

# Radcor & LoopFest

15th International Symposium  
on Radiative Corrections

XIX Workshop on Radiative  
Corrections for the LHC and  
Future Colliders

17-21 May, 2021, FSU, Tallahassee, FL, USA

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## NEW FRONTIERS IN THE DETERMINATION OF PDFS AT THE LHC



European Research Council

Established by the European Commission

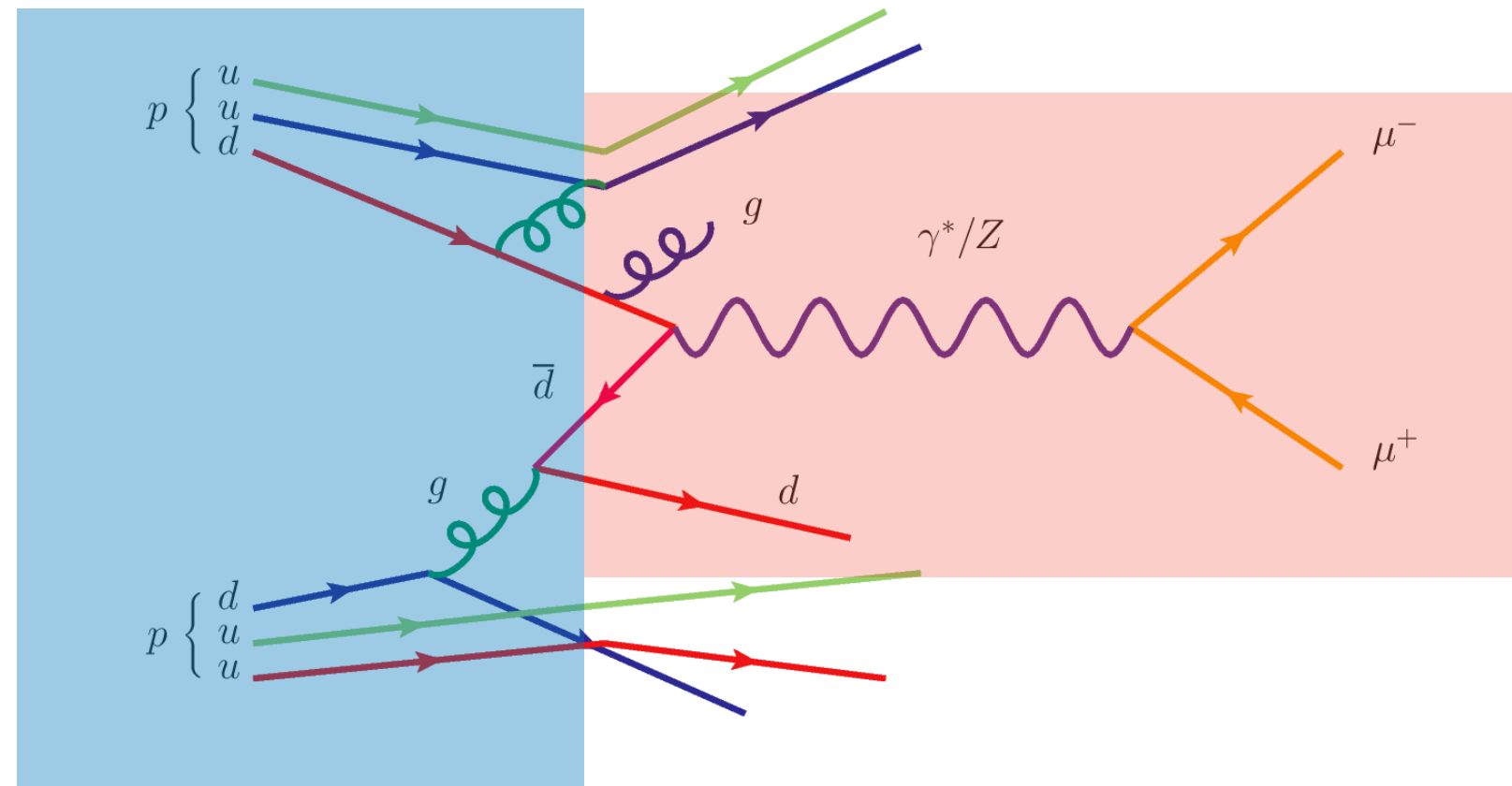
# OUTLINE

- Introduction
- Towards 1% precision in PDFs
  - ➔ Progress in PDF determination
  - ➔ Experimental data & Methodological advances
- New challenges
  - ➔ Theory: missing higher order uncertainties & electroweak corrections
  - ➔ Interpretation: Interplay between PDFs and indirect New Physics searches in high mass tails
- Conclusions and outlook

# INTRODUCTION

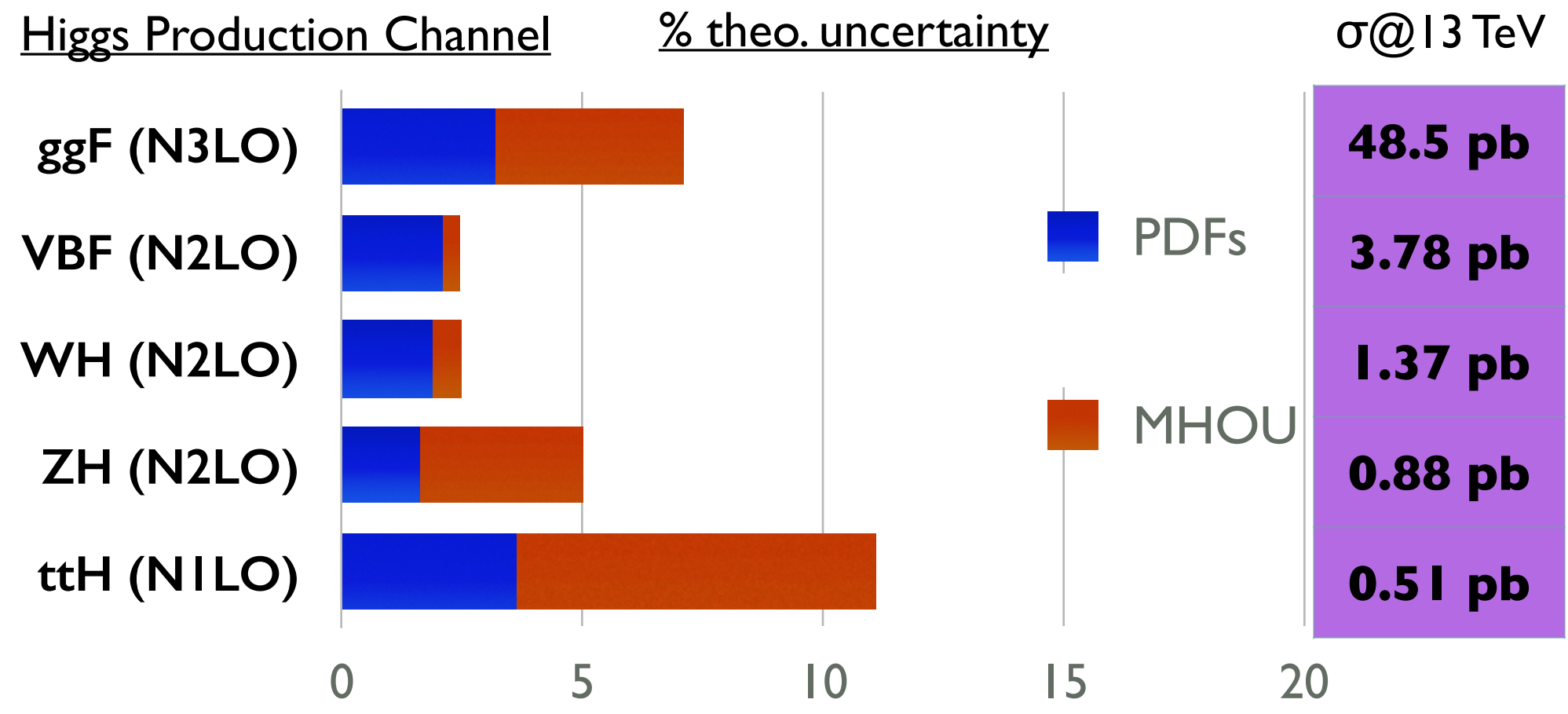
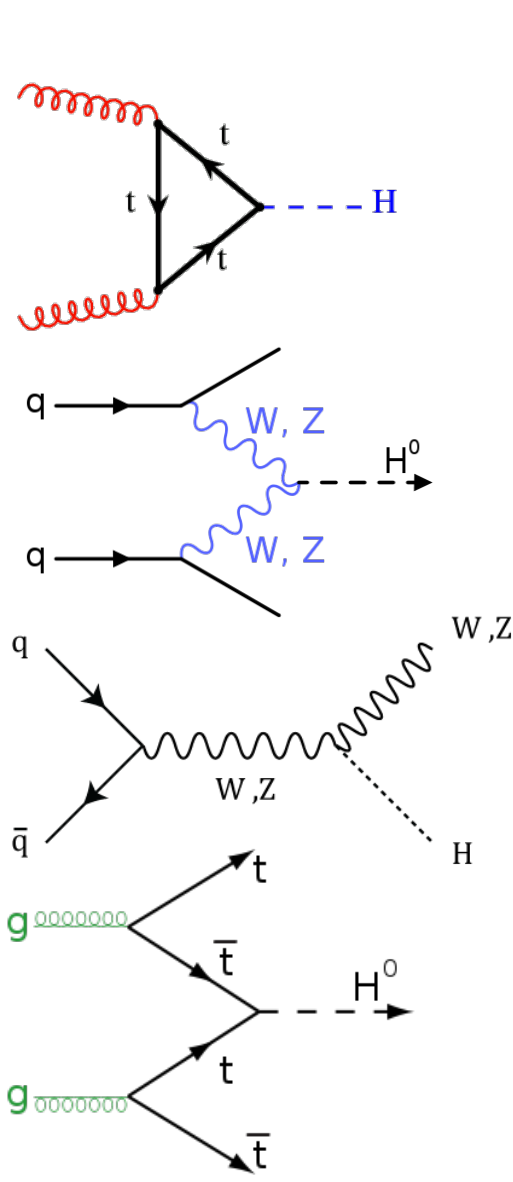
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# WHY ARE PDFs SO IMPORTANT FOR PRECISION PHYSICS ...



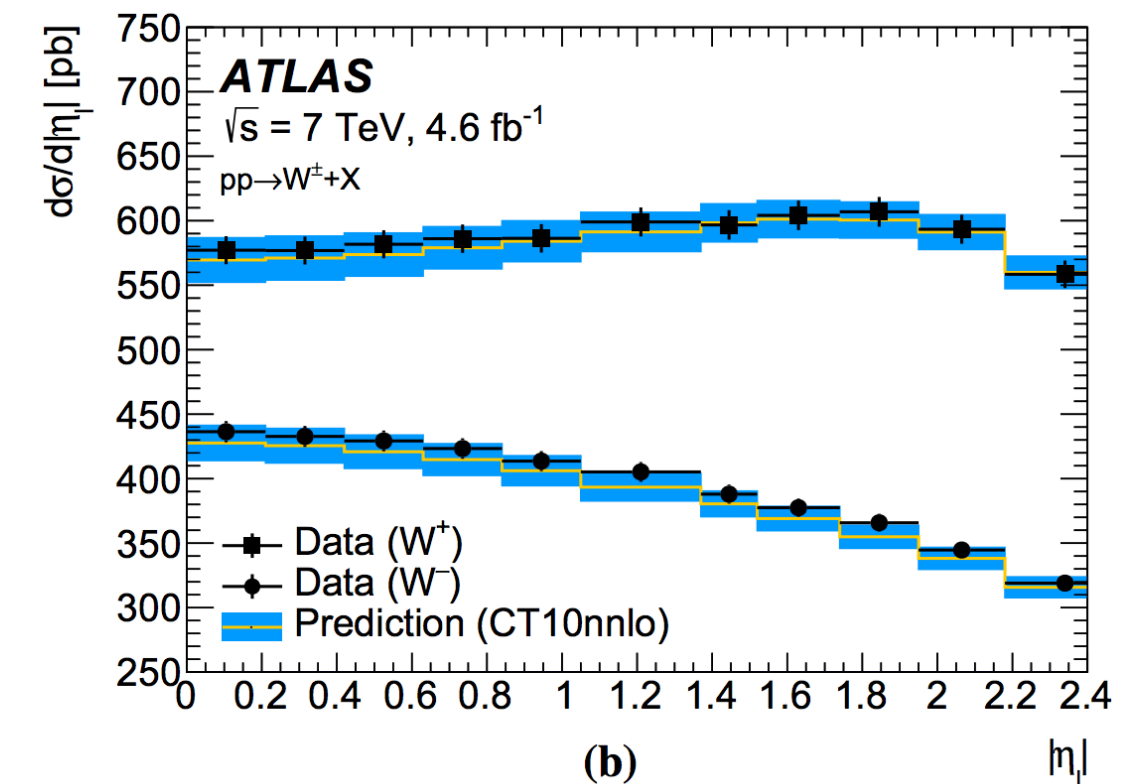
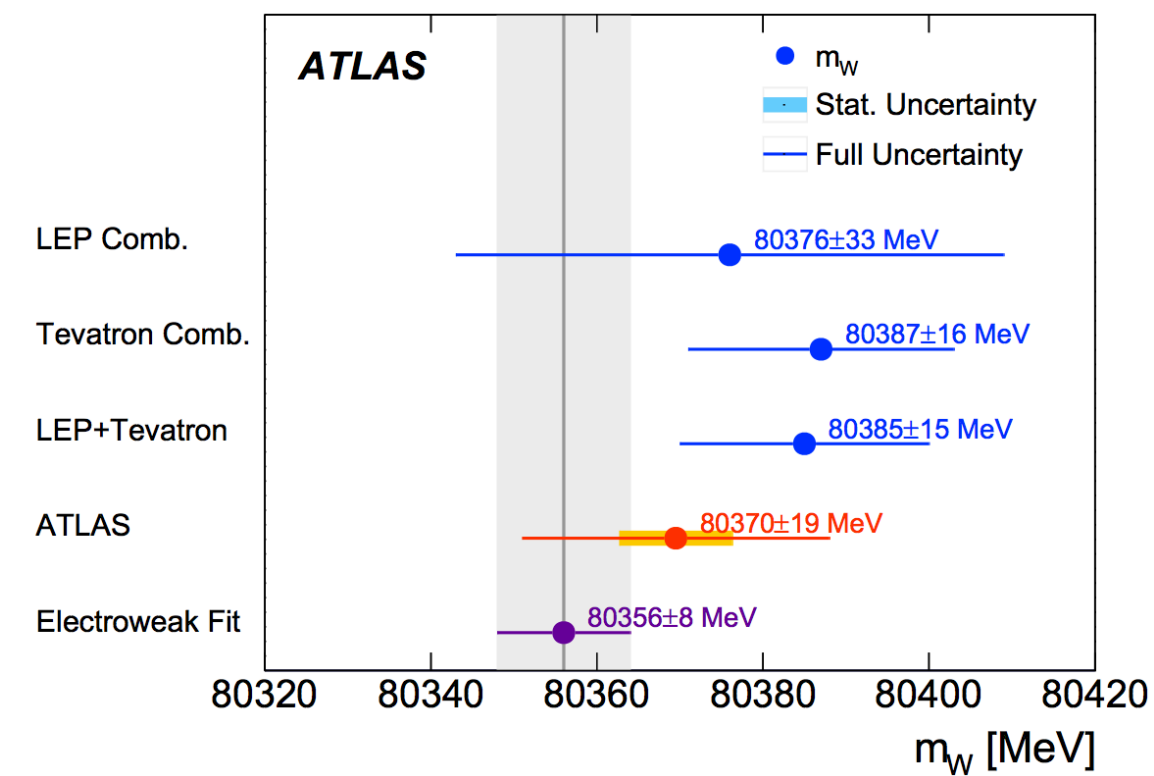
$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

## #1: Higgs physics



HXSWG Yellow report (2016)

## #2: Determination of SM parameters

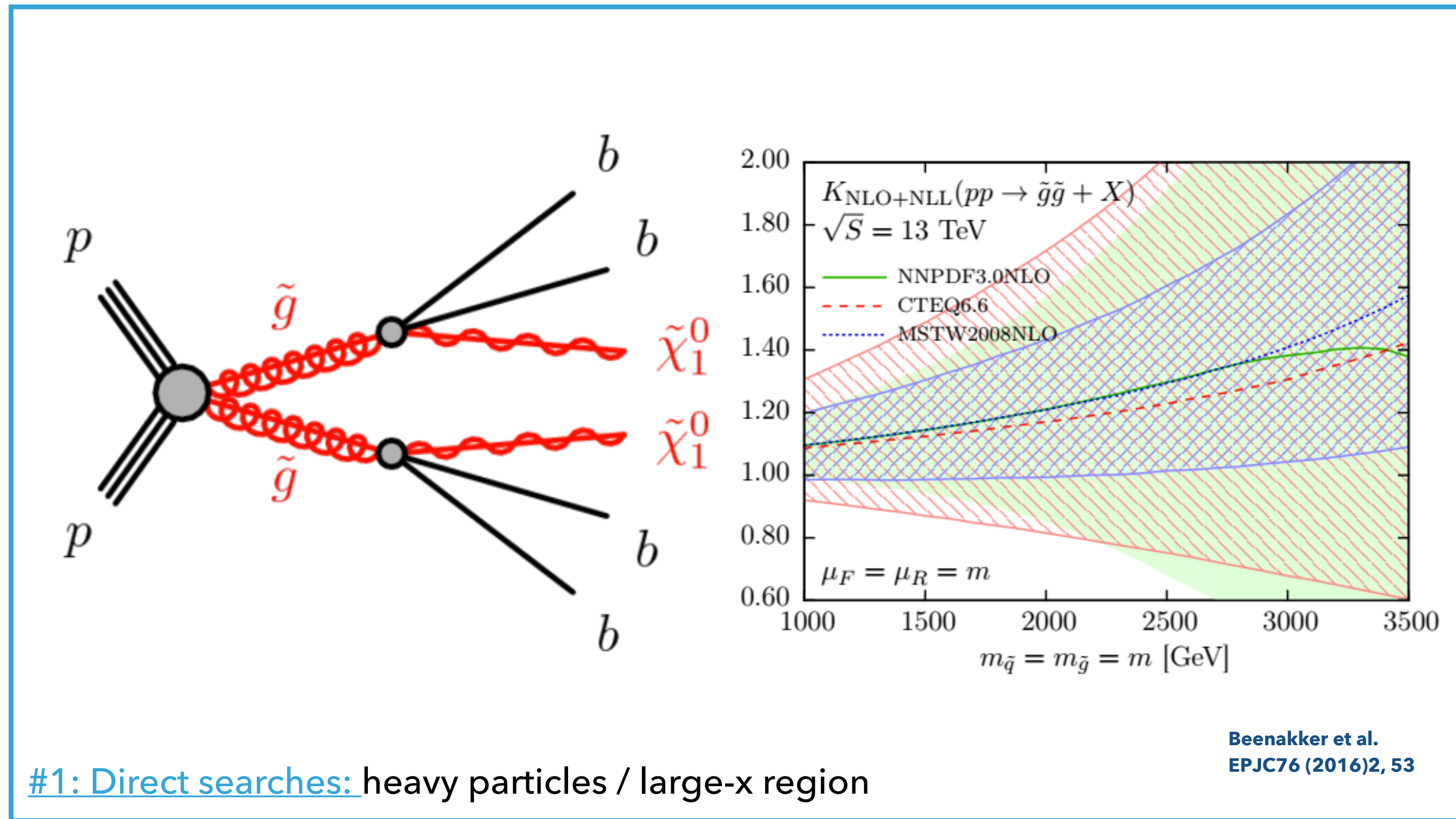
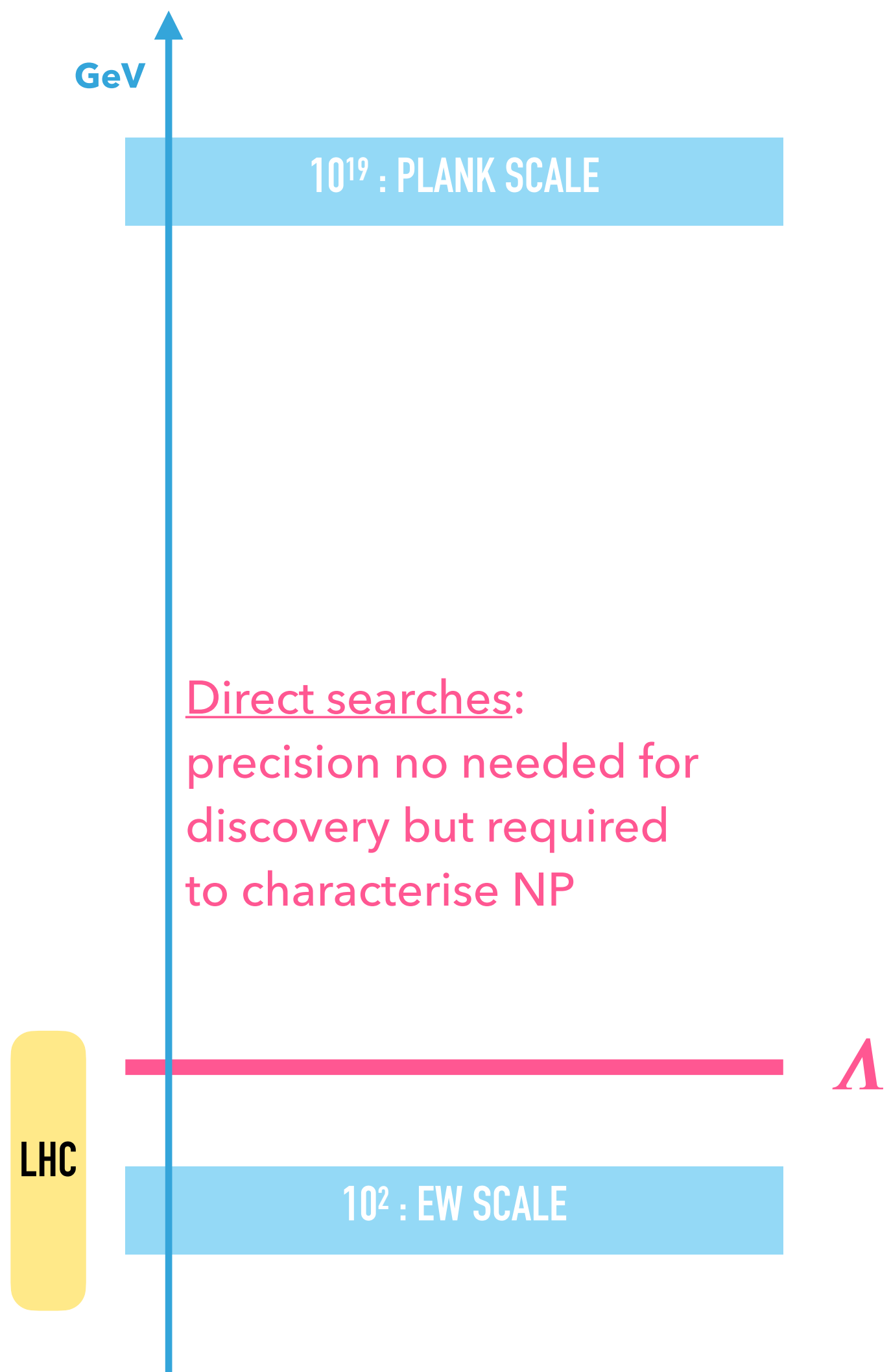


ATLAS collaboration, EPJC 78 (2018) 110

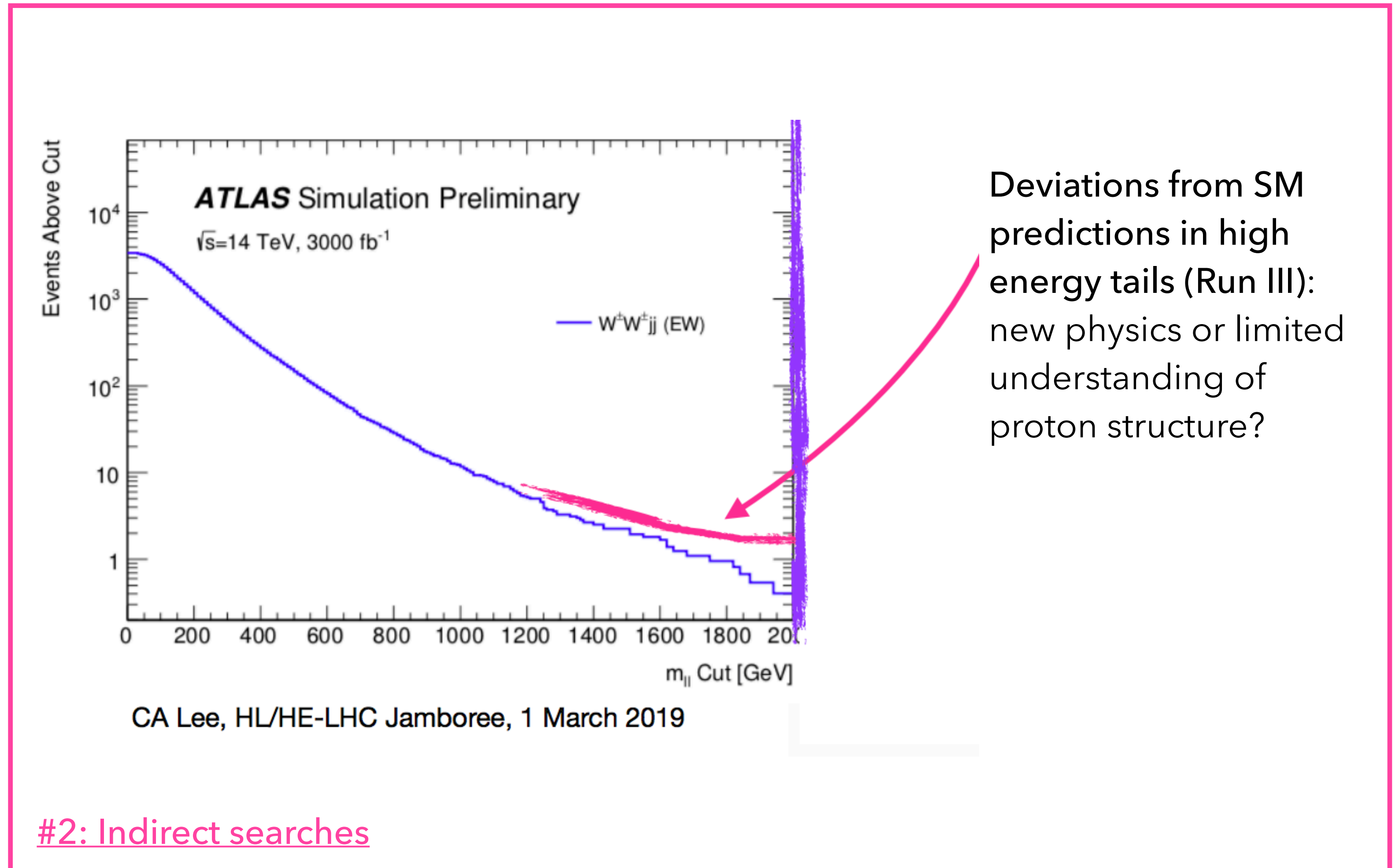
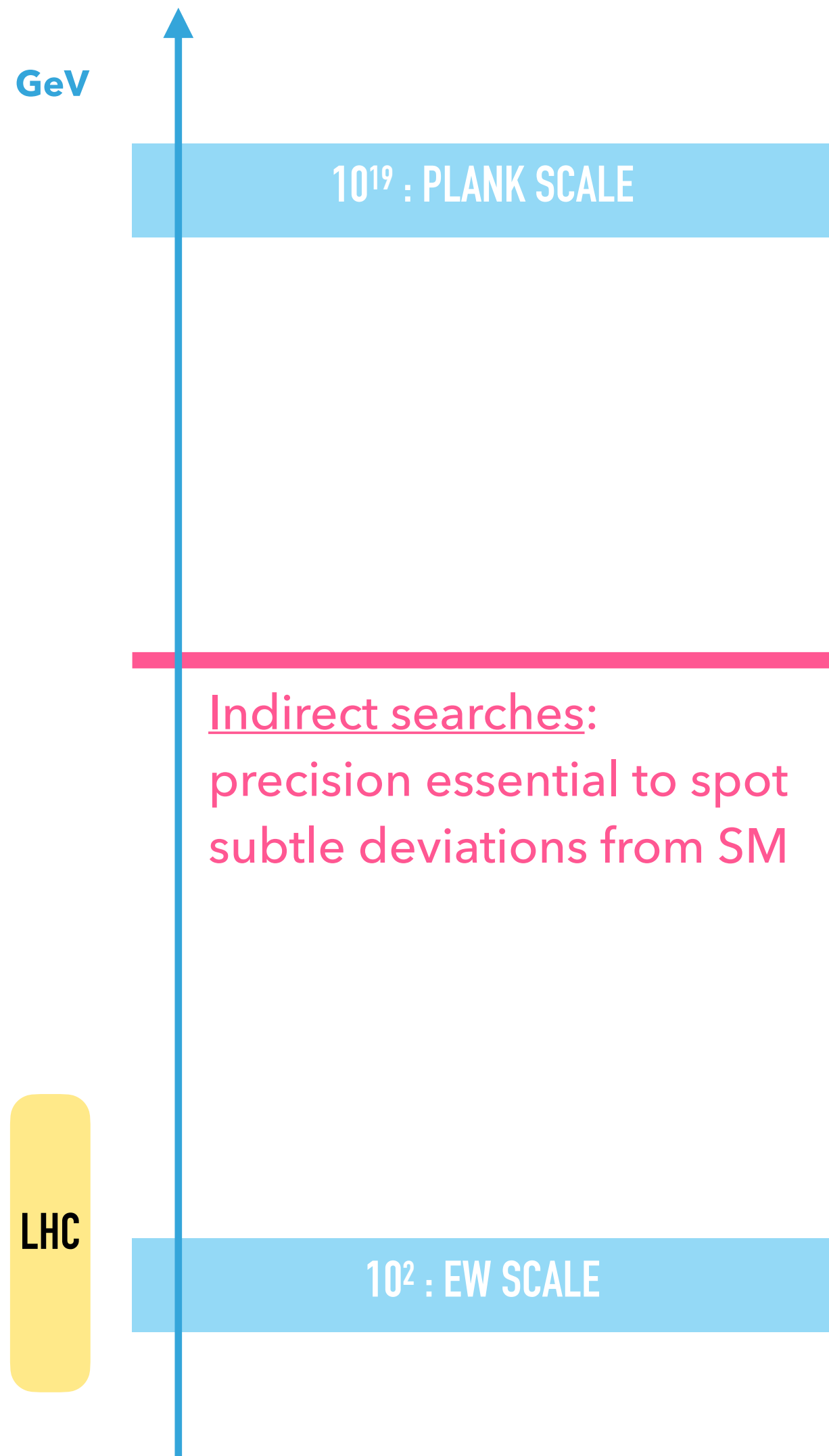
Channel	$m_{W^+} - m_{W^-}$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$W \rightarrow e\nu$	-29.7	17.5	0.0	4.9	0.9	5.4	0.5	0.0	24.1	30.7
$W \rightarrow \mu\nu$	-28.6	16.3	11.7	0.0	1.1	5.0	0.4	0.0	26.0	33.2
Combined	-29.2	12.8	3.3	4.1	1.0	4.5	0.4	0.0	23.9	28.0

$$\eta = -\ln \tan(\theta/2)$$

# ... AND FOR NEW PHYSICS SEARCHES



# ... AND FOR NEW PHYSICS SEARCHES



# TOWARDS 1% PRECISION IN PDF DETERMINATION

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$$f_i(x, \mu)$$

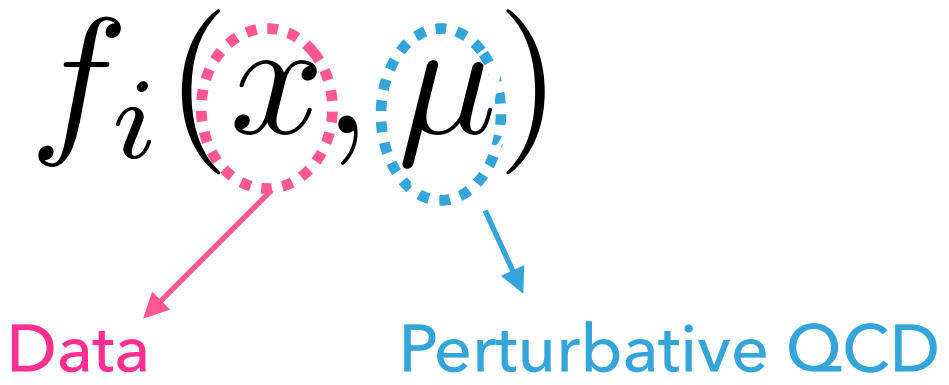
Perturbative QCD

- DGLAP evolution equations fully known up to NNLO and partially at N3LO  
[Moch, Vermaseren, Vogt (2004)]  
[Herzog, Moch, Vermaseren, Vogt, Bonvini...]
- Most theory predictions for processes in PDF fits known at NNLO

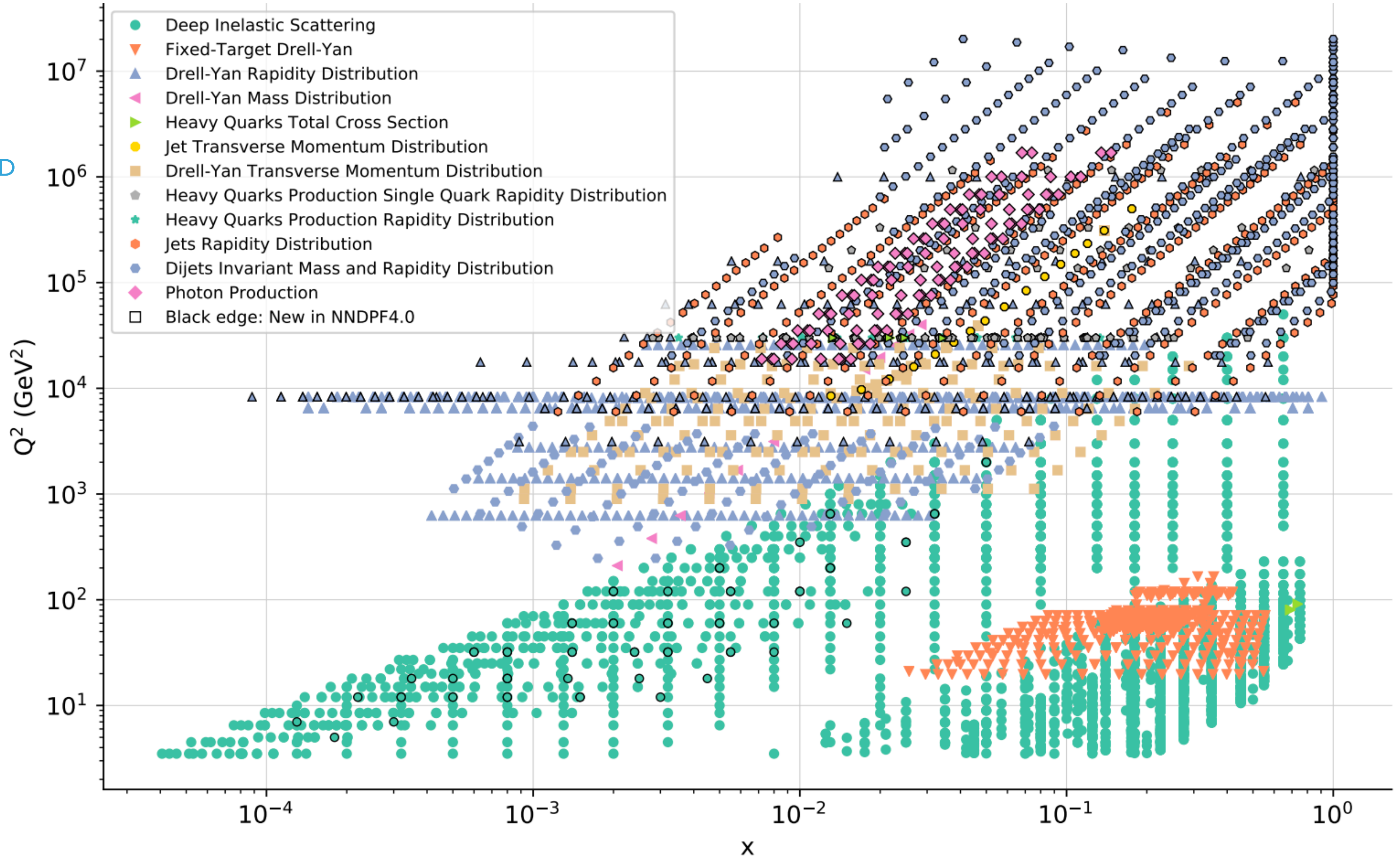


# DETERMINATION OF PDFS

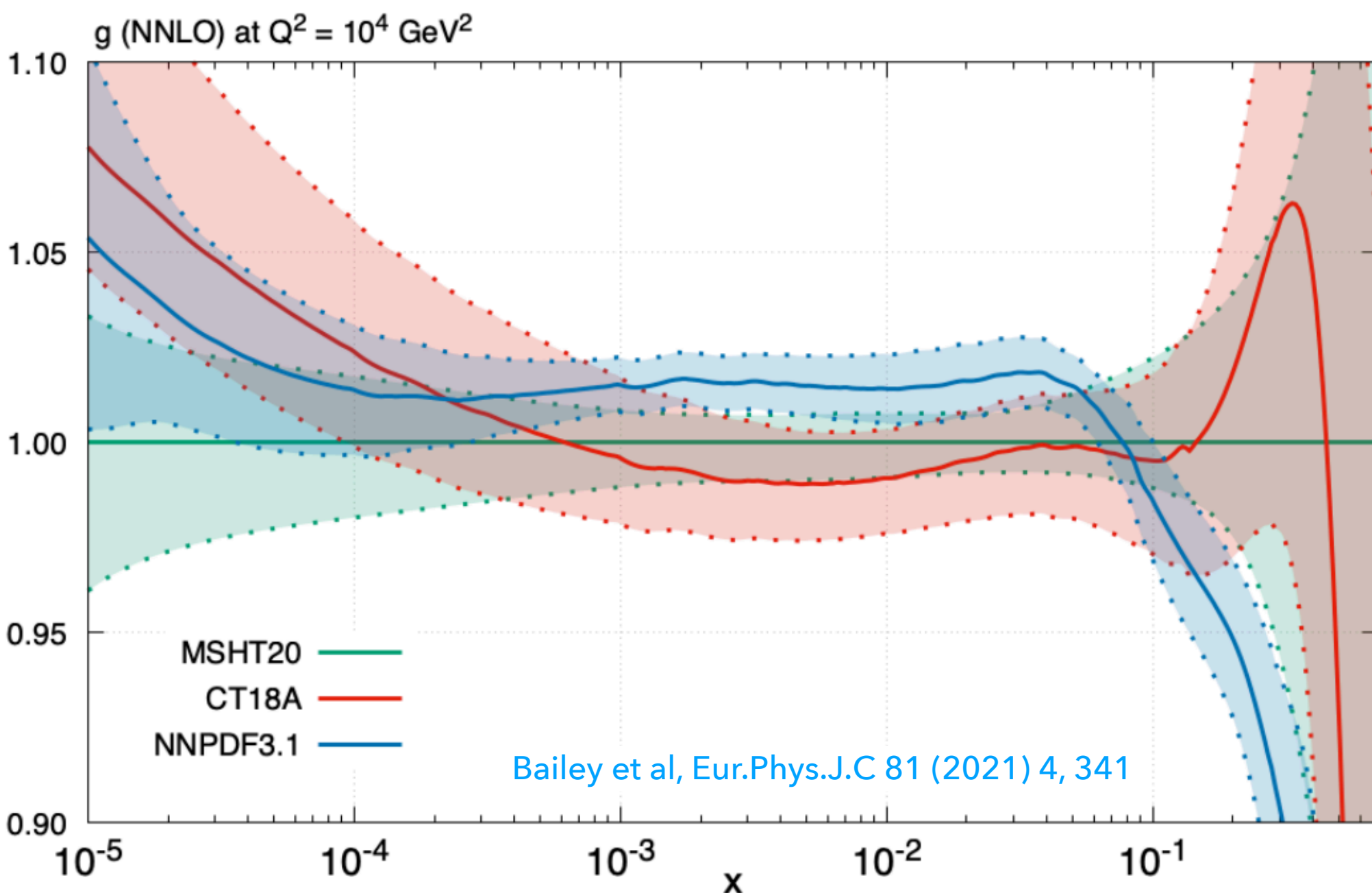
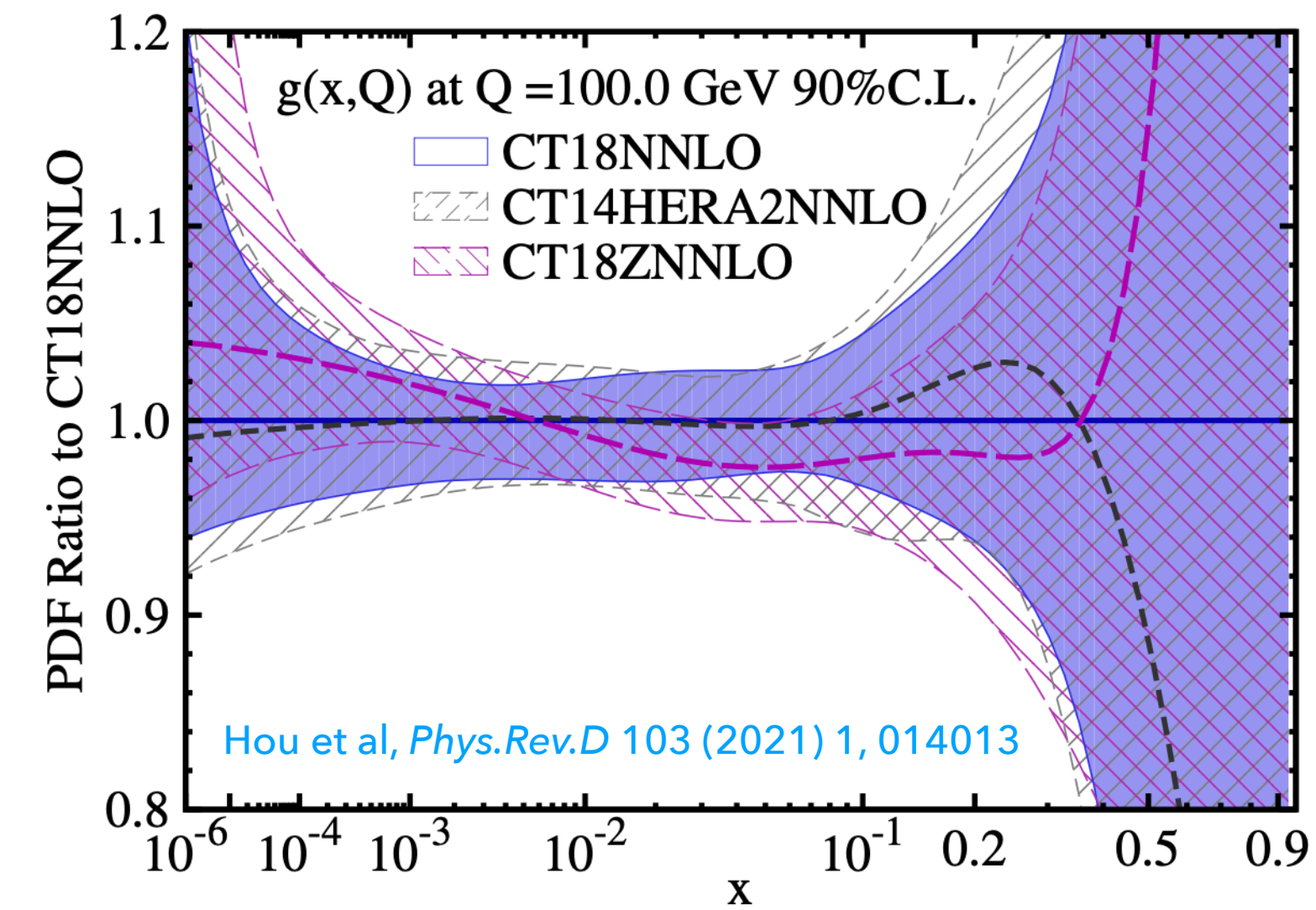
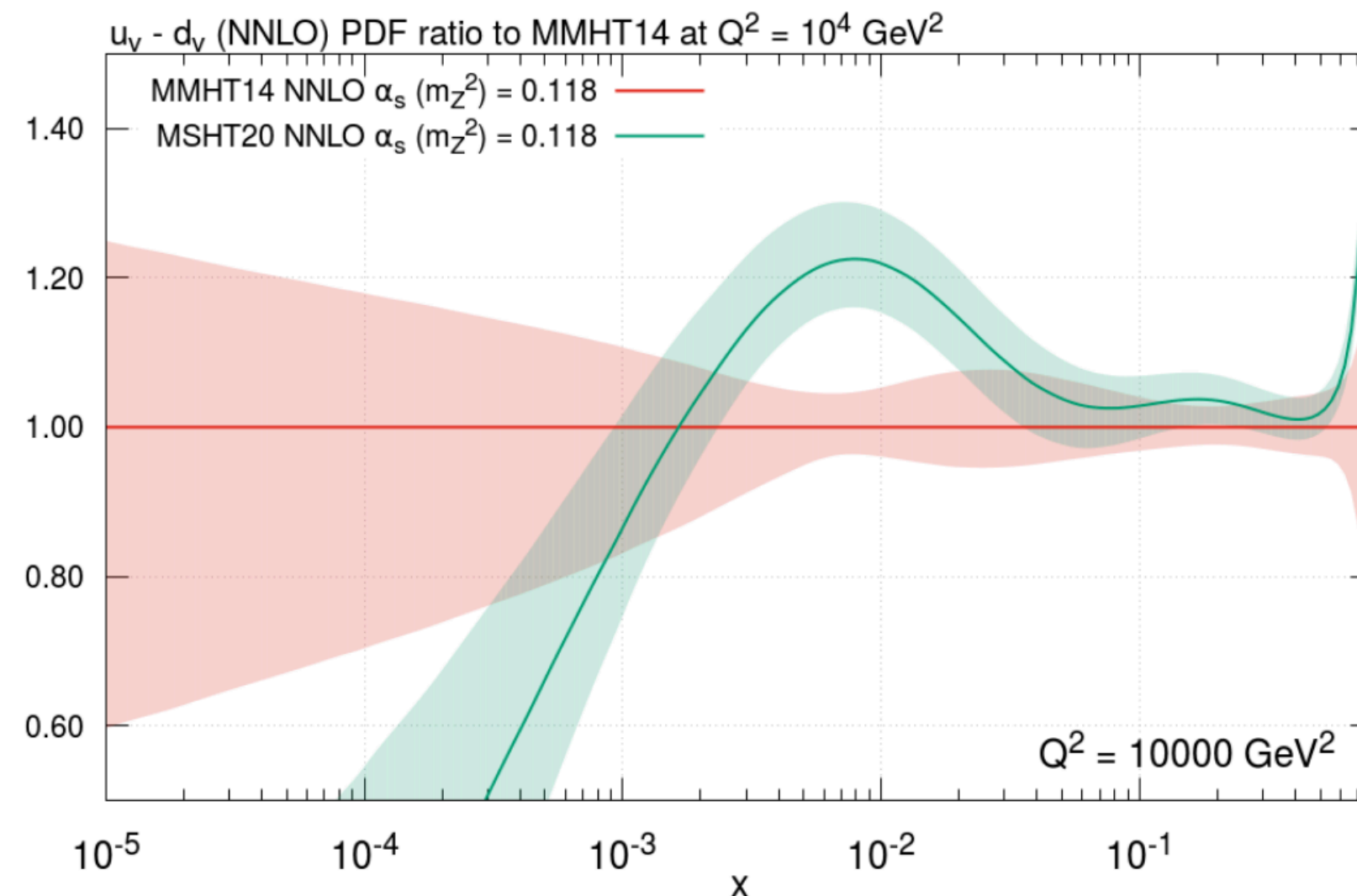
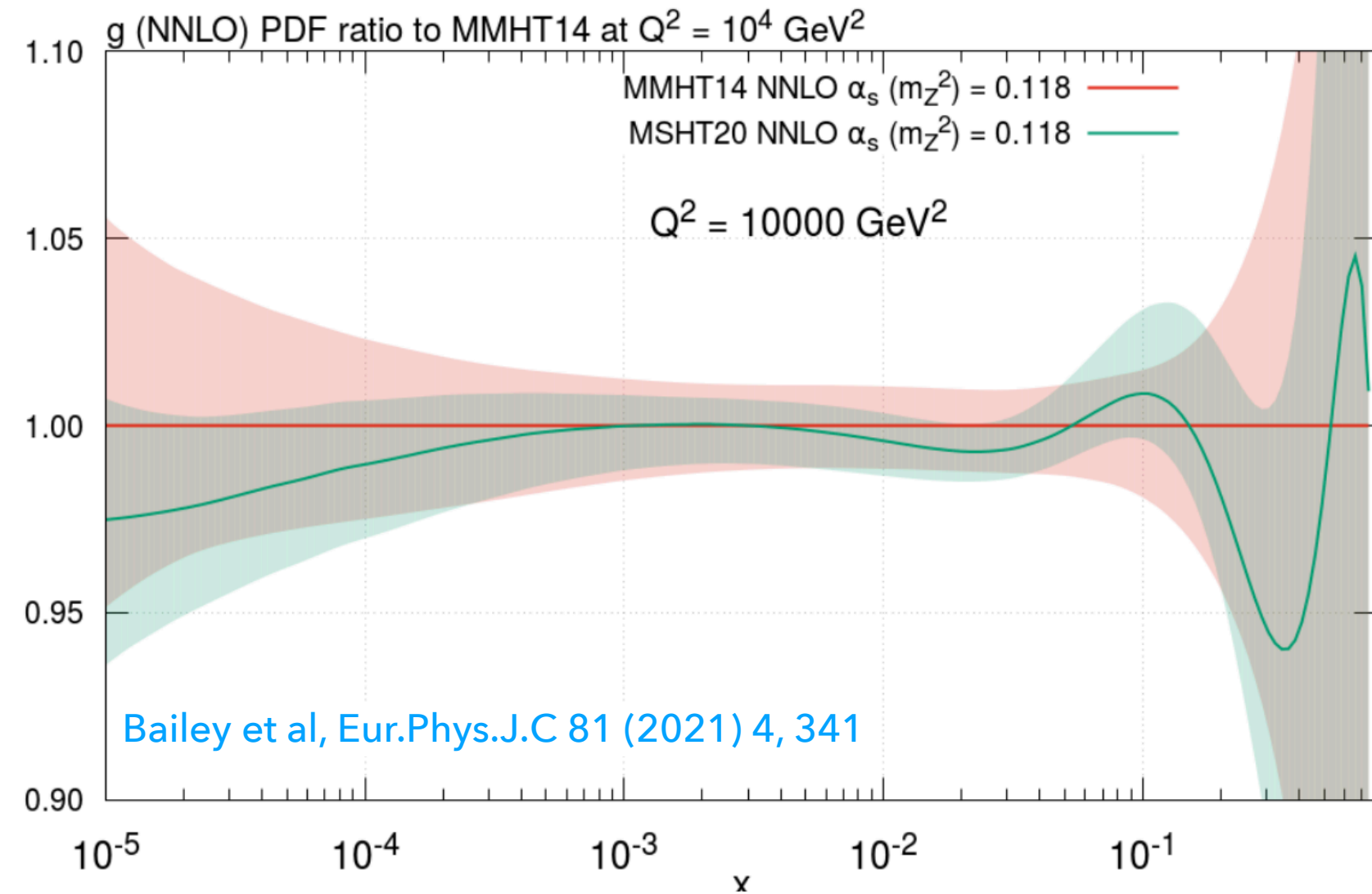
$$\chi^2 = \sum_{i,j=1}^{N_{\text{dat}}} (D_i - T_i(\theta_{\text{PDF}})) (\text{COV})_{ij}^{-1} (D_j - T_j(\theta_{\text{PDF}}))$$



- DGLAP evolution equations fully known up to NNLO and partially at N3LO
- Most theory predictions for processes in PDF fits known at NNLO
- Precision of the most data of the order of a few percents
- Mostly from correlated systematic uncertainties



# A LOT OF RECENT PROGRESS



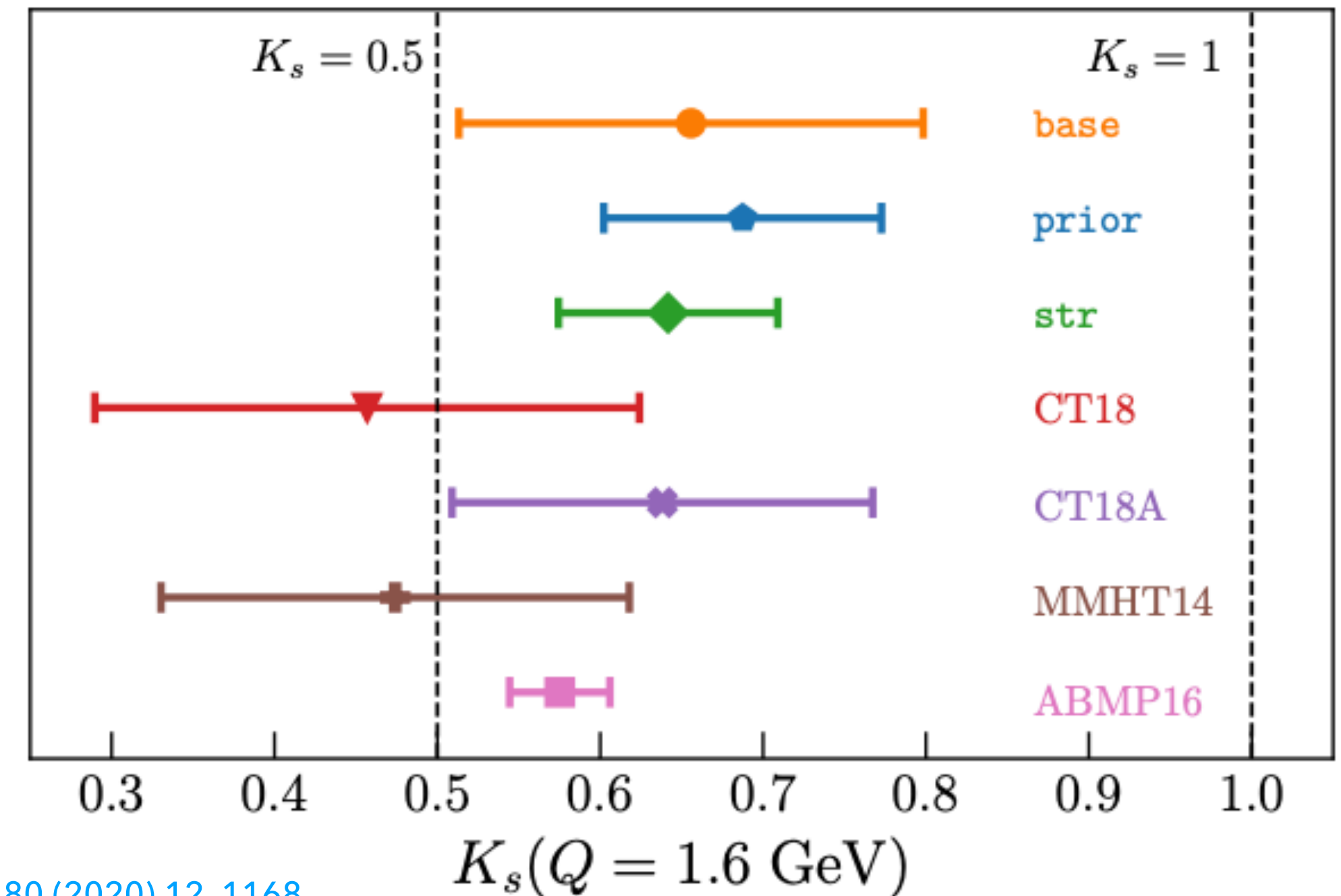
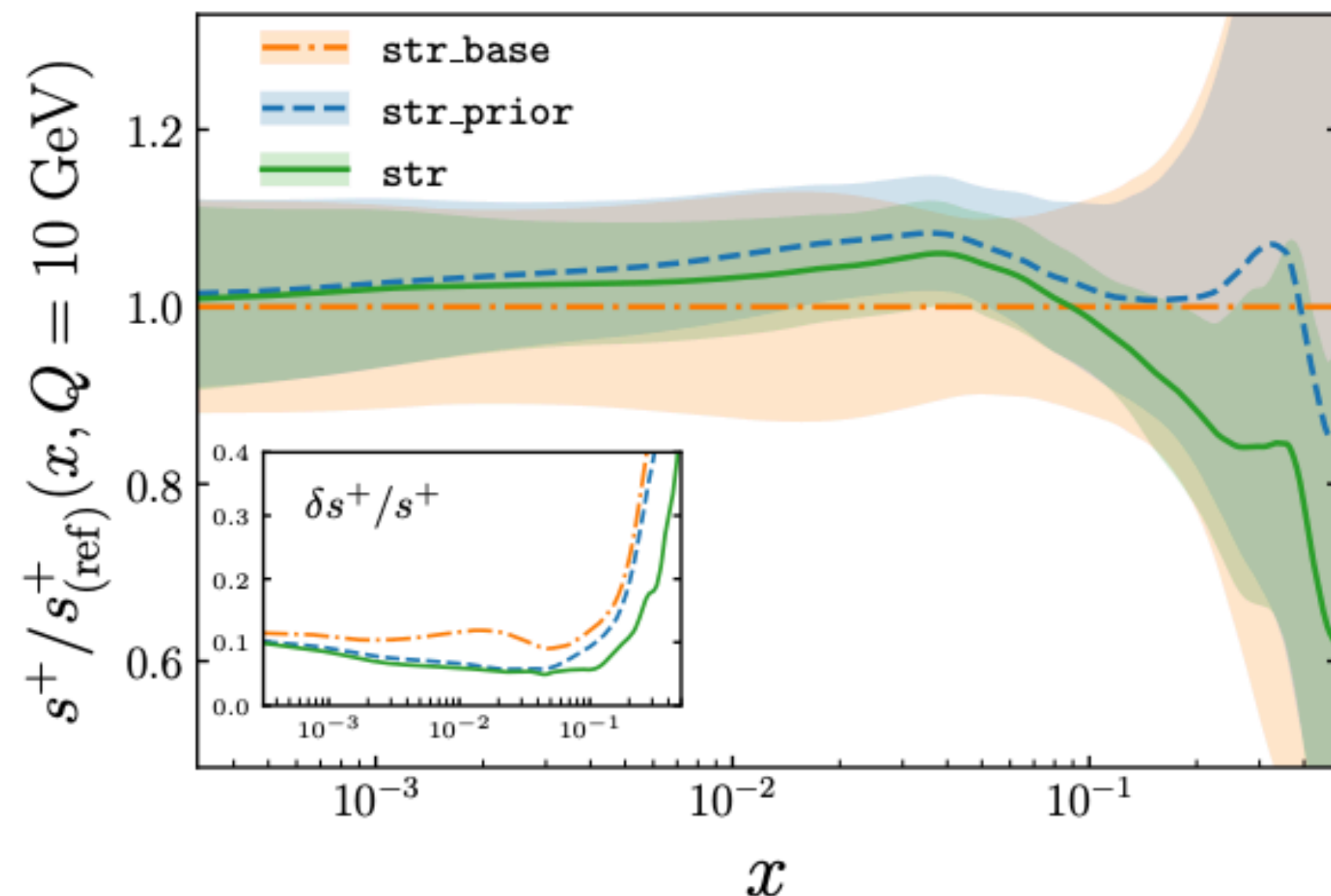
- In recent updates from global PDF fitting collaborations (CT18, MSHT20) the effect of LHC data is driving the PDF uncertainties down, although highly correlated data provide big challenge
- The increased precision of the data and their strong correlation demands methodological improvements (more flexible parametrisation, more refined statistical techniques)
- Some tension among data observed (CT18 vs CT18Z)
- Ongoing benchmark among NNPDF3.1, MSHT20 and CT18 (see J. Houston's talk on Friday)

# DATA COMPATIBILITY AND STRANGENESS

Process	Dataset	$n_{\text{dat}}$	$\chi^2_{\text{base}}$	$\chi^2_{\text{pr}}$	$\chi^2_{\text{str}}$
$\nu\text{DIS} (\mu\mu)$		76/76/95	0.70	0.71	0.53
	NuTeV	76/76/76	0.70	0.71	0.53
	NOMAD	—/—/19	[9.0]	[8.8]	0.55
$W, Z$ (incl.)		327/418/418	1.38	1.40	1.40
	ATLAS	—/61/61	3.22	1.65	1.67
$W+c$		—/37/37	[0.76]	0.68	0.60
	CMS	—/15/15	[1.10]	0.98	0.96
	ATLAS	—/22/22	[0.53]	0.48	0.42
$W+\text{jets}$	ATLAS	—/32/32	[1.58]	1.18	1.18
<b>Total</b>		<b>3917/4077/4096</b>	<b>1.17</b>	<b>1.17</b>	<b>1.17</b>

- Long standing tension between fixed-target and LHC data in the strange sector much accommodated
- Satisfactory description of all datasets (no evidence of tension)
- Sizeable constrains from NOMAD data compatible with collider data
- Moderate suppression of strange PDFs
- Good consistency of  $K_s$  across PDF sets

$$K_s(Q^2) = \frac{\int_0^1 dx [s(x, Q^2) + \bar{s}(x, Q^2)]}{\int_0^1 dx [\bar{u}(x, Q^2) + \bar{d}(x, Q^2)]}$$



# NNPDF4.0: THE ROLE OF LHC DATA

Data set	NNPDF4.0	NNPDF3.1	ABMP16	CT18	MSHT20
ATLAS $W, Z$ 7 TeV (2010)	✓	✓	✓	✓	✓
ATLAS $W, Z$ 7 TeV (2011)	✓	✓	✗	✓	✓
ATLAS low-mass DY 7 TeV	✓	✓	✗	✗	✗
ATLAS high-mass DY 7 TeV	✓	✓	✗	✗	✓
ATLAS $W$ 8 TeV	✓	✗	✗	✗	✓
ATLAS DY 2D 8 TeV	✓	✗	✗	✗	✓
ATLAS high-mass DY 2D 8 TeV	✓	✗	✗	✗	✓
ATLAS $\sigma_{W,Z}$ 13 TeV	✓	✗	✓	✗	✗
ATLAS $W^+$ +jet 8 TeV	✓	✗	✗	✗	✓
ATLAS $Z$ $p_T$ 8 TeV	✓	✓	✗	✓	✓
ATLAS $\sigma_{tt}^{\text{tot}}$ 7, 8 TeV	✓	✓	✓	✗	✗
ATLAS $\sigma_{tt}^{\text{tot}}$ 13 TeV	✓	✓	✓	✗	✗
ATLAS $t\bar{t}$ lepton+jets 8 TeV	✓	✓	✗	✓	✓
ATLAS $t\bar{t}$ dilepton 8 TeV	✓	✗	✗	✗	✓
ATLAS single-inclusive jets 7 TeV, R=0.6	✗	✓	✗	✓	✓
ATLAS single-inclusive jets 8 TeV, R=0.6	✓	✗	✗	✗	✗
ATLAS dijets 7 TeV, R=0.6	✓	✗	✗	✗	✗
ATLAS direct photon production 13 TeV	✓	✗	✗	✗	✗
ATLAS single top $R_t$ 7, 8, 13 TeV	✓	✗	✓	✗	✗
ATLAS single top diff. 7, 8 TeV	✓	✗	✗	✗	✗
ATLAS single top diff. 8 TeV	✓	✗	✗	✗	✗

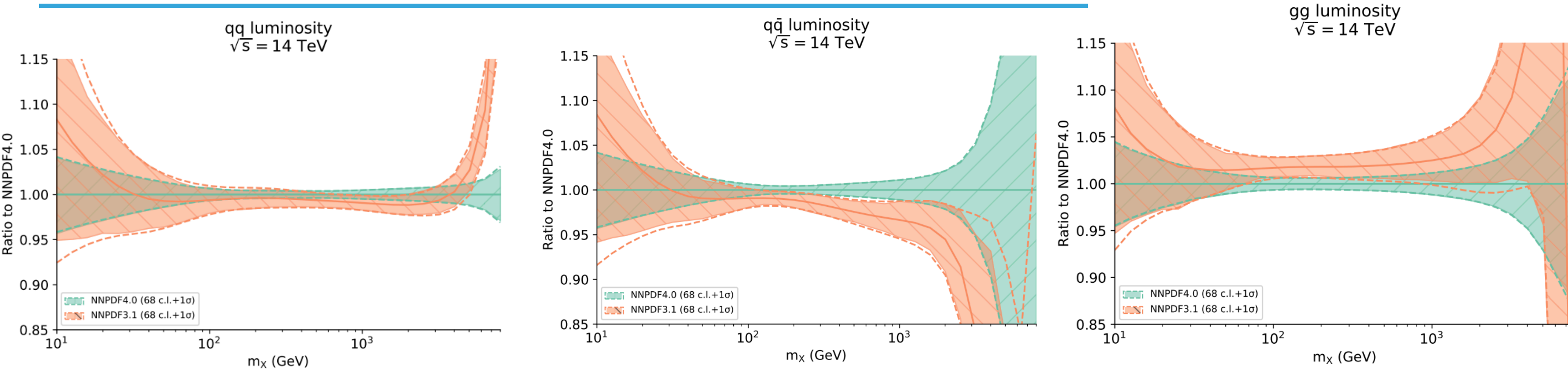
Data set	NNPDF4.0	NNPDF3.1	ABMP16	CT18	MSHT20
LHCb $Z$ 940 pb	✓	✓	✗	✗	✓
LHCb $Z \rightarrow ee$ 2 fb	✓	✓	✓	✓	✓
LHCb $W, Z \rightarrow \mu$ 7 TeV	✓	✓	✓	✓	✓
LHCb $W, Z \rightarrow \mu$ 8 TeV	✓	✓	✓	✓	✓
LHCb $Z \rightarrow \mu\mu, ee$ 13 TeV	✓	✗	✗	✗	✗

Data set	NNPDF4.0	NNPDF3.1	ABMP16	CT18	MSHT20
CMS $W$ electron asymmetry 7 TeV	✓	✓	✗	✓	✓
CMS $W$ muon asymmetry 7 TeV	✓	✓	✓	✓	✗
CMS Drell-Yan 2D 7 TeV	✓	✓	✗	✗	✓
CMS $W$ rapidity 8 TeV	✓	✓	✓	✓	✓
CMS $Z$ $p_T$ 8 TeV	✓	✓	✗	✓	✗
CMS $W + c$ 7 TeV	✓	✓	✗	✗	✓
CMS $W + c$ 13 TeV	✓	✗	✗	✗	✗
CMS single-inclusive jets 2.76 TeV	✗	✓	✗	✗	✓
CMS single-inclusive jets 7 TeV	✗	✓	✗	✓	✓
CMS dijets 7 TeV	✓	✗	✗	✗	✗
CMS single-inclusive jets 8 TeV	✗	✗	✗	✓	✓
CMS 3D dijets 8 TeV	✓	✗	✗	✗	✗
CMS $\sigma_{tt}^{\text{tot}}$ 5 TeV	✓	✗	✓	✗	✗
CMS $\sigma_{tt}^{\text{tot}}$ 7, 8 TeV	✓	✓	✓	✗	✓
CMS $\sigma_{tt}^{\text{tot}}$ 13 TeV	✓	✓	✓	✗	✗
CMS $t\bar{t}$ lepton+jets 8 TeV	✓	✓	✗	✗	✓
CMS $t\bar{t}$ 2D dilepton 8 TeV	✓	✗	✗	✓	✓
CMS $t\bar{t}$ lepton+jet 13 TeV	✓	✗	✗	✗	✗
CMS $t\bar{t}$ dilepton 13 TeV	✓	✗	✗	✗	✗
CMS single top $\sigma_t + \sigma_{\bar{t}}$ 7 TeV	✓	✗	✓	✗	✗
CMS single top $R_t$ 8, 13 TeV	✓	✗	✓	✗	✗

- NNPDF4.0 is upcoming new set from NNPDF based on very large set of data from LHC Run I and Run II (see [T.Giani's talk on Friday](#))
- O(5000) data points and first time inclusion of di-jets preferred over inclusive jets based on [Khalek et al, Eur.Phys.J.C 80 (2020) 8, 797]

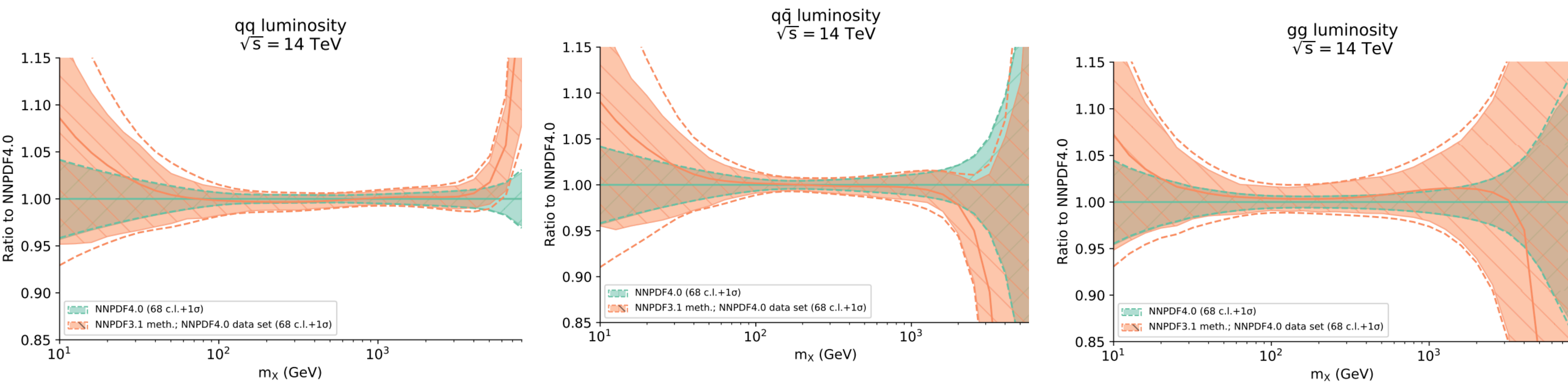
# NNPDF4.0: THE ROLE OF METHODOLOGY

## NNPDF3.1 vs NNPDF4.0



METHODOLOGY DATA	NNPDF3.1	NNPDF4.0
NNPDF3.1 (4093)	1.19	1.12
NNPDF4.0 (4491)	1.25	1.17

## NNPDF4.0 data - NNPDF3.1 vs NNPDF4.0 methodology



METHODOLOGY DATA	NNPDF3.1	NNPDF4.0
NNPDF3.1 (4093)	1.19	1.12
NNPDF4.0 (4491)	1.25	1.17

- ➡ Shift in parton luminosities mostly due to inclusion of O(500) more data points
- ➡ Parton luminosities based on same dataset are consistent with each other but 4.0 methodology displays smaller uncertainty than 3.1 methodology: NNPDF4.0 more accurate and superior to previous methodology

**THEORY FRONTIERS**

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# THEORY UNCERTAINTIES IN PDF FITS

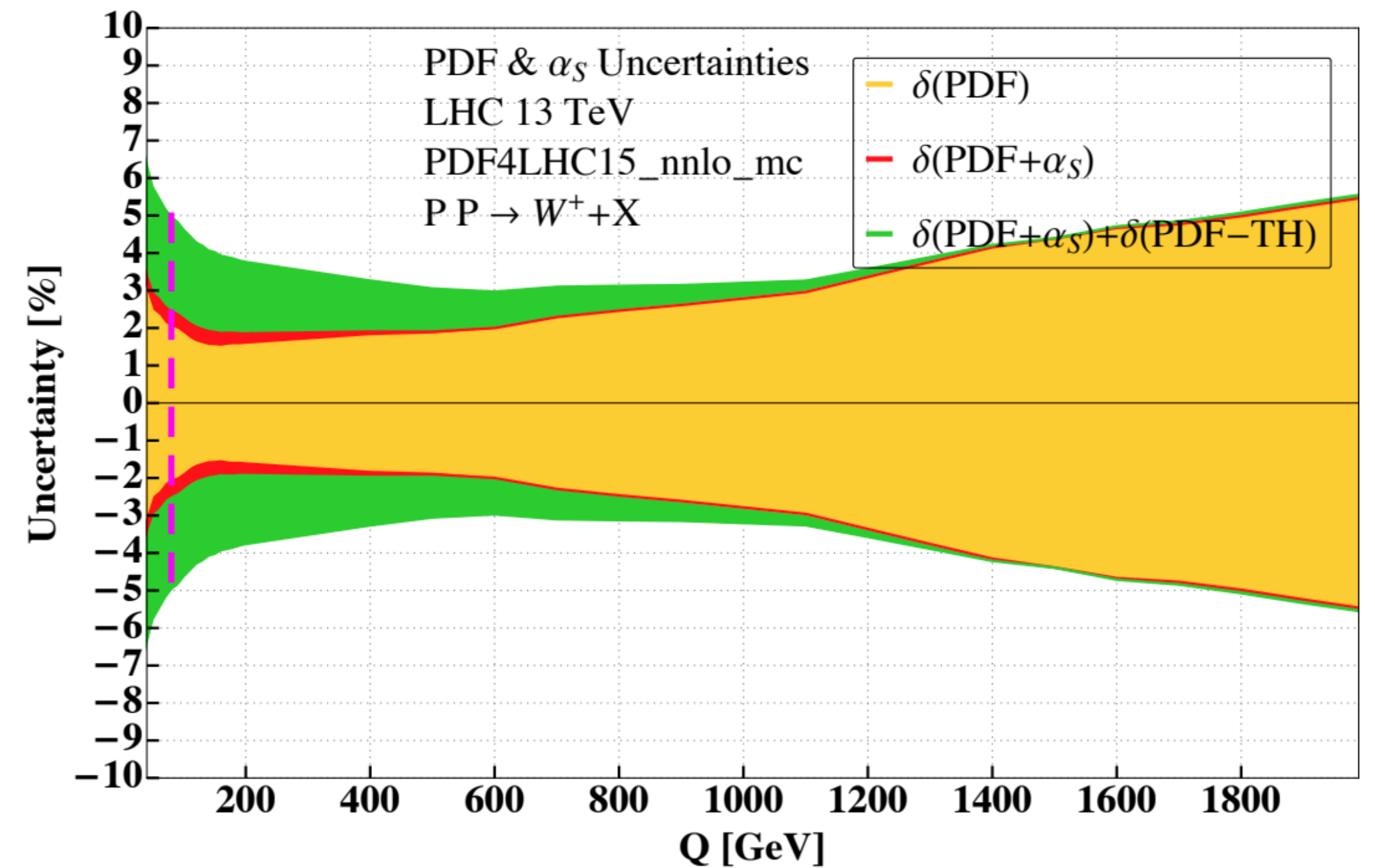
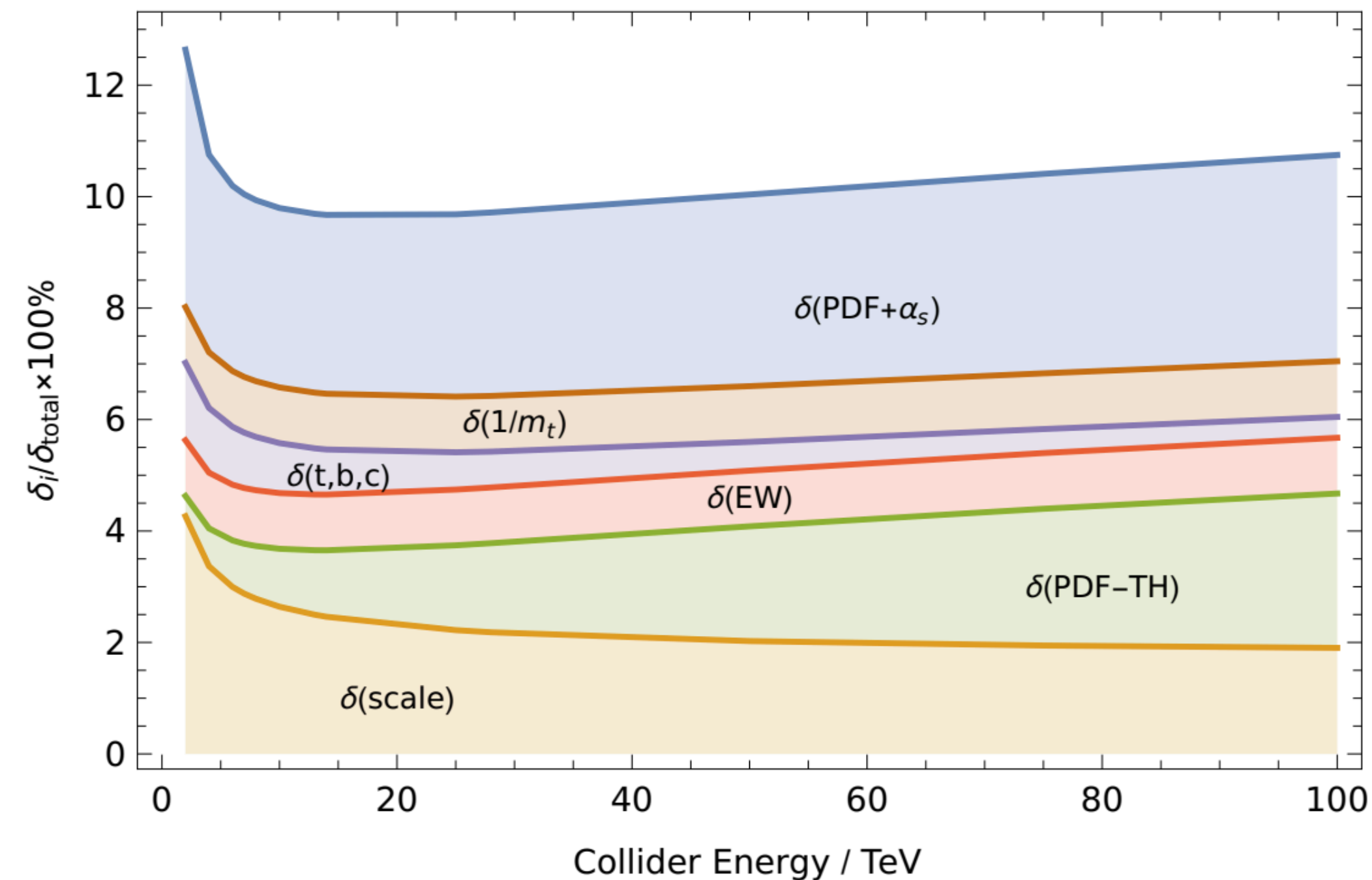
$$\sigma = \alpha_s^p \sigma_0 + \alpha_s^{p+1} \sigma_1 + \alpha_s^{p+2} \sigma_2 + \mathcal{O}(\alpha_s^{p+3})$$

- ▶ Standard global PDF fits based on fixed-order NNLO QCD calculations (using fast interpolation grid for NLO predictions accompanied by local K-factors for NNLO). PDF uncertainty reflects experimental uncertainty.
- ▶ N3LO is now the precision frontier for partonic cross sections (N3LO splitting functions partially known in  $N_c \rightarrow \infty$  limit)
- ▶ Mismatch between perturbative order of partonic cross section and PDFs becoming significant source of uncertainty

$$\delta(\text{PDF} - \text{TH}) = \frac{1}{2} \left| \frac{\sigma_{\text{NNLO-PDFs}}^{(2)} - \sigma_{\text{NLO-PDFs}}^{(2)}}{\sigma_{\text{NNLO-PDFs}}^{(2)}} \right|$$

## Gluon-gluon fusion into Higgs

## Drell-Yan



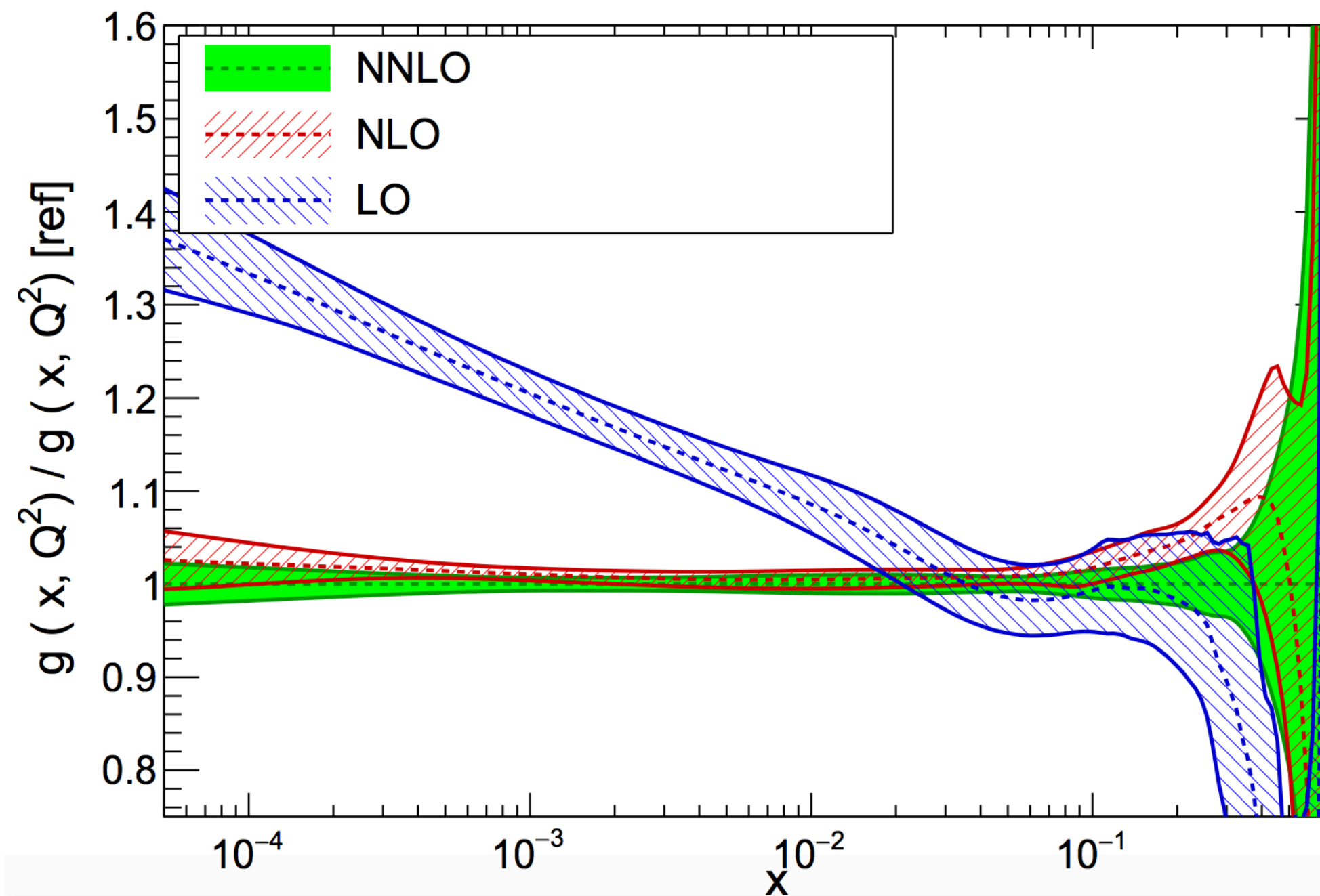
# THEORY UNCERTAINTIES IN PDF FITS

$$\sigma = \alpha_s^p \sigma_0 + \alpha_s^{p+1} \sigma_1 + \alpha_s^{p+2} \sigma_2 + \mathcal{O}(\alpha_s^{p+3})$$

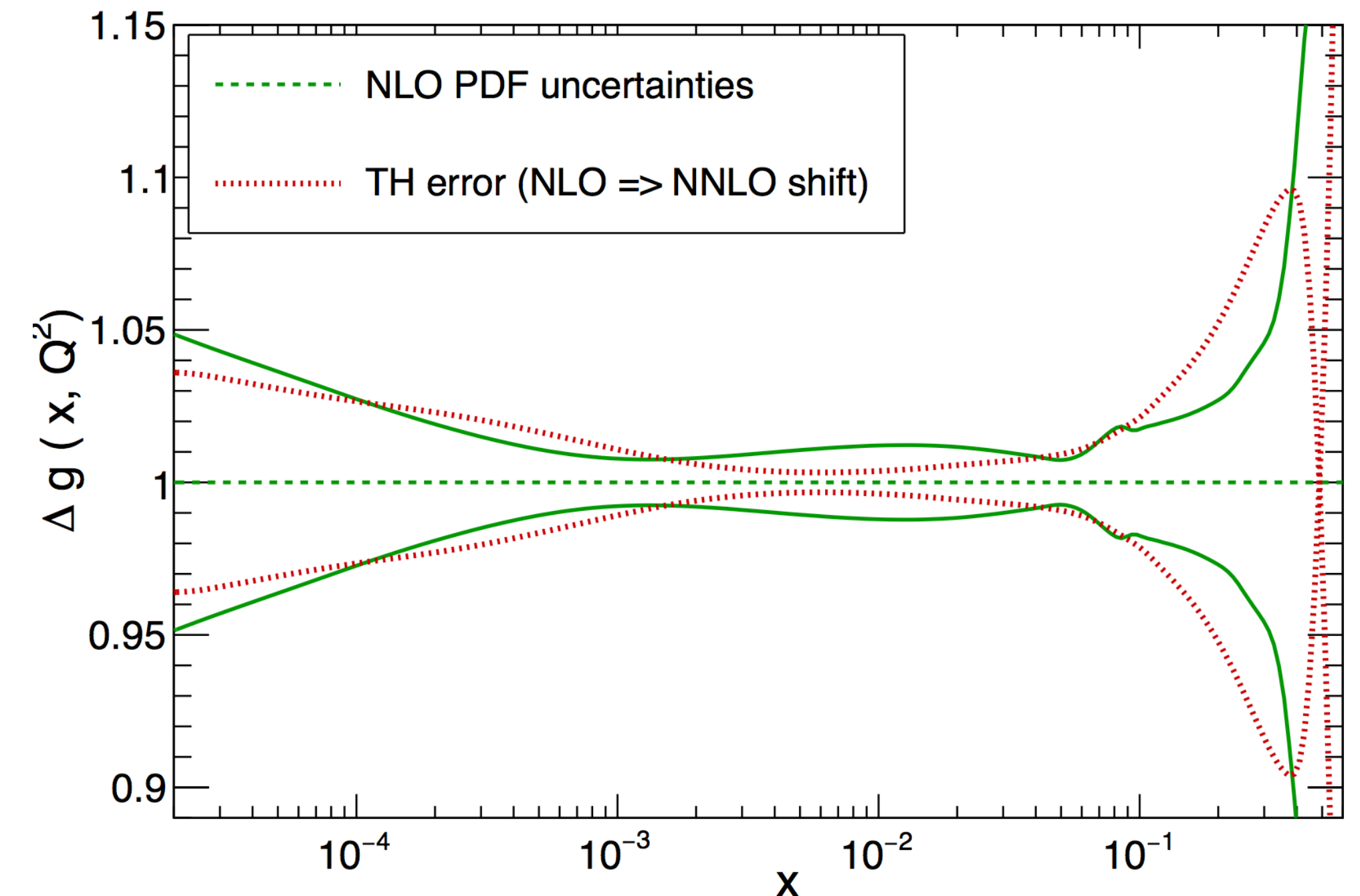
- ▶ Standard global PDF fits based on fixed-order NNLO QCD calculations (using fast interpolation grid for NLO predictions accompanied by local K-factors for NNLO). PDF uncertainty reflects experimental uncertainty.
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$$\delta(\text{PDF} - \text{TH}) = \frac{1}{2} \left| \frac{\sigma_{\text{NNLO-PDFs}}^{(2)} - \sigma_{\text{NLO-PDFs}}^{(2)}}{\sigma_{\text{NNLO-PDFs}}^{(2)}} \right|$$

NNPDF3.1,  $Q = 100 \text{ GeV}$



NNPDF3.1,  $Q^2 = 10^4 \text{ GeV}^2$



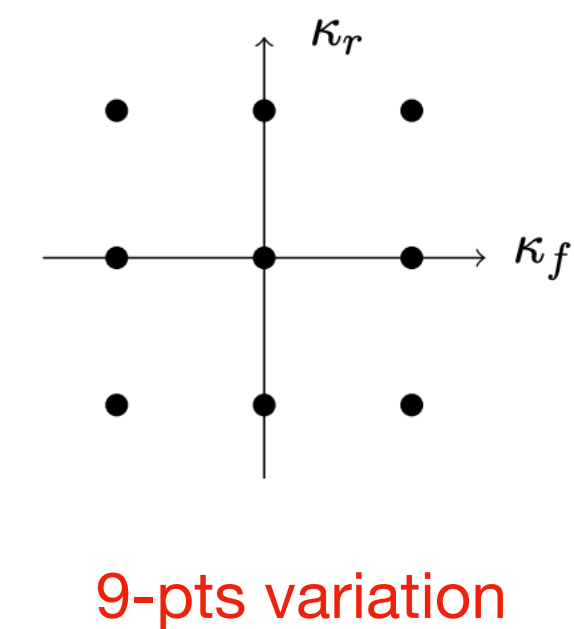
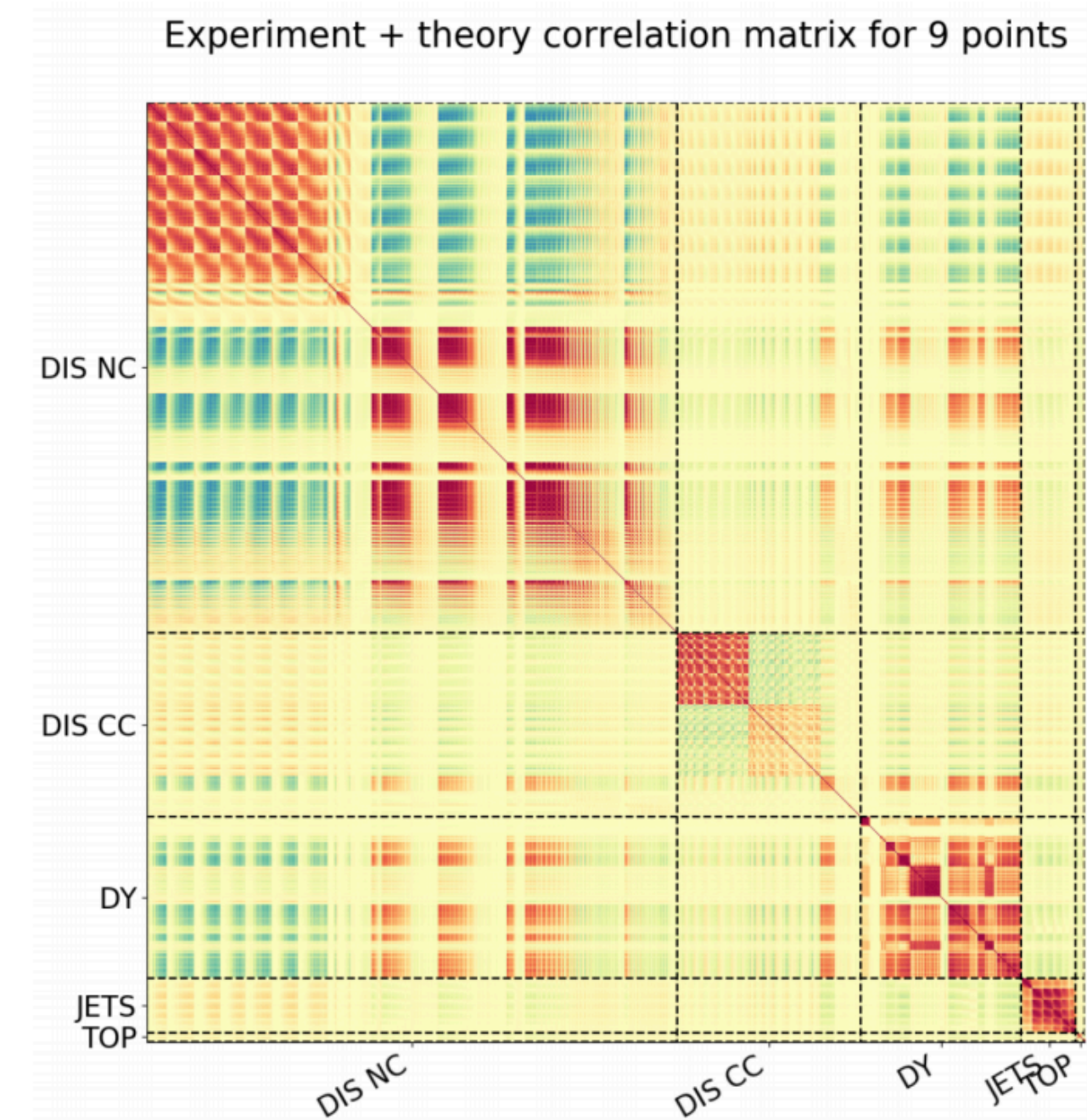
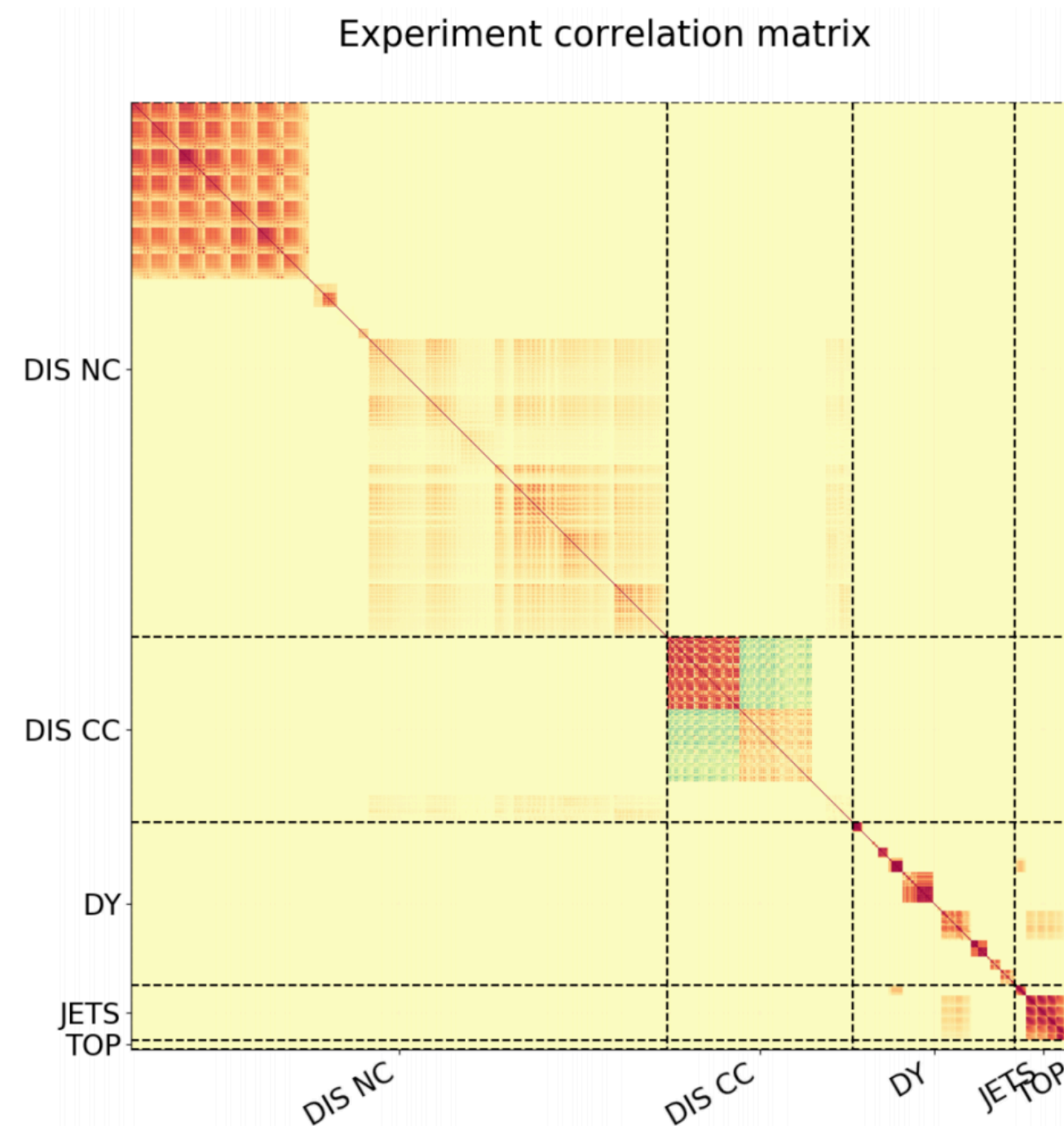


# THEORY UNCERTAINTIES IN PDF FITS

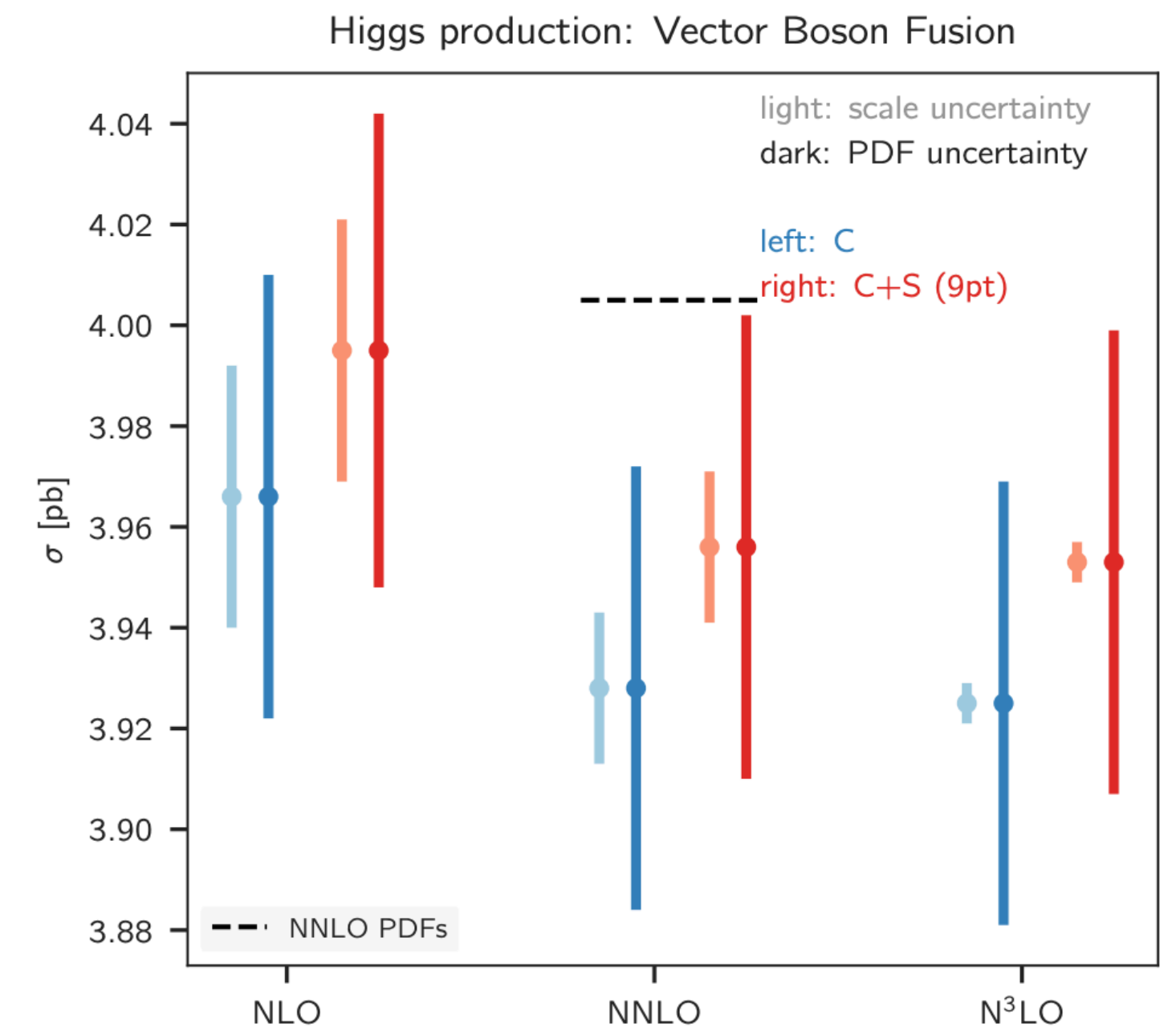
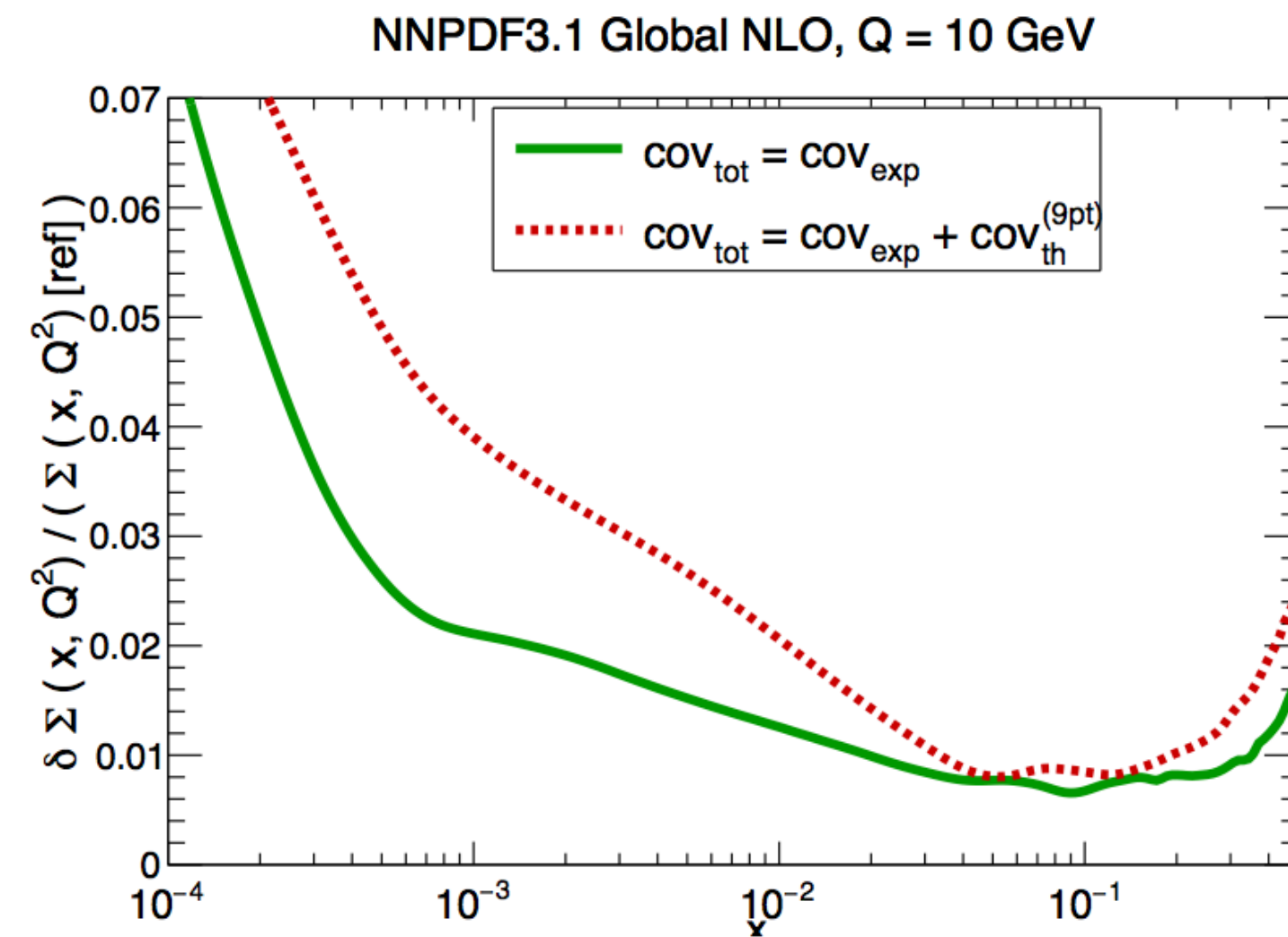
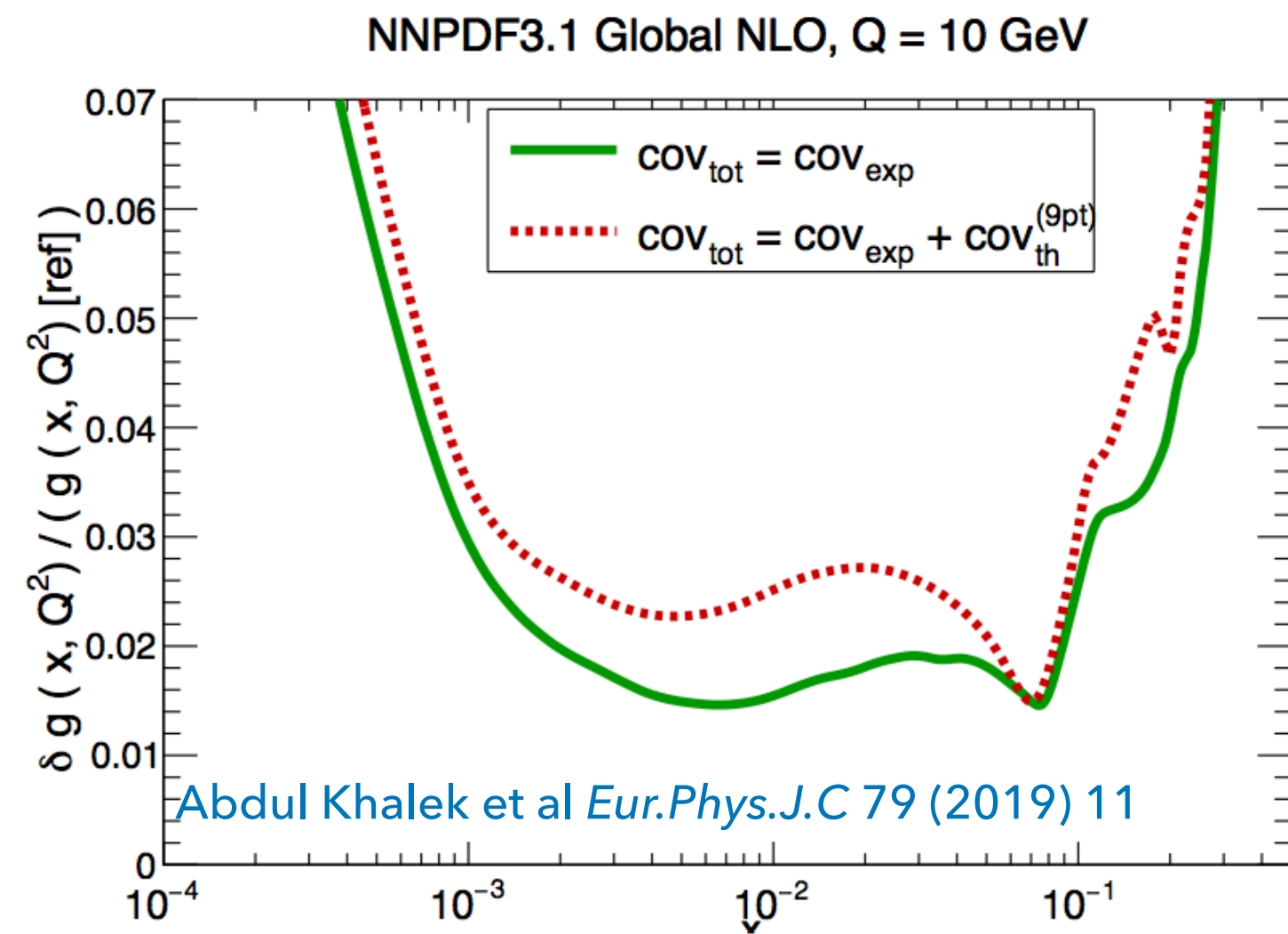
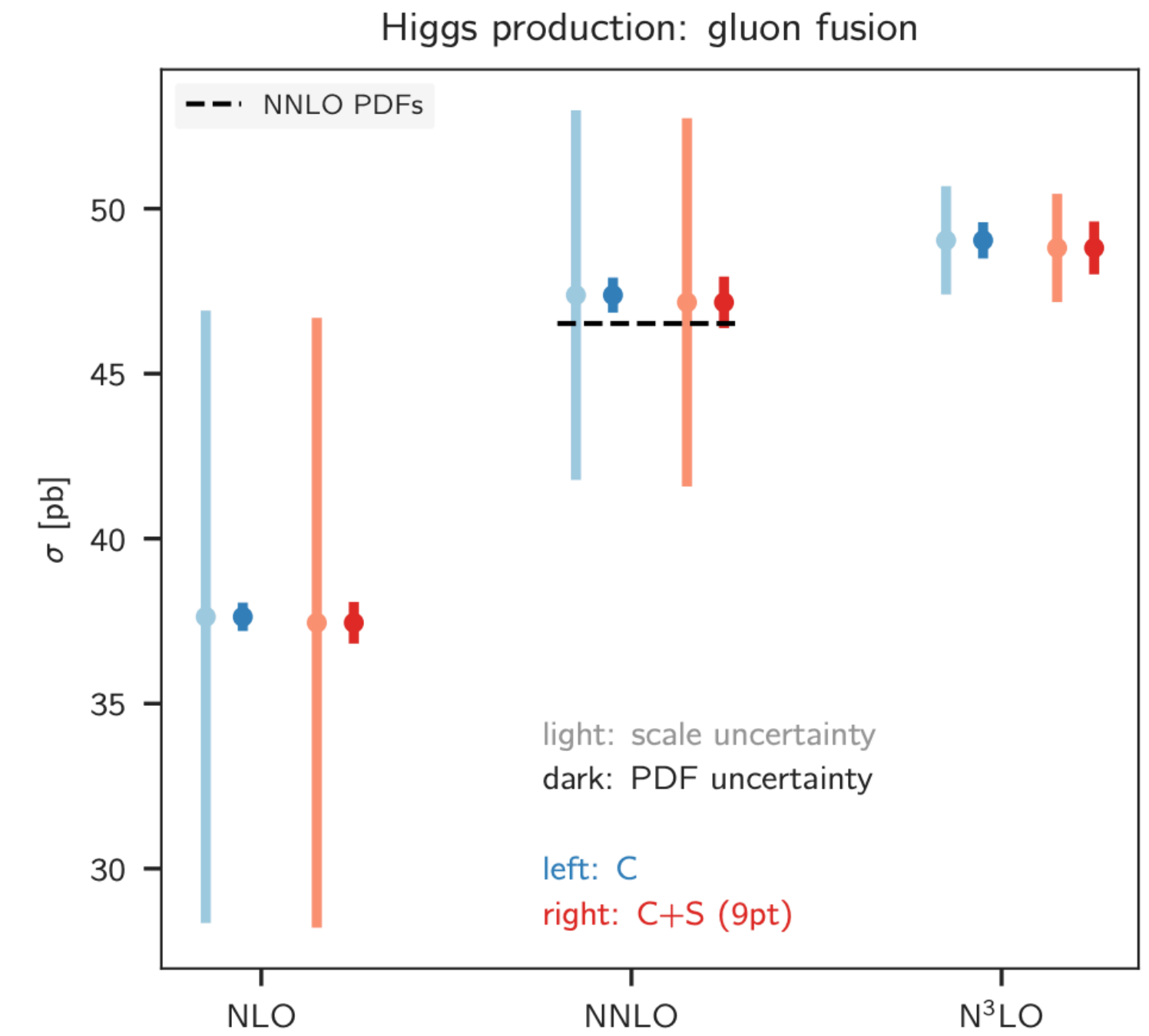
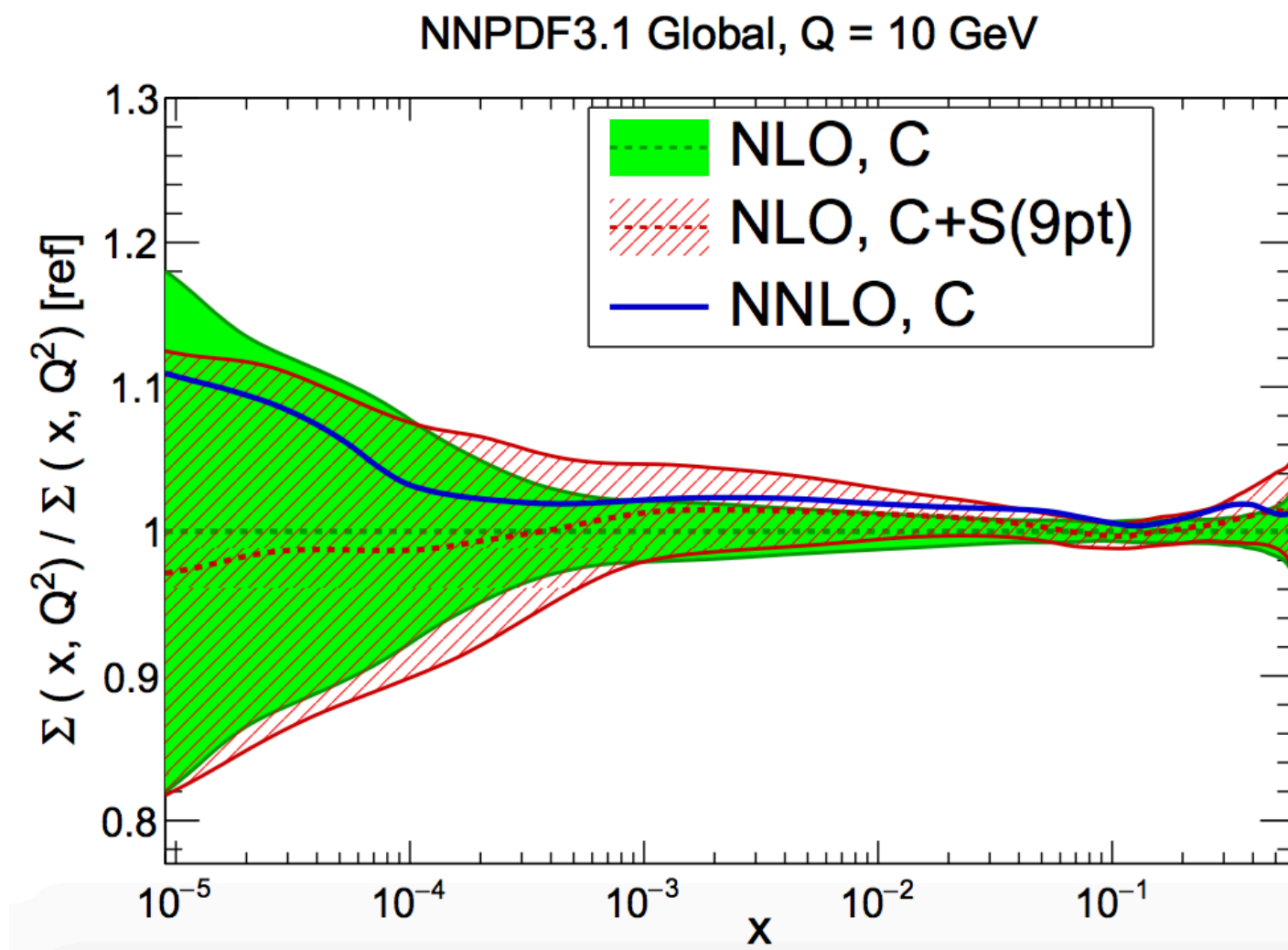
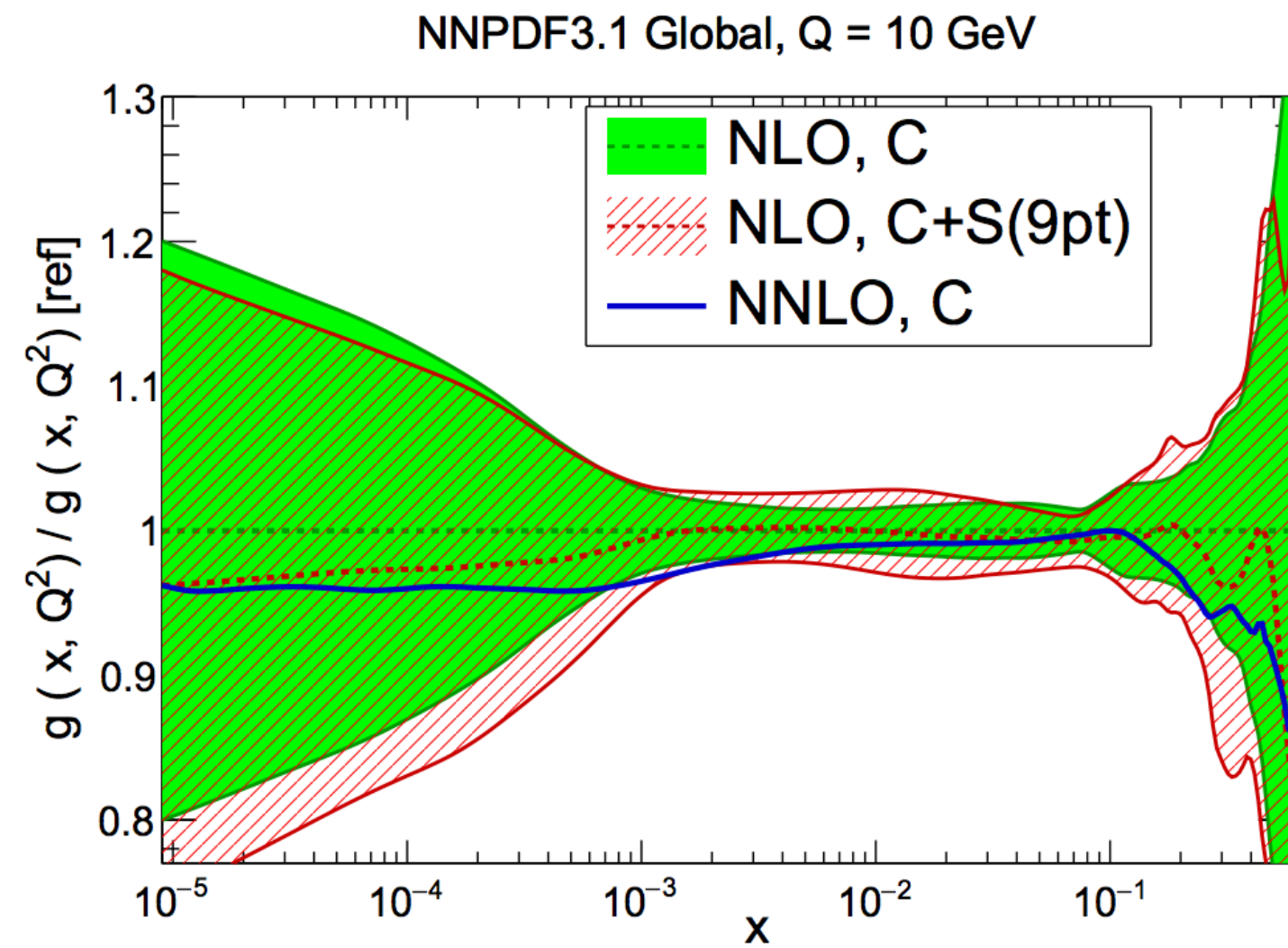
- ➔ How to include Missing Higher Order Uncertainties in a PDF fit? So far tested only at NLO but work in progress for NNLO
- ➔ Construct a theory covariance matrix from scale-varied cross sections and combine it with the experimental covariance matrix  
[R.D. Ball et al, Eur.Phys.J.C 79 (2019) 11, 931, Eur.Phys.J. C (2019) 79:838]

$$\chi^2 = \sum_{m,n=1}^N (d_m - t_m)(\text{COV}_{\text{exp}} + \text{COV}_{\text{th}})^{-1}_{mn} (d_n - t_n)$$

- ➔ Assumptions: experimental and theoretical errors independent and Gaussian
- ➔ Accounting for the theory covariance matrix will modify the relative weight that each of the datasets carries in the global fit: processes with higher MHOUs will be “de-weighted”
- ➔ Assumptions on correlation of scales and scale ratio will determine the specific form of the covariance matrix



# THEORY UNCERTAINTIES IN PDF FITS



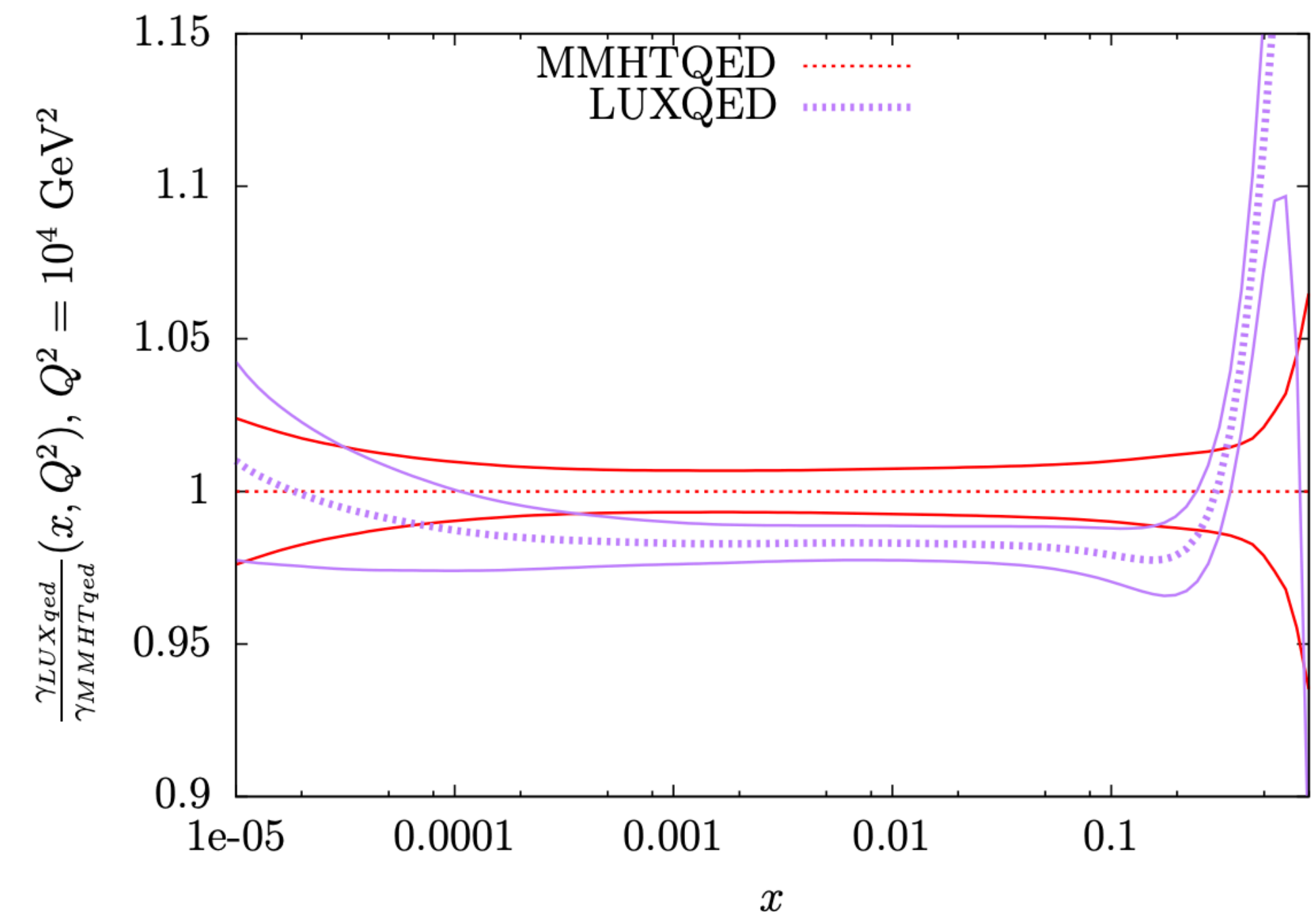
➡ Missing correlation between scale variation in PDF fits and hard cross sections  
 [Harland-Lang, Thorne *Eur.Phys.J.C* 79 (2019) 3, 225]

# NLO EW CORRECTIONS FOR PDF FITS

- ▶ If we aim to 1% accuracy NLO EW corrections do matter.
- ▶ As the LHC reaches higher invariant mass regions and pT regions EW corrections increasingly relevant
- ▶ Currently NLO EW corrections included for some observables in MSHT20 (via K-factors) [Bailey et al 2012.04684]
- ▶ NLO EW corrections not included by default in NNPDF4.0 nor CT18 (large invariant mass regions, large Z pT excluded => less constraints to large-x PDFs)

- ➔ QED corrections in DGLAP evolution [Bertone et al, APFEL, Comput.Phys.Commun. 185 (2014)]
- ➔ Photon PDFs [Manohar et al Phys.Rev.Lett. 117 (2016), Bertone et al SciPost Phys. 5 (2018) 1, 008, Harland-Lang JHEP 79 (2019) 10]
- ➔ NLO EW corrections for all processes included in PDF fits [Frederix et al, JHEP 07 (2018) 185]

What is needed

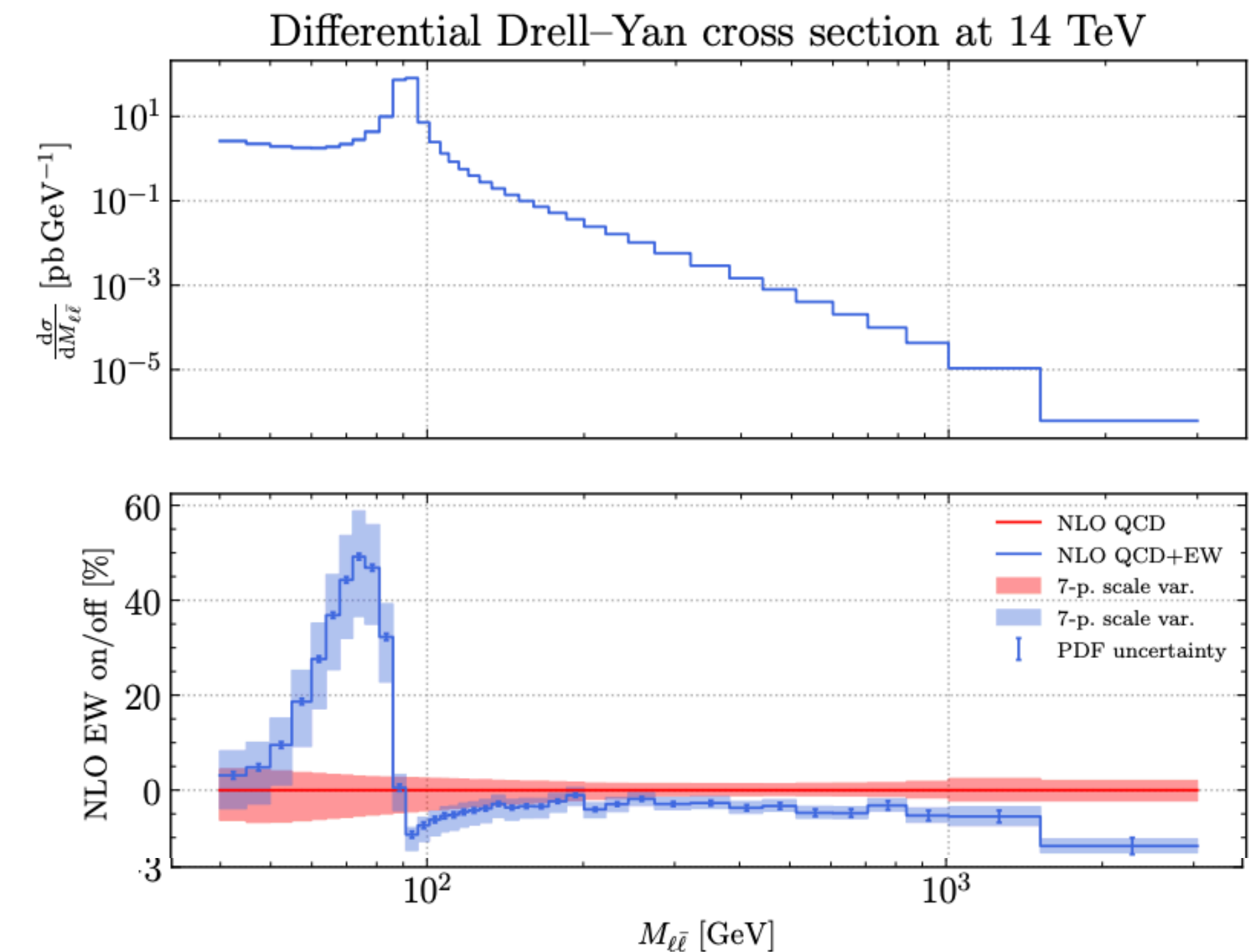


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- ➔ NLO EW corrections for all processes included in PDF fits [Frederix et al, JHEP 07 (2018) 185]
- ➔ Fast interpolating grids: PineAPPL [Carrazza, Nocera, Schwan, Zaro JHEP 12 (2020) 108]
- ➔ Careful scrutiny of data (no FSR nor photon-initiated subtraction & observable definition in experimental data)  
(see C. Schwan's talk on Friday)

What is needed

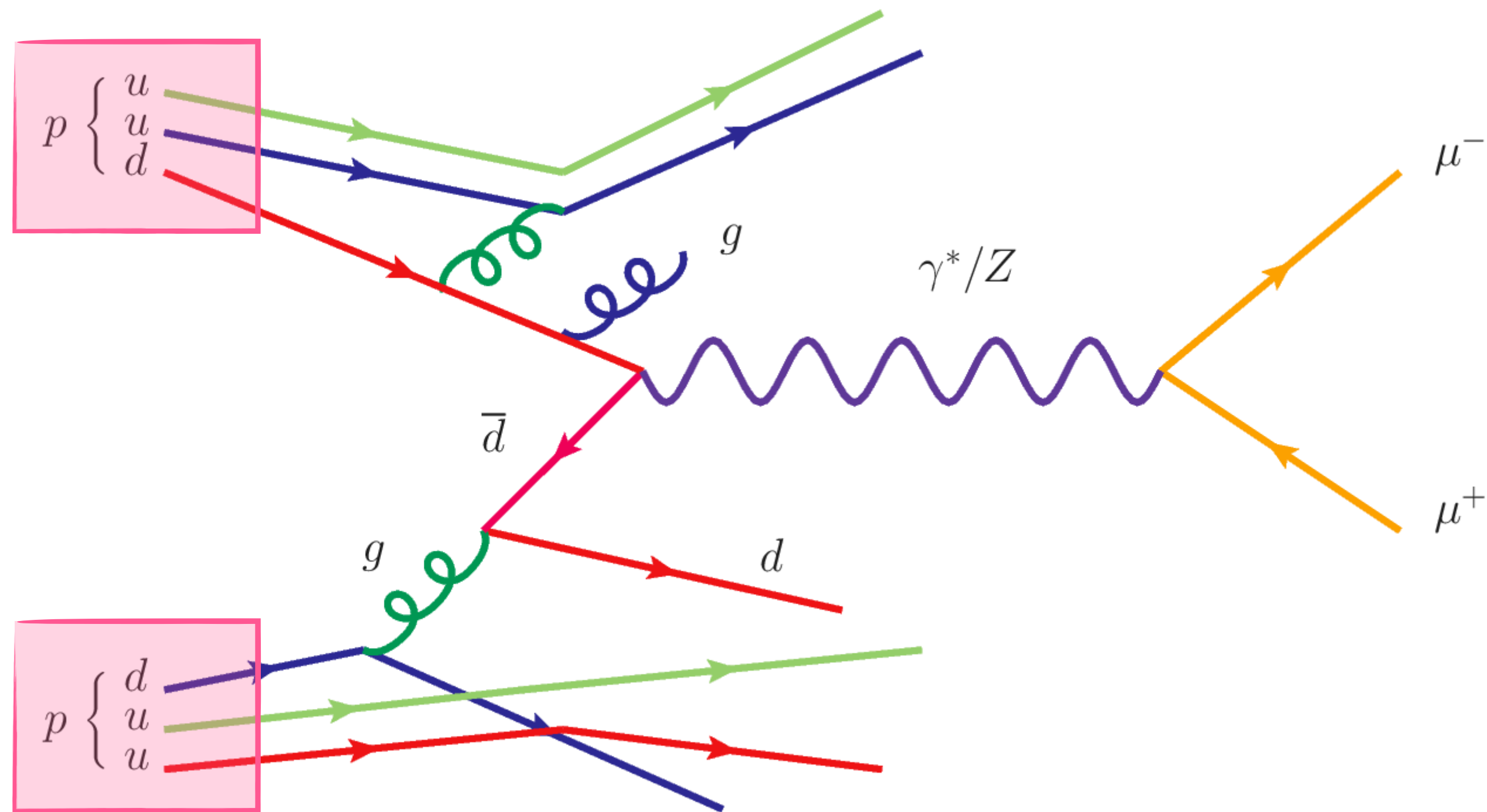


Carrazza, Nocera, Schwan, Zaro JHEP 12 (2020) 108

# PDFS AND NEW PHYSICS INTERPLAY IN HIGH ENERGY TAILS

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# PDF AND SMEFT FIT INTERPLAY

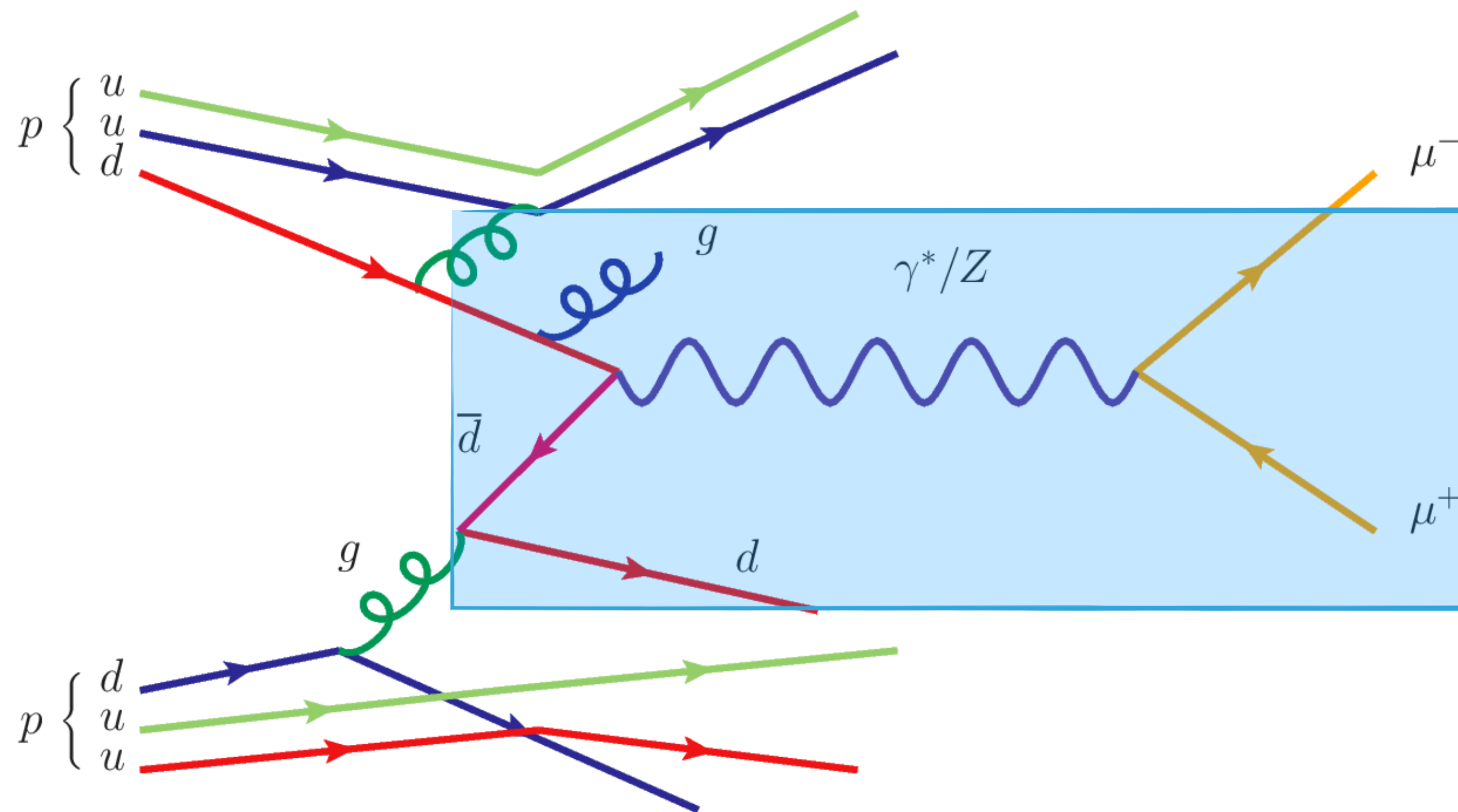


$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

LHC Data
 $f_i(\{\theta_k\})$ 
Assume SM in theory predictions

Fit PDF parameters  $\{\theta_i\}$

# PDF AND SMEFT FIT INTERPLAY

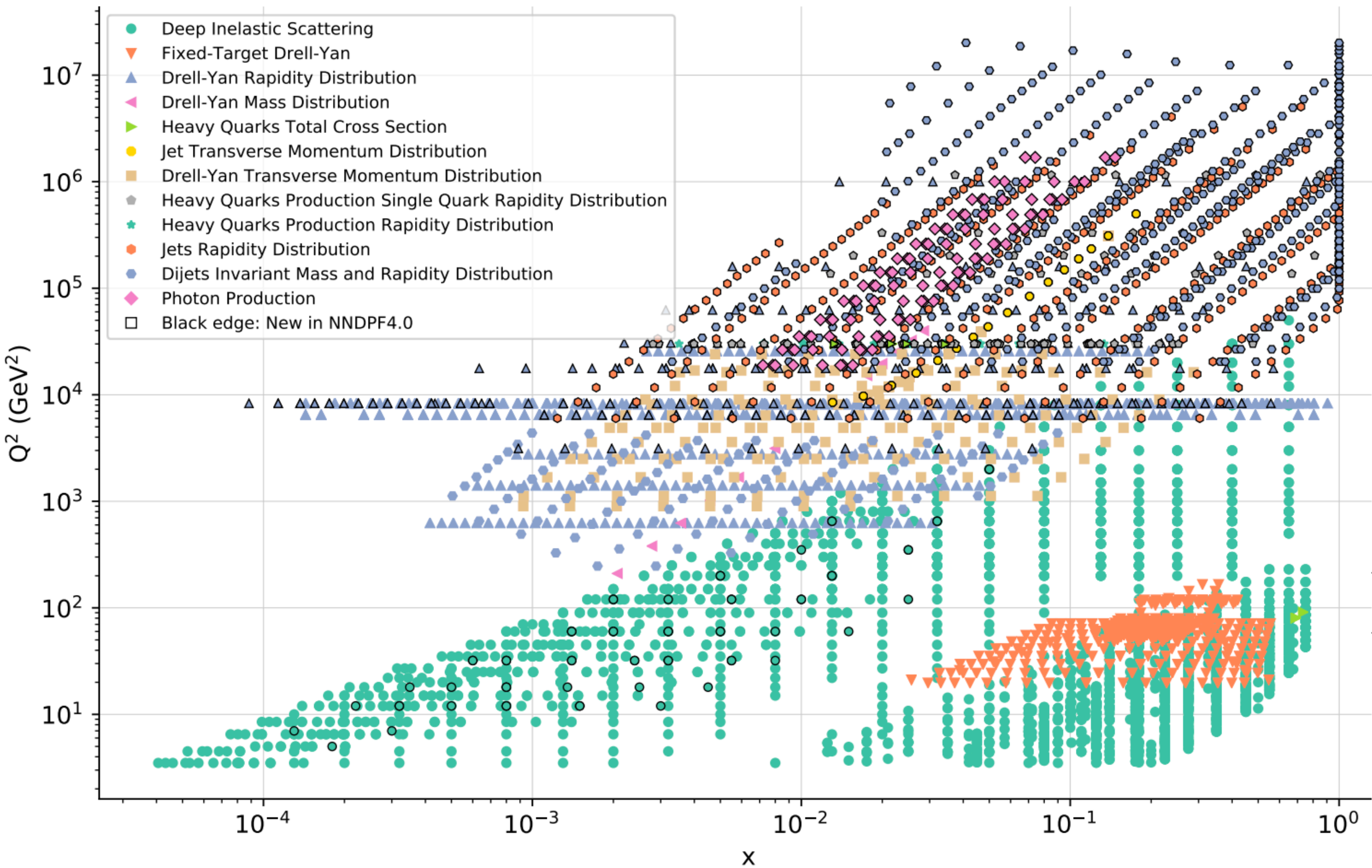


$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

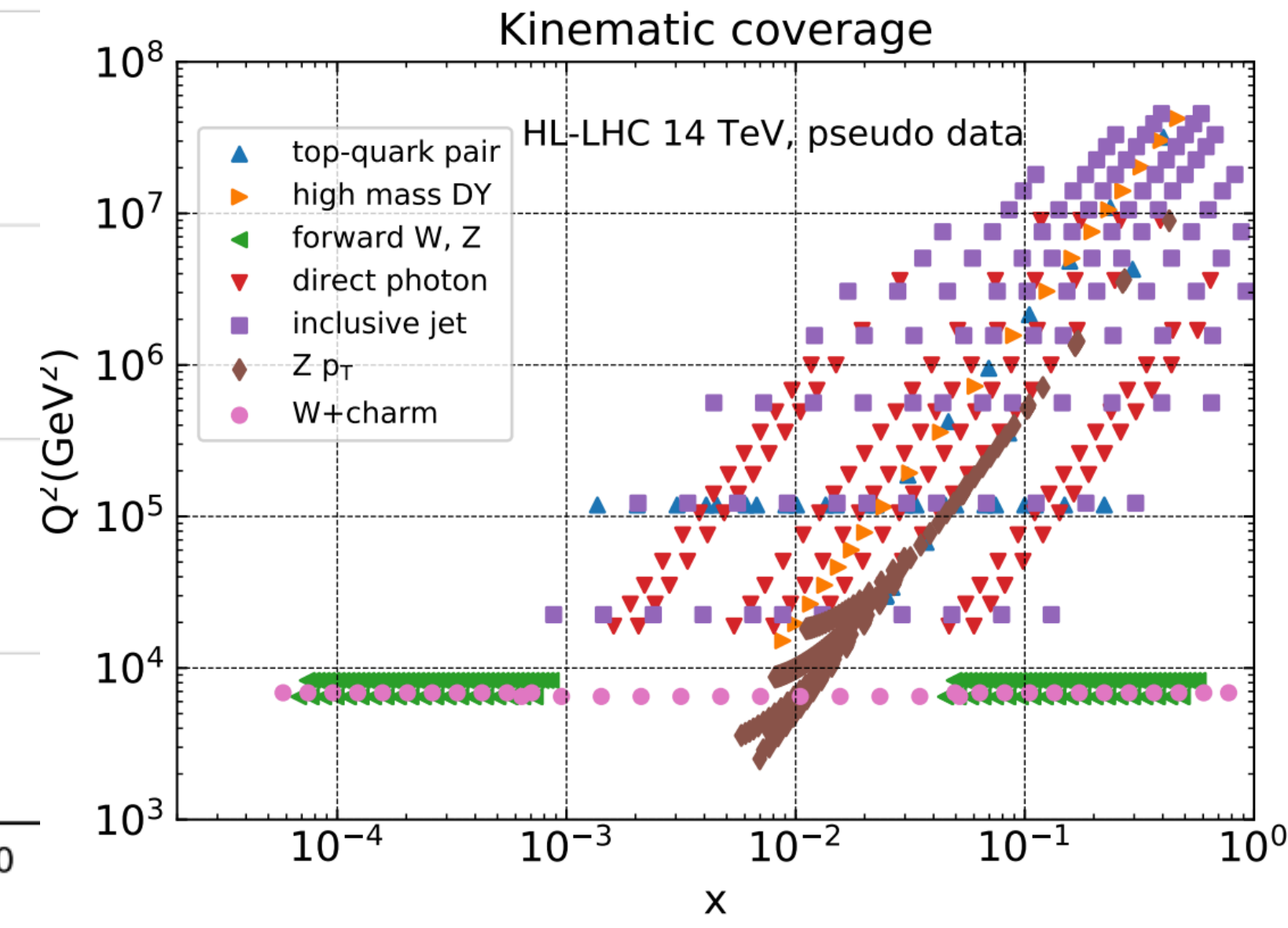
LHC Data
Assume SM PDFs
 $\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots$

Fit of Wilson Coefficients  $\{c_i\}$

# KINEMATIC OVERLAP



- ➡ Top pair production and single top data included in [Hartland et al 1901.05965]
- ➡ Dijets data in [Bordone et al 2103.10332] [Alioli et al 1706.03068]
- ➡ Drell-Yan data in [Farina et al 1609.08157, Torre et al 2008.12978]
- ➡ Inclusive jets in [Alte et al 1711.07484]
- ➡ Overlap enhanced in HL-LHC projections [Abdul Khalek et al 1810.03639]



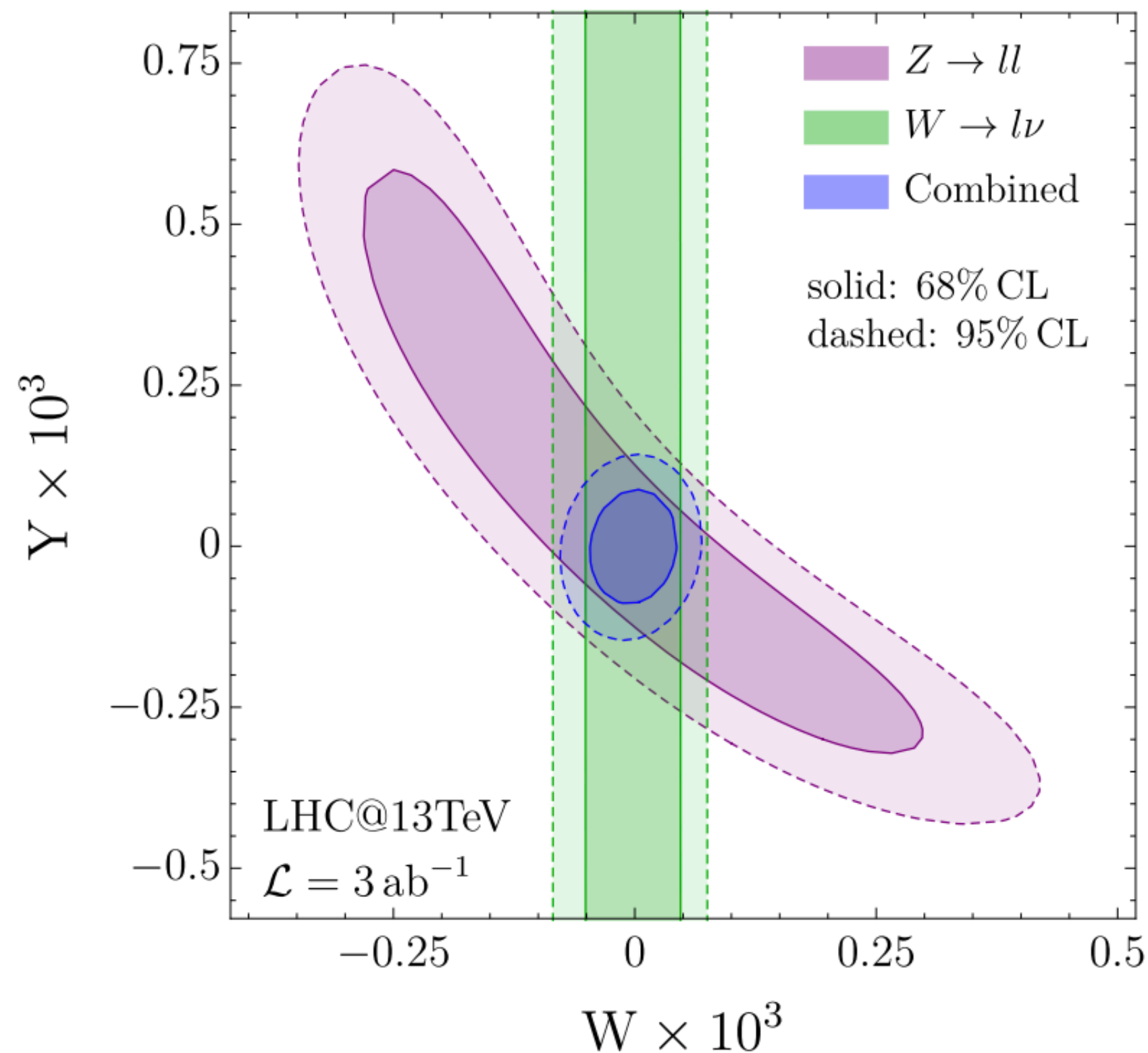


# SHOULD WE WORRY ABOUT PDF AND SMEFT INTERPLAY?

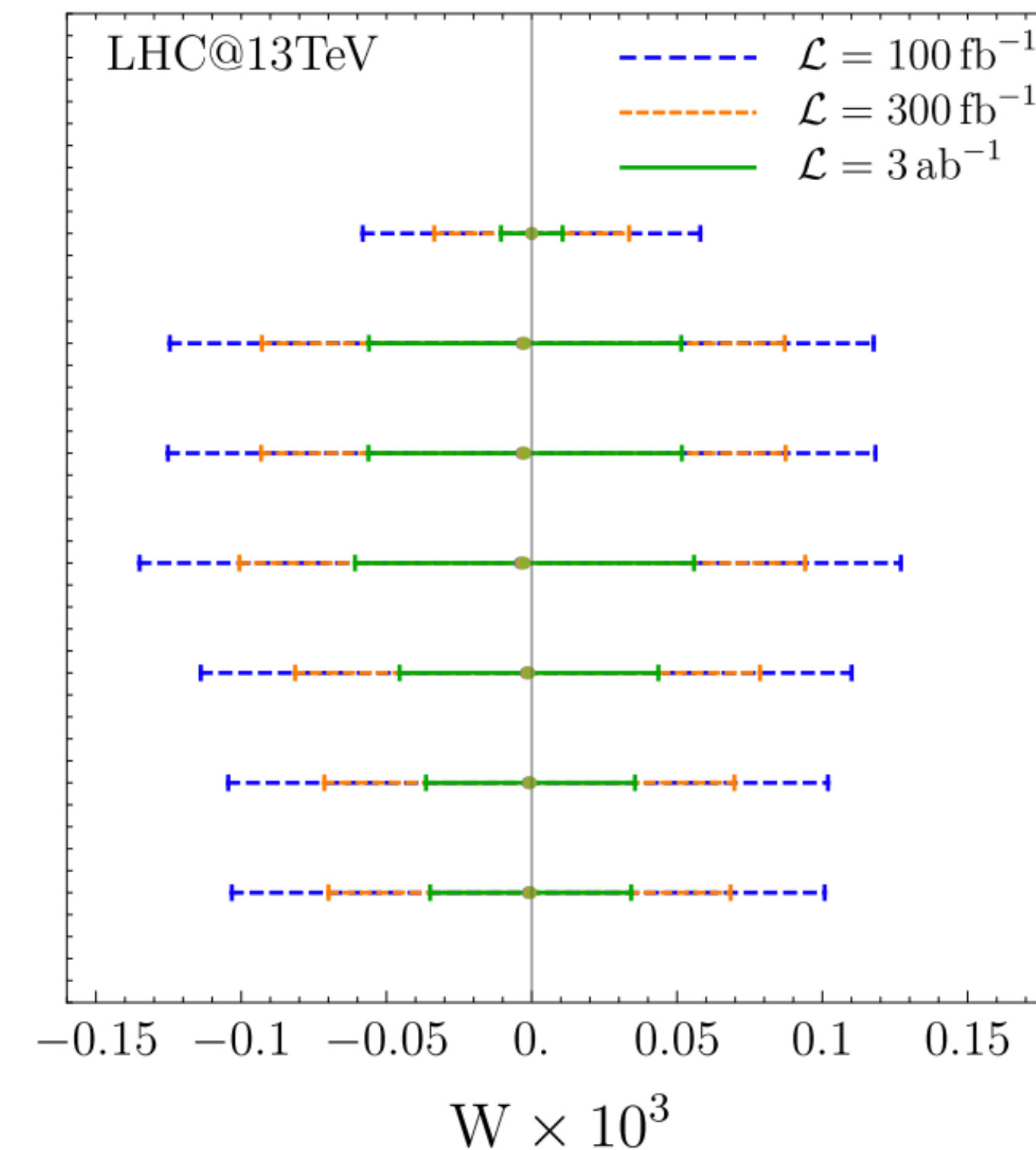
- First study of interplay in case of DIS data  
[Carrazza et al Phys.Rev.Lett. 123 (2019) 13, 132001]
- Case study: EW oblique corrections in high-mass NC and CC Drell-Yan tails
- They are powerful probes of quark-lepton contact interactions that produce growing-with-energy effects. [Torre et al, 2008.12978]

$$\mathcal{L}_{\text{SMEFT}} \supset -\frac{\hat{W}}{4m_W^2}(D_\rho W_{\mu\nu}^a)^2 - \frac{\hat{Y}}{4m_W^2}(\partial_\rho B_{\mu\nu})^2$$

Torre et al, 2008.12978



Combined bound



Only Stat

No Exp

No Syst

Baseline

Half PDF

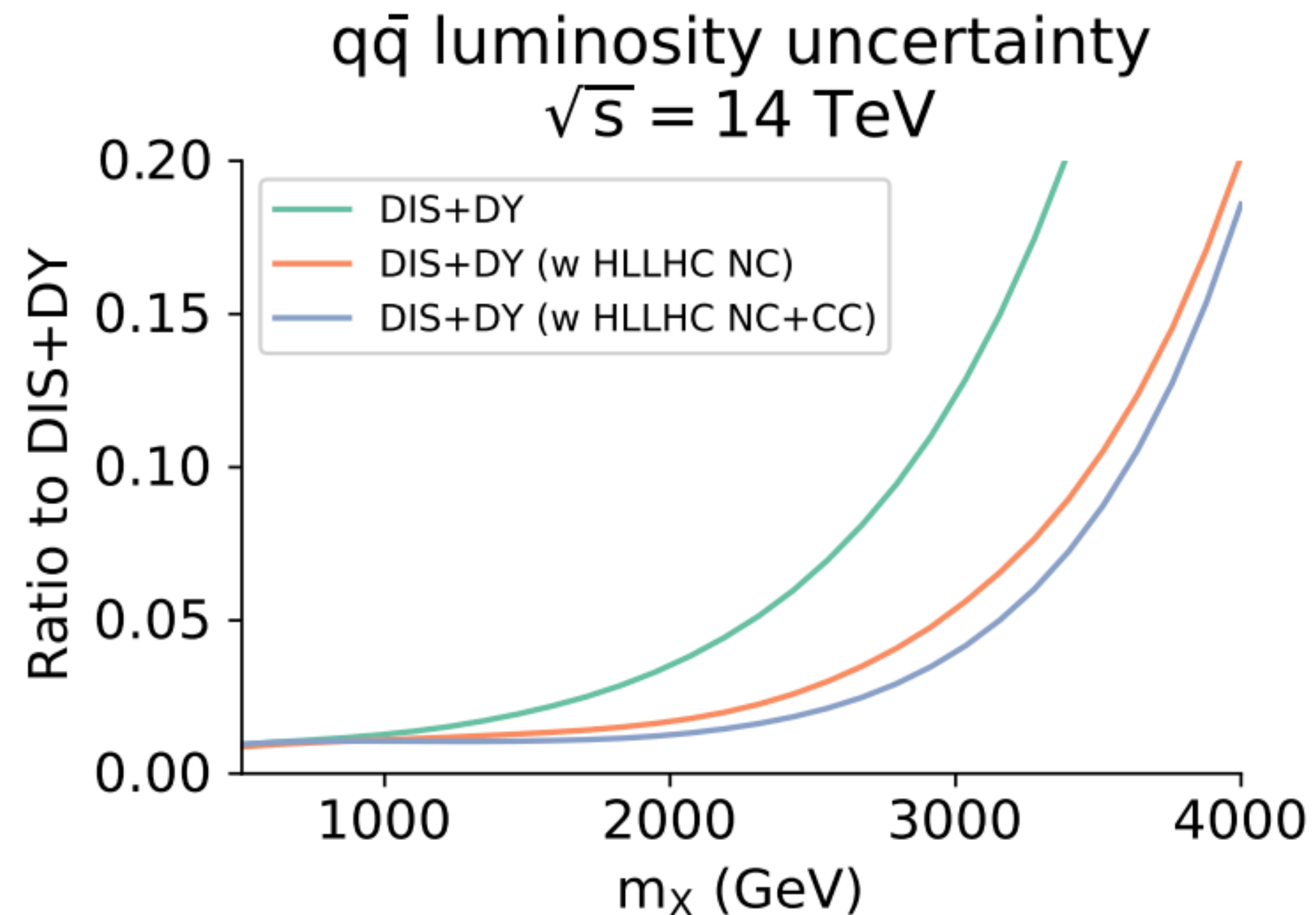
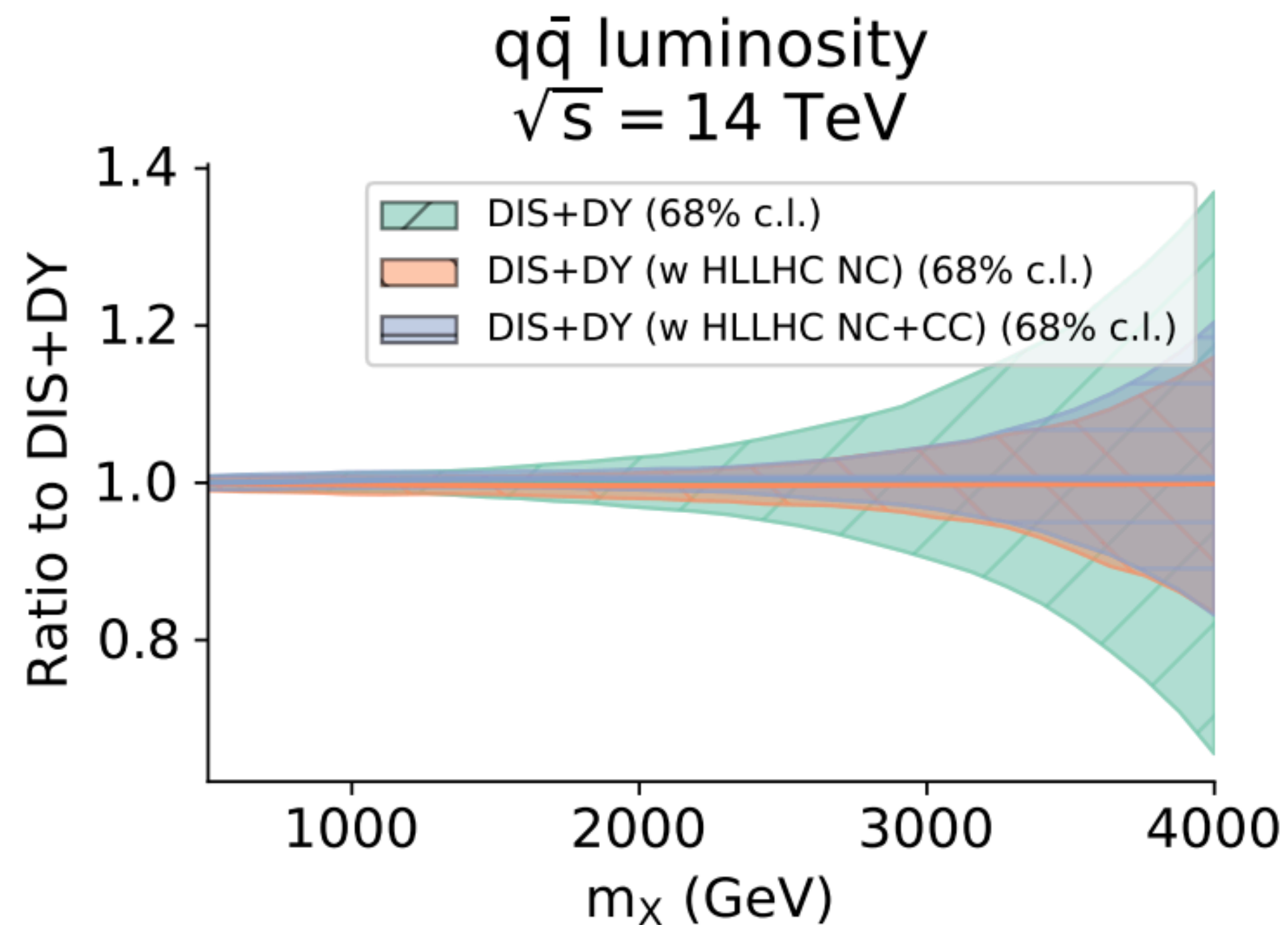
**No PDF**

No TH

PDF set: PDF4LHC15\_nlo\_30\_pdfas

# SHOULD WE WORRY ABOUT PDF AND SMEFT INTERPLAY?

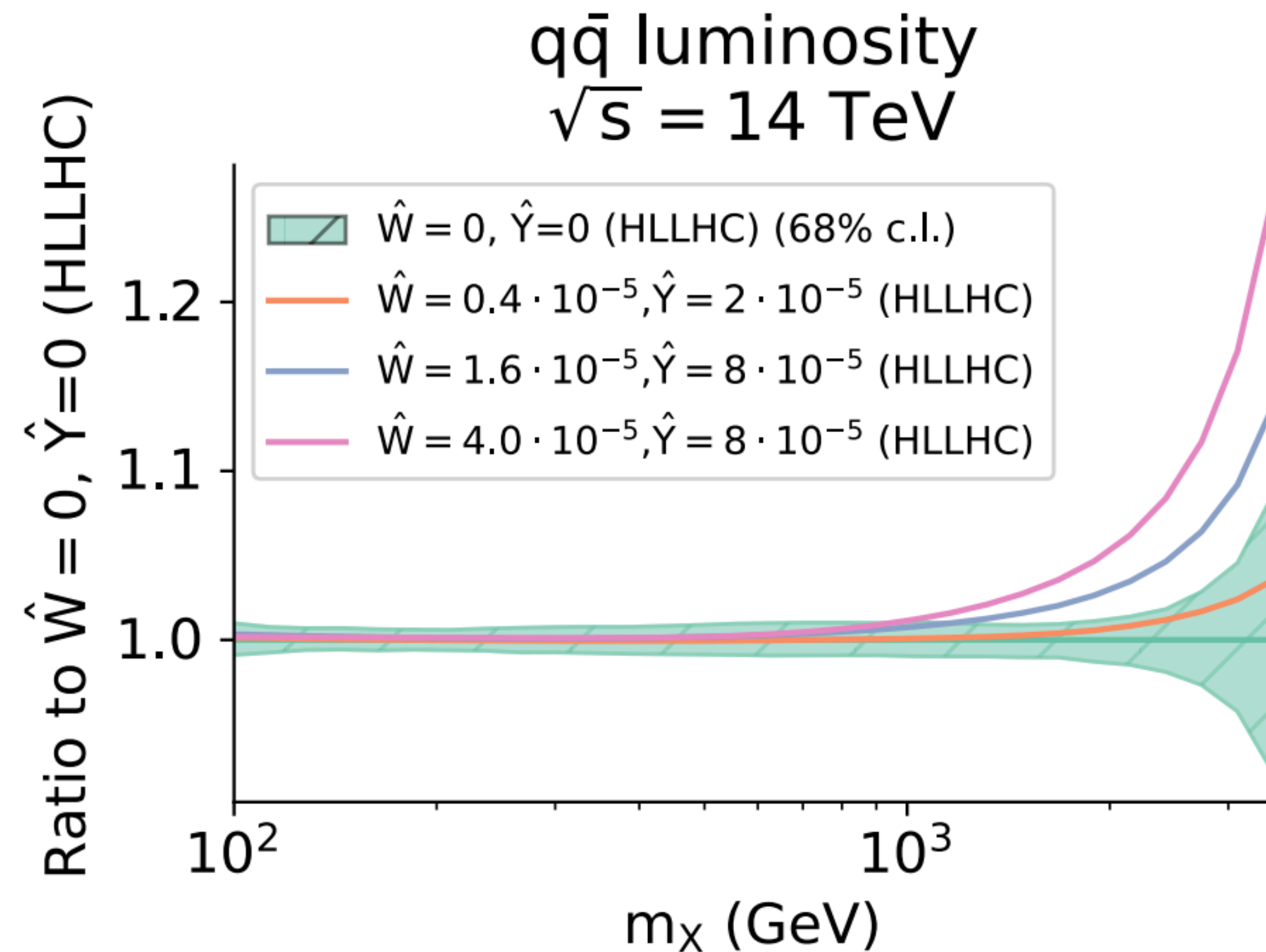
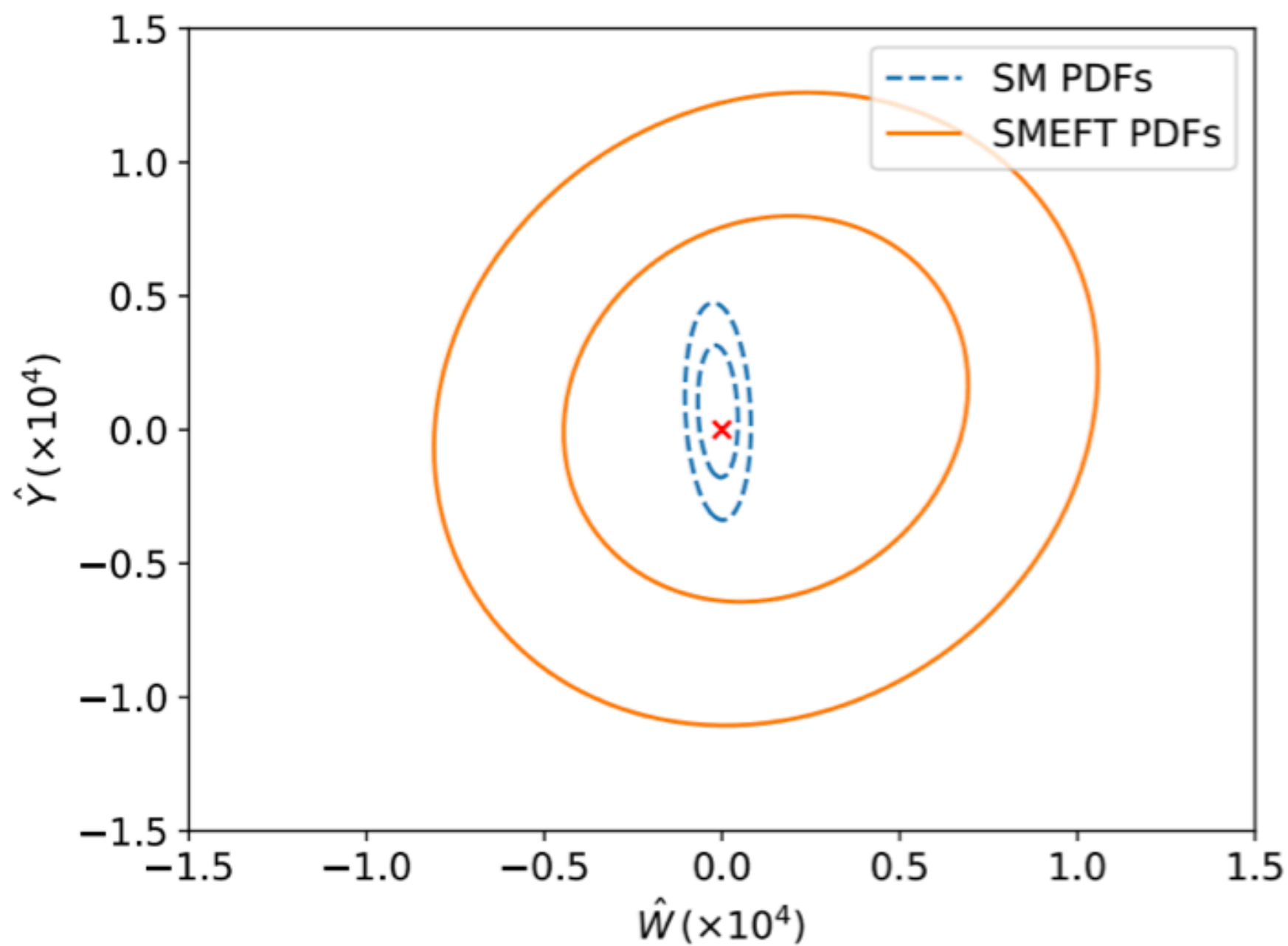
- A similar analysis has been performed, now with emphasis on PDF and their interplay with bounds on oblique operators + flavour-specific 4-fermion operator coupling muons and b-quarks in [Greljo et al, 2104.02723]
- Settings:
  - ➔ PDF fit based on DIS, Drell-Yan on-shell and low-mass data from ATLAS, CMS and LHCb
  - ➔ + Run I and II ATLAS and CMS high mass NC Drell-Yan data
  - ➔ + HL-LHC projections for NC and CC Drell-Yan data
  - ➔ SM predictions at NNLO QCD + NLO EW and SMEFT corrections added via local K-factors



# SHOULD WE WORRY ABOUT PDF AND SMEFT INTERPLAY?

- Non negligible interplay with Run I and Run II data, strong interplay at HL-LHC
- Compare Wilson coefficients bounds from HL-LHC projections assuming SM PDFs (that include NC+CC data) to the bounds on the same Wilson coefficients obtained from a simultaneous fit of PDFs and Wilson coefficients
- Not accounting for interplay (using PDFs as a black box) leads to over-constrained bounds
- Note that HL-LHC projections based on pseudo-data. Simultaneous fits of SMEFT and PDFs could point to a different minimum, and not only to larger uncertainties!

Greljo et al, 2104.02723



# CONCLUSIONS

- ▶ The path towards 1% accurate PDFs opens up new fascinating challenges
- ▶ Precise and accurate determination of the proton structure is key to make progress in precision phenomenology
- ▶ Need: robust methodology & solid statistical tests of methodology
- ▶ Benchmark effort would benefit of public releases of PDF codes and inputs!
  
- ▶ Current uncertainties partially underestimated due to theory uncertainty not accounted for at NNLO & other effects (fixed-order calculations [[Alekhin et al 2104.02400](#)], full account of electroweak corrections, resummations, nuclear corrections [[Ball et al 2105.05114](#)]...)
- ▶ Proposal for inclusion of missing higher order uncertainties has been assessed at NLO.  
To go at NLO, need development of evolution code with scale variations at NNLO
  
- ▶ Time to study the interplay between indirect new physics searches and PDFs
- ▶ The preferred avenue ahead is to be able to perform simultaneous fits (like for PDFs and  $\alpha_s$ )
- ▶ In parallel a more careful investigation of definition of "safe" PDF sets & account for PDF uncertainties

**THANK YOU FOR YOUR ATTENTION!**