

Exotic Hadrons in Heavy Ion Collisions

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- A very brief overview on the state-of-art of exotic states
- The exotics in HICs?
- Molecular, tetraquark and triangle singularities interpretations in HICs?

Summary of some of our recent results (several strategies):

- Final yields [$T_{cc}(3985)^+$, $Z_{cs}(3985)^-$, $\chi_{c1}(4274)$, $R = \frac{N_{X(3872)}}{N_{\psi(2S)}} \dots$]
- Challenge: femtoscopy [$D_1(2420)$, $D_1(2430)$, $B\bar{B}$]
- Three-body dynamics ($K^*(4307)$, $D_{1s}^*(2860)$, $X(2890)$, $\phi(2170)$, ...)
- Efimov states [Λnn , ...]
- Ultraperipheral collisions [$D\bar{D}$, $B\bar{B}$, ...]



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Hundreds of observed conventional hadrons

Gell-Mann (1964), ...

BARYONS: qqq ($3 \otimes 3 \otimes 3 = 1 \oplus \dots$)

MESONS: $q\bar{q}$ ($3 \otimes \bar{3} = 1 \oplus \dots$)

Properties \Rightarrow QCD-like quark models



Proton



Anti-proton



Neutron



Lambda



Pion chargé π^+



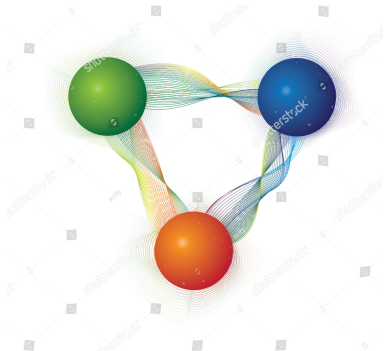
Kaon neutre K^0



Méson B^0



J/ψ



Unconventional Hadrons?

Question

Is it possible an unconventional hadronic structure?

QCD does not forbid more complicated combinations!!!

Tetraquarks $\Rightarrow qq\bar{q}\bar{q}$ ($3 \otimes 3 \otimes \bar{3} \otimes \bar{3} = 1 \oplus \dots$)

Pentaquarks $\Rightarrow qqqq\bar{q}$ ($3 \otimes 3 \otimes 3 \otimes 3 \otimes \bar{3} = 1 \oplus \dots$)

Glueballs $\Rightarrow gg \dots g$ ($8 \otimes 8 \dots \otimes 8 = 1 \oplus \dots$)

Hybrids $\Rightarrow q\bar{q}g$ ($3 \otimes \bar{3} \otimes 8 = 1 \oplus \dots$)

If exist: new objects to study confinement mechanism;
If not exist: theory should explain why not!!!

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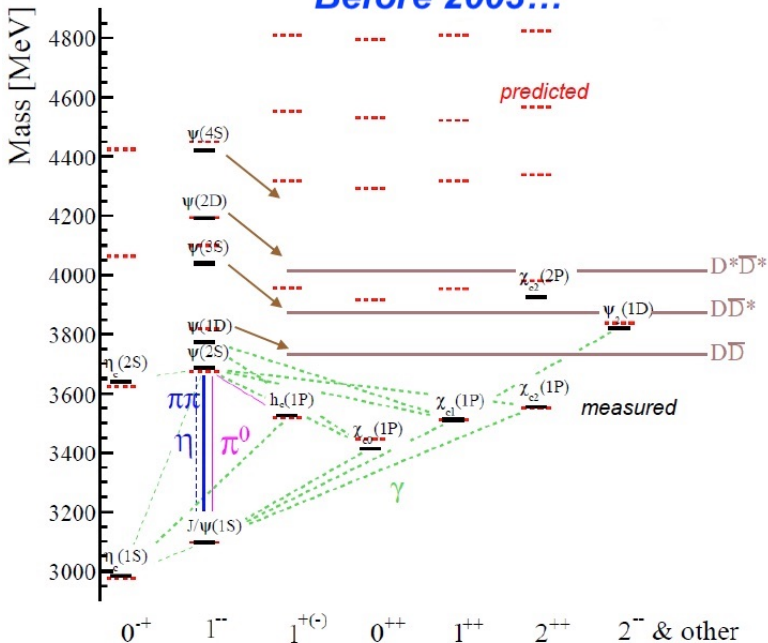
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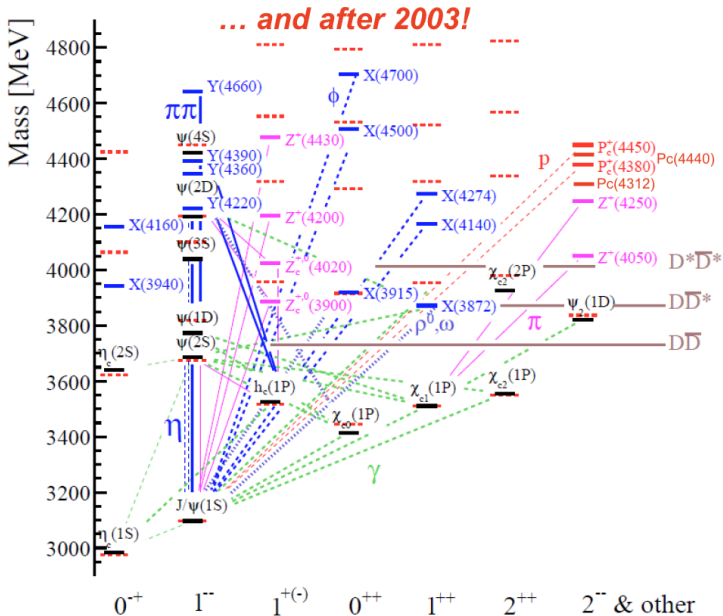
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If not exist: theory should explain why not!!!

Before 2003...



Figures from Olsen, Skwarnicki, Zieminska



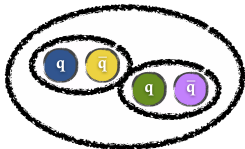


(Adapted from Skwarnicki, 2018)



Interpretations for composition and binding mechanisms?

- Hadron Molecules



- Hybrids



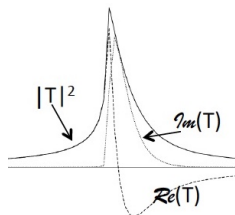
- Glueballs



- Tetraquarks



- Kinematical effects (TS's)



- ...



Example of the debate on prompt production of $X(3872)$

Esposito et al., EPJC (2021);
2006.15044

- Comover interaction model:

$$\tau \frac{N_Q}{d\tau} = -\langle v\sigma \rangle_Q \rho_c N_Q;$$

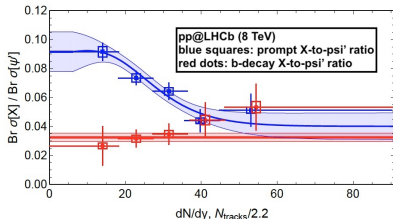
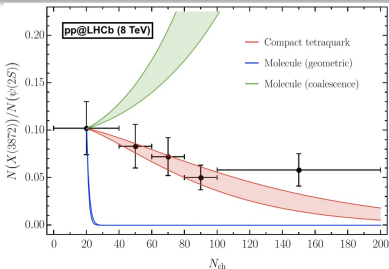
$$\langle v\sigma \rangle_{4q} \sim \pi r_{4q}^2 \simeq 11.6 \text{ mb};$$

$$\langle v\sigma \rangle_{Mol} \sim \pi r_{Mol}^2 \simeq 1197 \text{ mb}$$

- Data \Rightarrow tetraquark nature

Braaten et al., PRD (2021);
2012.13499

- $\langle v\sigma \rangle_{Mol}$: probability-weighted sum of $\langle v\sigma \rangle(\pi D^{(*)})$
- non-relativistic XEFT
- Assumption: $f_{out,Q}^{(prompt)}$ out of reach of comoving pions
- Data \Rightarrow molecular picture



Theoretical perspective

A compelling and unified understanding has not yet emerged

- No single theoretical framework explains the exotics collection
- Candidates: different interpretations (hadron molecule, diquark-antidiquark, kinematic effects, ...)
- (m, Γ) can be explained by different models or even superposition of them
- Necessity of more observables to distinguish their internal structure
- Let us focus on a promising scenario



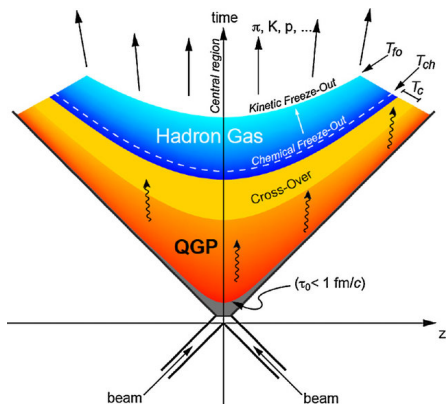
Promising alternative: exotics in HICs

Early stages of HIC's

- Large number of Q 's produced
- Q 's coalesce to form multiquarks

Hadron gas phase

- Multiquarks: interact with other hadrons
- Absorption / production
- Ex. $X\pi \rightarrow D^{(*)}\bar{D}^{(*)}$ or $D^{(*)}\bar{D}^{(*)} \rightarrow X\pi$
- Properties \rightarrow interpretation



(Braun-Munzinger and Donigus, Nucl. Phys. A 987 (2019) 144)



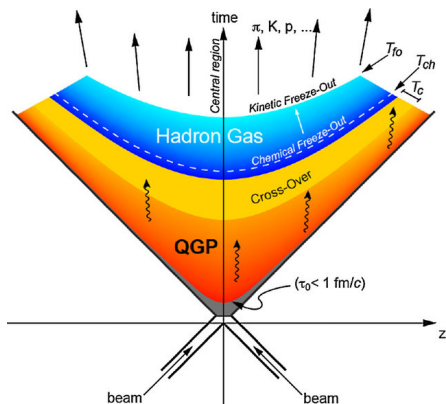
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First evidence for $X(3872)$ in HICs

CMS-LHC, Phys. Rev. Lett. 128 (2022) 032001

- Prompt $X(3872)$ -production in $PbPb$ collisions, $\sqrt{s} = 5.02$ TeV

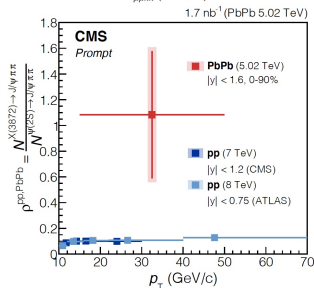
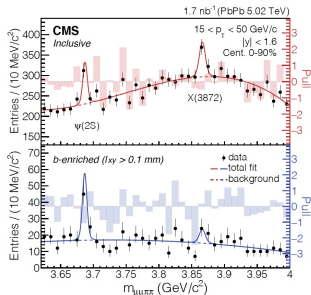
$$X(3872) \rightarrow J/\psi \pi^+ \pi^-$$

$$\rightarrow \mu^+ \mu^- \pi^+ \pi^-$$

- $\rho^{(PbPb)} = \frac{N_{X(3872)}}{N_{\psi(2S)}} = 1.08 \pm 0.9 \pm 0.52$

$$\rho^{(PbPb)} \simeq 10 \rho^{(pp)}$$

Unique experimental input to investigate the properties and nature of multiquark systems



First measurement of $X(3872)$ in p Pb collisions!

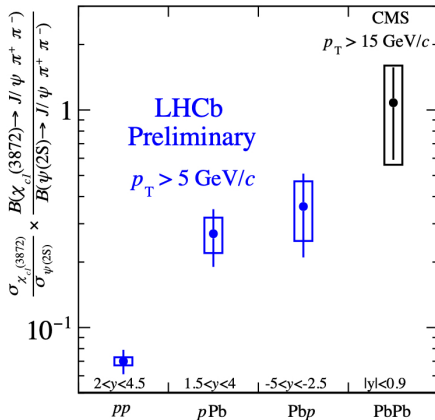
LHCb-LHC,
LHCb-CONF-2022-001 (2022)

- Prompt $X(3872)$ -production in p Pb (Pb p) collisions, $\sqrt{s} = 8.16$ TeV

$$X(3872) \rightarrow J/\psi \pi^+ \pi^- \\ \rightarrow \mu^+ \mu^- \pi^+ \pi^-$$

- $\rho^{(PbPb)} = \frac{N_{X(3872)}}{N_{\psi(2S)}} = 0.27 \pm 0.08 \pm 0.05$

- $X(3872)$: different dynamics in the medium!!
- Higher hadronic densities \rightarrow quark coalescence as the dominant mechanism?!



Strategy 1 - Multiplicity, size dependence, ... in HICs

Hadronic Interactions \Rightarrow Effective Lagrangians



Amplitudes \Rightarrow Cross Sections \Rightarrow Therm. Av. Cross Sections



Coalescence Model, Bjorken picture \Rightarrow Kinetic (rate) equation



Time Evolution and size dependence of $N_{T_{cc}}, N_X$

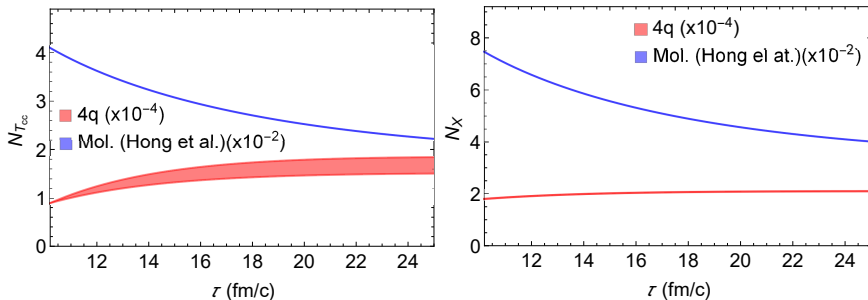


Diff. spatial configuration \Rightarrow diff. hadronic interactions \Rightarrow diff. final yields
 $N_X^{(4q)} \neq N_X^{(Mol)}$

Time Evolution of T_{cc} Multiplicity - Results

Abreu, Navarra, Vieira, PRD (2022); 2202.10882

Pb - Pb at $\sqrt{s_{NN}} = 5.02$ TeV

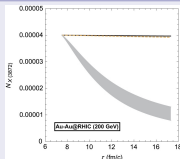


Difference between $N^{(4q)}$ and $N^{(Mol)}(\tau_H)$ decreases but remains large!

Other states

Collaboration USP-UFBA: Navarra, Nielsen, Torres, Kamchandani, LMA, Vasconcellos, Vieira ...

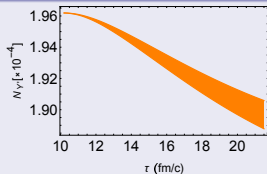
$X(3872) [(cq\bar{c}\bar{q}); 0(1^{++})]$



[PRD 90, 114023 (2014); PTEP 2016, 103B01 (2016)

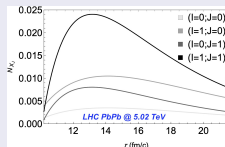
PLB 761, 303 (2016); IJMPA 33, 1850180 (2018), ...]

$\chi_{c1}(4274) [(cs\bar{c}\bar{s}); 0^+(1^{++})]$



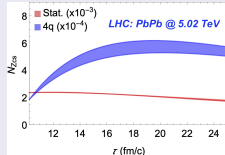
[2306.07446 [hep-ph]; another paper to appear]

$X_J(2900) [\bar{c}\bar{s}ud); 1(0, 1^+)]$



[PRD 103, 036013 (2021); PoS 012 (2022)]

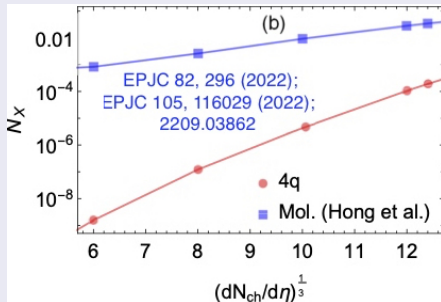
$Z_{cs}(3985)^- [(cs\bar{c}\bar{u})\frac{1}{2}(1^+)]$



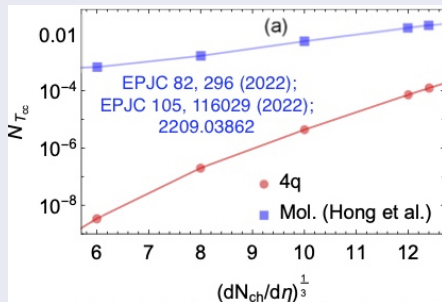
[PRD 106, 076001 (2022); PRD 107 (2023)]

System size dependence

$X(3872) [(cq\bar{c}\bar{q}); 0(1^{++})]$



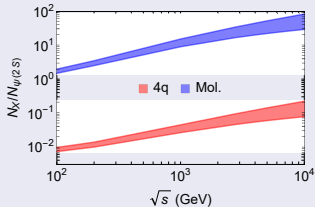
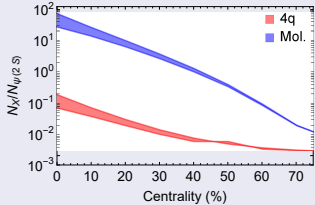
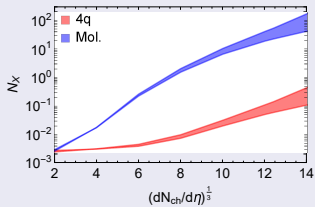
$T_{cc}(3875)^+ [(cc\bar{q}\bar{q}); J^P = 1^+]$



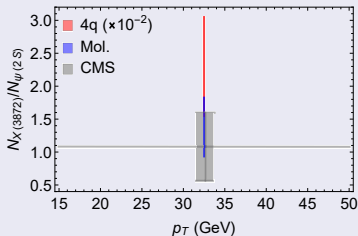
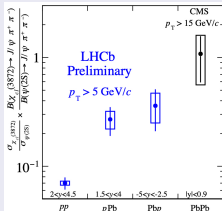
- Multiplicities grow fast with the system size!
- Molecules and tetraquarks: in the same way!



Preliminary results for $R = N_X/N_{\Psi(2S)}$



LHCb-CONF-2022-001 (2022)



Strategy 2 - a challenge: femtoscopy

- Definition - Correlation Function

$$C(\vec{p}_1, \vec{p}_2) = \frac{N(\vec{p}_1, \vec{p}_2)}{N(\vec{p}_1)N(\vec{p}_2)} \simeq \int d^3\vec{r} S_{12}(\vec{r}) |\Psi(\vec{r}, \vec{p})|$$

$S_{12}(\vec{r})$: source function (usually a Gaussian function)

$\Psi(\vec{r}, \vec{p})$: relative outgoing wave function of the two particles

\vec{p} : relative momentum

- Using Bethe–Salpeter approach:

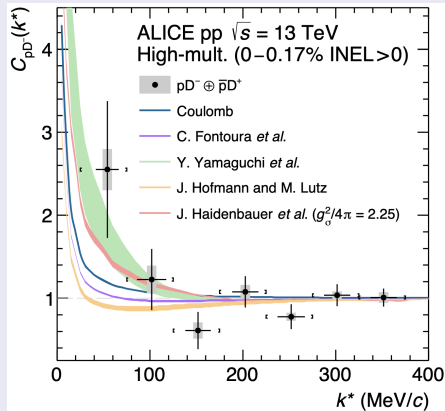
$$C_i(\vec{p}) = 1 + 4\pi \int_0^\infty r^2 dr S_{12}(r) \left(\sum_J |\omega_{ji} \tilde{\Psi}_{ji}(r, \vec{p})|^2 - j_0^2(pr) \right)$$

where

$$\tilde{\Psi}_{ji}(r, \vec{p}) = \delta_{ji} j_0(pr) + T_{ji} \int d^3\vec{q} \frac{j_0(qr)}{E - w_1^{(j)}(\vec{q}) - w_2^{(j)}(\vec{q}) + i\eta}$$

T_{ji} : transition-matrix elements

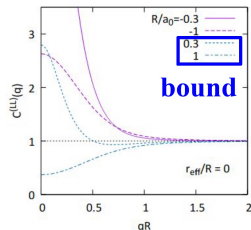
ALICE (2201.05352)



First study of the two-body scattering involving charm hadrons

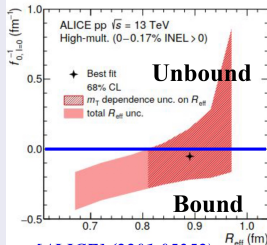
$$k \cot \delta = -\frac{1}{a_0} + \frac{1}{2} r_{\text{eff}} k^2 + \mathcal{O}(k^3)$$

(Nuclear and atomic phys. convention.)

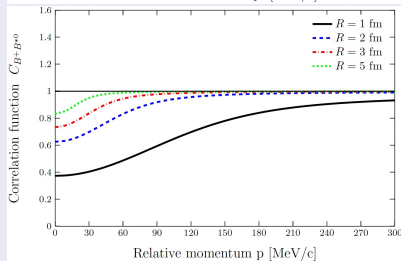
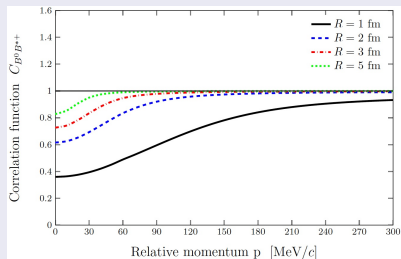


$$k \cot \delta = +\frac{1}{f_0} + \frac{1}{2} r_{\text{eff}} k^2 + \mathcal{O}(k^3)$$

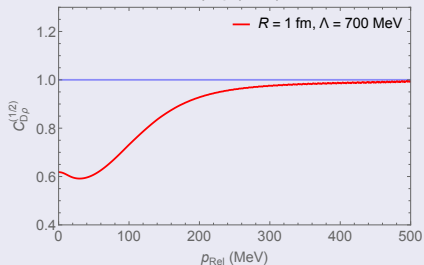
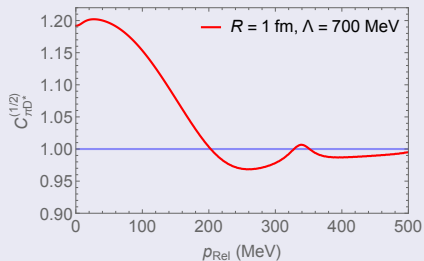
(High-E. phys. convention.)



T_{bb} (UFBA-U. Valencia [Feijoo,
Molina, Oset], U. Huzhou [Dai])
2309.00444 [hep-ph]



Preliminary results: $D_1(2420)$
(UFBA-USP [Alberto, Kanchan])



Summary

- Hadron Spectrum: richer than what we expected
- New particle zoo near $D^{(*)}\bar{D}^*$, $B^{(*)}\bar{B}^*$ thresholds: not $(\bar{q}q, qq\bar{q})$

General description of exotic states?

- It remains a great challenge!!!
- More experimental and theoretical investigations are necessary to shed light into their dynamics
- HICs: promising testing ground for their structure

Thank You!!!

Partial financial support:



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