

# The role of radiation in Toda chain hydrodynamics

From a many-body perspective, classical integrable systems fall into two broad categories: fluids and chains. The former are particle-based and their hydrodynamics closely mirrors that of quantum models. Chain systems, on the other hand, behave like integrable wave equations, with their long-time dynamics separating into solitons and dispersive radiation. While soliton gases are relatively well understood, they generally don't represent thermodynamic ensembles, and the role of radiation in GGEs remains an open question.

We focus on the Toda chain, whose inverse scattering spectrum includes both a solitonic mode and radiation. Using tools from random matrix theory, we compute average scattering data for random initial conditions. Radiation appears in generic GGEs, paving the way toward a coupled soliton–radiation hydrodynamic description.

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**Session Classification:** Participants Talks