

QCHSC 2024

The XVth Quark Confinement and the Hadron Spectrum Conference

Study of T_{cc} and $X(3872)$

Jia-Jun Wu (University of Chinese Academy of Sciences)

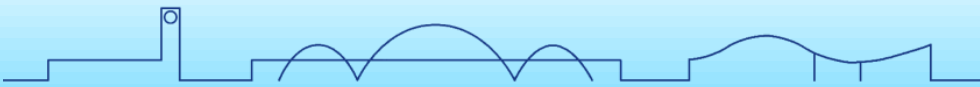
Collaborator: G.-J. Wang(KEK), Zhi Yang(UESTC), Makoto Oka(RIKEN),
Shi-lin Zhu(PKU)

Scib.2024.07.012 [hep-ph] 2306.12406

QCHSC2024

2024.08.22

Cairns, Queensland, Australia

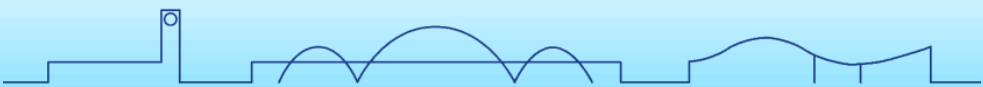


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Outline

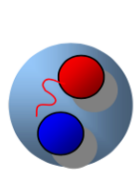
- Background
- Introduction of HEFT and OBE
- The generation of T_{cc}
- The nature of $X(3872)$
- Summary and Outlook



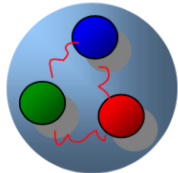
Background

Traditional Quark model

conventional hadron



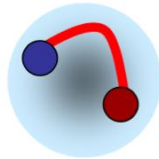
$(q \bar{q})$



(qqq)

Exotic

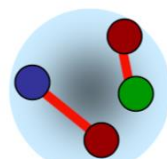
Hybrid



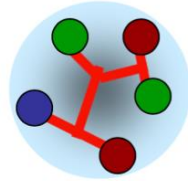
Glueball



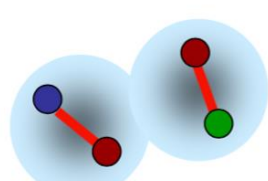
Tetraquark



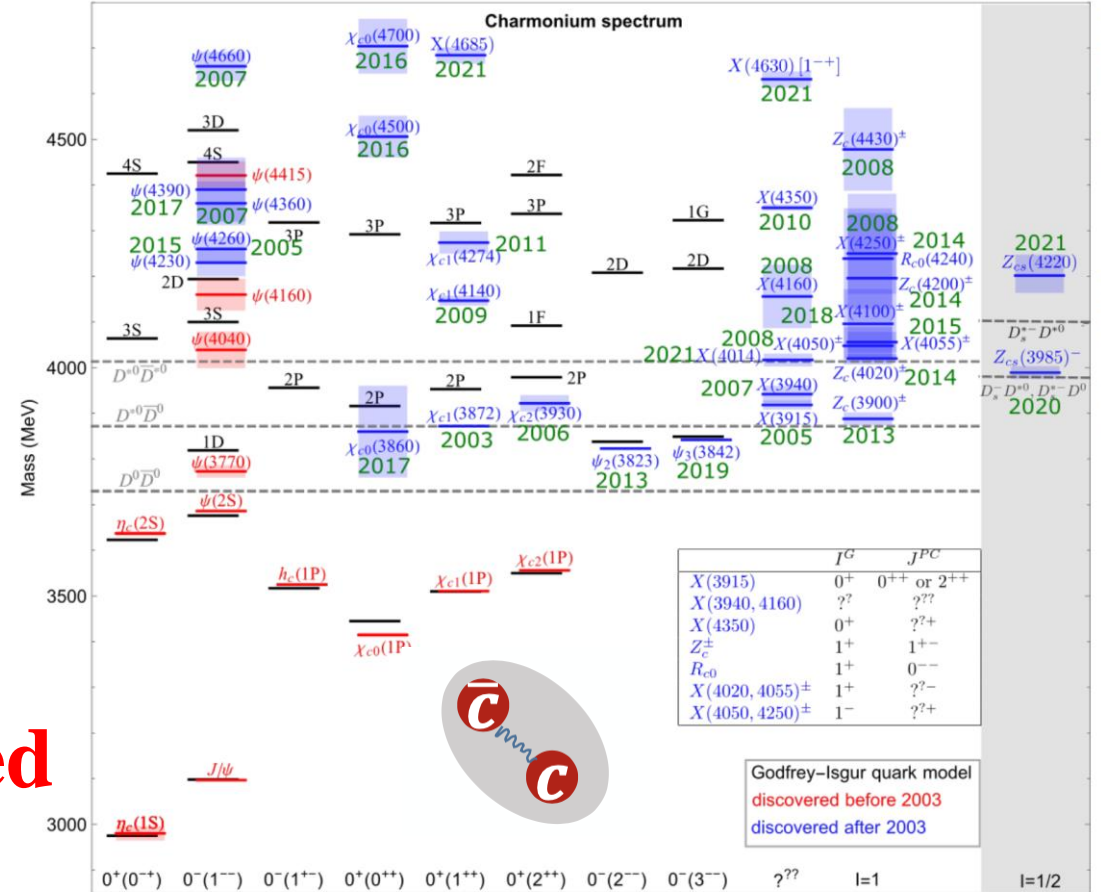
Pentaquark



Hadronic molecule



Question: How is a hadron composed of these possible components?



Background

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strong interaction

Colorful → quark level

Colorless → hadron level



Background

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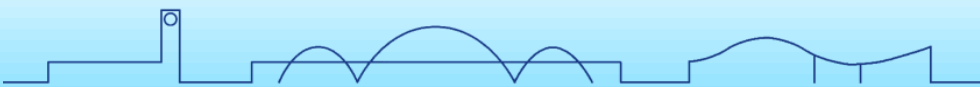
Colorful → quark level

Colorless → hadron level

A more **comprehensive framework** for **systematically** describing hadrons

**Include quark level
and hadron level.**

**Not only one, at least
a set of hadron**



Introduction of HEFT

Section B Tue. 16:00 Curtis Abell $\Delta(1600)$
 Section C Wed. 18:10 Guang-Juan Wang Ds, Bs
 Section C Thu. 14:00 Lu Meng Tcc

$$H = H_0 + H_I$$

$$H_0 = \sum_{i=1,n} |B_i\rangle m_i \langle B_i| + \sum_{\alpha} |\alpha(k_{\alpha})\rangle \left[\sqrt{m_{\alpha 1}^2 + k_{\alpha}^2} + \sqrt{m_{\alpha 2}^2 + k_{\alpha}^2} \right] \langle \alpha(k_{\alpha})|$$

$|B_i\rangle$ bare state, bare mass m_i

$|\alpha(k_{\alpha})\rangle$ non-interaction channels

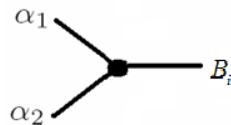
←→ Quark level

←→ Hadron level

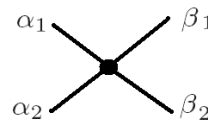
$$H_I = \hat{g} + \hat{v}$$

$$\hat{g} = \sum_{\alpha} \sum_{i=1,n} \left[|\alpha(k_{\alpha})\rangle g_{i,\alpha}^+ \langle B_i| + |B_i\rangle g_{i,\alpha} \langle \alpha(k_{\alpha})| \right]$$

$$\hat{v} = \sum_{\alpha,\beta} |\alpha(k_{\alpha})\rangle v_{\alpha,\beta} \langle \beta(k_{\beta})|$$

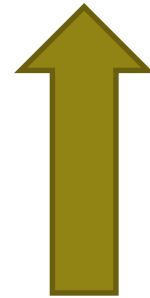


From 3P0 model, and the wavefunction of quark model



One boson exchange (OBE)

Resonance
 (Mass, width, pole position, coupling)



HEFT



T matrix
 (phase shift,
 Inelasticity)



Lattice spectrum



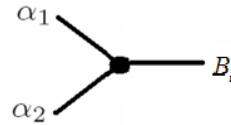
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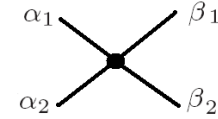
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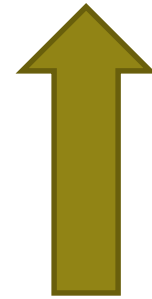


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**Lattice
spectrum**

Question: Two interactions ?
Too many solutions of a+b=5



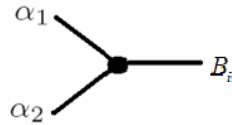
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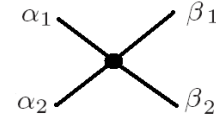
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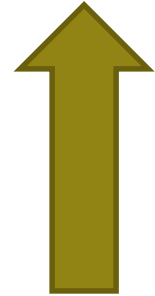


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(Mass, width, pole position, coupling)



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Lattice spectrum

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Model

Study X(3872)

dependence!

from T_{cc}

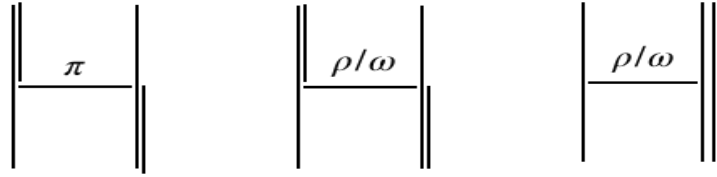


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Introduction of OBE and DD^* vs $D\bar{D}^*$

The interaction between D and D^* OBE



$$V_\pi = \frac{g^2}{f_\pi^2} \frac{(q \cdot \epsilon_\lambda)(q \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_\pi^2},$$

$$V_{\rho/\omega}^u = -2\lambda^2 g_V^2 \frac{(\epsilon_{\lambda'}^\dagger \cdot q)(\epsilon_\lambda \cdot q) - q^2 (\epsilon_\lambda \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_{\rho/\omega}^2},$$

$$V_{\rho/\omega}^t = \frac{\beta^2 g_V^2}{2} \frac{(\epsilon_\lambda \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_{\rho/\omega}^2}. \quad \text{PWA Just S-wave}$$

$$\mathcal{V}(l, l', S, j) = \frac{1}{(2\pi)^3} \sqrt{\frac{1}{2E_D^i 2E_D^f 2E_K^i 2E_K^f}} \\ 2\pi \int d\cos\theta V^v(\vec{p}_f, \vec{p}_i) \left(\frac{\Lambda^2}{\Lambda^2 + p_f^2}\right)^2 \left(\frac{\Lambda^2}{\Lambda^2 + p_i^2}\right)^2$$

- $g = 0.57$ from the decay width of $D^* \rightarrow D\pi$, while undetermined parameters λ & β .

Heavy Quark Symmetry

$$D^{(*)} D^{(*)}$$

$$H_a^{(Q)} = \frac{1+\not{v}}{2} [P_a^{*\mu} \gamma_\mu - P_a \gamma_5]$$

$$\bar{H}_a^{(Q)} \equiv \gamma_0 H^{(Q)\dagger} \gamma_0 = [P_a^{*\mu} \gamma_\mu + P_a^\dagger \gamma_5] \frac{1+\not{v}}{2}$$

$$P = (D^0, D^+, D_s^+) \& P^* = (D^{*0}, D^{*+}, D_s^{*+})$$

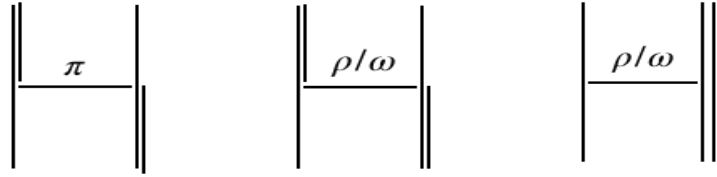
$$\mathcal{L}_{MH^{(Q)}H^{(Q)}} = ig \text{Tr} [H_b^{(Q)} \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a^{(Q)}]$$

$$\mathcal{L}_{VH^{(Q)}H^{(Q)}} = i\beta \text{Tr} [H_b^{(Q)} v_\mu (V_{ba}^\mu - \rho_{ba}^\mu) \bar{H}_a^{(Q)}] \\ + i\lambda \text{Tr} [H_b^{(Q)} \sigma_{\mu\nu} F^{\mu\nu}(\rho)_{ba} \bar{H}_a^{(Q)}]$$



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$$H_a^{(\bar{Q})} \equiv C (\mathcal{C} H_a^{(Q)} \mathcal{C}^{-1})^T \mathcal{C}^{-1} = [P_{a\mu}^{(\bar{Q})} \gamma^\mu - P_a^{(\bar{Q})} \gamma_5] \frac{1-\not{v}}{2}$$

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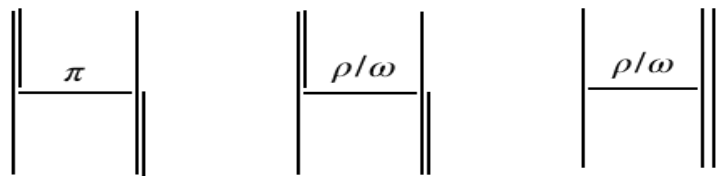
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$$H_a^{(\bar{Q})} \equiv C (\mathcal{C} H_a^{(Q)} \mathcal{C}^{-1})^T \mathcal{C}^{-1} = [P_{a\mu}^{(\bar{Q})} \gamma^\mu - P_a^{(\bar{Q})} \gamma_5] \frac{1-\not{v}}{2}$$

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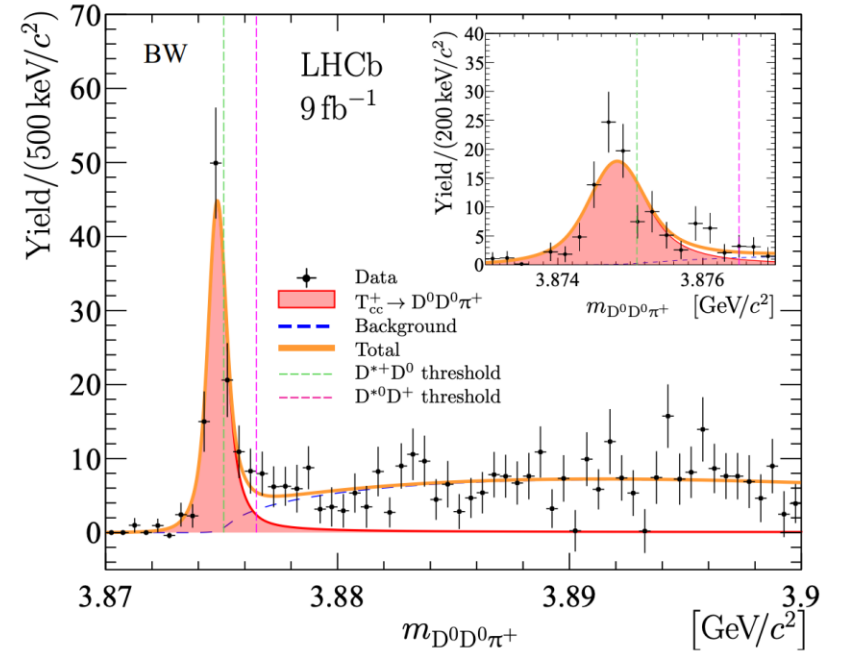
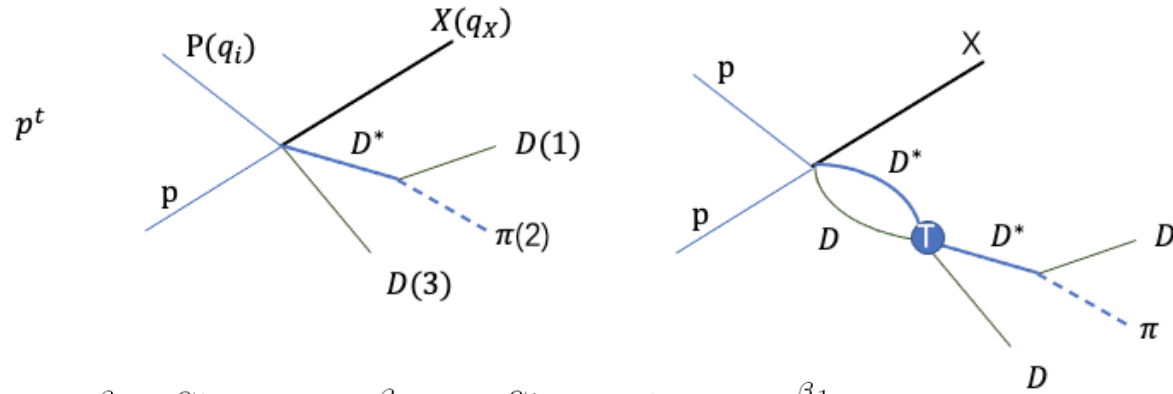
	wave function	$I(J^{PC})$	u -channel : π	u -channel : ρ/ω	t -channel : ρ/ω
DD^*	$\frac{1}{\sqrt{2}}(D^+D^{*0} - D^0D^{*+})$	$0(1^+) [T_{cc}^+]$	$\frac{3}{2}V_\pi$	$\frac{3}{2}V_\rho^u - \frac{1}{2}V_\omega^u$	$-\frac{3}{2}V_\rho^t + \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}(D^+D^{*0} + D^0D^{*+})$	$1(1^+)$	$\frac{1}{2}V_\pi$	$\frac{1}{2}V_\rho^u + \frac{1}{2}V_\omega^u$	$\frac{1}{2}V_\rho^t + \frac{1}{2}V_\omega^t$
$D\bar{D}^*$	$\frac{1}{\sqrt{2}}([D^+D^{*-}] + [D^0\bar{D}^{*0}])$	$0(1^{++})[X(3872)]$	$\frac{3}{2}V_\pi$	$-\frac{3}{2}V_\rho^u - \frac{1}{2}V_\omega^u$	$-\frac{3}{2}V_\rho^t - \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}([D^+D^{*-}] - [D^0\bar{D}^{*0}])$	$1(1^{++})$	$-\frac{1}{2}V_\pi$	$\frac{1}{2}V_\rho^u - \frac{1}{2}V_\omega^u$	$\frac{1}{2}V_\rho^t - \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}(\{D^+D^{*-}\} + \{D^0\bar{D}^{*0}\})$	$0(1^{+-})[h_c]$	$-\frac{3}{2}V_\pi$	$\frac{3}{2}V_\rho^u + \frac{1}{2}V_\omega^u$	$-\frac{3}{2}V_\rho^t - \frac{1}{2}V_\omega^t$
	$\frac{1}{\sqrt{2}}(\{D^+D^{*-}\} - \{D^0\bar{D}^{*0}\})$	$1(1^{+-}) [Z_c(3900)]$	$\frac{1}{2}V_\pi$	$-\frac{1}{2}V_\rho^u + \frac{1}{2}V_\omega^u$	$\frac{1}{2}V_\rho^t - \frac{1}{2}V_\omega^t$

The mass differences leads to isospin breaking, our calculations are based on the physical states of the particles.



The generation of T_{cc}

$$pp \rightarrow X D^0 D^0 \pi^+$$



$$t_{\alpha,\beta} = V_{\alpha,\beta} + \sum_{\gamma} V_{\alpha,\gamma} \frac{1}{E - \sqrt{m_{\gamma_1}^2 + k_{\gamma}^2} - \sqrt{m_{\gamma_2}^2 + k_{\gamma}^2} + i\epsilon} t_{\gamma,\beta}$$

$$t_{\alpha,\beta}(k_{\alpha}, k_{\beta}, E) = V_{\alpha,\beta}(k_{\alpha}, k_{\beta}) + \sum_{\gamma} \int k_{\gamma}^2 dk_{\gamma} \frac{V_{\alpha,\gamma}(k_{\alpha}, k_{\gamma}) t_{\gamma,\beta}(k_{\gamma}, k_{\beta}, E)}{E - \sqrt{m_{\gamma_1}^2 + k_{\gamma}^2} - \sqrt{m_{\gamma_2}^2 + k_{\gamma}^2} + i\epsilon}$$

$$|\mathcal{M}|^2 = |a_{pp \rightarrow DD^* X}|^2 \sum_{\lambda_X} \epsilon_{\mu}(p_X, \lambda_X) \epsilon_{\mu'}^{\dagger}(p_X, \lambda_X) \sum_j \mathcal{B}_{j\mu} \mathcal{B}_j^{\dagger\mu'}$$

$$\mathcal{B}_j^{\mu}(p_{12}, p_{23}) = g \left\{ \frac{-i(p_{12}^{\mu} - \frac{p_{12}^{\mu} p_{12} \cdot p_{\pi}}{m_{D^*}^2})}{p_{12}^2 - m_{D^*}^2 + im_{D^*} \Gamma_{D^*}} \right\}_j + \sum_{i=1,2} ig \left\{ \int dq_{D^*} q_{D^*}^2 \frac{d\Omega_{q_{D^*}}}{4\pi} \frac{\sqrt{2w_{D_2}}}{\sqrt{2w_{D^*}}} \frac{\sqrt{2w_{D_{12}^*}}}{\sqrt{2w_D}} \frac{T_{ij}^{J00}(M, |q_{D^*}|, |p_{12}|)}{(M - w_{D^*}^i) - w_D^i + i\epsilon} \frac{\epsilon_a^{*\mu}(w_{D^*}, q_{D^*}) \epsilon_a(p_{12}) \cdot p_{\pi}}{p_{12}^2 - m_{D^*}^2 + im_{D^*} \Gamma_{D^*}} \right\}_j + (p_{D_1} \rightarrow p_{D_2})$$

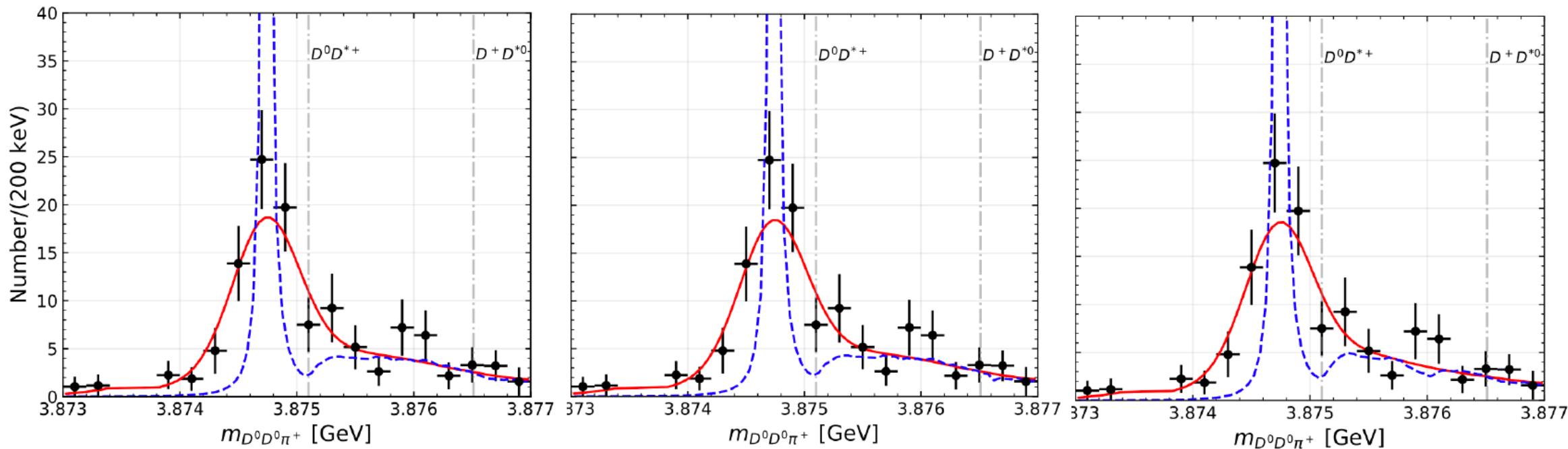


The generation of T_{cc}

$$pp \rightarrow X D^0 D^0 \pi^+$$

Λ (fixed)	λ (/GeV)	β
0.8 GeV	0.890 ± 0.20	0.810 ± 0.11
1 GeV	0.683 ± 0.025	0.687 ± 0.017
1.2 GeV	0.587 ± 0.21	0.550 ± 0.12
1.17 GeV	0.56	0.9

Cheng, et al. PRD 106,016012



Λ (GeV)	BE (keV)	Γ (keV)	$\sqrt{\langle r^2 \rangle}$	$I = 0$	$I = 1$	$P(D^0 D^{*+})$	$P(D^+ D^{*0})$	$\frac{\text{Res}(D^0 D^{*+})}{\text{Res}(D^+ D^{*0})}$
0.8	-387.7	67.3	4.8 fm	95.8%	4.2%	70.0%	30.0%	$-1.063 + 0.001I$
1.0	-393.0	70.4	4.7 fm	95.8%	4.2%	70.0%	30.0%	$-1.055 + 0.001I$
1.2	-391.6	72.7	4.7 fm	95.7%	4.3%	70.3%	29.7%	$-1.052 + 0.001I$

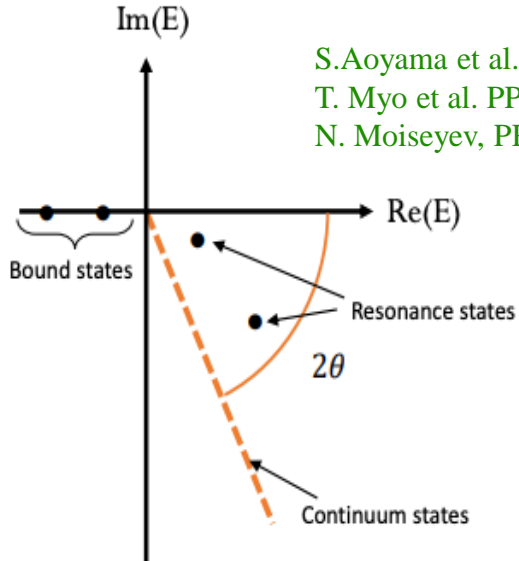


The nature of T_{cc}

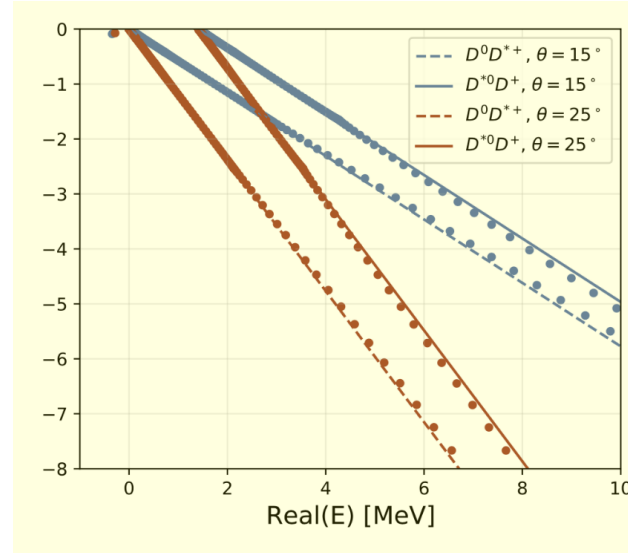
Complex scaling method

$$\mathbf{r} \rightarrow \mathbf{r}e^{i\theta}, \quad \mathbf{q} \rightarrow \mathbf{q}e^{-i\theta} \quad H_\theta \Phi_\theta = E_\theta \Phi_\theta,$$

$$\left[\begin{array}{l} \overline{D^{*0}}D^0 / \overline{D^0}D^{*0} \\ \dots \\ D^{*-}D^+ / D^{*+}D^- \end{array} \right. \left. \begin{array}{l} \text{Coupled-channel} \\ \text{effect} \end{array} \right]$$

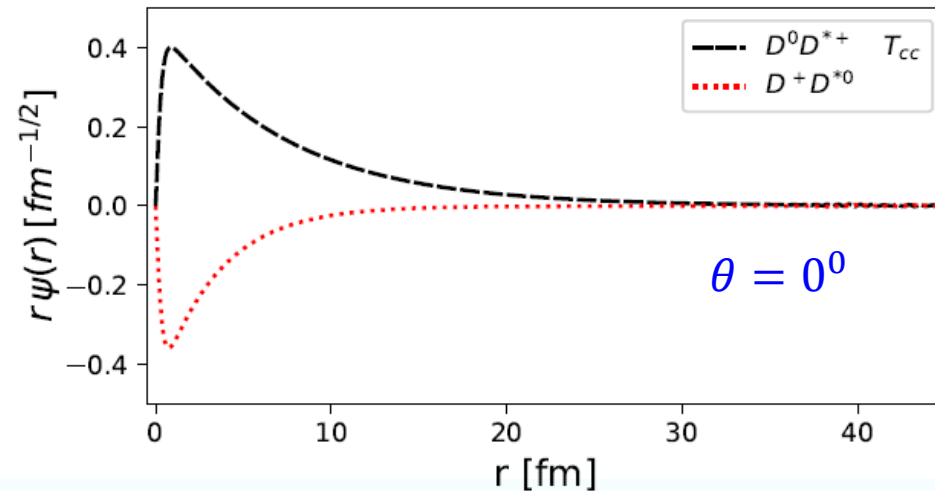


S.Aoyama et al. PTP. 116, 1 (2006).
T. Myo et al. PPNP. 79, 1 (2014)
N. Moiseyev, PR 302, 212 (1998)



- **Bound state: T_{cc}**
 $m_{T_{cc}} = 3874.7 \text{ MeV}$,
 $\Delta E = -393 \text{ keV}$
 $\Gamma_{T_{cc}} = 70.4 \text{ keV}$

- $\sqrt{\langle r^2 \rangle} = 4.7 \text{ fm}$
- 70.0% $D^{*+}D^0$, 30.0% D^+D^{*0}



95.8%, $DD^*(I=0)$
4.2% $DD^*(I=1)$

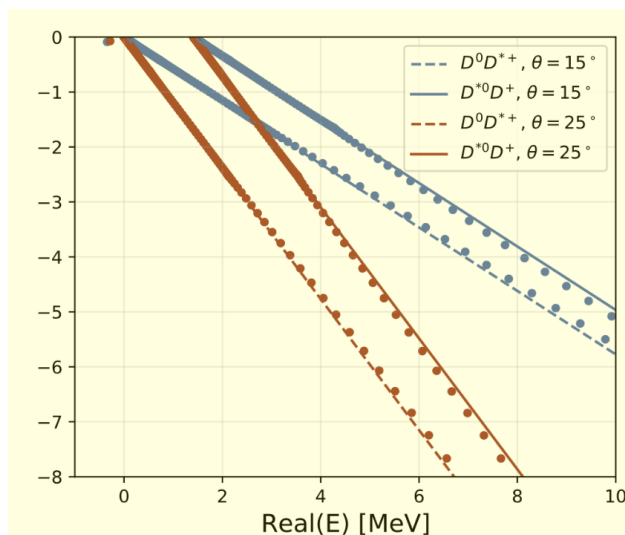
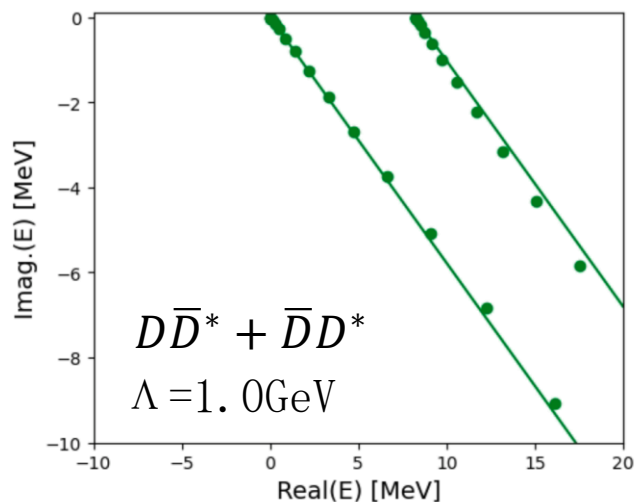
Because of mass difference

$$[I=0] = \frac{1}{\sqrt{2}}(D^{*+}D^0 - D^{*0}D^+)$$

$$[I=1] = \frac{1}{\sqrt{2}}(D^{*+}D^0 + D^{*0}D^+)$$

Produce $X(3872)$ with pure $D\bar{D}^* + \bar{D}D^*$

From the interaction of DD^* to obtain the interaction of $D\bar{D}^* + \bar{D}D^*$, check $X(3872)$ exists or not by pure $D\bar{D}^* + \bar{D}D^*$ interaction, without $c\bar{c}$ state.

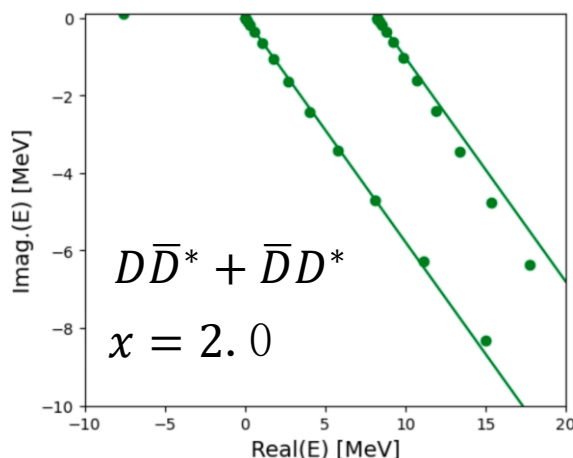
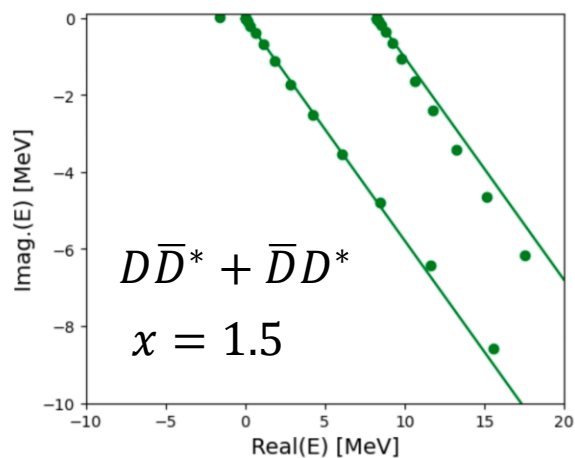


- **Bound state: T_{cc}**
 $m_{T_{cc}} = 3874.7 \text{ MeV}$,
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 $\Gamma_{T_{cc}} = 70.4 \text{ keV}$

- $\sqrt{\langle r^2 \rangle} = 4.7 \text{ fm}$

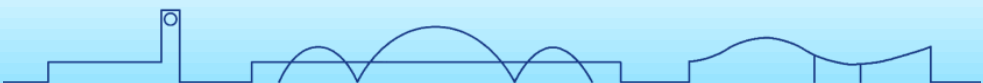
- 70.0% $D^{*+} D^0$, 30.0% $D^+ D^{*0}$

$$V'_{\bar{D}^* D} = \chi * V_{\bar{D}^* D}$$



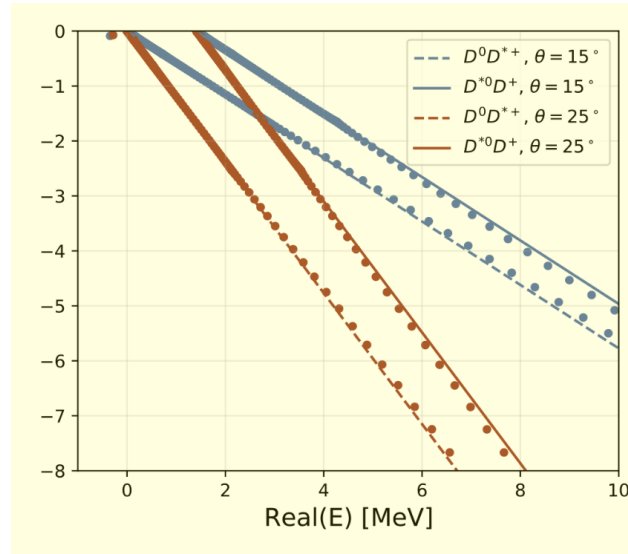
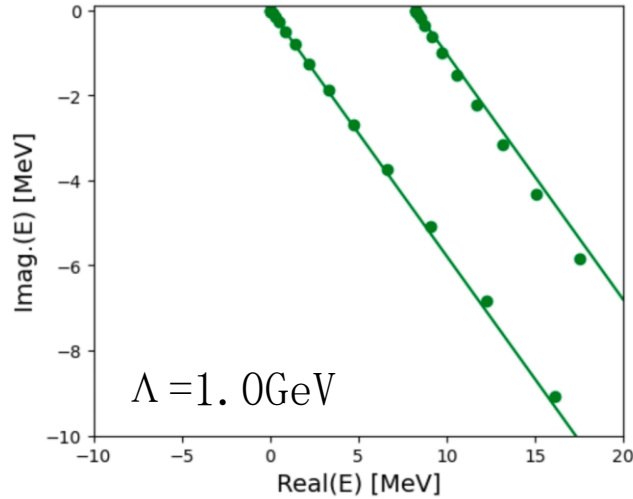
First of all, it is attractive interaction while it is not enough to form a bound state, while just a virtual state

$$3870.0 + 0.26 i \text{ MeV}$$



Produce X(3872) with $D\bar{D}^* + \bar{D}D^*$ and $c\bar{c}$

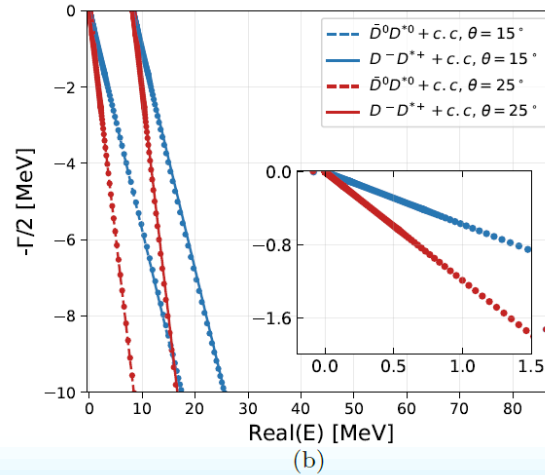
From the interaction of DD^* to obtain the interaction of $D\bar{D}^* + \bar{D}D^*$, check X(3872) exists or not by pure $D\bar{D}^* + \bar{D}D^*$ interaction, without $c\bar{c}$ state.



- **Bound state: T_{cc}**
 $m_{T_{cc}} = 3874.7 \text{ MeV}$,
 $\Delta E = -393 \text{ keV}$
 $\Gamma_{T_{cc}} = 70.4 \text{ keV}$
- $\sqrt{\langle r^2 \rangle} = 4.7 \text{ fm}$
- 70.0% $D^{*+}D^0$, 30.0% D^+D^{*0}

Attractive interaction BUT not enough to form a bound state

- A bare state shows the $c\bar{c}$ bare state component. $\chi_{c1}(2P, 3940)$ and its wave function, determined by the quark model.
- The interaction parameter $\gamma = 4.69$ for the 3P0 model is determined through $\psi(3770)$ to $D\bar{D}$.
- Therefore the analysis of X(3872) does **not** introduce any **additional parameters**.



- **Bound state for X(3872)**
 $\Delta E = -80.4 \text{ keV}$
 $\Gamma_{T_{cc}} = 32.5 \text{ keV}$
- $\sqrt{\langle r^2 \rangle} = 11.2 \text{ fm}$
- 94.0% $\bar{D}^{*0}D^0$, 4.8% $D^{*-}D^+$, 1.2% $c\bar{c}$



The nature of T_{cc} and $X(3872)$

- T_{cc} bound state of $D^{*+}D^0$

$$\Delta E = -393 \text{ keV} \quad \Gamma_{T_{cc}} = 70.4 \text{ keV}$$

- $\sqrt{\langle r^2 \rangle} = 4.7 \text{ fm}$

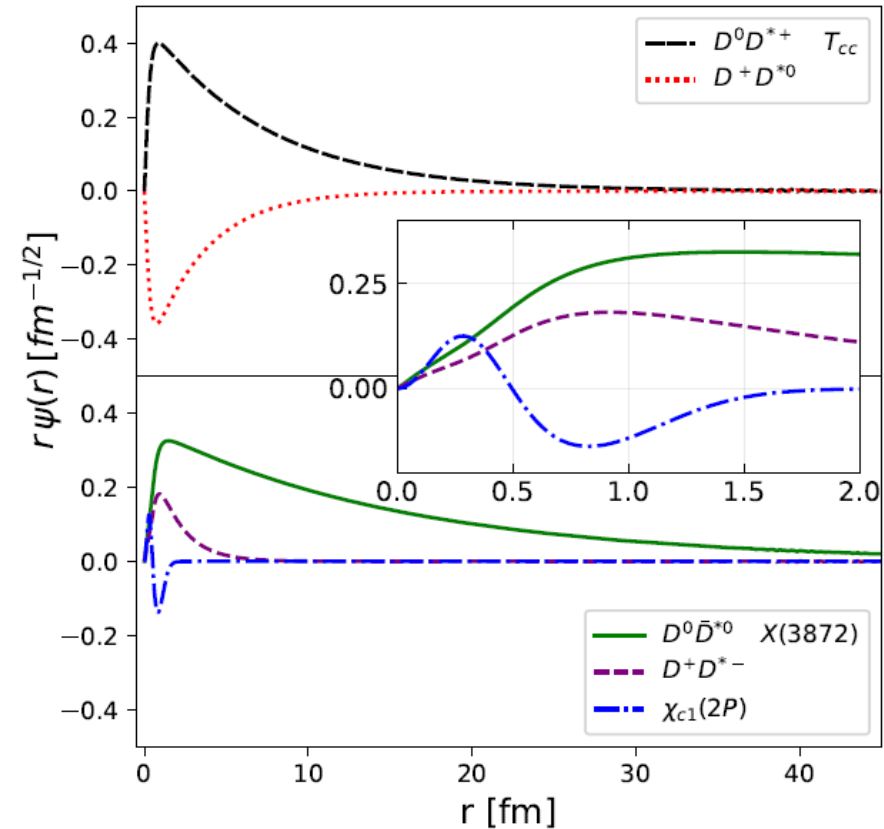
- 70.0% $D^{*+}D^0$, 30.0% D^+D^{*0}

- $X(3872)$ bound state of $\bar{D}^{*0}D^0$

$$\Delta E = -80.4 \text{ keV} \quad \Gamma_{T_{cc}} = 32.5 \text{ keV}$$

- $\sqrt{\langle r^2 \rangle} = 11.2 \text{ fm}$

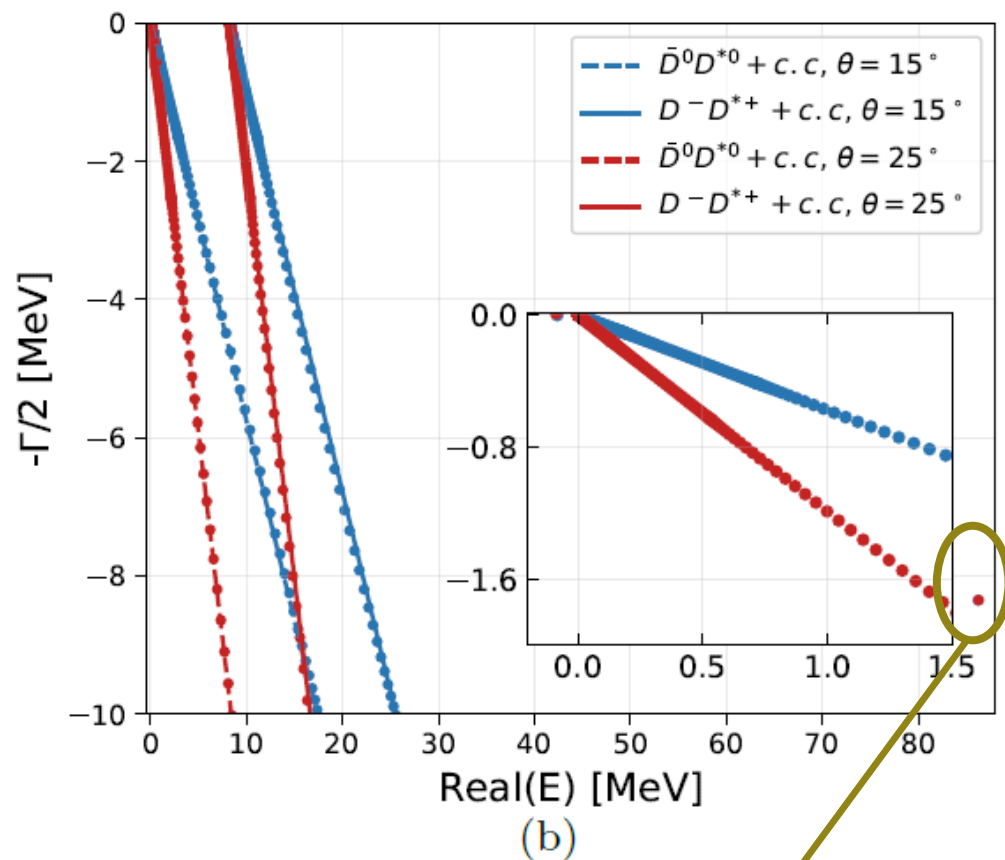
- 94.0% $\bar{D}^{*0}D^0$, 4.8% $D^{*-}D^+$, 1.2% $c\bar{c}$



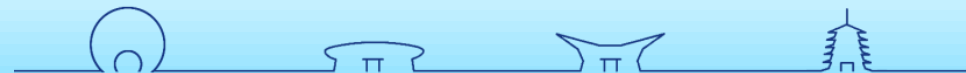
ΔE of $X(3872)$ is extremely small, a significant $D^{*0}\bar{D}^0$ wave function, dominates in long-range
the $c\bar{c}$ component predominant in short-range, it is important to form this bound state



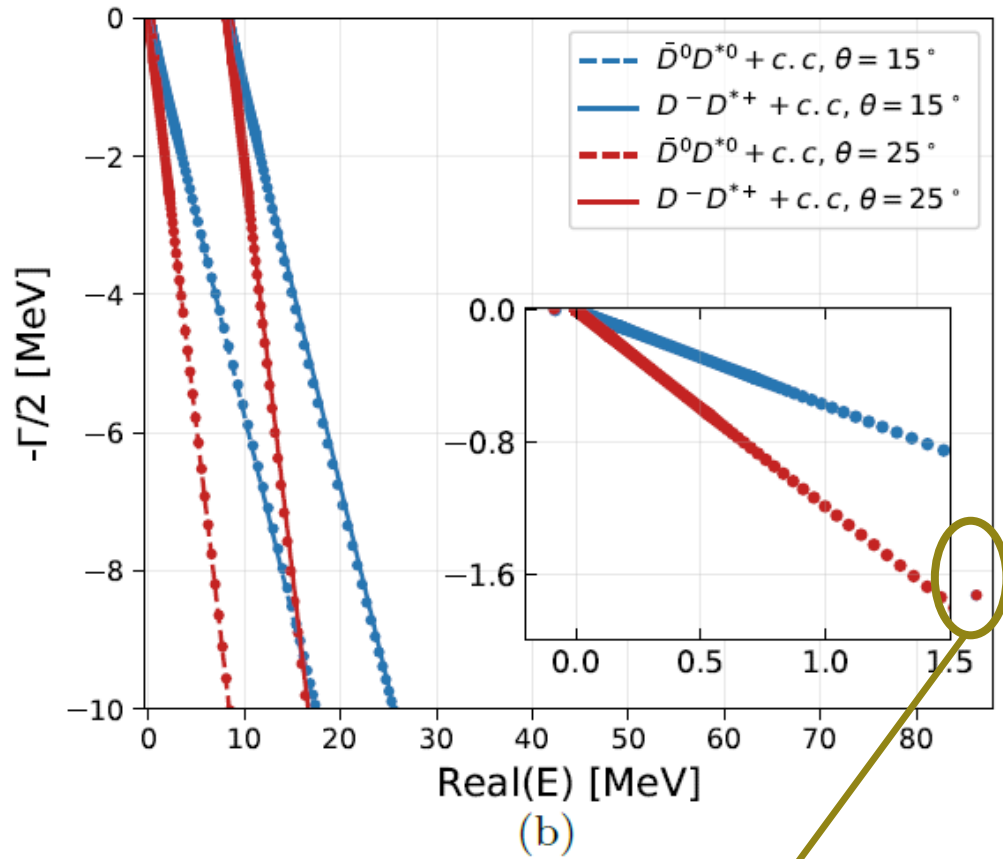
Prediction



- $\chi_{c1}(2p)$
 $M = 3957.9 \text{ MeV}$ $\Gamma_{\chi_{c1}(2P)} = 16.7 \text{ MeV}$
- Main decay channel: $\bar{D}^* D$



Prediction



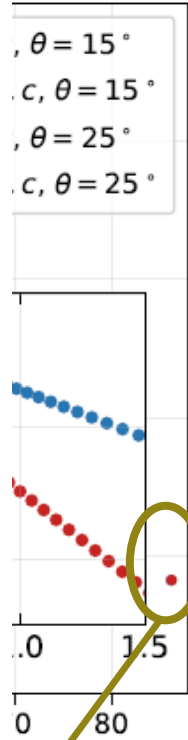
- $\chi_{c1}(2p)$
 $M = 3957.9 \text{ MeV}$ $\Gamma_{\chi_{c1}(2P)} = 16.7 \text{ MeV}$
- Main decay channel: $\bar{D}^* D$

J^{PC}	$Lq\bar{q}$	$Sq\bar{q}$		
0^{-+}	0	0	$\eta_c(2980)$	$\eta_c(2S)$
1^{-}	0	1	$J/\psi(3096)$	$\psi(2S), \dots$
	2	1	$\psi(3770)$	
1^{+-}	1	0	$h_c(3525)$	z_c
0^{++}	1	1	$\chi_{c0}(3414)$	$\chi_{c0}(3860)$
1^{++}	1	1	$\chi_{c1}(3510)$?
2^{++}	1	1	$\chi_{c2}(3556)$	$\chi_{c2}(3930)$
2^{-}	2	1	$\psi_2(3823)$	
3^{-}	2	1	$\psi_3(3842)$	
2^{-+}	2	0	?	



Prediction

J^{PC}	$Lq\bar{q}$	$Sq\bar{q}$		
0^{-+}	0	0	$\eta_c(2980)$	$\eta_c(2S)$
1^{--}	0	1	$J/\psi(3096)$	$\psi(2S), \dots$
	2	1	$\psi(3770)$	
1^{+-}	1	0	$h_c(3525)$	z_c
0^{++}	1	1	$\chi_{c0}(3414)$	$\chi_{c0}(3860)$
1^{++}	1	1	$\chi_{c1}(3510)$?
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2^{--}	2	1	$\psi_2(3823)$	
3^{--}	2	1	$\psi_3(3842)$	
2^{-+}	2	0	?	



• $\chi_{c1}(2p)$

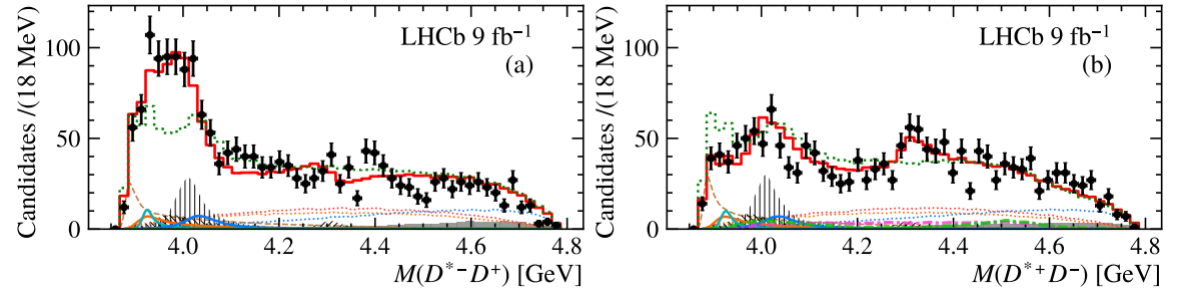
$M = 3957.9 \text{ MeV} \quad \Gamma_{\chi_{c1}(2P)} = 16.7 \text{ MeV}$

• Main decay channel: $\bar{D}^* D$

Observation of new charmonium(-like) states
in $B^+ \rightarrow D^{*\pm} D^{\mp} K^+$ decays

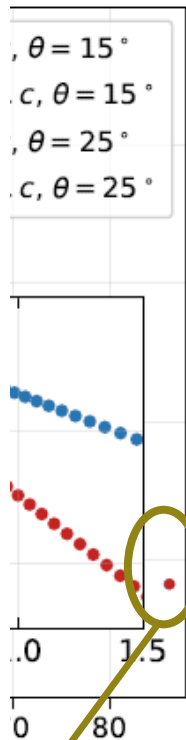
LHCb Collaboration 2406.03156

$\chi_{c1}(4010) \quad J^{PC} = 1^{++}$
 $m_0 = 4012.5^{+3.6+4.1}_{-3.9-3.7} \text{ GeV} \quad \Gamma_0 = 62.7^{+7.0+6.4}_{-6.4-6.6} \text{ MeV}$



Prediction

J^{PC}	$Lq\bar{q}$	$Sq\bar{q}$		
0^{++}	0	0	$\eta_c(2980)$	$\eta_c(2S)$
1^{--}	0	1	$J/\psi(3096)$	$\psi(2S), \dots$
	2	1	$\psi(3770)$	
1^{+-}	1	0	$h_c(3525)$	z_c
0^{++}	1	1	$\chi_{c0}(3414)$	$\chi_{c0}(3860)$
1^{++}	1	1	$\chi_{c1}(3510)$?
2^{++}	1	1	$\chi_{c2}(3556)$	$\chi_{c2}(3930)$
2^{--}	2	1	$\psi_2(3823)$	
3^{--}	2	1	$\psi_3(3842)$	
2^{+-}	2	0	?	



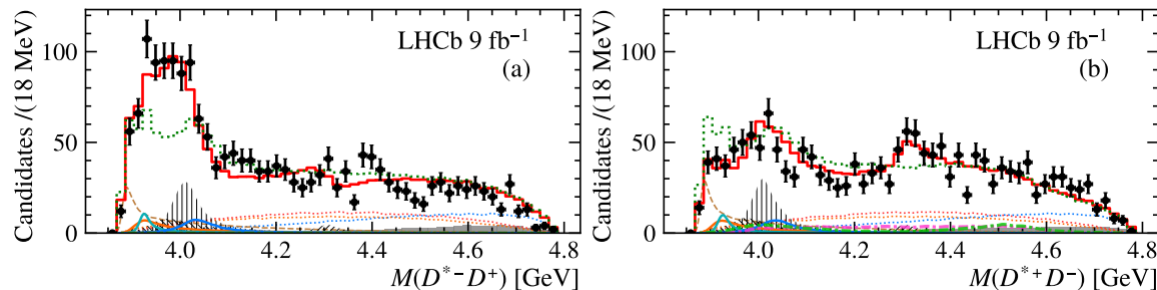
- $\chi_{c1}(2p)$
 $M = 3957.9 \text{ MeV}$ $\Gamma_{\chi_{c1}(2p)} = 16.7 \text{ MeV}$
- Main decay channel: $\bar{D}^* D$

Observation of new charmonium(-like) states
 in $B^+ \rightarrow D^{*\pm} D^{\mp} K^+$ decays

LHCb Collaboration 2406.03156

$$\chi_{c1}(4010) \quad J^{PC} = 1^{++}$$

$$m_0 = 4012.5^{+3.6+4.1}_{-3.9-3.7} \text{ MeV} \quad \Gamma_0 = 62.7^{+7.0+6.4}_{-6.4-6.6} \text{ MeV}$$



X(3872) Relevant $D\bar{D}^*$ Scattering in $N_f = 2$ Lattice QCD

H. Li, C. Shi, Y. Chen, M. Gong, J. Liang et al

CLQCD 2402.14541

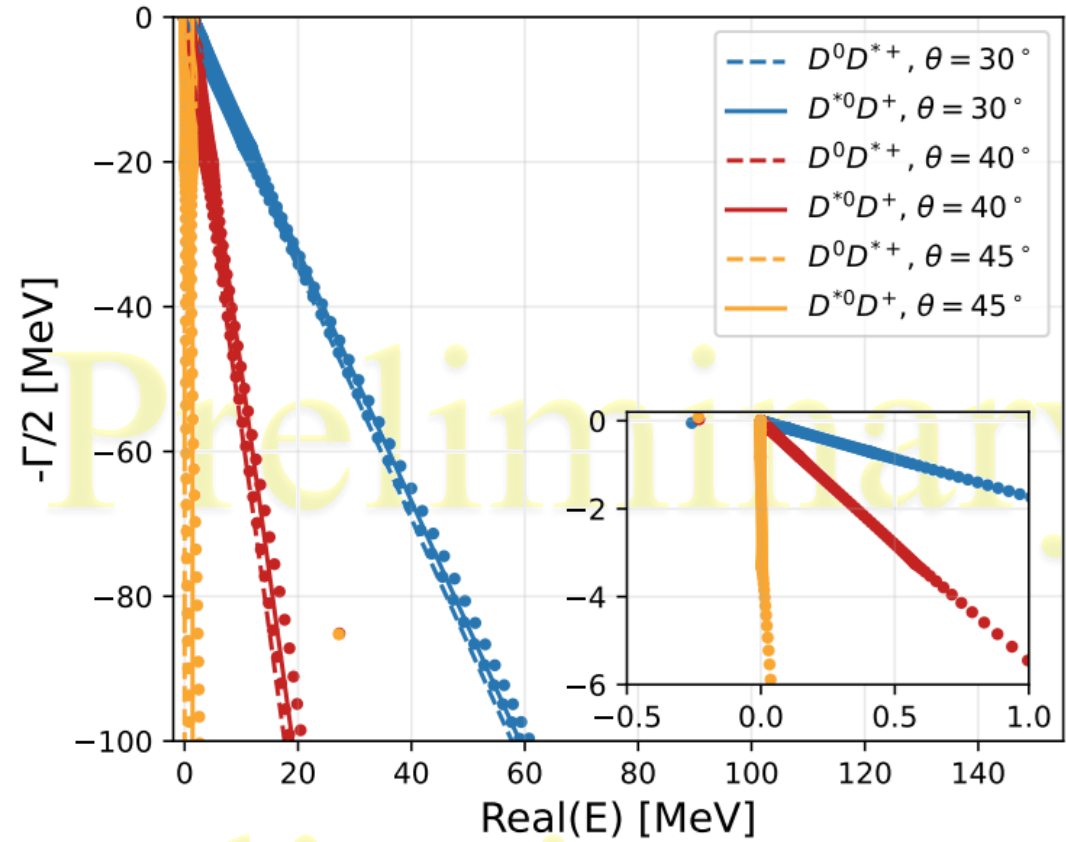
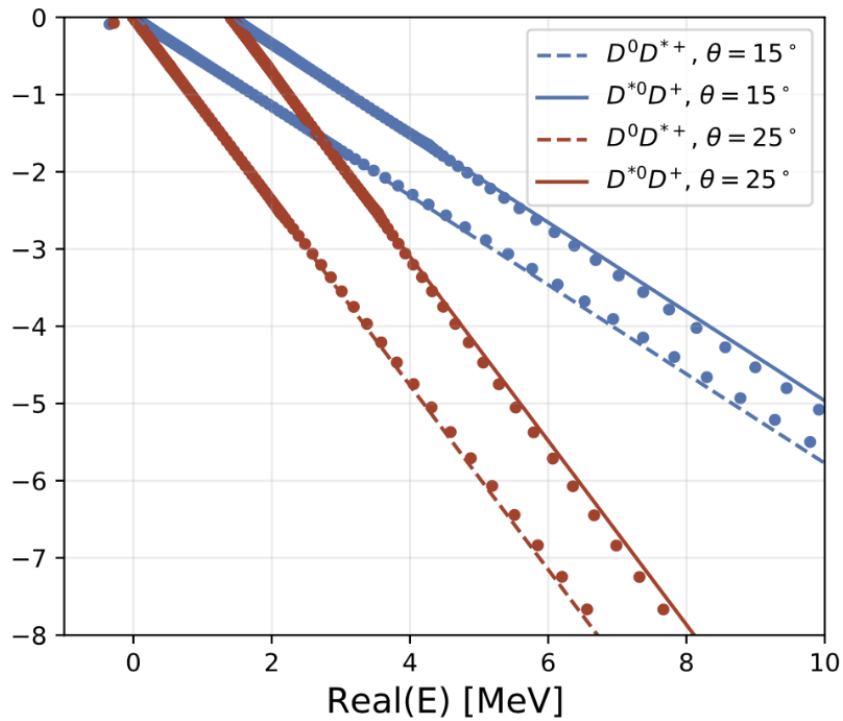
$$t(s) = \frac{K(s)}{1 - K(s)i\rho(s)}$$

$$K(s) = \frac{g}{M^2 - s} + \gamma$$

m_π (MeV)	250(3)	307(2)	362(1)	417(1)
Bound state from $E_{2,3}$				
E_B (MeV)	$-9.7^{+2.1}_{-2.2}$	$-9.7^{+1.9}_{-2.0}$	$-1.3^{+0.6}_{-0.8}$	$-1.3^{+0.8}_{-1.0}$
BW fit from $E_{3,4}$				
m_R (MeV)	3924(5)	3926(6)	3969(4)	3995(4)
Γ_R (MeV)	63(23)	57(18)	37(13)	57(10)
Bound state pole and residual from $E_{2,3,4}$				
E_B (MeV)	-11(1)	-10(2)	-1.6(7)	-1.7(7)
Resonance pole and residue				
m_R (MeV)	4008(4)	4029(4)	4050(3)	4071(3)
Γ_R (MeV)	60(6)	38(9)	43(8)	50(7)
$\text{Br}_{D\bar{D}^*}$ (%)	~ 100	~ 100	~ 100	~ 100



Prediction

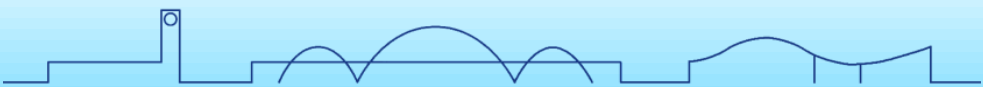


A new T_{cc} resonance $M=3902.4$ MeV, $\Gamma=170.3$ MeV, $I \sim 1$



Summary

- Through T_{cc} to determine the DD^* interaction
- Through fixed DD^* interaction, and the nature of bare state to study $X(3872)$
- We find that the $\bar{D}D^*$ component dominates in $X(3872)$, but it is mainly distributed in the long-range part, i.e., >1 fm, while the bare state still dominates in the short-range part.
- We predict $X(3957)$ which may corresponding to $X(4010)$ from LHCb

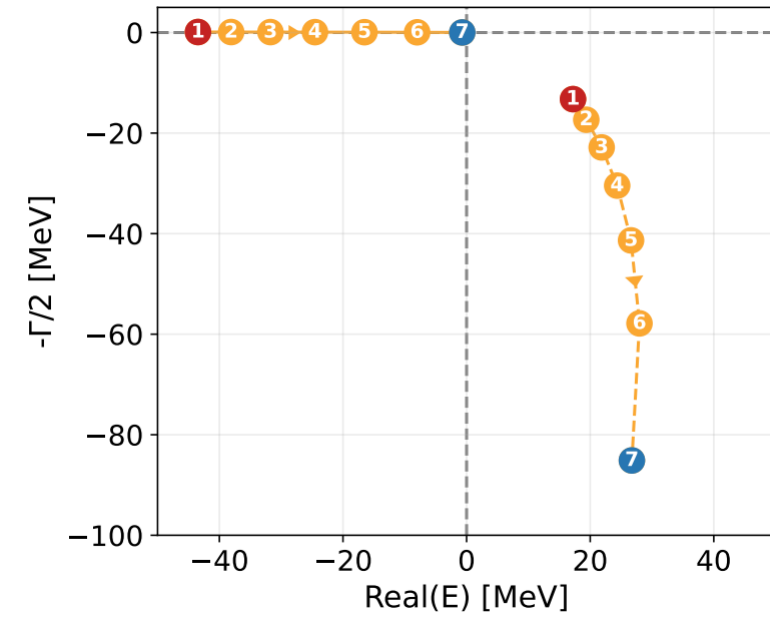
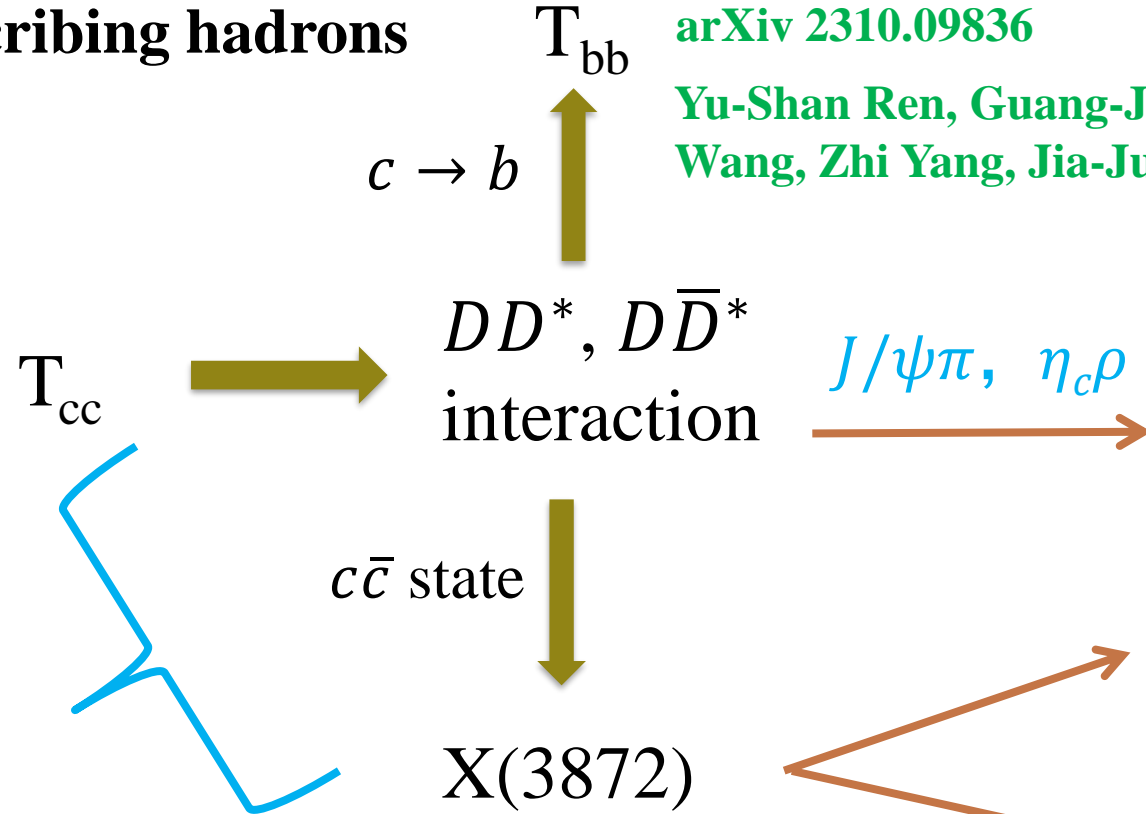


A more **comprehensive**
framework for
systematically
describing hadrons

Outlook

arXiv 2310.09836

Yu-Shan Ren, Guang-Juan
 Wang, Zhi Yang, Jia-Jun Wu



Study $Z_c(3900)$, soon ...

Study the decay of $X(3872)$, soon...

Study the decay of $X(4010)$

Lattice spectrum
 soon...

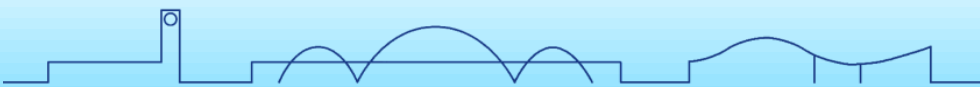


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FB23



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University of Chinese Academy of Science China Center of Advanced Science and Technology
Institute of Theoretical Physics, Chinese Academy of Sciences South China Normal University
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TOPICS

- Few-body aspects of atomic and molecular physics
- Hadrons and related high-energy physics
- Neutrinos and their interactions with matter
- Strange and exotic matter, including hypernuclear physics
- Few-nucleon systems, including QCD inspired approaches
- Few-body aspects of nuclear physics and nuclear astrophysics
- Interdisciplinary aspects of few-body physics and techniques

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