

Charged particle multiplicity in pp-collisions from the dilute Glasma

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August 21, 2024

Based on
A. Ipp, M. Leuthner, D. I. Müller, S. Schlichting, K. Schmidt and P. Singh,
Energy-momentum tensor of the dilute (3+1)D Glasma
Phys.Rev.D 109 (2024) 9, 094040
and subsequent work

XVIth Quark Confinement and the Hadron Spectrum Conference
Track D: Deconfinement
Cairns, Queensland, Australia



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Charged particle mu from the c



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Singh,

XVIth Quark Con





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FWF Österreichischer
Wissenschaftsfonds

$\int dk \Pi$
Doktoratskolleg
Particles and Interactions

Charged particle multiplicity in pp-collisions from the dilute Glasma

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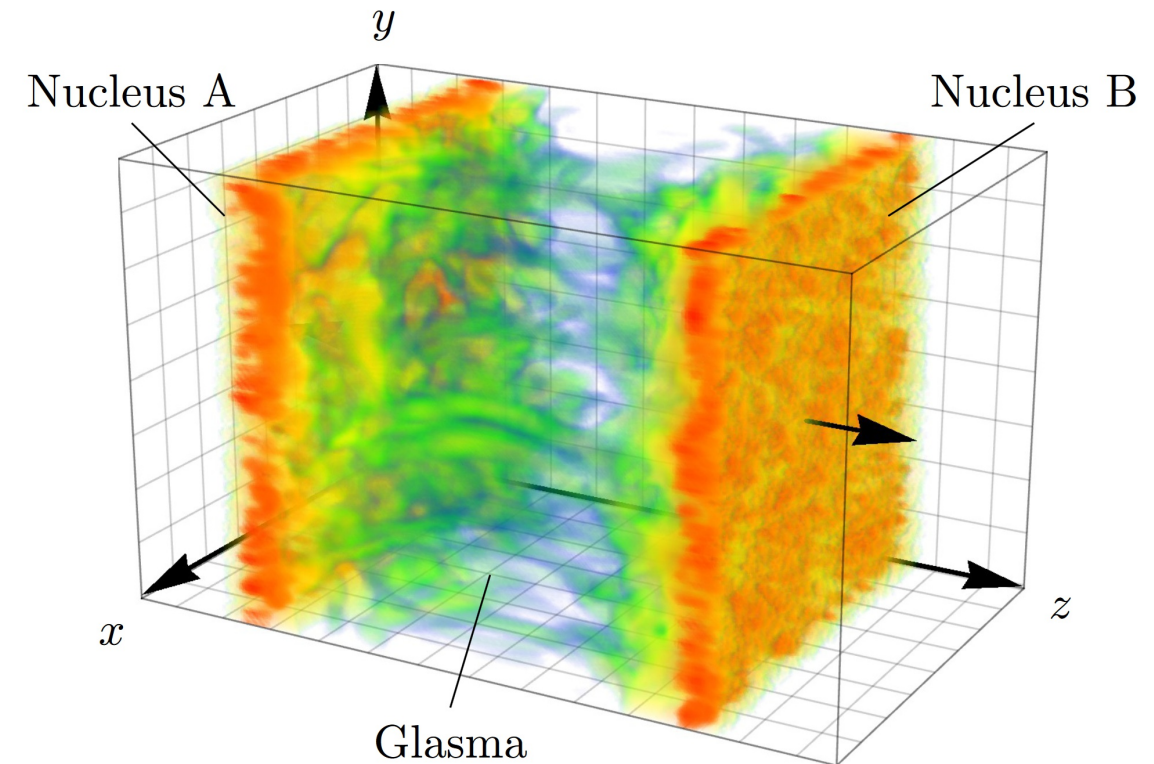
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The Glasma

- ...is mostly discussed in the context of HIC
- ...is something between a glass (CGC) and a plasma (QGP)

therefore

- ...is the precursor to the **quark-gluon plasma**
- ...is a classical state characterized by large gluon occupation numbers
- ...provides initial conditions for hydro simulations of the QGP



A. Ipp, D. I. Müller, Phys. Lett. B771 (2017) 74–79

Color glass condensate

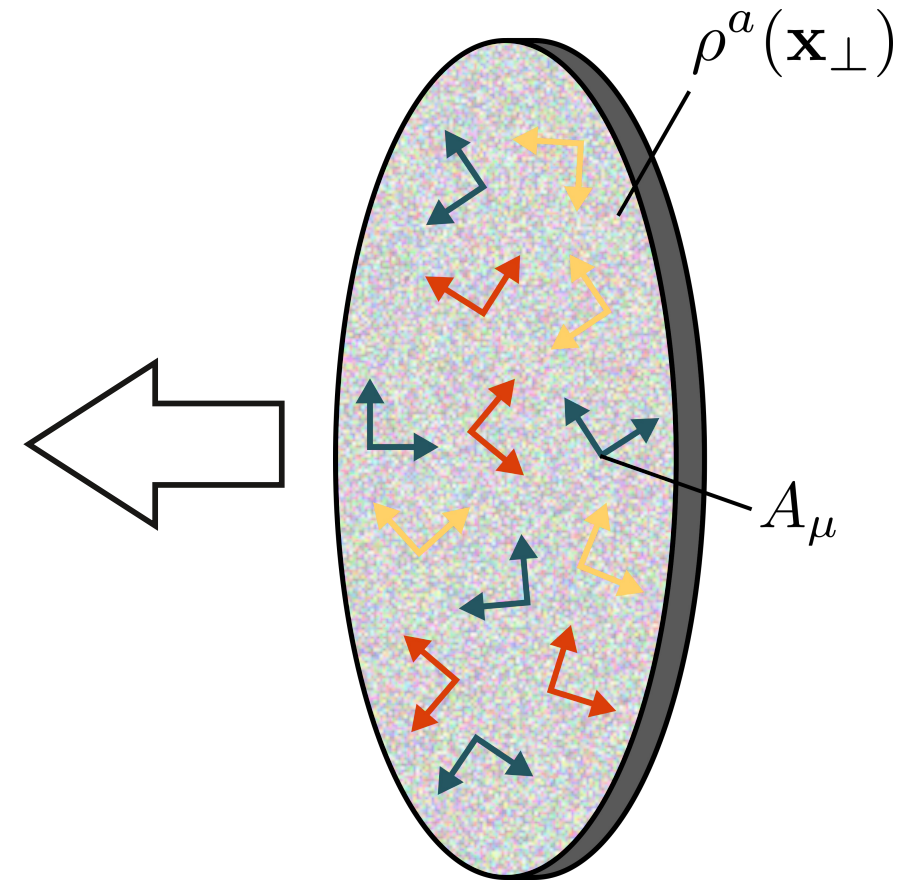
Effective theory for high energy QCD

Separation of scales into

- Hard partons – color charges ρ
- Soft partons – gauge field A_μ

Moving ρ leads to current J

$$D_\mu F^{\mu\nu} = J^\nu$$



Color glass condensate

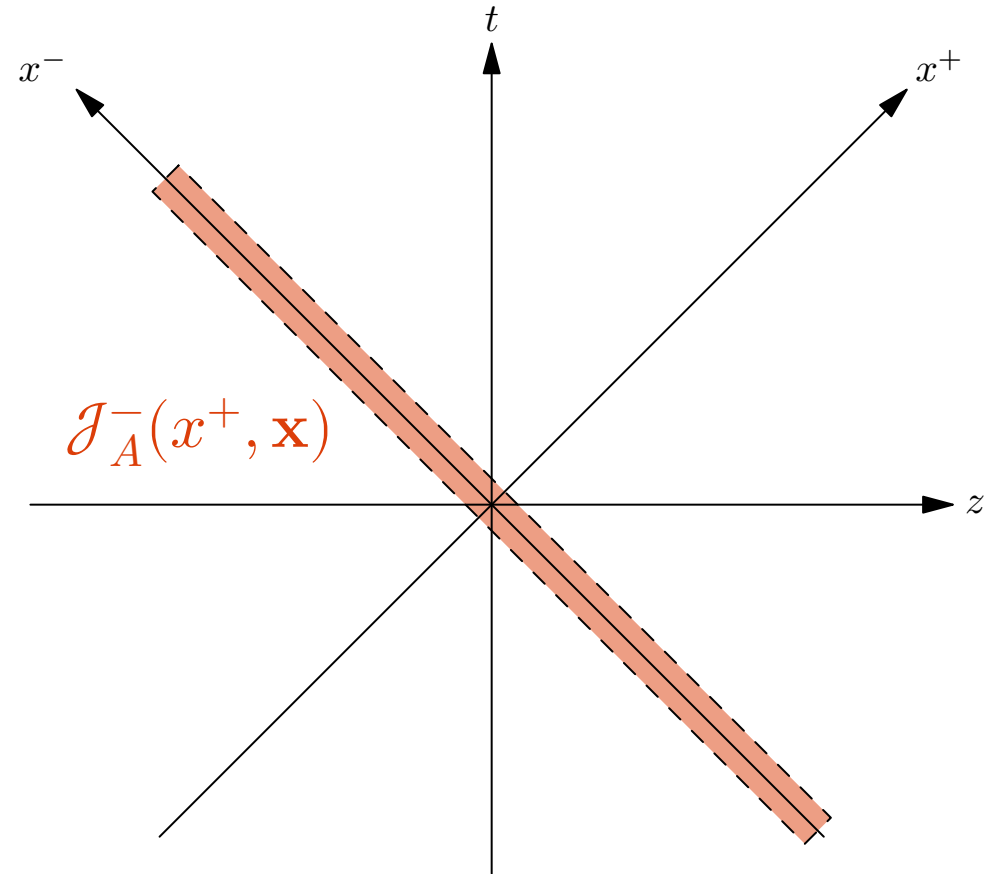
Consider nucleus A moving to the left

Color current \mathcal{J}_A^- is a stochastic variable

Classical Yang-Mills equations $\mathcal{D}_\mu \mathcal{F}^{\mu\nu} = \mathcal{J}^\nu$

in covariant gauge $\partial_\mu \mathcal{A}_A^\mu = 0$ gives gauge field \mathcal{A}_A via

$$-\Delta_\perp \mathcal{A}_A^-(x^+, \mathbf{x}) = \mathcal{J}_A^-(x^+, \mathbf{x})$$



Color glass condensate

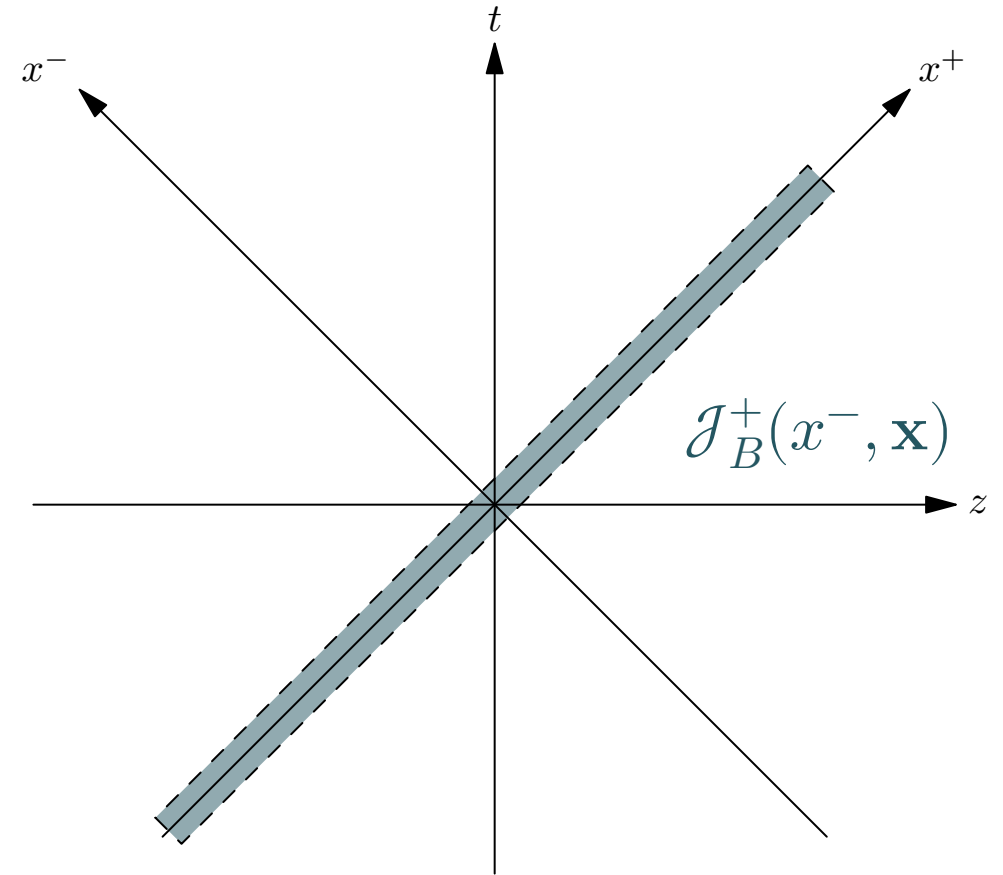
Consider nucleus B moving to the right

Color current \mathcal{J}_B^+ is a stochastic variable

Classical Yang-Mills equations $\mathcal{D}_\mu \mathcal{F}^{\mu\nu} = \mathcal{J}^\nu$

in covariant gauge $\partial_\mu \mathcal{A}_B^\mu = 0$ gives gauge field \mathcal{A}_B via

$$-\Delta_\perp \mathcal{A}_B^+(x^-, \mathbf{x}) = \mathcal{J}_B^+(x^-, \mathbf{x})$$



Color glass condensate

In **forward lightcone** full Yang-Mills equations

$$D_\mu F^{\mu\nu} = J^\nu$$

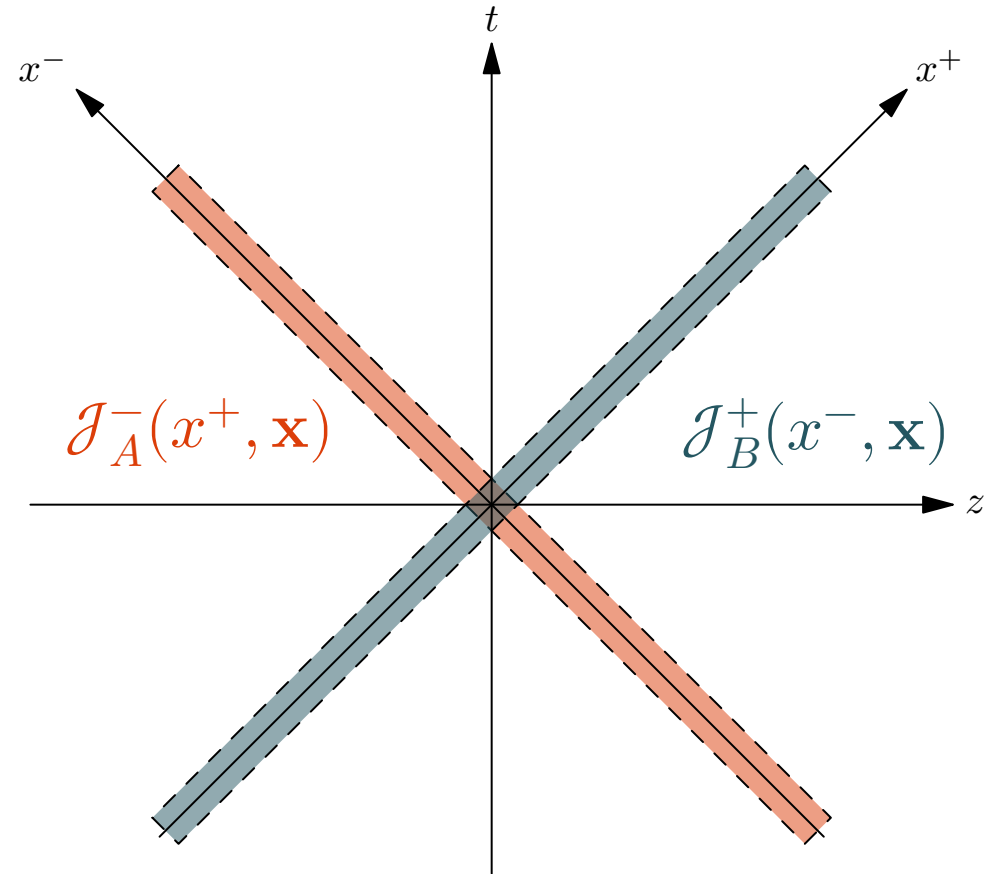
with

$$A^\mu(x) = \mathcal{A}_A^\mu(x) + \mathcal{A}_B^\mu(x) + a^\mu(x),$$

$$J^\mu(x) = \mathcal{J}_A^\mu(x) + \mathcal{J}_B^\mu(x) + j^\mu(x)$$

must hold. Also,

$$D_\mu J^\mu = 0.$$



Color glass condensate

In **forward lightcone** full Yang-Mills equations

$$D_\mu F^{\mu\nu} = J^\nu$$

with

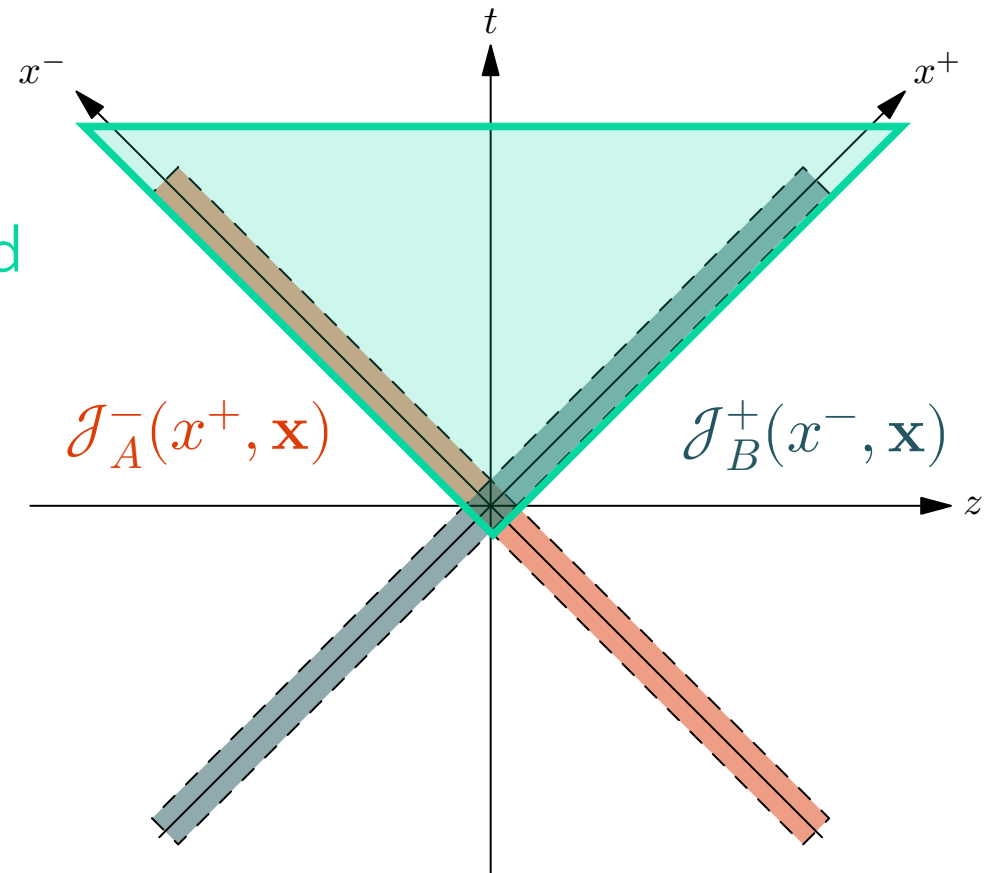
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Glasma field



Color glass condensate

In **forward lightcone** full Yang-Mills equations

$$D_\mu F^{\mu\nu} = J^\nu$$

with

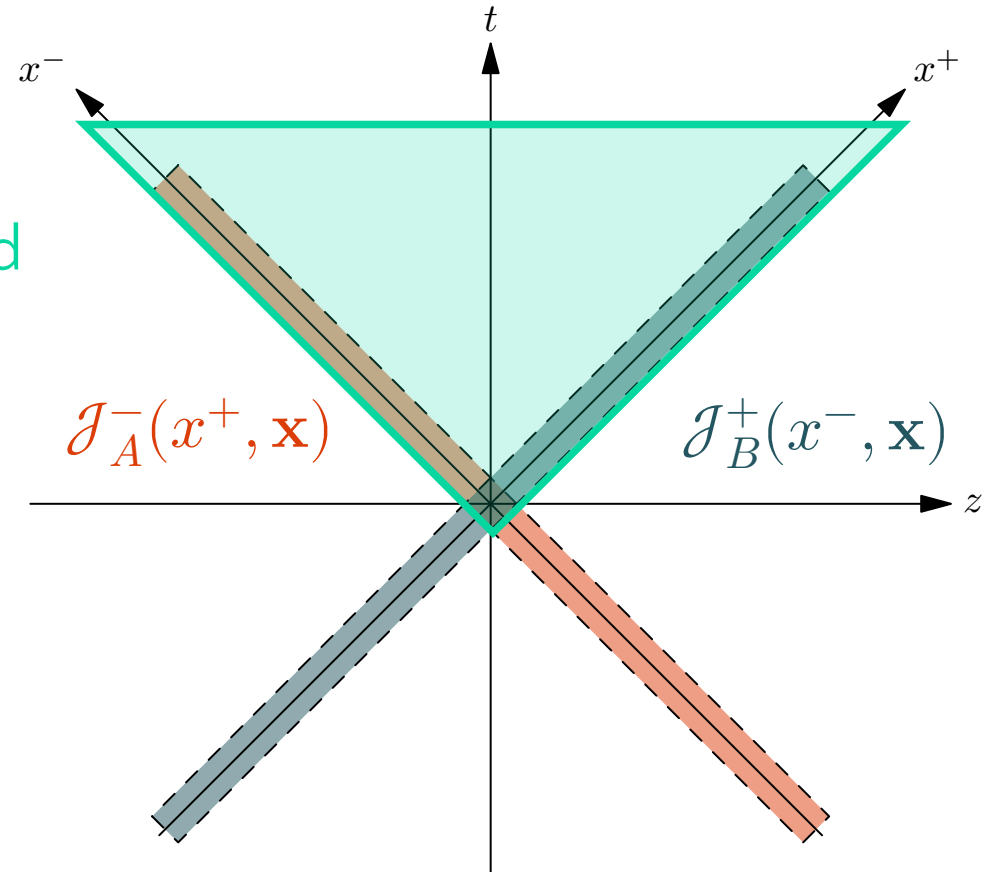
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$$J^\mu(x) = \mathcal{J}_A^\mu(x) + \mathcal{J}_B^\mu(x) + j^\mu(x)$$

must hold.

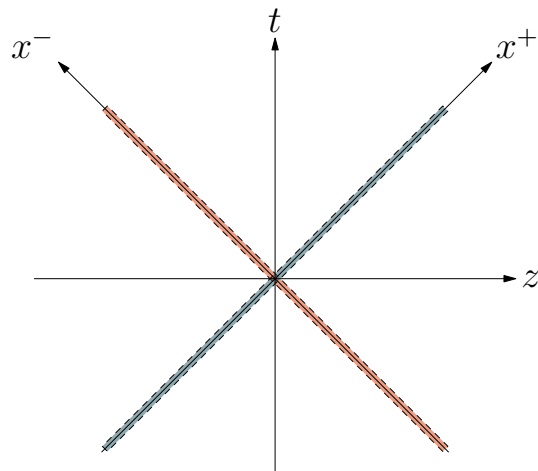
No analytic solution for this system!

Glasma field



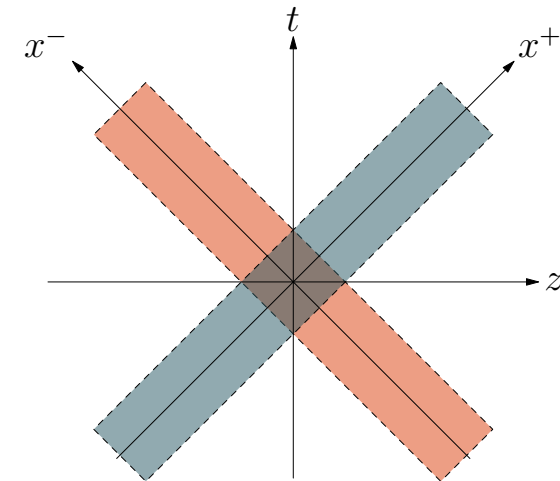
Breaking boost-invariance

2D nuclei
infinitely Lorentz-contracted



no info about rapidity dependence
of observables (**boost-invariance**)

3D nuclei
with longitudinal extent



gives rapidity profile of observables

Dilute approximation

In **forward lightcone** full Yang-Mills equations

$$D_\mu F^{\mu\nu} = J^\nu$$

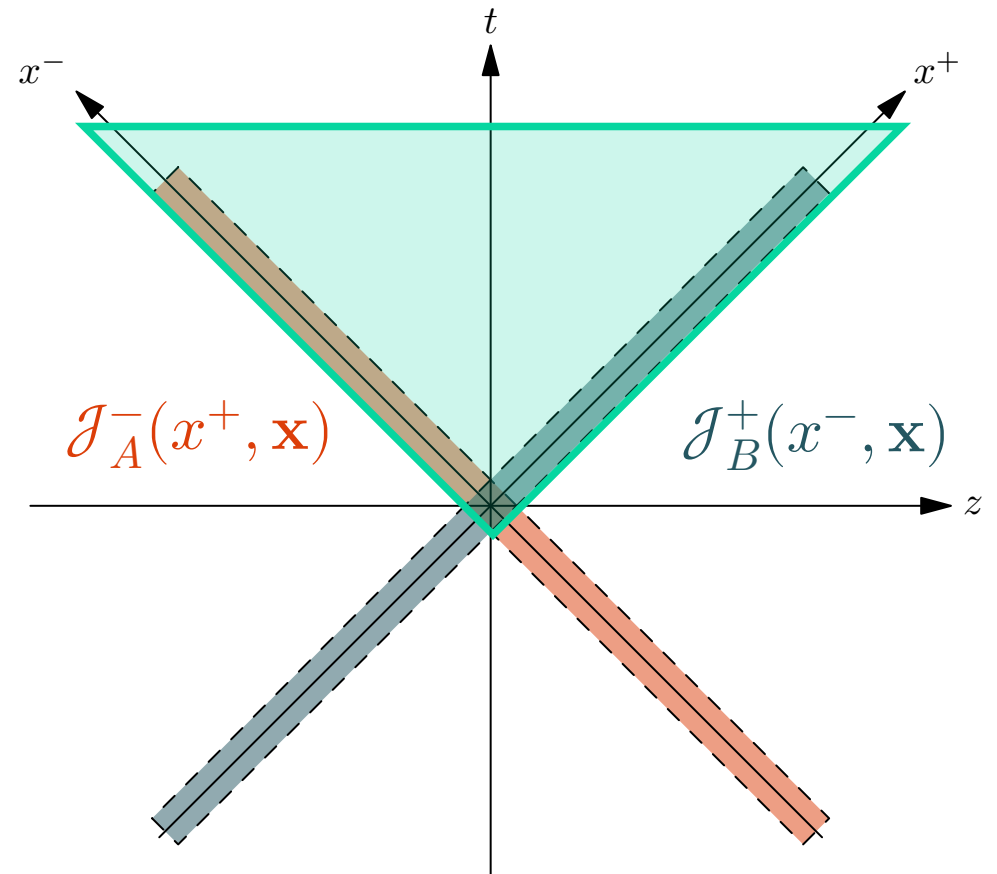
with

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$$J^\mu(x) = \mathcal{J}_A^\mu(x) + \mathcal{J}_B^\mu(x) + j^\mu(x)$$

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Dilute approximation

In **forward lightcone** full Yang-Mills equations

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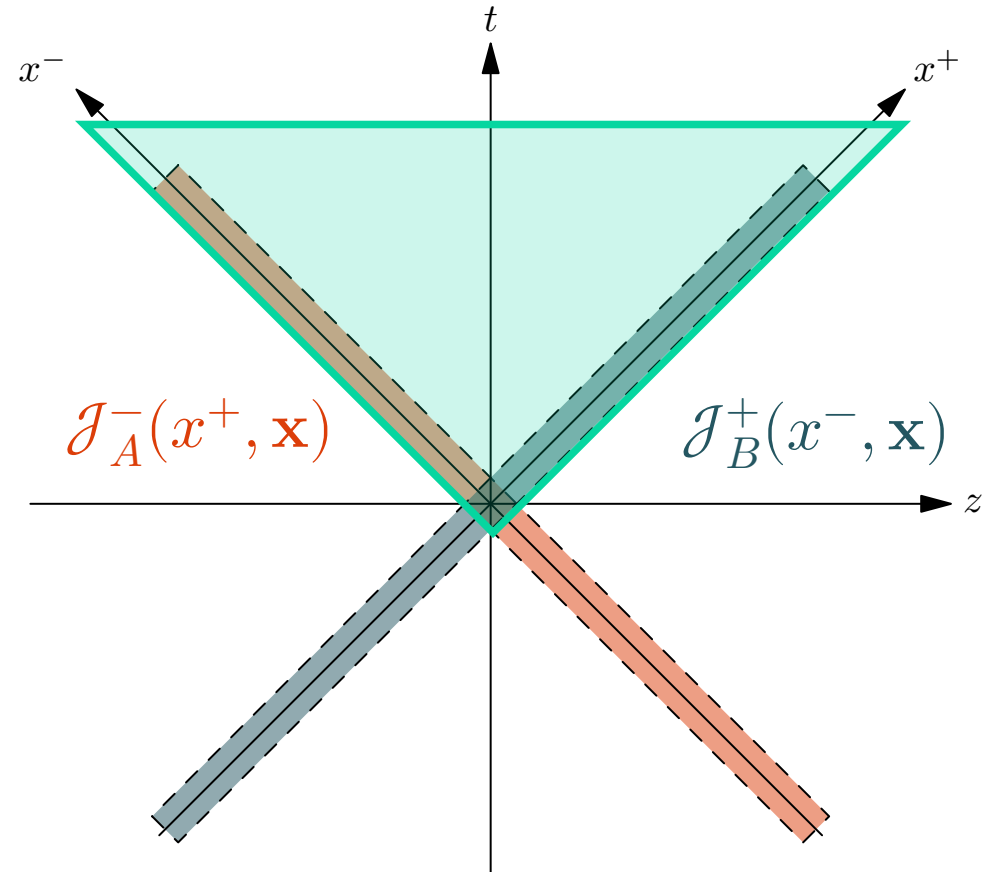
We assume weak sources!

$$A^\mu(x) = \mathcal{A}_A^\mu(x) + \mathcal{A}_B^\mu(x) + a^\mu(x),$$

$$J^\mu(x) = \mathcal{J}_A^\mu(x) + \mathcal{J}_B^\mu(x) + j^\mu(x)$$

must hold. Also,

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Dilute approximation

In **forward lightcone** full Yang-Mills equations

$$D_\mu F^{\mu\nu} = J^\nu$$

with

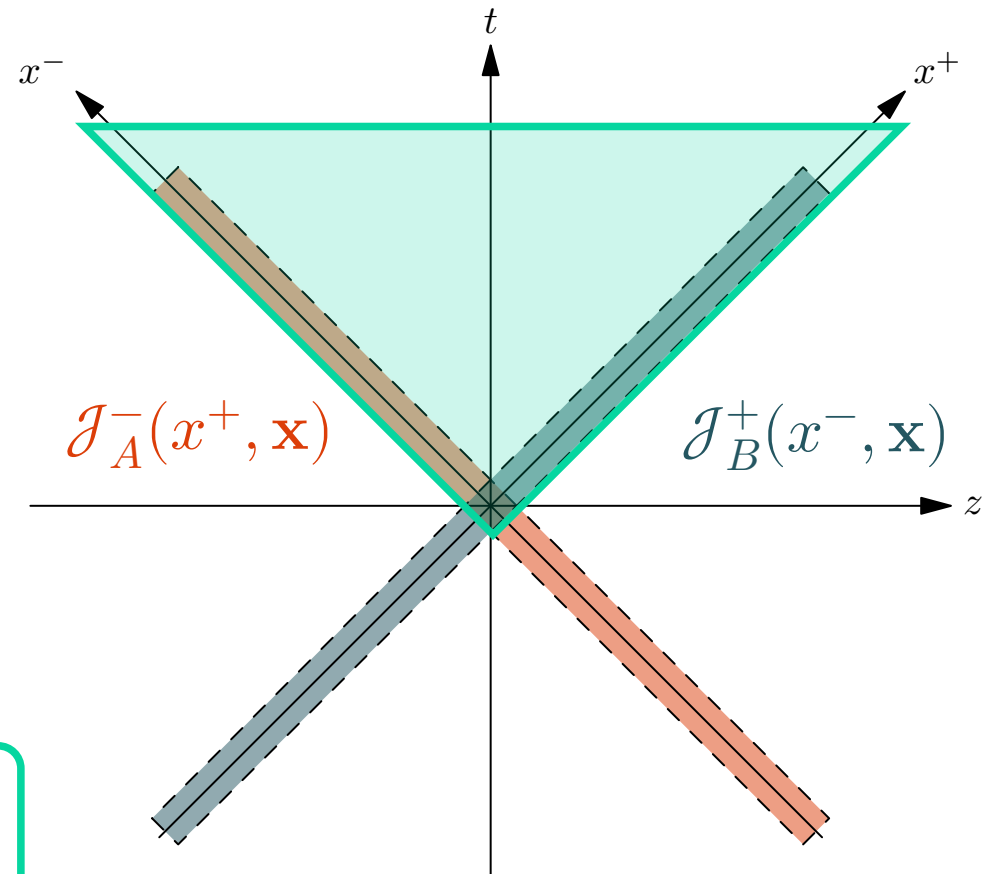
We assume weak sources!

$$A^\mu(x) = \mathcal{A}_A^\mu(x) + \mathcal{A}_B^\mu(x) + a^\mu(x),$$

$$J^\mu(x) = \mathcal{J}_A^\mu(x) + \mathcal{J}_B^\mu(x) + j^\mu(x)$$

must hold.

→ power series expansion in \mathcal{J}_A and \mathcal{J}_B
keep $\mathcal{O}(\mathcal{J}_A \mathcal{J}_B)$, drop higher orders



Dilute approximation

Covariant conservation of current:

$$\begin{aligned} D_\mu J^\mu &= \partial_\mu J^\mu - ig[A_\mu, J^\mu] \\ &= \mathcal{D}_{A,\mu} \mathcal{J}_A^\mu + \mathcal{D}_{B,\mu} \mathcal{J}_B^\mu + \partial_\mu j^\mu - ig[\mathcal{A}_{A,\mu}, \mathcal{J}_B^\mu] - ig[\mathcal{A}_{B,\mu}, \mathcal{J}_A^\mu] = 0 \end{aligned}$$

$$\partial_- j^- = ig[\mathcal{A}_B^+, \mathcal{J}_A^-]$$

$$\partial_+ j^+ = ig[\mathcal{A}_A^-, \mathcal{J}_B^+]$$

Dilute approximation

Yang-Mills equations:

$$\begin{aligned}
 [D_\mu, F^{\mu\nu}] &= [\mathcal{D}_{A,\mu}, \mathcal{F}_A^{\mu\nu}] + [\mathcal{D}_{B,\mu}, \mathcal{F}_B^{\mu\nu}] + \partial_\mu (\partial^\mu a^\nu - \partial^\nu a^\mu - ig[\mathcal{A}_A^\mu, \mathcal{A}_B^\nu] - ig[\mathcal{A}_B^\mu, \mathcal{A}_A^\nu]) \\
 &\quad - ig[\mathcal{A}_{A,\mu}, \partial^\mu \mathcal{A}_B^\nu - \partial^\nu \mathcal{A}_B^\mu] - ig[\mathcal{A}_{B,\mu}, \partial^\mu \mathcal{A}_A^\nu - \partial^\nu \mathcal{A}_A^\mu] \\
 &= \mathcal{J}_A^\nu + \mathcal{J}_B^\nu + j^\nu.
 \end{aligned}$$

$$\partial_\mu \partial^\mu a^+ = ig[\mathcal{A}_A^-, \partial_- \mathcal{A}_B^+] + j^+$$

$$\partial_\mu \partial^\mu a^- = ig[\mathcal{A}_B^+, \partial_+ \mathcal{A}_A^-] + j^-$$

$$\partial_\mu \partial^\mu a^i = ig[\mathcal{A}_A^-, \partial_i \mathcal{A}_B^+] + ig[\mathcal{A}_B^+, \partial_i \mathcal{A}_A^-]$$

Glasma field

$$a^+(x) = \frac{g}{2} f_{abc} t^c \int_{\mathbf{p}, \mathbf{q}} \int_0^\infty dz^+ \int_0^\infty dz^- \tilde{\mathcal{A}}_A^{-a}(x^+ - z^+, \mathbf{p}) \tilde{\mathcal{A}}_B^{+b}(x^- - z^-, \mathbf{q})$$

$$\times \frac{(-(\mathbf{p} + \mathbf{q})^2 + 2\mathbf{q}^2) z^+}{|\mathbf{p} + \mathbf{q}| \tau_z} J_1(|\mathbf{p} + \mathbf{q}| \tau_z) e^{-i(\mathbf{p} + \mathbf{q}) \cdot \mathbf{x}},$$

$$a^-(x) = \frac{g}{2} f_{abc} t^c \int_{\mathbf{p}, \mathbf{q}} \int_0^\infty dz^+ \int_0^\infty dz^- \tilde{\mathcal{A}}_A^{-a}(x^+ - z^+, \mathbf{p}) \tilde{\mathcal{A}}_B^{+b}(x^- - z^-, \mathbf{q})$$

$$\times \frac{+(\mathbf{p} + \mathbf{q})^2 - 2\mathbf{p}^2) z^-}{|\mathbf{p} + \mathbf{q}| \tau_z} J_1(|\mathbf{p} + \mathbf{q}| \tau_z) e^{-i(\mathbf{p} + \mathbf{q}) \cdot \mathbf{x}},$$

$$a^i(x) = \frac{g}{2} f_{abc} t^c \int_{\mathbf{p}, \mathbf{q}} \int_0^\infty dz^+ \int_0^\infty dz^- \tilde{\mathcal{A}}_A^{-a}(x^+ - z^+, \mathbf{p}) \tilde{\mathcal{A}}_B^{+b}(x^- - z^-, \mathbf{q})$$

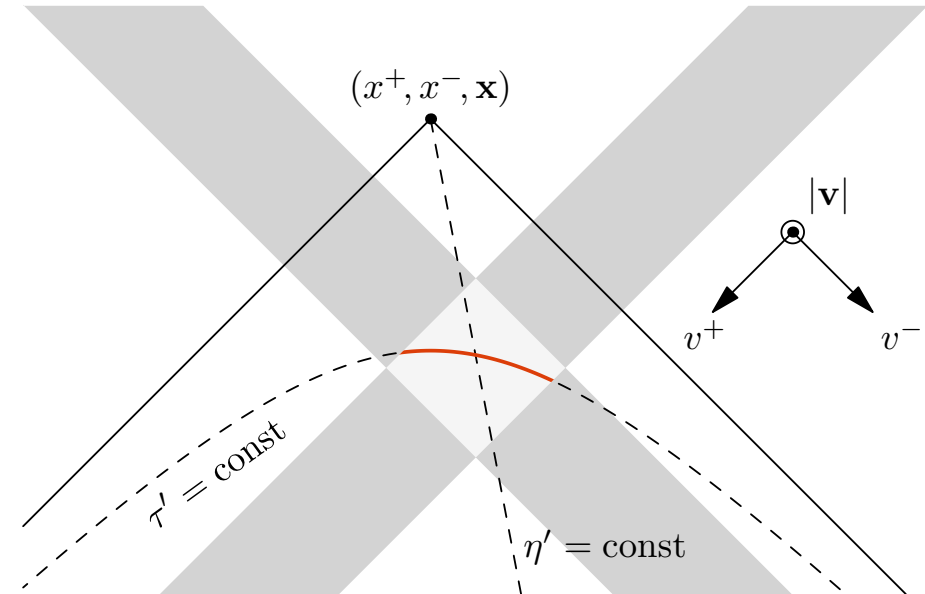
$$\times i(\mathbf{p}^i - \mathbf{q}^i) J_0(|\mathbf{p} + \mathbf{q}| \tau_z) e^{-i(\mathbf{p} + \mathbf{q}) \cdot \mathbf{x}}.$$

Glasma field strength tensor

$$f^{+-} = -\frac{g}{2\pi} \int_{\mathbf{v}} \int_{-\infty}^{\infty} d\eta' V$$

$$f^{\pm i} = \frac{g}{2\pi} \int_{\mathbf{v}} \int_{-\infty}^{\infty} d\eta' (V^{ij} \mp \delta^{ij} V) \frac{v^j e^{\pm\eta'}}{|\mathbf{v}| \sqrt{2}}$$

$$f^{ij} = -\frac{g}{2\pi} \int_{\mathbf{v}} \int_{-\infty}^{\infty} d\eta' V^{ij}$$



$$V := f_{abc} t^c \partial^i \mathcal{A}_A^{-a} \left(x^+ - \frac{|\mathbf{v}|}{\sqrt{2}} e^{+\eta'}, \mathbf{x} - \mathbf{v} \right) \partial^i \mathcal{A}_B^{+b} \left(x^- - \frac{|\mathbf{v}|}{\sqrt{2}} e^{-\eta'}, \mathbf{x} - \mathbf{v} \right)$$

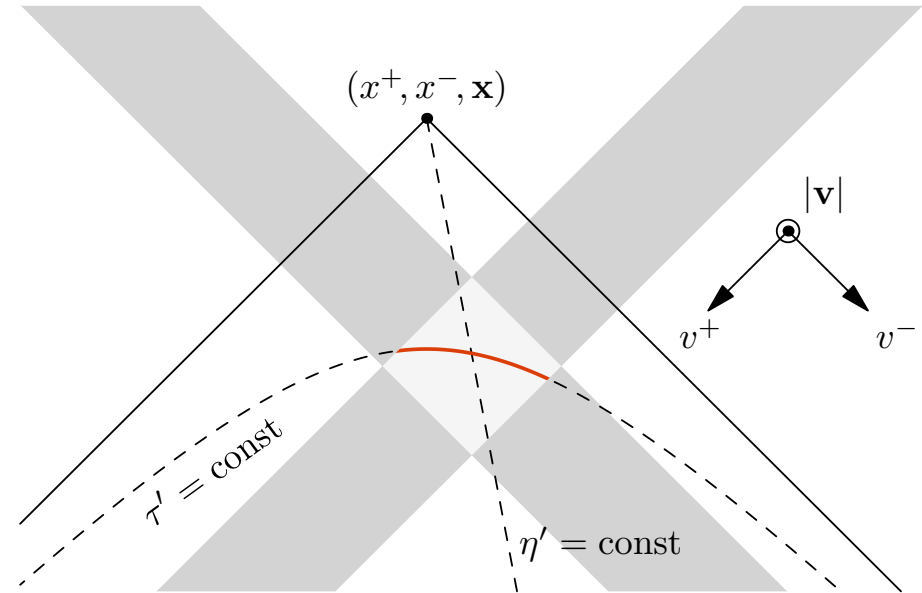
$$V^{ij} := f_{abc} t^c \left(\partial^i \mathcal{A}_A^{-a}(\dots) \partial^j \mathcal{A}_B^{+b}(\dots) - \partial^j \mathcal{A}_A^{-a}(\dots) \partial^i \mathcal{A}_B^{+b}(\dots) \right)$$

Glasma field strength tensor

$$f^{+-} = -\frac{g}{2\pi} \int_{\mathbf{v}} \int_{-\infty}^{\infty} d\eta' V$$

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$$V^{ij} := f_{abc} t^c \left(\partial^i \mathcal{A}_A^{-a}(\dots) \partial^j \mathcal{A}_B^{+b}(\dots) - \partial^j \mathcal{A}_A^{-a}(\dots) \partial^i \mathcal{A}_B^{+b}(\dots) \right)$$

See K. Schmidt's talk!

Color charge correlator

Color charges are drawn from Gaussian probability functional defined by 1-pt. function

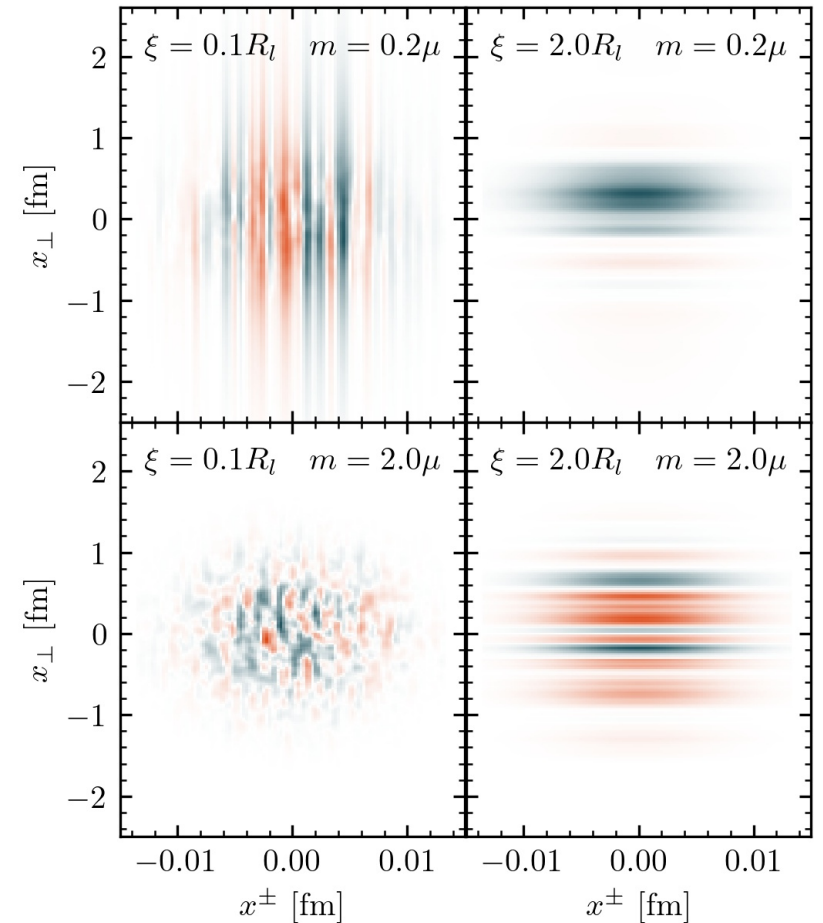
$$\langle \rho^a(x^\pm, \mathbf{x}) \rangle = 0$$

and 2-pt. function

$$\begin{aligned} \langle \rho^a(x^\pm, \mathbf{x}) \rho^b(y^\pm, \mathbf{y}) \rangle &= g^2 \mu^2 \delta^{ab} T\left(\frac{x^\pm + y^\pm}{2}, \frac{\mathbf{x} + \mathbf{y}}{2}\right) \\ &\times U_\xi(x^\pm - y^\pm) \delta^{(2)}(\mathbf{x} - \mathbf{y}) \end{aligned}$$

with

$$\begin{aligned} T(x^\pm, \mathbf{x}) &= \frac{1}{\sqrt{2\pi} R_l} e^{-\frac{(x^\pm)^2}{2R_l^2}} e^{-\frac{\mathbf{x}^2}{2R^2}} \\ U_\xi(x^\pm - y^\pm) &= \frac{1}{\sqrt{2\pi} \xi^2} e^{-\frac{(x^\pm - y^\pm)^2}{2\xi^2}} \end{aligned}$$



Color charge correlator

Color charge
defined by

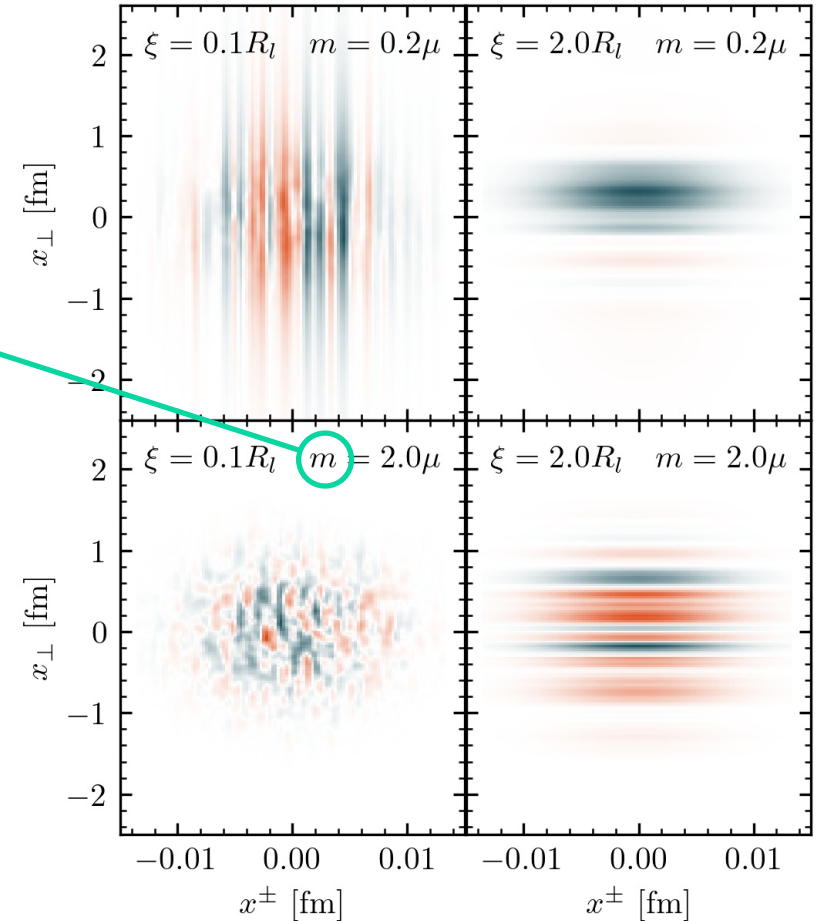
$$\mathcal{A}_{A/B}^{\mp a}(x^\pm, \mathbf{x}) = \int_{\mathbf{k}} \frac{\tilde{\rho}_{A/B}^a(x^\pm, \mathbf{k})}{\mathbf{k}^2 + m^2} e^{-\mathbf{k}^2/(2\Lambda_{UV}^2)} e^{-i\mathbf{k}\cdot\mathbf{x}},$$

and 2-pt. function

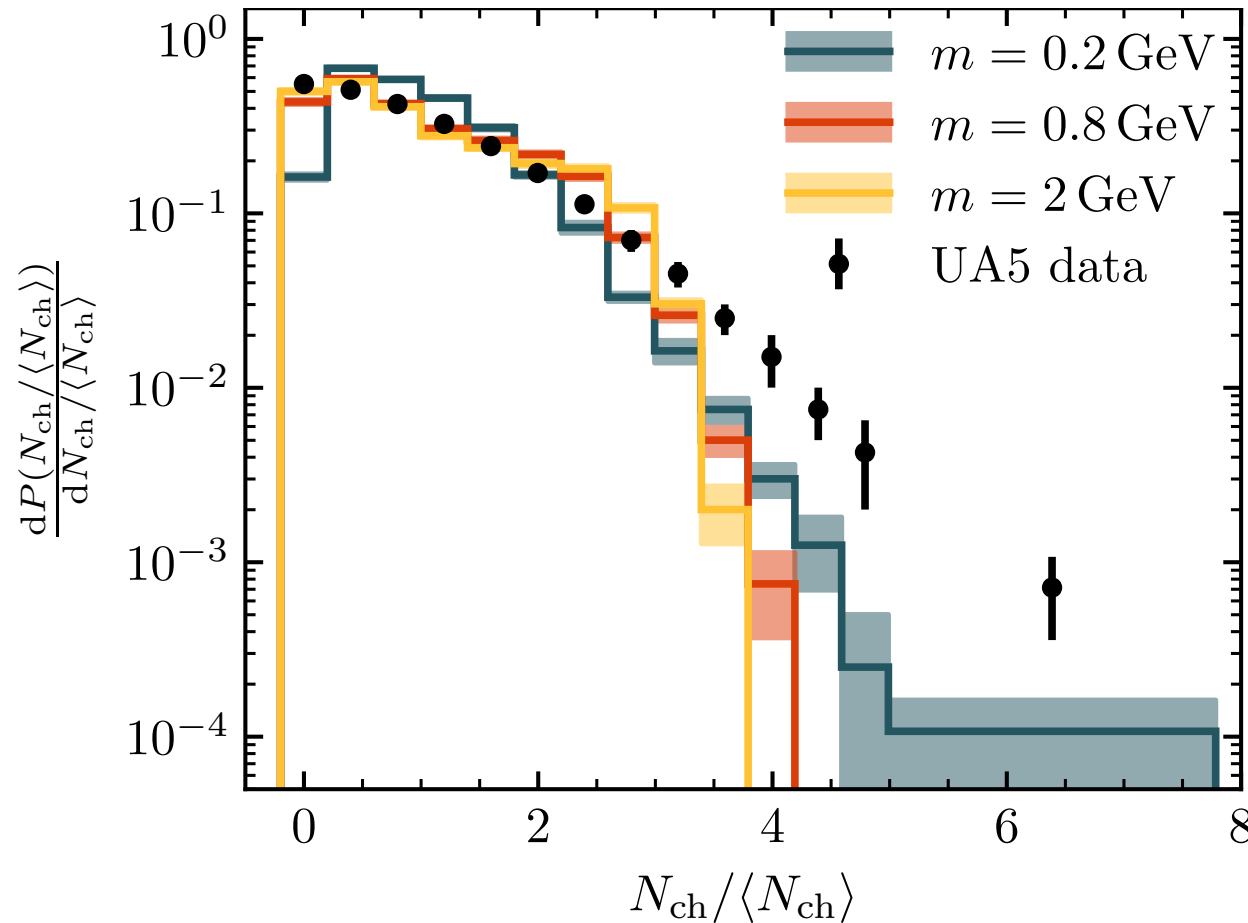
$$\begin{aligned} \langle \rho^a(x^\pm, \mathbf{x}) \rho^b(y^\pm, \mathbf{y}) \rangle &= g^2 \mu^2 \delta^{ab} T\left(\frac{x^\pm + y^\pm}{2}, \frac{\mathbf{x} + \mathbf{y}}{2}\right) \\ &\quad \times U_\xi(x^\pm - y^\pm) \delta^{(2)}(\mathbf{x} - \mathbf{y}) \end{aligned}$$

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pp-collisions: results



$$\sqrt{s} = 200 \text{ GeV}, \eta \approx 0$$

Large multiplicity events are severely underestimated!

This is a known effect!

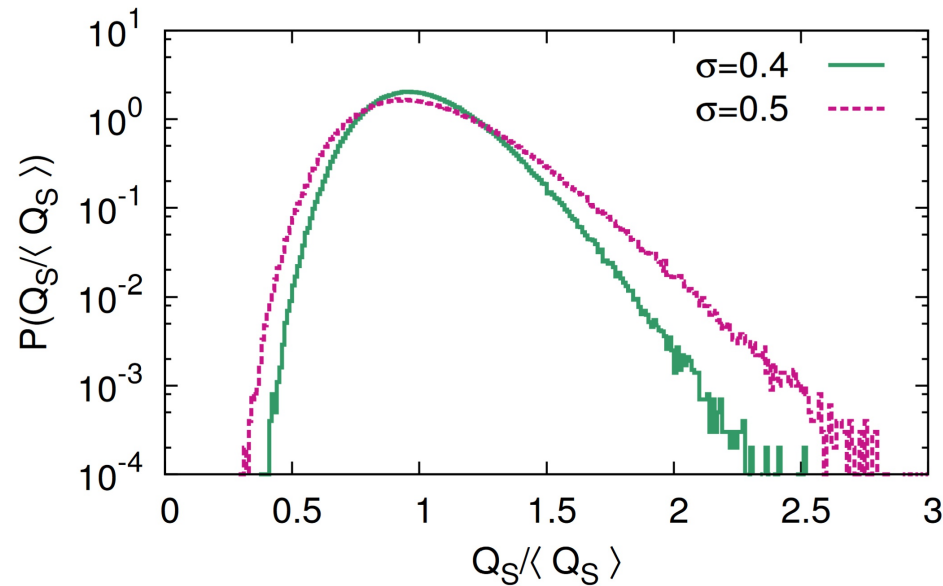
B. Schenke, P. Tribedy, R. Venugopalan
Phys. Rev. C 89.2 (2014), p. 024901

L. McLerran, P. Tribedy
Nucl. Phys. A 945 (2016), pp. 216–225

Saturation momentum fluctuations

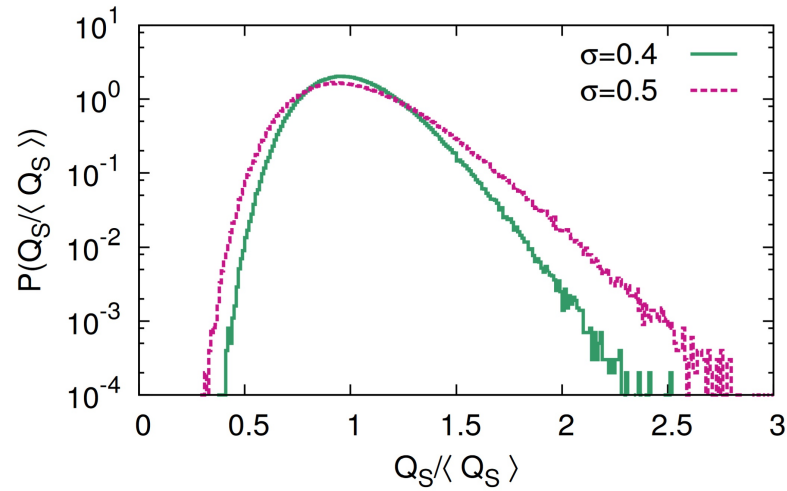
Let Q_s (i.e. color charge) fluctuate on event-by-event basis with factor drawn from

$$P(\ln(Q_s^2/\langle Q_s^2 \rangle)) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{\ln^2(Q_s^2/\langle Q_s^2 \rangle)}{2\sigma^2}\right).$$

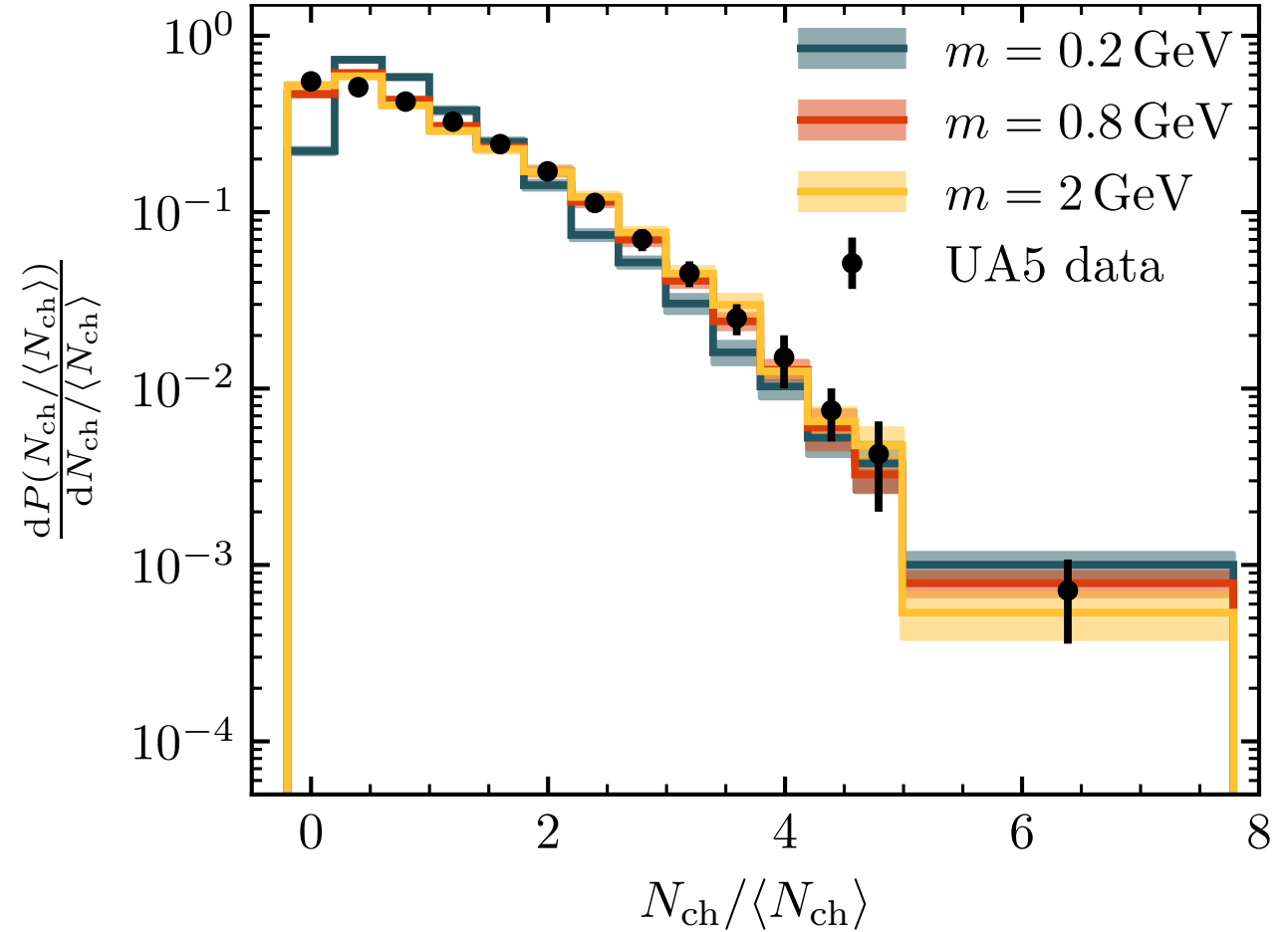


L. McLerran, P. Tribedy, Nucl. Phys. A
945 (2016), pp. 216–225

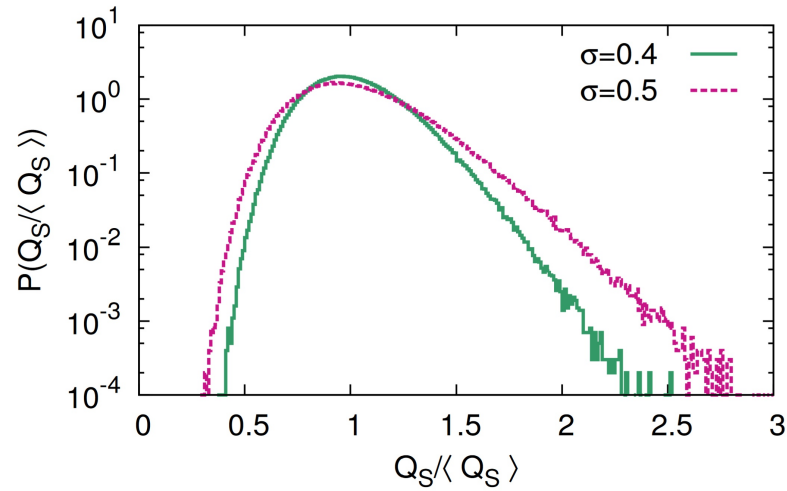
Saturation momentum fluctuations



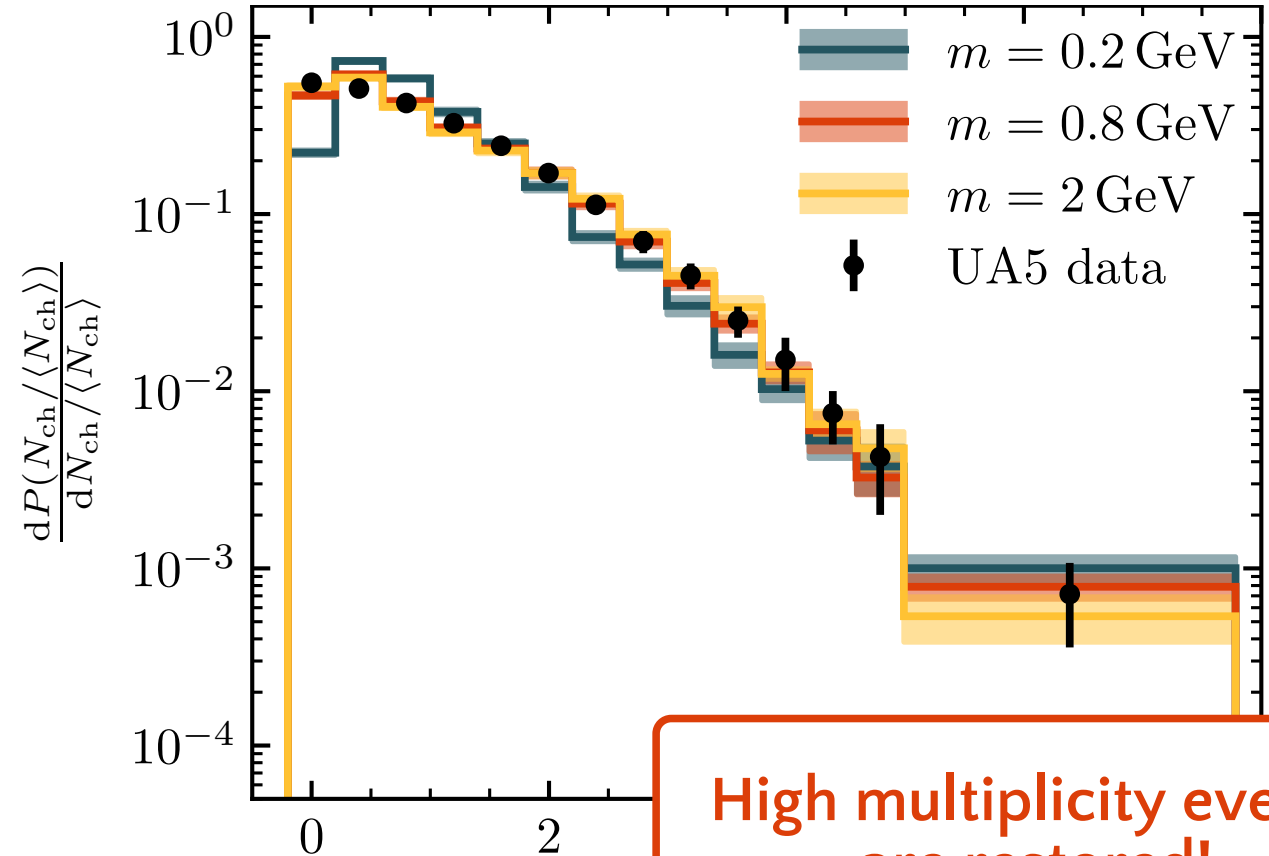
m	0.2 GeV	0.8 GeV	2 GeV
σ_{opt}	0.26	0.22	0.21



Saturation momentum fluctuations



m	0.2 GeV	0.8 GeV	2 GeV
σ_{opt}	0.26	0.22	0.21



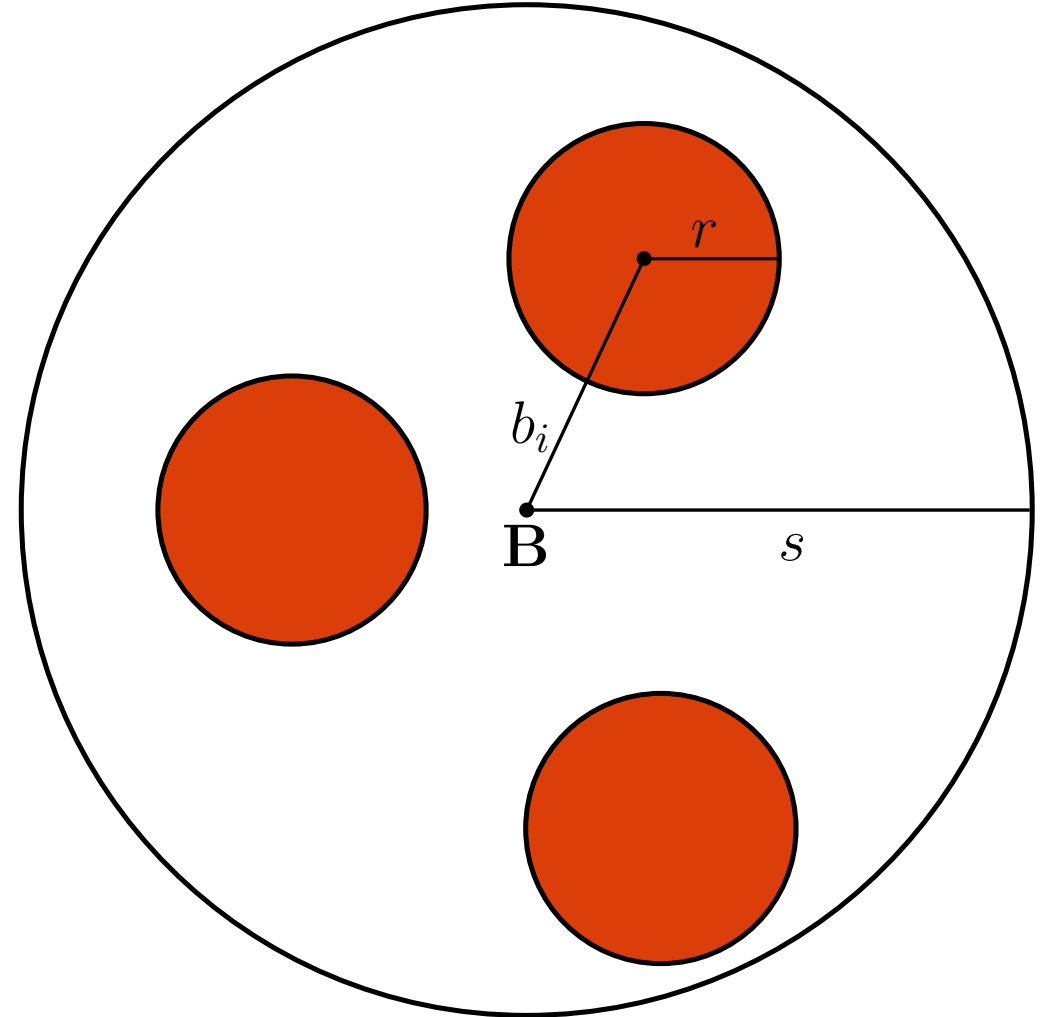
Valence quark hot spots

Alternatively:

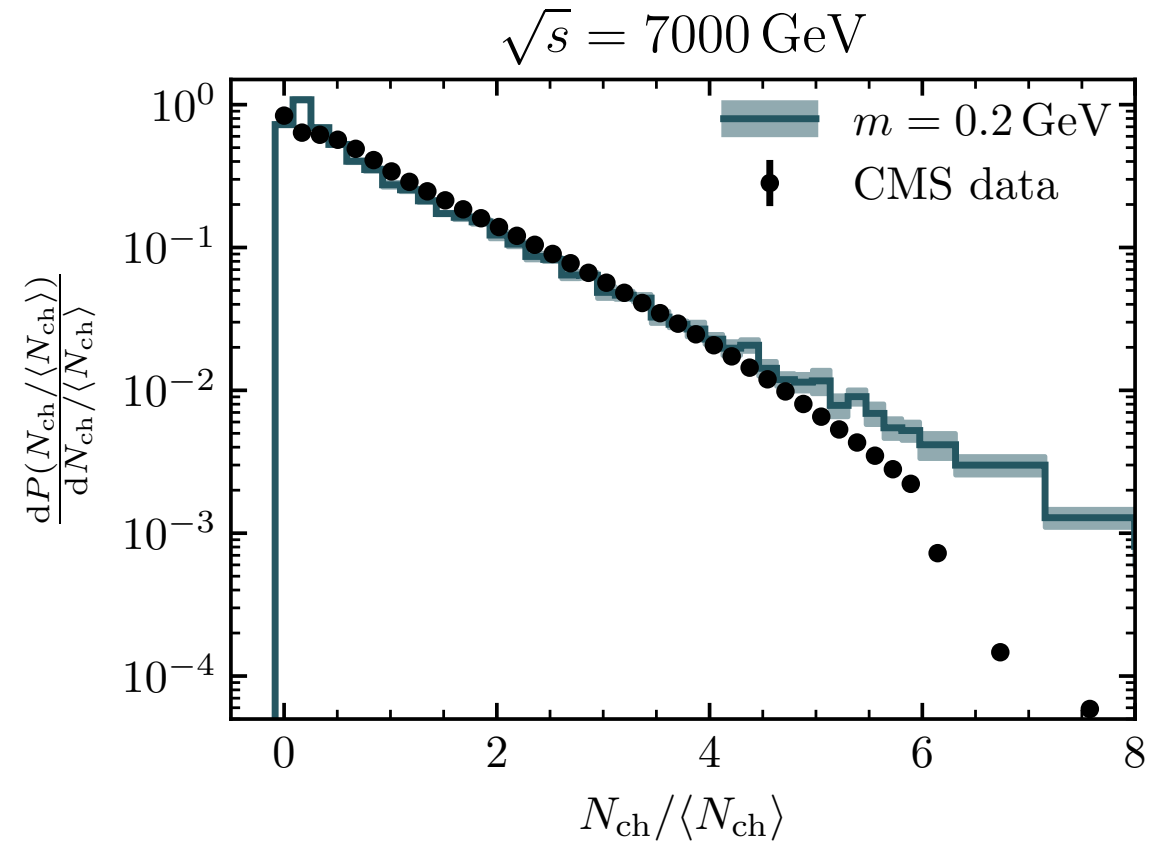
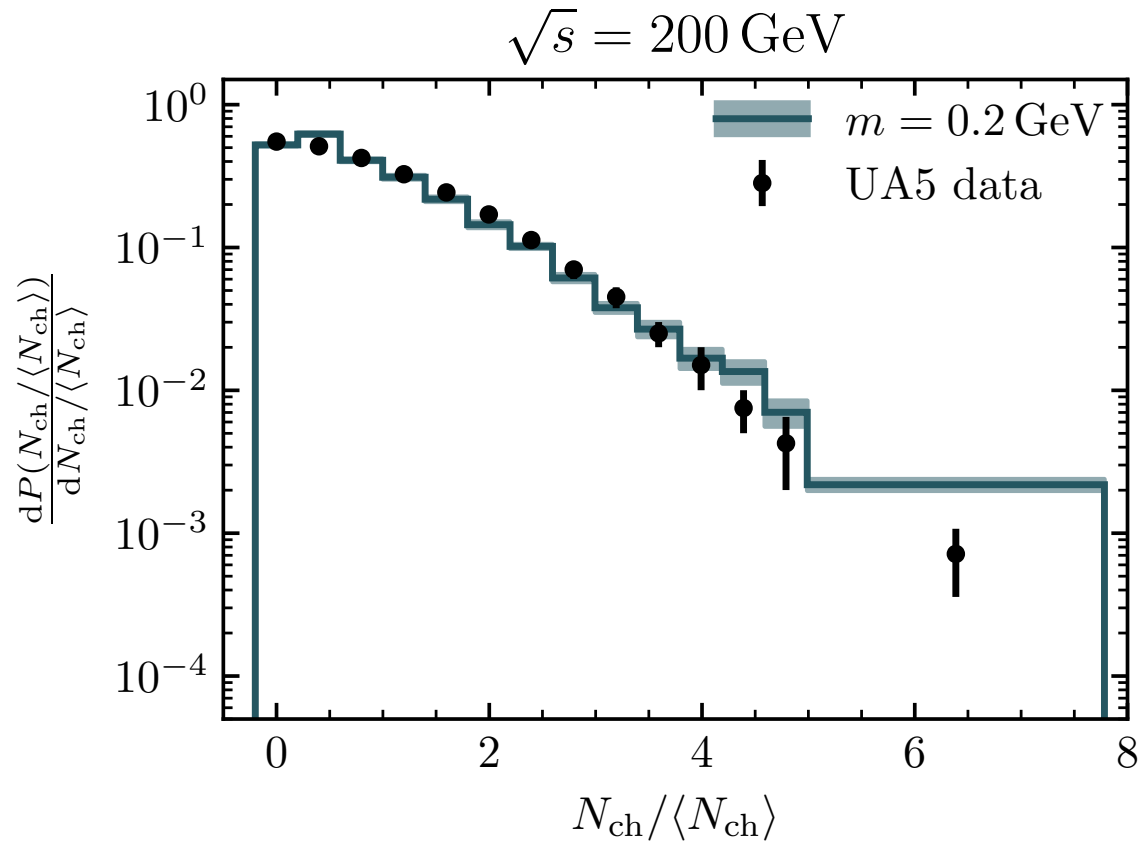
let nucleon consist of distinct hot spots

$n_v = 3$ (valence quarks)

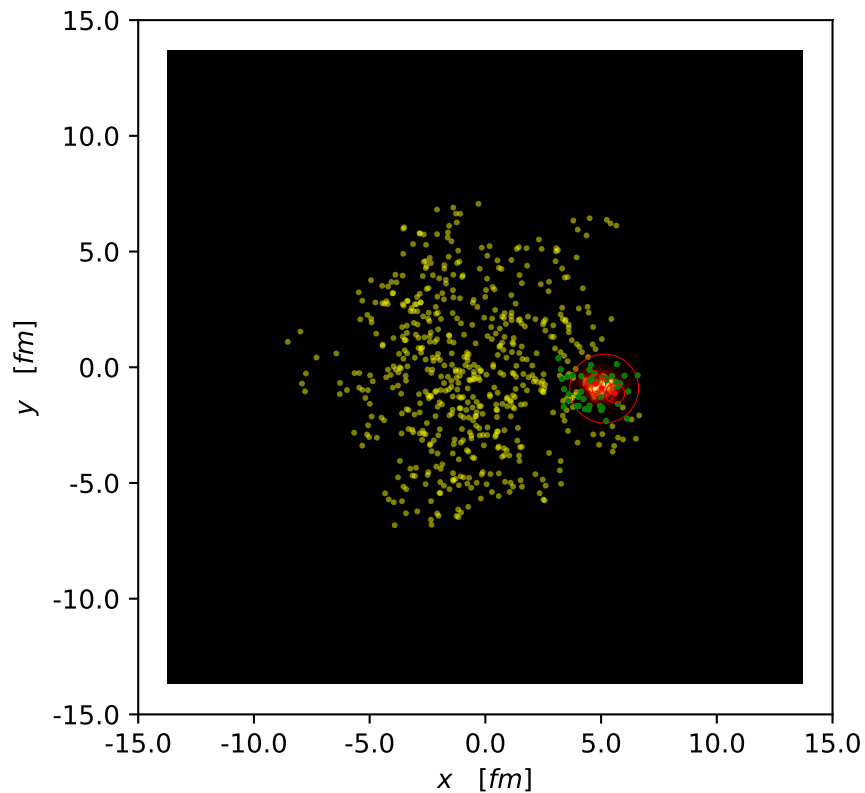
- are modeled as Gaussians with width r
- their positions are drawn from Gaussian dist. with width s (proton size)



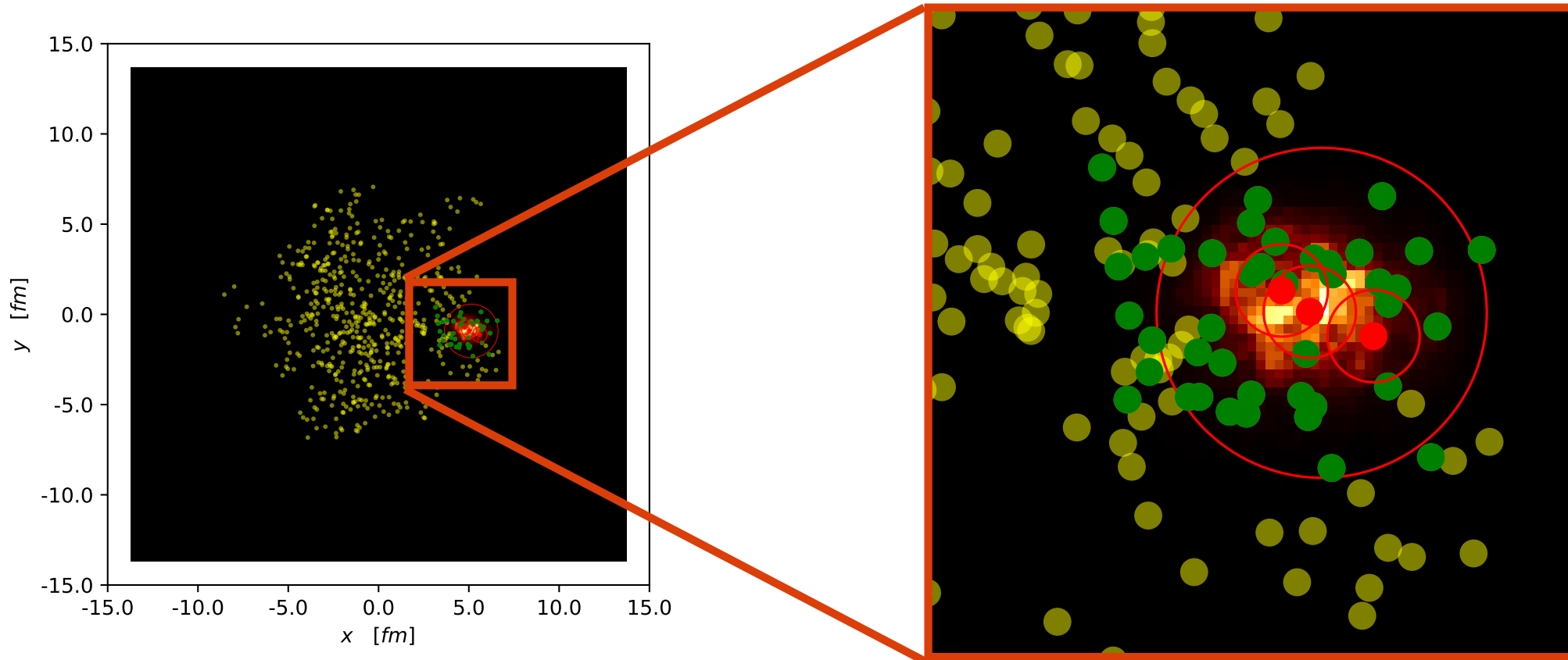
Valence quark hot spots



Use these nucleons to build heavy nuclei and study i.e. pA-collisions



Use these nucleons to build heavy nuclei and study i.e. pA-collisions



WIP coming up:

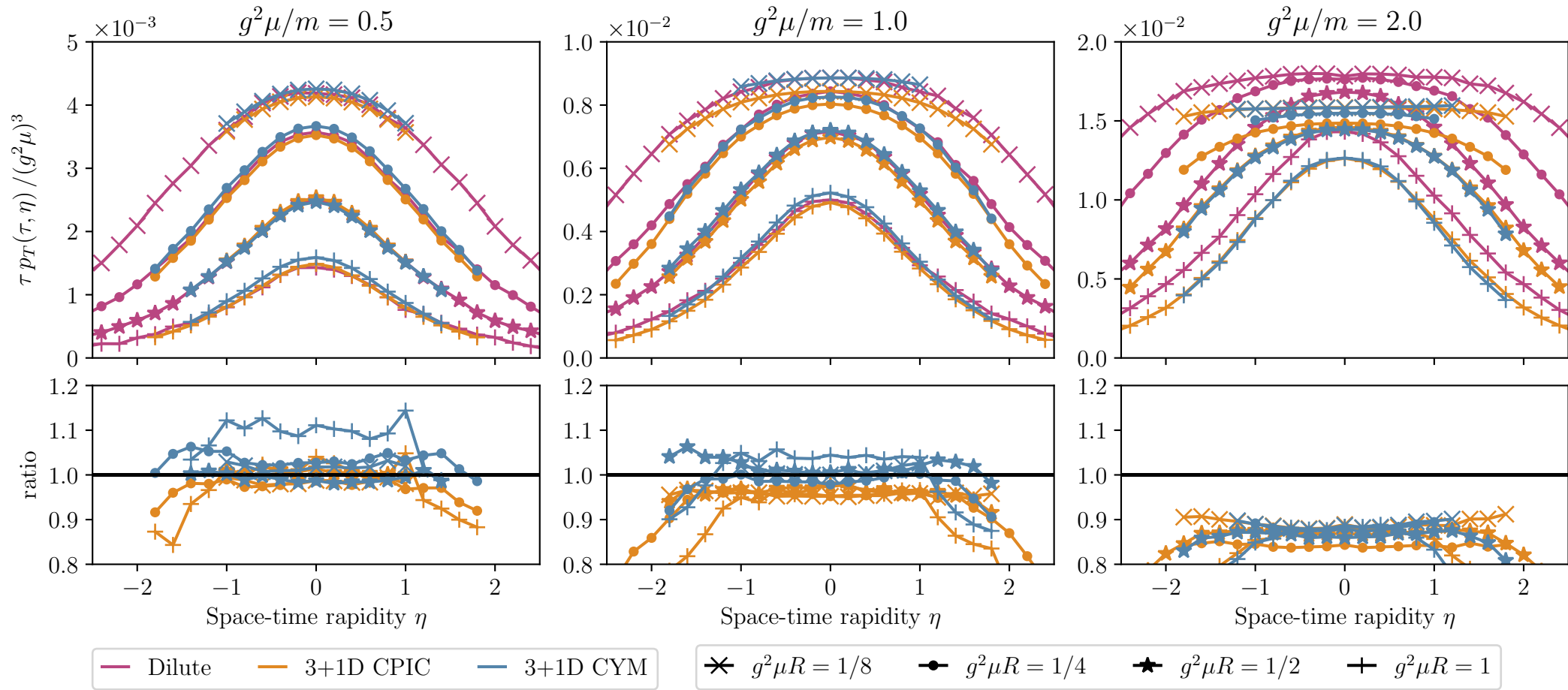
- simulate many events at $\eta = 0$
- select highest energy (\sim multiplicity) pA events
- simulate these events over large η range
- study **event plane** decorrelations with η through violations of $V_{n\Delta} = v_n^a v_n^b$
 - $\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n \cos(n(\phi - \Psi_n))$
 - $\frac{dN^{\text{pair}}}{d\Delta\phi} \propto 1 + 2 \sum_n V_{n\Delta} \cos(n\Delta\phi)$
- **Event plane** fluctuations depend mostly on initial state
- \rightarrow constrain model parameters and learn about longitudinal structure of nucleons and nuclei



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Backup slides

Comparison to lattice simulations



A. Ipp, D. I. Müller, S. Schlichting, P. Singh
Phys.Rev.D 104 (2021) 11, 114040

Shifted Milne coordinates

Milne coordinates

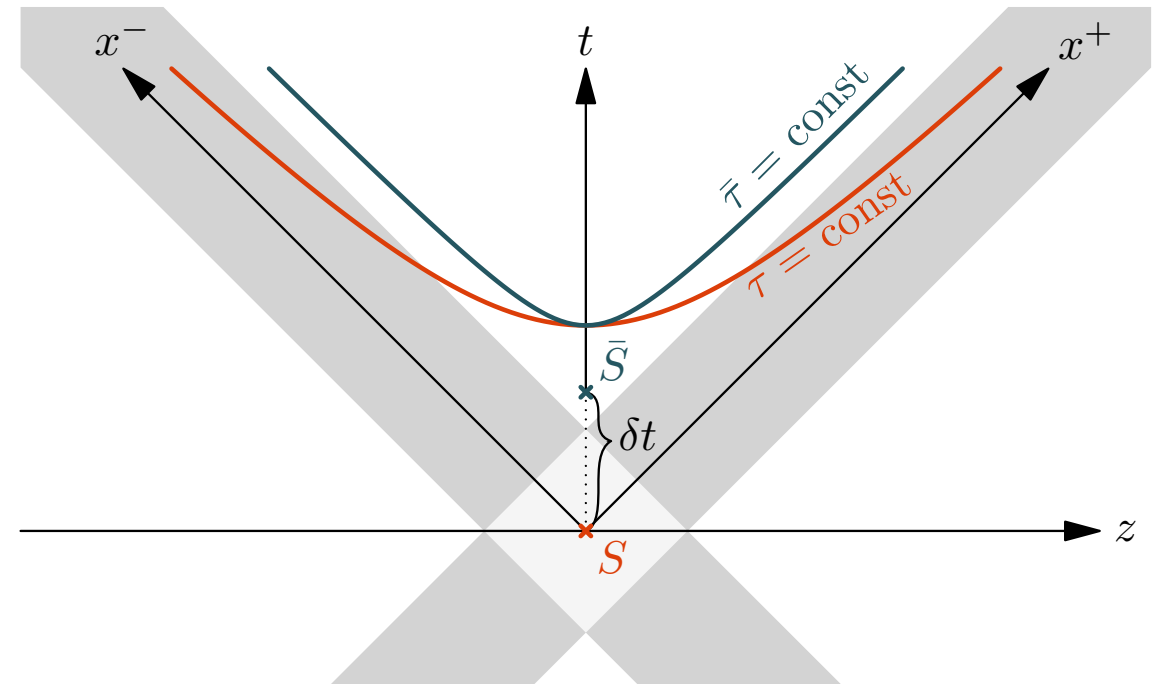
$$\tau = \sqrt{2x^+x^-} = \sqrt{t^2 - z^2}$$

$$\eta_s = \frac{1}{2} \ln \left(\frac{x^+}{x^-} \right) = \text{artanh} \left(\frac{z}{t} \right)$$

are used to parametrize observables of the Glasma.

For extended collision region it is not obvious where to put the origin!

We shift the origin to avoid $\bar{\tau} = \text{const}$ hyperbolas entering the nuclei!



Energy-momentum tensor

$$T^{\mu\nu} = 2 \text{Tr} \left[f^{\mu\rho} f_{\rho}{}^{\nu} + \frac{1}{4} g^{\mu\nu} f^{\rho\sigma} f_{\rho\sigma} \right]$$

τ - and η -components depend on (arbitrary) origin \rightarrow also look at local rest frame energy density ϵ_{LRF}

$$T^{\mu}{}_{\nu} u^{\nu} = \epsilon_{\text{LRF}} u^{\mu}$$

(u^{μ} is the only timelike eigenvector of $T^{\mu}{}_{\nu}$)

pp-collisions: rejection sampling

1. define the thickness function

$$t(\mathbf{x}) = \frac{1}{2\pi s^2} \exp\left(-\frac{\mathbf{x}^2}{2s^2}\right)$$

2. define the overlap function

$$T(b) = \int d^2\mathbf{x} t(\mathbf{x} + \mathbf{b}/2)t(\mathbf{x} - \mathbf{b}/2) = \frac{1}{4\pi s^2} \exp\left(-\frac{b^2}{4s^2}\right)$$

3. define the (average) number of parton-parton collisions

$$N_{gg} := N_g^2 \sigma_{gg} T(b).$$

4. the probability of at least 1 interaction is

$$P_{\text{ia}}(b) = 1 - \exp\left(-N_g^2 \sigma_{gg} T(b)\right).$$

pp-collisions: rejection sampling

5. define the effective nucleon-nucleon cross section

$$\sigma_{NN} = \int d^2\mathbf{b} P_{\text{ia}}(b).$$

6. the differential interaction probability is

$$\frac{d^2P}{d\mathbf{b}^2} = \frac{1 - \exp(-N_g^2 \sigma_{gg} T(b))}{\int d^2\mathbf{b} (1 - \exp(-N_g^2 \sigma_{gg} T(b)))}.$$

7. we simulate protons as Gaussian blobs and randomly sample impact parameters