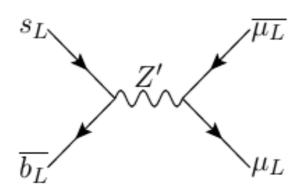
Hadron Collider Sensitivity for Z's for Flavour Anomalies



Matthew Dolan

Based on B.C. Allanach, Tyler Corbett, MJD, Tevong You; 1810.02166





Flavour Anomalies?

- Deviations in ratios of branching ratios in certain flavour processes involving b → s transitions, e.g.
 - Explain with New Physics involving a $b \to s \mu^+ \mu^-$ transition

$$R_K \equiv \frac{BR(B \to K\mu^+\mu^-)}{BR(B \to Ke^+e^-)}, \qquad R_{K^*} \equiv \frac{BR(B \to K^*\mu^+\mu^-)}{BR(B \to K^*e^+e^-)}.$$

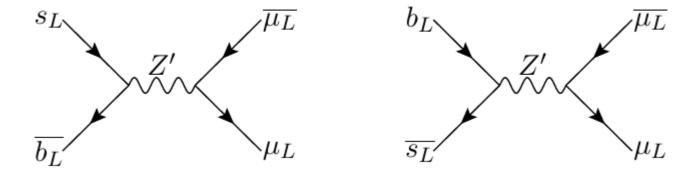
Also in the angular variable P_5' , $BR(B_s \to \phi \mu^+ \mu^-)$, $R_{D^{(*)}}$

UV-complete explanations involve either flavour-violating Z's and/or leptoquarks.

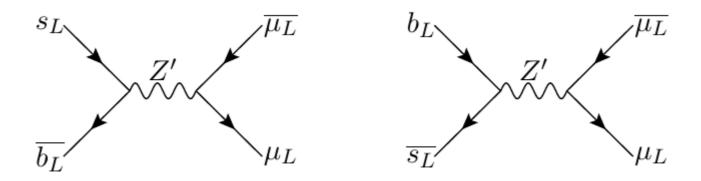
Focus today on Z' scenario (leptoquarks: work in progress).

Flavour Anomalies?

- Establish properties of new resonances through direct production at colliders.
 - Direct probe of new physics explaining aspects of fermion mass problem.
 - Perturbative unitarity: New Physics enters below 80 TeV.



Flavour Anomalies?

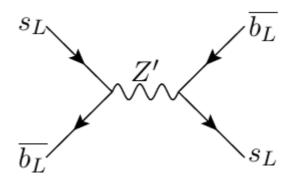


$$\mathcal{L}_{Z'f} = (g_{sb}Z'_{\rho}\overline{s_L}\gamma^{\rho}b_L + \text{h.c.}) + g_{\mu\mu}Z'_{\rho}\overline{\mu_L}\gamma^{\rho}\mu_L + \dots$$

Equal couplings to LH and RH muons also works. RH-only enhances $R_{K^{\ast}}$ rather than diminishes it. Fits to anomalies require:

$$g_{bs}g_{\mu\mu} = -x \left(\frac{M_{Z'}}{31\text{TeV}}\right)^2$$
 $x = 1.00 \pm 0.25.$

Constraints



$$\mathcal{L}_{Z'f} = (g_{sb}Z'_{\rho}\overline{s_L}\gamma^{\rho}b_L + \text{h.c.}) + g_{\mu\mu}Z'_{\rho}\overline{\mu_L}\gamma^{\rho}\mu_L + \dots$$

Same Lagrangian also leads to $B_s - \bar{B}_s$ mixing. Some discussion in literature about hadronic form factors

Small g_{bs} Large $g_{\mu\mu}$

$$|g_{bs}| \lesssim M_{Z'}/(148 \text{ TeV})$$
 or $|g_{bs}| \lesssim M_{Z'}/(600 \text{ TeV})$

Trident production
$$\nu_{\mu}\gamma^{*} \rightarrow \nu_{\mu}\mu^{+}\mu^{-} \longrightarrow g_{\mu\mu} \lesssim M_{Z'}/(0.39 \text{TeV})$$

Simplified Models

Primes indicate weak gauge eigenbasis

Coupling constants determined by UV-completion

Define gauge-invariant simplified models

$$\mathcal{L}_{Z'f} = \left(\overline{\mathbf{Q}'_{\mathbf{L}}}_{i}\lambda_{ij}^{(Q)}\gamma^{\rho}\mathbf{Q}'_{\mathbf{L}j} + \overline{\mathbf{L}'_{\mathbf{L}}}_{i}\lambda_{ij}^{(L)}\gamma^{\rho}\mathbf{L}'_{\mathbf{L}j}\right)Z'_{\rho}$$

Find couplings in mass-basis

$$-\mathcal{L}_{Y} = \overline{\mathbf{u}_{\mathbf{L}}^{\prime}} V_{u_{L}} V_{u_{L}}^{\dagger} m_{u} V_{u_{R}} V_{u_{R}}^{\dagger} \mathbf{u}_{\mathbf{R}}^{\prime} + \overline{\mathbf{d}_{\mathbf{L}}^{\prime}} V_{d_{L}} V_{d_{L}}^{\dagger} m_{d} V_{d_{R}} V_{d_{R}}^{\dagger} \mathbf{d}_{\mathbf{R}}^{\prime} + \overline{\mathbf{e}_{\mathbf{L}}^{\prime}} V_{e_{L}} V_{e_{L}}^{\dagger} m_{e} V_{e_{R}} V_{e_{R}}^{\dagger} \mathbf{e}_{\mathbf{R}}^{\prime} + \overline{\mathbf{n}_{\mathbf{L}}^{\prime}}^{c} V_{\nu_{L}}^{*} V_{\nu_{L}}^{T} m_{\nu} V_{\nu_{L}} V_{\nu_{L}}^{\dagger} \mathbf{n}_{\mathbf{L}}^{\prime} + h.c. + \dots$$

Defines mass-basis

$$\mathbf{u}_{\mathbf{R}} \equiv V_{u_R}^{\dagger} \mathbf{u}_{\mathbf{R}}', \qquad \mathbf{u}_{\mathbf{L}} \equiv V_{u_L}^{\dagger} \mathbf{u}_{\mathbf{L}}', \qquad \mathbf{d}_{\mathbf{R}} \equiv V_{d_R}^{\dagger} \mathbf{d}_{\mathbf{R}}', \qquad \mathbf{d}_{\mathbf{L}} \equiv V_{d_L}^{\dagger} \mathbf{d}_{\mathbf{L}}',$$

$$\mathbf{e}_{\mathbf{R}} \equiv V_{e_R}^{\dagger} \mathbf{e}_{\mathbf{R}}', \qquad \mathbf{e}_{\mathbf{L}} \equiv V_{e_L}^{\dagger} \mathbf{e}_{\mathbf{L}}', \qquad \mathbf{n}_{\mathbf{L}} \equiv V_{\nu_L}^{\dagger} \mathbf{n}_{\mathbf{L}}'.$$

CKM and PMNS matrices

$$V = V_{u_L}^{\dagger} V_{d_L}, \qquad U = V_{\nu_L}^{\dagger} V_{e_L}.$$

$$\mathcal{L} = \left(\overline{\mathbf{u}_{\mathbf{L}}}V\Lambda^{(Q)}V^{\dagger}\gamma^{\rho}\mathbf{u}_{\mathbf{L}} + \overline{\mathbf{d}_{\mathbf{L}}}\Lambda^{(Q)}\gamma^{\rho}\mathbf{d}_{\mathbf{L}} + \overline{\mathbf{n}_{\mathbf{L}}}U\Lambda^{(L)}U^{\dagger}\gamma^{\rho}\mathbf{n}_{\mathbf{L}} + \overline{\mathbf{e}_{\mathbf{L}}}\Lambda^{(L)}\gamma^{\rho}\mathbf{e}_{\mathbf{L}}\right)Z'_{\rho},$$

$$\Lambda^{(Q)} \equiv V_{d_{L}}^{\dagger}\lambda^{(Q)}V_{d_{L}}, \qquad \Lambda^{(L)} \equiv V_{e_{L}}^{\dagger}\lambda^{(L)}V_{e_{L}}$$

Mixed up-muon and down-muon models

MUM model:

$$\Lambda^{(Q)} = g_{bs} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \qquad \Lambda^{(L)} = g_{\mu\mu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\mathcal{L}_{Z'f} = (g_{sb}Z'_{\rho}\overline{s_L}\gamma^{\rho}b_L + \text{h.c.}) + g_{\mu\mu}Z'_{\rho}\overline{\mu_L}\gamma^{\rho}\mu_L + \dots$$

Gives the original Lagrangian plus other terms. Mixing hides in neutrino and up sectors.

Branching ratios are effectively 50:50 muons and muon neutrinos.

| MUM | model |
|-------------------|-------|
| mode | BR |
| $ u_i \bar{ u}_k$ | 0.5 |
| $\mu^+\mu^-$ | 0.5 |

$$\mathcal{L} = \left(\overline{\mathbf{u}_{\mathbf{L}}}V\Lambda^{(Q)}V^{\dagger}\gamma^{\rho}\mathbf{u}_{\mathbf{L}} + \overline{\mathbf{d}_{\mathbf{L}}}\Lambda^{(Q)}\gamma^{\rho}\mathbf{d}_{\mathbf{L}} + \overline{\mathbf{n}_{\mathbf{L}}}U\Lambda^{(L)}U^{\dagger}\gamma^{\rho}\mathbf{n}_{\mathbf{L}} + \overline{\mathbf{e}_{\mathbf{L}}}\Lambda^{(L)}\gamma^{\rho}\mathbf{e}_{\mathbf{L}}\right)Z'_{\rho},$$

$$\Lambda^{(Q)} \equiv V_{d_{L}}^{\dagger}\lambda^{(Q)}V_{d_{L}}, \qquad \Lambda^{(L)} \equiv V_{e_{L}}^{\dagger}\lambda^{(L)}V_{e_{L}}$$

Mixed up-muon and down-muon models

$$\Lambda^{(Q)} = g_{tt} V^{\dagger} \cdot \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot V, \qquad \Lambda^{(L)} = g_{\mu\mu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Gives Z' couplings to mixed down-type quarks and LH top.

UV completed by 'Third Family Hypercharge Model'

Allanach and Davighi, 1809.01158

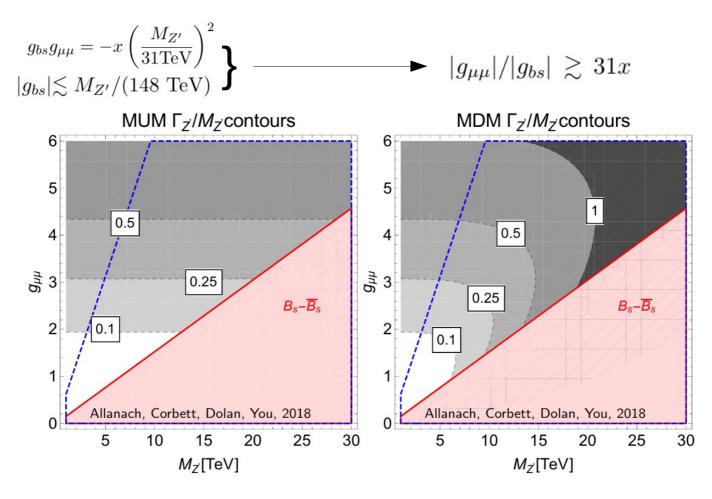
$$g_{bs} = V_{ts}^* V_{tb} g_{tt}.$$

Enhanced couplings to bb: by factor $1/|V_{ts}| \sim 25$

| MDM model | | | | | | | | |
|---------------------|---------|----------|------------------------|----------|-------------|------|-------------|--|
| mode | BR | mode | BR | mode | BR | mode | BR | |
| $\nu_i \bar{\nu}_k$ | (1-z)/2 | t ar t | z/2 | jj' | $y^2 z X/2$ | bj | $y^2 z Y/2$ | |
| $\mu^+\mu^-$ | (1-z)/2 | $ar{b}b$ | $y^2 z V_{tb} ^4 / 2$ | $ar{b}j$ | $y^2 z Y/2$ | | | |

$$X \equiv \left| |V_{td}|^2 + |V_{ts}|^2 + 2\Re(V_{ts}^* V_{td}) \right|^2 \qquad z \equiv \sum_{i,j=1}^3 BR(Z' \to q_i \bar{q}_j) = \frac{3y^2}{1+y^2}, \qquad Y = |V_{tb}|^2 |V_{td} + V_{ts}|^2$$

However, these resonances may be quite wide.



Will focus on dimuon channel

$$pp \to Z' \to \mu^+ \mu^-$$

However, these resonances may be quite wide.

$$\mathcal{D}_{\mu\nu}(p^2) = \frac{-i\eta_{\mu\nu}}{p^2 - M_{Z'}^2 + i\Gamma_{Z'}M_{Z'}}$$

Breit-Wigner propagator assumes the narrow-width approximation. Resummation of 1-loop corrections at fixed $\hat{s} = M_{Z'}^2$

For wider resonances partonic CoM energy can be further from pole in propagator.

$$\mathcal{D}_{\mu\nu}(p^2) = \frac{-i\eta_{\mu\nu}}{p^2 - M_{Z'}^2 + i\frac{p^2}{M_{Z'}^2}\Gamma_{Z'}M_{Z'}}.$$

$$M_{Z'} = 13 \text{ TeV}, g_{\mu\mu} = 2.1, \Gamma_{Z'}/M_{Z'} = 12\%$$

$$M_{Z'} = 17 \text{ TeV}, g_{\mu\mu} = 2.7, \Gamma_{Z'}/M_{Z'} = 19\%$$

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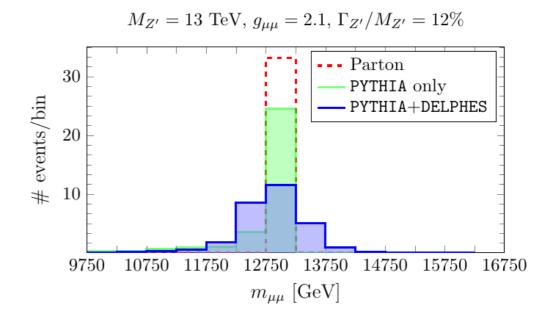
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$$M_{Z'} = 17 \text{ TeV}, g_{\mu\mu$$

FeynRules → MadGraph → Pythia → Delphes toolchain.

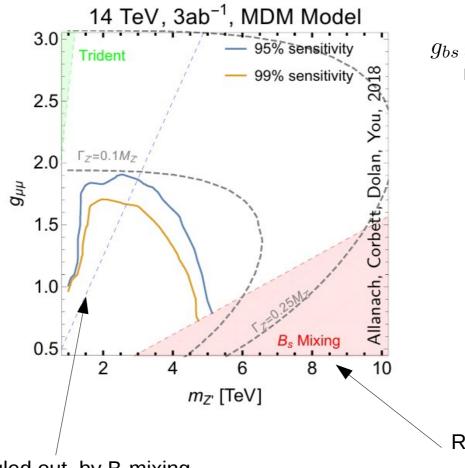
Detector simulation matters for FCC: multi-TeV muons have small bending and resolution degrades.



HL-LHC Sensitivity

HL-LHC doesn't have sensitivity to the MUM model: g_{bs} is small and so are b-quark PDFs.

In the MDM model the bb coupling is enhanced relative to the bs coupling. Leads to larger crosssections.

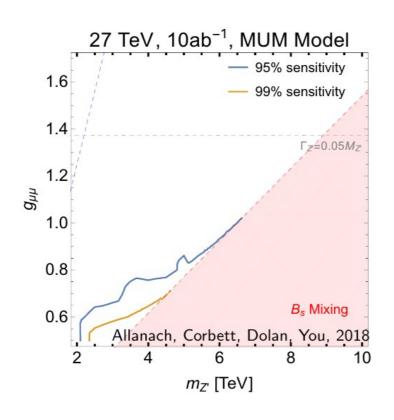


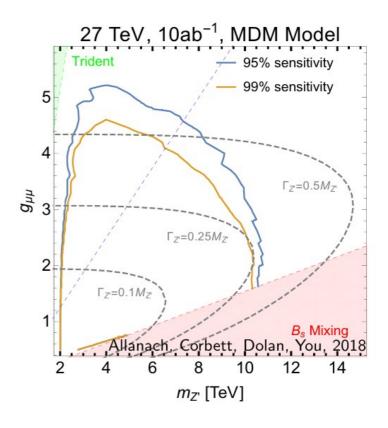
 g_{bs} set in these plots by requiring agreement with anomalies

Ruled out by B-mixing

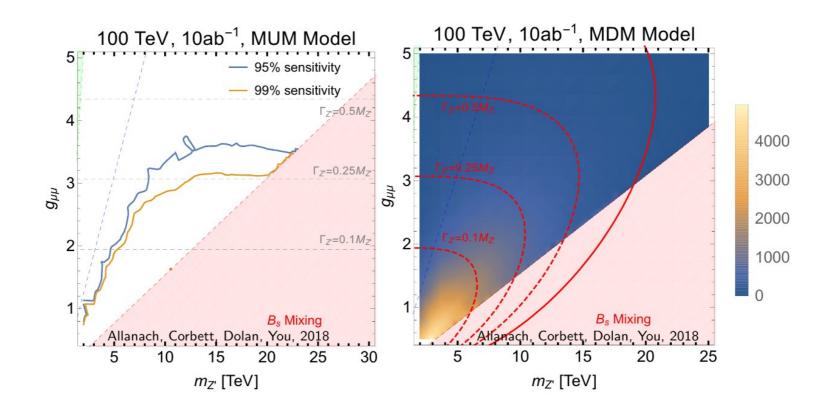
Possibly ruled out by B-mixing

Large benefits to going up in energy, since b-quark PDFs increase.

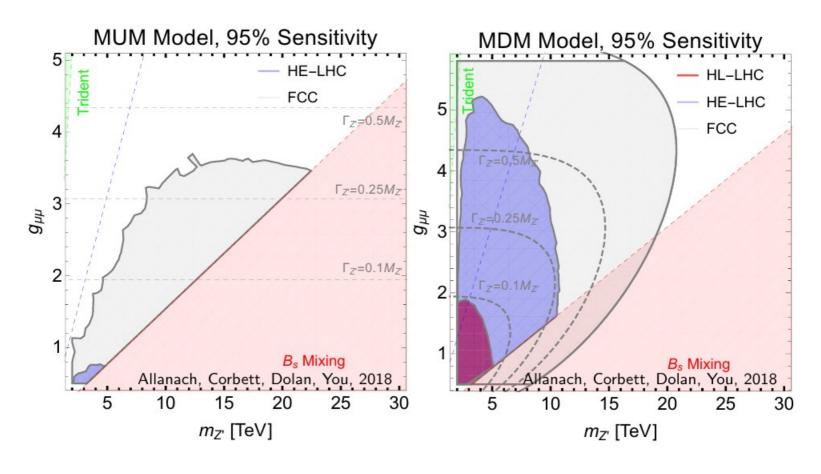




- FCC in principle has sensitivity over the whole MDM parameter space studied.
 - At extremes of parameter space perturbation theory untrustworthy.



Summary plots



Conclusions

- R_K and $R_{K^{(*)}}$ require the existence of New Physics, if confirmed.
- May require large couplings, leading to resonances with large widths.
 - Would provide strong case for future high-energy hadron collider.

• (We should build a big collider.)