

Physics overview of J-PARC (Hadron)

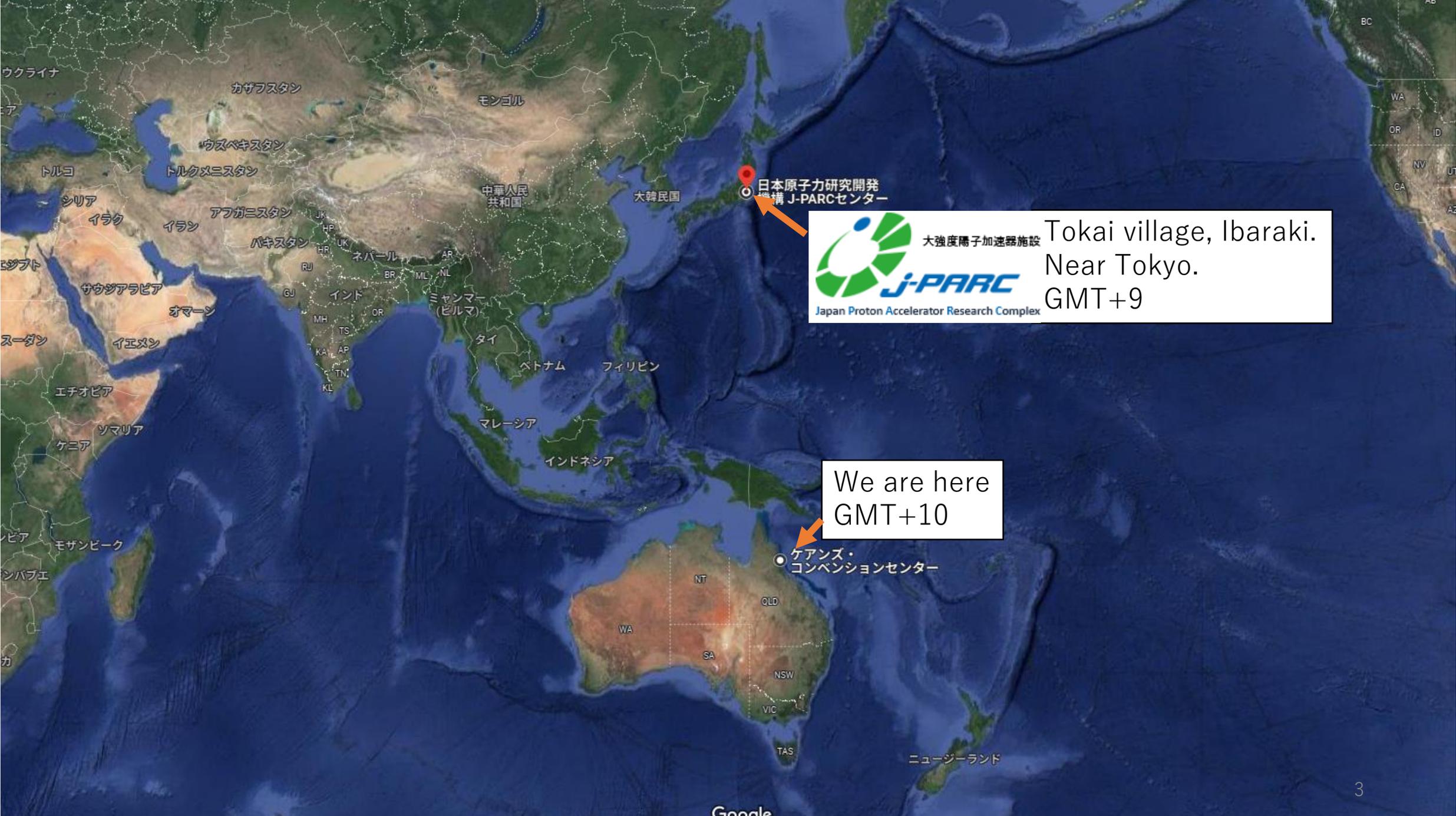
K. Aoki
KEK/J-PARC

XVIth Quark Confinement and the Hadron Spectrum Conference
19-24 Aug. 2024

Picture taken on 19 Aug
Cairns

Contents

- J-PARC
- J-PARC HD (Hadron Experimental Facility) and beam lines
- Physics Motivation
- List of experiments already finished or in data-taking period
- Pick up some of experiments and discuss results and introduce some of on-going experiment.
- Future projects.



日本原子力研究開発
機構 J-PARCセンター



Tokai village, Ibaraki.
Near Tokyo.
GMT+9

We are here
GMT+10

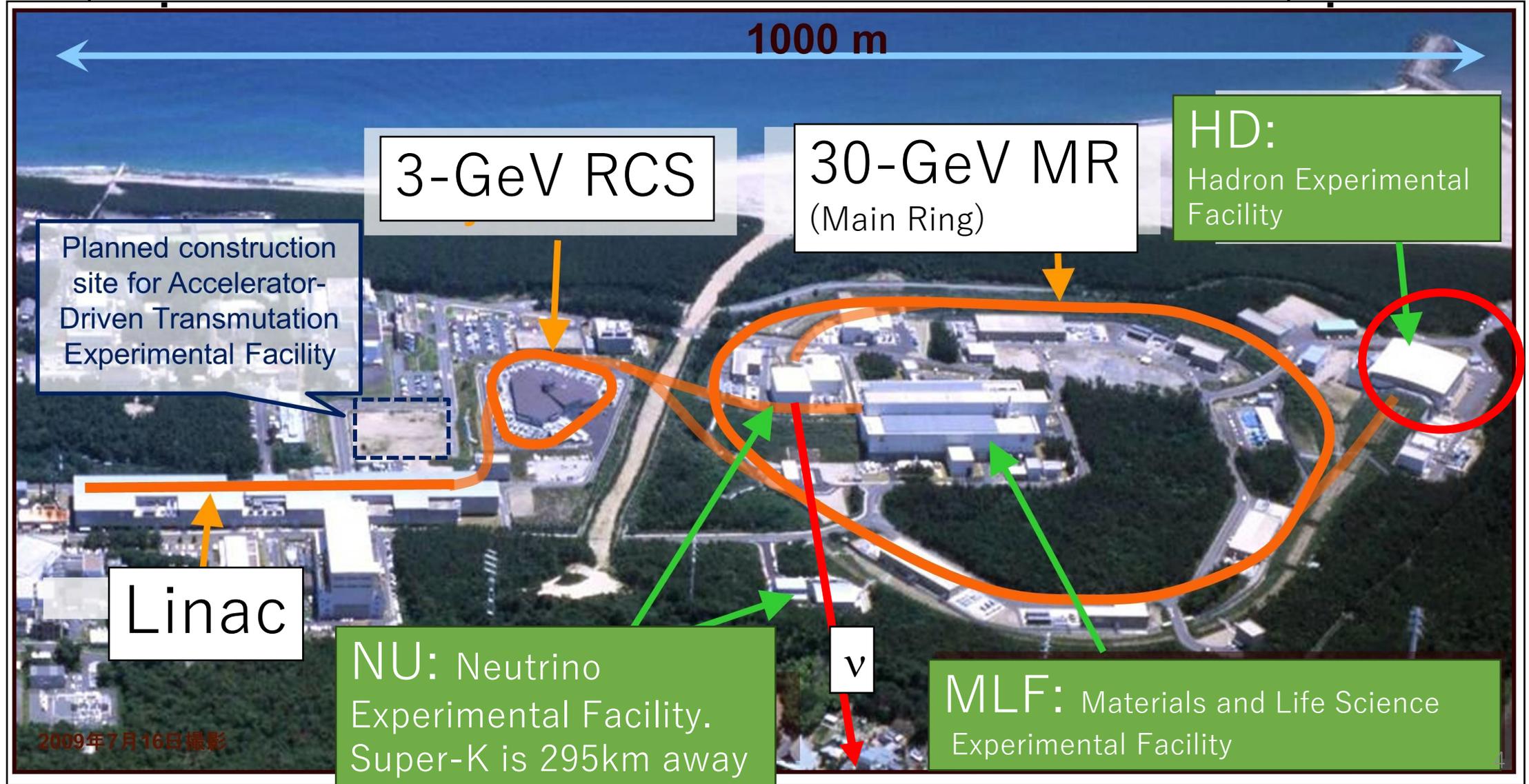
ケアンズ・
コンベンションセンター

J-PARC

Japan Proton Accelerator Research Complex



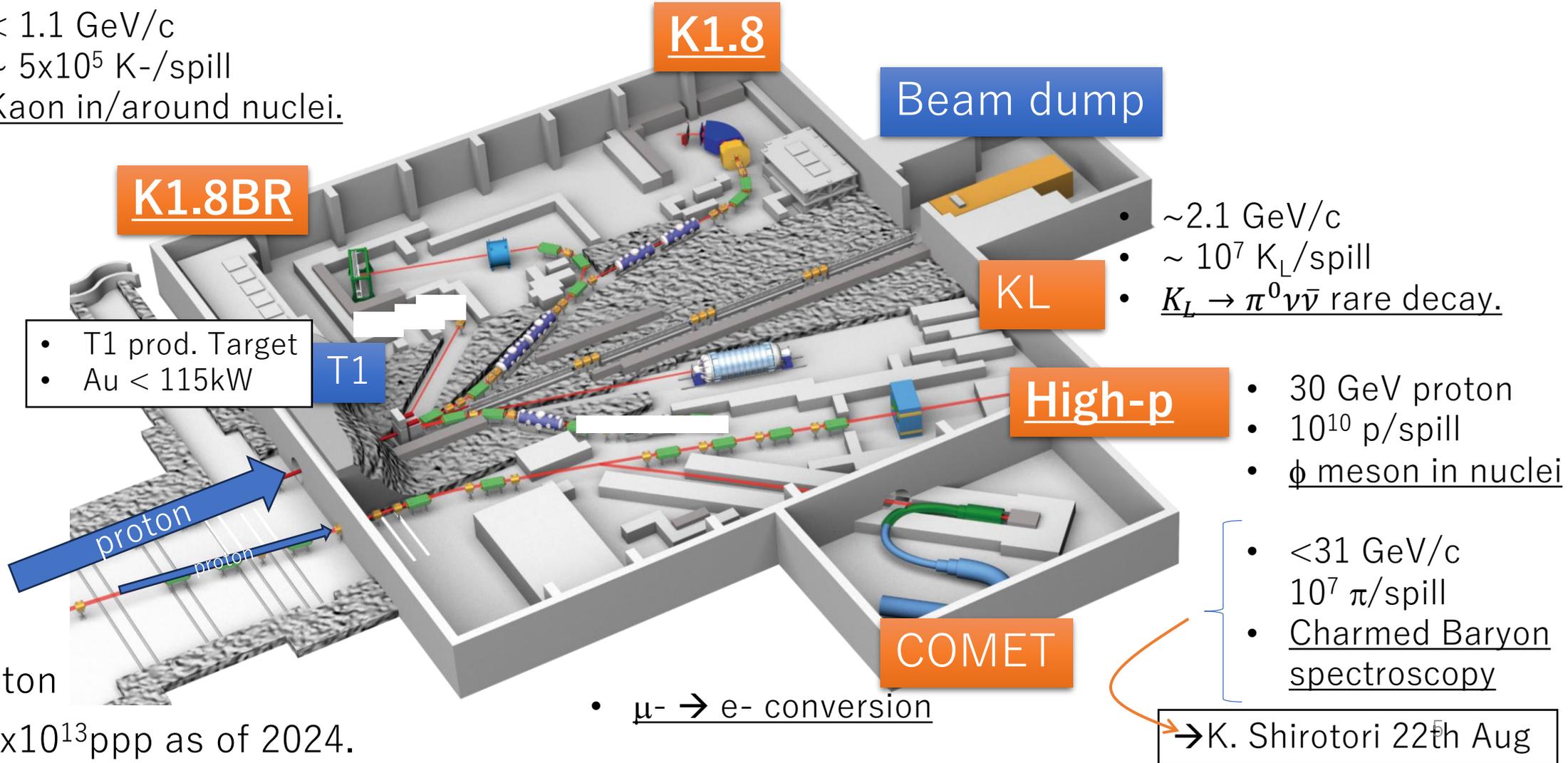
Japan Atomic Energy Agency



Beam lines at J-PARC HD (Hadron Exp. Facility)

- $< 1.1 \text{ GeV}/c$
- $\sim 5 \times 10^5 \text{ K}^-/\text{spill}$
- Kaon in/around nuclei.

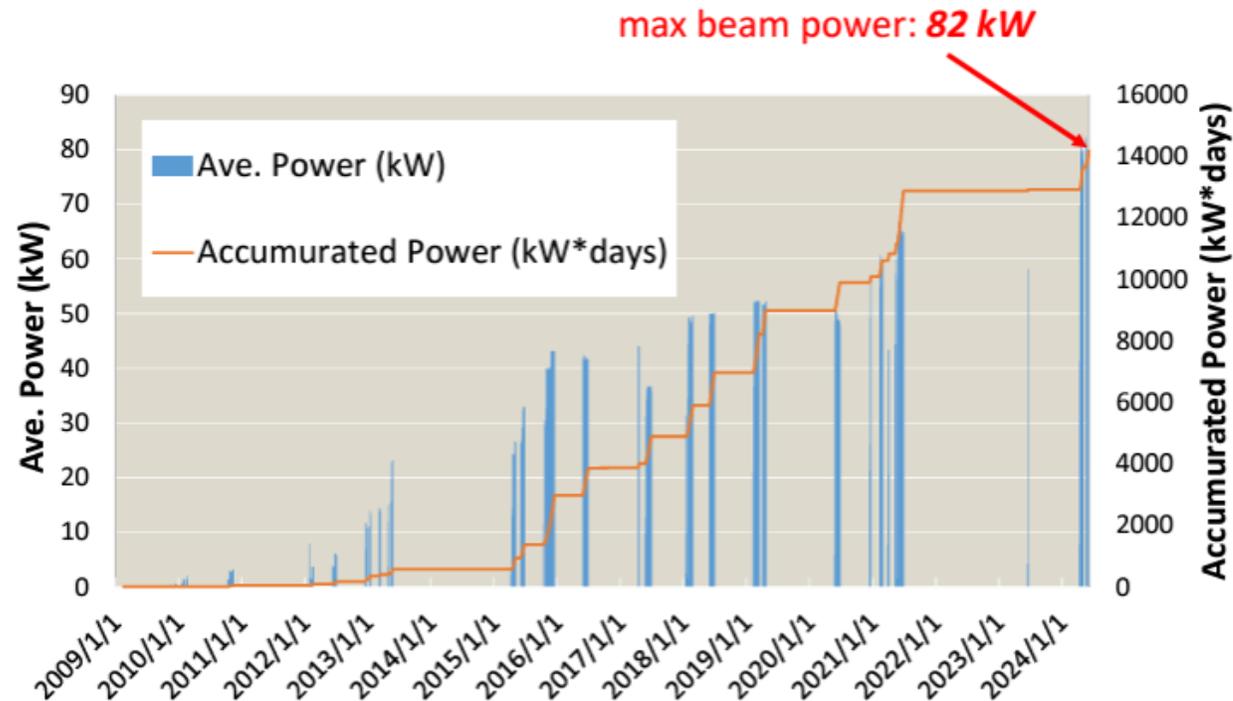
- $< 2.0 \text{ GeV}/c$
- $\sim 10^6 \text{ K}^-/\text{spill}$
- $S=-1, -2$ Hypernuclei, YN scatt.



SX (Slow extraction) beam power

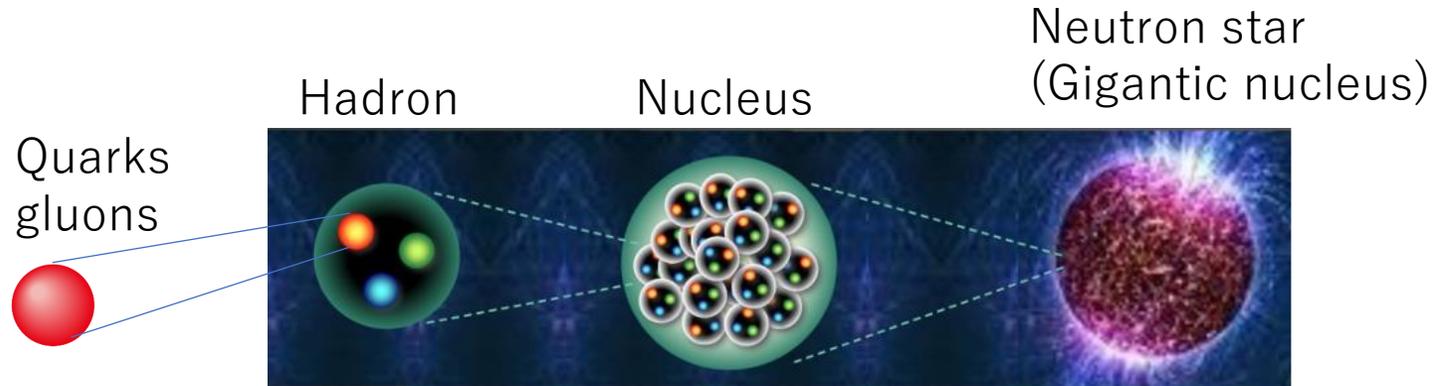
- Beam power gradually increased over the 15 years.
- Reached 82kW. 30GeV proton, $7.2E13$ /spill. Spill=4.24 sec.

SX Beam Power History



Physics motivation in one slide:

Understand strongly interacting system from quark to neutron star.



- Quark \rightarrow Hadron : How quarks and gluons form hadrons?
 - Quark Confinement. Spontaneous breaking of chiral symmetry.
 - Meson in nuclei \rightarrow ϕ (high-p, E16), K^{bar} (K1.8BR, E15)
- Hadron \rightarrow Nucleus \rightarrow Neutron Star : Property of dense matter?
 - Precise Baryon-Baryon interaction incl. hyperons and its density dependence
 - ΣN Scattering experiment (K1.8, E40)
 - $S=-1, -2$ hypernuclei and γ -ray spectroscopy. (K1.8)

Experiments completed or data-taking.

- K1.8 beam line:YN int. by $S=-1$, -2 hypernuclei and scatt.
 - Completed
 - E19: Search for Θ^+ pentaquark in $\pi^- p \rightarrow K^- X$ reactions
 - E27: Search for a nuclear K^{bar} bound state K^-pp in $d(\pi^+,K^+)$
 - E10 1st : Neutron rich Λ hypernuclei (${}^6_{\Lambda}\text{H}$) search ($S=-1$)
 - E13: γ -ray spectroscopy of light hypernuclei ${}^4_{\Lambda}\text{He}$
 - E05: Spectroscopic study of Ξ^- hypernuclei, ${}^{12}_{\Xi}\text{Be}$, via ${}^{12}\text{C}$ (K^-,K^+) ($S=-2$)
 - Events in bound region. E70 is going to measure it with x4 resolution.
 - E07: Systematic study of double strangeness system with an emulsion-counter hybrid method.
 - Xi- hypernuclei (IBUKI 1st uniquely identified state, IRRAWADY)
 - E40: Cross sections of Σp scatterings.
 - E03 1st: Measurement of X rays from Ξ^- atom.
 - E42: Search for H-dibaryon with a Large Acceptance Hyperon Spectrometer
 - Blind analysis. Not opened yet.
 - Data taking
 - E70 : Proposal for the next E05 run with the S-2S spectrometer
 - E96 : X rays from Ξ^- C atom with an active fiber target system

Experiments completed or data-taking.

- K1.8BR beam line: $\bar{K}N$ interaction
 - Completed
 - E15: A search for deeply-bound kaonic states by in-flight $^3\text{He}(K^-,n)$
 - E31: Spectroscopic study of hyperon resonance below KN threshold via $d(K^-,n)$
 - E62: Precision Spectroscopy of kaonic atom X-rays with TES.
 - data taking
 - E73: $^3_{\Lambda}\text{H}$ and $^4_{\Lambda}\text{H}$ mesonic weak decay lifetime meas with $^{3,4}\text{He}(K^-,\pi^0)^{3,4}_{\Lambda}\text{H}$.
- KL beam line: BSM
 - Data taking
 - E14: $K_L \rightarrow \pi^0 \nu \bar{\nu}$ experiment.
- High-p beam line: Meson in medium
 - Data taking (Commissioning.)
 - E16: Measurements of spectral change of vector mesons in nuclei

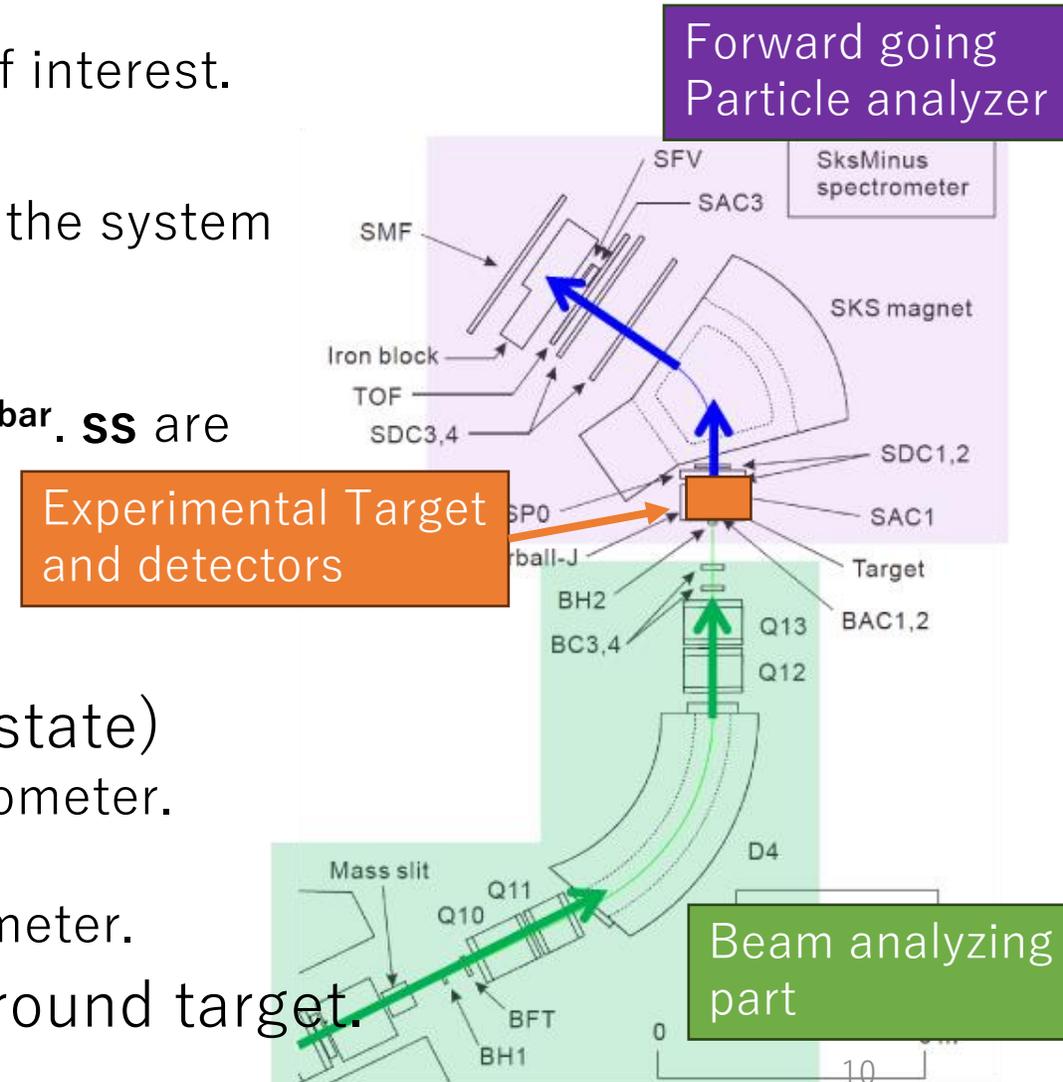
K1.8 beam line : $S=-1,-2$ hypernucleus, YN scattering experiment.

Hyperon, hypernuclei production scheme

- (beam , out-going particle)
- (K^-, π) -- $S=-1$ system
 - \mathbf{s} in the beam and the \mathbf{s} is put into the system of interest.
- (π, K^+) -- $S=-1$ system
 - \mathbf{ss}^{bar} pair created. K^+ take away \mathbf{s}^{bar} . \mathbf{s} is put in the system of interest.
- (K^-, K^+) -- $S=-2$ system
 - \mathbf{s} in the beam and \mathbf{ss}^{bar} created. K^+ take away \mathbf{s}^{bar} . \mathbf{ss} are put into the system of interest.

K1.8 common concept

- Missing mass technique. (Initial state)
 \leftrightarrow invariant Mass (Final state)
 - Incoming beam is analyzed by beam line spectrometer.
 - Experimental target. (Seed of hypernuclei)
 - Out-going particle analyzed by forward spectrometer.
- Experiment specific detectors are placed around target.
 - γ -ray detectors / nuclear emulsion etc..



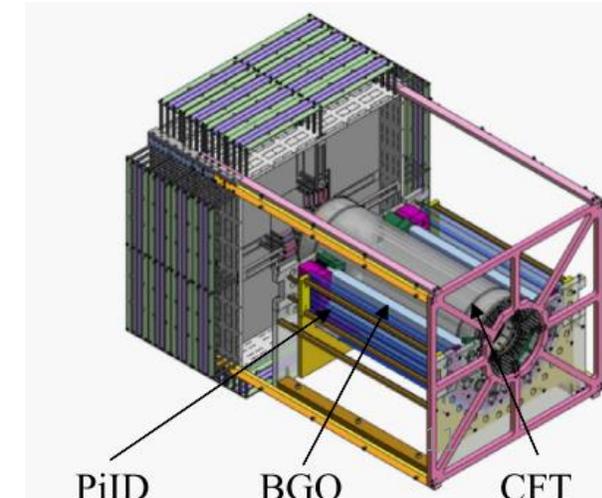
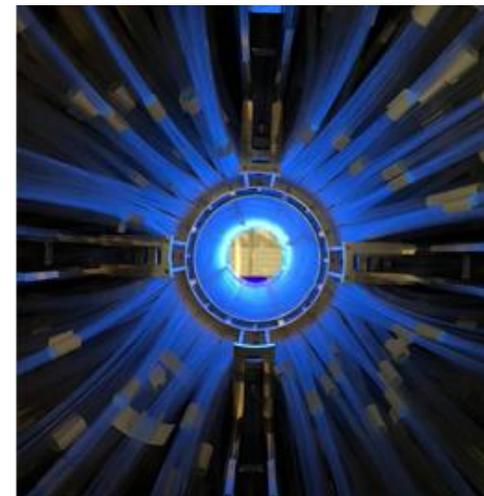
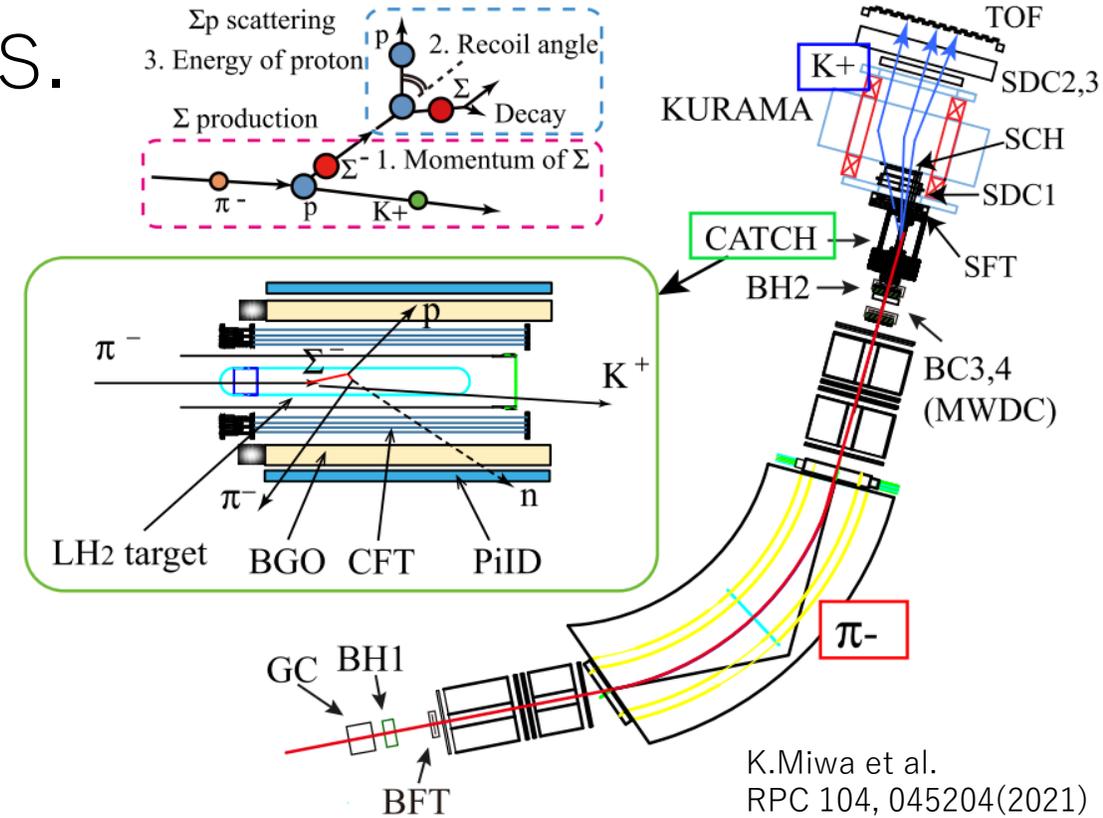
J-PARC E40 : Σp scatterings.

- Σ^\pm “beam” produced in LH2 target

- $p(\pi^-, K^+) : \pi^- p \rightarrow K^+ \Sigma^-$
- $p(\pi^+, K^+) : \pi^+ p \rightarrow K^+ \Sigma^+$
 - beam line spectrometer (π^\pm) + KURAMA spectrometer (K^+)
 - Missing mass (Σ^\pm)

- Σp scattering

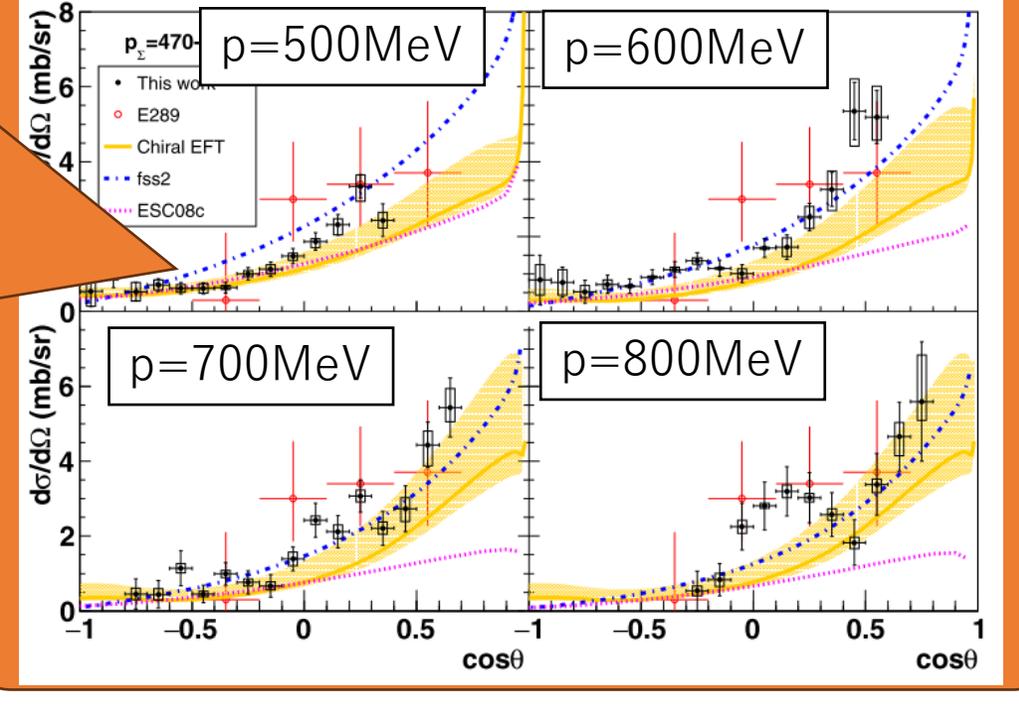
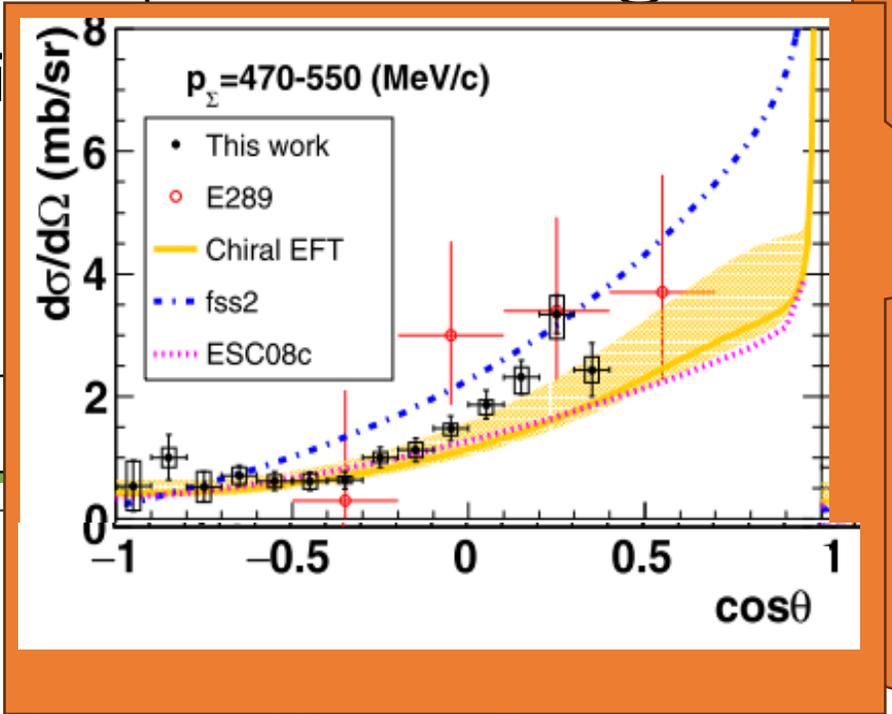
- $\Sigma^- p \rightarrow \Sigma^- p$ 4500 events.
- $\Sigma^+ p \rightarrow \Sigma^+ p$ 2400 events.
- $\Sigma^- p \rightarrow \Lambda n$ 1000 events.
 - Detected by CATCH



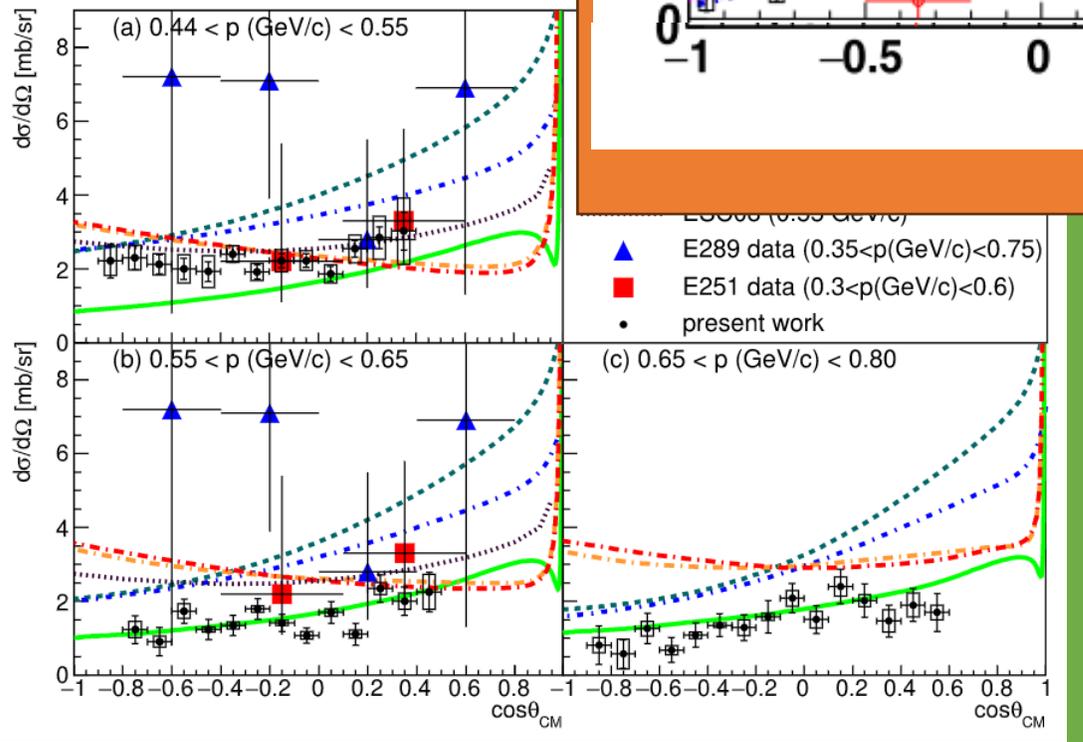
J-PARC E40 : Σp scatterings.

- Improved statistics compared to old measurements.

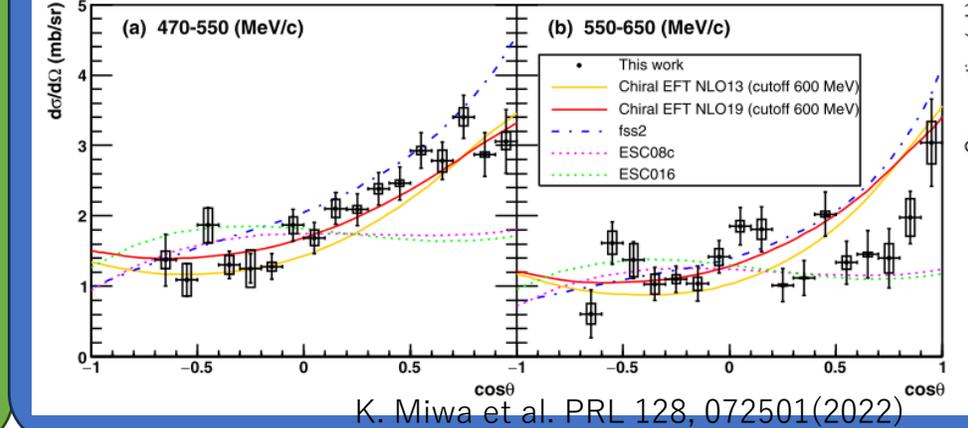
$\Sigma^- p \rightarrow \Sigma^- p$ K.Miwa et al. RPC 104, 045204(2021)



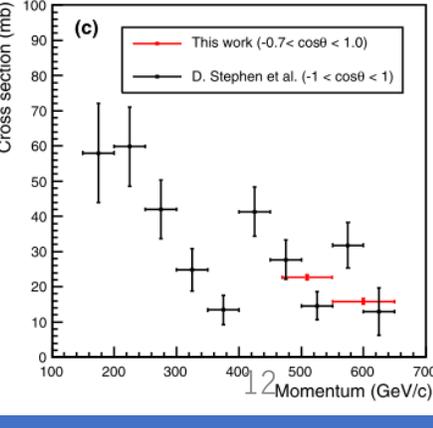
$\Sigma^+ p \rightarrow \Sigma^+ p$



$\Sigma^- p \rightarrow \Lambda n$

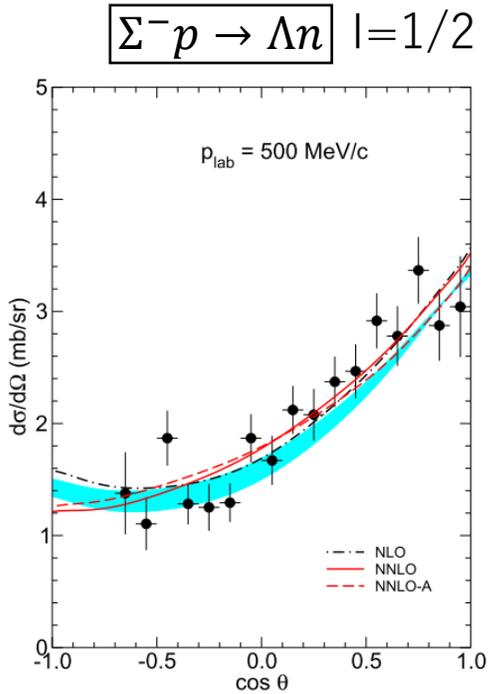


Total cross section

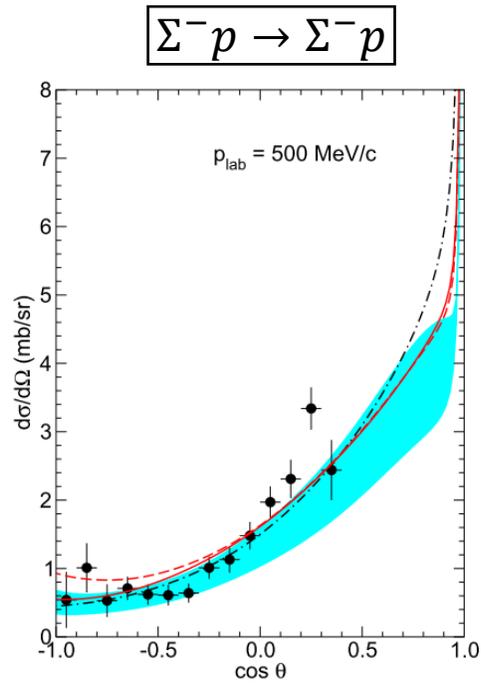


J-PARC E40 : Σp scatterings.

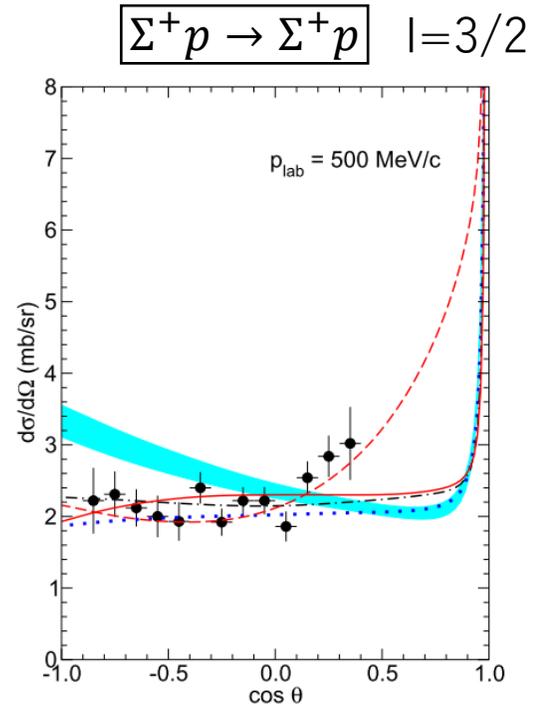
Cyan: NLO19 (w/o E40 data) ,
 Solid: NNLO fit w/ E40 data.
 Dashed NNLO-A: fine tuned to
 500MeV/c data.



K. Miwa et al.
 PRL 128, 072501(2022)



K. Miwa et al.
 RPC 104, 045204(2021)



T. Nanamura et al.
 PTEP 2022 093D01

1 and 3 refer to spin singlet and triplet
 even/odd refer to OAM

BB channel (I)	1 even or 3 odd	3 even or 1 odd
$NN(I=0)$	—	(10*)
$NN(I=1)$	(27)	—
$\Lambda N(I=\frac{1}{2})$	$\frac{1}{\sqrt{10}}[(8_s) + 3(27)]$	$\frac{1}{\sqrt{2}}[-(8_a) + (10^*)]$
$\Sigma N(I=\frac{1}{2})$	$\frac{1}{\sqrt{10}}[3(8_s) - (27)]$	$\frac{1}{\sqrt{2}}[(8_a) + (10^*)]$
$\Sigma N(I=\frac{3}{2})$	(27)	(10)

- E40 data has stimulated NNLO Chiral EFT.

- Haidenbauer et al., Eur. Phys.J.A 59, 3 (2023)

- No additional LEC (Low Energy Constant) at this level except for 3BF. 3BF LEC not considered.
 - Cyan: NLO19 (w/o E40 data) , Solid: NNLO fit w/ E40 data.
 - NLO19 successful reproduce a) and b) but not c). Fit w/ E40 improves.
 - c) Sensitive to 10-plet in SU(3) which does not appear NN interaction.

- Parameters not uniquely determined. Additional information needed. Polarized ΛN scattering experiment planned. \rightarrow J-PARC E86

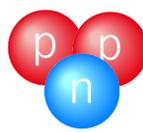
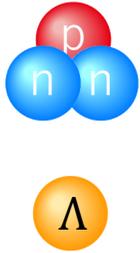
J-PARC E13

S=-1 hypernuclei γ -ray

Mirror nuclei ${}^3\text{H}$ vs ${}^3\text{He}$

- $\Delta M = 18$ keV
- $\Delta B = 764$ keV \rightarrow 70keV after Coulomb corr.
 - $\rho - \omega$ mixing : Ann. Rev. N.P. Sci. 56,253(2006)

Core nucleus



$J=1/2^+$

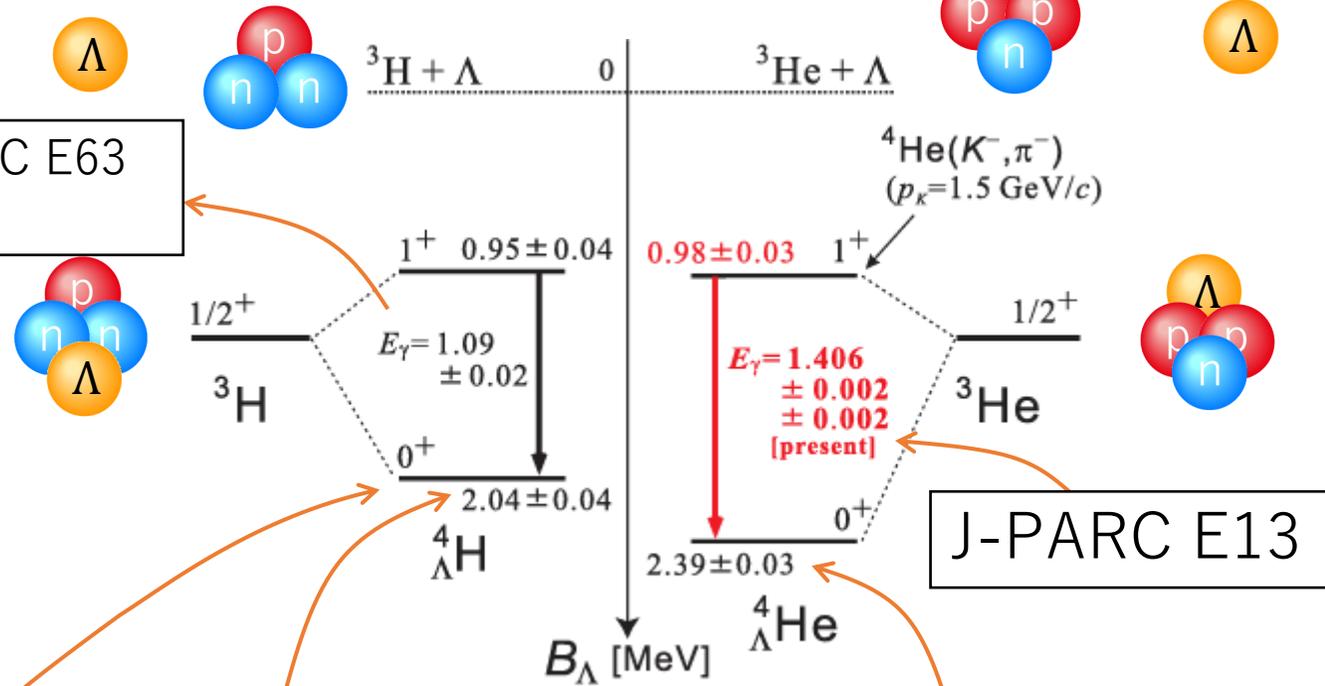
$J=1/2^+$

To be measured \rightarrow J-PARC E63
 \rightarrow H. Tamura 22th Aug.

Mirror nuclei

T.O. Yamamoto et al,
 PRL115, 222501 (2015)

- J-PARC E13 confirmed that that surely charge symmetry is broken. ΛN CSB interaction has spin-dependence.
- $\Lambda\text{N}-\Sigma\text{N}$ coupling plays an important role in CSB.



These g.s. energy deduced from old emulsion data.

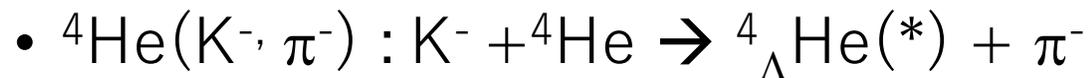
Update on g.s are expected from J-PARC E07
 Emulsion automated-scan and Machine learning.

MAMI-C Measurement: $2.157 \pm 0.005 \pm 0.077$ MeV
 Nucl. Phys. A 954, 149 (2016)

J-PARC E13

S=-1 hypernuclei γ -ray

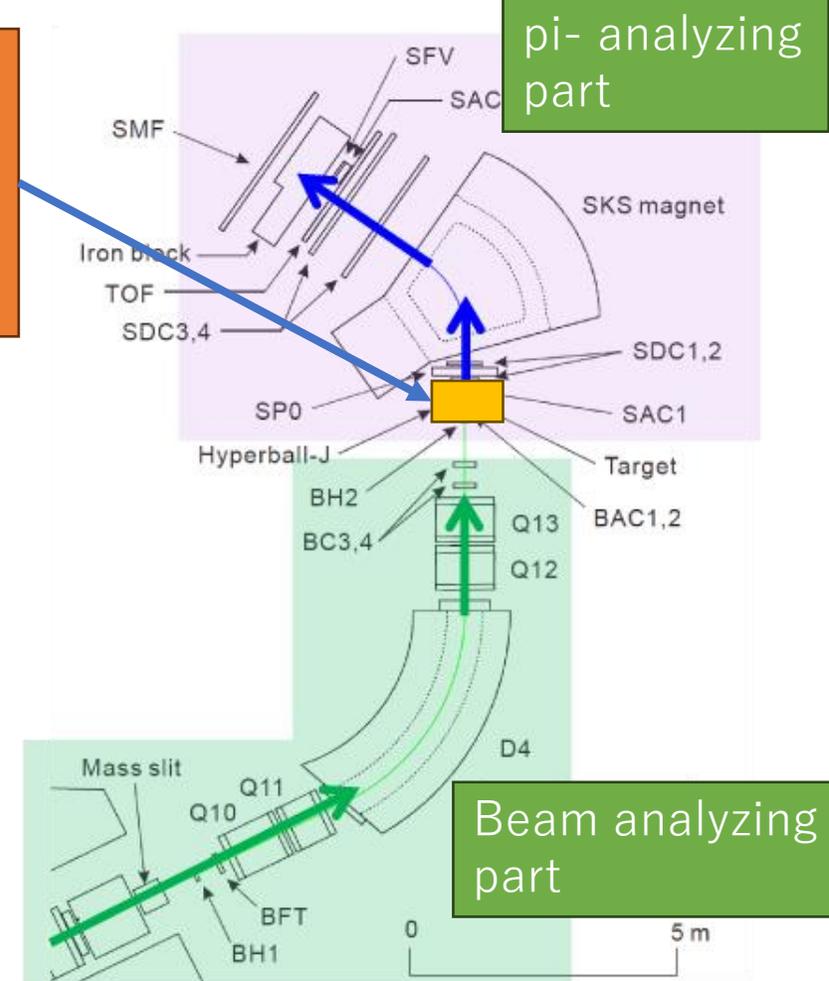
• Reactions



• Detectors

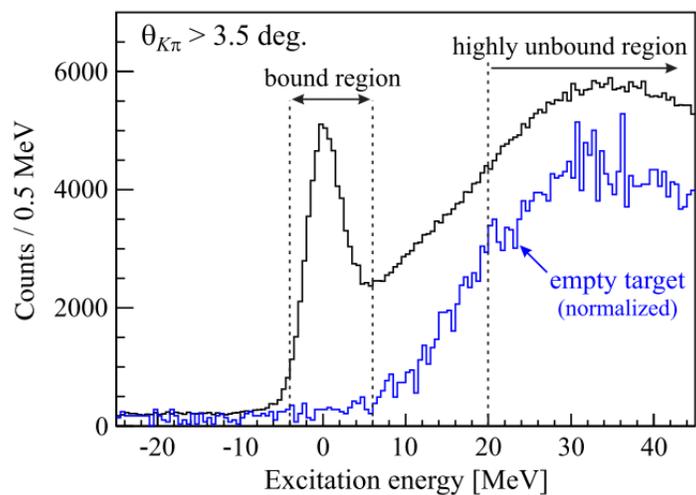
- K- beam (1.5GeV/c) and out-going π^- are analyzed.
- Simultaneous γ -ray measurement by Hyperball-J
 - High resolution Ge instead of NaI used by previous measurement.

Liq. He target
Hyperball-J
(Ge detector array)

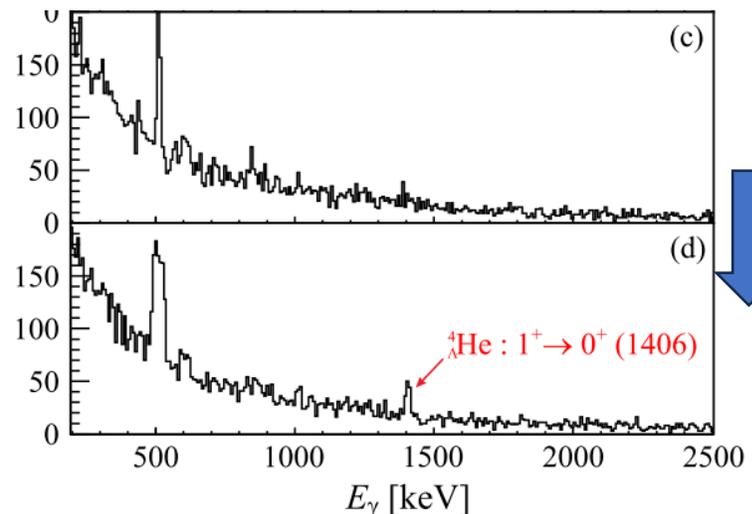


Taken from slide by M. Ukai
At J-PARC Hadron 2024.

Missing mass, identify ${}^4_{\Lambda}\text{He}$



γ energy



Event-by-event
Doppler correction

K- beam: 1.5 GeV/c, 2.3E10 K-,
K/pi ~ 2-3, 3E5/spill
Liq. He target (2.7g/cm²) 12cm ϕ x 23cm

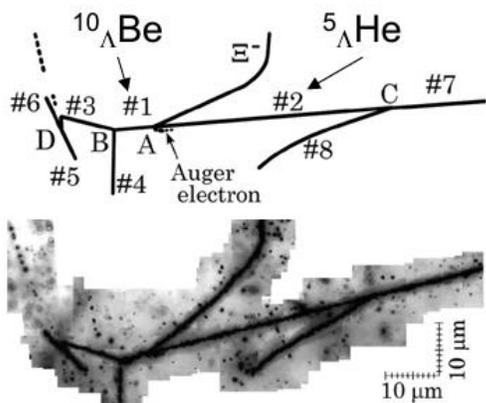
J-PARC E07

S=-2 hypernuclei by Hybrid emulsion method

Slide by
K. Miwa 2nd HEF-EX.

- Emulsions – literally photographic films that capture particle reactions.
- Hybrid – Ξ^- productions were recorded by counters, later search for corresponding position in emulsion by microscope.

(KEK-E325)
KISO event



K. Nakazawa et al., PTEP. 2015, 033D02

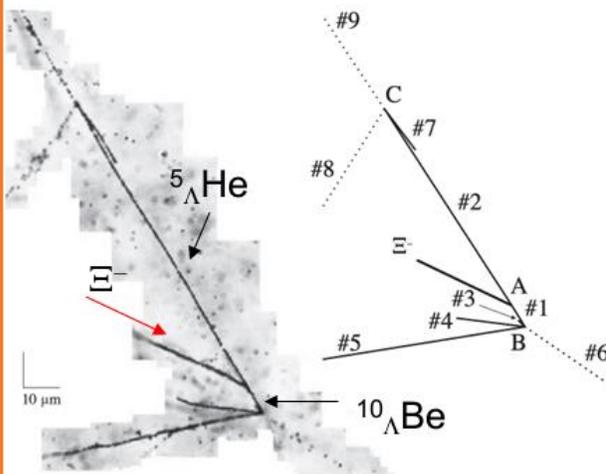
1st discovery of clear Ξ^- nuclear state

Two possibilities of B_{Ξ^-} depending on $^{10}\Lambda\text{Be}$ state

- $B_{\Xi^-} (^{10}\Lambda\text{Be}_{g.s.}) = 3.87 \pm 0.21 \text{ MeV}$
- $B_{\Xi^-} (^{10}\Lambda\text{Be}_{1st. Ex.}) = 1.03 \pm 0.18 \text{ MeV}$

(J-PARC E07)

IBUKI event



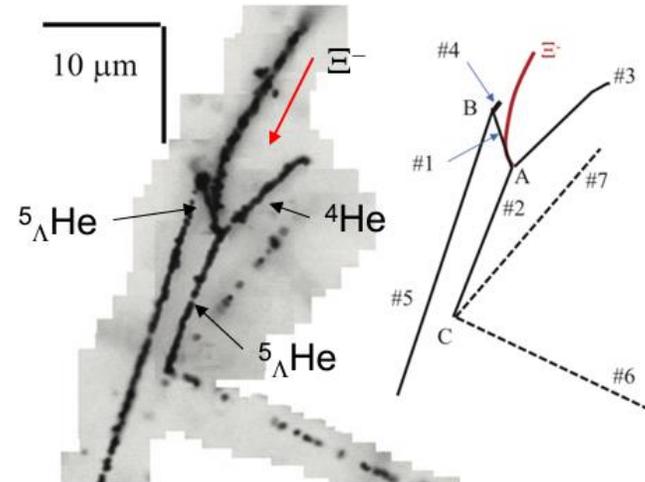
S. H. Hayakawa et al.,
Physical Review Letters, 126, 062501 (2021)

1st uniquely identified Ξ^- nuclear state

One reaction process satisfied kinematical consistency.

- $B_{\Xi^-} = 1.27 \pm 0.21 \text{ MeV}$

$\Xi^- + ^{14}\text{N} \rightarrow ^5\Lambda\text{He} + ^5\Lambda\text{He} + ^4\text{He} + n$
IRRAWADDY event



M. Yoshimoto et al., PTEP. 2021, 073D02

1st observation of nuclear s-state of Ξ^- hypernucleus

(This state maybe $^{14}\text{C} + \Xi^0$)

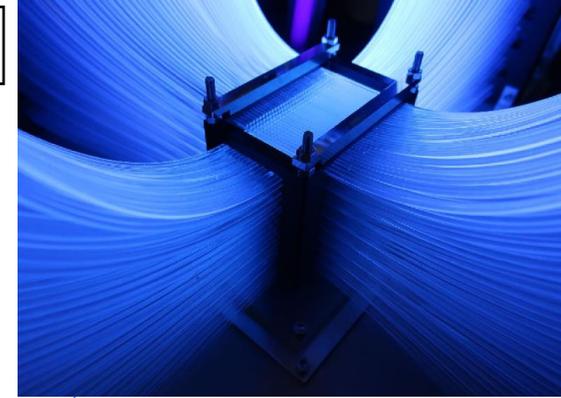
E.Friedman, A.Gal PLB837, 137640(2023)

- $B_{\Xi^-} = 6.27 \pm 0.27 \text{ MeV}$

$\Xi^- + ^{14}\text{N}$
hypernuclei

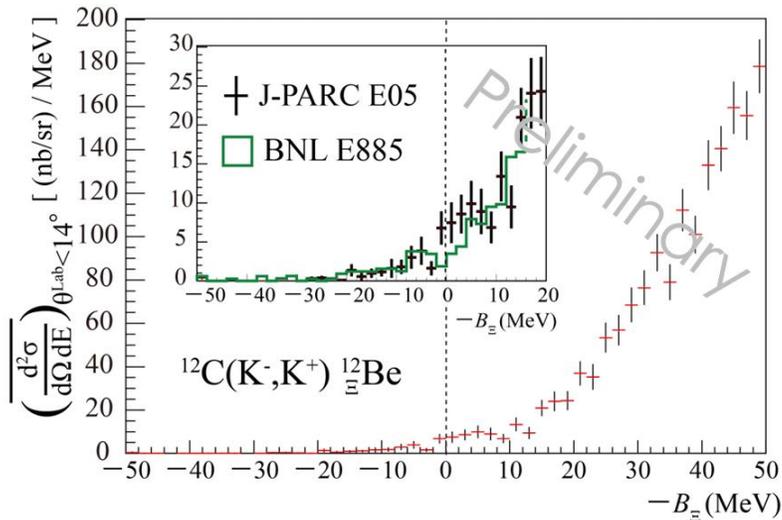
J-PARC E05(done) and E70(data taking)

AFT



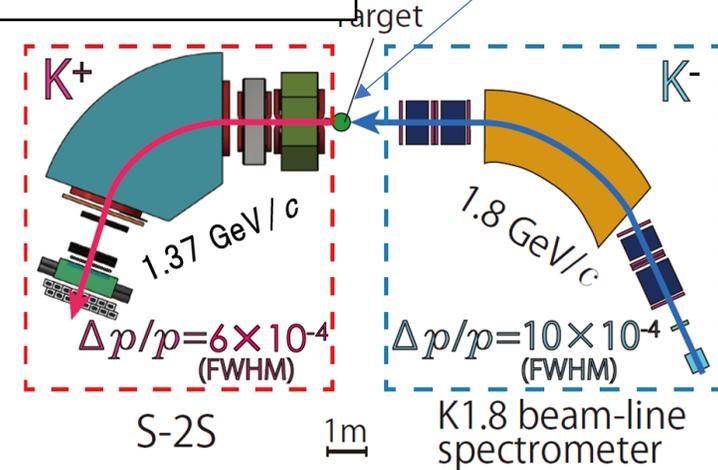
- ${}^{12}_{\Xi}\text{Be}$ via ${}^{12}\text{C}(K^-, K^+)$ reaction.
- Ξ^- nucleus search by
 - Missing mass.

J-PARC E05 results [submitted]
Events in bound region. Not clear.

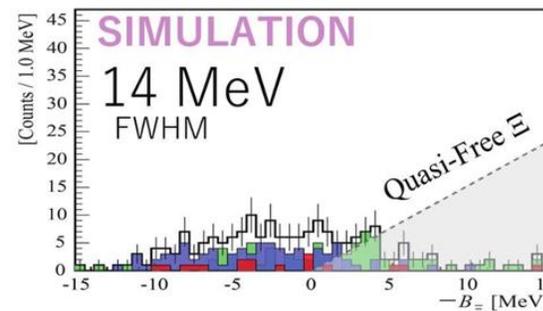


Resolution : 8 MeV (FWHM)

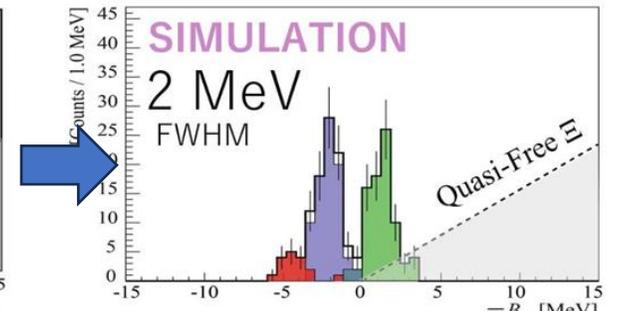
J-PARC E70: data taking.
+Spectrometer upgrade
+Active Fiber Target : Measure energy loss in target. Correction.



BNL E885 resolution



E70 resolution



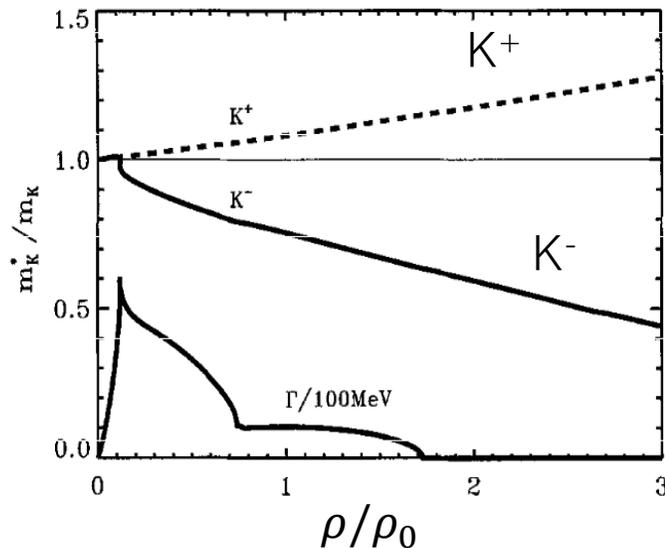
T. Gogami et al, EPJ web conf 271, 11002
($J^\pi = 1_1^-, 1_2^-, \text{ and } 1_3^-$)

K1.8BR : J-PARC E15 – $\bar{K}NN$ (“K-pp”)

A search for deeply-bound kaonic states by in-flight ${}^3\text{He}(\text{K}^-,n)$

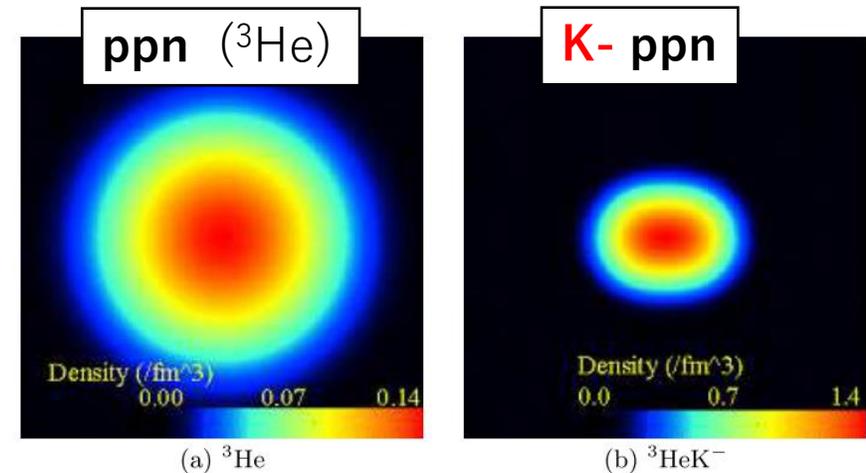
- \bar{K} : K^- and \bar{K}^0
- $\bar{K}N$ Strong attraction in $l=0$. $\Lambda(1405) = \bar{K}N$ molecule
- Larger Kaonic nucleus? $\bar{K}NN, \bar{K}NNN \dots$

SU(3) χ EFT that reproduce $\Lambda(1405)$ as Bound-state of $K^{\text{bar}}N$,
Suggests K- mass dropping in medium

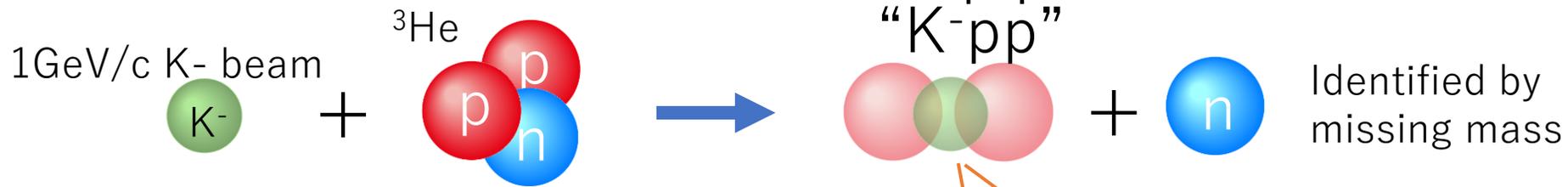


K- mass reduction in medium?

Theoretical calculation suggests shrinkage of the system. Glue like role of K.
This early study may not be realistic, but interesting thing may happen.

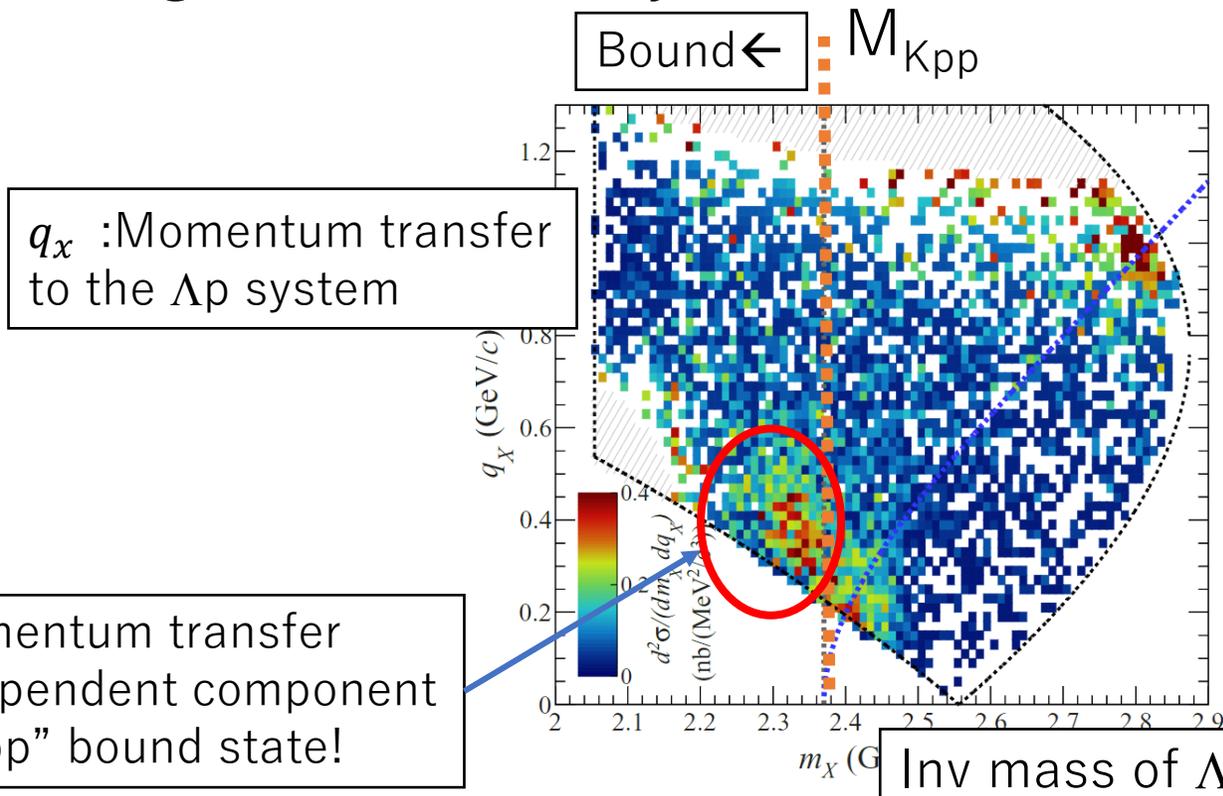


J-PARC E15 – $\bar{K}NN$ (“K-pp”)



• Exclusive analysis

- “K-pp” invariant mass.
- Missing mass to identify neutron



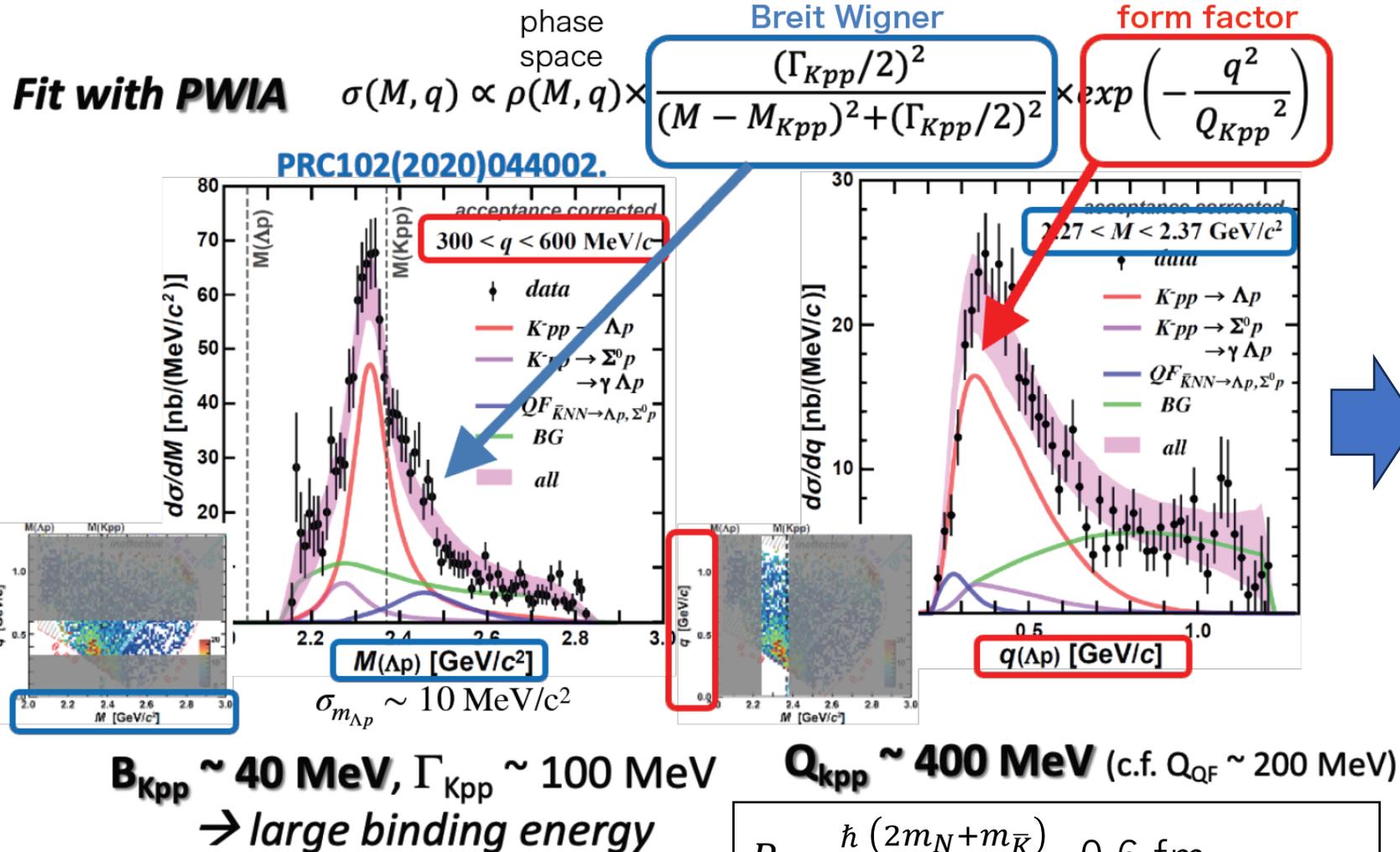
Quasi-free process.

$$M = \sqrt{4m_N^2 + m_K^2 + 4m_N \sqrt{m_K^2 + q_x^2}}$$

Momentum transfer = K^{bar} momentum

“ $\bar{K}NN$ ” model fitting

$0.3 < q_x < 0.6$ GeV/c: Signals are well separated from other process

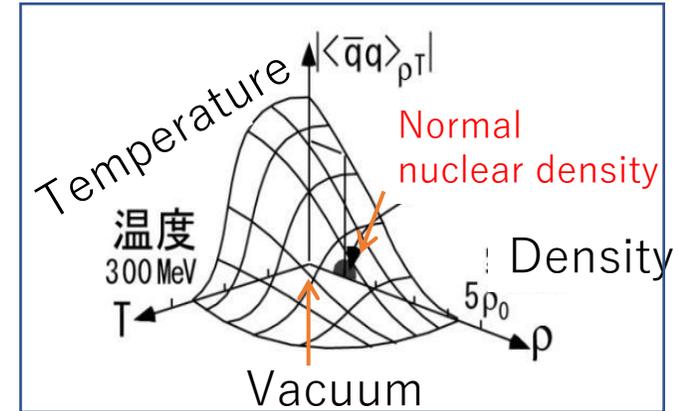


- Mesonic decay published
 - Yamaga et al. PRC110, 014002 (2024)
- Preliminary $\bar{K}NN$ results obtained. Effort continued \rightarrow J-PARC E80
- Upgrading detector.
 - x1.6 larger solid angle
 - x4 higher neutron detection eff.
 - Aim at data taking 2026.
- To study
 - $\bar{K}NN$ (J-PARC E80)
 - $\bar{K}N$ in detail.
 - Spin parity
 - Isospin partner K-pn
 - And more...

High-p : J-PARC E16 [on-going] ϕ meson in nuclei

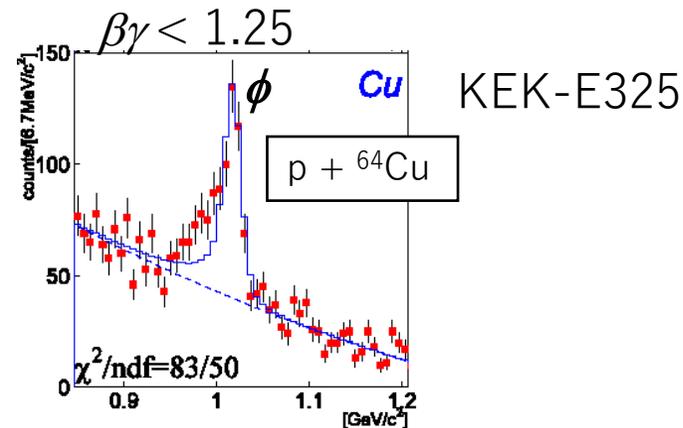
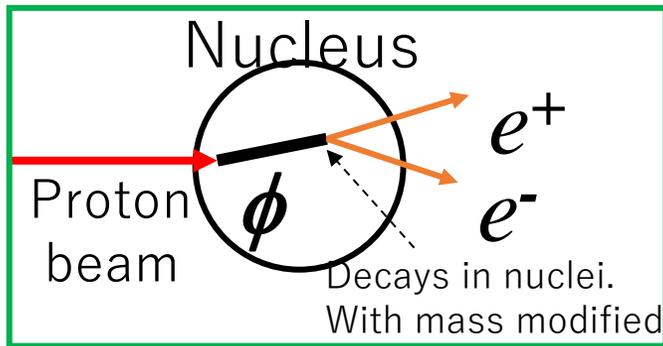
- Spontaneous breaking of chiral symmetry plays an important role in generating hadron mass.
- Chiral symmetry breaking $\langle \bar{q}q \rangle \neq 0$ depends on density.
- KEK E325
 - 12GeV $p + A \rightarrow \rho/\omega/\phi \rightarrow e^+e^-$
 - Observed what can be interpreted as an in-medium spectral change of ϕ . 3.4% mass reduction at ρ_0 .
 - Chiral symmetry restored in nuclei?

NJL model
M. Lutz et al.
Nucl. Phys. A542,52(1992)



J-PARC E16 experiment:

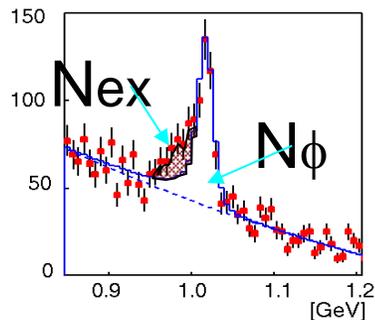
- 30GeV $p + A \rightarrow \rho/\omega/\phi \rightarrow e^+e^-$, (K^+K^- E88)
- Compared to E325, 6 times stat in 1st Run, Resolution 11 \rightarrow 6 MeV
- Spectrometer constructed for 1st physics run.
- Commissioning run finished in June 2024.
- 1st physics RUN in 2025.



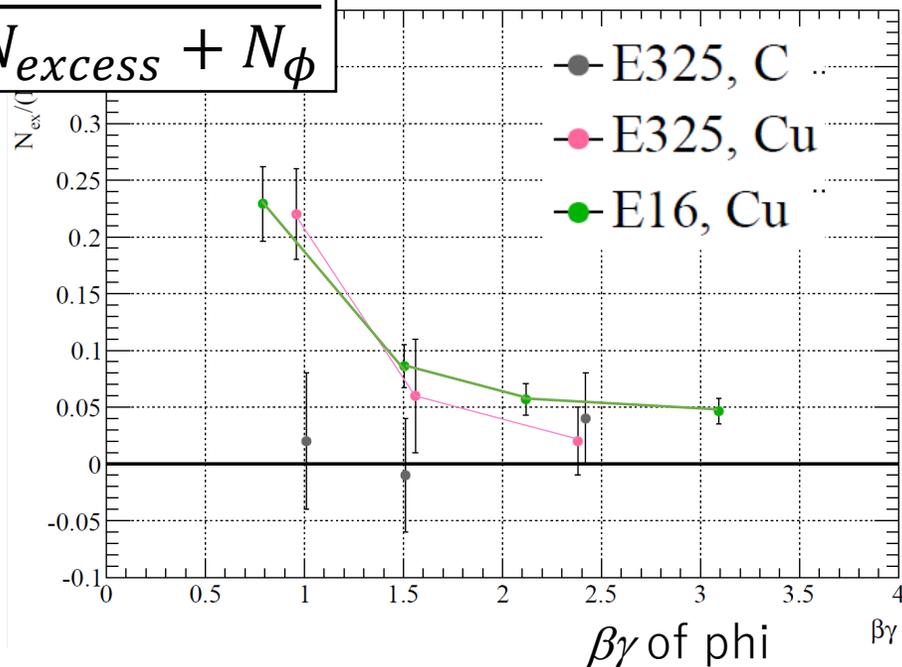
J-PARC E16

- 1st RUN expectation and beyond.

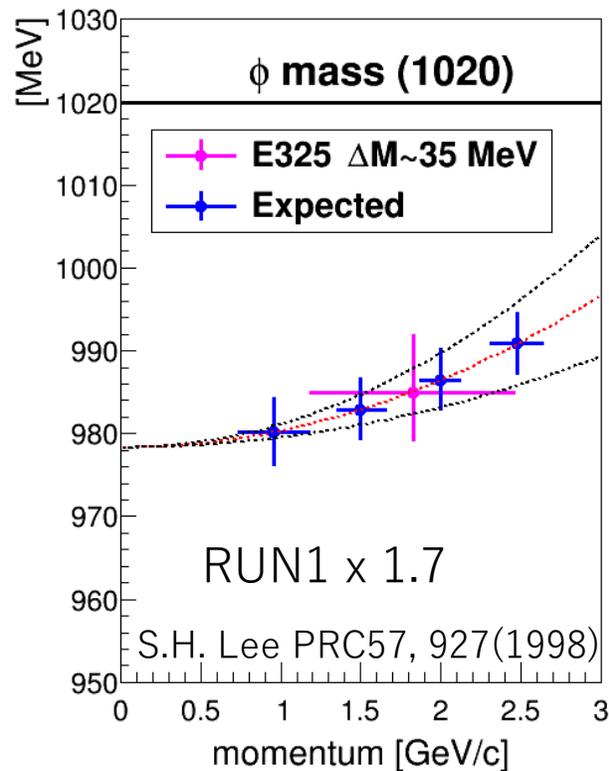
1st RUN expectation.
Clear tendency



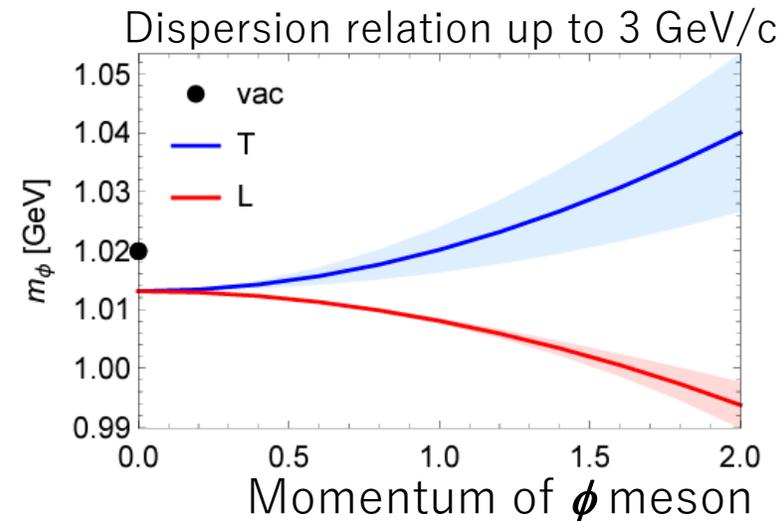
$$\frac{N_{excess}}{N_{excess} + N_{\phi}}$$



Dispersion relation can be obtained.



Polarization dependence can be accessed.

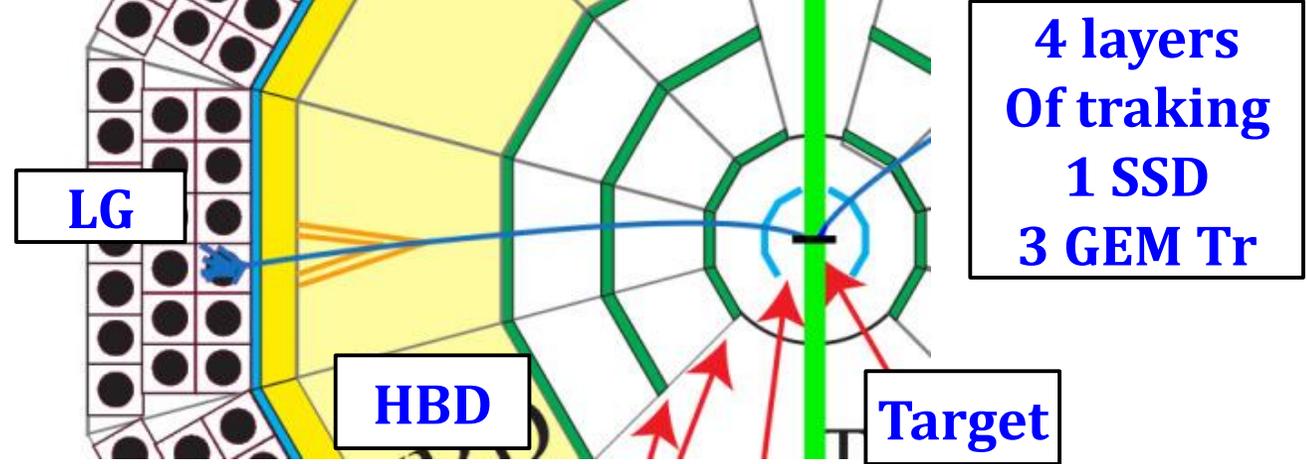


H.J. Kim, P.Gubler, PLB805, 135412 (2020)
I.W. Park et al, PRD 107, 074033 (2023)

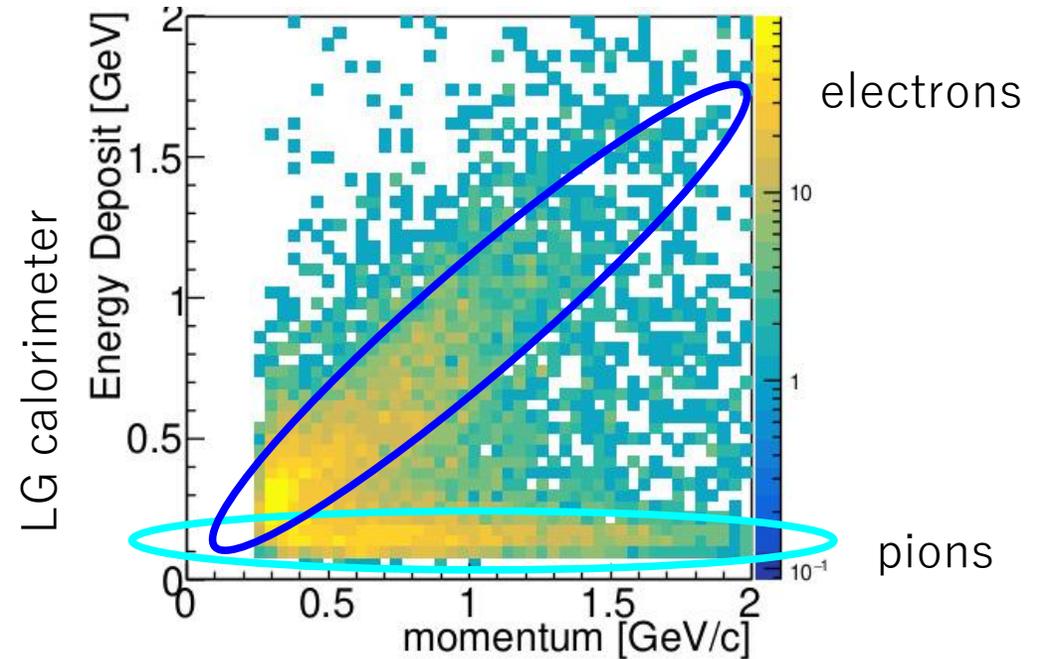
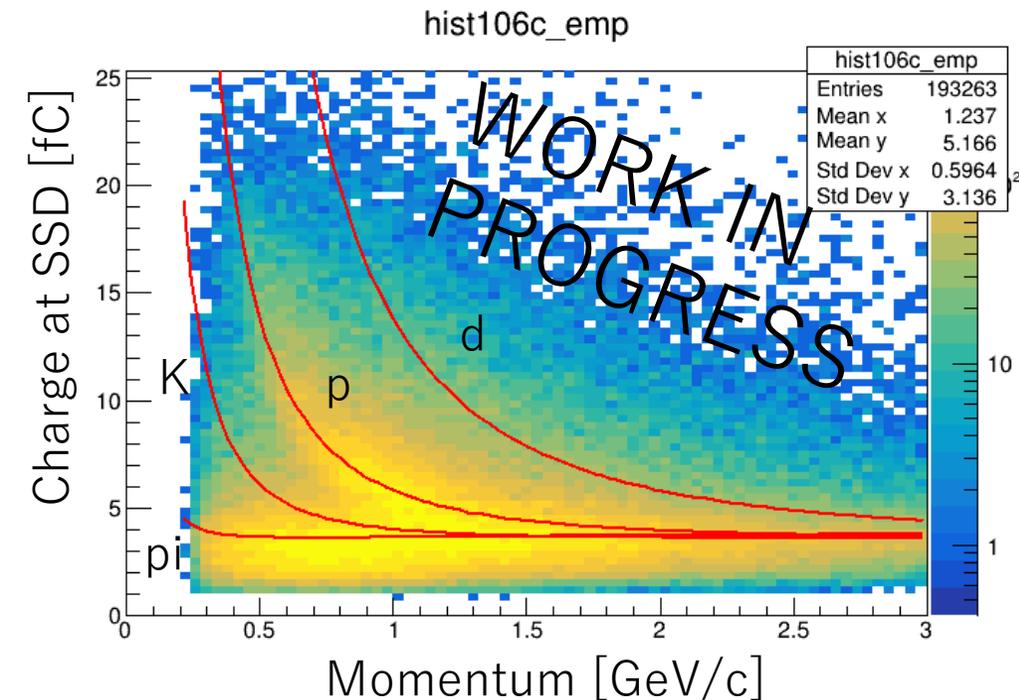
J-PARC E16

from commissioning run.

- Tracking: 1-layer of Silicon detector and 3-layers of GEM tracker.
- Silicon detector was developed in collaboration with GSI-CBM.
- Clear proton locus. SSD worked.

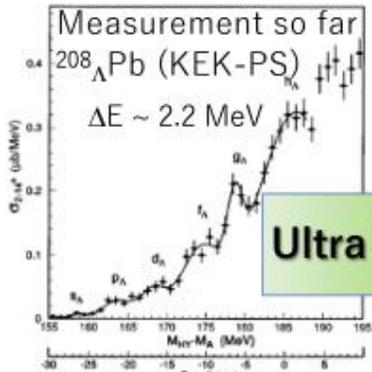


- Hadron Blind Detector (Cherenkov detector) to enhance electrons.
- Clear Momentum vs Energy (deposit on LG calorimeter) correlation of electron seen.



Hadron Hall Extension

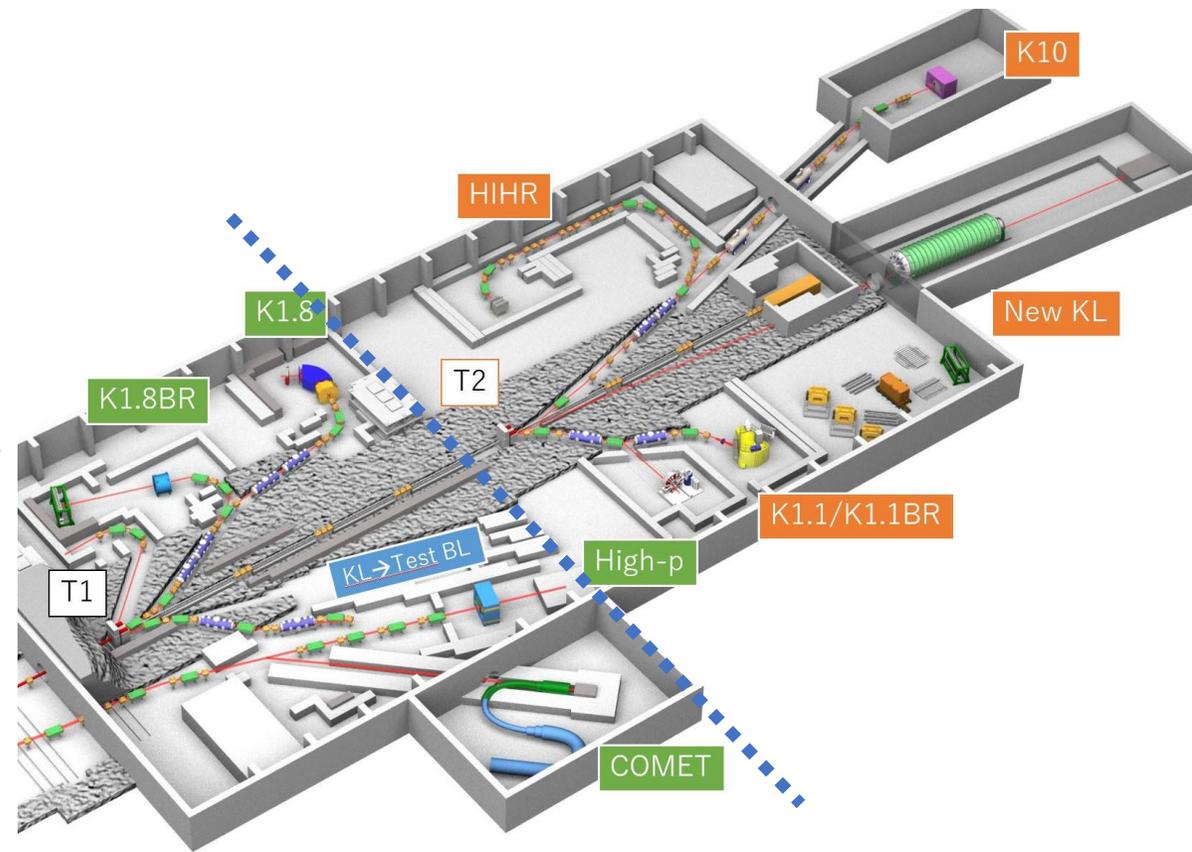
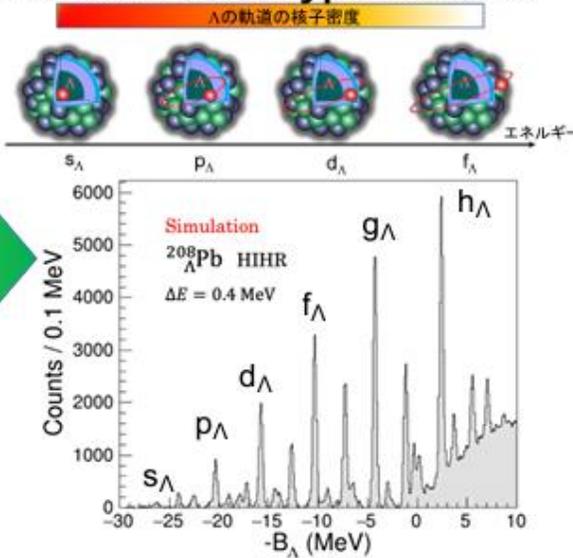
Elucidation of **YN interaction in nuclear matter**
 First high-resolution spectroscopy of the heaviest Λ hypernucleus



Ultra high-resolution

Resolution 400 keV
 (5 times better than KEK-PS)

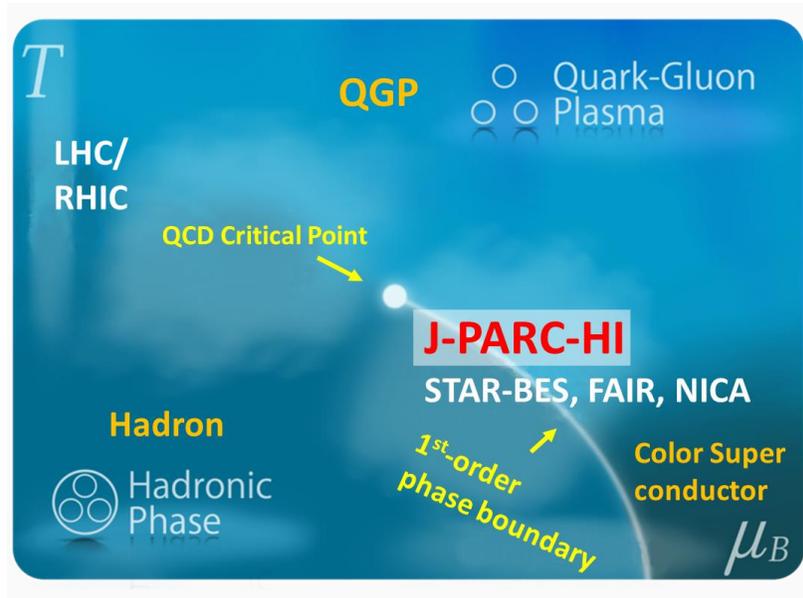
World's first high-precision spectroscopy of the heaviest Λ hypernucleus ($^{208}_{\Lambda}\text{Pb}$)



- Selected 1st priority in KEK PIP2022 (Project Implementation Plan)
- More beam lines with additional functionality
 - HIHR : High Intensity High Resolution beam by dispersion matching.
 - High precision systematic Λ hypernuclear spectroscopy up to Pb. Reveal 3BF.
 - K10 $\Omega\Xi^*$ spectroscopy, K1.1 polarized Λp scattering, New KL.

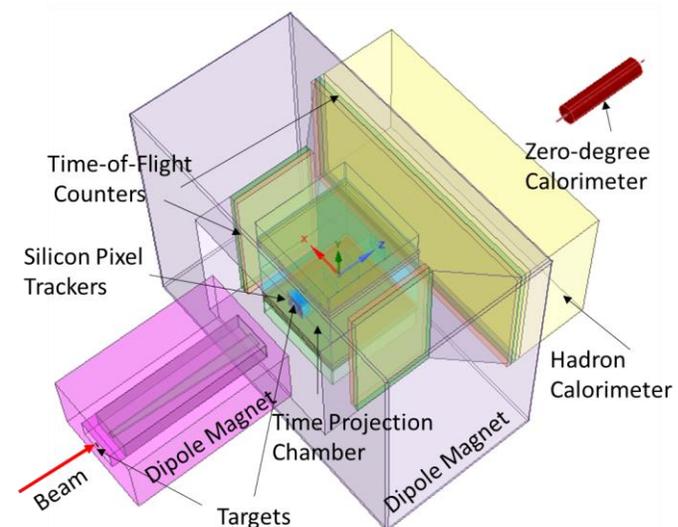
Future J-PARC Heavy Ion program

Explore the QCD phase diagram



EOS of Neutron Star
 New state of the matter
 Quark Phase
 Color Super conductivity
 Hadron physics in finite density

- Facility Upgrades Plan
 - New accelerator injector
 - New spectrometer
- Staging approach
 - Phase1:
 - Beam Intensity: 10^8 Hz for Au
 - Upgrade of the current E16 spectrometer
 - New LINAC and reuse of KEK-PS booster
 - Phase 2
 - Beam Intensity: 10^{11} Hz
 - New booster and new spectrometer



Schematic view of final spectrometer

$$E_{\text{lab}}(\text{Au}) = 1-12 \text{ AGeV}$$

$$\sqrt{s_{NN}} = 1.9-4.9 \text{ GeV}$$

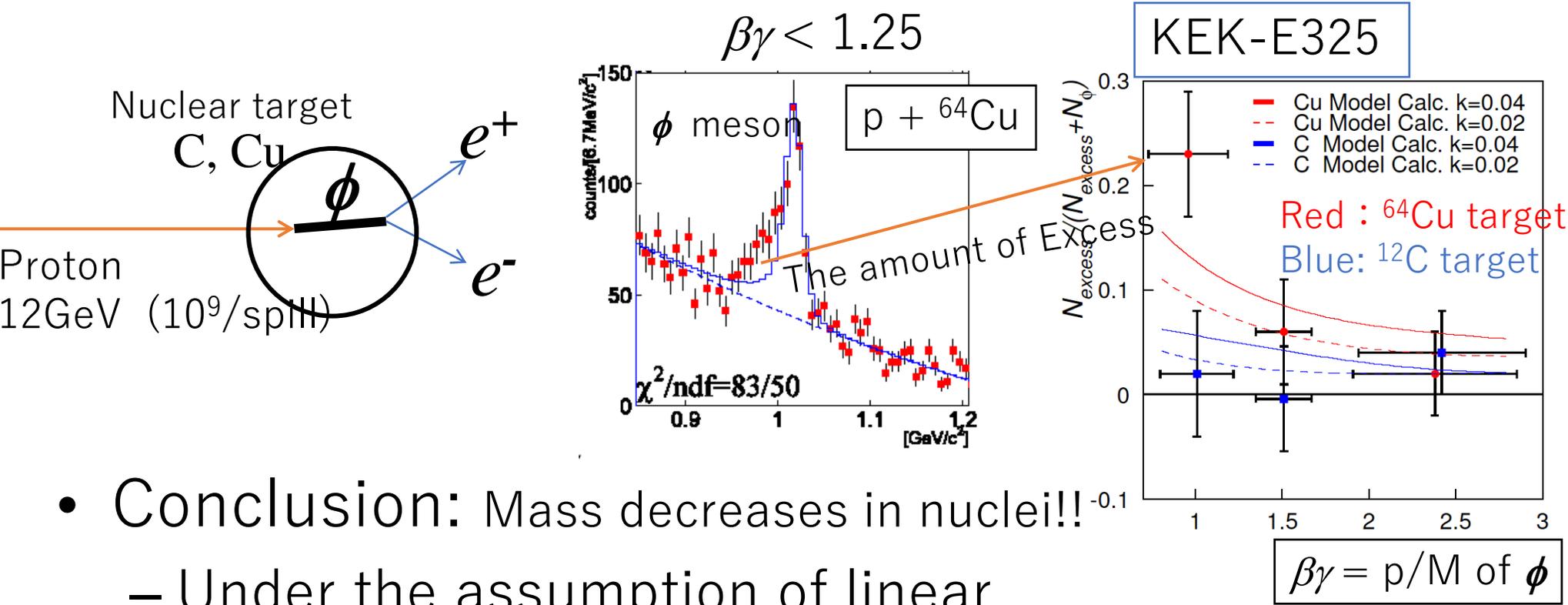
Summary

- J-PARC HD (Hadron) hosts many beam lines and various experimental programs conducted.
- Some of the experimental results and on-going efforts were introduced.
 - YN interaction by $S=-1, -2$ hypernuclear spectroscopy
 - YN interaction by YN scattering experiment.
 - Meson in nuclei, ϕ in A and $K^{\text{bar}}\text{NN}$ system and more.
- Future projects
 - Hadron Hall extension
 - J-PARC HI program

Backup slides

KEK-E325 results of ϕ meson

- The world's first results of ϕ modification.



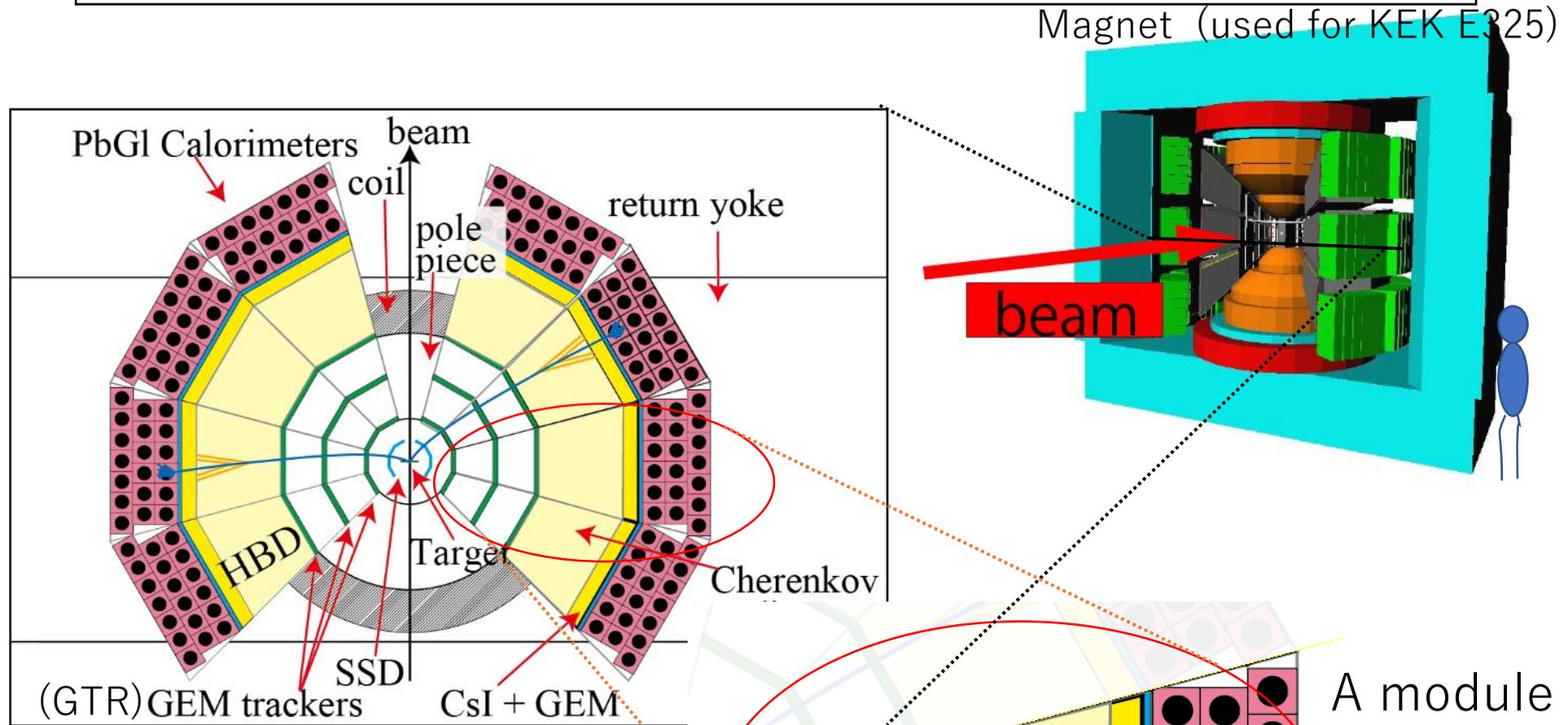
Assumption
In analysis

$$\frac{m(\rho)}{m(0)} = 1 - k_1 \left(\frac{\rho}{\rho_0} \right)$$

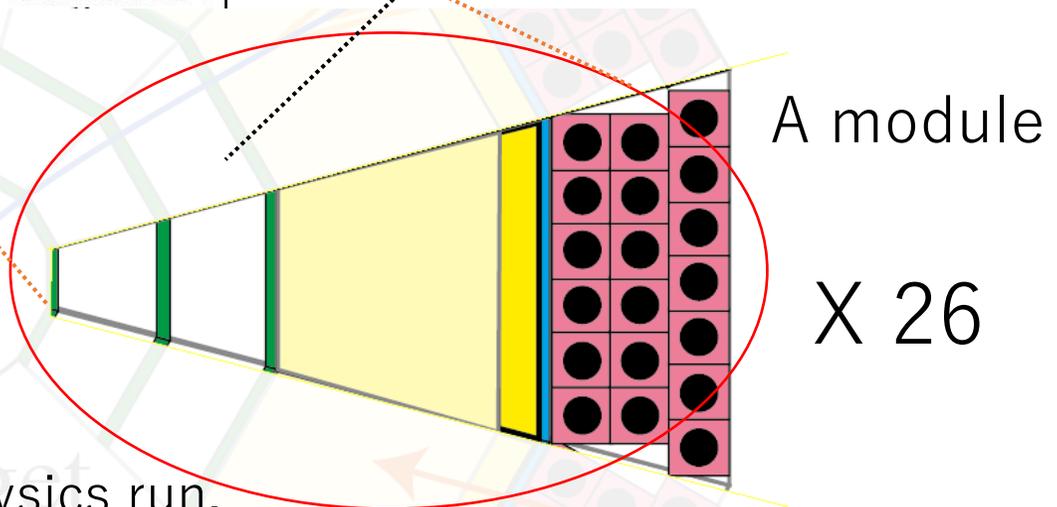
$$\frac{\Gamma(\rho)}{\Gamma(0)} = 1 + k_2 \left(\frac{\rho}{\rho_0} \right)$$

- Conclusion: Mass decreases in nuclei!!
 - Under the assumption of linear dependence of mass and width on density.
 - Mass: $-3.4^{+0.6}_{-0.7}\%$ ↓ At normal nuclear density
 - Width: $\times 3.6^{+1.8}_{-1.2}$

The J-PARC E16 spectrometer



SSD : Tracking
GTR : Tracking
HBD : eID (Cherenkov)
LG : eID (Calorimeter)
26 modules in total. 8 for the 1st physics run.



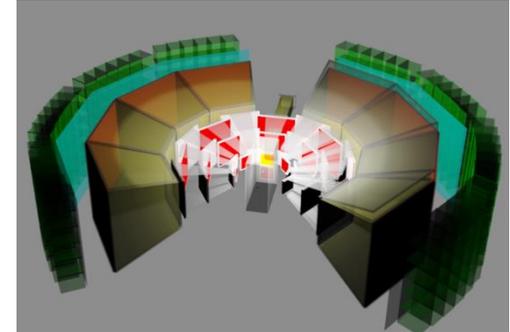
Staging approach

- **RUN 0a/b/c/d - 2020,2021,2023** – 413hrs.
 - **10 (SSD) + 8 (GTR) + 8 (HBD) + 8 (LG)** at last
 - Gradually increased acceptance and reached interm. Goal.
 - C+Cu targets
 - Beam / Detector commissioning
- **RUN 0e - 2024 (Apr.19-Jun.3) -- 206 hours.**
 - **8(SSD) + 10 (GTR) + 8 (HBD) + 8 (LG)**
 - Beam / Detector comm. + yield.
 - Upgraded Accelerator / DAQ. / Detectors.

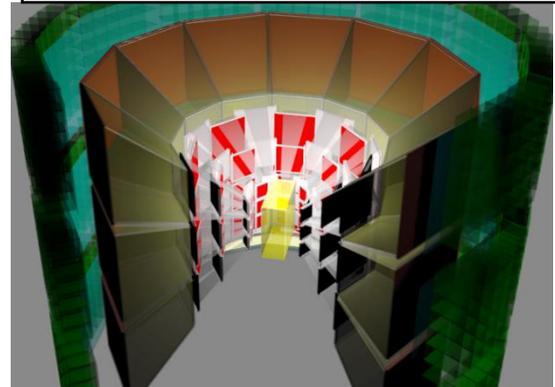
- **RUN 1 2025(?)** -- 1280hrs (~53days)
 - **10 (SSD) + 10 (GTR) + 8 (HBD) + 8(LG)**
 - Physics data taking. ϕ : 15k for Cu.
 - Needs PAC approval based on comm. Runs.
- **RUN 2** -- 2560 hrs (~107 days)
 - **26 (SSD) + 26 (GTR) + 26 (HBD) + 26 (LG)**
 - + Pb/CH2 target
 - Needs additional budget.

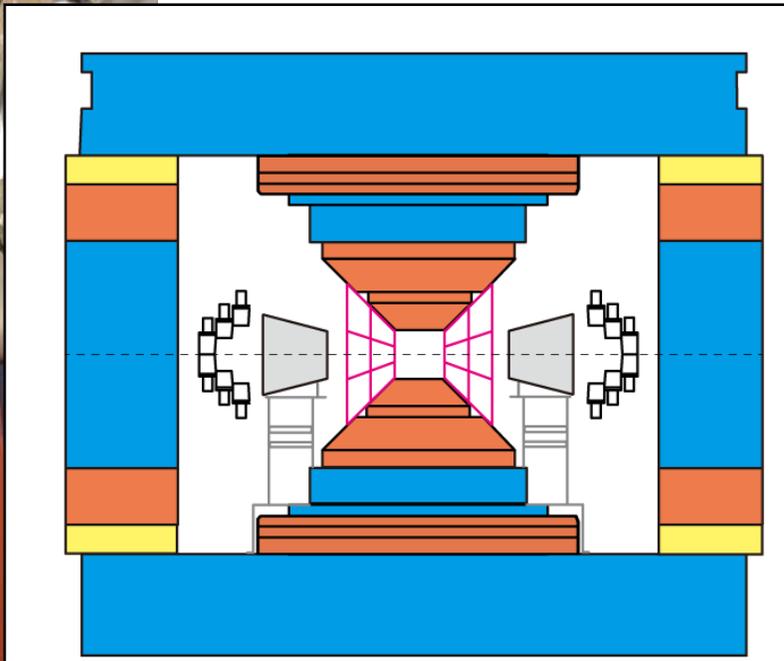
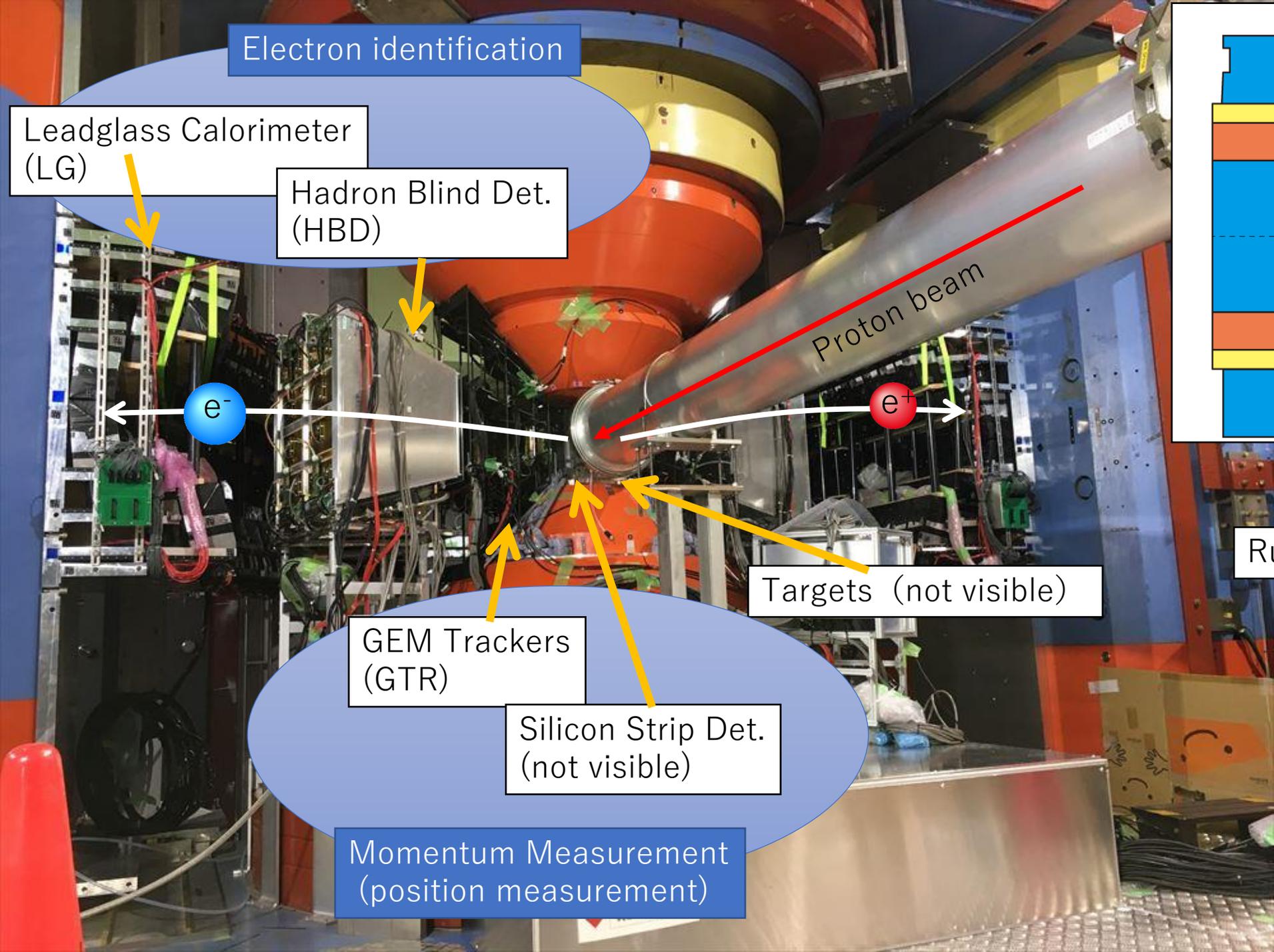
↑
PAC
Executed!
Approved!

RUN 1 (8 modules)



RUN 2 (26 modules)

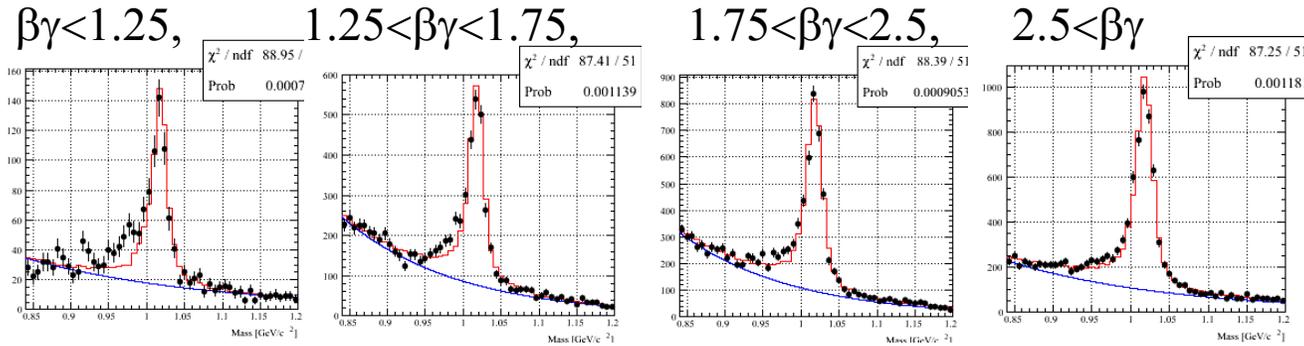




Run0b/c configuration(2021)

RUN1, Cu (INPUT:E325-BW)

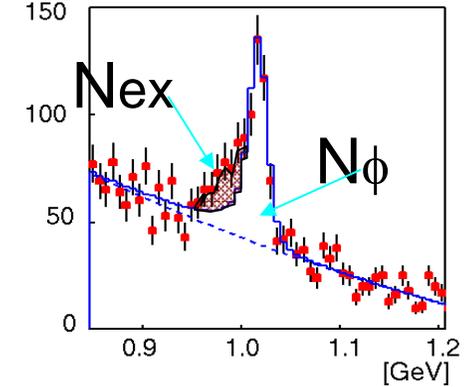
Excess ratio vs $\beta\gamma$



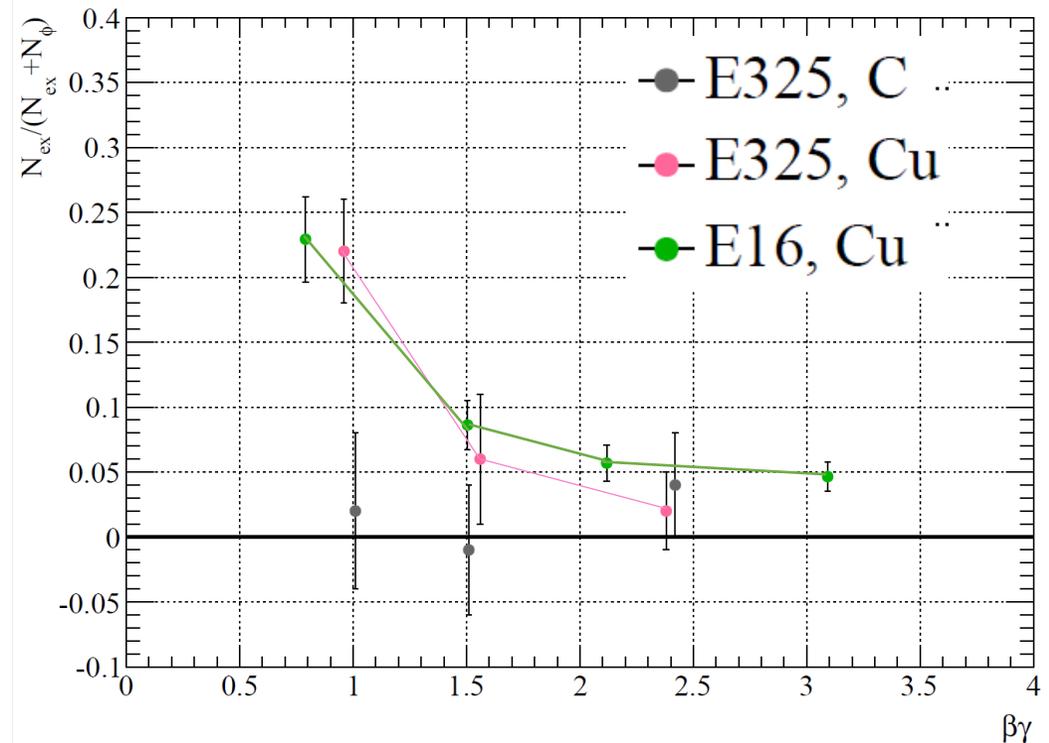
(Fit fails when vacuum shapes are used.)

- $\sim 15\text{k } \phi$ for Cu target expected in RUN1
- All $\beta\gamma$ bins for Cu are significant in E16
- (cf) E325 only fastest $\beta\gamma$ bin is significant.

- Larger excess in lower $\beta\gamma$ bin.
- The tendency becomes clearer and more significant compared to E325.



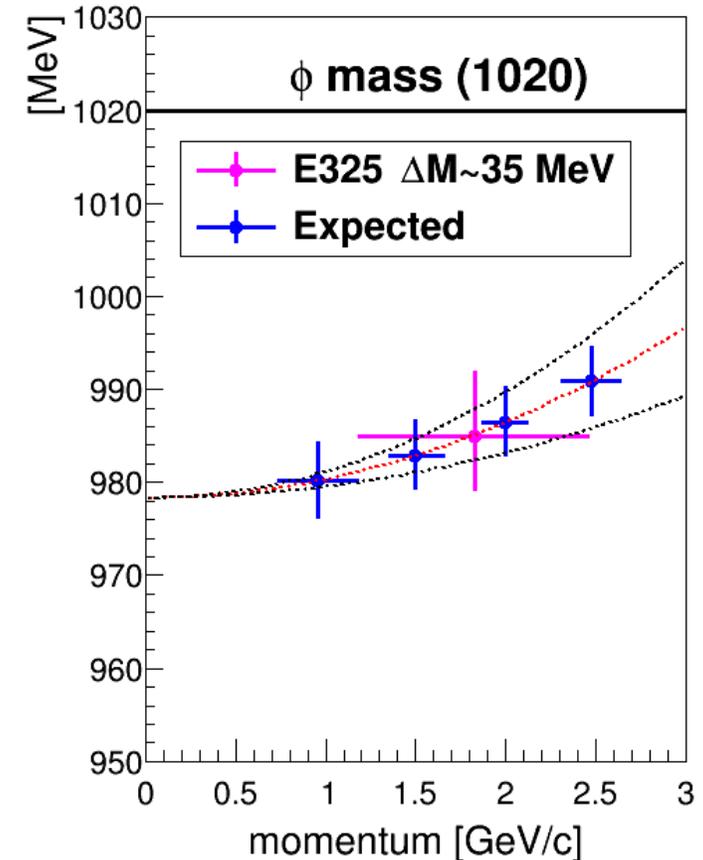
$$\frac{N_{excess}}{N_{excess} + N_{\phi}}$$



Momentum dependence (Dispersion relation)

- Momentum dependence of mass can be obtained for the first time.
- Expectation of $RUN1 \times 1.7$ is shown.
- Dispersion relation itself is an important property of pseudo particles.
- We can extrapolate mass into 0 momentum, where most of the QCDSR calculation results apply.
- More discussion on later slides.

H.Kim P. Gubler PLB805, 10 (2020) extends the validity of momentum range.
Show you on later slides.

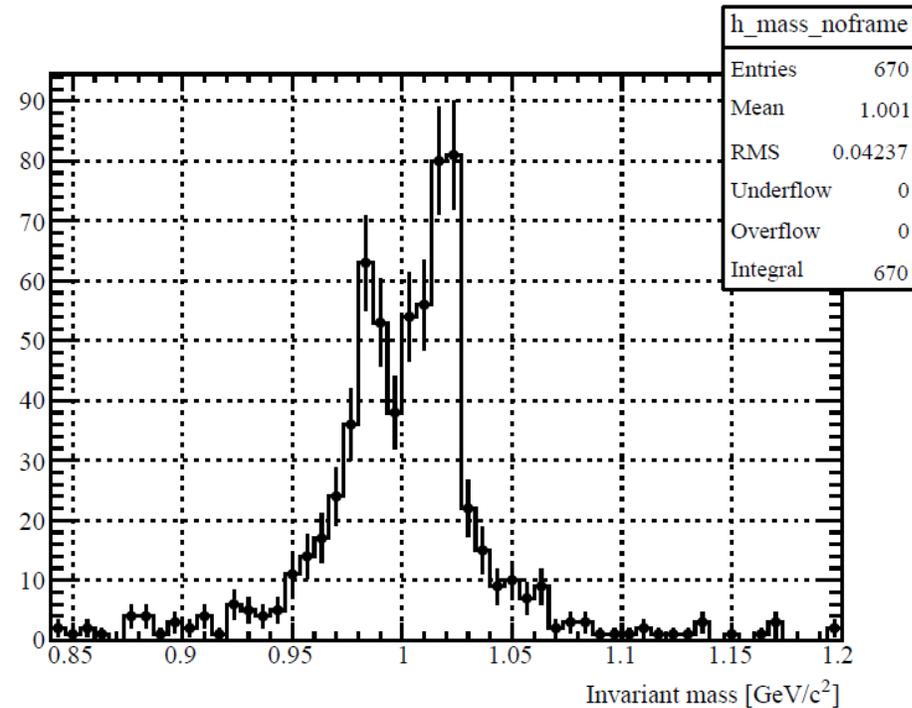


S.H. Lee PRC57, 927(1998)

Expected in RUN2

- RUN2 stat (320shifts)
- INPUT: E325-BW

- Pb target
- $\beta\gamma < 0.5$



BB interaction flavor SU(3)

- $8 \times 8 =$
 $27 +$ (NN world.)
 $10^* +$ (NN world.)

 $10 +$ (appears ΣN $I=3/2$)
 $8_s +$ (Pauli forbidden)
 $8_a +$
 1

•

Table 2. SU(3) content of the different interaction channels with total strangeness S and isospin I . The upper half refers to the space-spin symmetric states ${}^3S_1, {}^1P_1, {}^3D, \dots$, and the lower half to the space-spin antisymmetric states ${}^1S_0, {}^3P, {}^1D_2, \dots$.

S	I	Channels	SU(3)-irreps
Space-spin symmetric			
0	0	NN	$\{10^*\}$
-1	1/2	$\Lambda N, \Sigma N$	$\{10^*\}, \{8\}_a$
	3/2	ΣN	$\{10\}$
-2	0	$N\Xi$	$\{8\}_a$
	1	$N\Xi, \Sigma\Sigma$ $\Sigma\Lambda$	$\{10\}, \{10^*\}, \{8\}_a$ $\{10\}, \{10^*\}$
Space-spin antisymmetric			
0	1	NN	$\{27\}$
-1	1/2	$\Lambda N, \Sigma N$	$\{27\}, \{8\}_s$
	3/2	ΣN	$\{27\}$
-2	0	$\Lambda\Lambda, N\Xi, \Sigma\Sigma$	$\{27\}, \{8\}_s, \{1\}$
	1	$N\Xi, \Sigma\Lambda$	$\{27\}, \{8\}_s$
	2	$\Sigma\Sigma$	$\{27\}$

BB interaction in flavor SU(3)

- $8 \times 8 = 27 + 10 + 10^* + 8s + 8a + 1$

S	BB(I)	Symmetric	Anti-symmetric
0	$NN(I = 0)$	----	$[10^*]$
	$NN(I = 1)$	$[27]$	----
-1	ΛN	$\frac{1}{\sqrt{10}} ([8s] + 3[27])$	$\frac{1}{\sqrt{2}} (-[8a] + [10^*])$
	$\Sigma N(I = 1/2)$	$\frac{1}{\sqrt{10}} (3[8s] - [27])$	$\frac{1}{\sqrt{2}} ([8a] + [10^*])$
	$\Sigma N(I = 3/2)$	$[27]$	$[10]$
-2	$\Lambda\Lambda$	$\frac{1}{\sqrt{5}} ([8s] + \frac{9}{2\sqrt{30}} [27] + \frac{1}{2\sqrt{2}} [1])$	----
	$\Xi N(I = 0)$	$\frac{1}{\sqrt{5}} ([8s] - \frac{\sqrt{3}}{\sqrt{10}} [27] + \frac{1}{\sqrt{2}} [1])$	$[8a]$
	$\Xi N(I = 1)$	$\frac{\sqrt{3}}{\sqrt{5}} [8s] + \frac{\sqrt{2}}{\sqrt{5}} [27]$	$\frac{1}{\sqrt{3}} (-[8a] + [10] + [10^*])$
	$\Sigma\Lambda$	$-\frac{\sqrt{2}}{\sqrt{5}} [8s] + \frac{\sqrt{3}}{\sqrt{5}} [27]$	$\frac{1}{\sqrt{2}} ([10] - [10^*])$
	$\Sigma\Sigma(I = 0)$	$\frac{\sqrt{3}}{\sqrt{5}} [8s] - \frac{1}{2\sqrt{10}} [27] - \frac{\sqrt{3}}{\sqrt{8}} [1]$	---
	$\Sigma\Sigma(I = 1)$	---	$\frac{1}{\sqrt{6}} (2[8a] + [10] + [10^*])$
	$\Sigma\Sigma(I = 2)$	$[27]$	---

Table based on PRC64, 054001 (2001)

Many theoretical calculation agrees with existence of $K^{\text{bar}}\text{NN}$, but results scattered.

AY: PRC65(2002)044005, PLB535(2002)70.
WG: PRC79(2009)014001.
BGL: PLB712(2012)132.
OHHMH: PRC95(2017)065202.
Kanada: EPLA57(2021)185.

