# Mixed QCD-EW corrections to Z and W boson production and their impact on the W mass measurements at the LHC

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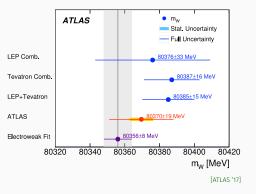
based on arxiv:1909.08428 [hep-ph], arxiv:2005.10221 [hep-ph], arxiv:2009.10386 [hep-ph] and arxiv:2103.02671 [hep-ph]

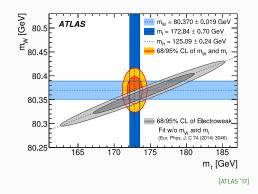
in collaboration with

- Federico Buccioni, Fabrizio Caola (Oxford)
- Maximilian Delto, Matthieu Jaquier, Kirill Melnikov (KIT)
- Raoul Röntsch (CERN)

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#### Precision W mass measurements

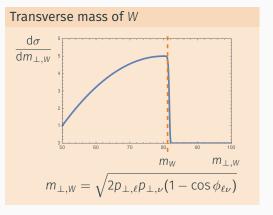


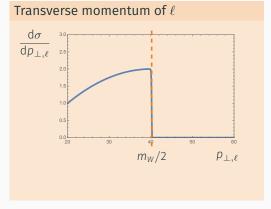


- High precision W mass measurements allow to cross-check the Standard Model
- ATLAS has measured  $m_W = (80\,370\pm19)\,\mathrm{MeV}$  [ATLAS '17]
- $\cdot$  ATLAS and CMS collaborations aim to reduce uncertainty to  $\mathcal{O}(10\,\text{MeV})$ 
  - ightarrow would rival precision from global electroweak fits
  - $\rightarrow$  would mean  $\mathcal{O}(0.01\%)$  uncertainty

# How to measure $m_W$ at hadron colliders

Need observables that are sensitive to  $m_W$ :



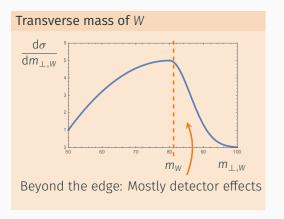


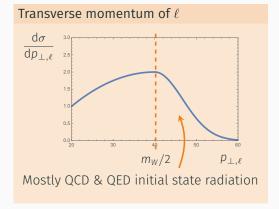
At LO and with idealized detectors both observables have sharp kinematic edges.

 $\rightarrow$  Very sensitive observables

# How to measure $m_W$ at hadron colliders

Need observables that are sensitive to  $m_W$ :





Starting from NLO and with realistic detectors the edges are washed out

# Theory predictions for $m_W$ measurements at hadron colliders

Standard tools (collinear factorisation, fixed-order perturbation theory, resummation, parton showers, ...) typically reach at most  $\mathcal{O}(1\%)$  uncertainties at N<sup>3</sup>LO.

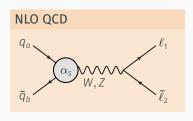
To measure  $m_W$  to a precision of  $\mathcal{O}(10 \,\text{MeV})$  we have to control theory uncertainties to a level of about  $\mathcal{O}(0.01\%)$ .

 $\rightarrow$  Straightforward application of standard tools falls short of required precision.

#### Consequences:

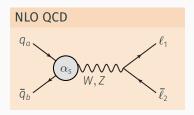
- 1. We cannot hope to predict distributions to this precision from first principles. Instead:
  - Measure Z distributions
  - · Parametrise them in QCD-motivated way
  - Transfer them to W distributions (bulk of QCD does not distinguish between W and Z)
- 2. Small effects that distinguish between Z and W bosons may matter.
  - $\rightarrow$  Electroweak corrections are obvious examples of such effects.

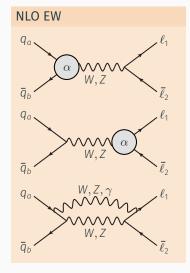
# Electroweak and QCD corrections to on-shell W and Z production



→ Only corrections to the initial state

# Electroweak and QCD corrections to on-shell W and Z production





 $\rightarrow$  initial state corrections

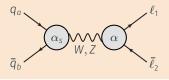
 $\rightarrow$  final state corrections

→ non-fact. corrections [Dittmaier, Huss, Schwinn '14]:

$$\sim \mathcal{O}\left(\alpha \frac{\Gamma}{m_V}\right) \sim \mathcal{O}\left(\alpha^2\right)$$

# Mixed QCD-EW corrections to on-shell W and Z production

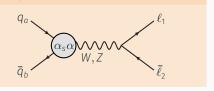
#### Mixed QCD-EW: Initial-Final



- Correction of NLO  $\otimes$  NLO type
- Previously investigated
   [Dittmaier, Huss, Schwinn '15] [Carloni Calame et al. '16]
- Estimated impact on m<sub>W</sub> measurement:

 $\delta m_W \sim \mathcal{O}(15 \, \text{MeV})$ 

#### Mixed QCD-EW: Initial-Initial

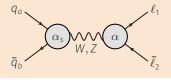


- Correction of NNLO type
- Generated lots of recent activity
  [De Florian, Der, Fabre '18] [Cieri, de Florian, Der, Mazzitelli '20]
  [Bonciani, Buccioni, Rana, Triscari, Vicini '19]
  [Bonciani, Buccioni, Rana, Vicini '20] [Dittmaier, Schmidt, Schwarz '20]
  [Heller, von Manteuffel, Schabinger, Spiesberger '20]
  [Buonocore, Grazzini, Kallweit, Savioni, Tramontano '21]
- Subject of this talk

[Delto, Jaquier, Melnikov, Röntsch '19] [Buccioni, Caola, Delto, Jaquier, Melnikov, Röntsch '20] [AB, Buccioni, Caola, Delto, Jaquier, Melnikov, Röntsch '20] [AB, Buccioni, Caola, Delto, Jaquier, Melnikov, Röntsch '21]

# Mixed QCD-EW corrections to on-shell W and Z production

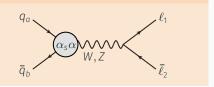
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#### Mixed OCD-EW: Initial-Initial



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- [De Florian, Der, Fabre '16] [Cipe 2021 n. Der, Mazzitelli '20]
  [Boncian Br. LoopFeSt 2021 n. Der, Mazzitelli '20]
  RADCOR Long Range (1998) · Generated lots of recent activity

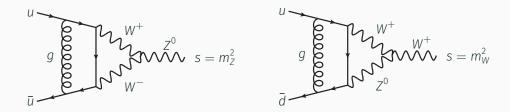
"Heller von Manarna Sankarmaier, Schmidt, Schwarz 20]

- Wed: Narayan Rana ontano '21] Thu: Luca Buonocore

IAB BERTILL Andreas von Manteuffel

Two-loop amplitudes

#### Form factors for on-shell W and Z bosons



What needs to be calculated?  $\rightarrow$  Only on-shell form factors (Narrow-width approximation simplifies the problem)

- · Z: Mixed QCD-EW corrections are known [Kotikov, Kühn, Veretin '07]
- W: Mixed QCD-EW corrections were not yet publicly available
  - ightarrow We calculated the missing integrals and completed the form factor

#### Calculation of the W form factor



This is a non-trivial, but tractable calculation.

**\*** 

35 master integrals 
$$I \sim \int \frac{[d^d k_1][d^d k_2]}{[k_2^2 - m_W^2] \dots [(k_2 - p_{12})^2 - m_Z^2]}$$

10 MI with internal W and Z

→ Calculated using differential equations

$$\partial_z I(z,\varepsilon) = A(z,\varepsilon)I(z,\varepsilon)$$
 with  $z = \frac{m_W^2}{m_Z^2}$ 

25 MI known in the literature

[Aglietti, Bonciani '03] [Aglietti, Bonciani '04] [Bonciani, Di Vita, Mastrolia, Schubert '16] with the equal mass case (z = 1) as boundary conditions

Results can be expressed in terms of well-understood iterated integrals (GPLs)

$$G_{a,\vec{b}}(y) = \int_0^y \frac{G_{\vec{b}}(t)}{t-a} dt$$
,  $G_a(y) = \int_0^y \frac{1}{t-a} dt$ ,  $G_0(y) = \ln(y)$ ,  $z = \frac{y}{(1+y)^2}$ 

# Analytic results for the W form factor

```
\Re \widetilde{\mathcal{M}}_{\mathrm{mix}} =
                     (Q_u^2 + Q_d^2)C_F\left[\frac{1}{\epsilon}\left(-\frac{3}{16} + \frac{1}{4}\pi^2 - 3\zeta_3\right) + \left(\frac{3}{8} - \frac{1}{2}\pi^2 + 6\zeta_3\right)\ln\left(\frac{M_W^2}{u^2}\right) + \frac{1}{4}\frac{(27z + 13)(1 - z)^2}{z^3}H_1(z)\right]
                        +\frac{(1-z)^2(1+z)}{z^3}\left(\frac{3}{4}H_1(z)\pi^2-\frac{9}{2}H_{1,0,0}(z)-\frac{9}{2}H_{1,0,1}(z)\right)-\frac{1}{4}\frac{(5z+3)(1-z)(1+z)}{z^3}H_{-1,0}(z)
                        +\frac{(1-z)(1+z)^2}{z^3}\left(-\frac{3}{2}H_{-1,-1,0}(z)+\frac{3}{2}H_{-1,0,0}(z)+3H_{-1,0,1}(z)+2H_{-1,-1,-1,0}(z)-2H_{-1,-1,0,0}(z)\right)
                        -6H_{-1,-1,0,1}(z) - 2H_{-1,0,-1,0}(z) + H_{-1,0,0,1}(z) + H_{0,-1,0,0}(z) + 4H_{0,-1,0,1}(z) + \left(-\frac{1}{4}H_{-1}(z) + \frac{1}{6}H_{-1,-1}(z) + \frac{1}{6}H_{-1
                        -\frac{1}{6}H_{0,-1}(z)\Big)\pi^2 - 3H_{-1}(z)\zeta_3\Big) + \frac{1}{32}\frac{7z^2 - 72z + 64}{z^2} + \frac{1}{24}\frac{50z^2 - 5z - 16}{z^2}\pi^2 - \frac{3}{2}\frac{8z^2 - z - 2}{z^2}\zeta_3 - \frac{11}{180}\pi^4
                     +\frac{(1-z)}{z^2}\left(\frac{1}{2}(9z+11)H_{0,1}(z)-\frac{1}{2}(3z+4)H_{0,0,1}(z)+\frac{1}{4}(23z+16)H_{0,0}(z)+(3z+2)\left(\frac{1}{2}H_{0,-1,0}(z)\right)\right)
                        -\frac{17}{8}H_0(z)\Big)\Big) + \frac{\left(z^2 + 3z + 1\right)(1-z)}{z^3} \left(\frac{1}{3}H_{0,1}(z)\pi^2 - 2H_{0,1,0,0}(z) - 2H_{0,1,0,1}(z)\right) \Big] + C_F\left[\frac{z+2}{1-z}\left(-\frac{1}{6}H_{0,0}(z)\pi^2 - 2H_{0,1,0,0}(z)\right)\right] + C_F\left[\frac{z+2}{1-z}\left(-\frac{1}{6}H_{0,0}(z)\pi^2 - 2H_{0,0}(z)\right)\right] + C_F\left[\frac{z+2}{1-z}\left(-\frac{1}{6}H_{0,0}(z)\pi^2 - 2H_{0,0}(z)\right]\right] + C_F\left[\frac{z+2}{1-z}\left(-\frac{1}{6}H_{0,0}(z)\pi^2 - 2H_{0,0}(z)\right]\right] + C_F\left[\frac{z+2}{1-z}\left(-\frac{1}{6}H_{0,0}(z)\pi^2 - 2H_{0,0}(z)\right]\right]
                          +4H_0(z)\zeta_3 + \frac{1}{8}\frac{(5z-2)(2z^2+12z+11)}{(1-z)z^2}H_{0,1}(z) + \frac{1}{8}\frac{43z^2+7z-16}{(1-z)z^2}H_{0,0}(z) - \frac{1}{48}\frac{10z^3+5z^2+20z-16}{(1-z)z^2}\pi^2
                          -\frac{1}{16}\frac{8z^3 + 142z^2 + 23z - 34}{(1-z)z^2}H_0(z) + \frac{1}{120}\frac{5z - 36}{1-z}\pi^4 - \frac{1}{8}\frac{4z^2 - 17z + 8}{(1-z)z^2} + \frac{2z^2 - 2z + 1}{(1-z)z^2}\left(\frac{1}{4}(3z + 4)H_{0,0,1}(z)\right)
                          +\left(3z+2\right)\left(-\frac{3}{4}\zeta_{3}-\frac{1}{4}H_{0,-1,0}(z)\right)+\frac{\left(2z^{2}-6z+3\right)\left(1+z\right)}{z^{3}}\left(\frac{3}{4}H_{1,0,0}(z)+\frac{3}{4}H_{1,0,1}(z)-\frac{1}{8}H_{1}(z)\pi^{2}\right)
                        -\frac{1}{(1-z)z}\left(\frac{1}{8}H_{0,0,0}(z)+\frac{1}{2}\left(9z^2-8z-2\right)\zeta_3+\frac{5}{48}H_0(z)\pi^2\right)+\frac{\left(2z^2-2z+1\right)(1+z)^2}{(1-z)z^3}\left(\frac{3}{4}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,0}(z)+\frac{1}{2}H_{-1,-1,
                        -\frac{3}{7}H_{-1,0,0}(z) - \frac{3}{9}H_{-1,0,1}(z) - H_{-1,-1,-1,0}(z) + H_{-1,-1,0,0}(z) + 3H_{-1,-1,0,1}(z) + H_{-1,0,-1,0}(z)
                        -\frac{1}{2}H_{-1,0,0,1}(z)-\frac{1}{2}H_{0,-1,0,0}(z)-2H_{0,-1,0,1}(z)+\Big(\frac{1}{8}H_{-1}(z)-\frac{1}{12}H_{-1,-1}(z)+\frac{1}{12}H_{0,-1}(z)\Big)\pi^2+\frac{3}{2}H_{-1}(z)\zeta_3\Big)
                        +\frac{1}{8}\frac{4z^{3}+64z^{2}-z-13}{z^{3}}H_{1}(z)+\frac{1}{8}\frac{\left(5z+3\right)\left(2z^{2}-2z+1\right)\left(1+z\right)}{\left(1-z\right)^{-3}}H_{-1,0}(z)+\frac{z^{4}-4z^{2}+z+1}{\left(1-z\right)^{-3}}\left(H_{0,1,0,0}(z)+\frac{z^{4}-4z^{2}+z+1}{2z^{2}-2z+1}\right)H_{-1,0}(z)
                        +H_{0,1,0,1}(z) - \frac{1}{6}H_{0,1}(z)\pi^2 + \left[\frac{\sqrt{4z-1}}{8\pi}\left(-\frac{10z+3}{1-z}(H_r(z^{-1})-\pi)-(\pi H_0(z)+H_{0,r}(z^{-1}))+\frac{17z+4}{1-z}H_{r,0}(z^{-1})\right)\right]
                        -\frac{6z+1}{1-z}(i\pi^2-3i\pi H_r(z^{-1})-3H_{r,1}(z^{-1}))\right)-\frac{1}{8}\frac{3z+2}{(1-z)z}(H_{r,r}(z^{-1})-\pi H_r(z^{-1}))-\frac{1}{8}\frac{30z^2-20z-1}{(1-z)z}H_{r,r,0}(z^{-1})
                        +\frac{1}{8}\frac{1}{(1-z)^{2}}(H_{0,r,r}(z^{-1})-\pi H_{0,r}(z^{-1}))-\frac{1}{8}\frac{6z^{2}-4z+1}{(1-z)^{2}}(H_{r,0,r}(z^{-1})-\pi H_{r,0}(z^{-1}))+\frac{1}{2}\frac{3z-2}{1-z}\left(-3H_{r,r,1}(z^{-1})-\pi H_{r,0}(z^{-1})\right)
                        -3 i \pi H_{r,r}(z^{-1})+i \pi^2 H_r(z^{-1})-i \frac{\pi^3}{6} \Big)+\frac{z+2}{1-z} \Big(i \frac{\pi^3}{6} H_0(z)+i \pi^2 H_{0,r}(z^{-1})-3 i \pi H_{0,r,r}(z^{-1})-3 H_{0,r,r,0}(z^{-1}) \Big)
                        -3H_{0,r,r,1}(z^{-1}) - 4i\pi\zeta_3
```

The analytic result is now available and even reasonably compact.

Non-factorising part of finite remainder becomes this simple when expressed in terms of iterated integrals over  $z=\frac{m_W^2}{m_Z^2}$ 

$$H_{a,\vec{b}}(z) = \int_0^z f_a(t) H_{\vec{b}}(t) dt$$

with HPL- and square root letters

$$f_1(t) = \frac{1}{1-t}, \quad f_0(t) = \frac{1}{t},$$
  
 $f_{-1}(t) = \frac{1}{1+t}, \quad f_r(t) = \frac{1}{\sqrt{t(4-t)}}$ 

# Subtraction

# Infrared singularities

Cross-sections develop IR singularities in soft and collinear limits of massless particles → cancel between real and virtual corrections

· Use a subtraction scheme to make poles from real radiation explicit

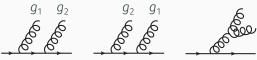
- Build on progress with NNLO QCD subtraction schemes to tackle mixed QCD-EW corrections (here: nested soft-collinear subtraction scheme)
  - · Z: Abelianisation of NNLO QCD subtraction is sufficient
  - W: New contributions from radiating W bosons

# Subtraction for mixed QCD-EW corrections: triple-collinear limits

We can make use of simplifications compared to NNLO QCD.

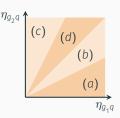
#### Triple-collinear limits

• NNLO QCD: Overlapping singularities in triple-collinear limits



ightarrow Needs 4 sectors to disentangle collinear singularities

$$\eta_{ij} = \frac{1}{2}(1-\cos\theta_{ij})$$

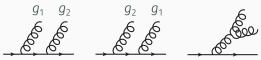


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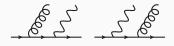
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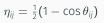


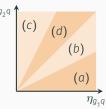
- ightarrow Needs 4 sectors to disentangle collinear singularities
- Mixed QCD-EW: Collinear limit of photon and gluon is not singular

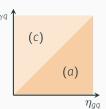


 $\rightarrow$  2 sectors can be dropped in  $q\bar{q}$  channel

Overall: No new collinear limits arise compared to NNLO QCD







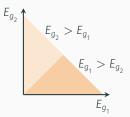
#### Subtraction for mixed QCD-EW corrections: double-soft limits

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#### Double-soft limits

- · NNLO QCD: Overlapping singularities in the double-soft limit
  - · Non-trivial double-soft eikonal function
  - Distinguish rates at which energies of soft particles vanish

$$1 = \theta(E_{g_1} - E_{g_2}) + \theta(E_{g_2} - E_{g_1})$$



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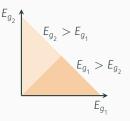
$$1 = \theta(E_{g_1} - E_{g_2}) + \theta(E_{g_2} - E_{g_1})$$

- Mixed QCD-EW: Soft gluons and photons are not entangled
  - $\cdot$  Double-soft limit factorises into NLO QCD imes NLO QED

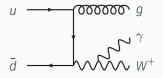
$$\lim_{E_g, E_{\gamma} \to 0} |\mathcal{M}_{Wg\gamma}|^2 = g_s^2 \operatorname{Eik}_g(p_u, p_{\bar{d}}; p_g) e^2 \operatorname{Eik}_{\gamma}(p_u, p_{\bar{d}}, p_W; p_{\gamma}) |\mathcal{M}_W|^2$$

$$\operatorname{Eik}_g(p_u, p_{\bar{d}}; p_g) = 2C_F \frac{(p_u \cdot p_{\bar{d}})}{(p_u \cdot p_g)(p_g \cdot p_{\bar{d}})}$$

• No need to distinguish  $E_g > E_\gamma$  vs.  $E_\gamma > E_g$ 



# Subtraction for mixed QCD-EW corrections: radiating W bosons



New contribution compared to NNLO QCD: W bosons can radiate photons

- Mass of W boson prevents collinear singularities
- · Soft limit of photon is still singular
  - · Requires soft eikonal function for massive emitter
  - QCD and QED factorise in soft limit ightarrow only NLO eikonal functions necessary

$$\begin{aligned} \mathsf{Eik}_{\gamma}(p_{u}, p_{\bar{d}}, p_{W}; p_{\gamma}) &= \left\{ Q_{u} Q_{d} \frac{2(p_{u} \cdot p_{\bar{d}})}{(p_{u} \cdot p_{\gamma})(p_{\bar{d}} \cdot p_{\gamma})} - Q_{W}^{2} \frac{p_{W}^{2}}{(p_{W} \cdot p_{\gamma})^{2}} \right. \\ &\left. + Q_{W} \left( Q_{u} \frac{2(p_{W} \cdot p_{u})}{(p_{W} \cdot p_{\gamma})(p_{u} \cdot p_{\gamma})} - Q_{d} \frac{2(p_{W} \cdot p_{\bar{d}})}{(p_{W} \cdot p_{\gamma})(p_{\bar{d}} \cdot p_{\gamma})} \right) \right\} \end{aligned}$$

Estimates for impact on W mass

# Results for W production: Cross sections for $pp o W^+ o e^+ u_e$

- We include only initial-initial contributions
- Write cross section as  $\sigma = \sigma_{\rm LO} + \delta\sigma_{\rm NLO}^{\rm QCD} + \delta\sigma_{\rm NLO}^{\rm EW} + \delta\sigma_{\rm NNLO}^{\rm QCD-EW} + \dots$

$\sigma$ [pb]	$\mu = m_{\rm W}$	$\mu = m_W/2$	$\mu=m_W/4$
$\sigma_{LO}$	6007.6	5195.0	4325.9
$\delta\sigma_{NLO}^{QCD}$	508.8	1137.0	1782.2
$\delta\sigma_{NLO}^{EW}$	2.1	-1.0	-2.6
$\delta\sigma_{ m NNLO}^{ m QCD-EW}$	-2.4	-2.3	-2.8

 $\bar{q}_{a}$   $\bar{q}_{b}$   $\alpha_{s}$  W,Z  $\bar{\ell}_{2}$   $q_{a}$   $q_{a}$ 

Results for: 13 TeV LHC,  $G_{\mu}$  scheme,

 $\mu_{\rm R} = \mu_{\rm F} = \mu \in \{m_{\rm W}, m_{\rm W}/2, m_{\rm W}/4\}\text{,}$ 

NNPDF3.1luxQED

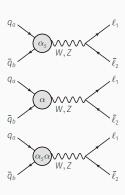
Selection criteria:  $p_{T,e} > 15 \text{ GeV}$ ,  $p_{T,\text{miss}} > 15 \text{ GeV}$ ,  $-2.4 < y_e < 2.4$ .

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• NLO EW corrections are tiny O(0.02%) (mostly due to  $G_{\mu}$  scheme)

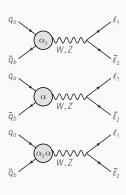


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$\delta\sigma_{ m NNLO}^{ m QCD-EW}$	-2.4	-2.3	-2.8

• Mixed QCD-EW corrections are very small, about  $\mathcal{O}(0.05\%)$ , but not obviously irrelevant for  $m_W$  measurements at the LHC



### Estimate W mass shifts from mixed QCD-EW corrections

Objective: Estimate impact of new corrections on W boson mass

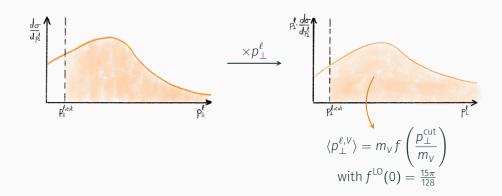
#### Considerations:

- Should combine W and Z measurements
  - → model what is done in experiments
  - $\rightarrow$  make use of available precision for Z mass
- · Should be physically and conceptually simple and transparent
- · Should be accessible with our calculations

#### Construction of our observable

We use the average transverse momentum of the charged lepton (V = W, Z):

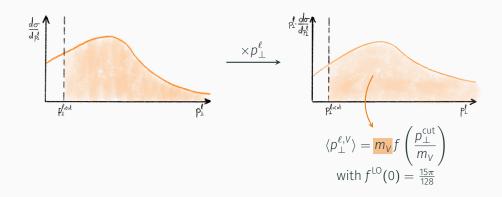
$$\langle p_{\perp}^{\ell,V} \rangle = \frac{\int d\sigma_{V} \times p_{\perp}^{\ell}}{\int d\sigma_{V}}$$



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$$\langle p_{\perp}^{\ell,V} \rangle = \frac{\int d\sigma_{V} \times p_{\perp}^{\ell}}{\int d\sigma_{V}}$$



Use the average lepton  $p_{\perp}$  in W and Z production as well as the Z mass to construct an observable for the W mass:

$$m_W^{\text{meas}} = \frac{\langle p_{\perp}^{\ell,W} \rangle^{\text{meas}}}{\langle p_{\perp}^{\ell,Z} \rangle^{\text{meas}}} m_Z C_{\text{th}}$$

Use the average lepton  $p_{\perp}$  in W and Z production as well as the Z mass to construct an observable for the W mass:

Measurement from LHC

$$m_W^{\text{meas}} = \frac{\langle p_{\perp}^{\ell,W} \rangle^{\text{meas}}}{\langle p_{\perp}^{\ell,Z} \rangle^{\text{meas}}} m_Z C_{\text{th}}$$

$$0 < m_Z$$

Measurement from LHC

Use the average lepton  $p_{\perp}$  in W and Z production as well as the Z mass to construct an observable for the W mass:

Measurement from LEP 
$$m_W^{\rm meas} = \frac{\langle p_\perp^{\ell,W} \rangle^{\rm meas}}{\langle p_\perp^{\ell,Z} \rangle^{\rm meas}} \frac{1}{m_Z} C_{\rm th}$$

Use the average lepton  $p_{\perp}$  in W and Z production as well as the Z mass to construct an observable for the W mass:

$$m_W^{\rm meas} = \frac{\langle p_\perp^{\ell,W} \rangle^{\rm meas}}{\langle p_\perp^{\ell,Z} \rangle^{\rm meas}} \, m_Z \, \frac{C_{\rm th}}{}$$

Theoretical correction factor

Use the average lepton  $p_{\perp}$  in W and Z production as well as the Z mass to construct an observable for the W mass:

$$m_W^{\rm meas} = \frac{\langle p_\perp^{\ell,W} \rangle^{\rm meas}}{\langle p_\perp^{\ell,Z} \rangle^{\rm meas}} \, m_Z \, C_{\rm th}$$

Theoretical correction factor

$$ightarrow$$
 Calculate via  $C_{
m th} = rac{m_W}{m_Z} rac{\langle p_\perp^{\ell,Z} 
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m th} = rac{m_W}{m_Z} rac{\langle p_\perp^{\ell,Z} 
angle^{
m th}}{\langle p_\perp^{\ell,W} 
angle^{
m th}}$ 

Adding a new correction to the theory

- $\rightarrow$  changes  $C_{\text{th}}$
- $\rightarrow$  changes extracted mass  $m_W^{\text{meas}}$

$$\frac{\delta m_W^{\text{meas}}}{m_W^{\text{meas}}} = \frac{\delta C_{\text{th}}}{C_{\text{th}}} = \frac{\delta \langle p_{\perp}^{\ell,Z} \rangle}{\langle p_{\perp}^{\ell,Z} \rangle} - \frac{\delta \langle p_{\perp}^{\ell,W} \rangle}{\langle p_{\perp}^{\ell,W} \rangle}$$

#### Shift on W mass

Estimates for shifts on 
$$W$$
 mass measurement via  $\delta m_W = \left(\frac{\delta \langle p_\perp^{\ell,Z} \rangle}{\langle p_\perp^{\ell,Z} \rangle} - \frac{\delta \langle p_\perp^{\ell,W} \rangle}{\langle p_\perp^{\ell,W} \rangle}\right) m_W$ 

	Inclusive	Fiducial cuts	Tuned cuts
NLO EW	1 MeV	3 MeV	−3 MeV
Mixed QCD-EW	−7 MeV	−17 MeV	−1 MeV

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Mixed QCD-EW corrections appear to have larger impact than NLO EW corrections

- +  $G_{\mu}$  input parameter scheme reduces size of NLO EW corrections
- Strong cancellation between changes in Z and W

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$$\delta m_W = \begin{pmatrix} \delta p_\perp^{\ell} \rangle & -\frac{\delta \langle p_\perp^{\ell,W} \rangle}{\langle p_\perp^{\ell,W} \rangle} \end{pmatrix} m_W \qquad \begin{array}{c} \text{NLO EW:} & \delta m_W \approx -31 \, \text{MeV} \\ \text{Mixed QCD-EW:} & \delta m_W \approx 54 \, \text{MeV} \\ \end{pmatrix}$$

## Shift on W mass

Estimates for shifts on W mass measurement via 
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- Cuts inspired by [ATLAS '17] analysis
- · Larger shifts than for inclusive setup

# W production:

$$p_{\perp}^{e^+} > 30 \, \text{GeV}$$

• 
$$p_{\perp}^{\text{miss}} > 30 \,\text{GeV}$$

$$\cdot \ |\eta_{e^+}| <$$
 2.4

• 
$$m_T^W > 60 \,\mathrm{GeV}$$

## Z production:

• 
$$p_{\perp}^{e^{\pm}} > 25 \,\text{GeV}$$

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NLO EW	1 MeV	3 MeV	−3 MeV
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- Cuts inspired by [ATLAS '17] analysis
- · Larger shifts than for inclusive setup
  - Relevant momenta:  $p_{\perp}^{e^{+}}/M_{V}$
  - ATLAS applies larger  $p_{\perp}^{e^{+}}$  cuts to W bosons than to Z bosons
  - Leads to small decorrelation between
     W and Z bosons

# W production:

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$$p_{\perp}^{e^{+}} > 30 \,\text{GeV}$$

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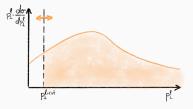
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# Shift on W mass

Estimates for shifts on W mass measurement via  $\delta m_W = \left(\frac{\delta \langle p_\perp^{\ell,Z} \rangle}{\langle p_\perp^{\ell,Z} \rangle} - \frac{\delta \langle p_\perp^{\ell,W} \rangle}{\langle p_\perp^{\ell,W} \rangle}\right) m_W$ 

	Inclusive	Fiducial cuts	Tuned cuts
NLO EW	1 MeV	3 MeV	−3 MeV
Mixed QCD-EW	−7 MeV	−17 MeV	−1 MeV

- · Size of shifts strongly depends on fiducial cuts
- Tune cuts  $(p_{\perp}^{e^+} \text{ from } W^+)$  such that  $C_{\text{th}} = 1$  at LO
- Impact of mixed QCD-EW gets reduced a lot
- → Fiducial cuts are an important factor for impact of mixed QCD-EW corrections



# Conclusions

#### Conclusions

- We calculate mixed QCD-EW corrections to fully-differential on-shell W and Z production at the LHC.
  - ightarrow Possible thanks to progress on amplitude calculations and subtraction schemes.
- Size of mixed QCD-EW corrections to the production part is  $\mathcal{O}(0.5)\%$ .
  - $\rightarrow$  Corrections are small but in line with expectations.
- Experimental measurements of  $m_W$  rely on similarity between W and Z distributions. Based on this, we build a transparent and simple model to estimate shifts on  $m_W$  via

$$\delta m_{W} = \left(\frac{\delta \langle p_{\perp}^{\ell,Z} \rangle}{\langle p_{\perp}^{\ell,Z} \rangle} - \frac{\delta \langle p_{\perp}^{\ell,W} \rangle}{\langle p_{\perp}^{\ell,W} \rangle}\right) m_{W}.$$

- We find that mixed QCD-EW corrections induce shifts on  $m_W$  that are comparable or larger than the target precision of  $\mathcal{O}(10)$  MeV.
- Further investigations on the impact of mixed QCD-EW corrections on  $m_W$  are clearly warranted. They should reflect all relevant details of experimental analyses.



## Infrared structure of the W form factor

The result for the form factor can be brought into a compact form.

Infrared poles are predicted by a "Catani-like" formula:

$$\begin{split} \left\langle F_{\text{LVV}+\text{LV}^2}^{\text{QCD} \otimes \text{EW}} \right\rangle &= \left( \frac{\alpha_{\text{S}}(\mu)}{2\pi} \frac{\alpha_{\text{EW}}}{2\pi} \right) \left[ I_{12,\text{QCD}} \cdot I_{12,\text{EW}} + \frac{e^{\varepsilon \gamma_{\text{E}}}}{\Gamma(1-\varepsilon)} \frac{H_{\text{QCD} \otimes \text{EW}}^W}{\varepsilon} \right] \left\langle F_{\text{LM}} \right\rangle \\ &+ \left( \frac{\alpha_{\text{S}}(\mu)}{2\pi} \right) I_{12,\text{QCD}} \left\langle F_{\text{LV}}^{\text{fin,EW}} \right\rangle + \left( \frac{\alpha_{\text{EW}}}{2\pi} \right) I_{12,\text{EW}} \left\langle F_{\text{LV}}^{\text{fin,QCD}} \right\rangle \\ &+ \left\langle F_{\text{LVV}+\text{LV}^2}^{\text{fin,QCD} \otimes \text{EW}} \right\rangle. \end{split}$$

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Building blocks:

$$\begin{split} I_{12,\text{QCD}} &= \left[\frac{e^{\varepsilon \gamma_E}}{\Gamma(1-\varepsilon)}\right] \left(\frac{\mu^2}{M_W^2}\right)^{\varepsilon} \left[-2C_F \cos(\pi \varepsilon) \left(\frac{1}{\varepsilon^2} + \frac{3}{2\varepsilon}\right)\right] \\ I_{12,\text{EW}} &= \left[\frac{e^{\varepsilon \gamma_E}}{\Gamma(1-\varepsilon)}\right] \left(\frac{\mu^2}{M_W^2}\right)^{\varepsilon} \left[-Q_u Q_d \cos(\pi \varepsilon) \left(\frac{2}{\varepsilon^2} + \frac{3}{\varepsilon}\right) + (Q_d - Q_u) Q_W \left(\frac{1}{\varepsilon^2} + \frac{5}{2\varepsilon}\right)\right] \\ H_{\text{QCD} \otimes \text{EW}}^W &= C_F \left[Q_u^2 + Q_d^2\right] \left(\frac{\pi^2}{2} - 6\zeta_3 - \frac{3}{8}\right) \end{split}$$

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- $\cdot$  Pole structure almost factorises into NLO QCD imes NLO EW
- Finite remainder  $\left\langle F_{\text{LW}+\text{LV}^2}^{\text{fin,QCD}\otimes \text{EW}}\right\rangle$  also consists of a factorising (NLO QCD  $\times$  NLO EW) and a non-factorising part

# Input parameters

#### Input parameters used:

 $m_t = 173.2 \,\text{GeV}$ 

$$G_F = 1.16639 \times 10^{-5} \text{ GeV}^{-2}$$
  
 $m_Z = 91.1876 \text{ GeV}$   
 $m_W = 80.398 \text{ GeV}$   
 $m_H = 125 \text{ GeV}$ 

- $\cdot$  We use the  $G_{\mu}$  input parameter scheme.
- PDFs: NNLO set NNPDF3.1luxQED with  $\alpha_{\rm S}(m_{\rm Z})=$  0.118
- Simulations for 13 TeV LHC
- Central scale:  $\mu_R = \mu_F = m_V/2$

## Detailed results for cross-sections and moments

Results for the cross-sections and average transverse momentum of the charged lepton for the inclusive setup of  $pp \to Z \to e^+e^-$  and  $pp \to W^+ \to e^+\nu_e$  (corrections only to the production part)

$$d\sigma_{Z,W} = \sum_{i,j=0} \alpha_s^i \alpha_W^i d\sigma_{Z,W}^{i,j} \qquad \qquad F_{Z,W}(i,j,\mathcal{O}) = \alpha_s^i \alpha_W^i \int d\sigma_{Z,W}^{i,j} \times \mathcal{O}$$

	V = Z		$V = W^+$			
	$\mu = m_Z/4$	$\mu = m_Z/2$	$\mu = m_Z$	$\mu = m_W/4$	$\mu=m_W/2$	$\mu=m_{\rm W}$
$F_V(0,0;1), [pb]$ $F_V(1,0;1), [pb]$ $F_V(0,1;1), [pb]$ $F_V(1,1;1), [pb]$	$ 1273 $ $ 570.2 $ $ -5810 \cdot 10^{-3} $ $ -2985 \cdot 10^{-3} $	$   \begin{array}{r}     1495 \\     405.4 \\     -6146 \cdot 10^{-3} \\     -2033 \cdot 10^{-3}   \end{array} $	$   \begin{array}{r}     1700 \\     246.9 \\     -6073 \cdot 10^{-3} \\     -1236 \cdot 10^{-3}   \end{array} $	$7434$ $3502$ $-1908 \cdot 10^{-3}$ $-8873 \cdot 10^{-3}$	8810 2533 3297 · 10 <sup>-3</sup> -7607 · 10 <sup>-3</sup>	10083 1580 10971 · 10 <sup>-3</sup> -7556 · 10 <sup>-3</sup>
$F_V(0,0; p_{\perp}^e)$ [GeV pb] $F_V(1,0; p_{\perp}^e)$ [GeV pb] $F_V(0,1; p_{\perp}^e)$ [GeV pb] $F_V(1,1; p_{\perp}^e)$ [GeV pb]	42741 23418 182.85 163.87	50191 17733 —192.77 —125.22	57073 12221 —189.11 —92.05	220031 124487 74.53 -553.87	260772 95132 243.54 482.0	298437 66090 484.82 —448.0

# Detailed results for W mass shifts

Detailed results for the shifts  $\delta m_W$  for different setups, orders and scales

$\delta m_W$ [MeV]		$\mu = m_V/4$	$\mu = m_V/2$	$\mu = m_V$
Inclusive	NLO EW	−0.1	0.3	0.2
	QCD-EW	−5.1	-7.5	-9.3
Fiducial	NLO EW	0.2	2.3	4.2
	QCD-EW	-16	—17	—19
Tuned fiducial	NLO EW	-4.4	-2.5	-0.8
	QCD-EW	3.9	-1.0	-5.7