

# Brane inflation models

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Dvali & Tye (PLB 1999)

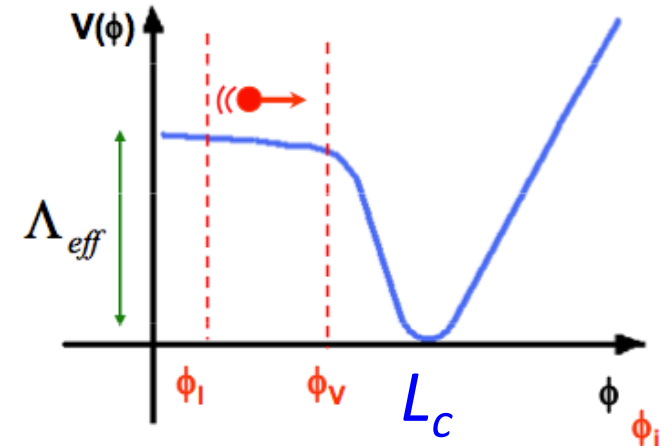
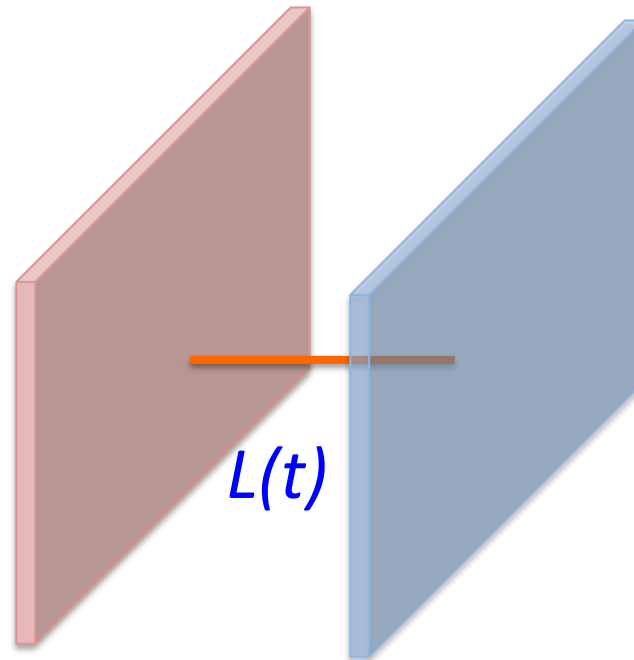
Randall and R. Sundrum (PRL 1999)

Goldberger & Wise (PRL 1999)

Kallosh, Linde, Roest & Yamada (JHEP 2017)

# Brane inflation

$$\phi \approx M_p^2 L(t)$$



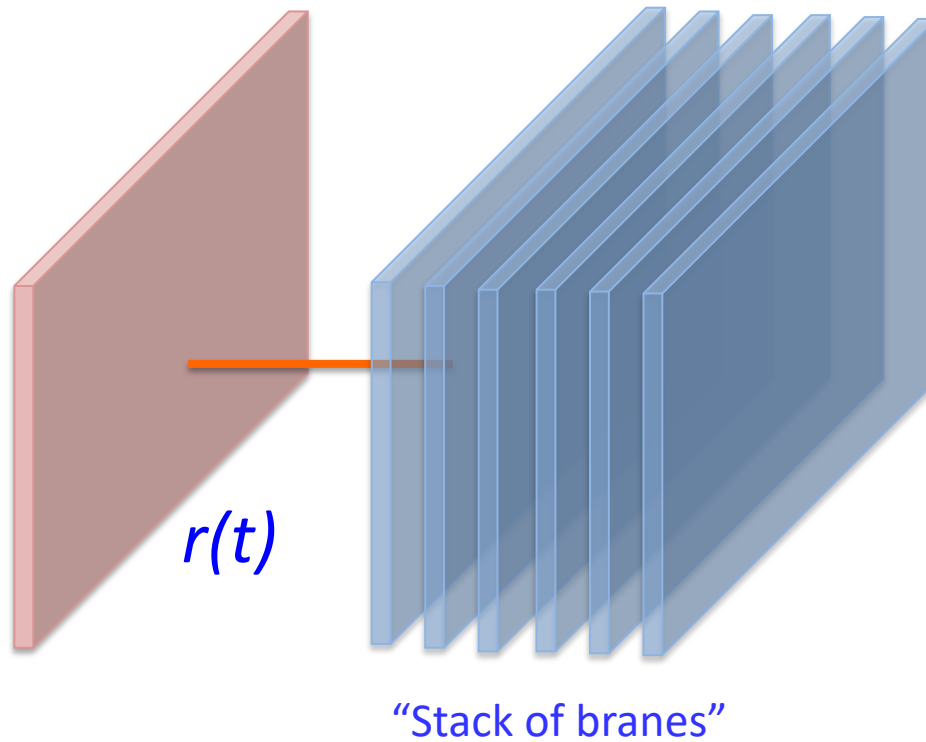
hidden brane

visible brane

# Brane inflation

Dvali & Tye's scenario

$$\phi \approx M_p^2 r(t)$$



# Brane inflation

Dvali & Tye's scenario

$\phi \approx M_p^2 r(t)$ ,  $N = \text{number of extra dimensions}$

$$V(r) = T(\alpha - f(r/r_0) + b_i \frac{e^{-m_i r}}{r^{N-2}} + \frac{c}{r^{N-2}} + kr)$$

*Contributions from:*

- 1) Modes (massive/massless) localized on the brane
- 2) Yukawa suppressed potential from exchange of the massive bulk modes
- 3) Exchange of the light bulk modes, like graviton or gauge
- 4) Confining potential  $\sim kr$  due to the strings stretching

# Brane inflation

Dvali & Tye's scenario

**Dvali-Tye** “We can find several types of interactions between a brane and a stack of brane inflation”.

Next ...

**Extended-Dvali-Tye** “We can effectively correct the Dvali-Tye scenario by including tunneling resonant modes”.

# Extended “Dvali-Tye” model



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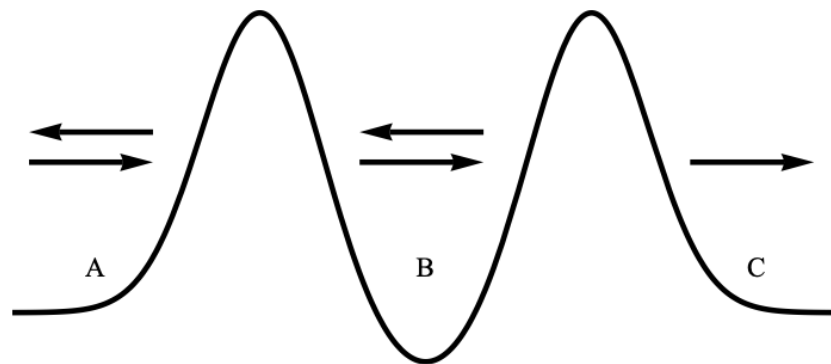
A domain wall description of brane inflation and observational aspects

R.M.P. Neves<sup>a</sup>, F.F. Santos<sup>a</sup>, F.A. Brito<sup>a,b,\*</sup>



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“Naïve WKB”

$$T = T_{A \rightarrow B} = T_{B \rightarrow C}$$

$$T_{A \rightarrow B} = K e^{-S}$$

$$T_{A \rightarrow C} \approx T^2$$

Doubly suppressed !

Tye and Wohns, 2009;

Saffin, Padilla and Copeland, 2008

Sarang, Shiu and Shlaer, 2008

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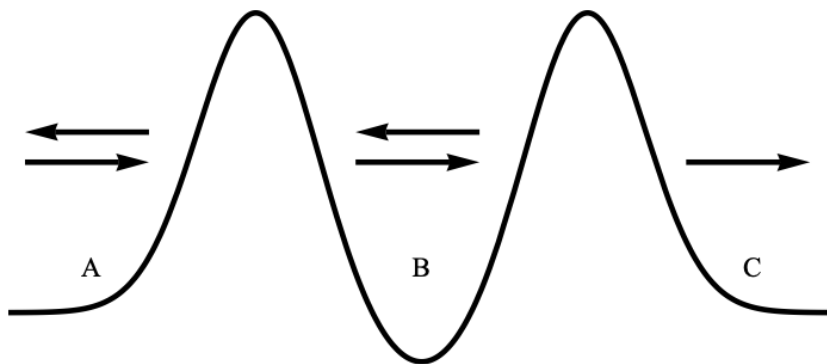
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“Naive WKB”

$$T = T_{A \rightarrow B} = T_{B \rightarrow C}$$

$$T_{A \rightarrow B} = K e^{-S}$$

$$T_{A \rightarrow C} \approx T^2$$

“Resonant tunneling phenomenon”

$$T_{A \rightarrow C} \approx T/2$$

Tye and Wohns, 2009;

Saffin, Padilla and Copeland, 2008

Sarang, Shiu and Shlaer, 2008

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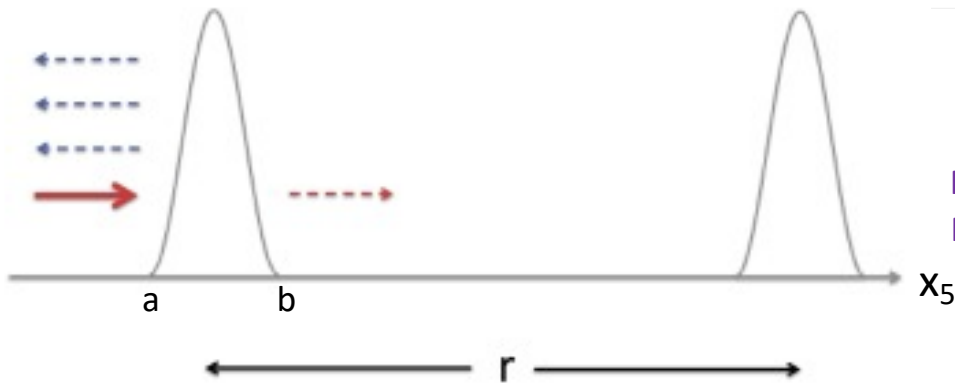
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## Transmission coefficient

$$T = \frac{4}{\left(4\theta^2 + \frac{1}{4\theta^2}\right) \cos^2 L + 4 \sin^2 L}$$

## Quantities dependent on the potential

$$L = \int_{-r}^r k(x_5) dx_5, \quad \theta = \exp\left(\int_a^b \kappa(x_5) dx_5\right)$$

Neves, Santos, Brito, 2020

Merzbacher, 1998



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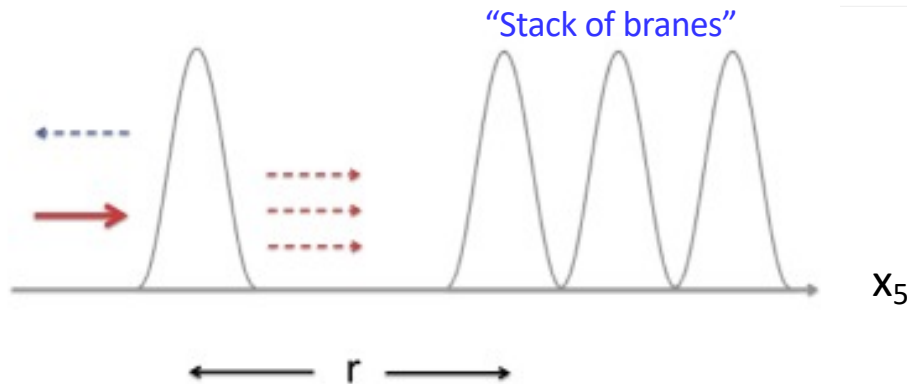
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Induced force in terms of the reflection coefficient  $R=1-T$ :

$$F_r = M_{wall} \ddot{r}(t) \simeq KR = -\frac{\partial U}{\partial r}$$

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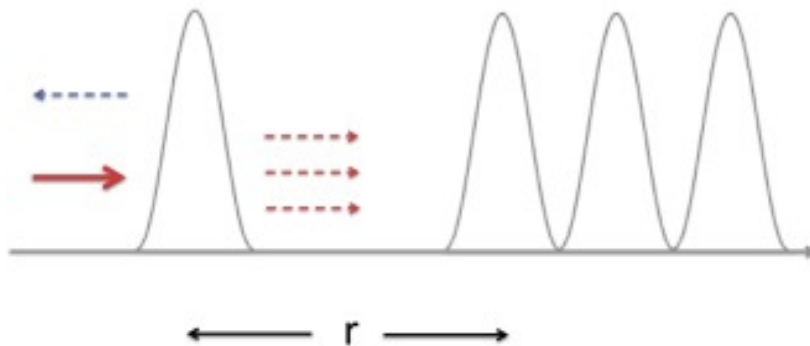
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“Stack of branes”



$x_5$

The induced potential on the brane

$$U(r) = Kr_0 \arctan\left(\frac{r}{r_0}\right) - Kr$$

Neves, Santos, Brito, 2020

Vilenkin and Shellard, 1994

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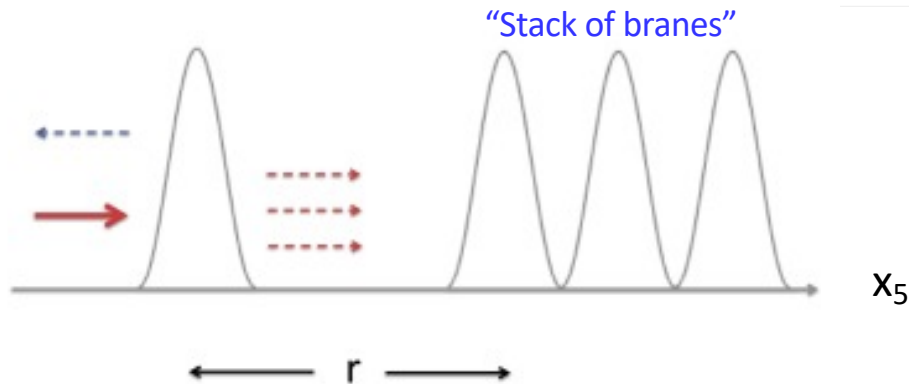
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Gravitational and/or electromagnetic linear contribution:

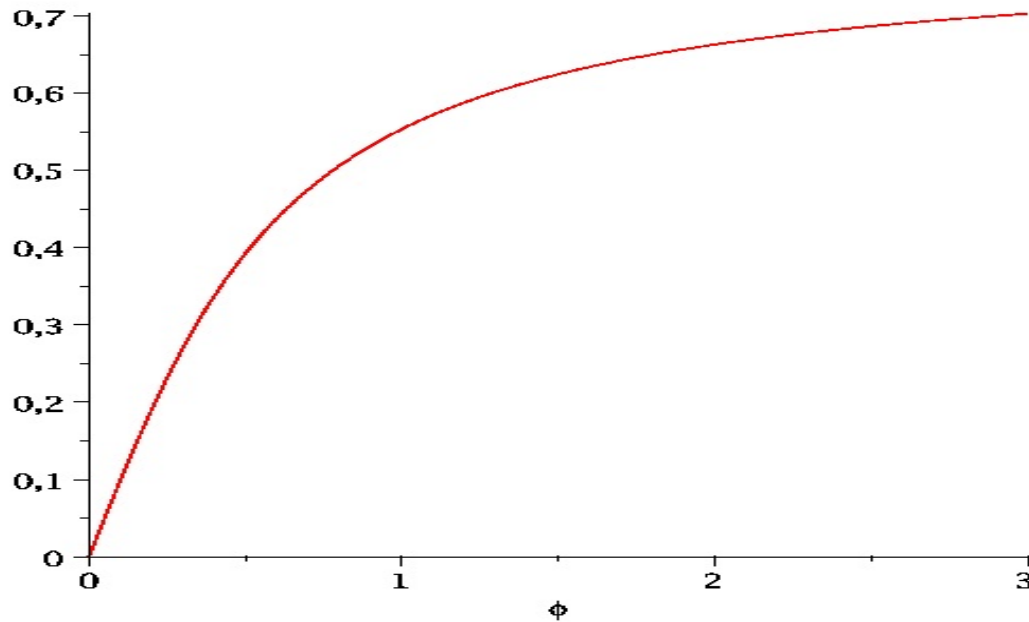
$$U_{eff}(r) = U(r) + \mathcal{E}_0 r$$

The effective induced potential on the brane

$$U_{eff}(r) = K r_0 \arctan\left(\frac{r}{r_0}\right)$$

Neves, Santos, Brito, 2020

# Extended “Dvali-Tye” model



Adapting the coordinates suitably:

$$\sqrt{T_{wall}} r(t) \longleftrightarrow \phi(t)$$

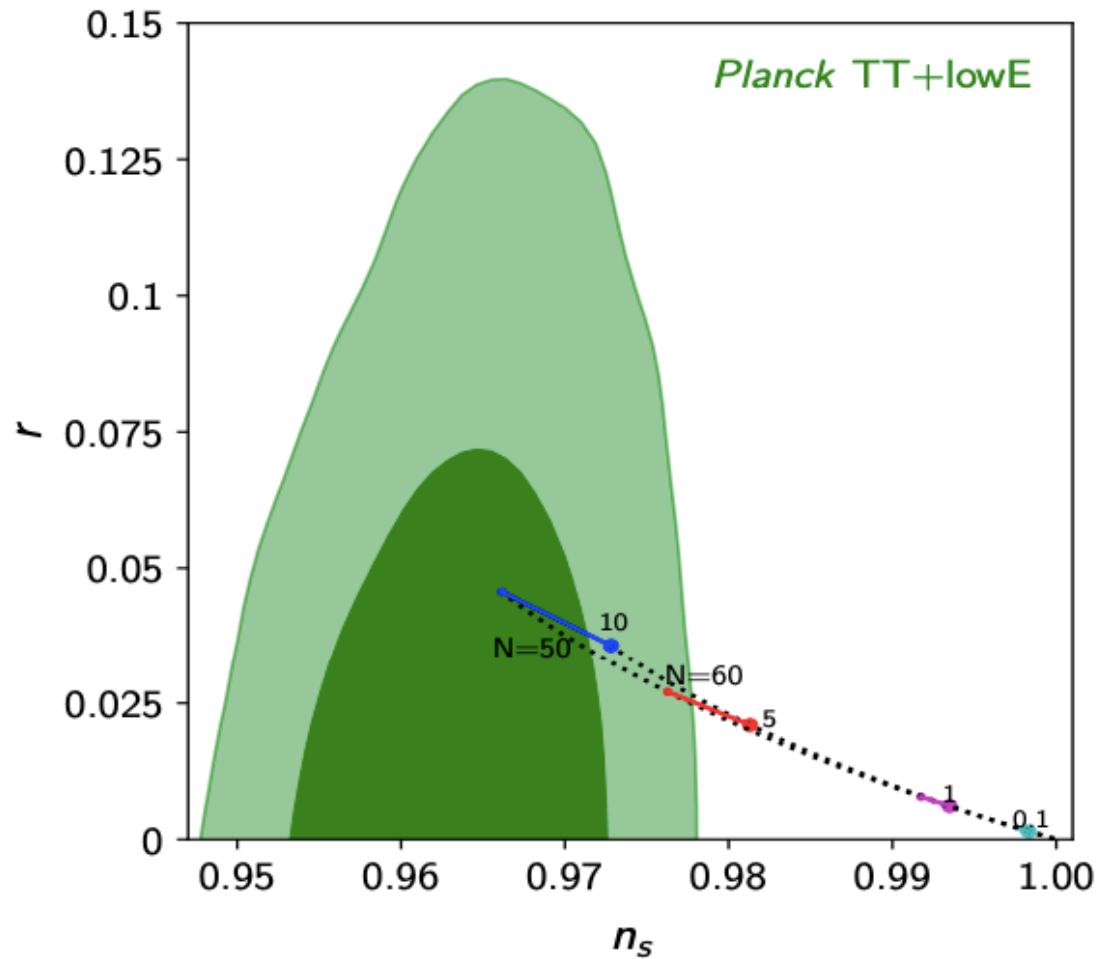
$$\beta = \sqrt{T_{wall}} r_0$$

Thus the induced inflaton potential on the brane is

$$V(\phi) = K\beta \arctan\left(\frac{\phi}{\beta}\right)$$

Neves, Santos, Brito, 2020

# Extended “Dvali-Tye” model

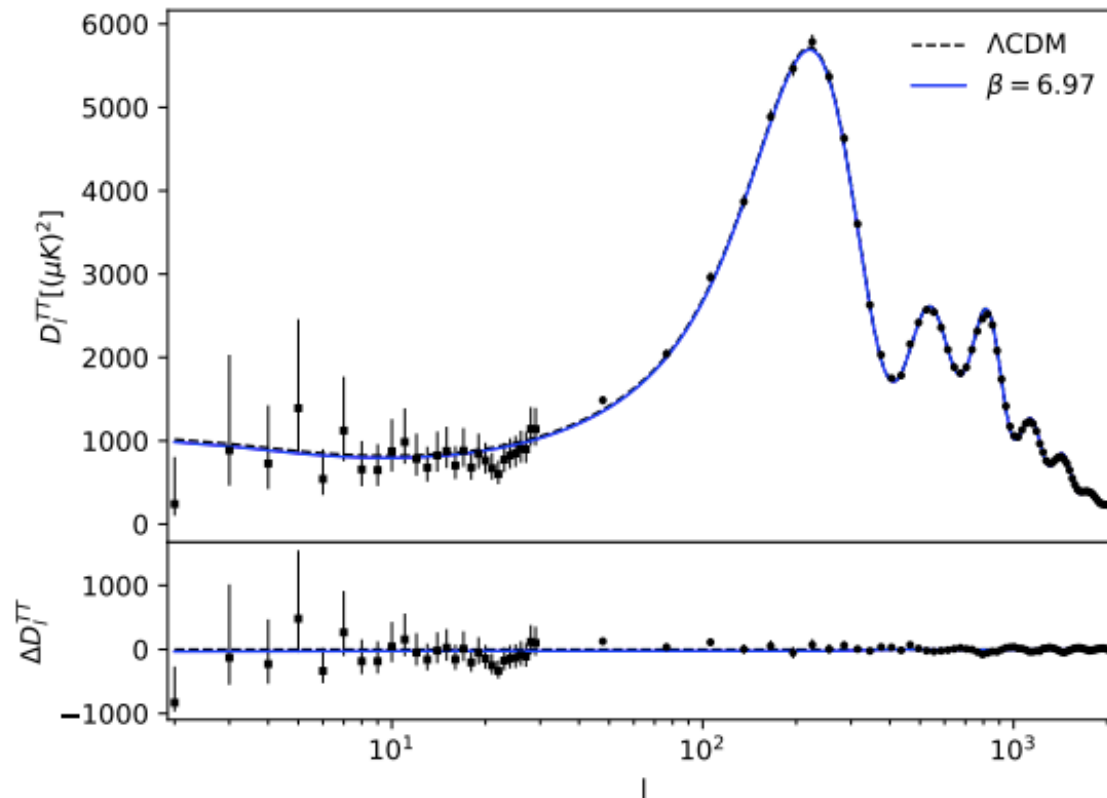


$$V(\phi) = K\beta \arctan\left(\frac{\phi}{\beta}\right)$$

Santos da Costa, Alcaniz, Brito & Neves (2020)

## Extended “Dvali-Tye” model

Temperature power spectrum for **Arctan** potential



# Conclusions

1. Our analysis shows that the predictions of the **Arctan model - inflation model** are very similar to the ones of the  $\Lambda$ CDM model (they agree at 68.3% C.L.)
2. The **Arctan model** is in agreement with the current observational data and can be derived from a 'fundamental theory' such as supergravity
3. Large values of  $\beta$  are in agreement with both **observational data and radion stabilization** at finite size in brane inflation scenario
4. Similar agreements were found in supergravity induced  $\beta$ -exponential inflation models studied recently (**Brito et al, JCAP 2018**).

Thank you !

