# <span id="page-0-0"></span>Search for short strings in  $e^+e^-$ -annihilation

M. E. Kozhevnikova In collaboration with: O. V.Teryaev A. G. Oganesian

Joint Institute for Nuclear Research

Grodno, August 2018

<span id="page-1-0"></span>[Introduction](#page-1-0) The fitting of experimental cross-sections data on +e<sup>−</sup>-ann<mark>i</mark>hilation to hadrons The calculation of D-function and the analysis of coefficients

# Plan of the presentation

- **1** Operator product expansion and short strings.
- $\bullet$  The fitting of experimental data on  $e^+e^-$ -annihilation to hadrons
- **3** PT and APT
- <sup>4</sup> Adler function and the Borel transform
- **Extraction of the power corrections in the OPE of D-function** related to short strings. Corellation between short string and gluon condensate.

つくい

**6** Conclusions

# <span id="page-2-0"></span>Introduction

Zakharov's short string $^1$  leads to the corrections in annihilation cross-section (or Adler function). In Cornell potential

$$
V(r) \approx -\frac{4\alpha_s(r)}{3r} + kr
$$

the second part kr describes short string potential and leads to the correction  $\sim$ k  $\overline{Q^2}$ , in OPE the first correction to  $e^+e^-$ -annihilation cross-section is  $\sim \frac{\langle G_{\mu\nu}G^{\mu\nu}\rangle}{\Omega^4}$  $\frac{1}{Q^4}$ .  $[k] = [M^2]$ Our purpose is an accurate analysis of Adler function and search for existing correction with dimension 2.

 ${}^{1}$ K.G. Chetyrkin, S. Narison, V.I. Zakharov, "Short-distance tachyonic gluon mass and  $1/Q^2$  corrections", Nucl.Phys. B550 (199[9\) 3](#page-1-0)[53](#page-3-0)[-3](#page-1-0)[74](#page-2-0)  $ORO$ M. E. Kozhevnikovaln collaboration with: O. V. Teryaev A [Search for short strings in](#page-0-0) e<sup>+</sup>e<sup>-</sup>-annihilation

#### [Introduction](#page-1-0)

<span id="page-3-0"></span>The fitting of experimental cross-sections data on e<sup>+</sup>e<sup>−</sup>-ann**ihilation to hadron to hadrons** The calculation of D-function and the analysis of coefficients

## Introduction



Fig.: String potential from lattice QCD (M.I. [Po](#page-2-0)l[ika](#page-4-0)[rp](#page-2-0)[ov](#page-3-0) [e](#page-4-0)[t](#page-0-0) [a](#page-1-0)[l.](#page-4-0)[\)](#page-5-0)

E

 $299$ 

<span id="page-4-0"></span>Introduction

QCD description of  $e^+e^-$  -annihilation cross-section at low  $Q^2$  . Operator product expansion and condensates. Gluon and quark condensate and corrections:

$$
C_4 = \frac{2\pi^2}{3}\left\langle\frac{\alpha_s GG}{\pi}\right\rangle, \quad C_6 = \frac{448\pi^3}{27}\alpha_s \left\langle \bar{q}q\right\rangle^2 \approx -0.116 \text{ GeV}^6
$$

New condensate connected with Zakharov's short string is possible. Gluon field compose the string configuration and leads to confinement

 $200$ 

# <span id="page-5-0"></span>Construction of the model of the data

The using data is obtained on the detectors CMD, CMD-2, BaBar, SND, M3N, DM1, DM2, OLYA, GG2:

$$
e^{+}e^{-} \rightarrow \pi^{+}\pi^{-}
$$
 (CMD and OLYA detectors),  
\n
$$
e^{+}e^{-} \rightarrow 2\pi^{+}2\pi^{-}
$$
 (BaBar),  
\n
$$
e^{+}e^{-} \rightarrow \pi^{+}\pi^{-}2\pi^{0}
$$
 (OLYA, CMD2, SND, DM2, Frascati-ADONE-GAN  
\n
$$
e^{+}e^{-} \rightarrow 3\pi^{+}3\pi^{-}
$$
 (BaBar),  
\n
$$
e^{+}e^{-} \rightarrow 2\pi^{+}2\pi^{-}2\pi^{0}
$$
 (BaBar).  
\n
$$
\chi^{2}
$$
-functional:  
\n
$$
\chi^{2}(a_{1},...,a_{d}) = \frac{1}{N_{d.f.}} \sum_{n=1}^{N} \frac{(f_{exp}(s_{n}) - f_{th}(s_{n}; \{a_{1},...,a_{d}\}))^{2}}{\delta f_{exp}(s_{n})^{2}},
$$

 $QQ$ 

where  $\left\{\left(s_{i}, f_{\mathsf{exp}}(s_{i})\right)\right\}_{i=1,...,N}$  is an experimental points set,  $f_{\text{th}}(s; \{a_1, ..., a_d\})$  - the analytic function.

# Construction of the model of the data

The 3-resonance model was used, the form factor of each resonance was calculated according to the Breit-Wigner model.

$$
F^{\text{BW}}(s, m_V, \Gamma_V) = \frac{m_V^2(1 + d \cdot \Gamma_V/m_V)}{m_V^2 - s + f(s, m_V, \Gamma_V) - i \, m_V \Gamma_V(s)},
$$
  
\nwhere  $\Gamma_V(s) = \Gamma_V \left(\frac{k(s)}{k(m_V^2)}\right)^3$ ,  $k(s) = \frac{\sqrt{s - 4m_\pi^2}}{2}$ ,  
\n $f(s, m_V, \Gamma_V) = \Gamma_V \frac{m_V^2}{k(m_V^2)^3} \left[k^2(s)(h(s) - h(m_V^2)) - (s - m_V^2)k^2(m_V^2)h'(m_V^2)\right]$ ,  
\n $h(s) = \frac{2}{\pi} \frac{k(s)}{\sqrt{s}} ln(\frac{\sqrt{s} + 2 m_\pi}{2 m_\pi}), \quad h'(m_V^2) = h'(s)|_{s = m_V^2}$ ,

 $200$ 

there  ${\cal F}^{\rm BW}(0,m_V,\Gamma_V)=1$  automatically. The resonances  $\rho$ ,  $\omega$  and  $\rho'$ .

## <span id="page-7-0"></span>Construction of the model of the data

For cross-sections of the processes  $e^+e^- \rightarrow 2\pi^+2\pi^-,$  $e^+e^-\rightarrow\pi^+\pi^-2\pi^0$ ,  $e^+e^-\rightarrow2\pi^+2\pi^-2\pi^0$ , and  $e^+e^-\rightarrow3\pi^+3\pi^$ the description in the form of sum of three Gaussian curves, describing wide resonances, is assumed:

$$
F_{\text{Gauss}}\left(s,\{M_i,\sigma_i,\alpha_i\}\right)=\sum_{i=1}^3\,\alpha_i\,\mathrm{e}^{-(\sqrt{s}-M_i)^2/(2\sigma_i^2)}\,;
$$

$$
\sigma\left(s,\left\{M_i,\sigma_i,\alpha_i\right\}\right)[\mathsf{nb}] = \theta(s-4m_\pi^2)\,0.3839\cdot 10^6\,\mathsf{F}_\mathsf{Gauss}^2\,\frac{\pi\,\alpha_\mathsf{em}}{3s}\,\left(1-\frac{4m_\pi^2}{s}\right)^{3/2}
$$

.

# <span id="page-8-0"></span>Fitting. Results.



Fig.: Experimental and analytical dependencies of square pion form factor (left), of cross section (right) on the energy for the process  $e^+e^- \to \pi^+\pi^-$ ,  $\chi^2 = 1.05$ .

Data is taken from CMD and OLYA detectors<sup>2</sup>.

# <span id="page-9-0"></span>Fitting. Results.



Fig.: Experimental and analytical dependencies of cross section on the energy for the process  $e^+e^-\to 2\pi^+2\pi^-$ ,  $\chi^2=1.85$ . The fitting functions are taken as the sum of three Gaussian curves.

Data for  $e^+e^- \to 2\pi^+2\pi^-$  is taken from BaBar<sup>3</sup>.

 $3B$ . Aubert et al. (BABAR Collaboration) Phys. [Re](#page-8-0)v[.](#page-10-0) [D](#page-8-0)  $H$ [,](#page-10-0) [0](#page-4-0)[5](#page-5-0)[20](#page-14-0)[0](#page-15-0)[1](#page-4-0) [\(](#page-5-0)[2](#page-14-0)0[05](#page-0-0)[\).](#page-29-0)  $QQ$ M. E. Kozhevnikovaln collaboration with: O. V. Teryaev A. Search for short strings in  $e^+e^-$ -annihilation

# <span id="page-10-0"></span>Fitting. Results.



Fig.: Experimental and analytical dependencies of cross section on the energy for the process  $e^+e^-\to \pi^+\pi^-2\pi^0$ ,  $\chi^2=$  8.45.

Data for  $e^+e^- \to \pi^+\pi^-2\pi^0$  is taken from<sup>4</sup>.

<sup>4</sup>M. R. Whalley. J. Phys. G: Nucl. Part. Phys. 29,A1-A133 (2003), OLYA: L. M. Kurdadze et al. J. Exp. Theor. Phys. Lett. 43, 643-645 (1986), CMD2: R. R. Akhmetshin et al. Phys. Lett. B466, 392-402 (1999), ND: Dolinsky et al. , Phys. Rep. 202(1991) 99, OrsayDCI-DM2: B. Bisello et al. Preprint LAL-90-35 (1990), OrsayDCI-M3N: G. Cosme et al. Nucl. Phy[s. B](#page-9-0)[15](#page-11-0)[2,](#page-9-0) [2](#page-10-0)15[\(1](#page-5-0)[9](#page-4-0)[7](#page-15-0)9[\),](#page-5-0) [SN](#page-15-0)[D](#page-0-0). つくへ M. E. Kozhevnikovaln collaboration with: O. V.Teryaev A Search for short strings in e<sup>+</sup>e<sup>−</sup>-annihilation

# <span id="page-11-0"></span>Fitting. Results.



Fig.: Experimental and analytical dependencies of cross section on the energy for the processes  $e^+e^-\to 3\pi^+3\pi^-$  (left),  $\chi^2=$  0.62,  $e^+e^-\to 2\pi^+2\pi^-2\pi^0$  (right),  $\chi^2=1.03$ . The fitting functions are taken as the sum of three Gaussian curves.

Data is taken from BaBar <sup>5</sup>.

 $5B$ . Aubert et al. Phys. Rev. D73, 052003 (2006[\).](#page-10-0)  $\Box \rightarrow \Box \rightarrow \Box \rightarrow \Box$  $QQ$ M. E. Kozhevnikovaln collaboration with: O. V. Teryaev A. Search for short strings in  $e^+e^-$ -annihilation

# Fitting. Results.

Таблица: The fitting results for particular  $e^+e^-$ -annihilation channels



 $200$ 

 $d = 0.408 + 0.151$ Data from PDG:  $m_{\rho} = 0.77526 \pm 0.00025$  GeV;  $\Gamma_{\rho} = 0.1491 \pm 0.0008$  GeV;  $m_{\omega} = 0.78265 \pm 0.00012$  GeV;  $\Gamma_{\omega} = 0.00849 \pm 0.00008$  GeV;

## Fitting. Results.

#### Таблица: The fitting results for particular  $e^+e^-$ -annihilation channels



イロト イ母ト イヨト イヨト

 $2990$ 

э

<span id="page-14-0"></span>[Introduction](#page-1-0) The fitting of experimental cross-sections data on e<sup>+</sup>e<sup>−</sup>-annimidations at the power corrections at the power co<br>The calculation of *D-*function and the analysis of coefficients at the power corrections in the OPE of OP

# Fitting. Results.

Таблица: The fitting results for particular  $e^+e^-$ -annihilation channels



 $1.7.1$   $1.7.7$ 

イヨメ イヨメ

 $2990$ 

э

#### <span id="page-15-0"></span>R-ratio

By definition  $R$ -ratio is:

$$
R(s) = \frac{\sigma_{e^+e^- \to \text{hadrons}}(s)}{\sigma_{e^+e^- \to \mu^+ \mu^-}(s)}.
$$

The full  $R$ -ratio is equal to the sum of  $R$ -ratios of particular channels.

At  $s \leq s_0$  we use  $R(s)$ , obtained using experimental data, and at  $s > s_0$  we use the theoretical form.

 $200$ 

[Introduction](#page-1-0)

<span id="page-16-0"></span>The fitting of experimental cross-sections data on e<sup>+</sup>e<sup>−</sup>-ann**ihilation to hadron to hadrons** The calculation of D-function and the analysis of coefficients

# R-ratio



Fig.: The full R-ratio  $(R_{\text{exp}})$  in dependence on energy  $\sqrt{s}$  at  $\sqrt{s} \leq 3$  GeV (black), the experime[nta](#page-15-0)l data (blue) and the theoretical representati[on](#page-17-0)  $R_{\text{th}}(s)$  $R_{\text{th}}(s)$  $R_{\text{th}}(s)$  $R_{\text{th}}(s)$  $R_{\text{th}}(s)$  $R_{\text{th}}(s)$  $R_{\text{th}}(s)$  ([red](#page-29-0)[\).](#page-14-0)<br> $\epsilon_0 \approx 1.54^2 \text{ GeV}^2$  $s_0 \approx 1.54^2 \text{ GeV}^2$ 

つくへ

## <span id="page-17-0"></span>PT and APT

In ordinary Perturbaton Theory (PT) the non-physical pole (Landau-pole) exists because In $(Q^2/\Lambda^2)$  has singularity in  $Q=\Lambda,$ and running coupling has the form:

$$
\alpha_s(Q^2) = \frac{4\pi}{b_0} \frac{1}{\ln(Q^2/\Lambda^2)}.
$$

In Analytical Perturbaton Theory (APT) (Shirkov, Solovtsov) the coupling contains an additional term, excluding the pole:

$$
\mathcal{A}_s(Q^2) = \frac{4\pi}{b_0} \left[ \frac{1}{\ln(Q^2/\Lambda^2)} - \frac{\Lambda^2}{Q^2 - \Lambda^2} \right]
$$

.

つくへ

[Introduction](#page-1-0)

The fitting of experimental cross-sections data on e<sup>+</sup>e<sup>−</sup>-ann**ihilation to hadron to hadrons** The calculation of D-function and the analysis of coefficients

# PT and APT



Fig.: The ordinary (blue) and analytical (orange) running couplings in  $\frac{1}{18}$ . The ordinary (blue) and analytical (c  $-10<sup>-10</sup>$  $\equiv$ 

つくへ

# D-function

Adler function (D-function). The dispersion relation for D-function:

$$
D_{\text{Disp}}(Q^2) = Q^2 \int_0^\infty \frac{R_{\text{exp-th}}(s) ds}{(s+Q^2)^2}
$$

$$
R_{\text{exp-th}}(s) = R_{\text{exp}}(s) \,\theta(s < s_0) + R_{\text{th}}(s) \,\theta(s > s_0).
$$

The operator product expansion (OPE):

$$
D_{\text{PT+OPE}}(Q^2) = N_c \sum_q e_q^2 \left[ 1 + \frac{\alpha_s(Q^2)}{\pi} + \sum_{n \ge 1} \Gamma(n) \frac{c_n}{Q^{2n}} \right],
$$
  

$$
D_{\text{APT+OPE}}(Q^2) = N_c \sum_q e_q^2 \left[ 1 + \frac{\mathcal{A}_s(Q^2)}{\pi} + \sum_{n \ge 1} \Gamma(n) \frac{\tilde{c}_n}{Q^{2n}} \right], N_c = 3.
$$

The Borel transform. Sum rules.

$$
\Phi(M^2) = \hat{B}_{Q^2 \to M^2} [D(Q^2)] = \lim_{n \to \infty} \frac{(-Q^2)^n}{\Gamma(n)} \left[ \frac{d^n}{dQ^{2n}} D(Q^2) \right]_{Q^2 = nM^2}
$$

The Borel transform is applied to the both forms of  $D(Q^2)$ :

$$
\Phi_{\text{exp-th}}(M^2) = \int_0^\infty R_{\text{exp-th}}(s) \left(1 - \frac{s}{M^2}\right) e^{-s/M^2} \frac{ds}{M^2},
$$

$$
\Phi_{\text{PT+OPE}}(M^2) = \frac{3}{2} \left\{ \hat{B}_{Q^2 \to M^2} \left[ \frac{\alpha_s(Q^2)}{\pi} \right] + \frac{C_2}{M^2} + \frac{C_4}{M^4} + \frac{C_6}{M^6} \right\},\
$$

$$
\Phi_{\text{APT+OPE}}(M^2) = \frac{3}{2} \left\{ \hat{B}_{Q^2 \to M^2} \left[ \frac{\mathcal{A}_1(Q^2)}{\pi} \right] + \frac{\tilde{C}_2}{M^2} + \frac{\tilde{C}_4}{M^4} + \frac{\tilde{C}_6}{M^6} \right\}.
$$

The sum rules are:

$$
\Phi_{\text{PT+OPE}}(M^2) = \Phi_{\text{exp-th}}(M^2), \quad \Phi_{\text{APT+OPE}}(M^2) = \Phi_{\text{exp-th}}(M^2).
$$

 $200$ 

# The Borel transform. Sum rules.

The construction of the D-function using the data and subsequent application of the Borel transform leads to the **double smearing** of the data.

That method excludes the leading term in perturbative part (the Born contribution) in R-ratio, which is important in usual applications of QCD sum rules allowing one to observe the quark-hadron duality and get the accurate description of the properties of hadrons. At the same time, that method allows one to extract non-perturbative corrections (including that due to short strings) more accurately.

[Introduction](#page-1-0)

The fitting of experimental cross-sections data on e<sup>+</sup>e<sup>−</sup>-ann**ihilation to hadron to hadrons** The calculation of  $D$ -function and the analysis of coefficients

## Results:  $PT \cdot \Lambda = 0.25$  GeV

TABLE III: The fitting results for different intervals of  $M^2$  in the PT, statistical errors are only in  $\chi^2$ ,  $\Lambda = 0.25$  GeV. In the fifth column the  $\sigma$ -level where  $C_2 = 0$  is shown. In the sixth column the (anti)correlation between gluon condensate (g.c) and  $C_2$ ,  $g.c.(GeV^4) = A(GeV^2) \cdot C_2(GeV^2) + B(GeV^4)$ , is shown.

Range of $M^2$ , GeV	$C_2$ , $\text{GeV}^2$	$\frac{<\alpha_sGG>}{<\alpha_eV^4}$	$\chi^2$	$\sigma$ -level	(Anti)correlation
[10/20, 160/20]	$-0.093 \pm 0.054$	$0.025 \pm 0.008$	0.758	3	$-0.153 C_2 + 0.011$
[11/20, 120/20]	$-0.076 \pm 0.052$	$0.023 \pm 0.008$	0.553	3	$-0.154C_2 + 0.011$
[12/20, 100/20]	$-0.065 \pm 0.052$	$0.021 + 0.008$	0.406	$\overline{2}$	$-0.154C_2 + 0.011$
[13/20, 90/20]	$-0.058 \pm 0.053$	$0.020 \pm 0.008$	0.323	$\overline{2}$	$-0.154C_2 + 0.011$
[14/20, 80/20]	$-0.052 \pm 0.053$	$0.019 \pm 0.008$	0.265		$-0.155C_2 + 0.011$
[15/20, 70/20]	$-0.047 \pm 0.052$	$0.018 \pm 0.008$	0.212		$-0.155C_2 + 0.011$
[16/20, 60/20]	$-0.042 \pm 0.051$	$0.017 \pm 0.008$	0.156		$-0.155 C_2 + 0.011$
[17/20, 50/20]	$-0.037 \pm 0.048$	$0.016 \pm 0.007$	0.097		$-0.156 C_2 + 0.011$
[18/20, 40/20]	$-0.032 \pm 0.044$	$0.016 \pm 0.007$	0.041		$-0.156 C_2 + 0.011$
[19/20, 30/20]	$-0.027 \pm 0.036$	$0.015 \pm 0.006$	0.005		$-0.156 C_2 + 0.011$

Fig.: The fitting results for different intervals of  $M^2$  in PT,  $\Lambda=$  0.25 GeV

イロメ イ母メ イヨメ イヨメー

性

 $\Omega$ 

[Introduction](#page-1-0)

The fitting of experimental cross-sections data on e<sup>+</sup>e<sup>−</sup>-ann**ihilation to hadron to hadrons** The calculation of  $D$ -function and the analysis of coefficients

## Results:  $APT \cdot \Lambda = 0.25$  GeV

TABLE IV: The fitting results for different intervals of  $M^2$  in the APT, statistical errors are only in  $\chi^2$ ,  $\Lambda = 0.25$  GeV. In the fifth column the  $\sigma$ -level where  $C_2 = 0$  is shown. In the sixth column the (anti)correlation between gluon condensate (g.c) and  $C_2$ ,  $G_c(GeV^4) = A(GeV^2) \cdot C_2(GeV^2) + B(GeV^4)$ , is shown.

Range of $M^2$ , GeV	$C_2$ , $\text{GeV}^2$	$\sqrt{\frac{<\alpha_sGG>}{<\alpha_sQ}}$ , GeV <sup>4</sup>	$\chi^2$	$\sigma$ -level	(Anti)correlation
[10/20, 160/20]	$-0.067 \pm 0.053$	$0.026 \pm 0.008$	0.723	$\overline{2}$	$-0.159C_2 + 0.016$
[11/20, 120/20]	$-0.048 \pm 0.053$	$0.023 \pm 0.008$	0.508		$-0.159C_2 + 0.016$
[12/20, 100/20]	$-0.036 \pm 0.054$	$0.021 \pm 0.009$	0.368		$-0.159C_2 + 0.016$
[13/20, 90/20]	$-0.028 \pm 0.057$	$0.020 \pm 0.009$	0.296		$-0.159C_2 + 0.016$
[14/20, 80/20]	$-0.022 \pm 0.058$	$0.019 \pm 0.009$	0.244		$-0.159C_2 + 0.016$
[15/20, 70/20]	$-0.017 \pm 0.059$	$0.018 \pm 0.009$	0.195		$-0.159C_2 + 0.016$
[16/20, 60/20]	$-0.012 \pm 0.058$	$0.017 \pm 0.009$	0.142		$-0.159C_2 + 0.016$
[17/20, 50/20]	$-0.006 \pm 0.055$	$0.017 \pm 0.009$	0.086		$-0.160 C_2 + 0.016$
[18/20, 40/20]	$-0.000 \pm 0.051$	$0.016 \pm 0.008$	0.035		$-0.160 C_2 + 0.016$
[19/20, 30/20]	$0.006 \pm 0.045$	$0.015 \pm 0.007$	0.004		$-0.160 C_2 + 0.016$

Fig.: The fitting results for different intervals of  $M^2$  in APT,  $\Lambda = 0.25$  GeV

イロメ イ母メ イヨメ イヨメー

性

 $200$ 

#### Results: Results: PT vs APT,  $\Lambda = 0.25$  GeV

The regions  $\chi^2 \leq \chi^2_{\sf min} + 1$ ,  $\chi^2 \leq \chi^2_{\sf min} + 2$  and  $\chi^2 \leq \chi^2_{\sf min} + 3$  and the regions of existing data on gluon condensate (horizontal lines).



Fig.: Regions for PT (left), APT (right),  $\Lambda = 0.25$  GeV. The different ellipses are for different ranges on  $M^2$ 

#### Results: Results: PT vs APT,  $\Lambda = 0.35$  GeV

The regions  $\chi^2 \leq \chi^2_{\sf min} + 1$ ,  $\chi^2 \leq \chi^2_{\sf min} + 2$  and  $\chi^2 \leq \chi^2_{\sf min} + 3$  and the regions of existing data on gluon condensate (horizontal lines).



Fig.: Regions for PT (left), APT (right),  $\Lambda = 0.35$  GeV. The different ellipses are for different ranges on  $M^2$ 

医骨盆 医骨盆

#### Results: Results: PT vs APT,  $\Lambda = 0.45$  GeV

The regions  $\chi^2 \leq \chi^2_{\sf min} + 1$ ,  $\chi^2 \leq \chi^2_{\sf min} + 2$  and  $\chi^2 \leq \chi^2_{\sf min} + 3$  and the regions of existing data on gluon condensate (horizontal lines).



Fig.: Regions for PT (left), APT (right),  $\Lambda = 0.45$  GeV. The different ellipses are for different ranges on  $M^2$ 

**SACTO STATE OF ST** 

# Analysis

- $\bullet$  A new analysis is performed.  $C_2$  has negative sign and its compatibility to zero depends on the interval of  $\mathcal{M}^{2}$  , value of Λ and may happen only for lowest values of local gluon condensate. Dimension 2 operator is more close to zero for APT.
- (Anti)Corellation between short strings and local gluon condensate is found.
- We changed Λ and take valued 0.25 GeV, 0.35 GeV and 0.45 GeV. The  $C_2$  region is shifted from zero to negative values more at larger Λ.

 $\mathcal{A} \leftarrow \mathcal{A} \leftarrow \mathcal{A} \leftarrow \mathcal{A} \leftarrow \mathcal{A} \leftarrow \mathcal{A}$ 

# Conclusions

- The resonance contribution fitting model is developed, the Adler function with Borelization is obtained. Double smearing of the data - D-function and Borel transform.
- Short string strongly depends on gluon condensate. The range of  $M^2$  is varied. At different ranges of of  $M^2$  there are a bit different results of  $C_2$  and gluon condensate, however the properties are common - (anti)corellation between  $C_2$  and gluon condensate.
- Short string also depends on choice of either standard  $(PT)$  or modified  $(APT)$  pQCD. The APT results are shifted towards zero of  $C_2$  in comparison with PT results. APT make results more similar to well-known.

イロト イタト イモト イモト

 $\Omega$ 

# <span id="page-29-0"></span>Thank you for your attention!

M. E. Kozhevnikovaln collaboration with: O. V. Teryaev A. Search for short strings in  $e^+e^-$ -annihilation  $200$