

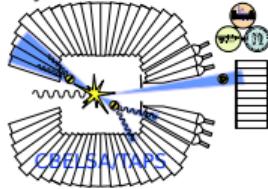
Recent results on baryon spectroscopy at ELSA and MAMI

QCHSC 2024

Farah Afzal for the CBELSA/TAPS and A2 collaboration

21.08.2024

University of Bonn

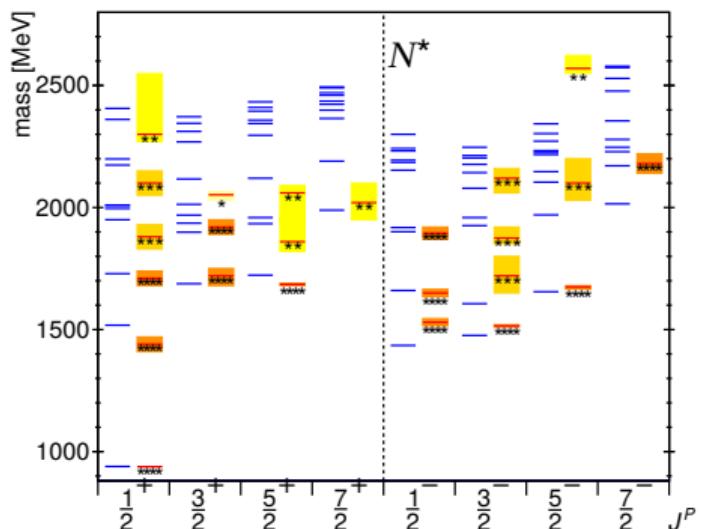


Light baryon spectroscopy

Light baryon excitation spectrum

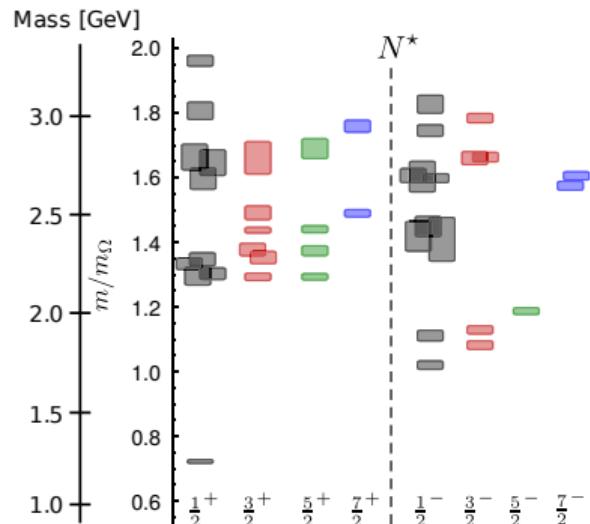
Bound states of strong QCD are not yet understood!

Quark model vs. experimental data



[U. Loering, B.C. Metsch, H.R. Petry, EPJA 10 (2001) 395-446]

Lattice QCD



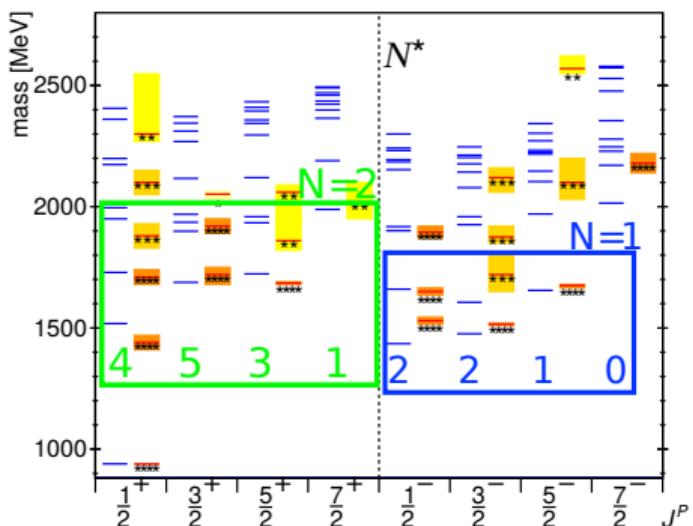
[R. G. Edwards et al., Phys. Rev. D 84 (2011) 074508]

- Discrepancy between theory and experiment: missing resonances, systematics of spectrum

Light baryon excitation spectrum

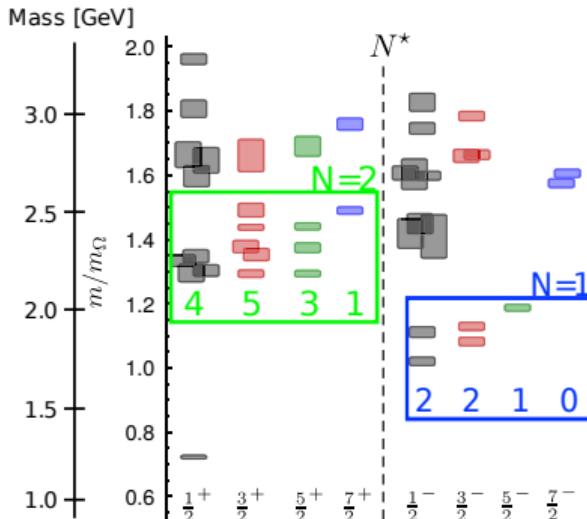
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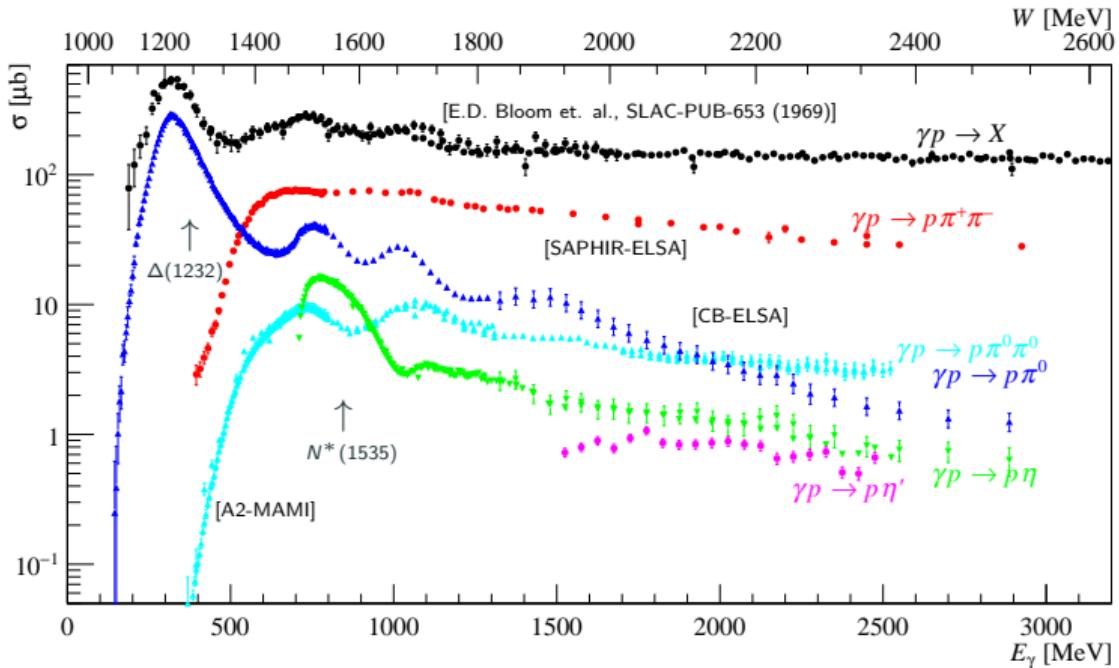
Lattice QCD



[R. G. Edwards et al., Phys. Rev. D 84 (2011) 074508]

- Discrepancy between theory and experiment: missing resonances, systematics of spectrum
- most resonances observed in elastic πN scattering until 2010 → experimental bias?

Worldwide effort to get high precision data (ELSA, MAMI, JLab, SPring-8, ...)



[A. Thiel, F. Afzal, Y. Wunderlich, Prog. Part. Nucl. Phys. 125 (2022) 103949]

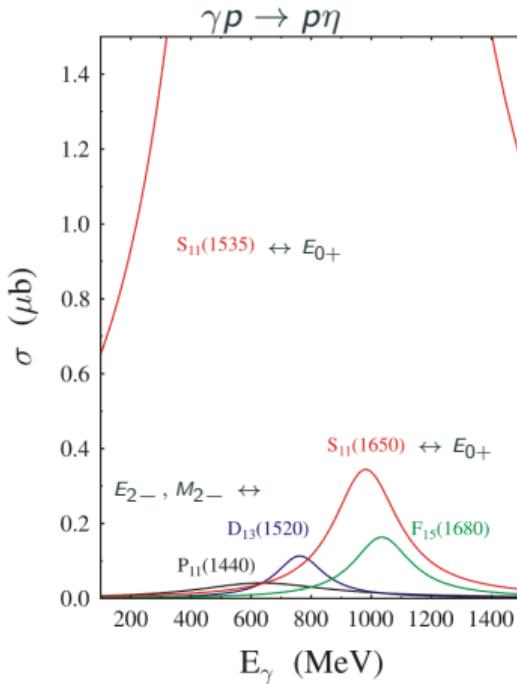
- Photoproduction reactions are an excellent tool to probe excitation spectra!
- Resonances contribute with different strength to distinct channels
- How can we disentangle contributing resonances?

Polarization observables in the 2-body kinematic system for the photoproduction of a pseudoscalar meson

Photon polarization		Target polarization	Recoil nucleon polarization	Target and recoil polarizations
		X Y Z _(beam)	X' Y' Z'	X' X' Z' Z' X Z X Z
unpolarized	σ	- T -	- P -	$T_{x'}$ $L_{x'}$ $T_{z'}$ $L_{z'}$
linear	$-\Sigma$	H (-P) -G	O _{x'} (-T) O _{z'}	(-L _z) (T _z) (L _x) (-T _x)
circular	-	F - -E	C _{x'} - C _{z'}	- - - -

$\sigma, \Sigma, T, P + 4$ double pol. observables needed for a unique solution

[W. Chiang and F. Tabakin, Phys. Rev., C55 (1997) 2054-2066]



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circular	-	F - -E	C _{x'} - C _z	- - - -

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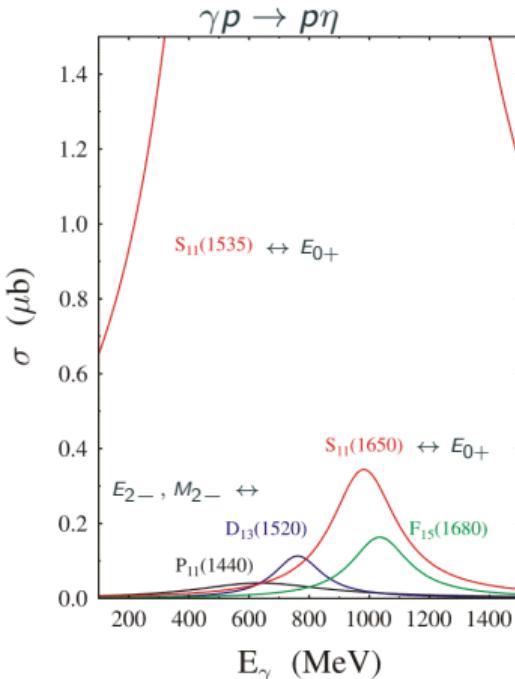
[W. Chiang and F. Tabakin, Phys. Rev., C55 (1997) 2054-2066]

$$\sigma \sim |E_{0+}|^2 + |E_{1+}|^2 + |M_{1+}|^2 + |M_{1-}|^2 + \dots$$

$$\Sigma \sim \underbrace{-2E_{0+}^* E_{2+} + 2E_{0+}^* E_{2-} - 2E_{0+}^* M_{2+} + 2E_{0+}^* M_{2-}}_{< S, D >} + \dots$$

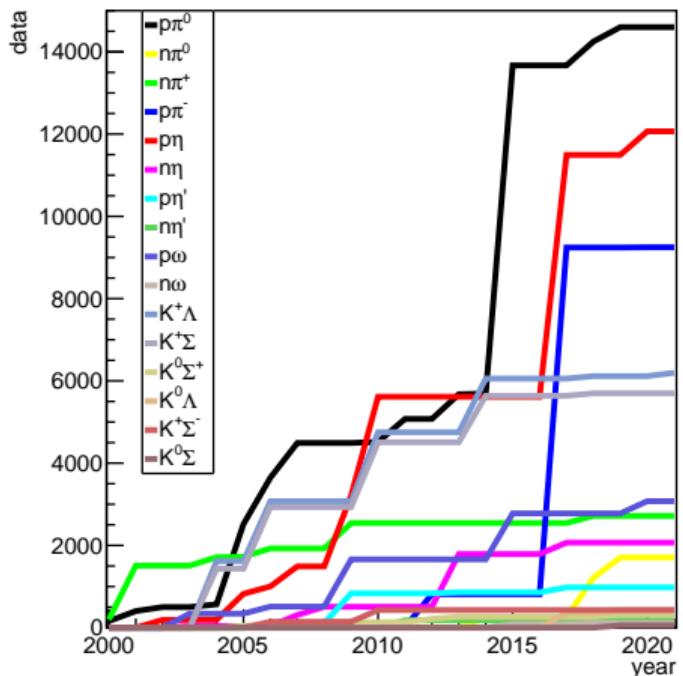
→ Polarization observables are sensitive to interference terms!

→ Interferences with the dominant *S*-wave (E_{0+}) important in η photoproduction!

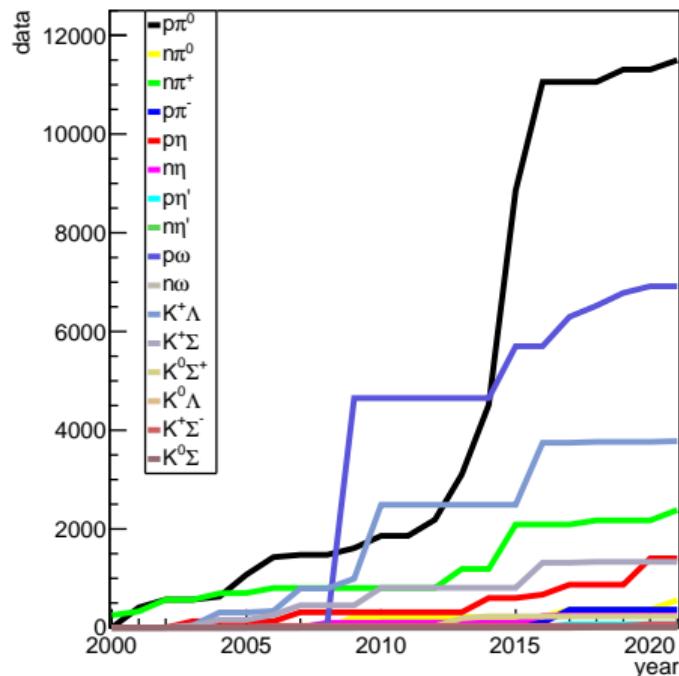


Development of database

Unpolarized cross section



Polarization observables



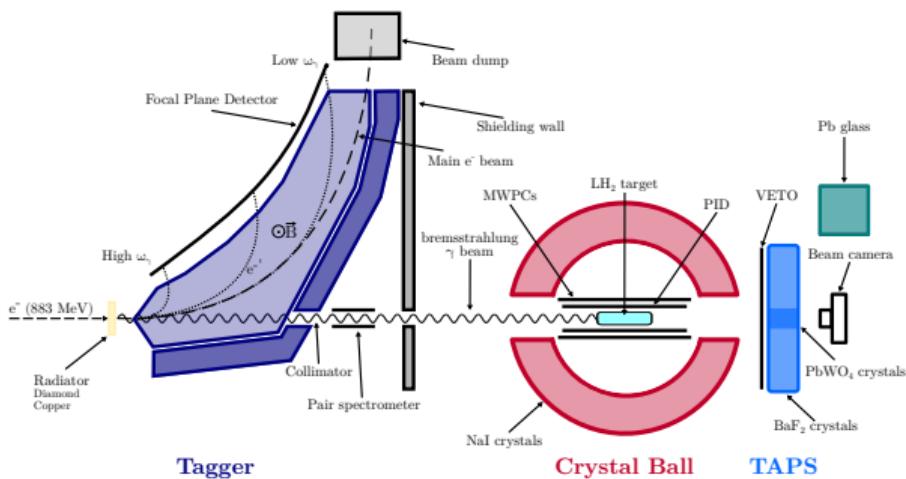
[A. Thiel, F. Afzal, Y. Wunderlich, Prog. Part. Nucl. Phys. 125 (2022) 103949]

Experimental facilities at MAMI and ELSA

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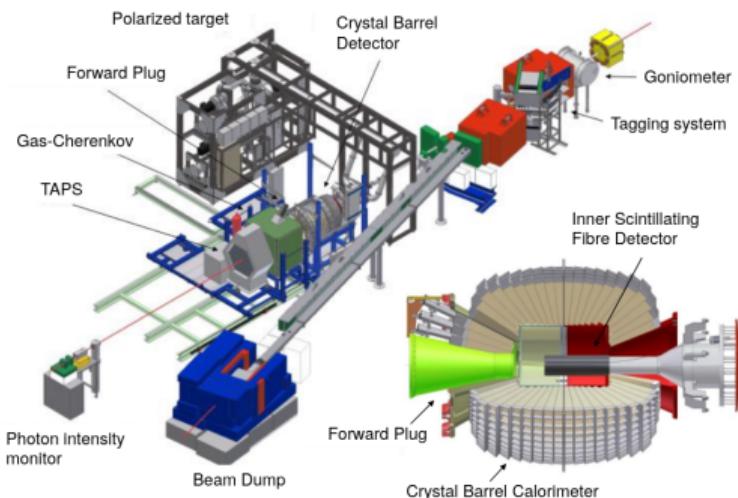
A2@MAMI

- Electron beam: 0.18 GeV - 1.6 GeV
- Continuous beam
- Crystal Ball (NaI) + TAPS (BaF₂ & PbWO₄)
- PID, MWPCs, Vetos



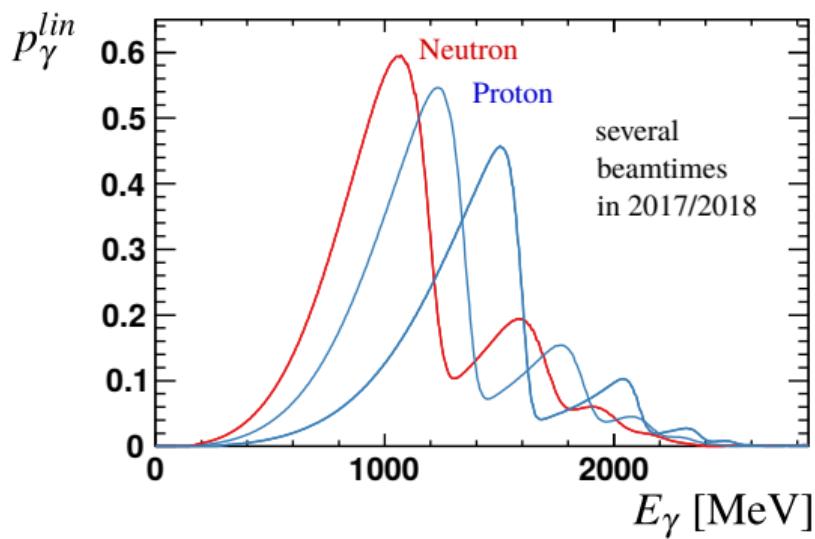
CBELSA/TAPS@ELSA:

- Electron beam: 0.6 GeV - 3.2 GeV
- Quasi-continuous beam
- Crystal Barrel (CsI) + MiniTAPS (BaF₂)
- Inner detector, Vetos



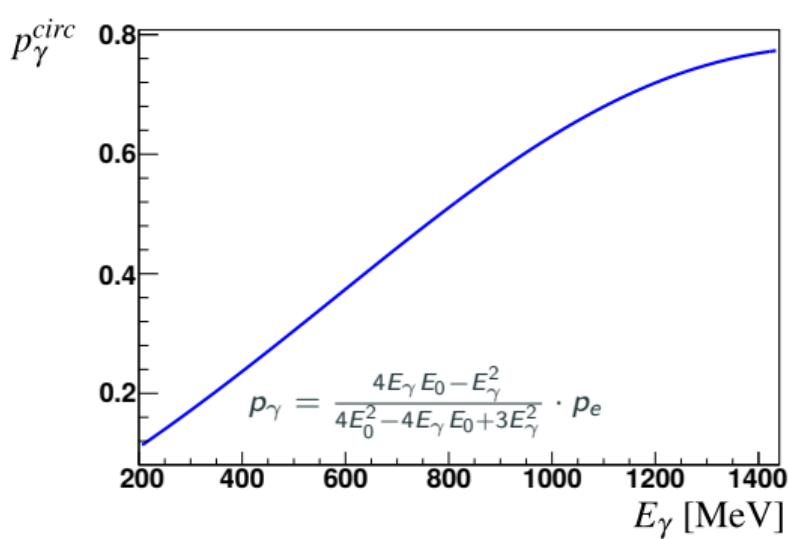
Linearly polarized photons

- diamond radiator needed
- coherent bremsstrahlung
- coherent edges at: e.g. 1200 MeV

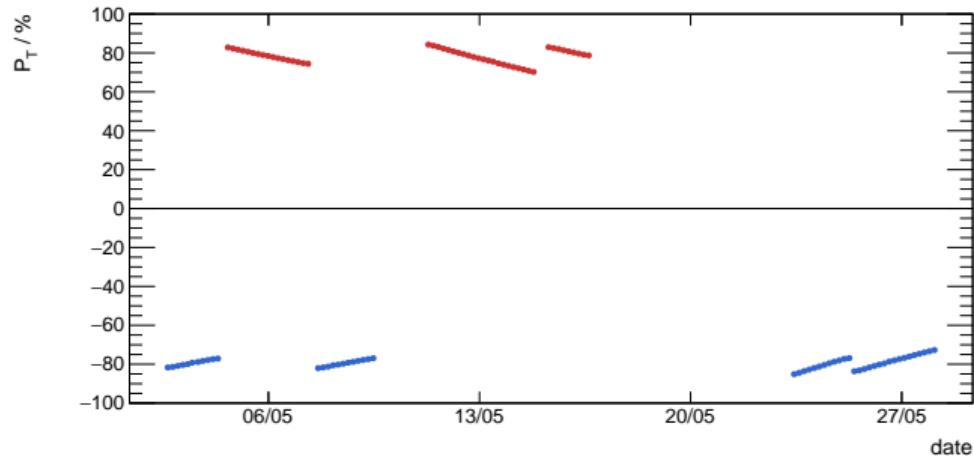


Circularly polarized photons

- long. polarized electrons needed
- helicity transfer to photons
- Mott/Møller measurement: $p_e \approx 75\% - 78\%$

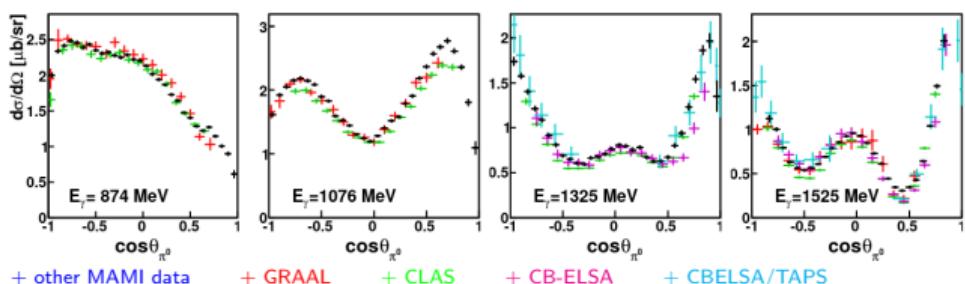
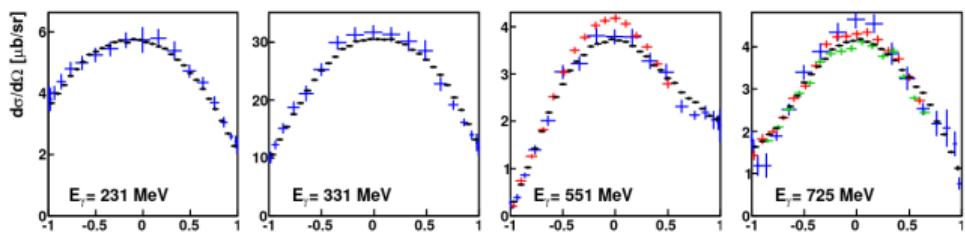
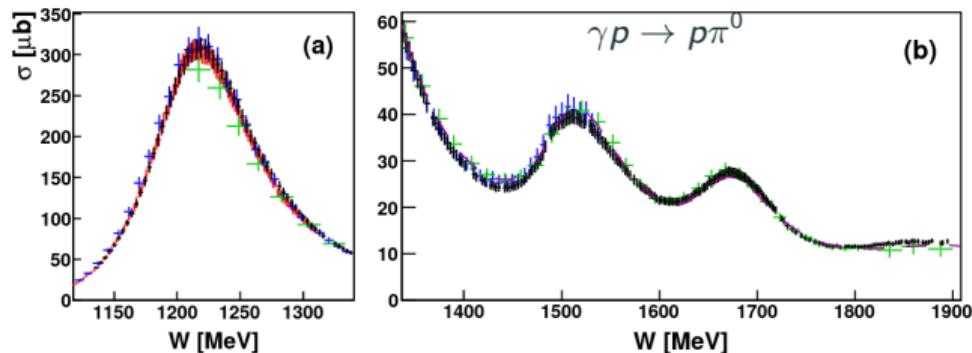


- Collaboration between Bonn (H. Dutz), Mainz (A. Thomas) and Bochum (G. Reicherz)
- polarization via Dynamic Nuclear Polarization DNP
- maximal pol. degree: $p_T \approx 89\%$
- relaxation times: 1800 h - 2000 h



Measurements off protons ($\gamma p \rightarrow p\pi^0$)

$\gamma p \rightarrow p\pi^0$: Measurement of cross sections (A2)



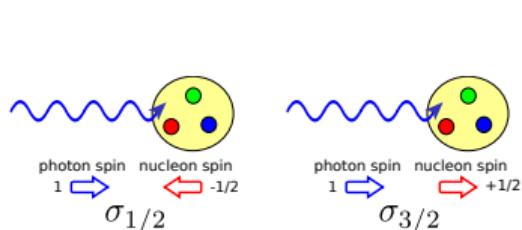
P. Adlarson et al., Phys. Rev. C92.2 (2015), p. 024617

+ other MAMI data, + other MAMI data, + CB-ELSA

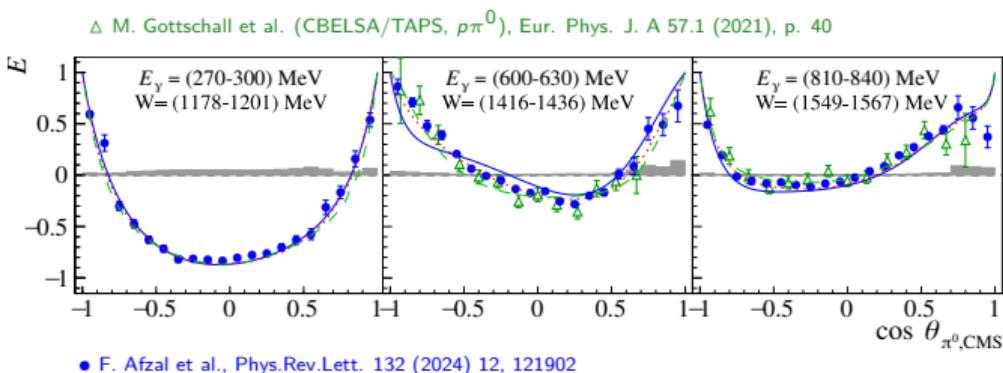
- fine energy binning
- full angular coverage
- increases existing data by 47%

Elliptically polarized photons (long. pol. electrons + diamond) and longitudinally polarized target:

$$\frac{d\sigma}{d\Omega}(\theta, \phi) = \frac{d\sigma}{d\Omega_0}(\theta) [1 - P_{lin}\Sigma \cos(2(\alpha - \phi)) - P_z(-P_{lin}G \sin(2(\alpha - \phi)) + P_{circ}E)]$$

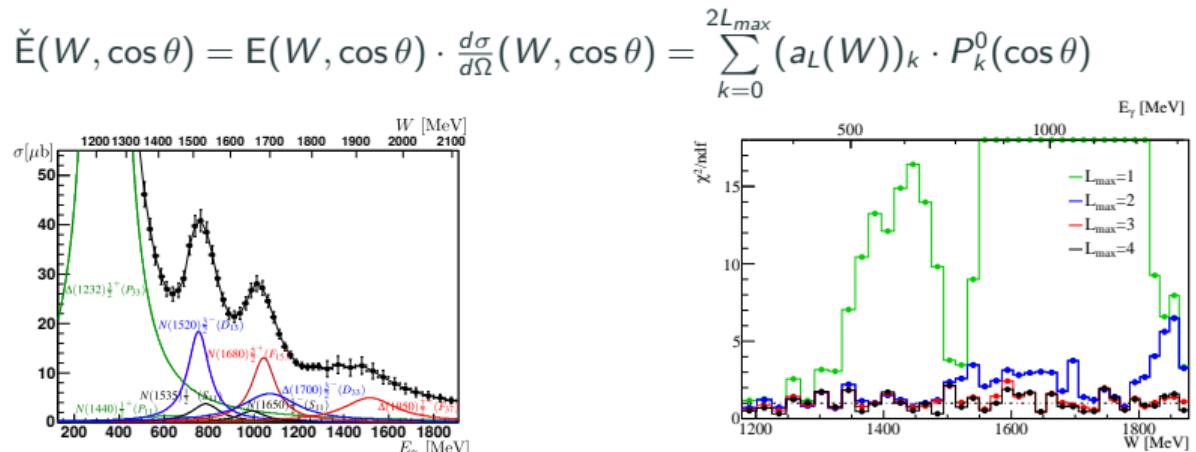


Helicity asymmetry: $E = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}$



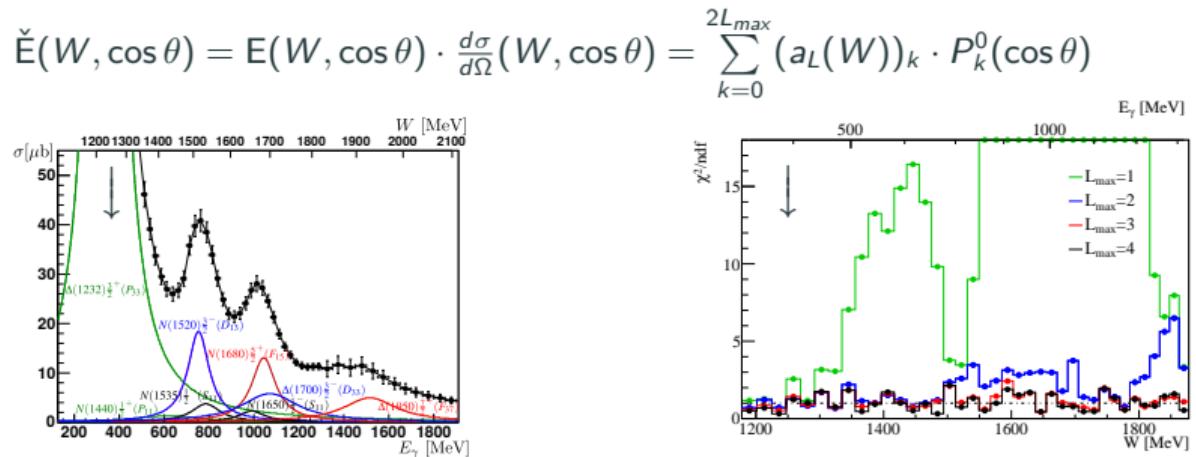
- Excellent agreement between A2 (diamond) and CBELSA/TAPS (amorphous)!
- Time and cost efficient measurement possible!

$\gamma p \rightarrow p\pi^0$: Dominant partial wave contributions (E (A2))

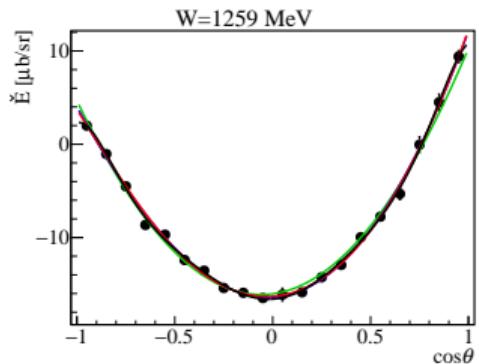


[Y. Wunderlich, F. Afzal et al., EPJA 53 (2017) 86]

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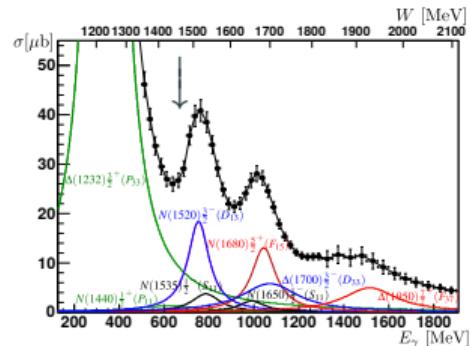


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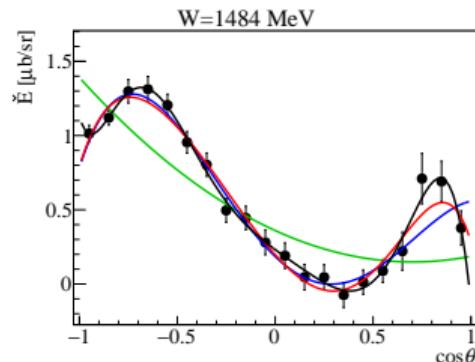
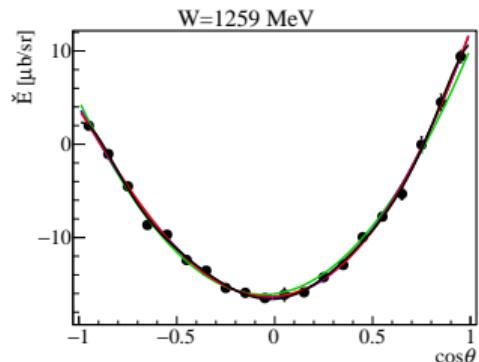
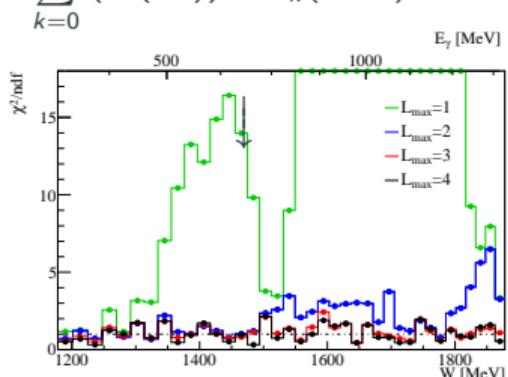


$\gamma p \rightarrow p\pi^0$: Dominant partial wave contributions (E (A2))

$$\check{E}(W, \cos \theta) = E(W, \cos \theta) \cdot \frac{d\sigma}{d\Omega}(W, \cos \theta) = \sum_{k=0}^{2L_{\max}} (a_L(W))_k \cdot P_k^0(\cos \theta)$$

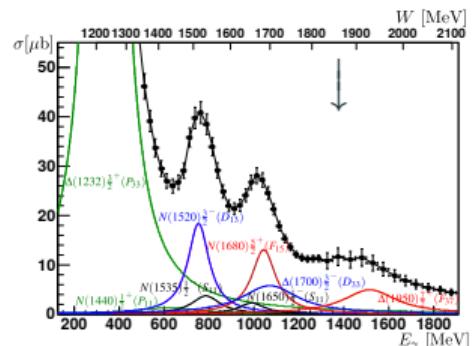


[Y. Wunderlich, F. Afzal et al., EPJA 53 (2017) 86]

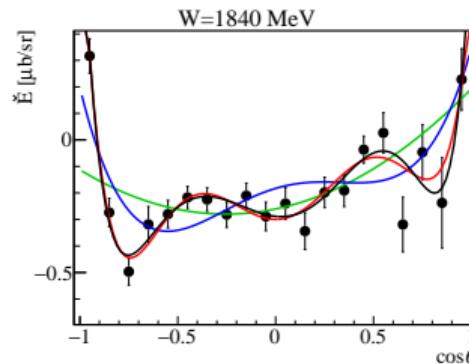
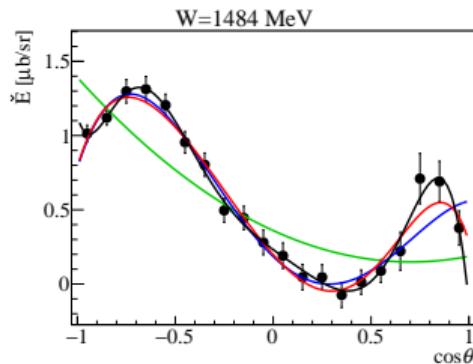
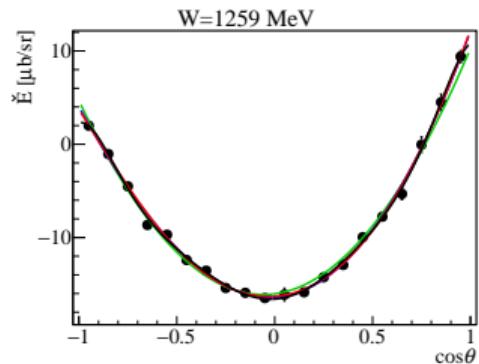
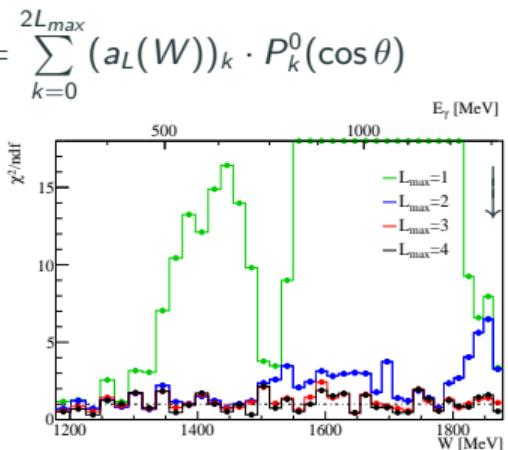


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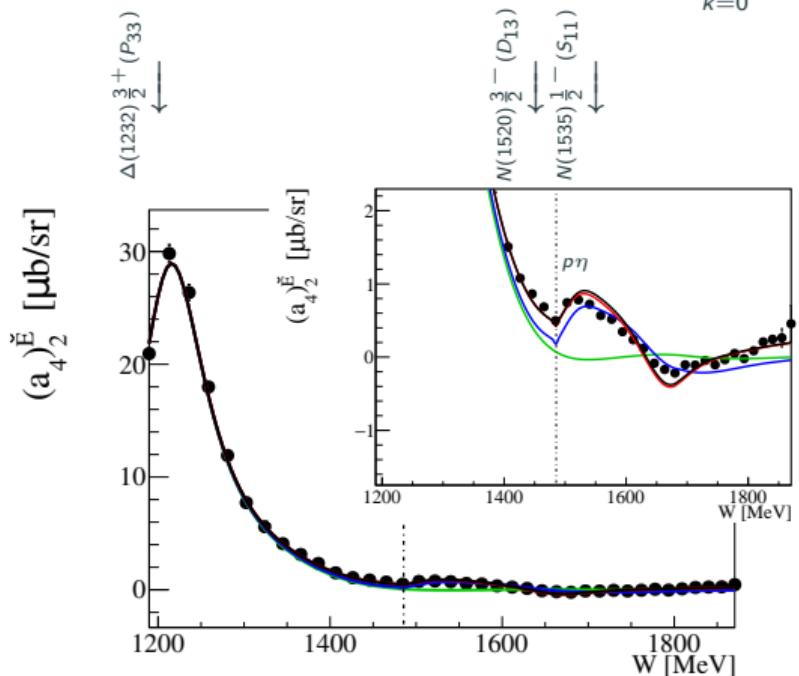


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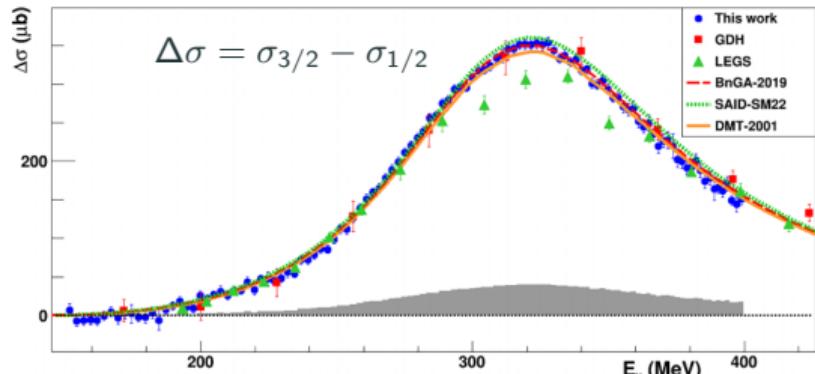
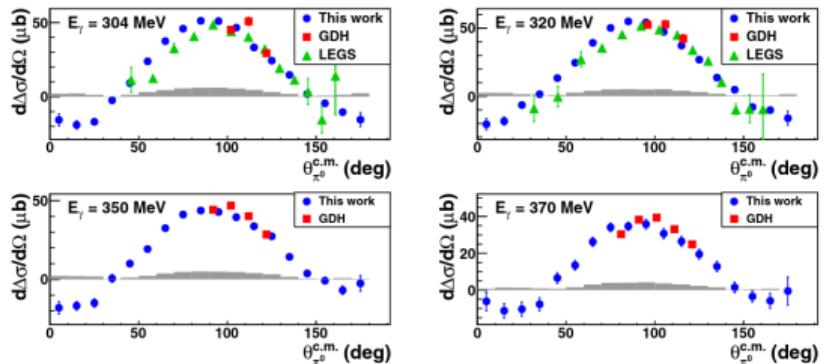
[F. Afzal et al., Phys.Rev.Lett. 132 (2024) 12, 121902]

$$\begin{aligned}
 (a_4)_2^{\check{E}} &= \langle P, P \rangle \\
 &+ \langle S, D \rangle + \langle D, D \rangle \\
 &+ \langle P, F \rangle + \langle F, F \rangle \\
 &+ \langle D, G \rangle + \langle G, G \rangle
 \end{aligned}$$

$p\eta$ cusp is well visible in the data and BnGa-2014-02 PWA ($\langle S, D \rangle$).

$E2/M1$ ratio in the $N \rightarrow \Delta(1232)$ transition (A2)

- Measurement with MAMI - 450 MeV e^- beam; New precision data for $\gamma p \rightarrow \pi^0 p$
- Quantify deviation from a spherical shape for the nucleon and/or the $\Delta(1232)$ resonance
→ Measurement of the resonant quadrupole transition ($E2$) relative to the resonant dipole transition ($M1$)
- Helicity dependent cross section in the $\Delta(1232)$ region
$$\Delta\sigma = \sigma_{3/2} - \sigma_{1/2}$$



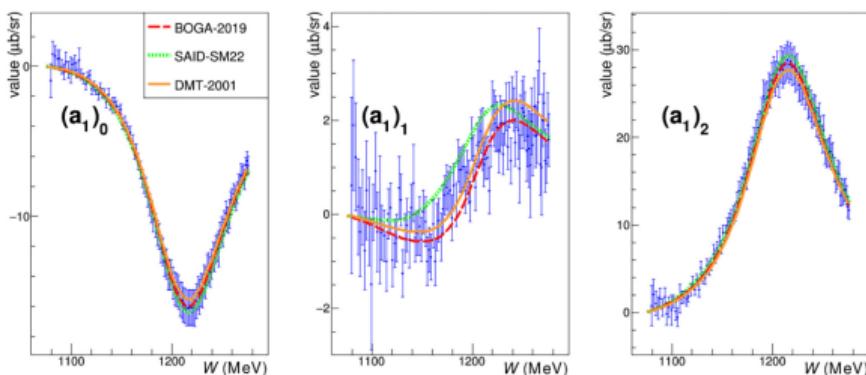
$E2/M1$ ratio in the $N \rightarrow \Delta(1232)$ transition (A2)

Legendre moment analysis truncating at

$L_{max} = 1$ (S and P -wave):

$$(a_1)_0 \simeq -\text{Im}[M_{1+}]^2 + 6\text{Im}[E_{1+}]\text{Im}[M_{1+}] ;$$

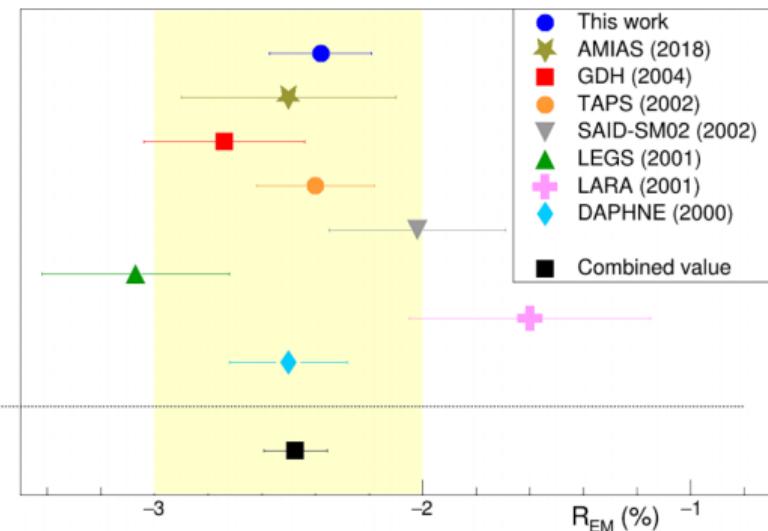
$$(a_1)_2 \simeq 2\text{Im}[M_{1+}]^2 - 2\text{Im}[M_{1-}]\text{Im}[M_{1+}] \simeq 2\text{Im}[M_{1+}]^2$$



$$R_L = \frac{1}{3} \frac{(a_1)_0}{(a_1)_2} + \frac{1}{6} \simeq R_{EM}$$

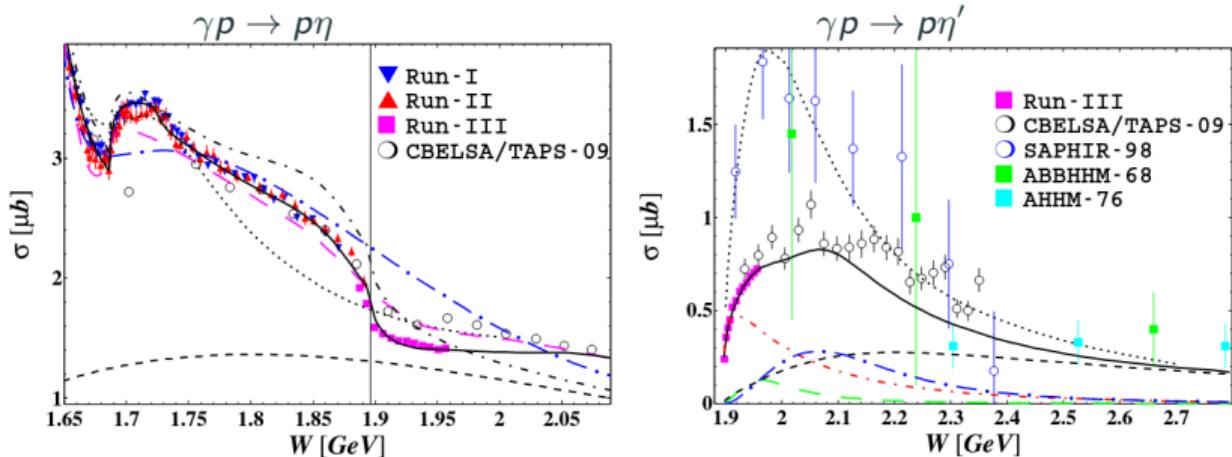
$$R_{EM} = \frac{E2}{M1} \equiv \left. \frac{\text{Im}[E_{1+}^{3/2}]}{\text{Im}[M_{1+}^{3/2}]} \right|_{M_\Delta}$$

E. Mornacchi et al., Phys.Rev.C 109 (2024) 5, 055201



Measurements off protons ($\gamma p \rightarrow p\eta$)

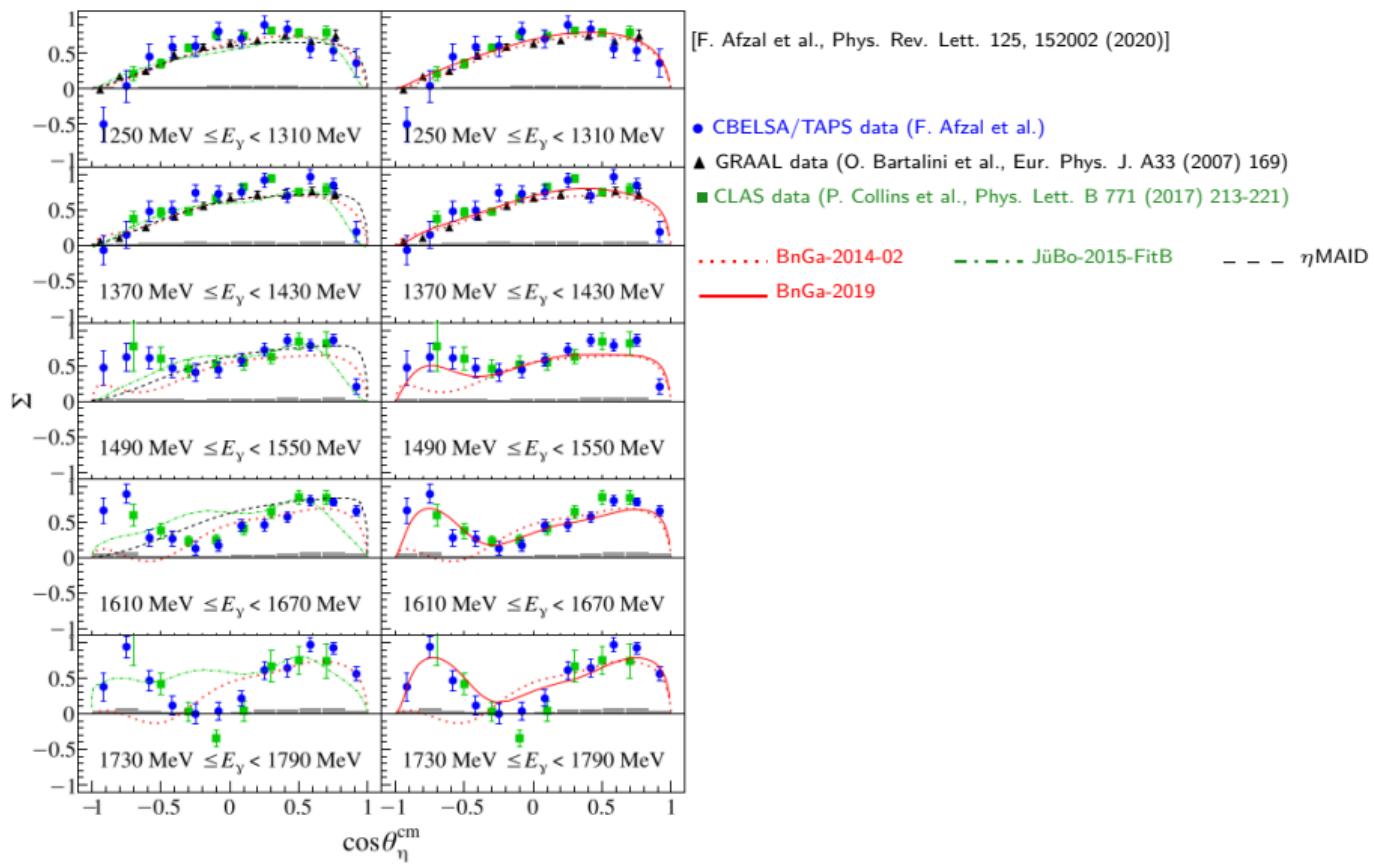
$\gamma p \rightarrow p\eta$: Measurement of cross sections (A2)



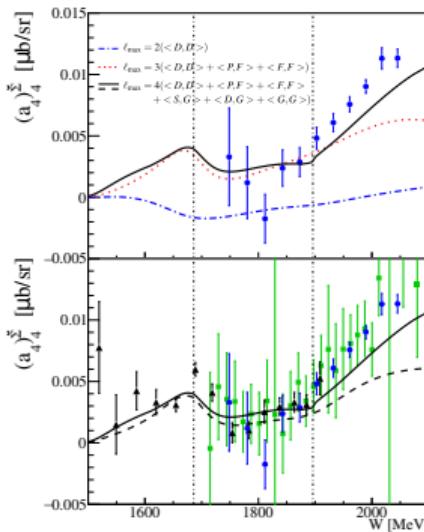
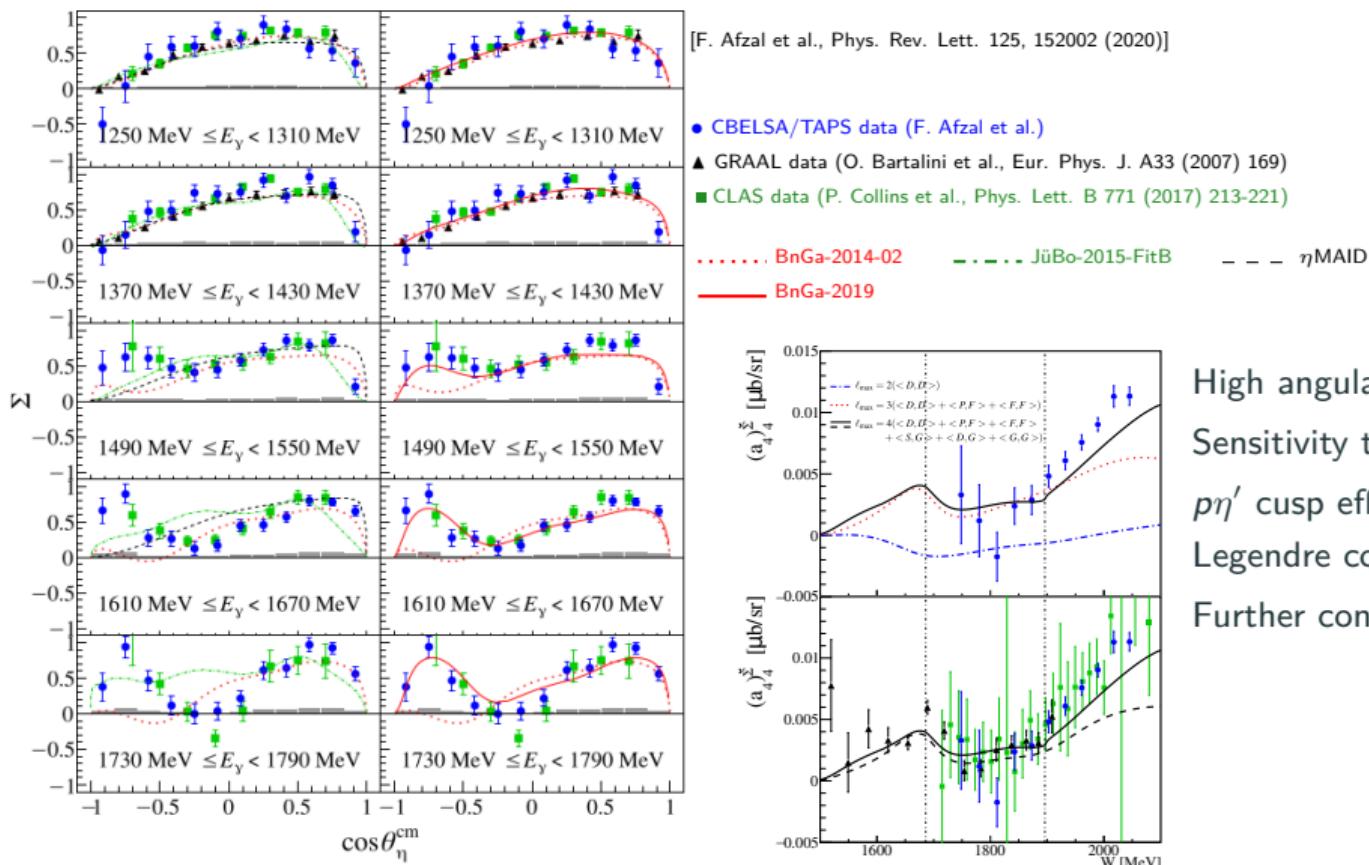
V.L. Kashevarov et al., Phys. Rev. Lett. 118, 21 (2017), p. 212001

- key role for description: 3 S -wave resonances: $N(1535)\frac{1}{2}^-$, $N(1650)\frac{1}{2}^-$ and $N(1895)\frac{1}{2}^-$
- strong $p\eta'$ cusp observed in $p\eta$ cross section
- $N(1895)\frac{1}{2}^-$ needed for description of $p\eta'$ cusp and fast rise of $p\eta'$ cross section

$\gamma p \rightarrow p\eta$: Precise beam asymmetry Σ data (CBELSA/TAPS)

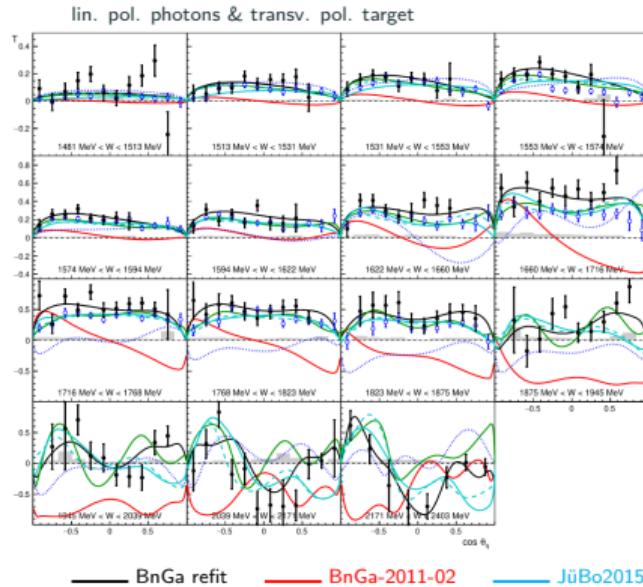


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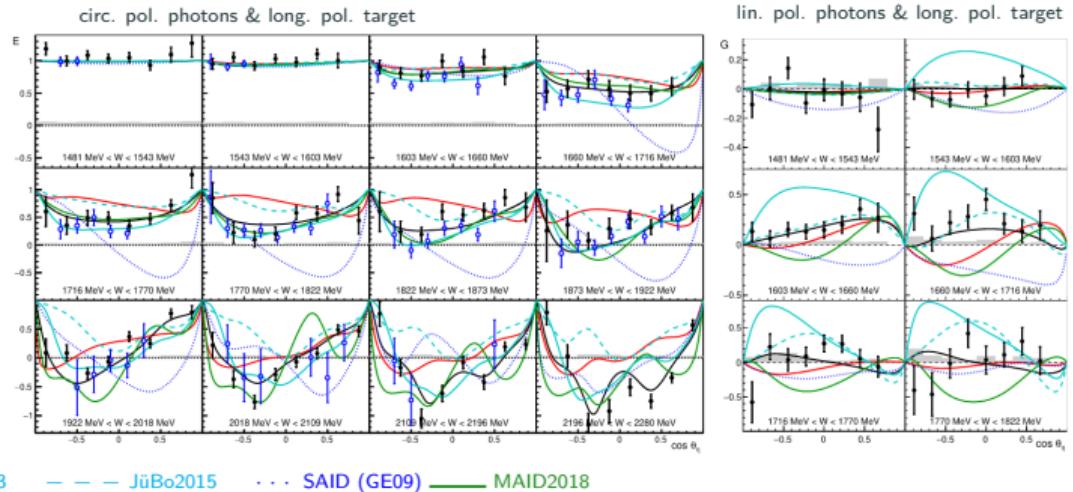


High angular coverage
Sensitivity to $< S, G >$ interference
 $p\eta'$ cusp effect visible in
Legendre coefficient!
Further confirmation of $N(1895)^{\frac{1}{2}^-}$!

Combined analysis of the polarization observables σ, G, E, T, P, H in $\gamma p \rightarrow p\eta$



J. Mueller et al., Phys. Lett. B 803 (2020), p. 135323



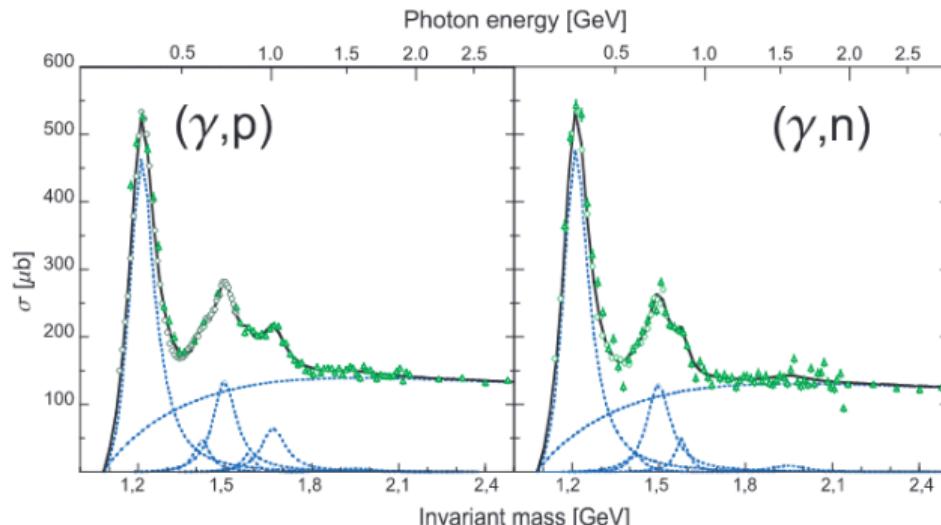
	$N(1535)\frac{1}{2}^-$	$N(1650)\frac{1}{2}^-$
BnGa refit	0.41 ± 0.04	0.33 ± 0.04
PDG 2017	$0.32 - 0.52$	$0.14 - 0.22$

Large and heavily discussed difference in the $p\eta$ -branching ratio of $N(1535)\frac{1}{2}^-$ and $N(1650)\frac{1}{2}^-$ now significantly reduced!

Measurements off neutrons

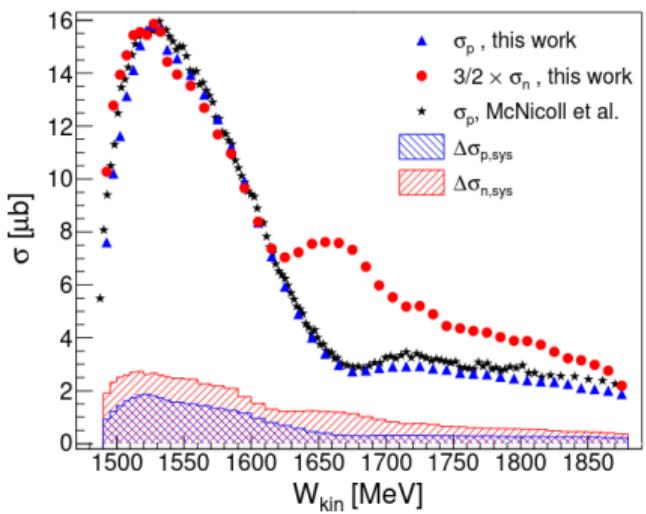
- Motivation:
 - Electromagnetic excitation is isospin dependent
 - Measurements off neutrons are essential for an isospin separation
 - Different resonance contributions possible

- Experimentally complicated to measure:
 - No free neutrons → helium, deuterium, deuterated butanol targets
 - Nuclear Fermi motion and FSI effects make interpretation of results difficult
 - Low detection efficiency of neutrons



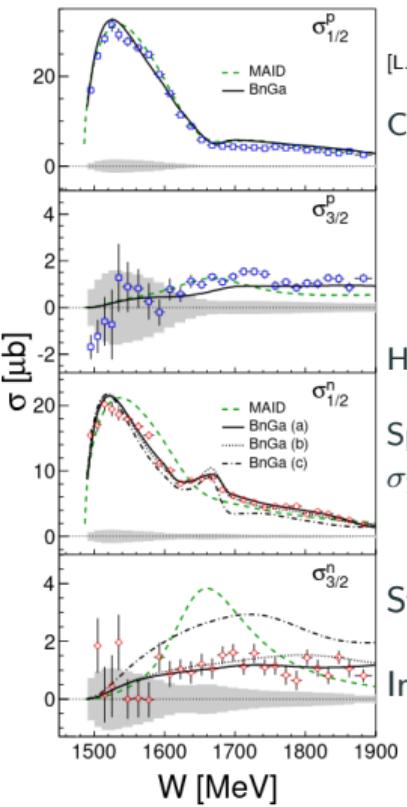
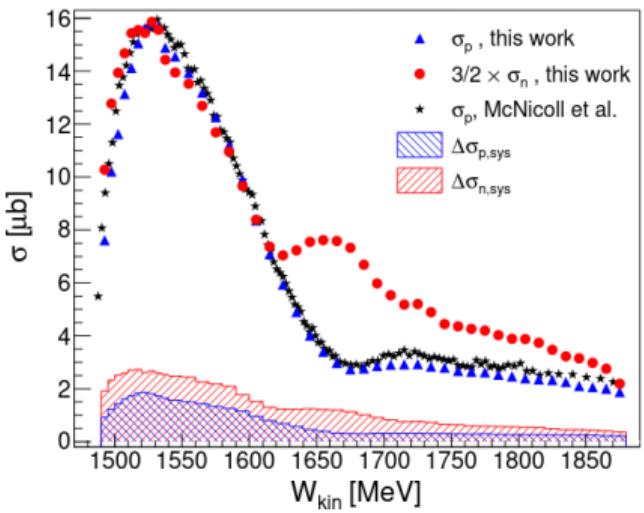
narrow peak observed in $\gamma n \rightarrow n\eta$
at $W = (1670 \pm 5)$ MeV with $\Gamma = 30$ MeV

[D. Werthmüller et al., Phys.Rev. C90 (2014) no.1, 015205]



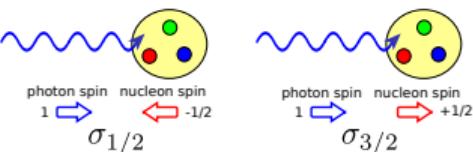
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[L. Witthauer et al., Phys. Rev. Lett. 117, no. 13, 132502 (2016)]

Circularly pol. photons & long. pol. target



$$\text{Helicity asymmetry: } E = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}$$

Spin dependent cross sections

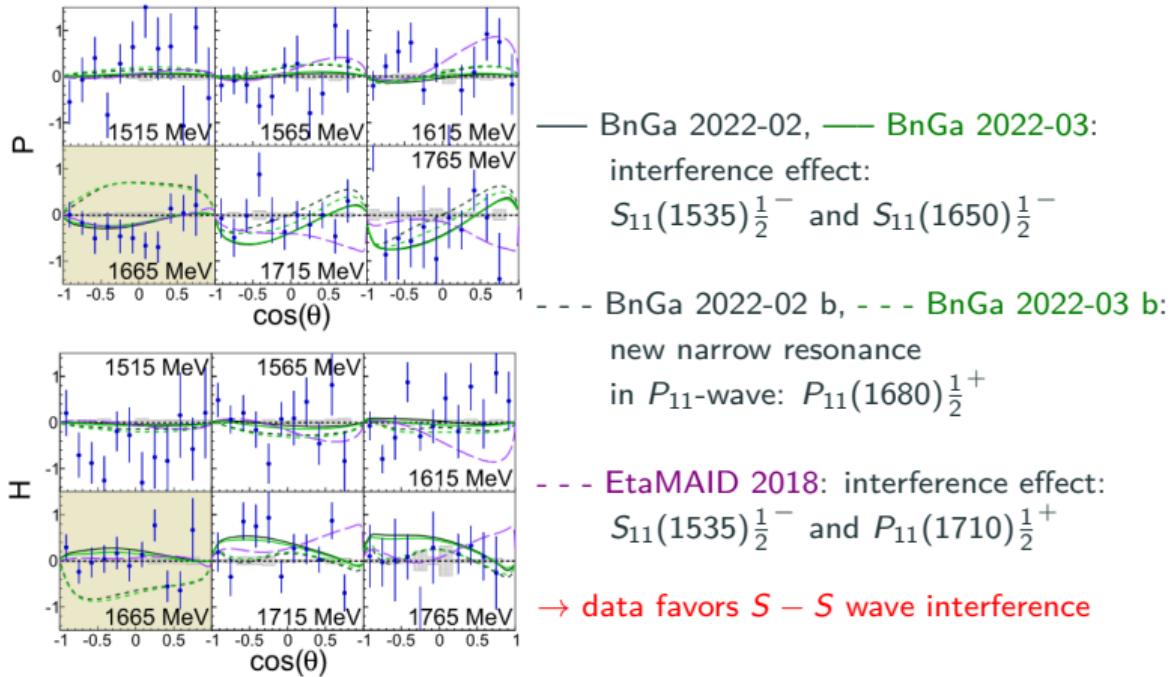
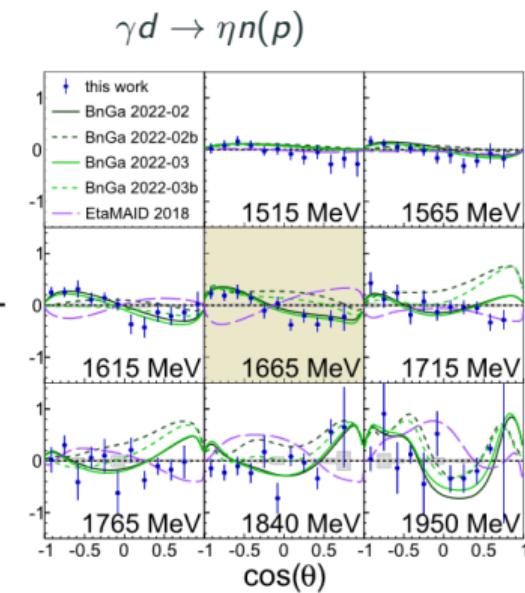
$$\sigma_{1/2(3/2)} = \sigma_0 \cdot (1 \pm E)$$

Structure only present in $\sigma_{1/2}^n$!

Intrinsic resonance/ interference effects?

$\gamma n \rightarrow n\eta$: Results of T, P, H (CBELSA/TAPS)

- More data taken for T, P, H with coherent edges at 1300 MeV, 1600 MeV
- Ongoing analyses of different final states ($N\pi^0, N\eta, N\eta', N\omega, N\pi^0\pi^0, N\pi^0\eta\dots$) and PWA of the data



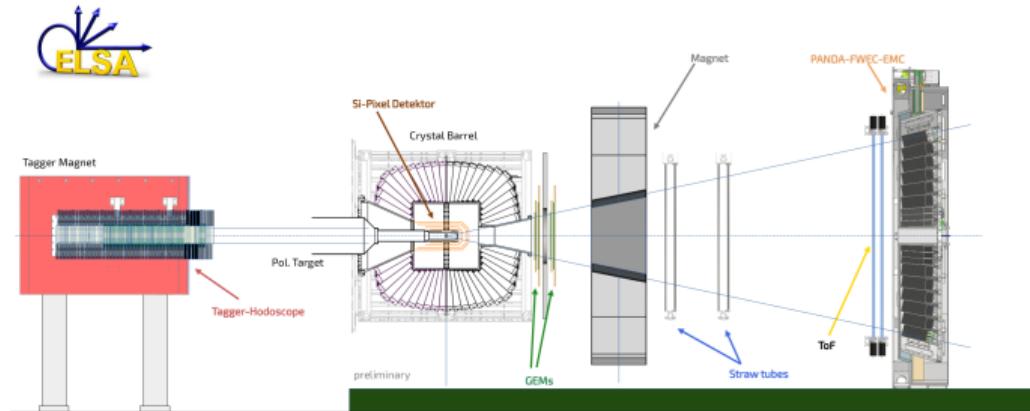
Impact of data

Impact of photoproduction data - Updates in PDG 2020

Particle	J^P	overall	PWA	$N\gamma$	$N\pi$	$\Delta\pi$	$N\sigma$	$N\eta$	ΛK	ΣK	$N\rho$	$N\omega$	$N\eta'$
N	$1/2^+$	****											
$N(1440)$	$1/2^+$	****	$\circ \diamond_g \star \triangleright$	****	****	****	***	-					-
$N(1520)$	$3/2^-$	****	$\circ \diamond \star \triangleright$	****	****	****	**	***					- - -
$N(1535)$	$1/2^-$	****	$\circ \diamond \star \triangleright$	****	****	****	*	*	****				- -
$N(1650)$	$1/2^-$	****	$\circ \diamond \star \triangleright$	****	****	****	*	****	- -	- -	- -		- -
$N(1675)$	$5/2^-$	****	$\circ \diamond \star \triangleright$	****	****	****	***	*	*	*	*		-
$N(1680)$	$5/2^+$	****	$\circ \diamond \star \triangleright$	****	****	****	***	*	*	*	*		- - -
$N(1700)$	$3/2^-$	***	$\circ \triangleright$	**	***	**	*	*	- -	-	-		-
$N(1710)$	$1/2^+$	***	$\circ \diamond \triangleright$	****	****	*	**	**	**	*	*	*	
$N(1720)$	$3/2^+$	****	$\circ \diamond \star \triangleright$	****	****	****	*	*	****	*	*	*	
$N(1860)$	$5/2^+$	**	\triangleright	*	**	*	*	*					
$N(1875)$	$3/2^-$	***	$\circ \triangleright$	**	**	*	**	*	*	*	*	*	
$N(1880)$	$1/2^+$	***	$\circ \triangleright$	**	*	**	*	*	**	**	*	*	
$N(1895)$	$1/2^-$	****	$\circ \triangleright$	****	*	*	*	****	**	**	*	*	****
$N(1900)$	$3/2^+$	****	$\circ \diamond \triangleright$	****	**	**	*	**	**	**	-	*	**
$N(1990)$	$7/2^+$	**	$\circ \diamond \triangleright$	**	**		*	*	*	*			
$N(2000)$	$5/2^+$	**	$\circ \star$	**	*	**	*	*	-	-	- -	*	
$N(2040)$	$3/2^+$	*	\triangleright	*									
$N(2060)$	$5/2^-$	***	$\circ \diamond_g \triangleright$	****	**	*	*	*	*	*	*	*	
$N(2100)$	$1/2^+$	***	$\circ \triangleright$	**	**	**	*	*			*	*	**
$N(2120)$	$3/2^-$	***	$\circ \triangleright$	****	**	**	**	**	*		*	*	*
$N(2190)$	$7/2^-$	****	$\circ \diamond \star \triangleright$	****	****	****	*	*	**	*	*	*	
$N(2220)$	$9/2^+$	****	$\circ \diamond \star$	**	****		*	*	*				
$N(2250)$	$9/2^-$	****	$\circ \diamond \star \triangleright$	**	****		*	*	*				
$N(2300)$	$1/2^+$	**											
$N(2570)$	$5/2^-$	**											
$N(2600)$	$11/2^-$	***	\star										
$N(2700)$	$13/2^+$	**											

- Until 2010: almost only results from πN scattering used in the PDG
- PWA groups:
 - BnGa-2019, ◊ JüBo-2017,
 - ★ SAID-MA19, ▷ KSU model
 include photoproduction data with different final states from several experiments
- Now: new values from the fits are entering the PDG!

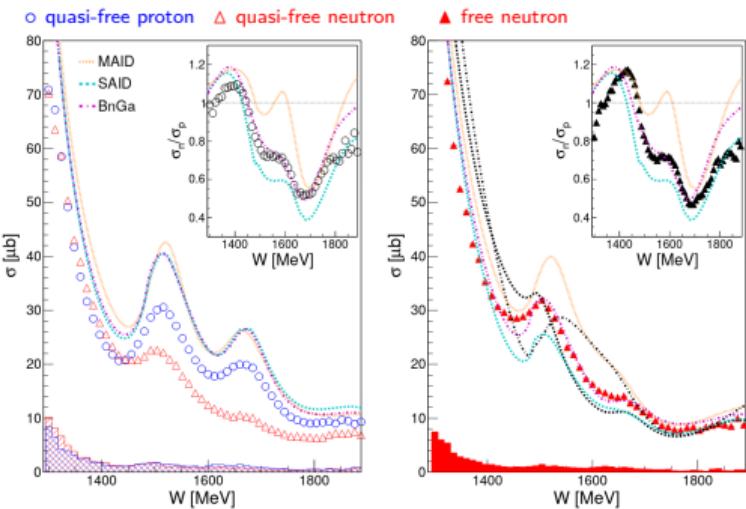
- Light baryon spectroscopy is experimentally challenging
 - Need to measure several polarization observables with large energy and angular coverage!
- High precision data measured at the A2 and CBELSA/TAPS experiments for many different final states
 - Sensitivity up to G -waves reached! $p\eta$ and $p\eta'$ cusps observed in pol. observables!
 - Significant contributions to confirming poorly known states like $N(1895)^{\frac{1}{2}-}$
 - Better understanding of narrow structure in $n\eta$ (S - S wave interference)
- Our knowledge of the spectrum and the properties of baryons is steadily increasing!
- More polarization observables data for photoproduction off the neutron for different final states
- Investigation of strange baryons: KY-photoproduction data - new experiment planned at ELSA



Backup Slides

Measurements off neutrons - cross section data for $\gamma d \rightarrow \pi^0 n(p)$ (A2)

- Complicated to measure due to no free neutrons \rightarrow helium, deuterium, deuterated butanol targets
- Nuclear Fermi motion effects eliminated by a complete kinematic reconstruction of the final state
- FSI estimated through comparison of quasi-free and free proton data



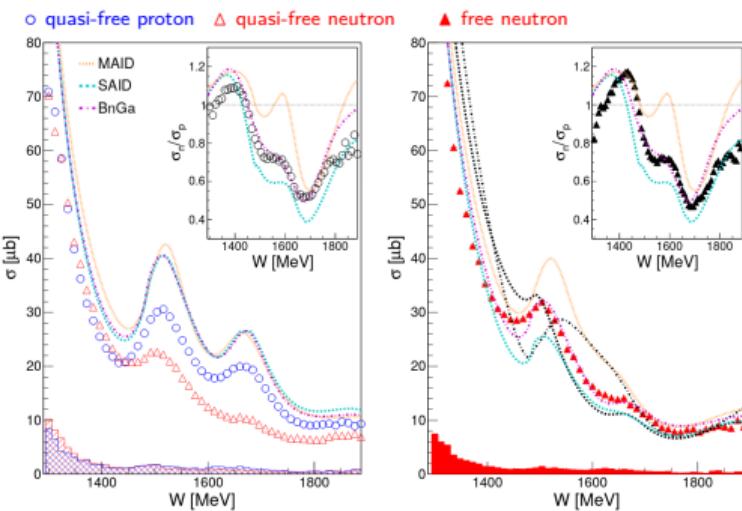
[M. Dieterle et al., Phys. Rev. Lett. 112.14 (2014), p. 142001]
[M. Dieterle et al., Phys. Rev. C (2018), pp. 065205-1-065205-28]

Significant FSI effects in quasi-free proton data

→ FSI effects corrected assuming FSI effect is equal for participant protons and neutrons!

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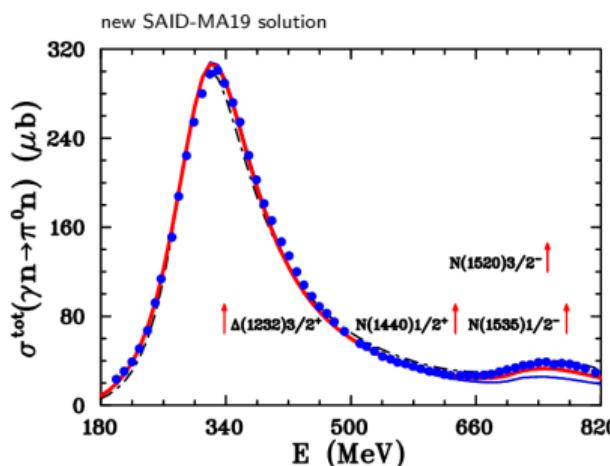
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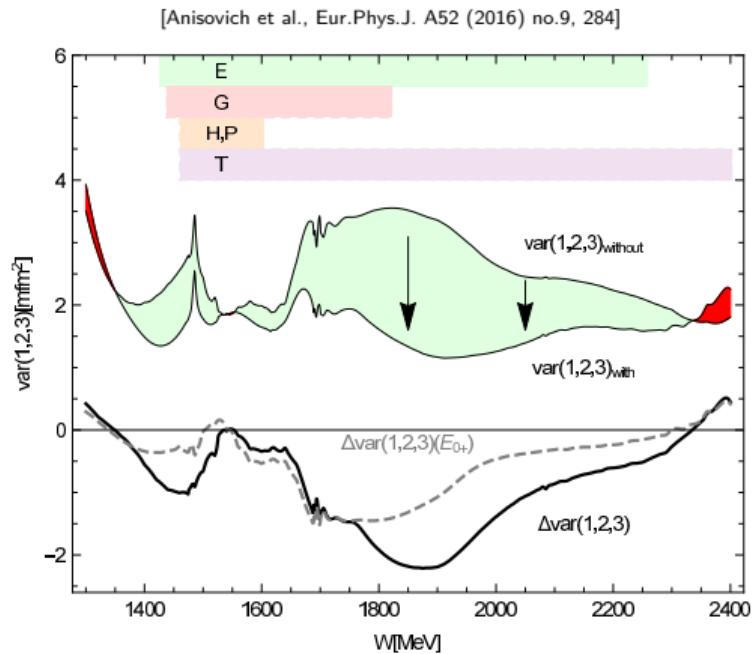
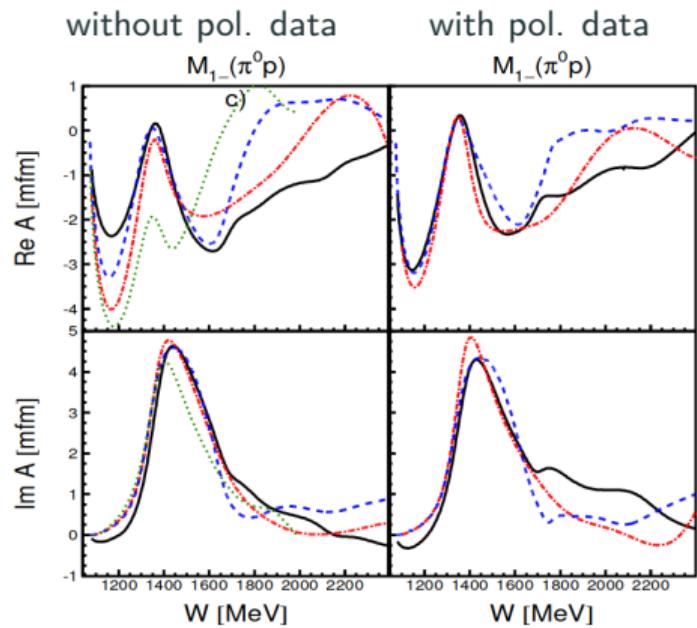


[W.J. Briscoe, Phys. Rev. C 100 (2019) 6, 065205]

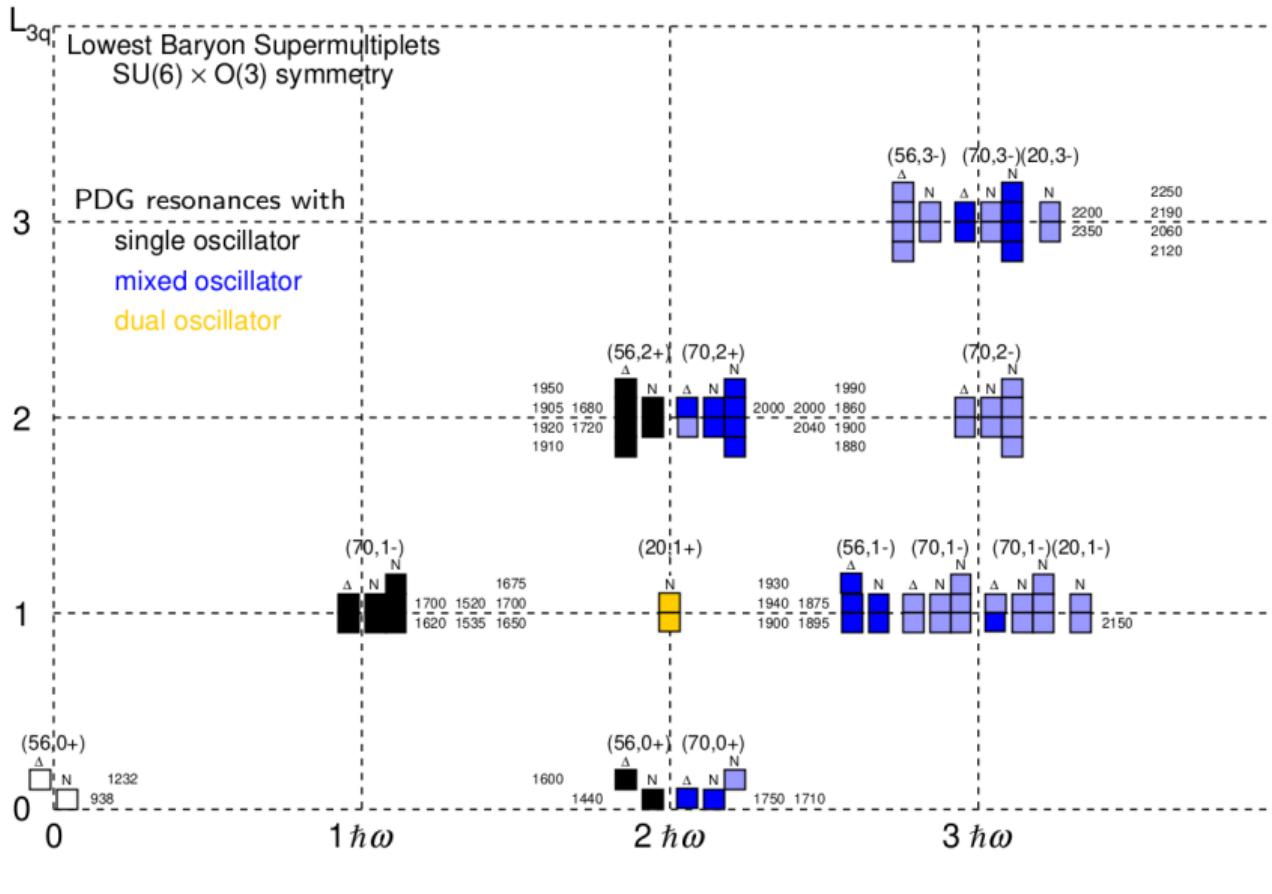
\rightarrow Photon decay amplitudes $A_{3/2}(n)$ and $A_{1/2}(n)$ for $N^* \rightarrow \gamma n$ extracted

Impact of polarization observables in $\gamma p \rightarrow p\pi^0$

- The variance of all the three PWAs (**JüBo**, **SAID**, **BnGa**) summed over all $\gamma p \rightarrow p\pi^0$ multipoles up to $L = 4$
- Variance between the different PWAs decreases!



$SU(6) \times O(3)$ supermultiplets

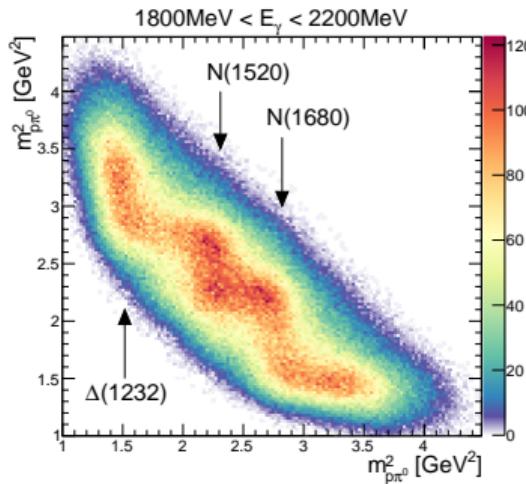
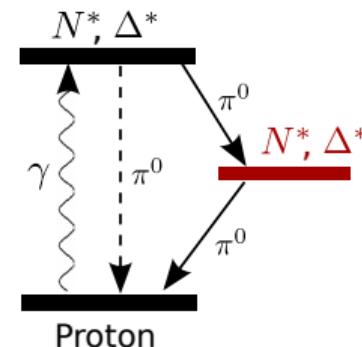
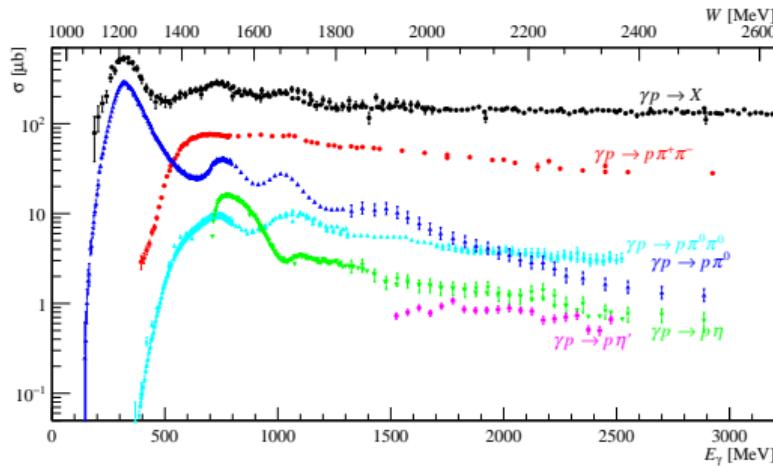


$$N = 2n_\varrho + 2n_\lambda + \ell_\varrho + \ell_\lambda$$

$\gamma p \rightarrow p\pi^0\pi^0$: Importance of cascade decays

- Multi-meson final states like $p\pi^0\pi^0$ are preferred at higher energies
- Less background amplitudes than $p\pi^+\pi^-$ but cannot discriminate between N^*/Δ^*
- Access to sequential decays

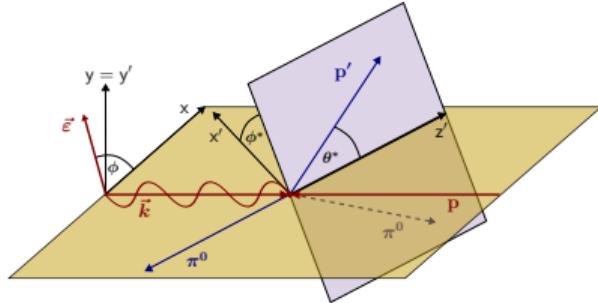
→ talk by P. Mahlberg [HK 57.1, Thursday, 14:00]



Polarization observables in $p\pi^0\pi^0$ - 4D extraction

Data analyzed in full 3 body kinematics

[T. Seifen et al., arXiv:2207.01981v1 [nucl-ex]]



5 kinematic variables:

$$E_\gamma, \cos \vartheta_{\pi^0}, m_{p\pi^0}, \phi_{p\pi^0}^*, \theta_{p\pi^0}^*$$

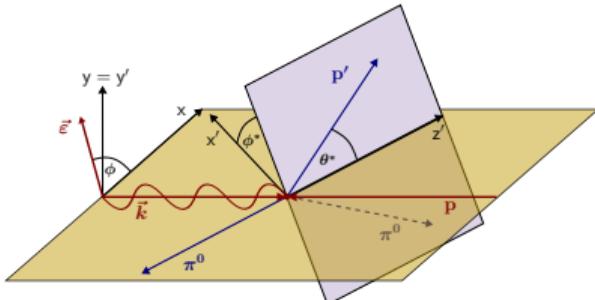
More pol. observables accessible

Photon Pol.		Target Pol. Axis		
		x	y	z
unpolarised	σ	P_x	P_y	P_z
linear $\sin(2\phi)$	I^s	P_x^s	P_y^s	P_z^s
linear $\cos(2\phi)$	I^c	P_x^c	P_y^c	P_z^c
circular	I^\odot	P_x^\odot	P_y^\odot	P_z^\odot

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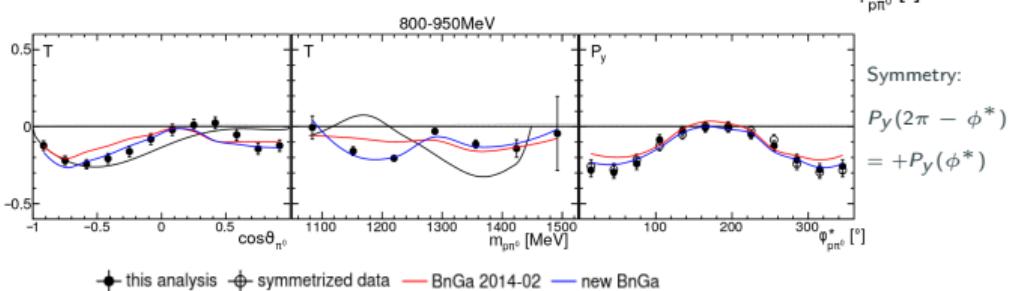
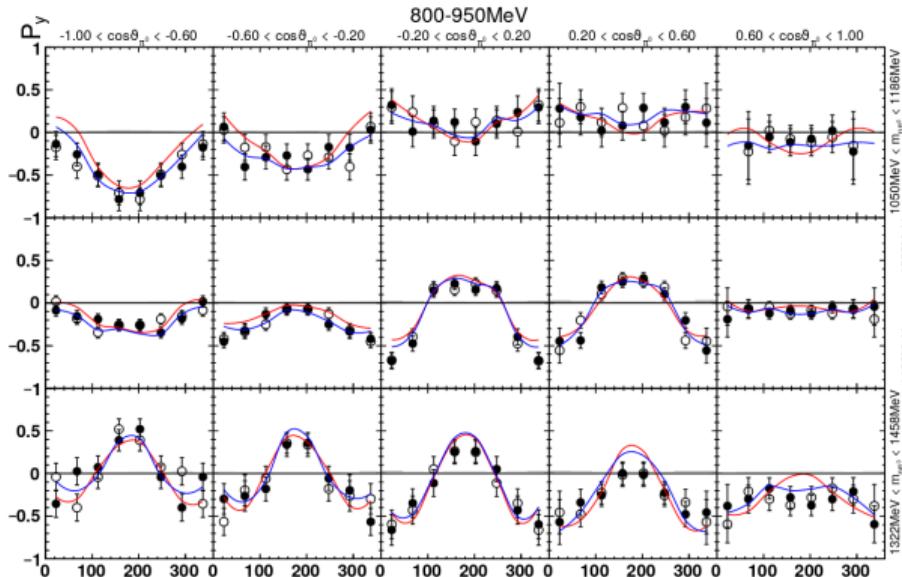
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circular	I^\odot	P_x^\odot	P_y^\odot	P_z^\odot



Polarization observables in $p\pi^0\pi^0$ - New branching ratios

4th resonance region:

	$\Delta(1910)\frac{1}{2}^+, \Delta(1920)\frac{3}{2}^+, \Delta(1905)\frac{5}{2}^+, \Delta(1950)\frac{7}{2}^+$ $\Delta^*, S = \frac{3}{2}, L = 2, \phi_{\text{space}}^S$	$N(1880)\frac{1}{2}^+, N(1900)\frac{3}{2}^+, N(2000)\frac{5}{2}^+, N(1990)\frac{7}{2}^+$ $N^*, S = \frac{3}{2}, L = 2, \phi_{\text{space}}^{MS} + \phi_{\text{space}}^{MA}$
BR into ground state $N(938)\pi$ or $\Delta(1232)\pi$	$(44 \pm 7)\%$	$(34 \pm 6)\%$
BR into excited states ($L=1$) $N(1520)\pi, N(1535)\pi, N\sigma$	$(5 \pm 2)\%$	$(21 \pm 5)\%$

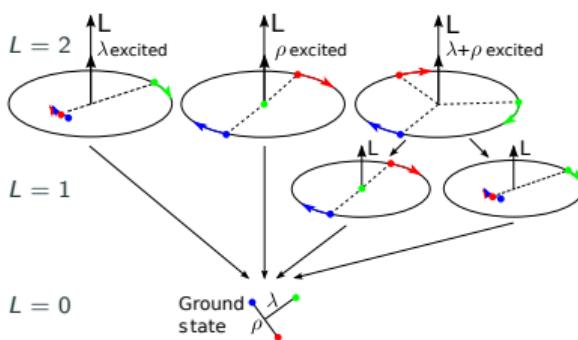
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[A. Thiel et al., Phys. Rev. Lett. 114, 091803]

Harmonic oscillator model (orbital excitation $L=2$)



Polarization observables in $p\pi^0\pi^0$ - New branching ratios

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