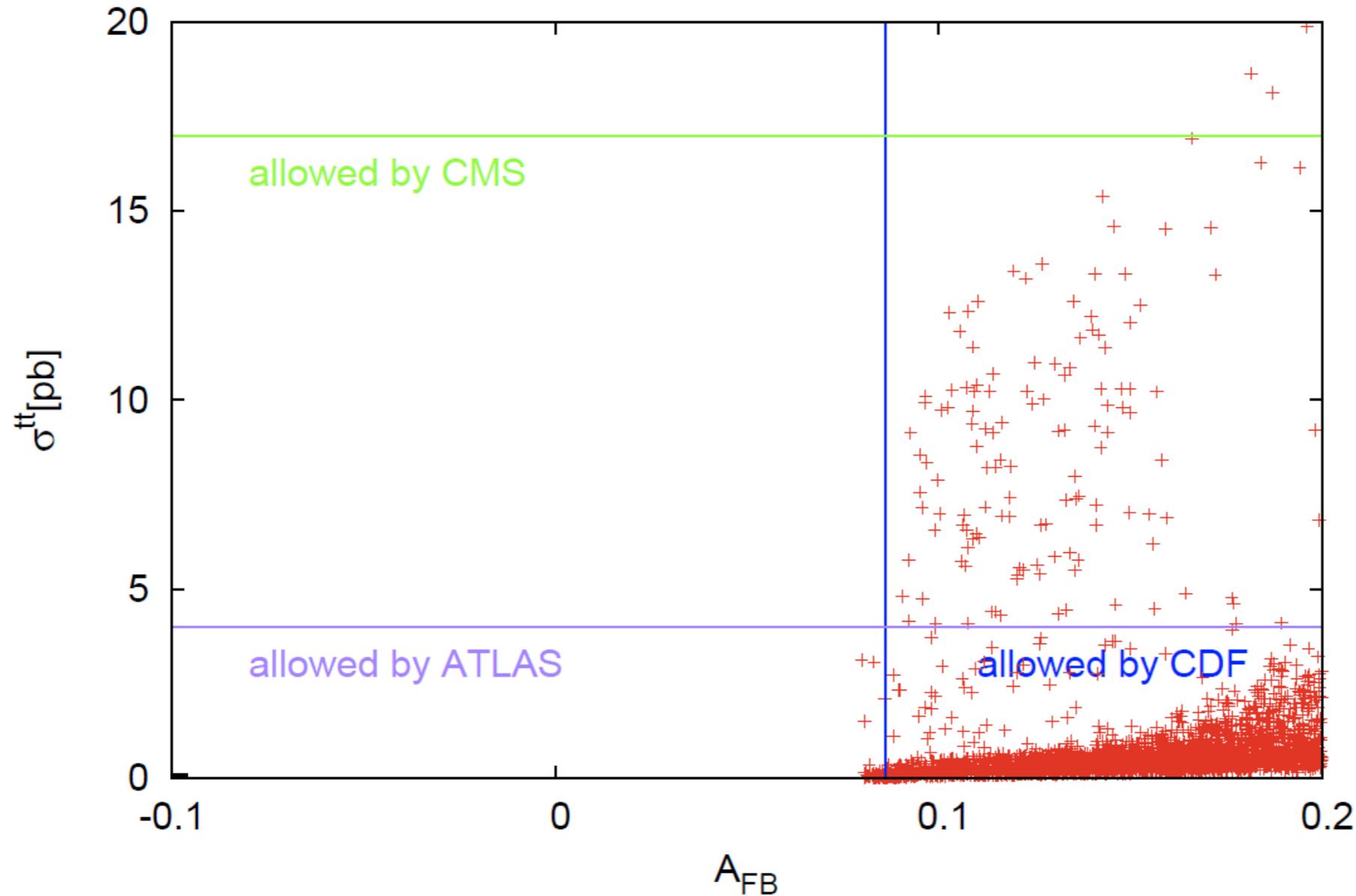
$$0.005 < \alpha_X < 0.025$$

$$0.5 < Y_{tu} < 1.5$$

$$0.5 < Y_{tu}^a < 1.5$$

Have a trouble with new CMS data  $< 0.39 \text{ pb}$

# $A_{\text{FB}}$ versus $\sigma_{\text{tt}}$



$m_h = 126 \text{ GeV}$

$180 \text{ GeV} < m_{Z'} < 1.5 \text{ TeV}$

$180 \text{ GeV} < m_a < 1 \text{ TeV}$

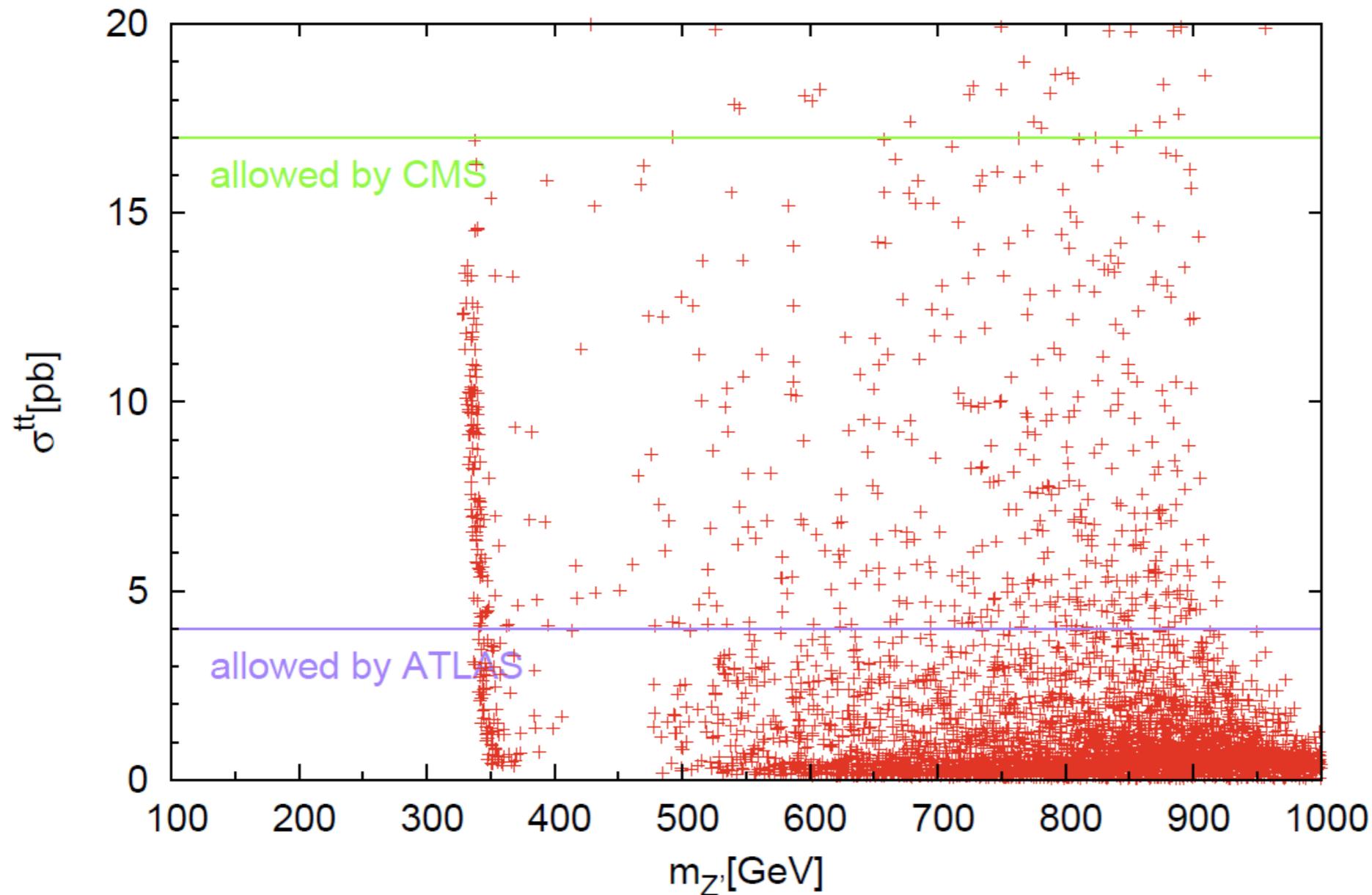
$0.005 < \alpha_X < 0.025$

$0.1 < Y_{tu} < 0.5$

$0.1 < Y_{tu}^a < 1.5$

Still OK with new CMS data  $< 0.39 \text{ pb}$

# $m_{Z'}$ versus $\sigma_{tt}$



$$m_h = 126 \text{ GeV}$$

$$180 \text{ GeV} < m_{Z'} < 1.5 \text{ TeV}$$

$$180 \text{ GeV} < m_a < 1 \text{ TeV}$$

$$0.005 < \alpha_X < 0.025$$

$$0.1 < Y_{tu} < 0.5$$

$$0.1 < Y_{tu}^a < 1.5$$

Still OK with new CMS data  $< 0.39 \text{ pb}$

# Summary for top FBA

- We constructed realistic  $Z'$  models with additional Higgs doublets that are charged under  $U(1)'$  : Based on local gauge symmetry, renormalizable, anomaly free and realistic Yukawa
- New **spin-one boson ( $Z'$ ) with chiral couplings** to the SM fermion requires a new **Higgs doublet that couples to the new  $Z'$**
- **This is also true for axigluon, flavor  $SU(3)_R$ ,  $W'$ , etc.**
- Our model can accommodate the top FB Asym @ Tevatron, the same sign top pair production, and the top CA@LHC

- Meaningless to say “The Z’ model is excluded by the same sign top pair production.”
- Important to consider a minimal consistent (renormalizable, realistic, anomaly free) in order to do phenomenology
- Flavor issues in B and charm systems were also studied (w/ Yuji Omura and C. Yu)
- Top longitudinal pol (which is zero in QCD because of Parity) could be another important tool for resolving the issue (Ko et al, Godbole et al, Degrande et al, etc)

**$B \rightarrow D^{(*)} \tau \nu$  and  $B \rightarrow \tau \nu$  in chiral  $U(1)'$  models  
with flavored multi Higgs doublets**

Ko, Omura, Yu, arXiv:1212.4607, JHEP(2013)

# Flavor-dependent U(1)' model

- Yukawa coupling in the mass base (2HDM)

- lightest Higgs h:  $V_h = Y_{ij}^u \overline{\hat{U}}_{Li} \hat{U}_{Rj} h + Y_{ij}^d \overline{\hat{D}}_{Li} \hat{D}_{Rj} h + Y_{ij}^e \overline{\hat{E}}_{Li} \hat{E}_{Rj} h + h.c.,$

$$Y_{ij}^u = \frac{m_i^u \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij} + \frac{2m_i^u}{v \sin 2\beta} (g_R^u)_{ij} \sin(\alpha - \beta) \cos \alpha_\Phi,$$

$$Y_{ij}^d = \frac{m_i^d \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij},$$

$$Y_{ij}^e = \frac{m_i^l \cos \alpha}{v \cos \beta} \cos \alpha_\Phi \delta_{ij},$$

- lightest charged Higgs h<sup>±</sup>:  $V_{h^\pm} = -Y_{ij}^{u-} \overline{\hat{D}}_{Li} \hat{U}_{Rj} h^- + Y_{ij}^{d+} \overline{\hat{U}}_{Li} \hat{D}_{Rj} h^+ + h.c.,$

$$Y_{ij}^{u-} = \sum_l (V_{\text{CKM}})_{li}^* \left\{ \frac{\sqrt{2}m_l^u \tan \beta}{v} \delta_{lj} - \frac{2\sqrt{2}m_l^u}{v \sin 2\beta} (g_R^u)_{lj} \right\},$$

$$Y_{ij}^{d+} = (V_{\text{CKM}})_{ij} \frac{\sqrt{2}m_j^d \tan \beta}{v},$$

- lightest pseudoscalar Higgs a:  $V_a = -iY_{ij}^{au} \overline{\hat{U}}_{Li} \hat{U}_{Rj} a + iY_{ij}^{ad} \overline{\hat{D}}_{Li} \hat{D}_{Rj} a + iY_{ij}^{ae} \overline{\hat{E}}_{Li} \hat{E}_{Rj} a + h.c.,$

$$Y_{ij}^{au} = \frac{m_i^u \tan \beta}{v} \delta_{ij} - \frac{2m_i^u}{v \sin 2\beta} (g_R^u)_{ij},$$

$$Y_{ij}^{ad} = \frac{m_i^d \tan \beta}{v} \delta_{ij},$$

$$Y_{ij}^{ae} = \frac{m_i^l \tan \beta}{v} \delta_{ij}.$$

**Comparison with  
other similar works**

# Top-Philic Scalar

Simplest ansatz violates SU(2) gauge symmetry

$$\mathcal{L} = -S [y_{st} \bar{t}_L t_R + H.c.]$$

Introduce another Higgs doublet  $H_t$  with odd  $Z_t$  parity

$$\begin{aligned} \mathcal{L} = & D_\mu H_t^\dagger D^\mu H_t - m_{H_t}^2 |H_t|^2 - \lambda_{H_t} |H_t|^4 - \lambda_{HH_t} |H|^2 |H_t|^2 + \lambda |H^\dagger H_t|^2 \\ & - \lambda \left[ (H^\dagger H_t)^2 - H.c. \right] - \left[ y'_{H_t} \overline{Q'_{3L}} \widetilde{H}_t t'_R + H.c. \right] (-m_{12}^2 H^\dagger H_t + H.c.????) \end{aligned}$$

Models by Das, C.Kao (1996); Soni et al (2000),...

If we implement  $Z_t$  to  $U(1)_t$ , we end up with Ko-Omura-Yu model discussed in this talk

# Top-Philic spin-1

Naive guess will be something like this:

$$\mathcal{L} = -g_t Z'_\mu [g_V \bar{t} \gamma^\mu t + g_A \bar{t} \gamma^\mu \gamma_5 t] = -g_t Z'_\mu [g_L \bar{t}_L \gamma^\mu t_L + g_R \bar{t}_R \gamma^\mu t_R]$$

If top couplings are chiral under new  $U(1)'$ , there is a problem with the top Yukawa coupling

One way out of this problem is to introduce a new Higgs doublet coupled to  $Z'$

Again, Ko-Omura-Yu model

So let me talk about Ko-Omura-Yu Model

# Conclusion

- In this talk, I showed that theory predictions based on simplified toy model and the simplest UV completions can be vastly different
- Simplified models often used for data analysis are arbitrary truncations of underlying theories, and not even well defined EFT
- They are useful if the stuffs put away under the rug (such as gauge invariance, renormalizability, unitarity, anomaly cancellation, realistic Yukawa's, etc.) do not affect the physical observables we study

# Conclusion-Con'd

- Very often you don't know a priori if this assumption is true or not
- When some simple model can explain some phenomena, it is important to work out various UV completions and study the detailed phenomenology
- More examples in DM physics which could not be covered here, lacking time

# Lesson from $\pi \rightarrow \mu \nu_\mu$

- The simplest guess for the EFT is not correct:

$$\mathcal{L}_{\text{eff}} \sim \pi \bar{\mu} \nu_\mu \quad (\text{dim-4}) \quad (\text{X})$$

- The correct guess is  $\mathcal{L}_{\text{eff}} \sim \partial_\mu \pi \bar{\mu} \gamma^\mu \nu$  (dim-5:OK)

- In the SM, the correct answer is dim-6 involving quarks,  $\sim \bar{u}_L \gamma_\mu d_L \mu_L \gamma^\mu \nu_L$

- We may have been doing something similar for DM physics too