

# Working Group 3

Reunião de 22/05/24

Alberto Martinez

Fernando Navarra

Renato Higa

Kanchan Khemchandani

WG3 : aprender física de hadrons no LHC (QCD, QGP, CGC, espectros...)

Sub-produto: melhorar o nível de discussão dentro do grupo e do IFUSP

Sub-grupo: produção de exóticos em colisões AA periféricas e no EIC  
(Fernando Sobrinho, Celsina Azevedo, Luciano Abreu, Carlos Bertulani)

Sub-grupo: produção de exóticos em colisões AA centrais.  
(Luciano Abreu, Alberto M. Torres)

Sub-grupo: busca da junção bariônica  
(Fernando Navarra, Richard Terra)

Sub-grupo: distribuição de multiplicidades e CGC  
(Fernando Navarra, Guilherme Germano, Henrique M. Fontes)

Sub-grupo: estrutura de exóticos  
(Alberto M. Torres, Renato Higa, Kanchan Khemchandani, Breno Agatão)

O que aconteceu entre 05/24 e 10/24 ?

# 5 Artigos Publicados

inspirehep.net

(os que antes estavam submetidos)

## Emergence of Koba-Nielsen-Olsen scaling in multiplicity distributions in jets produced at the LHC #1

G.R. Germano (Sao Paulo U.), F.S. Navarra (Sao Paulo U.), G. Wilk (NCBJ, Warsaw), Z. Wlodarczyk (Jan Kochanowski U.) (Jun 7, 2024)

Published in: *Phys.Rev.D* 110 (2024) 3, 034026 • e-Print: 2406.04856 [hep-ph]

 pdf  DOI  cite  claim  reference search  0 citations

## Production of meson molecules in ultraperipheral heavy ion collisions #2

F.C. Sobrinho (Sao Paulo U.), L.M. Abreu (Sao Paulo U. and Bahia U.), C.A. Bertulani (Texas A-M, Commerce and Darmstadt, Tech. Hochsch.), F.S. Navarra (Sao Paulo U.) (May 4, 2024)

Published in: *Phys.Rev.D* 110 (2024) 3, 034037 • e-Print: 2405.02645 [hep-ph]

 pdf  DOI  cite  claim  reference search  2 citations

## $X(3872)$ to $\psi(2S)$ yield ratio in heavy-ion collisions #3

L.M. Abreu (Bahia U. and Sao Paulo U.), F.S. Navarra (Sao Paulo U.), H.P.L. Vieira (Bahia U.) (Jan 20, 2024)

Published in: *Phys.Rev.D* 110 (2024) 1, 014011 • e-Print: 2401.11320 [hep-ph]

 pdf  DOI  cite  claim  reference search  2 citations

## Can a femtoscopic correlation function shed light on the nature of the lightest charm axial mesons? #4

K.P. Khemchandani (Sao Paulo State U.), Luciano M. Abreu (Sao Paulo U. and Bahia U.), A. Martinez Torres (Sao Paulo U.), F.S. Navarra (Sao Paulo U.) (Dec 18, 2023)

Published in: *Phys.Rev.D* 110 (2024) 3, 036008 • e-Print: 2312.11811 [hep-ph]

 pdf  DOI  cite  claim  reference search  5 citations

## Interaction of exotic states in a hadronic medium: the $Z_c(3900)$ case #5

L.M. Abreu (Bahia U. and Sao Paulo U.), R.O. Magalhães (Bahia U.), F.S. Navarra (Bahia U.), H.P.L. Vieira (Sao Paulo U.) (Oct 28, 2023)

Published in: *J.Phys.G* 51 (2024) 9, 095003 • e-Print: 2310.18747 [hep-ph]

 pdf  DOI  cite  claim  reference search  2 citations

## Hadronic scattering effects on $\psi(2S)$ suppression in relativistic heavy-ion collisions

#1

L.M. Abreu (Bahia U. and Sao Paulo U.), F.S. Navarra (Sao Paulo U.), H.P.L. Vieira (Bahia U.) (Sep 19, 2024)

e-Print: [2409.12755](#) [hep-ph]

 pdf  cite  claim

 reference search  0 citations

## Nuclear Fragmentation at the Future Electron-Ion Collider

#2

C.A. Bertulani, Y. Kucuk, F.S. Navarra (Aug 19, 2024)

e-Print: [2408.10157](#) [nucl-th]

 pdf  cite  claim

 reference search  0 citations

## Heavy $K^*$ mesons with open charm from $KD^{(*)}D^*$ interactions

#1

Xiu-Lei Ren, K.P. Khemchandani, A. Martínez Torres (Sep 24, 2024)

e-Print: [2409.16281](#) [hep-ph]

 pdf  cite  claim

 reference search  0 citations

## A study of the $\phi N$ correlation function

#2

Luciano M. Abreu (Bahia U.), Philipp Gubler (JAEA, Ibaraki and Sao Paulo U.), K.P. Khemchandani (Sao Paulo U.), A. Martinez Torres (Sao Paulo U.), Atsushi Hosaka (JAEA, Ibaraki and Sao Paulo U. and Osaka U., Res. Ctr. Nucl. Phys.) (Sep 8, 2024)

e-Print: [2409.05170](#) [hep-ph]

 pdf  cite  claim

 reference search  0 citations

# 1 Publicação em Proceedings

**How the hadron gas affects  $X(3872)$  and  $\psi(2S)$  production in heavy ion collisions**

*Luciano M. Abreu<sup>1,\*</sup>, Fernando S. Navarra<sup>1,\*\*</sup>, and Hildeson P.L. Vieira<sup>1,\*\*\*</sup>*

Proceedings of the QCD@Work- International Workshop on QCD - Theory and Experiment (2024); 18-21/6/24 Trani, Itália. EPJ Web of Conferences (F. Navarra)

# 4 Participações em Conferências

Hadron spectroscopy and the new unexpected resonances, 22-28/9/24, Paraty, RJ (F. Navarra, R. Higa, A. Martinez)

IV Encontro de Primavera da SBF, 24-27/9/24, Belo Horizonte, MG (A. Martinez)

## 4 Teses Concluidas

Nathalia Fukase (mestrado - Kanchan Khemchandani)

Vinicius B. B. Ader (mestrado - Renato Higa)

Murilo S. de Godoy (mestrado - Renato Higa)

Fernando César Sobrinho (mestrado - Fernando Navarra)

## Organização de Eventos Científicos

Advances in QCD at the LHC and the EIC, 9-15/11/2025, Paraty, RJ  
(Fernando Navarra)

# Qualitativamente

Sub-grupo: produção de exóticos em colisões AA UPC e no EIC :

Refinamento do cálculo da seção de choque de produção do estado ligado D+D-

Extensão para o EIC

(ver apresentação da Celsina Azevedo)

Estudo de fragmentação nuclear em UPC e no EIC

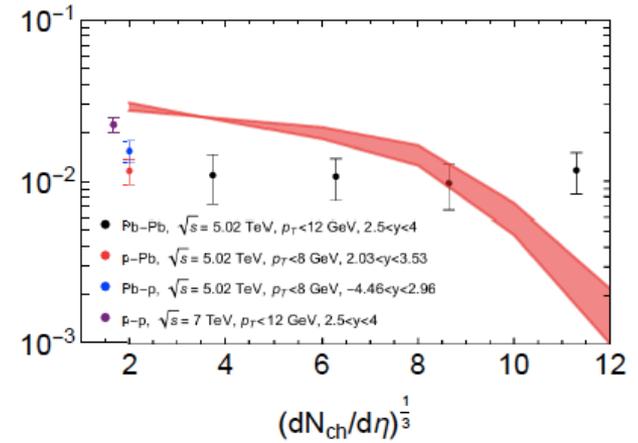
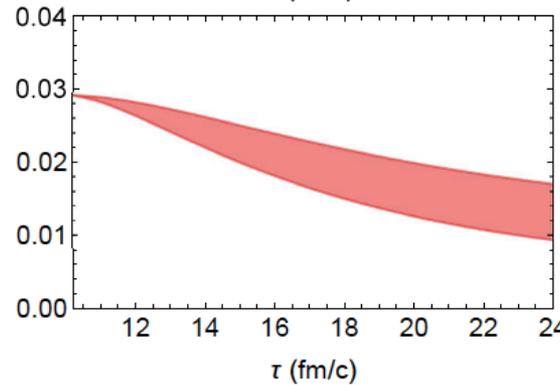
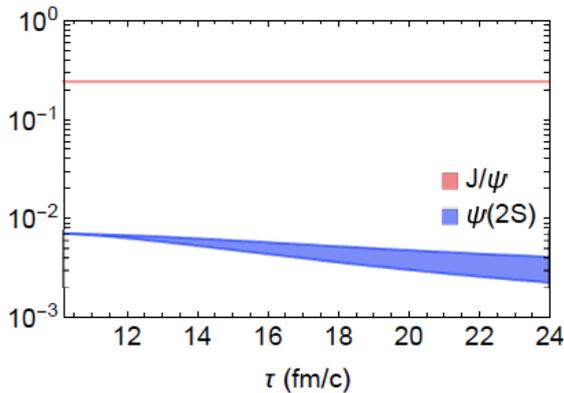
Nuclear Fragmentation at the Future Electron-Ion Collider

C.A. Bertulani, Y. Kucuk, F.S. Navarra (Aug 19, 2024)

e-Print: 2408.10157 [nucl-th]

# Sub-grupo: produção de exóticos em colisões AA centrais

Extensão do cálculo  $X(3972)/\Psi(2S) \rightarrow \Psi(2S)/J/\psi$



## Femtoscopia

A study of the  $\phi N$  correlation function

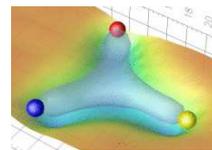
#2

Luciano M. Abreu (Bahia U.), Philipp Gubler (JAEA, Ibaraki and Sao Paulo U.), K.P. Khemchandani (Sao Paulo U.), A. Martinez Torres (Sao Paulo U.), Atsushi Hosaka (JAEA, Ibaraki and Sao Paulo U. and Osaka U., Res. Ctr. Nucl. Phys.) (Sep 8, 2024)

e-Print: 2409.05170 [hep-ph]

(ver apresentação do Alberto Martinez Torres)

## Sub-grupo: busca da junção bariônica



Produção de charmonium em pp e pA

(ver apresentação do Richard Terra)

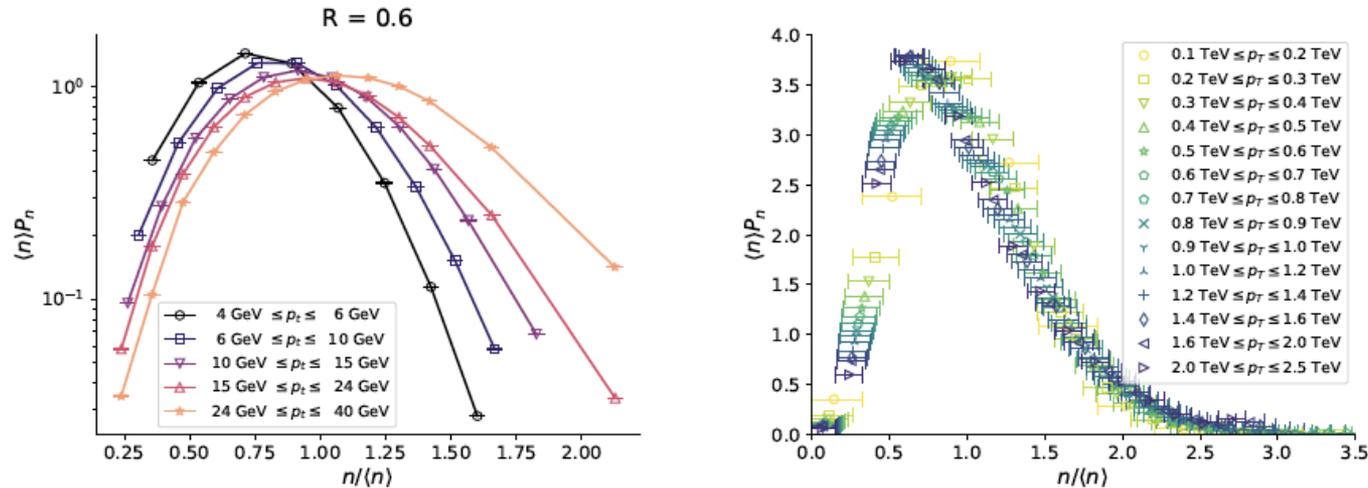
# Sub-grupo: distribuição de multiplicidades e CGC

## Scaling de KNO em jatos (Guilherme Germano)

### Emergence of Koba-Nielsen-Olsen scaling in multiplicity distributions in jets produced at the LHC

G.R. Germano (Sao Paulo U.), F.S. Navarra (Sao Paulo U.), G. Wilk (NCBJ, Warsaw), Z. Włodarczyk (Jan Kochanowski U.) (Jun 7, 2024)

Published in: *Phys.Rev.D* 110 (2024) 3, 034026 • e-Print: 2406.04856 [hep-ph]

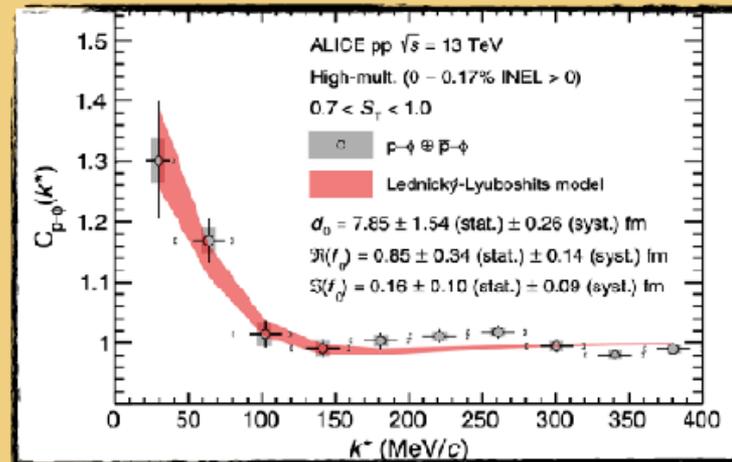


Separação da física soft e semi-hard nas distribuições de multiplicidade

(ver apresentação do Henrique M. Fontes)

# $\phi N$ CORRELATION FUNCTION

ALICE Collaboration,  
Phys. Rev. Lett 127,  
172301 (2021)

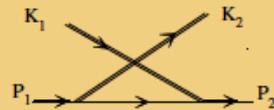
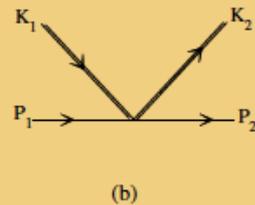
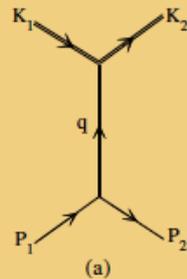


- OZI rule:  $\phi N$  interaction biased (weak interaction: distinct quark content)  $\implies$  Studies of  $\phi$  photo-production data suggest weak  $\phi N$  interaction.
- Lattice QCD [Hatsuda et al., PRD106,074507(2022)]:  $\phi N$  interaction in Spin 3/2 is attractive (they use  $\phi - N$  currents, and neglect explicit coupled channels). Spin 1/2: too many coupled channels (complicated).
- Analysis of the  $\phi N$  correlation function without coupled channels and a phenomenological  $\phi N$  potential [Chizzali et al., PLB 848,138358 (2024)]: They use the spin 3/2 scattering length obtained by lattice in their  $V_{3/2}$  potential and fit the spin 1/2 parameters in  $V_{1/2} \implies$  They find that spin 1/2  $\phi N$  interaction is attractive (bound state with  $\simeq 13$ -60 MeV of binding).

# MODEL

- Khemchandani et al., Phys. Rev. D83,114041 (2011)

$\rho N, \omega N, \phi N, K^* \Lambda, K^* \Sigma, \pi N, K \Sigma, K \Lambda, \eta N$       Hidden Local  
 $N^*(1535)[J^P = 1/2^-], N^*(1650)[J^P = 1/2^-]$       symmetry ( Bando  
 $N^*(1700)[J^P = 3/2^-], N^*(2100)[J^P = 3/2^-]$       and collaborators)



$$V_{VB}^{I,S} = V_{t,VB}^{I,S} + V_{s,VB}^{I,S} + V_{u,VB}^{I,S} + V_{CT,VB}^{I,S}$$

$$\begin{aligned}
 \mathcal{L}_{VB} = & -g \left\{ \langle \bar{B} \gamma_\mu \left[ \mathbb{V}_8^\mu, B \right] \rangle + \langle \bar{B} \gamma_\mu B \rangle \langle \mathbb{V}_8^\mu \rangle \right. \\
 & + \frac{1}{4M} \left( F \langle \bar{B} \sigma_{\mu\nu} \left[ \mathbb{V}_8^{\mu\nu}, B \right] \rangle + D \langle \bar{B} \sigma_{\mu\nu} \left\{ \mathbb{V}_8^{\mu\nu}, B \right\} \rangle \right) \\
 & \left. + \langle \bar{B} \gamma_\mu B \rangle \langle \mathbb{V}_0^\mu \rangle + \frac{C_0}{4M} \langle \bar{B} \sigma_{\mu\nu} \mathbb{V}_0^{\mu\nu} B \rangle \right\}
 \end{aligned}$$

Spin-dependent interactions,  
 Vector-Baryon and Pseudosclar-  
 Baryon as coupled channels

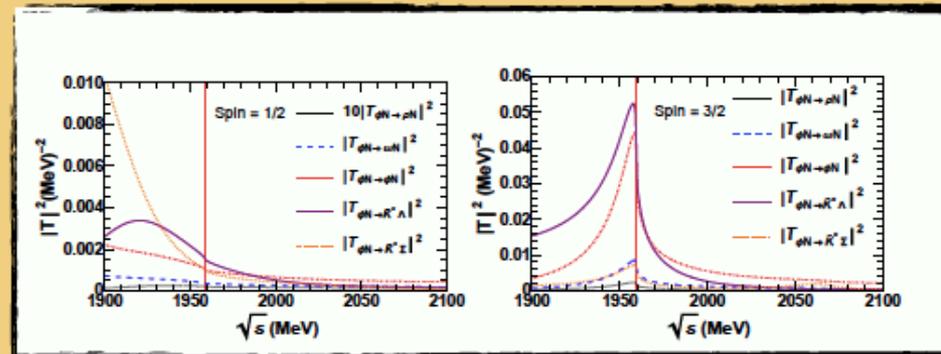
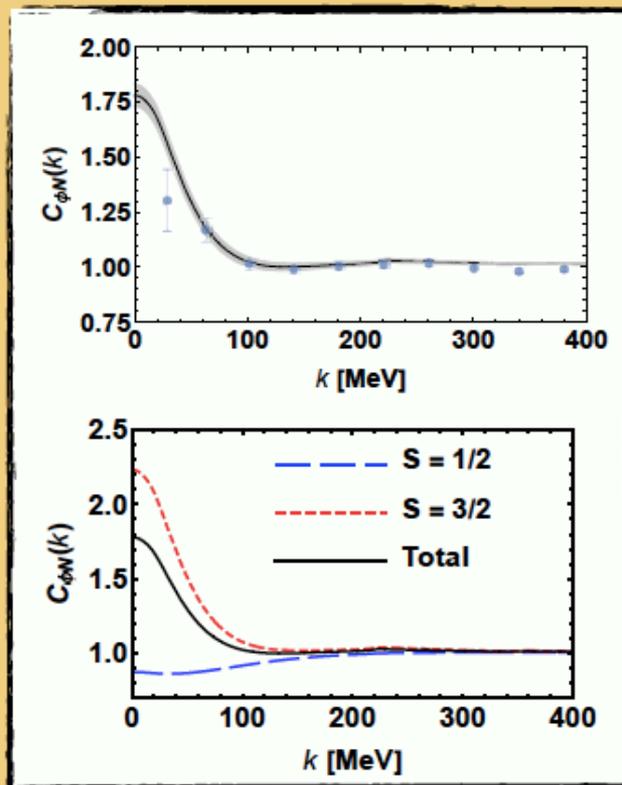
# RESULTS

- Correlation functions of two hadrons: femtoscopy

$$C_{\phi N}(k) = \frac{1}{3}C_{\phi N}^{(\frac{1}{2})}(k) + \frac{2}{3}C_{\phi N}^{(\frac{3}{2})}(k)$$

Data points : S. Acharya, et al., Alice collaboration, Phys. Rev. Lett. 127, 172301 (2021)

Coupled channel analysis for  $\phi N$ : correlation function cannot distinguish the existence or not of a  $\phi N$  quasi-bound state



Abreu, Gubler, Khemchandani, Martínez Torres, Hosaka, submitted to Phys. Lett. B (arXiv: 2409.05170v1)

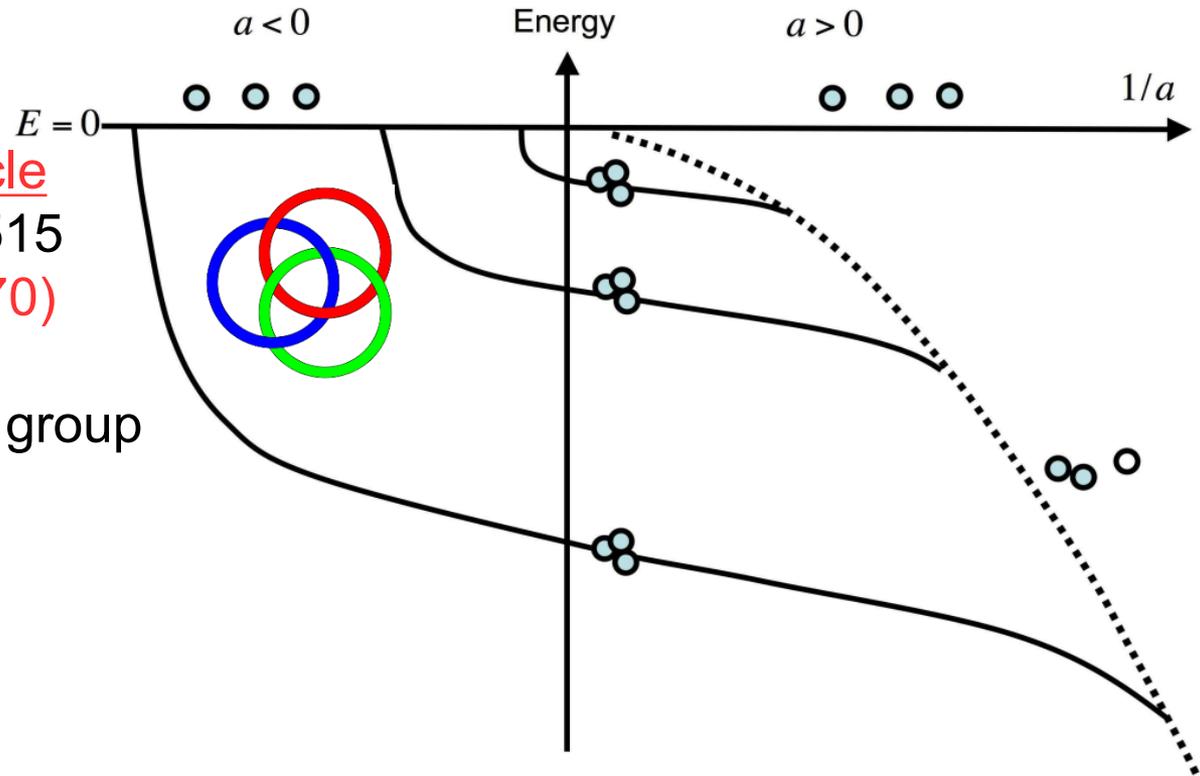
# Física dos estados de Efimov (Renato Higa)



# Efimov effect

PLB 33, 563 (1970)

- RG-flow towards a limit-cycle
- Efimov states:  $E^{(n+1)}/E^{(n)} \sim 515$
- V. Efimov, PLB33, 563 (1970)
- Ahrus group
- ITA-UNESP-UNICMP-UFF group
- Seattle group
- Purdue-Colorado group
- ...



Bhaduri et al., Am.J.Phys. 79, 274 (2011)

# Hypernucleus: $\Lambda nn$

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Search for evidence of  ${}^3_{\Lambda}n$  by observing  $d + \pi^-$  and  $t + \pi^-$  final states in the reaction of  ${}^6\text{Li} + {}^{12}\text{C}$  at 2A GeV

C. Rappold *et al.* (HypHI Collaboration)  
Phys. Rev. C **88**, 041001(R) – Published 10 October 2013

Article References Citing Articles (67) PDF HTML Export Citation



## ABSTRACT

The experimental data obtained from the reaction of  ${}^6\text{Li}$  projectiles at 2A GeV on a fixed graphite target were analyzed to study the invariant mass distributions of  $d + \pi^-$  and  $t + \pi^-$ . Indications of a signal in the  $d + \pi^-$  and  $t + \pi^-$  invariant mass distributions were observed with significances of 5.3  $\sigma$  and 5.0  $\sigma$ , respectively, when including the production target, and 3.7  $\sigma$  and 5.2  $\sigma$ , respectively, when excluding the target. The estimated mean values of the invariant mass for  $d + \pi^-$  and  $t + \pi^-$  signal were  $2059.3 \pm 1.3 \pm 1.7$  MeV/ $c^2$  and  $2993.7 \pm 1.3 \pm 0.6$  MeV/ $c^2$  respectively. The lifetime estimation of the possible bound states yielding to  $d + \pi^-$  and  $t + \pi^-$  final states were deduced to be as  $181^{+30}_{-24} \pm 25$  ps and  $190^{+47}_{-35} \pm 36$  ps, respectively. Those final states may be interpreted as the two-body and three-body decay modes of a neutral bound state of two neutrons and a  $\Lambda$  hyperon,  ${}^3_{\Lambda}n$ .

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Spectroscopic study of a possible  $\Lambda nn$  resonance and a pair of  $\Sigma NN$  states using the  $(e, e'K^+)$  reaction with a tritium target

B. Pandey *et al.* (Hall A Collaboration)  
Phys. Rev. C **105**, L051001 – Published 20 May 2022

Article References No Citing Articles PDF HTML Export Citation



## ABSTRACT

A mass spectroscopy experiment with a pair of nearly identical high-resolution spectrometers and a tritium target was performed in Hall A at Jefferson Lab. Utilizing the  $(e, e'K^+)$  reaction, enhancements, which may correspond to a possible  $\Lambda nn$  resonance and a pair of  $\Sigma NN$  states, were observed with an energy resolution of about 1.21 MeV ( $\sigma$ ), although greater statistics are needed to make definitive identifications. An experimentally measured  $\Lambda nn$  state may provide a unique constraint in determining the  $\Lambda n$  interaction, for which no scattering data exist. In addition, although bound  $A = 3$  and 4  $\Sigma$  hypernuclei have been predicted, only an  $A = 4$   $\Sigma$  hypernucleus ( ${}^4_{\Sigma}\text{He}$ ) was found, utilizing the  $(K^-, \pi^-)$  reaction on a  ${}^4\text{He}$  target. The possible bound  $\Sigma NN$  state is likely a  $\Sigma^0 nn$  state, although this has to be confirmed by future experiments.

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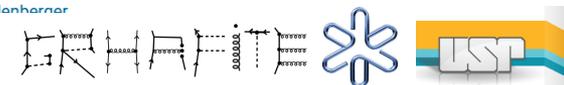
Perspective | Published: 14 September 2021

## New directions in hypernuclear physics

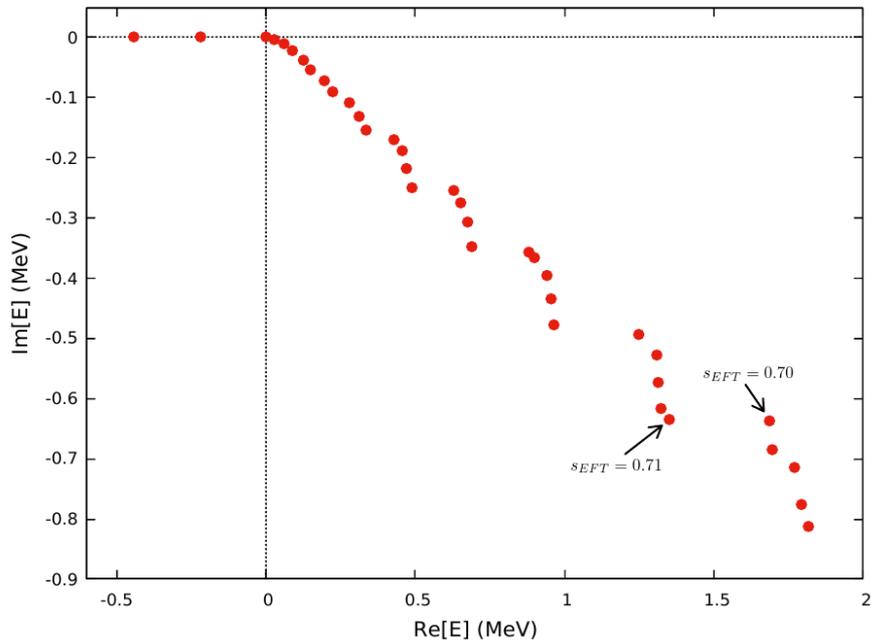
Takehiko R. Saito , Wenbou Dou, Vasyi Drozd, Hiroyuki Ekawa, Samuel Escrig, Yan He, Nasser Kalantar-Nayestanaki, Ayumi Kasagi, Myroslav Kavatsyuk, Enqiang Liu, Yue Ma, Shizu Minami, Abdul Muneem, Manami Nakagawa, Kazuma Nakazawa, Christophe Rappold, Nami Saito, Christoph Scheidenberger, Masato Taki, Yoshiki K. Tanaka, Junya Yoshida, Masahiro Yoshimoto, He Wang & Xiaohou

Nature Reviews Physics **3**, 803–813 (2021) | Cite this article

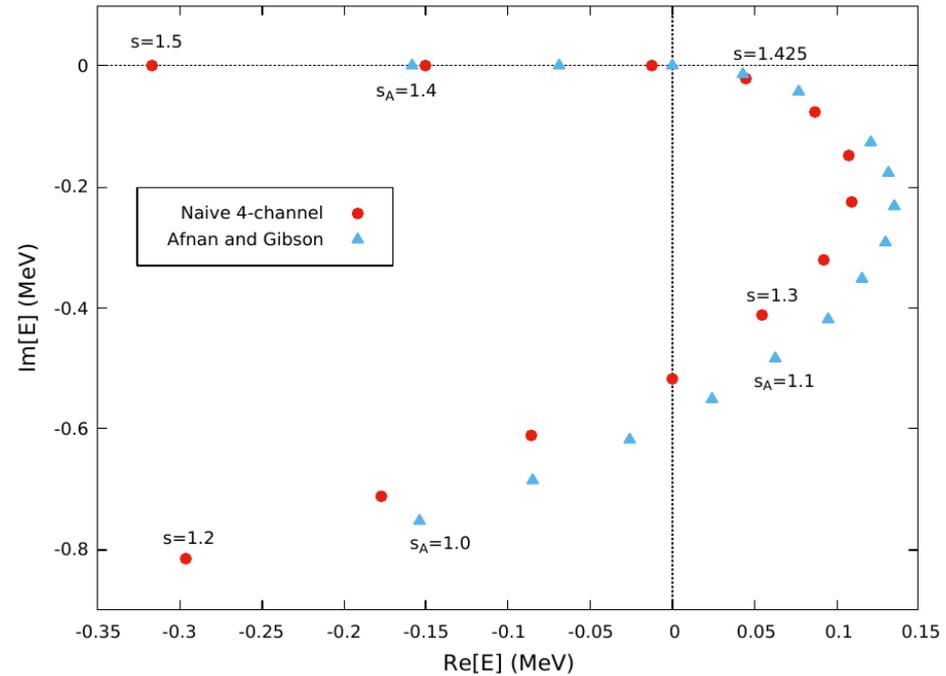
Breno A. Garcia, MSc. thesis



# Hypernucleus: $\Lambda nn$



EFT



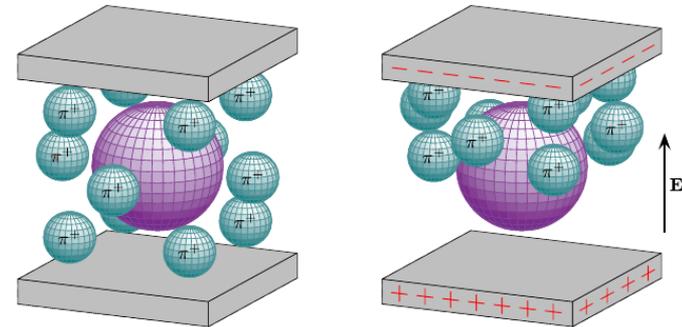
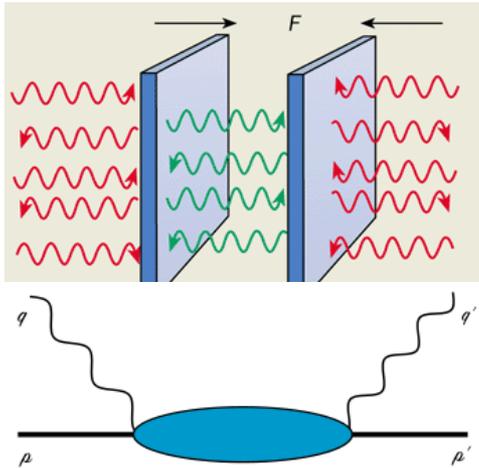
Separable potential

# Casimir-Polder forces btw two neutrons

F. Hagelstein et al. / Progress in Particle and Nuclear Physics 88 (2016) 29–97

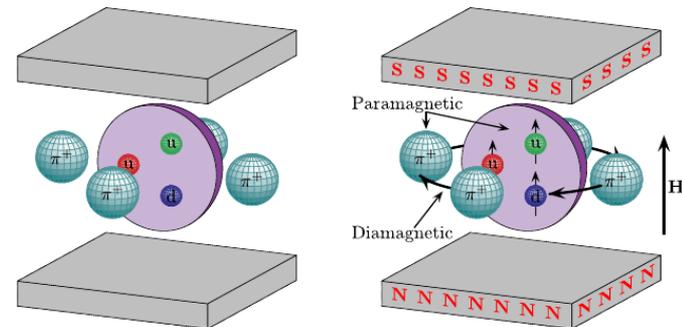
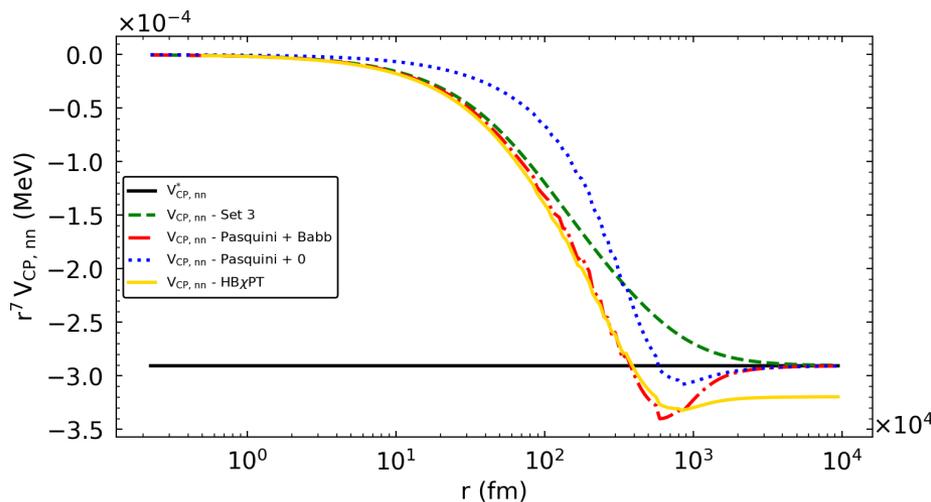
33

Hagelstein, et al., PPNPhys. 88, 29 (2016)



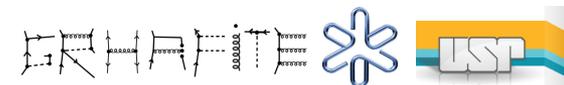
**Fig. 2.1.** Naive view of the proton, consisting of a pion cloud and a quark core, placed between the plates of a parallel plate capacitor. The left (right) figure shows the capacitor discharged (charged).  
Source: Plot courtesy of Phil Martel.

Babb, RH, Hussein, EPJA 53, 126 (2017)

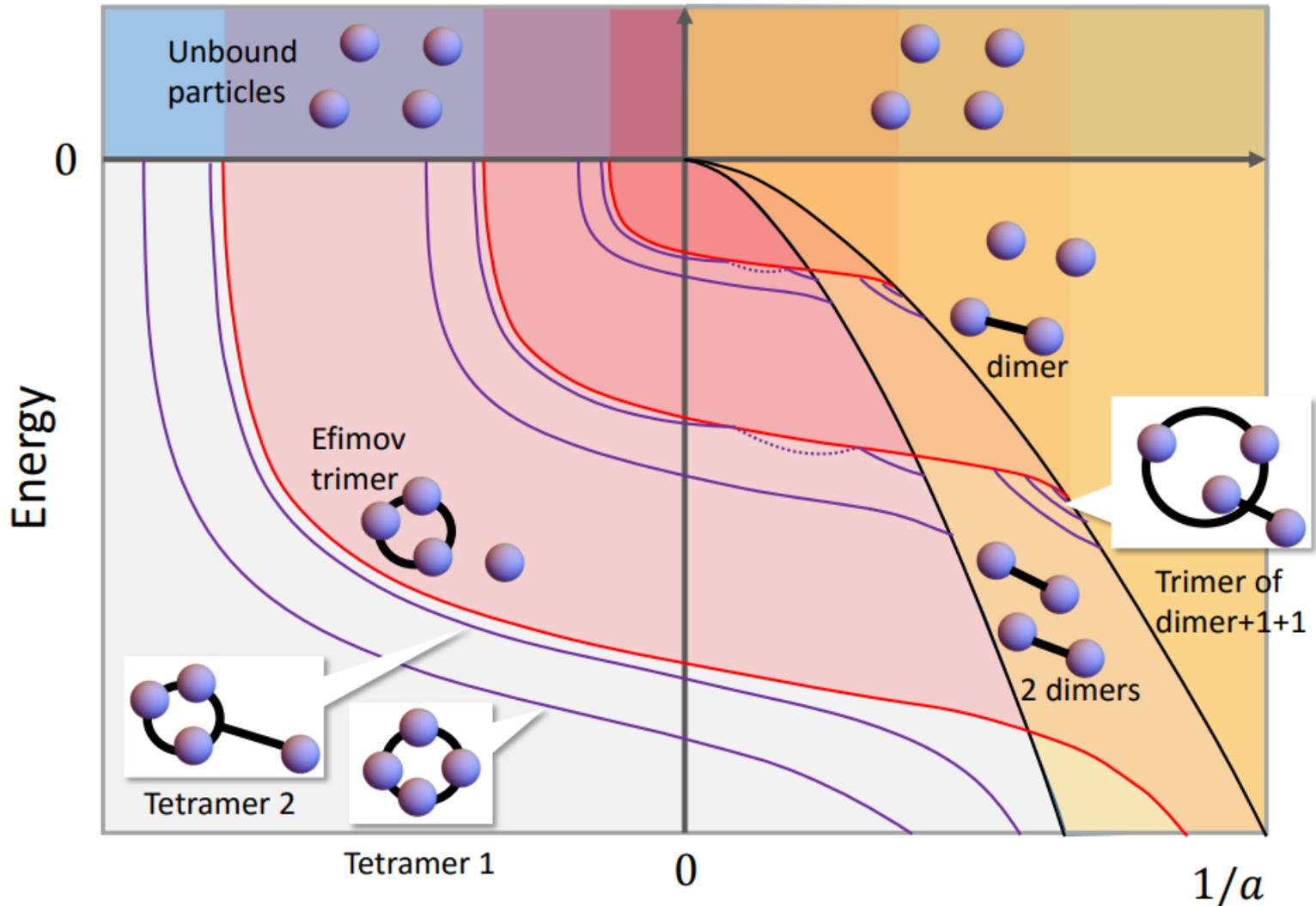


Naive view of the proton, consisting of a pion cloud and a quark core, placed between the poles of a magnet. The left (right) figure shows the magnetic field turned off (on).  
lot courtesy of Phil Martel.

Relevance to UCN physics  
M. S. Godoy's MSc. Thesis



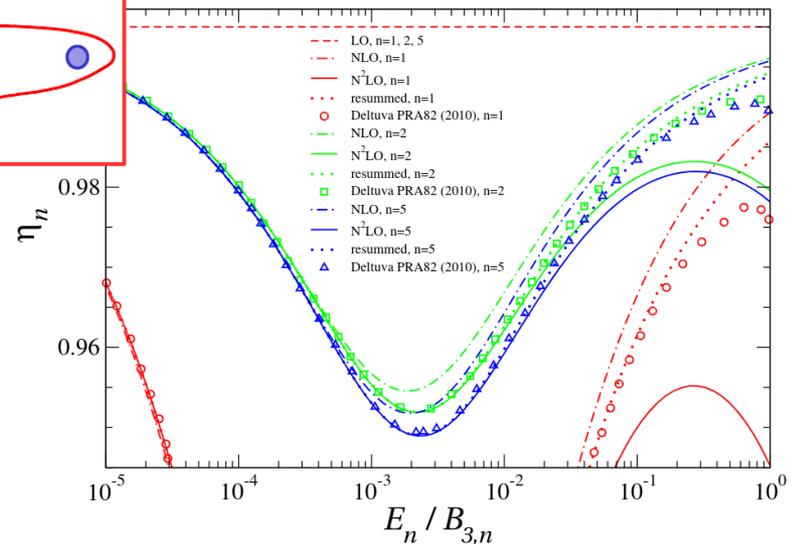
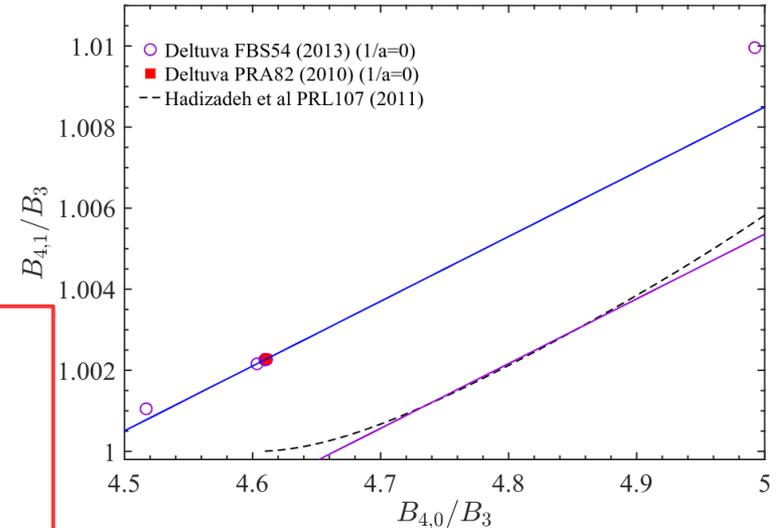
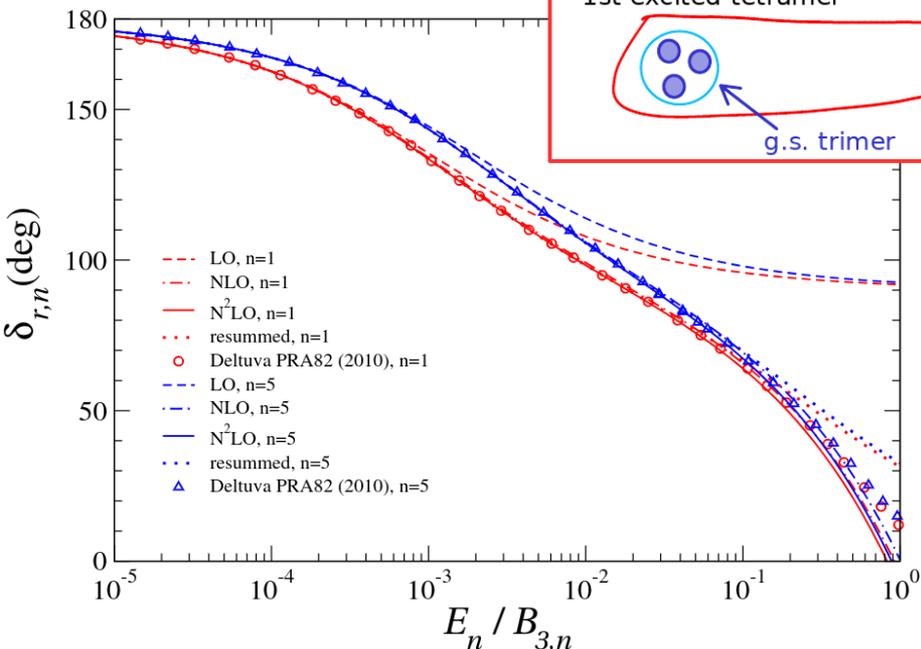
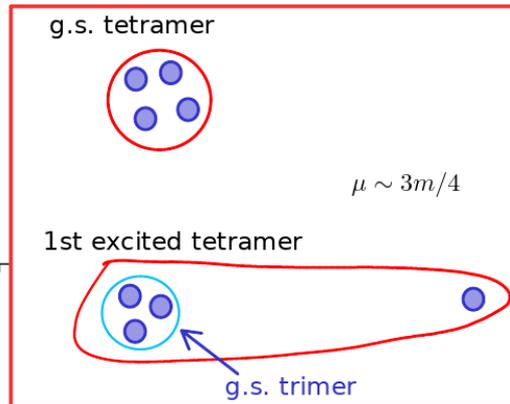
# Universality: four bosons



Naidon, Endo, Rep.Prog.Phys. 80, 056001 (2017)

# EFT and universality of SRI

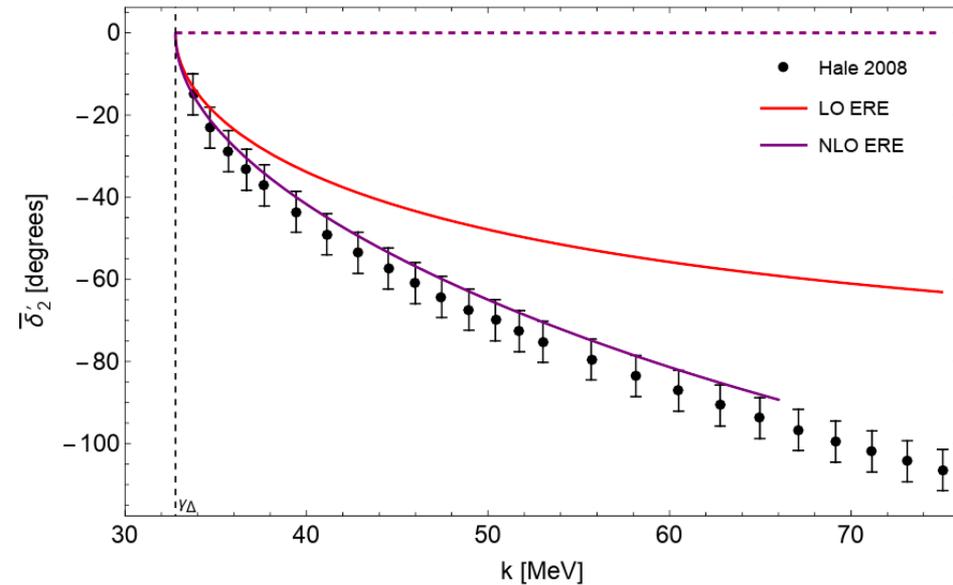
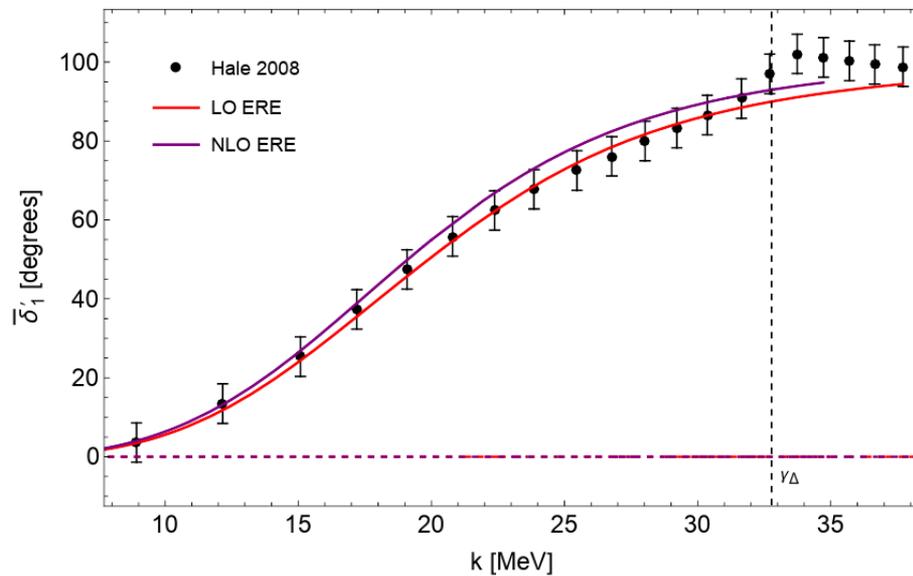
- Importance of 4BF: NLO
- Excited 4Bsyst: halo structure
- Predictions for boson-trimer obs.
- F. Wu, T.Frederico, RH, U.van Kolck
- (PRA109, 043301)



# 1<sup>st</sup> excited <sup>4</sup>He nucleus: Halo EFT approach

resonant state between  $p$ -<sup>3</sup>H and  $n$ -<sup>3</sup>He  
coupled-channel problem  
ATOMKI anomaly: X(16) boson

Matheus F. Cichocki, IC project:  
X(3872)



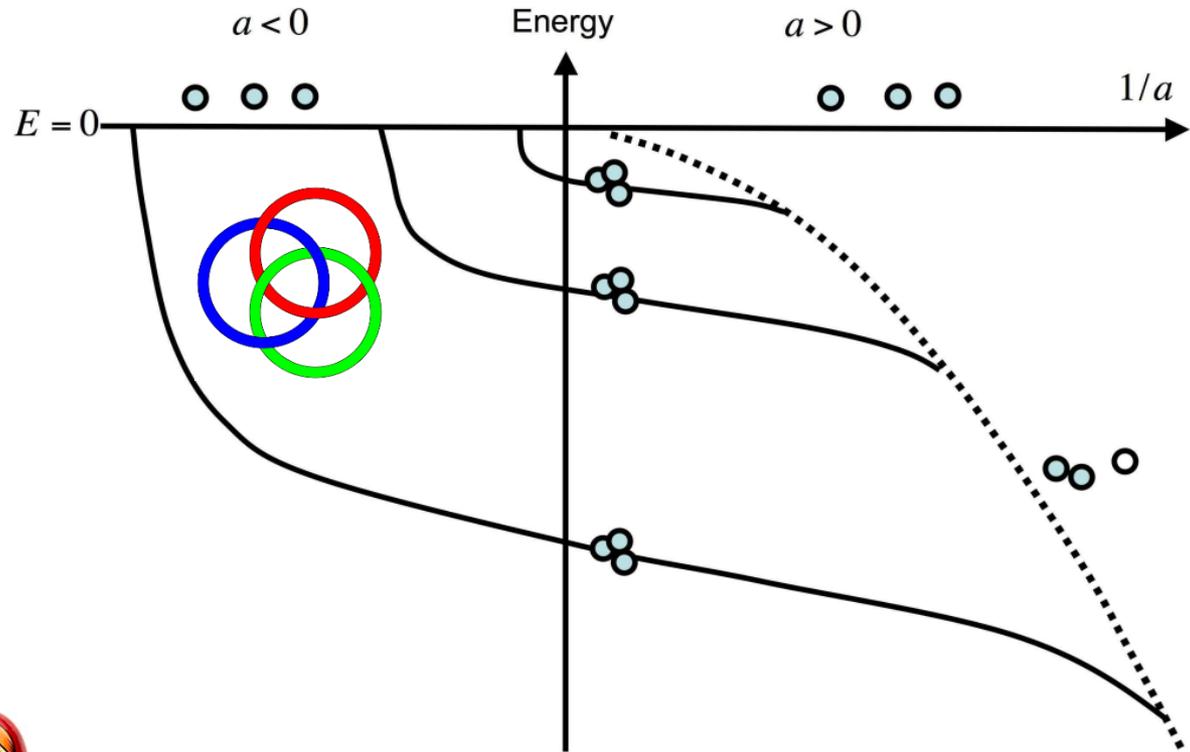
$$E_R \approx 0.127 \text{ MeV}; \Gamma_R \approx 0.288 \text{ MeV}$$

FIM



# Efimov effect

PLB 33, 563 (1970)

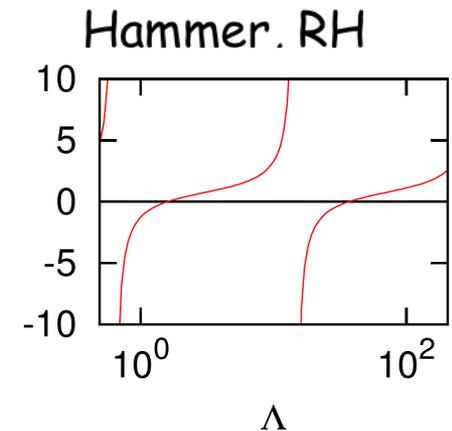
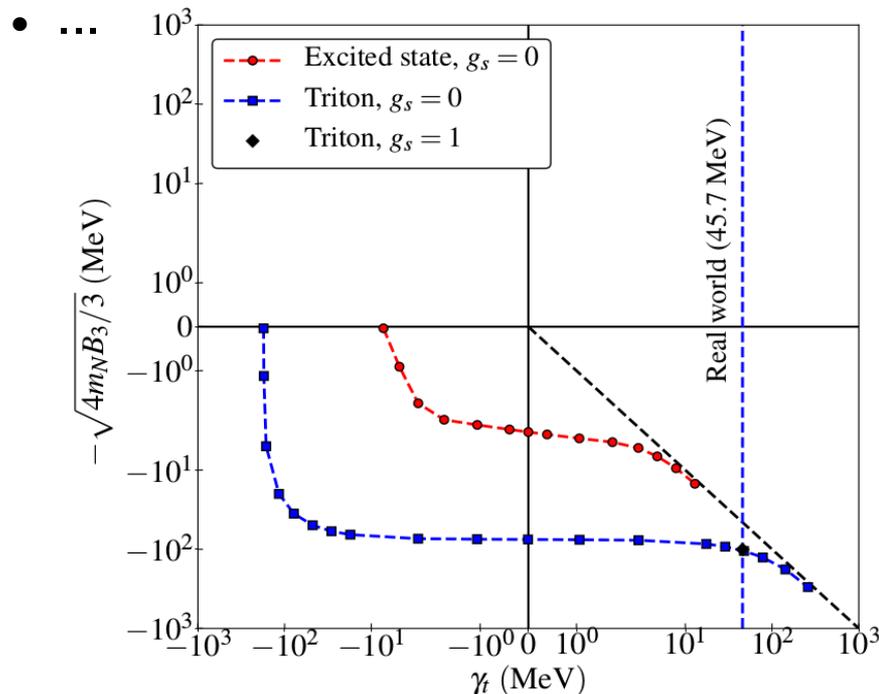
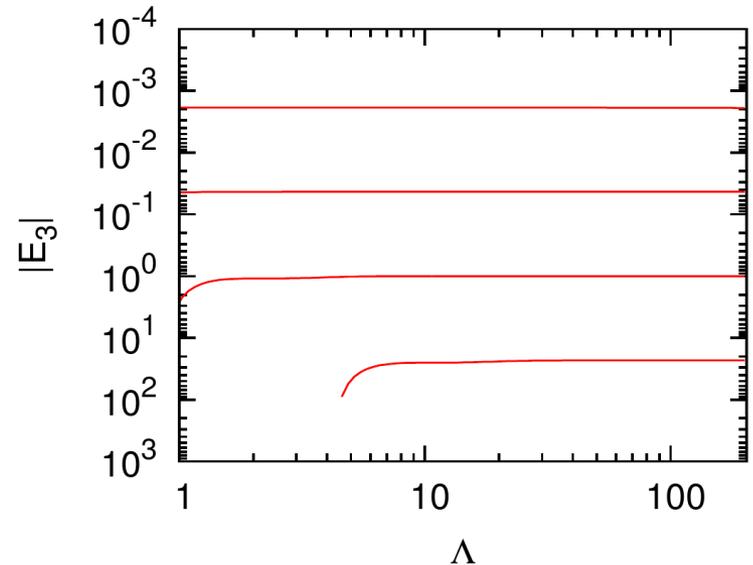


Bhaduri et al., Am.J.Phys. 79, 274 (2011)



# EFT and universality of SRI

- **RG-flow** towards a **limit-cycle**
- **Efimov states:**  $E^{(n+1)}/E^{(n)} \sim 515$
- **V. Efimov, PLB33, 563 (1970)**
- Ahrus group
- ITA-UNESP-UNICMP-UFF group
- Seattle group
- Purdue-Colorado group



Rupak, Vaghani,  
RH van Kolck (2019)

# Hypernucleus: $\Lambda nn$

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Search for evidence of  ${}^3_{\Lambda}n$  by observing  $d + \pi^-$  and  $t + \pi^-$  final states in the reaction of  ${}^6\text{Li} + {}^{12}\text{C}$  at 2A GeV

C. Rappold *et al.* (HypHI Collaboration)  
Phys. Rev. C **88**, 041001(R) – Published 10 October 2013

Article References Citing Articles (67) PDF HTML Export Citation



## ABSTRACT

The experimental data obtained from the reaction of  ${}^6\text{Li}$  projectiles at 2A GeV on a fixed graphite target were analyzed to study the invariant mass distributions of  $d + \pi^-$  and  $t + \pi^-$ . Indications of a signal in the  $d + \pi^-$  and  $t + \pi^-$  invariant mass distributions were observed with significances of 5.3  $\sigma$  and 5.0  $\sigma$ , respectively, when including the production target, and 3.7  $\sigma$  and 5.2  $\sigma$ , respectively, when excluding the target. The estimated mean values of the invariant mass for  $d + \pi^-$  and  $t + \pi^-$  signal were  $2059.3 \pm 1.3 \pm 1.7 \text{ MeV}/c^2$  and  $2993.7 \pm 1.3 \pm 0.6 \text{ MeV}/c^2$  respectively. The lifetime estimation of the possible bound states yielding to  $d + \pi^-$  and  $t + \pi^-$  final states were deduced to be as  $181^{+30}_{-24} \pm 25 \text{ ps}$  and  $190^{+47}_{-35} \pm 36 \text{ ps}$ , respectively. Those final states may be interpreted as the two-body and three-body decay modes of a neutral bound state of two neutrons and a  $\Lambda$  hyperon,  ${}^3_{\Lambda}n$ .

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Spectroscopic study of a possible  $\Lambda nn$  resonance and a pair of  $\Sigma NN$  states using the  $(e, e'K^+)$  reaction with a tritium target

B. Pandey *et al.* (Hall A Collaboration)  
Phys. Rev. C **105**, L051001 – Published 20 May 2022

Article References No Citing Articles PDF HTML Export Citation



## ABSTRACT

A mass spectroscopy experiment with a pair of nearly identical high-resolution spectrometers and a tritium target was performed in Hall A at Jefferson Lab. Utilizing the  $(e, e'K^+)$  reaction, enhancements, which may correspond to a possible  $\Lambda nn$  resonance and a pair of  $\Sigma NN$  states, were observed with an energy resolution of about 1.21 MeV ( $\sigma$ ), although greater statistics are needed to make definitive identifications. An experimentally measured  $\Lambda nn$  state may provide a unique constraint in determining the  $\Lambda n$  interaction, for which no scattering data exist. In addition, although bound  $A = 3$  and 4  $\Sigma$  hypernuclei have been predicted, only an  $A = 4 \Sigma$  hypernucleus ( ${}^4_{\Sigma}\text{He}$ ) was found, utilizing the  $(K^-, \pi^-)$  reaction on a  ${}^4\text{He}$  target. The possible bound  $\Sigma NN$  state is likely a  $\Sigma^0 nn$  state, although this has to be confirmed by future experiments.

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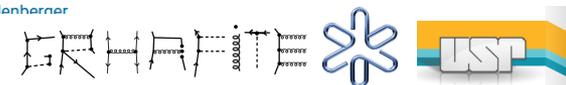
Perspective | Published: 14 September 2021

## New directions in hypernuclear physics

Takehiko R. Saito, Wenbou Dou, Vasyi Drozd, Hiroyuki Ekawa, Samuel Escrig, Yan He, Nasser Kalantar-Nayestanaki, Ayumi Kasagi, Myroslav Kavatsyuk, Enqiang Liu, Yue Ma, Shizu Minami, Abdul Muneem, Manami Nakagawa, Kazuma Nakazawa, Christophe Rappold, Nami Saito, Christoph Scheidenberger, Masato Taki, Yoshiki K. Tanaka, Junya Yoshida, Masahiro Yoshimoto, He Wang & Xiaohou

Nature Reviews Physics 3, 803–813 (2021) | Cite this article

Breno A. Garcia, MSc. thesis



# Hypernucleus: $\Lambda nn$

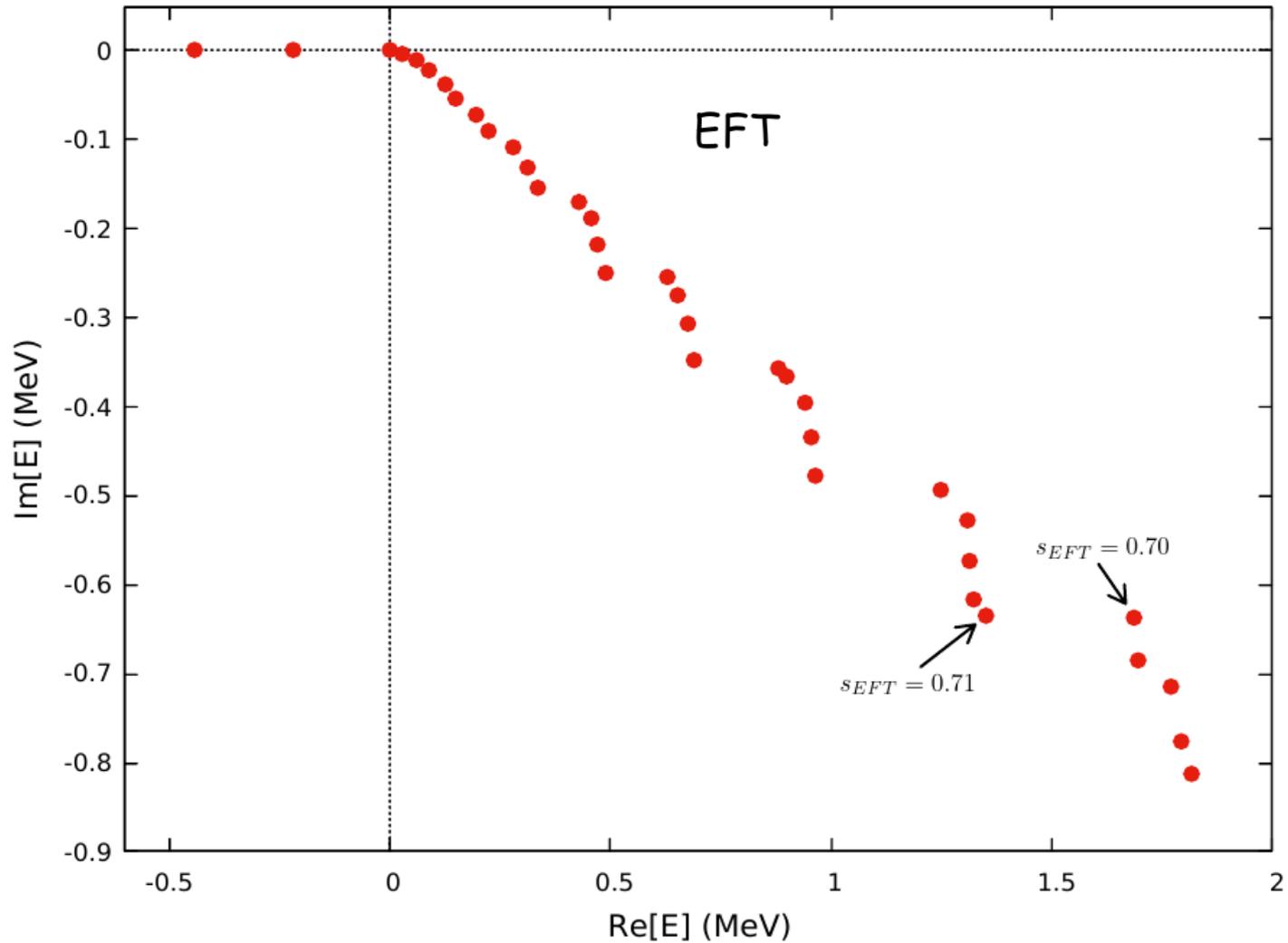
$$a_{nn} = -18.9 \pm 0.4 \text{ fm}, \quad r_{nn} = 2.75 \pm 0.11 \text{ fm}$$

Nijmegen potential model D

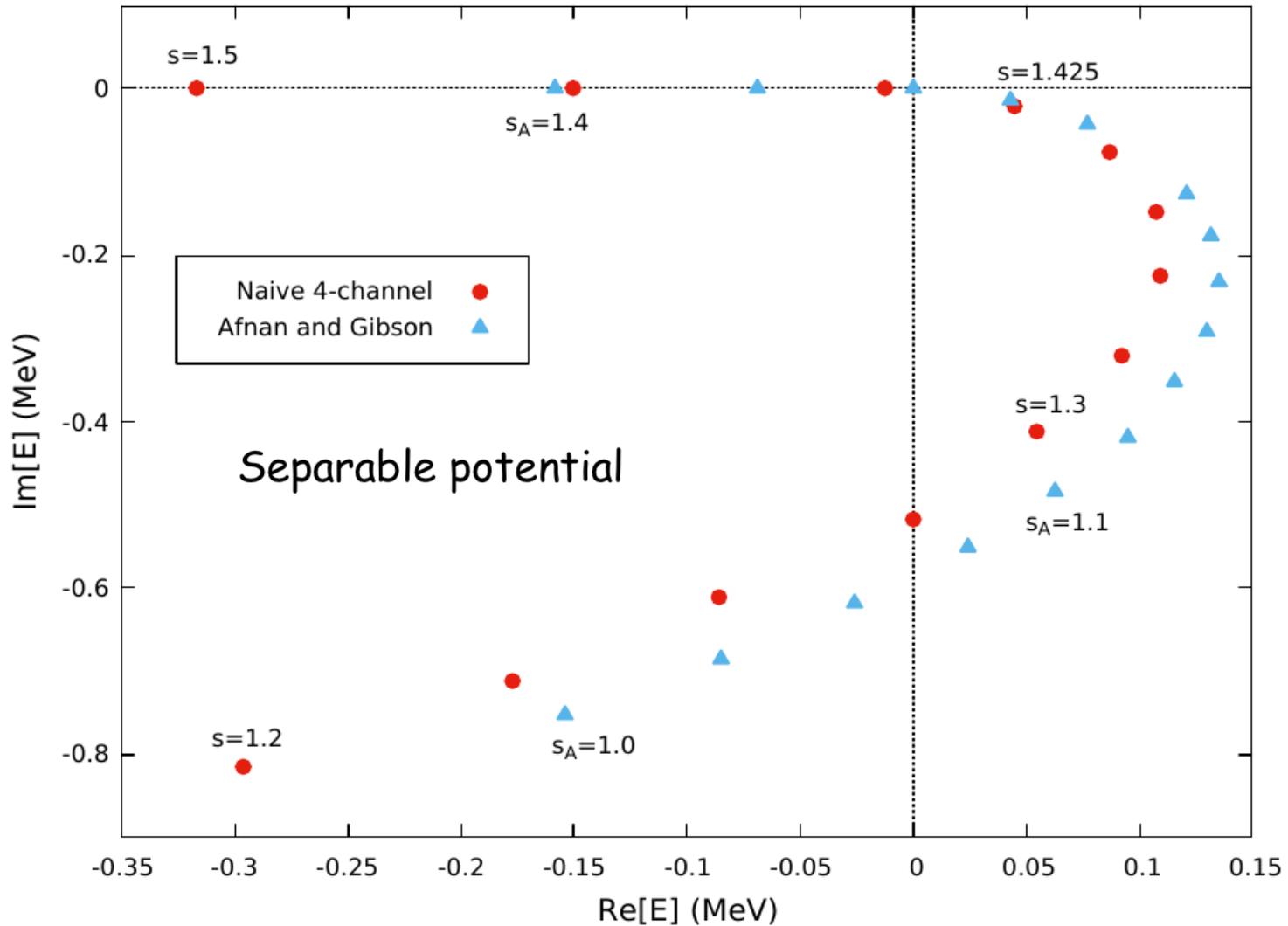
	$\Lambda p$	$\Lambda n$
$a_s$	$-1.77 \pm 0.28$	$-2.03 \pm 0.32$
$r_s$	$3.78 \pm 0.35$	$3.66 \pm 0.32$
$a_t$	$-2.06 \pm 0.12$	$-1.84 \pm 0.10$
$r_t$	$3.18 \pm 0.12$	$3.32 \pm 0.11$

$$T_{\Lambda n} \Rightarrow S_{EFT} T_{\Lambda n}$$

# Hypernucleus: $\Lambda nn$



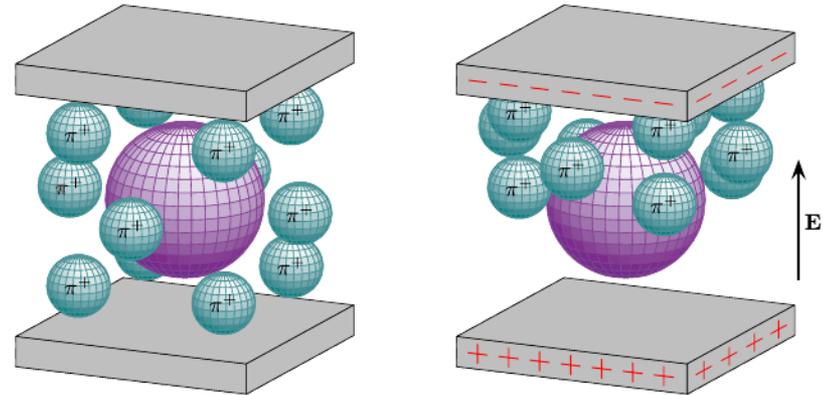
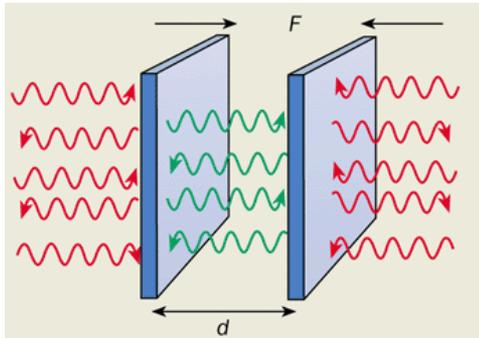
# Hypernucleus: $\Lambda nn$



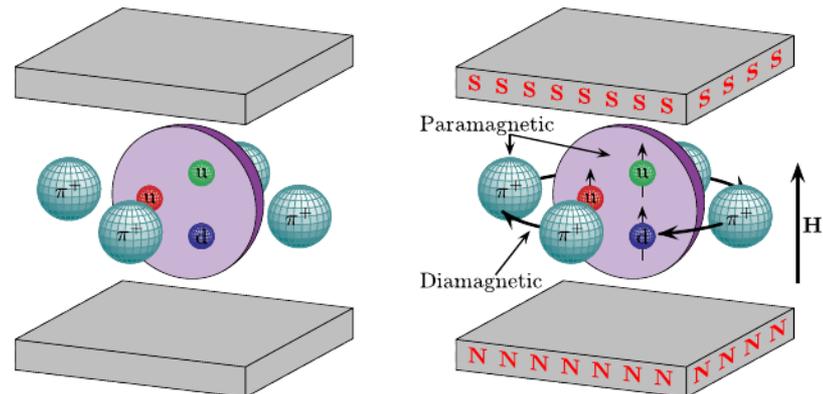
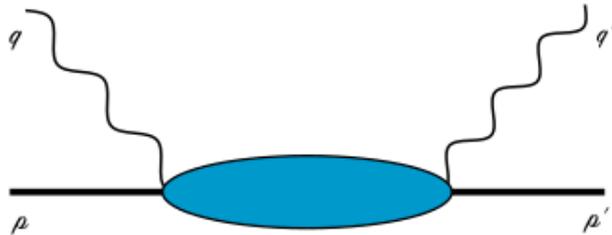
# Casimir-Polder forces btw two neutrons

F. Hagelstein et al. / Progress in Particle and Nuclear Physics 88 (2016) 29–97

33



**Fig. 2.1.** Naive view of the proton, consisting of a pion cloud and a quark core, placed between the plates of a parallel plate capacitor. The left (right) figure shows the capacitor discharged (charged).  
Source: Plot courtesy of Phil Martel.

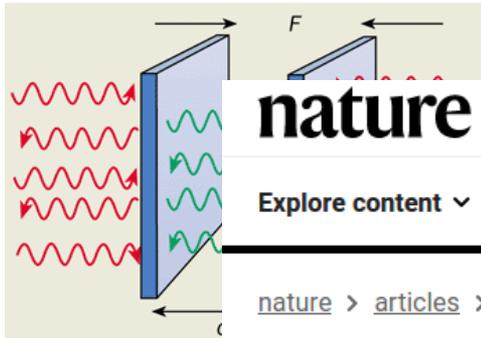


**Fig. 2.2.** Naive view of the proton, consisting of a pion cloud and a quark core, placed between the poles of a magnet. The left (right) figure shows the external magnetic field turned off (on).  
Source: Plot courtesy of Phil Martel.

# Casimir-Polder forces btw two neutrons

F. Hagelstein et al. / Progress in Particle and Nuclear Physics 88 (2016) 29–97

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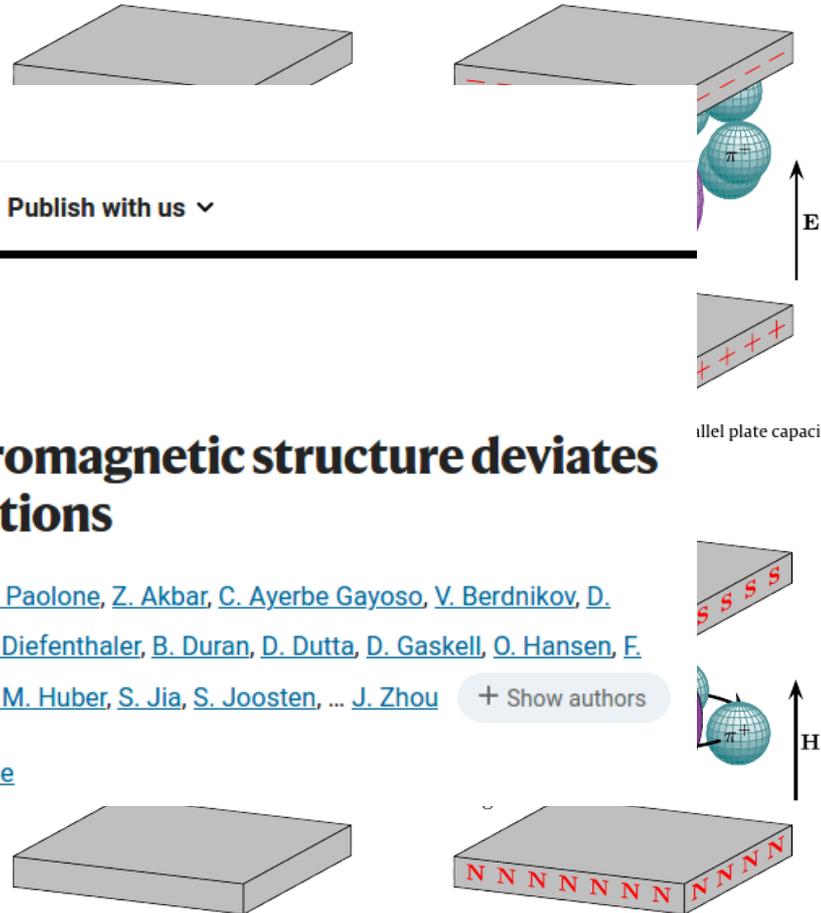
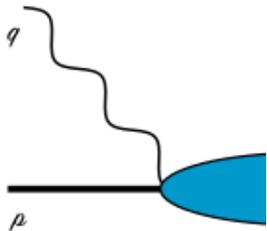
Article | [Published: 19 October 2022](#)

## Measured proton electromagnetic structure deviates from theoretical predictions

[R. Li](#), [N. Sparveris](#) ✉, [H. Atac](#), [M. K. Jones](#), [M. Paolone](#), [Z. Akbar](#), [C. Ayerbe Gayoso](#), [V. Berdnikov](#), [D. Biswas](#), [M. Boer](#), [A. Camsonne](#), [J.-P. Chen](#), [M. Diefenthaler](#), [B. Duran](#), [D. Dutta](#), [D. Gaskell](#), [O. Hansen](#), [F. Hauenstein](#), [N. Heinrich](#), [W. Henry](#), [T. Horn](#), [G. M. Huber](#), [S. Jia](#), [S. Joosten](#), ... [J. Zhou](#)

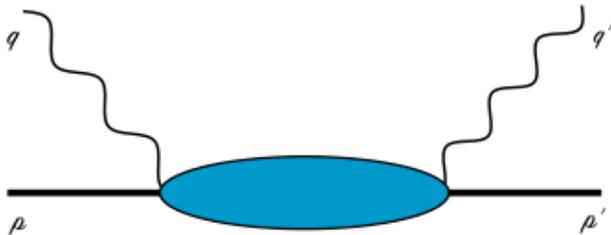
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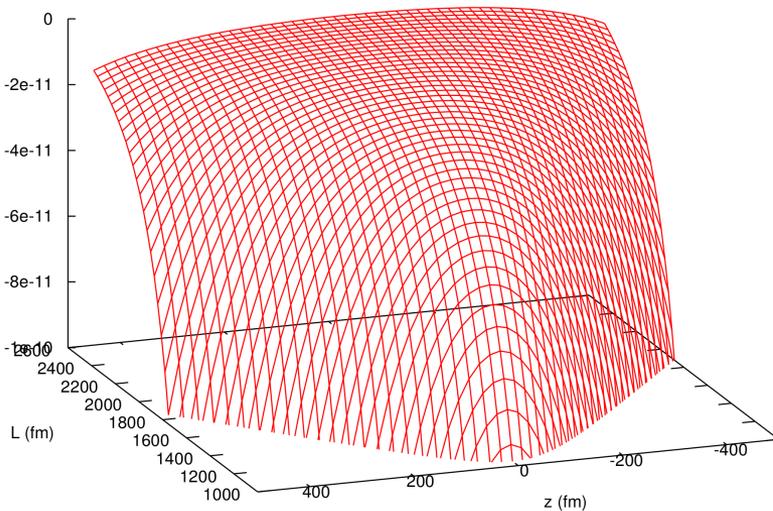
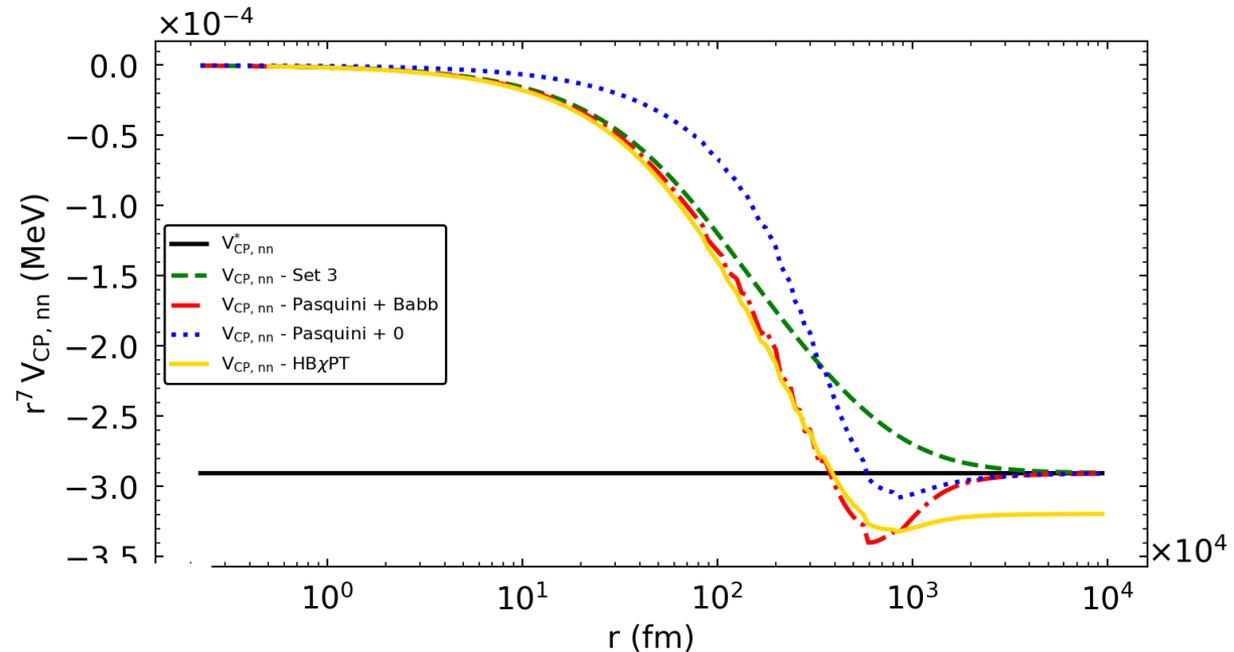


**Fig. 2.2.** Naive view of the proton, consisting of a pion cloud and a quark core, placed between the poles of a magnet. The left (right) figure shows the external magnetic field turned off (on).  
Source: Plot courtesy of Phil Martel.

# Casimir-Polder forces btw two neutrons

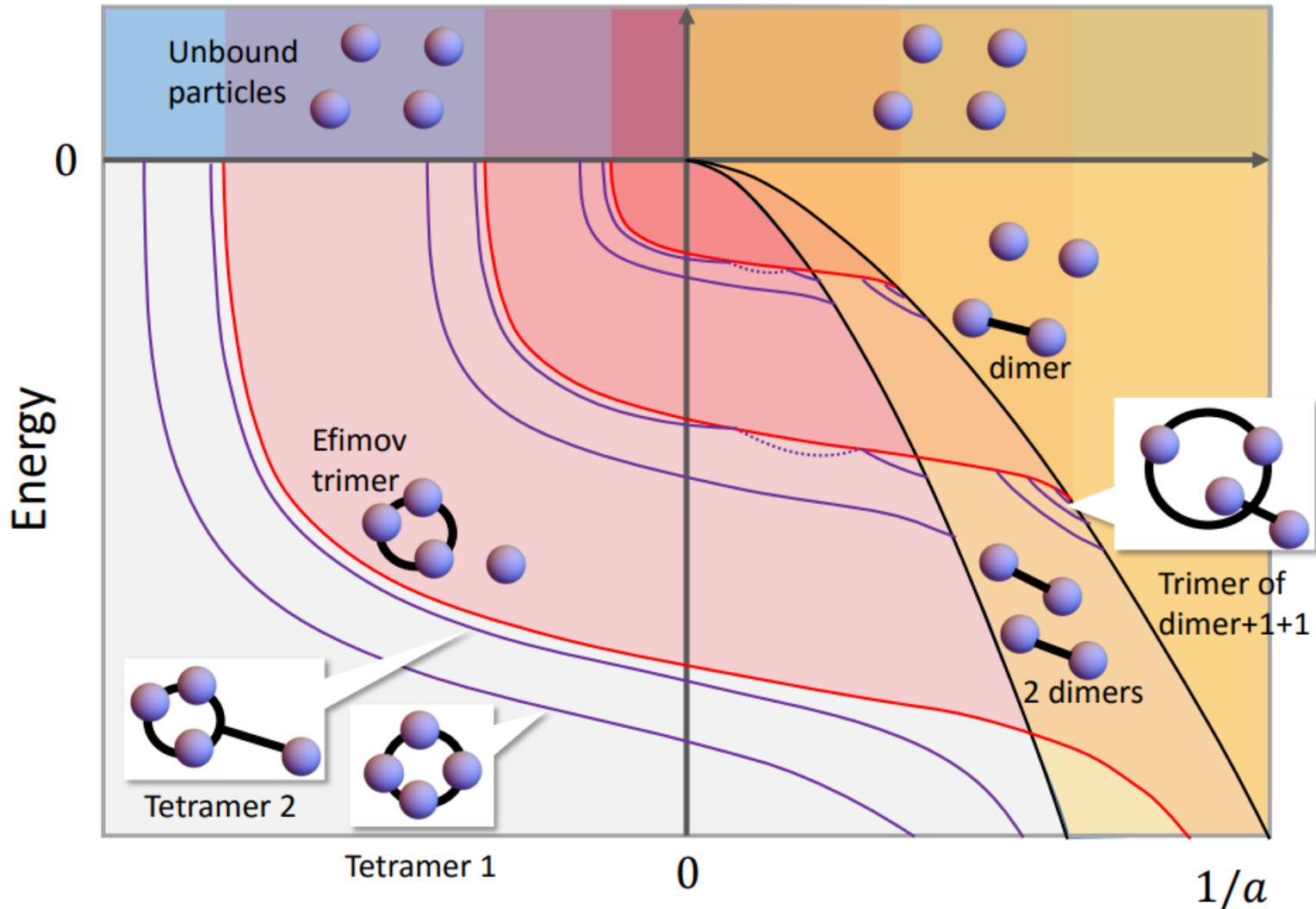


Relevance to UCN physics  
M. S. Godoy's MSc. Thesis



Babb, RH, Hussein, EPJA 53, 126 (2017)

# Universality: four bosons



Naidon, Endo, Rep.Prog.Phys. 80, 056001 (2017)

# Universality: four bosons

Controversy: 4B parameter necessary?

- Yes – Adhikari et al., PRL 74, 487 (1995), Yamashita et al., EurPhysLett 75, 555 (2006), Hadizadeh et al., PRL 107, 135304 (2011)
- No – Hammer, Platter, EPJA 32, 113 (2007), von Stecher et al., Nature Phys. 5, 417 (2009)
- EFT – 4B param. Is a NLO effect
- Bazak et al., PRL 122, 143001 (2019)
- Wu, Frederico, RH, van Kolck, PRA 109, 043301 (2024)

# Energy correlations

$$\text{LO: } \begin{cases} B_{4,0}^{(0)} = \kappa_0 B_3, \\ B_{4,1}^{(0)} = \kappa_1 B_3, \end{cases} \Rightarrow B_{4,1}^{(0)} = \frac{\kappa_1}{\kappa_0} B_{4,0}^{(0)},$$

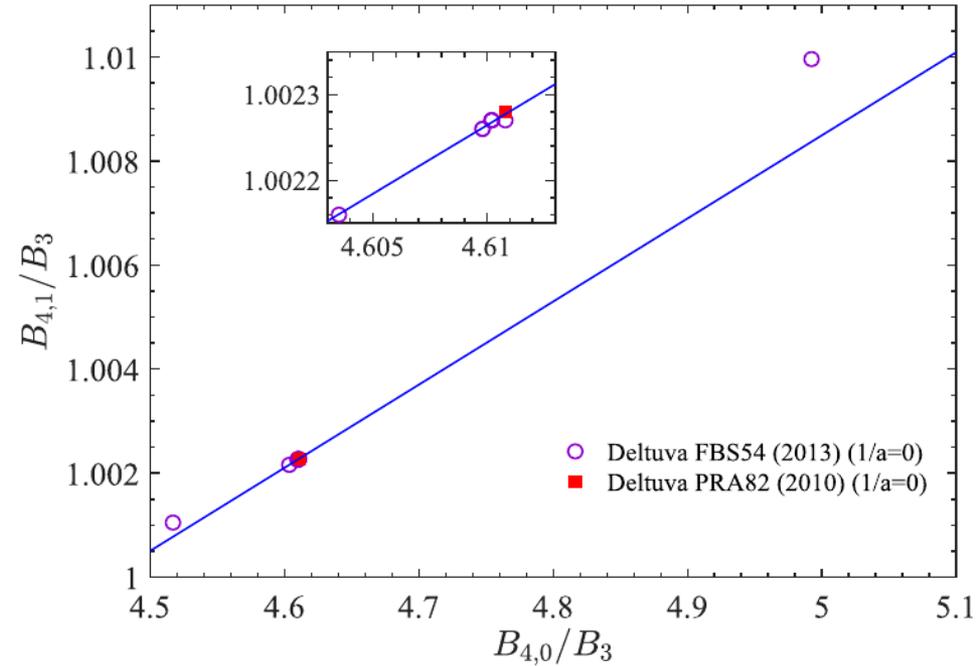
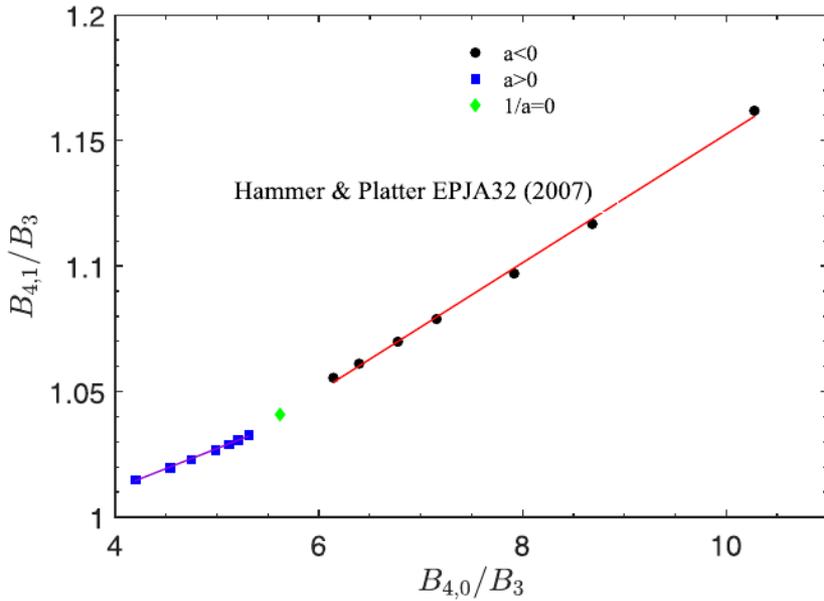
$$\begin{cases} \frac{\Gamma_{4,0}^{(0)}}{2} = \gamma_0 B_3 = \frac{\gamma_0}{\kappa_0} B_{4,0}^{(0)}, \\ \frac{\Gamma_{4,1}^{(0)}}{2} = \gamma_1 B_3 = \frac{\gamma_1}{\kappa_0} B_{4,0}^{(0)}, \end{cases}$$

# Energy correlations

$$\text{LO: } \begin{cases} B_{4,0}^{(0)} = \kappa_0 B_3, \\ B_{4,1}^{(0)} = \kappa_1 B_3, \end{cases} \Rightarrow B_{4,1}^{(0)} = \frac{\kappa_1}{\kappa_0} B_{4,0}^{(0)},$$

$$\text{NLO: } \frac{B_{4,0}^{(1)}}{B_3} = \kappa_1 - \frac{\lambda_1}{\lambda_0} \kappa_0 + \frac{\lambda_1}{\lambda_0} \frac{B_{4,0}^{(1)}}{B_3} + \left( \frac{\eta_1}{\eta_0} - \frac{\lambda_1}{\lambda_0} \right) \eta_0 (a_2 \sqrt{mB_3})^{-1} + z r_2 \sqrt{mB_3}$$

# Energy correlations



$$\frac{B_{4,0}^{(1)}}{B_3}$$

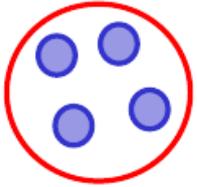
$$\frac{B_{4,0}^{(1)}}{B_3}$$

$$\frac{B_{4,0}^{(1)}}{B_3}$$

$$\frac{\lambda_1}{\lambda_0}$$

# 1<sup>st</sup> excited tetramer: Halo EFT approach

g.s. tetramer



$$k_{g.s.} \sim \sqrt{2\mu(B_{4,0} - B_3)} \sim \sqrt{(\kappa_0 - 1)2\mu B_3} > \sqrt{2\mu B_3} \sim \frac{3}{2}M_{hi}^{\text{halo}}$$

$$\mu \sim 3m/4$$

1st excited tetramer

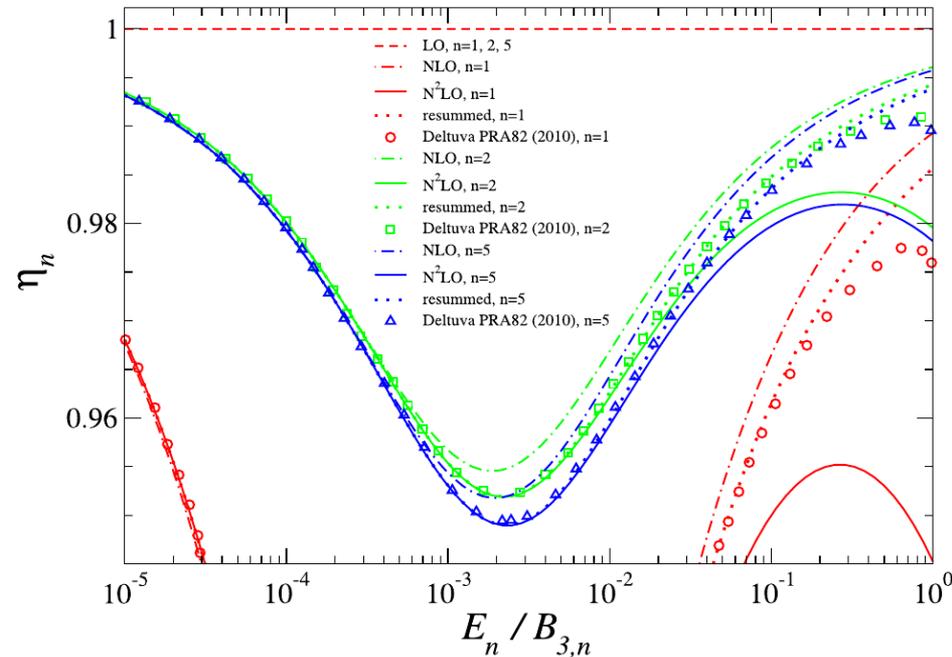
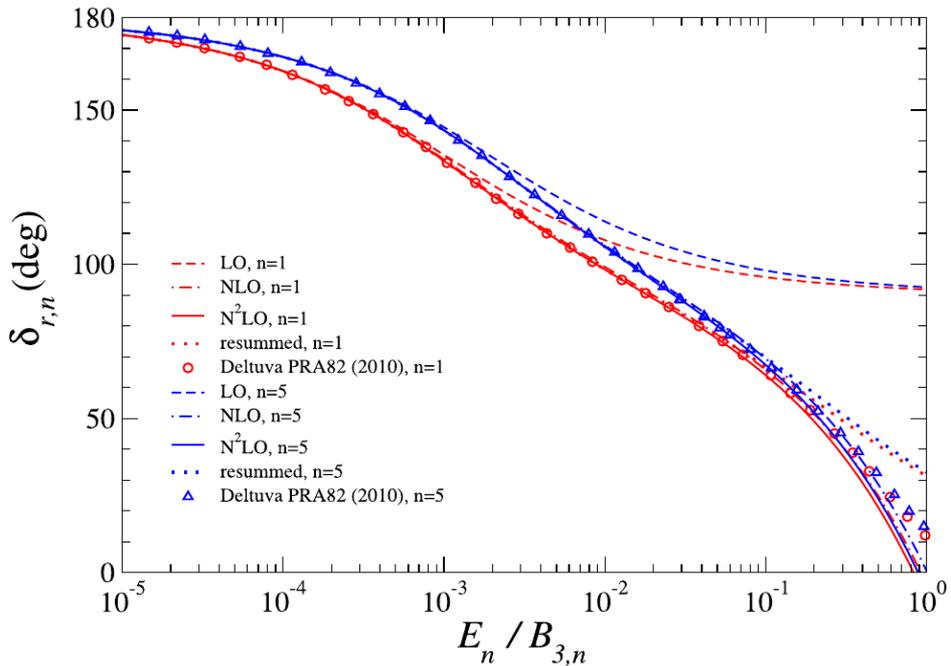


$$k_{1st\ ex.} \sim M_{lo}^{\text{halo}} \sim \sqrt{2\mu(B_{4,1} - B_3)} \sim \sqrt{(\kappa_1 - 1)2\mu B_3}$$

g.s. trimer

$$\frac{k_{1st.ex.}}{k_{g.s.}} \ll 1$$

# 1<sup>st</sup> excited tetramer: Halo EFT approach



$$m(B_{4,1} - B_3)\langle r^2 \rangle = \frac{1}{16} \left[ 1 + \frac{r_0}{a_0} + 3 \frac{r_0^2}{2} a_0^2 + \dots + \langle r_C^2 \rangle \right]$$

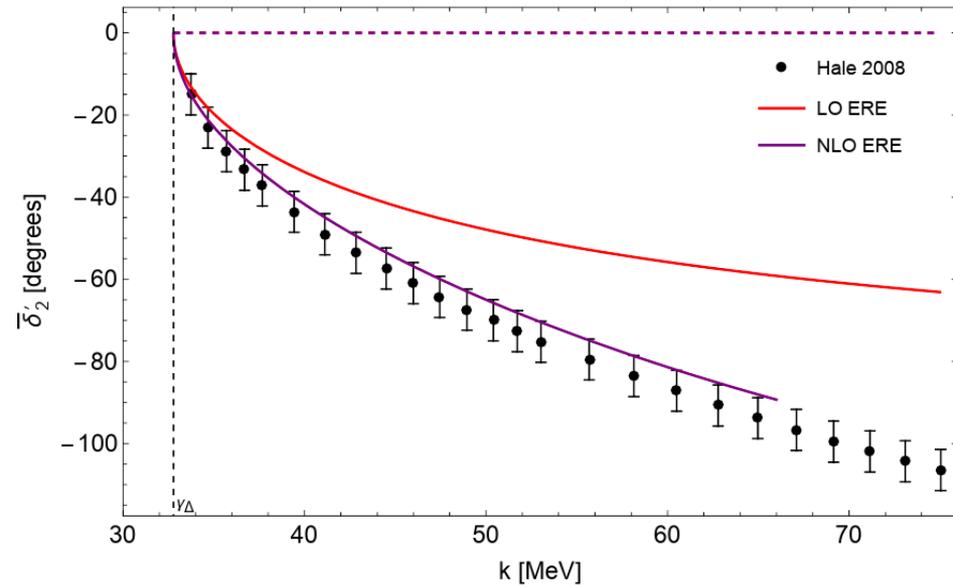
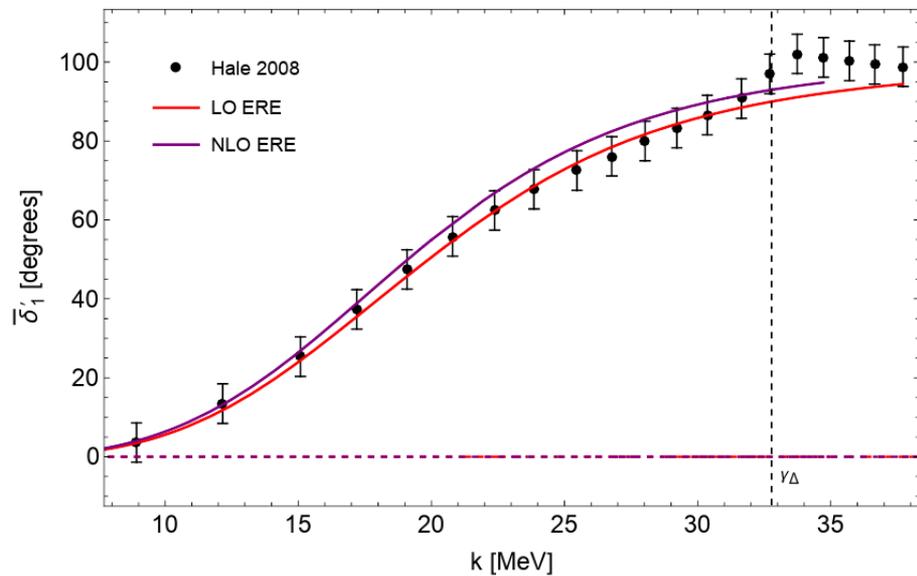
$$\approx 0.0625 + 0.0175 + 0.0074 + \dots \approx 0.0901$$

Hiyama-Kamimura: 0.0851

corrected  $\langle r_C^2 \rangle$ :

# 1<sup>st</sup> excited <sup>4</sup>He nucleus: Halo EFT approach

resonant state between  $p$ -<sup>3</sup>H and  $n$ -<sup>3</sup>He  
coupled-channel problem  
ATOMKI anomaly:  $X(16)$  boson

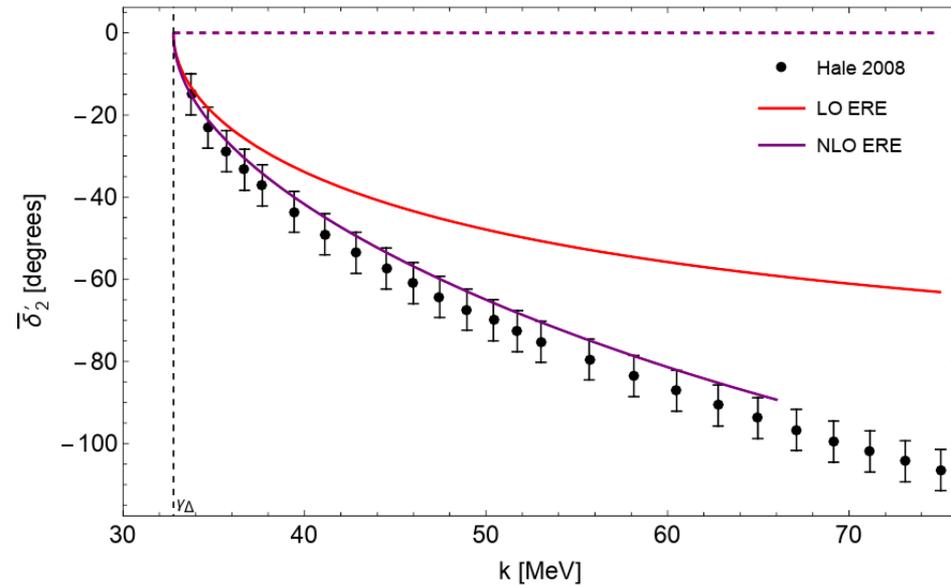
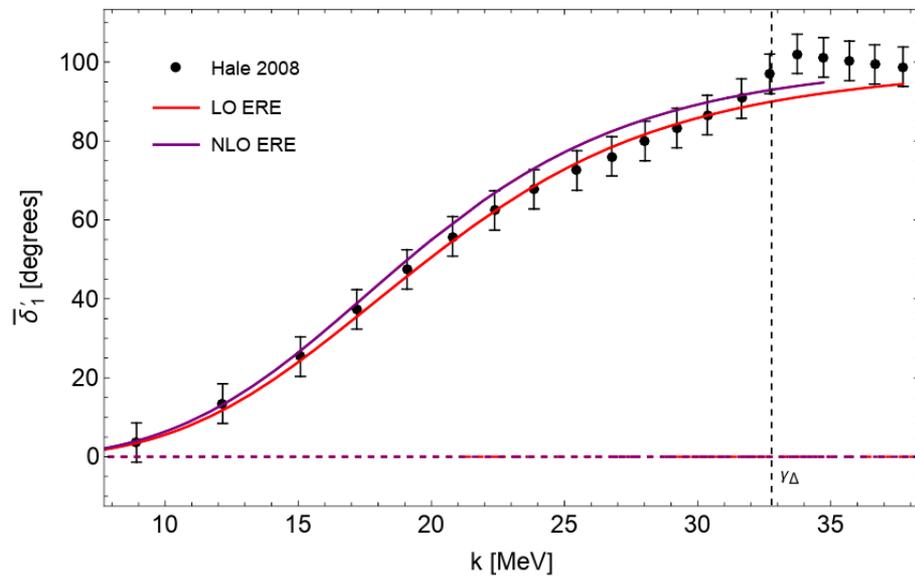


$$E_R \approx 0.127\text{MeV}; \Gamma_R \approx 0.288\text{MeV}$$

# 1<sup>st</sup> excited <sup>4</sup>He nucleus: Halo EFT approach

resonant state between  $p$ -<sup>3</sup>H and  $n$ -<sup>3</sup>He  
coupled-channel problem  
ATOMKI anomaly:  $X(16)$  boson

Matheus F. Cichocki, IC project:  
 $X(3872)$



$$E_R \approx 0.127\text{MeV}; \Gamma_R \approx 0.288\text{MeV}$$

