Prospects for Hyperon Physics with BESIII

VIS

Tord Johansson

for the BESIII collaboration

Workshop on Many Manifestations of Nonpertubative QCD Cabury, São Paolo 2018



Hyperons are a laboratory for strong interaction physics.

- Production
- Structure
- Spectroscopy
- Decay pattern
- Interaction
- •
- •





"How are baryons affected by replacing light quarks by strange quarks?"



"What is the role of spin?"



The parity-violating weak hyperon decay gives access to spin observables. $\Lambda \rightarrow p + \pi^-$

 $I(\cos\theta_p) = N(1 + \alpha_{\Lambda} P_{\Lambda} \cos\theta_p)$

P = Polarisation,

 α = decay asymmetry parameter



Hyperon decays acts as a Polarimeter



without polarisation filter

with polarisation filter

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Spin observables, upolarised beam and target



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$$P_y = Polarisation$$

 $C_{ij} =$ Spin correlations



Electromagnetic Form Factors

 Electromagnetic Form Factors (EMFF) of hadrons are among the most basic quantities containing information about hadron internal structure. They provide access to the spatial charge and magnetisation distributions.





Not much is experimentally known about hyperon EM structure. Basically only static properties.

Why?

The short hyperon life-times makes it impossible to measure Space-Like (SL) FF's.

=> Only hyperon Time-Like (TL) EMFF's are accessible in experiments. Small cross sections.



 e^+e^- -collisions are currently the best way to investigate hyperon EMFF's.



 $e^+e^- \leftrightarrow \overline{B}B$





Non-zero momentum of final state particles at threshold.



Baryon vertex matrix element: $\Gamma^{\mu} = F_1^B(q^2)\gamma^{\mu} + \frac{\kappa}{2M_B}F_2^B(q^2)i\sigma^{\mu\nu}q_{\nu}$ The Dirac ($F_1(q^2)$) and Pauli ($F_2(q^2)$) EMFF's is related to the charge (G_E) and magnetization (G_M) (Sachs) EMFF's via the relations:

$$G_E = F_1 - \tau F_2$$
; $\tau = \frac{q^2}{4M_B^2}$
 $G_M = F_1 + F_2$

$$G_E(0) = Z$$
$$G_M(0) = Z + \kappa = \mu_B$$

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• Time-like FF's are complex due to inelasticity:

$$\operatorname{Re}\left[G_{E}(q^{2})G_{M}^{*}(q^{2})\right] = \left|G_{E}(q^{2})\right| \left|G_{M}(q^{2})\right| \cos \Delta \phi$$
$$\operatorname{Im}\left[G_{E}(q^{2})G_{M}^{*}(q^{2})\right] = \left|G_{E}(q^{2})\right| \left|G_{M}(q^{2})\right| \sin \Delta \phi$$

 $\Delta \phi$ = the relative phase between G_E and G_M .

Three observables determine the Time-Like Form Factors.

- A relative phase between G_E and G_M gives polarisation effects on the final state even if the initial state is unpolarised.



The differential cross section in the one-photon exchange picture is given by:

$$\frac{d\sigma}{d\cos\theta} = \frac{\alpha^2 \beta C}{4q^2} \left(\left| G_M \right|^2 \left(1 + \cos^2 \theta \right) + \frac{1}{\tau} \left| G_E \right|^2 \sin^2 \theta \right);$$

$$\tau = \frac{q^2}{4m_B^2}, \ \beta = \sqrt{1 - 1/\tau}, \ C = \text{Coulomb factor} = \frac{y}{(1 - e^{-y})}, \ y = \pi \alpha / \beta$$



The differential cross section at one energy is sufficient to extract the modulii of $|G_E|$ and $|G_M| \stackrel{\text{\tiny CO}}{=}$.



Increasingly difficult to measure $|G_E|$ as q^2 increases due to the $1/\tau$ term \cong .

Only ${}^{3}S_{1}$ and ${}^{3}D_{1}$ waves are allowed in the final state.



pQCD predicts:

$$\lim_{Q^2 \to \infty} G_{E,M}(Q^2)_{Q^2 \to \infty} = \lim_{q^2 \to \infty} G_{E,M}(q^2) \quad \Leftrightarrow \text{ Space-Like FF} = \text{Time-Like FF}.$$

$$\Rightarrow \Rightarrow \text{ Time-Like FF become real.}$$

$$G_{E,M}(q^2) \propto q^{-4}$$



Proton EMFF features



pQCD region reached at $Q \approx 6$ Gev/c²?

$$\mathsf{TL} |F_p| = 2\mathsf{x} \mathsf{SL} |F_p| ?$$

Sign of a diquark-quark structure of the proton? Kroll et al., PLB 316 (1993) 546



Data (so far) has not allowed for a statistically significant extraction of the modulii of $|G_E|$ and $|G_M|$ for hyperons. One therefore defines an effective Form Factor from the total cross section:

$$\sigma_{tot} = \frac{4\pi\alpha^2\beta C}{3q^2} \left[\left| G_M \right|^2 + \frac{\left| G_E \right|^2}{2\tau} \right] \Longrightarrow \left| G_{eff} \right| = \left(\frac{2\tau \left| G_M \right|^2 + \left| G_E \right|^2}{2\tau + 1} \right)^{\frac{1}{2}} \implies \left| G_{eff} \right| \propto \sqrt{\sigma_{tot}}$$





 $e^+e^- \rightarrow Y\overline{Y}$ @ CLEO-c

 $G_E = 0$ assumed

"Good" diquark (Λ) VS, "Bad" diquark (Σ⁰) ? Jaffe & Wilczek, PRL 91 (2003)





PRD 96 (2017) 092004



Final State Interaction (FSI)

Haidenbauer et al., NPA 929 (2014) 102

90 17

120

60

0

0

30





Difficult to reconcile BESIII and PS185 data.



More data needed! (BESIII!)



Threshold enhancement in $e^+e^- \rightarrow \Lambda_c^+\Lambda_c^-$

Strong influence from X(4630)



PRL 101 (2008) 172001



PRL 120 (2018) 111101



 $e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-$



Shape of theory curve primarily given by X(4630)

Dai et al., PRD 96 (2017) 116001



More data needed! (BESIII!)







First measurement of $|G_E/G_M|$ for Λ_c^+

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√s [MeV]	IG _E /G _M I
4574.5	$1.10 \pm 0.14 \pm 0.07$
4599.5	$1.23 \pm 0.06 \pm 0.03$

PRL 120 (2018) 111101 22



What is known about apart from Effective FF's for Λ hyperons?

BaBar \approx 200 events in total \diamondsuit

$$1.16 < \frac{|G_E|}{|G_M|} < 2.72 \quad q < 2.4 \text{ GeV}$$
$$0 < \frac{|G_E|}{|G_M|} < 1.37 \quad 2.4 \le q < 2.8 \text{ GeV}$$
$$-0.76 < \sin\Delta\phi < 0.98$$



Practically nothing.Until now!



Recap

The differential cross section in the one-photon exchange picture is given by:

$$\frac{d\sigma}{d\cos\theta} = \frac{\alpha^2 \beta C}{4q^2} \left(\left| G_M \right|^2 \left(1 + \cos^2 \theta \right) + \frac{1}{\tau} \left| G_E \right|^2 \sin^2 \theta \right);$$

$$\tau = \frac{q^2}{4m_B^2}, \ \beta = \sqrt{1 - 1/\tau}, \ C = \text{Coulomb factor} = \frac{y}{(1 - e^{-y})}, \ y = \pi \alpha / \beta$$

The polarisation arises from the interference between the ${}^{3}S_{1}$ and ${}^{3}D_{1}$ waves in the final state.

$$e^{+}e^{-} \rightarrow \Lambda\overline{\Lambda} \quad \hat{k}_{1} \xrightarrow{\theta_{0}} \hat{y}_{\overline{\lambda}}}$$

$$P_{y} = \frac{1}{\overline{\alpha}} \langle \cos \theta_{\overline{p}_{x}} \rangle$$

$$P_{y} = -\frac{\sin 2\theta \operatorname{Im} \left[G_{E} G_{M}^{*} \right] / \sqrt{\tau}}{\left(\left| G_{E} \right|^{2} \sin 2\theta \right) / \tau + \left| G_{M} \right|^{2} (1 + \cos^{2} \theta)} = -\frac{\sin 2\theta \sin \Delta \phi / \tau}{R \sin^{2} \theta + (1 + \cos^{2} \theta) / R}; \quad R = \left| \frac{G_{E}}{G_{M}} \right|$$

$$P_{z} = \frac{\sin 2\theta \operatorname{Im} \left[G_{E} G_{M}^{*} \right] / \sqrt{\tau}}{\left(\left| G_{E} \right|^{2} \sin 2\theta \right) / \tau + \left| G_{M} \right|^{2} (1 + \cos^{2} \theta)} = -\frac{\sin 2\theta \sin \Delta \phi / \tau}{R \sin^{2} \theta + (1 + \cos^{2} \theta) / R}; \quad R = \left| \frac{G_{E}}{G_{M}} \right|$$

$$P_{z} = \frac{\sin 2\theta \operatorname{Re} \left[G_{E} G_{M}^{*} \right] / \sqrt{\tau}}{\left(\left| G_{E} \right|^{2} \sin 2\theta \right) / \tau + \left| G_{M} \right|^{2} (1 + \cos^{2} \theta)} = -\frac{\sin 2\theta \cos \Delta \phi / \tau}{R \sin^{2} \theta + (1 + \cos^{2} \theta) / R}; \quad R = \left| \frac{G_{E}}{G_{M}} \right|$$

$$P_{z} = 2 \text{ gives modulus of the phase } \phi$$

$$P_{z} = -\frac{\sin 2\theta \operatorname{Re} \left[G_{E} G_{M}^{*} \right] / \sqrt{\tau}}{\left(\left| G_{E} \right|^{2} \sin 2\theta \right) / \tau + \left| G_{M} \right|^{2} (1 + \cos^{2} \theta)} = -\frac{\sin 2\theta \cos \Delta \phi / \tau}{R \sin^{2} \theta + (1 + \cos^{2} \theta) / R}; \quad Nuov. \operatorname{Cim}. A109(96)241$$

$$P_{z} = 2 \operatorname{gives the sign of the phase } \phi$$

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$$P_{y} = -\frac{\sin 2\theta \sin \Delta \phi / \tau}{R \sin^{2} \theta + (1 + \cos^{2} \theta) / R}; \quad R = \frac{|G_{E}|}{|G_{M}|} \qquad \qquad C_{zx} = -\frac{\sin 2\theta \cos \Delta \phi / \tau}{R \sin^{2} \theta + (1 + \cos^{2} \theta) / R}$$

$$\sqrt{s} = 2.386 \text{ GeV}$$

R=1R=1 $|\Delta \phi| = 15, 45, 60$ $|\Delta \phi| = +15, +45, +60$



Need statistics to determine C_{zx} , i.e the sign of $\Delta \phi \cong$. sufficient to add the data for -1<cos θ <0 and 0<cos θ <1 \bigoplus .





A multivariate parameterisation have been derived by G.Fäldt & A.Kupsc* to make **maximum use** of $e^+e^- \rightarrow \Lambda \overline{\Lambda}$ **exclusive data**:

$$W(\xi) = F_{0}(\xi) + \eta F_{5}(\xi) + \sqrt{1 - \eta^{2}} \sin(\Delta \Phi) (\alpha_{\Lambda} F_{3}(\xi) + \alpha_{\bar{\lambda}} F_{4}(\xi)) + \sqrt{1 - \eta^{2}} \sin(\Delta \Phi) (\alpha_{\Lambda} F_{3}(\xi) + \alpha_{\bar{\lambda}} F_{4}(\xi)) + \sqrt{1 - \eta^{2}} \cos(\Delta \Phi) F_{2}(\xi) + \eta F_{6}(\xi)); \quad \xi = (\theta, \theta_{1}, \phi_{1}, \theta_{2}, \phi_{2}), \quad \eta = \frac{\tau - R^{2}}{\tau + R^{2}}$$

$$F_{0}(\xi) = 1$$

$$F_{1}(\xi) = \sin^{2} \theta \sin \theta_{1} \sin \theta_{2} \cos \phi_{1} + \cos^{2} \theta \cos \theta_{1} \cos \theta_{2}$$

$$F_{2}(\xi) = \sin \theta \cos \theta (\sin \theta_{1} \cos \theta_{2} \cos \phi_{1} + \cos \theta_{1} \sin \theta_{2} \cos \phi_{2})$$

$$F_{3}(\xi) = \sin \theta \cos \theta \sin \theta_{1} \sin \phi_{1}$$

$$F_{4}(\xi) = \sin \theta \cos \theta \sin \theta_{2} \sin \phi_{2}$$

$$F_{5}(\xi) = \cos^{2} \theta$$

$$F_{6}(\xi) = \cos \theta_{1} \cos \theta_{2} - \sin^{2} \theta \sin \theta_{1} \sin \theta_{2} \sin \phi_{1} \sin \phi_{2}$$

- Allows for an unbinned ML fit.
- No need for acceptance corrections.
 (except for an overall normalisation factor)

*PLB 772(2017) 16 27



Energy scan 2014-2015

• World leading data sample between 2.0 and 3.08 GeV.





- Invariant mass cut: $|M(p\pi) - M_{\Lambda}| < 0.006 \text{ GeV/c}^2$
- $N_{signal} = 555 \pm 24$

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200

150

100

50

0 1.1

1.11

Events / 1MeV

 $N_{sidebands} = 14 \pm 4$







• Data fitted with an unbinned ML fit using the PDF from Fäldt & Kupsc.

$$W(\xi) = F_0(\xi) + \eta F_5(\xi) + \sqrt{1 - \eta^2} \sin(\Delta \Phi) \left(\alpha_{\Lambda} F_3(\xi) + \alpha_{\overline{\Lambda}} F_4(\xi) \right) + \alpha_{\Lambda} \alpha_{\overline{\Lambda}} \left(F_1(\xi) + \sqrt{1 - \eta^2} \cos(\Delta \Phi) F_2(\xi) + \eta F_6(\xi) \right); \ \xi = (\theta, \theta_1, \phi_1, \theta_2, \phi_2), \ \eta = \frac{\tau - R^2}{\tau + R^2}$$



- Data fitted with an unbinned ML fit using the PDF from Fäldt & Kupsc.
- Result:

$$R = 0.94 \pm 0.16 \pm 0.03 (\pm 0.02 \alpha_{\Lambda})$$

$$\Delta \Phi = 42^{o} \pm 16^{o} \pm 8^{o} (\pm 6^{o} \alpha_{\Lambda})$$

R€SⅢ

*PRD 76 (2007) 092006.

- Most precise result on *R* (BaBar: *R* = 1.73^{+0.99}_{-0.57} in 2.23 < *q* < 2.40 GeV*)
- First conclusive result on $\Delta \Phi$

 $(BaBar: -0.76 < sin\Delta\Phi < 0.98 \text{ in } 2.23 < q < 2.80 \text{ GeV}^*)$





The polarisation is induced by the interference between ${}^{3}S_{1}$ and ${}^{3}D_{1}$ waves between the final state hyperons.

 $e^+e^- \rightarrow Y\overline{Y}$ are perfect reactions to learn about the hyperon-antihyperon interaction.



Predictions have been made for *R* and the phase using potentials employed for the $\overline{p}p \rightarrow \Lambda \overline{\Lambda}$ reaction by Haidenbauer & Meißner.







The formalism of Fäldt & Kupsc has also been applied to BESIII data on

 $e^+e^- \to \gamma^* \to J/\psi \to \Lambda\bar{\Lambda}$



 $\frac{d\Gamma}{d\cos\theta} \propto 1 + \eta_{\psi}\cos^2\theta$





$$W(\xi) = F_0(\xi) + \eta F_5(\xi) + \sqrt{1 - \eta^2} \sin(\Delta \Phi) \left(\alpha_{\Lambda} F_3(\xi) + \alpha_{\overline{\Lambda}_{p,\overline{n}}} F_4(\xi) \right) + \sqrt{1 - \eta^2} \sin(\Delta \Phi) \left(\alpha_{\Lambda} F_3(\xi) + \alpha_{\overline{\Lambda}_{p,\overline{n}}} F_4(\xi) \right) + \alpha_{\Lambda} \alpha_{\overline{\Lambda}_{p,\overline{n}}} \left(F_1(\xi) + \sqrt{1 - \eta^2} \cos(\Delta \Phi) F_2(\xi) + \eta F_6(\xi) \right); \ \xi = (\theta, \theta_1, \phi_1, \theta_2, \phi_2), \ \eta = \frac{\tau - R^2}{\tau + R^2}$$



 α_{-}

 α_+

 $ar{lpha}_0$

 A_{CP}

 $\bar{\alpha}_0/\alpha_+$

△Φ=42.3°±0.6°±0.5°



$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013	PDG	CD an up up at in u
$-0.758 \pm 0.010 \pm 0.007$	$-0.71 {\pm} 0.08$	PDG	CP asymmetry.
$-9.692 \pm 0.016 \pm 0.006$	_		$A_{} = \frac{\alpha + \alpha_+}{\alpha + \alpha_+}$
$-0.006\pm0.012\pm0.007$	0.006 ± 0.021	PDG	$\alpha_{CP} = \alpha_{-} - \alpha_{+}$
$0.913 \pm 0.028 \pm 0.012$	_		





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Parameters	This work	Previous results	
η_w	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027	BESIII
$\Delta \Phi$ (rad)	$0.740 \pm 0.010 \pm 0.008$	_	
α_{-}	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013	PDG
$lpha_+$	$-0.758 \pm 0.010 \pm 0.007$	$-0.71 {\pm} 0.08$	PDG
$ar{lpha}_0$	$-9.693 \pm 0.016 \pm 0.006$	_	
A_{CP}	$-0.006 \pm 0.012 \pm 0.007$	0.006 ± 0.021	PDG
$ar{lpha}_0/lpha_+$	$0.913 \pm 0.028 \pm 0.012$	_	

First: Phase measurement between G_M^{ψ} and G_E^{ψ} $\overline{\alpha}_0$ decay asymmetry parameter

 $\alpha_{\Lambda \to p\pi^-}$ decay parameter is measured to be (17±3)% larger than the PDG value (> 5 σ)

Improved upper limit on A_{CP}

 $\overline{\alpha}_{_0}$ / $\alpha_{_+}$ deviates 3 σ from isospin symmetry prediction



No theoretical predictions exist for the phase and and $R(\eta_{\psi})$ for

$$e^+e^- \to \gamma^* \to J / \psi \to \Lambda \overline{\Lambda}$$



The floor is open for theorists!



Prospects and conclusions

BESIII has taken data at 10 energies from $\Lambda\overline{\Lambda}$ threshold to 2.9 GeV.

To come: Effective FF's for $\Sigma^0, \Sigma^+, \Xi^-$ + transition FF for $\Lambda\Sigma^0$.

Published data on $J/\psi, \psi(2S) \rightarrow Y\overline{Y}$ have, so far, focused on Branching Ratios and hyperon angular distributions based on $1.3x10^9 J/\psi$ and $0.45x10^9 J/\psi(2S)$ events from BESIII. There is a lot more to be analysed here!

A non-zero phase between spin 1/2 hyperons allows for a determination of their decay parameters and CP violation tests in the baryon sector.



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Prospects and conclusions

The multivariate formalism has now been extended in Uppsala to handle J/ψ decays to spin 3/2 + 3/2, 3/2 + 1/2 hyperons and 1/2 + 1/2 including decay chains.

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Decay mode	Events	$\mathcal{B}(imes 10^{-4})$
$J/\psi \to \Lambda\Lambda$	440675 ± 670	$19.43 \pm 0.03 \pm 0.33$
$\psi(2S) \to \Lambda \bar{\Lambda}$	31119 ± 187	$3.97 \pm 0.02 \pm 0.12$
$J/\psi \to \Sigma^0 \bar{\Sigma}^0$	111026 ± 335	$511.64 \pm 0.04 \pm 0.23$
$\psi(2S) \to \Sigma^0 \bar{\Sigma}^0$	6612 ± 82	$2.44 \pm 0.03 \pm 0.11$
$J/\psi \to \Sigma (1385)^0 \overline{\Sigma} (1385)^0$	102762 ± 852	10.71 ± 0.09
$J/\psi \to \Xi^0 \bar{\Xi}^0$	134846 ± 437	11.65 ± 0.04
$\psi(2S) \rightarrow \Sigma(1385)^0 \overline{\Sigma}(1385)^0$	2214 ± 148	0.69 ± 0.05
$\psi(2S) \to \Xi^0 \bar{\Xi}^0$	10839 ± 123	2.73 ± 0.03
$J/\psi \rightarrow \Xi^- \bar{\Xi}^+$	42811 ± 231	10.40 ± 0.06
$J/\psi \to \Sigma(1385)^- \bar{\Sigma}(1385)^+$	42595 ± 467	10.96 ± 0.12
$J/\psi \rightarrow \Sigma(1385)^+ \overline{\Sigma}(1385)^-$	52523 ± 596	12.58 ± 0.14
$\psi(2S) \to \Xi^- \bar{\Xi}^+$	5337 ± 83	2.78 ± 0.05
$\psi(2S) \rightarrow \Sigma(1385)^{-} \overline{\Sigma}(1385)^{+}$	1375 ± 98	0.85 ± 0.06
$\psi(2S) \rightarrow \Sigma(1385)^+ \overline{\Sigma}(1385)^-$	1470 ± 95	0.84 ± 0.05

Available data samples from BESIII

Potential data samples from BESIII

	$\mathcal{B}(\times 10)$	$)^{-4})$
$J/\psi \to \Xi(1530)^-\bar{\Xi}^+$	$5.9 \pm$	1.5
$J/\psi \to \Xi (1530)^0 \bar{\Xi}^0$	$3.3 \pm$	1.4
$J/\psi \to \Sigma(1385)^- \bar{\Sigma}^+$	$3.1 \pm$	0.5
$\psi(2S) \to \Omega^- \bar{\Omega}^+$	$0.47~\pm$	0.10

≈ 5x10⁹ J/ψ events are now collected @ BESIII





There is a lot more to come!

Stay posted!!





Antiproton-proton reactions are a hyperon factory via $\overline{p}p \rightarrow \overline{Y}Y$ reactions, both for ground state and excited hyperon.



- Strong interaction processes \Rightarrow High cross sections.
- Baryon number = $0 \Rightarrow$ No extra kaons needed.
 - \Rightarrow Low energy threshold.



- Same pattern in Y and \overline{Y} channels \hookrightarrow Consistency.



Fanda

Antihyperons/hyperon-pairs are accessible up to < 2740 MeV/c², i.e. up to $\Xi_c^* \Xi_c^*$.

