

Linear Modeling of Baryon-Dark Matter Interactions with CLASS

Introducing a Novel Resonance Interaction Type

Markus Rasmussen Mosbech

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Overview

Interacting
Dark
Matter

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- 1 Evolution
- 2 Dark Matter Interactions
- 3 Numerics
- 4 Results

Structure Formation

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Evolution

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Interactions

Numerics

Results

- Primordial perturbations
- Gravity

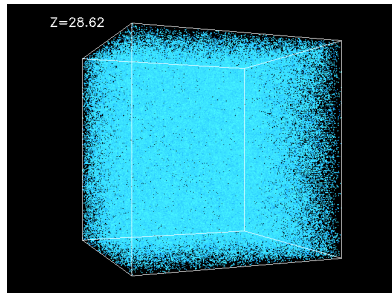


Figure: *simulations were performed at the National Center for Supercomputer Applications by Andrey Kravtsov (The University of Chicago) and Anatoly Klypin (New Mexico State University). Visualizations by Andrey Kravtsov.*

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- Primordial perturbations
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- Pressure

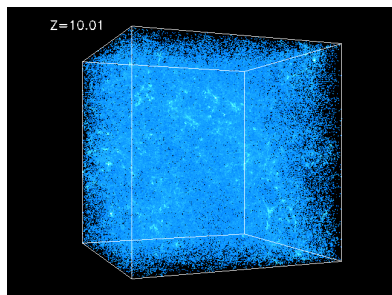


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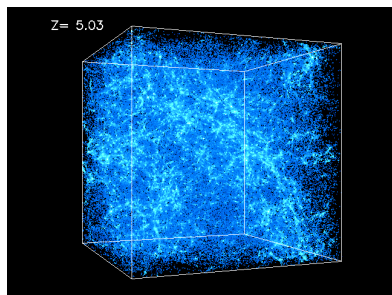


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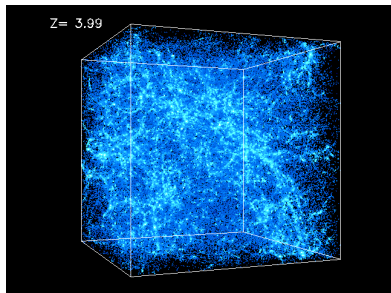


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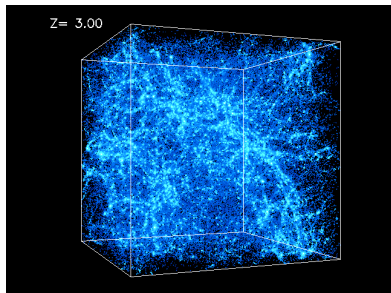


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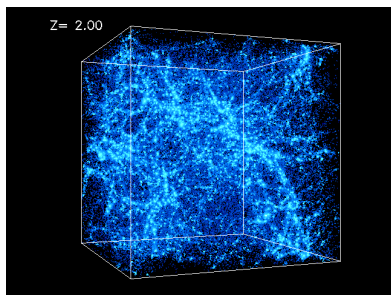


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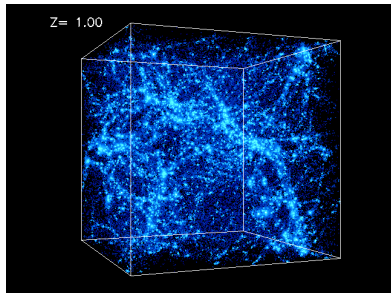


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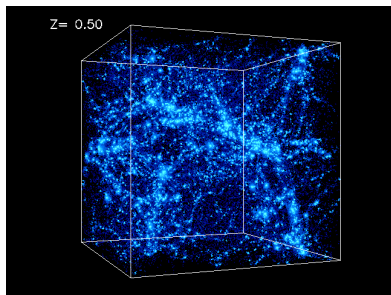


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The CMB spectrum

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- Observable

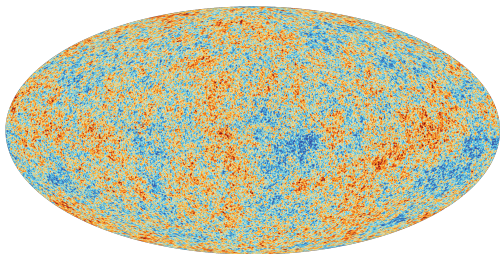


Figure: *by ESA/Planck collaboration*

The CMB spectrum

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Results

- Observable
- Recombination

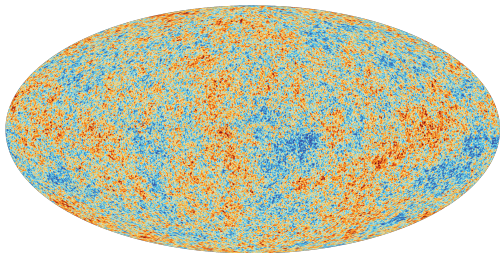


Figure: *by ESA/Planck collaboration*

The CMB spectrum

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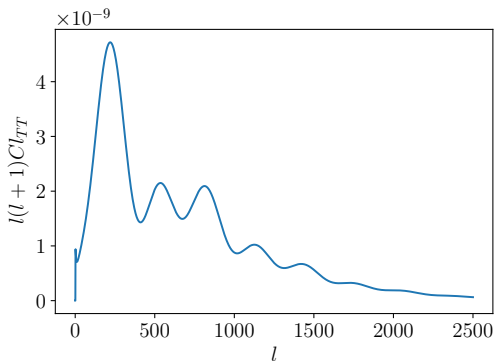
Evolution

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Interactions

Numerics

Results

- Observable
- Recombination
- Linear



Perturbation Theory

Interacting
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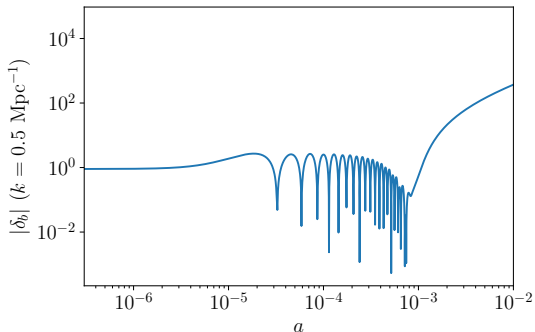
Evolution

DM
Interactions

Numerics

Results

- Small deviation from average



Perturbation Theory

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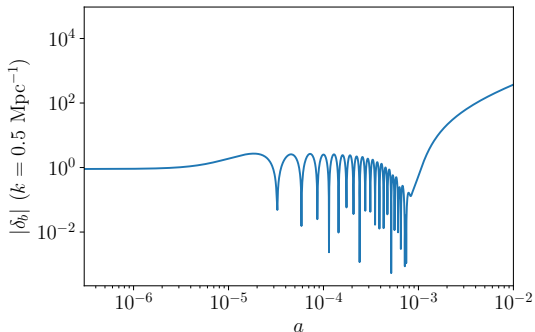
Evolution

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Numerics

Results

- Small deviation from average
- Early universe



Perturbation Theory

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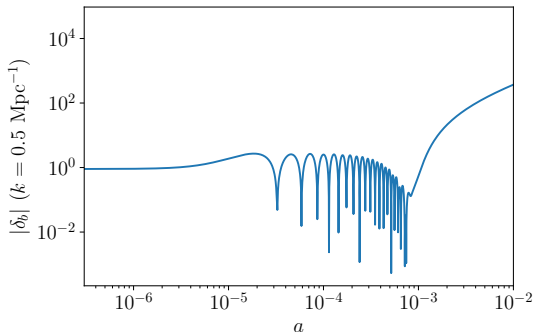
Evolution

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Numerics

Results

- Small deviation from average
- Early universe
- Advantages in Fourier space



The Boltzmann Equations

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Results

- Dark Matter

$$\dot{\delta}_{\text{cdm}} = -\theta_{\text{cdm}} + 3\dot{\Phi},$$

$$\dot{\theta}_{\text{cdm}} = -\frac{\dot{a}}{a}\theta_{\text{cdm}} + k^2\Psi.$$

The Boltzmann Equations

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Evolution

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Numerics

Results

- Dark Matter
- Baryons

$$\dot{\delta}_b = -\theta_b - 3\dot{\Phi},$$

$$\dot{\theta}_b = -\frac{\dot{a}}{a}\theta_b + c_s^2 k^2 \delta_b + \frac{4\bar{\rho}_\gamma}{3\bar{\rho}_b} a n_e \sigma_T (\theta_\gamma - \theta_b) + k^2 \Psi.$$

The Boltzmann Equations

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Evolution

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Results

- Dark Matter
- Baryons
- Photons

$$\dot{\delta}_\gamma = -\frac{4}{3}\theta_\gamma + 4\dot{\Phi}$$

$$\dot{\theta}_\gamma = k^2 \left(\frac{1}{4}\delta_\gamma - \sigma_\gamma \right)$$

$$+ an_e \sigma_T (\theta_b - \theta_\gamma) + k^2 \Psi$$

Temperature

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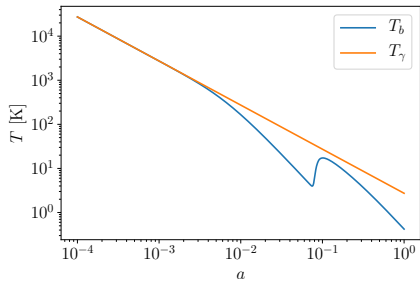
Evolution

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• Photons



Temperature

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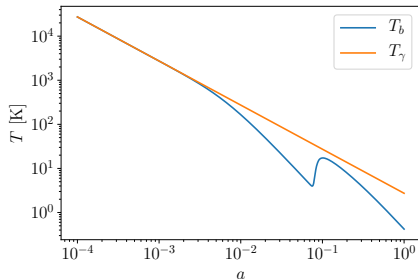
Evolution

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Results

- Photons
- Baryons



Temperature

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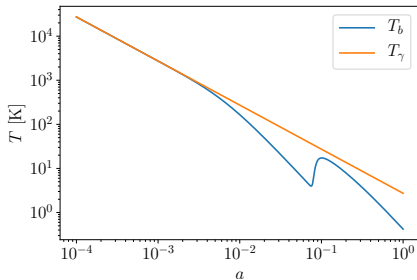
Evolution

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Numerics

Results

- Photons
- Baryons
- Cold dark matter



Temperature

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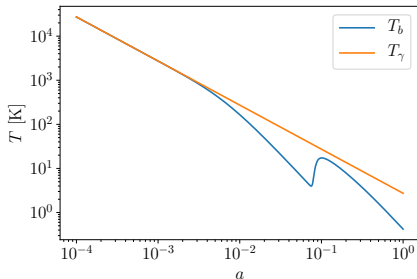
Evolution

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Results

- Photons
- Baryons
- Cold dark matter
- EDGES



Basic Premise

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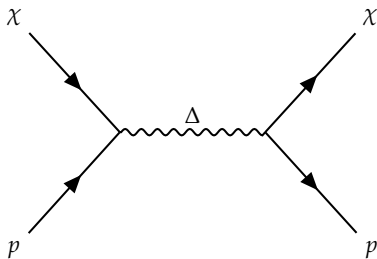
Evolution

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Interactions

Numerics

Results

- Nonzero interaction



Basic Premise

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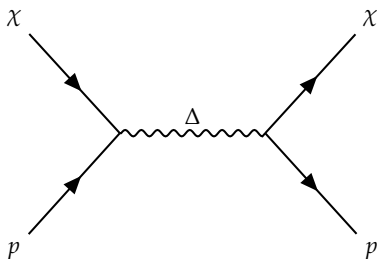
Evolution

DM
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Numerics

Results

- Nonzero interaction
- Velocity dependence



Basic Premise

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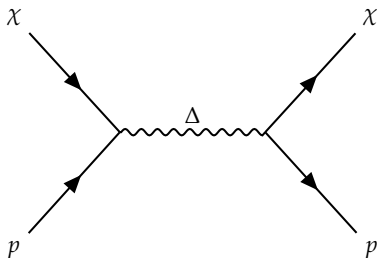
Evolution

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Numerics

Results

- Nonzero interaction
- Velocity dependence
- Nonzero temperature



Modified Boltzmann equations

Interacting
Dark
Matter

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Evolution

DM
Interactions

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Results

- Baryons

$$\begin{aligned}\dot{\delta}_b &= -\theta_b - 3\dot{\Phi}, \\ \dot{\theta}_b &= -\frac{\dot{a}}{a}\theta_b + c_s^2 k^2 \delta_b \\ &\quad + \frac{4\bar{\rho}_\gamma}{3\bar{\rho}_b} a n_e \sigma_T (\theta_\gamma - \theta_b) + k^2 \Psi. \\ &\quad + \frac{\rho_\chi}{\rho_b} R_\chi (\theta_\chi - \theta_b)\end{aligned}$$

$$R_\chi = \frac{a\rho_b}{m_\chi + m_H} \langle \sigma v \rangle \mathcal{F}_{\text{He}}$$

Modified Boltzmann equations

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Results

- Baryons
- Dark Matter

$$\begin{aligned}\dot{\delta}_{\text{cdm}} &= -\theta_{\text{cdm}} + 3\dot{\Phi}, \\ \dot{\theta}_{\text{cdm}} &= -\frac{\dot{a}}{a}\theta_{\text{cdm}} + k^2\Psi \\ &\quad + R_\chi(\theta_b - \theta_\chi)\end{aligned}$$

$$R_\chi = \frac{a\rho_b}{m_\chi + m_H} \langle\sigma v\rangle \mathcal{F}_{\text{He}}$$

Power Law Interaction

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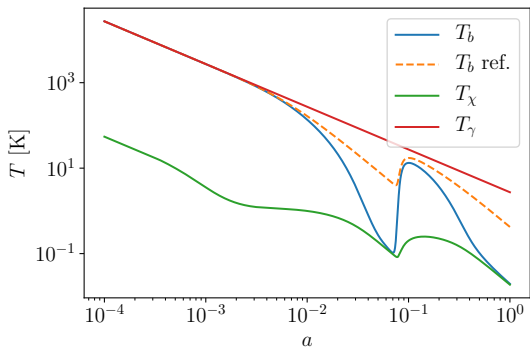
Evolution

DM
Interactions

Numerics

Results

- Coulomb



$$R_\chi = \frac{ac_n\rho_b\sigma_0}{m_\chi + m_H} \left(\frac{T_b}{m_H} + \frac{T_\chi}{m_\chi} + \frac{V_{\text{rms}}^2}{3} \right)^{\frac{n+1}{2}} \mathcal{F}_{\text{He}}$$

Power Law Interaction

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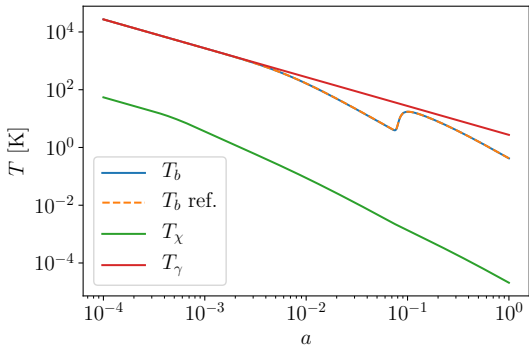
Evolution

DM
Interactions

Numerics

Results

- Coulomb
- Dipole



$$R_\chi = \frac{ac_n\rho_b\sigma_0}{m_\chi + m_H} \left(\frac{T_b}{m_H} + \frac{T_\chi}{m_\chi} + \frac{V_{\text{rms}}^2}{3} \right)^{\frac{n+1}{2}} \mathcal{F}_{\text{He}}$$

Resonance interaction

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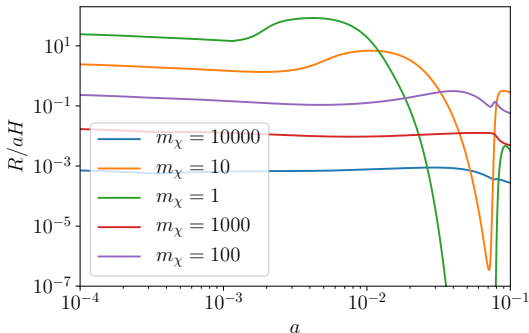
Evolution

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Results

- Assumptions



$$R_\chi = \frac{a\rho_b\sigma_0}{m_\chi + m_H} \frac{x_b x_\chi Q^{3/2}}{m_H m_\chi} K_1 \left(\frac{Q}{2} \sqrt{x_b x_\chi} \right) \mathcal{F}_{\text{He}}$$

Resonance interaction

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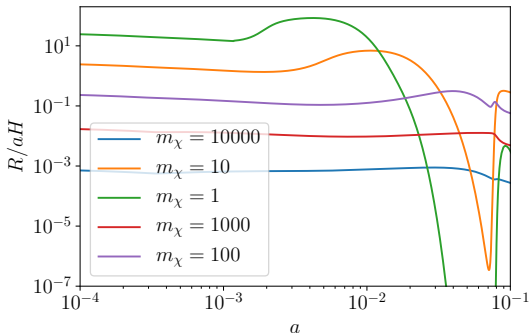
Evolution

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Results

- Assumptions
- Velocity dependence



$$R_\chi = \frac{a\rho_b\sigma_0}{m_\chi + m_H} \frac{x_b x_\chi Q^{3/2}}{m_H m_\chi} K_1 \left(\frac{Q}{2} \sqrt{x_b x_\chi} \right) \mathcal{F}_{\text{He}}$$

CLASS

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Numerics

Results

- Boltzmann solver



Figure: *from class-code.net*

CLASS

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- Boltzmann solver
- Linear



Figure: *from class-code.net*

CLASS

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Results

- Boltzmann solver
- Linear
- Modular



Figure: *from class-code.net*

Thermodynamics

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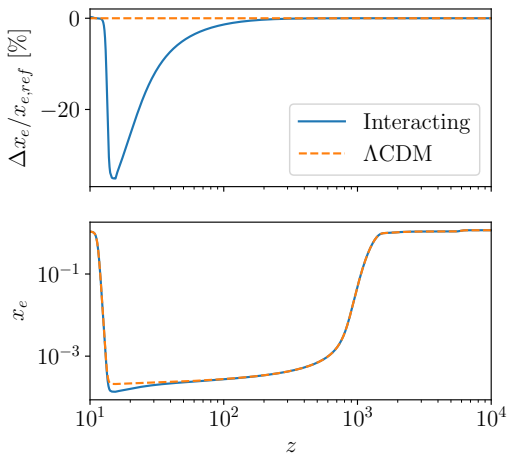
Evolution

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- Interactions



Thermodynamics

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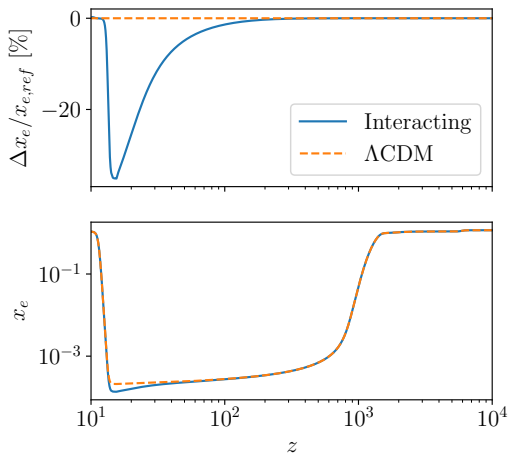
Evolution

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- Temperature



Thermodynamics

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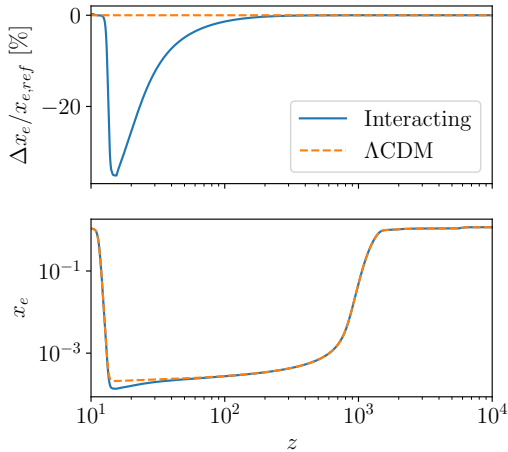
Evolution

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Results

- Interactions
- Temperature
- Recombination
+ reionisation



Perturbations

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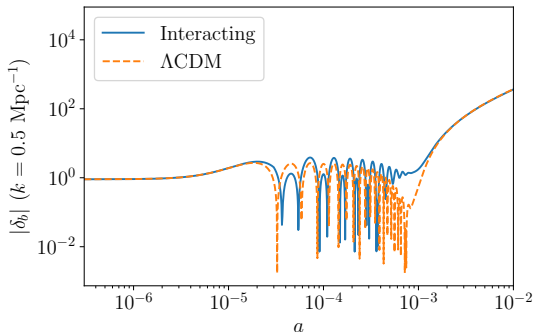
Evolution

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- Modified Boltzmann equations



Perturbations

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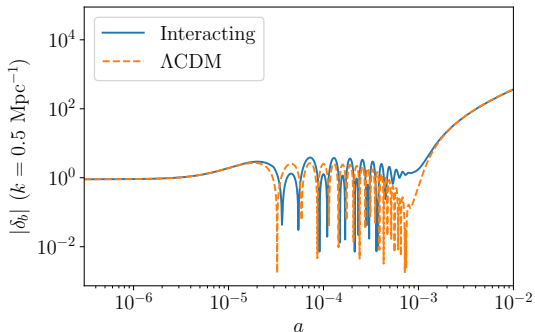
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- Modified Boltzmann equations
- Tight coupling approximation



Upper limit ΔCl_s

Interacting
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Matter

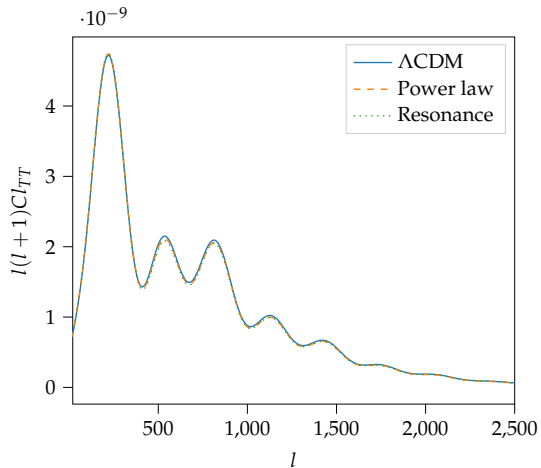
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Upper limit Δ Cl's

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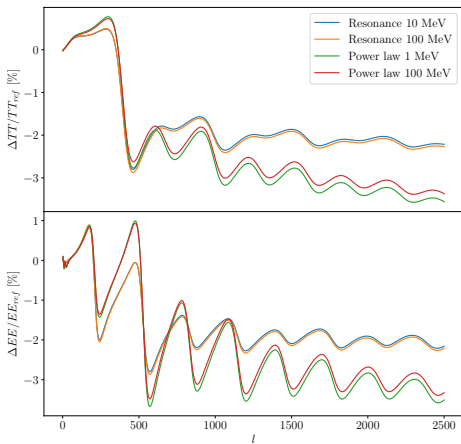
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Coulomb-like

Interacting
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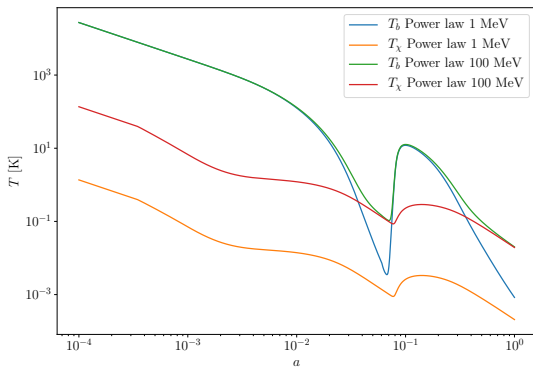
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Coulomb-like

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m_χ	1 MeV	100 MeV
σ_0 (95% CL.)	$2.2 \times 10^{-41} \text{ cm}^2$	$2.3 \times 10^{-41} \text{ cm}^2$
$T_b(z = 17.2)$	0.01 K	0.14 K

Resonance

Interacting
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Matter

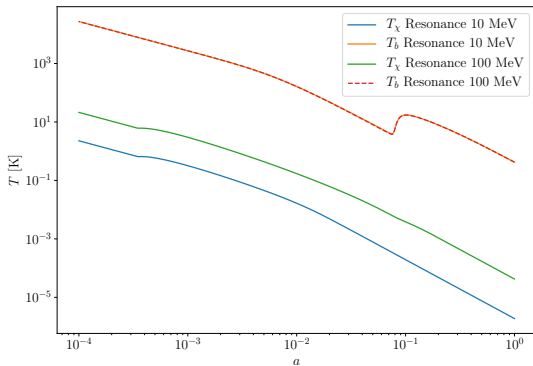
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Resonance

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m_χ	10 MeV	100 MeV
σ_0 (95% CL.)	5.2×10^{-9}	1.9×10^{-7}
$\tilde{\sigma}_0$ (95% CL.)	$1.2 \times 10^{-51} \text{ cm}^2$	$1.4 \times 10^{-52} \text{ cm}^2$
$T_b(z = 17.2)$	6.97 K	6.71 K

Further Results

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ϵ [MeV]	$m_\chi = 10$ MeV	$m_\chi = 100$ MeV
1×10^{-11}	$\sigma_0 = 1.05 \times 10^{-8}$	$\sigma_0 = 3.46 \times 10^{-7}$
1×10^{-10}	$\sigma_0 = 2.52 \times 10^{-9}$	$\sigma_0 = 8.36 \times 10^{-8}$
1×10^{-9}	$\sigma_0 = 1.39 \times 10^{-9}$	$\sigma_0 = 2.09 \times 10^{-8}$
1×10^{-8}	$\sigma_0 = 2.84 \times 10^{-9}$	$\sigma_0 = 1.61 \times 10^{-8}$
1×10^{-7}	$\sigma_0 = 9.88 \times 10^{-8}$	$\sigma_0 = 5.29 \times 10^{-8}$

ϵ [MeV]	$m_\chi = 1000$ MeV	$m_\chi = 5000$ MeV
1×10^{-11}	$\sigma_0 = 1.05 \times 10^{-5}$	$\sigma_0 = 1.25 \times 10^{-4}$
1×10^{-10}	$\sigma_0 = 2.59 \times 10^{-6}$	$\sigma_0 = 2.95 \times 10^{-5}$
1×10^{-9}	$\sigma_0 = 6.79 \times 10^{-7}$	$\sigma_0 = 7.09 \times 10^{-6}$
1×10^{-8}	$\sigma_0 = 1.93 \times 10^{-7}$	$\sigma_0 = 2.25 \times 10^{-6}$
1×10^{-7}	$\sigma_0 = 2.07 \times 10^{-7}$	$\sigma_0 = 2.52 \times 10^{-6}$

Table: *Inferred 95% confidence upper limits of σ_0 . Obtained with MontePython using Planck 2015 TT+TE+EE data.*

Further Results

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ϵ [MeV]	$m_\chi = 10$ MeV	$m_\chi = 100$ MeV
1×10^{-11}	$\tilde{\sigma}_0 = 4.43 \times 10^{-52} \text{ cm}^2$	$\tilde{\sigma}_0 = 5.29 \times 10^{-53} \text{ cm}^2$
1×10^{-10}	$\tilde{\sigma}_0 = 3.36 \times 10^{-52} \text{ cm}^2$	$\tilde{\sigma}_0 = 4.04 \times 10^{-52} \text{ cm}^2$
1×10^{-9}	$\tilde{\sigma}_0 = 5.86 \times 10^{-50} \text{ cm}^2$	$\tilde{\sigma}_0 = 3.19 \times 10^{-51} \text{ cm}^2$
1×10^{-8}	$\tilde{\sigma}_0 = 3.79 \times 10^{-48} \text{ cm}^2$	$\tilde{\sigma}_0 = 7.78 \times 10^{-50} \text{ cm}^2$
1×10^{-7}	$\tilde{\sigma}_0 = 4.17 \times 10^{-45} \text{ cm}^2$	$\tilde{\sigma}_0 = 8.08 \times 10^{-48} \text{ cm}^2$
ϵ [MeV]	$m_\chi = 1000$ MeV	$m_\chi = 5000$ MeV
1×10^{-11}	$\tilde{\sigma}_0 = 1.29 \times 10^{-53} \text{ cm}^2$	$\tilde{\sigma}_0 = 1.48 \times 10^{-53} \text{ cm}^2$
1×10^{-10}	$\tilde{\sigma}_0 = 1.00 \times 10^{-52} \text{ cm}^2$	$\tilde{\sigma}_0 = 1.10 \times 10^{-52} \text{ cm}^2$
1×10^{-9}	$\tilde{\sigma}_0 = 8.36 \times 10^{-52} \text{ cm}^2$	$\tilde{\sigma}_0 = 8.38 \times 10^{-51} \text{ cm}^2$
1×10^{-8}	$\tilde{\sigma}_0 = 7.52 \times 10^{-51} \text{ cm}^2$	$\tilde{\sigma}_0 = 8.41 \times 10^{-51} \text{ cm}^2$
1×10^{-7}	$\tilde{\sigma}_0 = 2.55 \times 10^{-49} \text{ cm}^2$	$\tilde{\sigma}_0 = 2.98 \times 10^{-49} \text{ cm}^2$

Table: *Inferred 95% confidence upper limits of $\tilde{\sigma}_0$. Obtained with MontePython using Planck 2015 TT+TE+EE data.*

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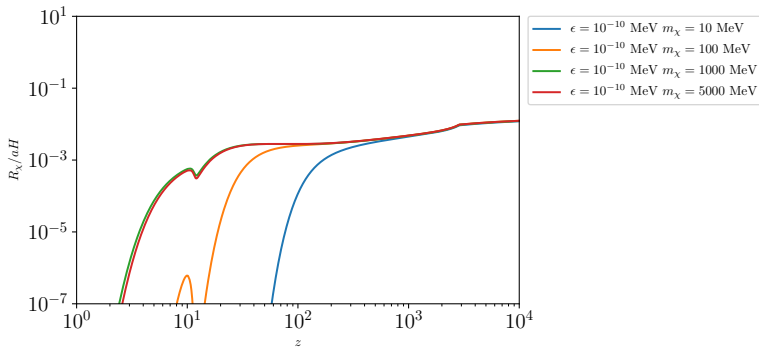


Figure: *The evolution of the momentum exchange rate R_χ for $\epsilon = 1 \times 10^{-10}$ MeV, using the inferred CMB upper limits for σ_0 .*

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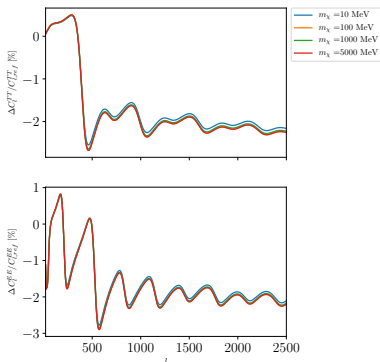


Figure: *Percent residuals of the TT (upper) and EE (lower) spectra with respect to Λ CDM for $\epsilon = 1 \times 10^{-10}$ MeV, using the inferred CMB upper limits for σ_0 .*

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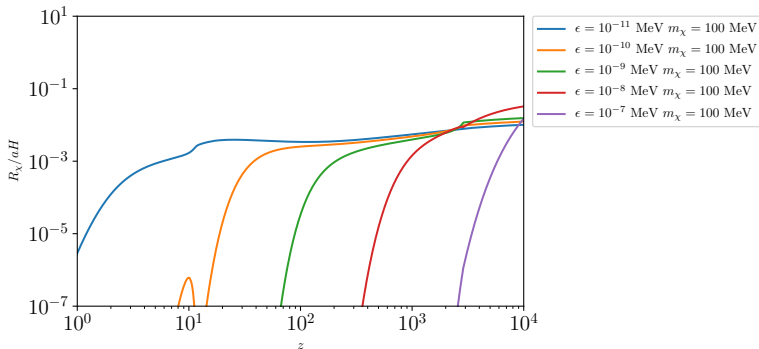


Figure: The evolution of the momentum exchange rate R_χ for $m_\chi = 100$ MeV, using the inferred CMB upper limits for σ_0 .

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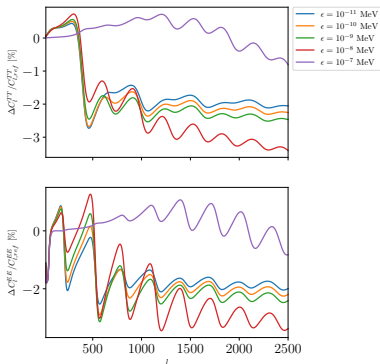


Figure: Percent residuals of the TT (upper) and EE (lower) spectra with respect to ΛCDM for $m_\chi = 100$ MeV, using the inferred CMB upper limits for σ_0 .

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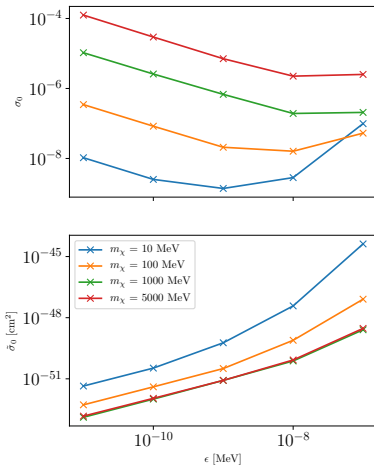


Figure: Inferred 95% upper limits for σ_0 (upper figure) and $\tilde{\sigma}_0$ (lower figure) as a function of ϵ for each tested m_χ .

Further Results

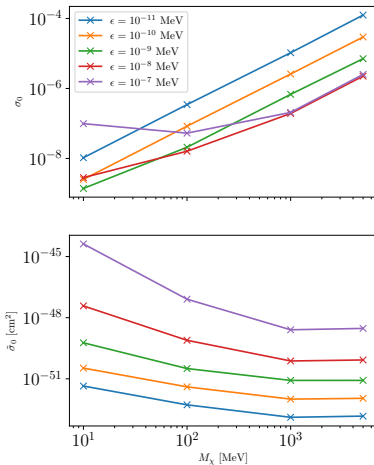


Figure: Inferred 95% upper limits for σ_0 (upper figure) and $\tilde{\sigma}_0$ (lower figure) as a function of m_χ for each tested ϵ .

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- Upper Limits

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- EDGES

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- EDGES
- Other constraints