



ÖSTERREICHISCHE AKADEMIE DER WISSENSCHAFTEN

WinterSchool

January 20 - 24, 2025

Today's Program

Part I: Introduction lecture

14:15 - 15:45

- Overview
- Theoretical Basics
- Data
- Training
- Evaluation
- Design and Techniques

Part II: Hands-on

16:15 - 18:00

- Questions
- Setup
- Some coding



Introduction to Deep Learning



Jan 20, 2025

Overview



Machine Learning as Artificial Intelligence

Artificial Intelligence

Any technique that enables computers to mimic human behaviour



Machine Learning

Learn to perform tasks from data without being explicitly programmed



Deep Learning

Extract patterns from data using deep neural networks

Supervised Learning

Labeled Training Data



Supervised Learning

Labeled Training Data



Face recognition



https://www.theguardian.com/technology/2019/jul/29/ what-is-facial-recognition-and-how-sinister-is-it

Speech recognition



https://support.apple.com/de-de/HT208336

Handwritten transcription

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https://www.behance.net/gallery/71324093/The-Handwritten-A

Medical diagnosis



https://www.wired.com/story/fmri-ai-suicide-ideation/

Unsupervised Learning





Unsupervised Learning



Image clustering



https://neurohive.io/en/state-of-the-art/deep-clustering-approach/

Generation tasks



Reinforcement Learning

Unlabeled Training Data



Game playing



https://deepmind.google/research/breakthroughs/alphago/

Algorithmic trading



https://www.mathworks.com/videos/reinforcement-learning-in-finance-1578033119150 .html

Robotics

Goal-oriented chatbots



https://towardsdatascience.com/training-a-goal-oriented-chatbot-with-deep-reinf orcement-learning-part-i-introduction-and-dce3af21d383



https://www.sciencenews.org/article/reinforcement-learn-ai-humanoid-robots

Reinforcement Learning

Unlabeled Training Data





Supervised Learning Tasks

Classification

Training: learn to predict a label out of a discrete set

Regression

Training: predict a label as a continuous value directly





Testing: accuracy as # of correctly predicted

Testing: distance/similarity to actual outcomes

Unsupervised Learning Tasks

Clustering

Training: learn to identify groups

Generation

Training: create representations to sample realistic outputs



Deep Learning

Deep Neural Networks



Input

Hidden

Output

Deep Learning

Deep Neural Networks



Why this?

- Hierarchical processing: several levels
- All-in-one model: human out of the loop (?!)
- Extremely expressive: can learn "anything"

Deep Learning

Deep Neural Networks



Why this?

- Hierarchical processing: several levels
- All-in-one model: human out of the loop (?!)
- Extremely expressive: can learn "anything"

Why now?

- Unprecedented amount of available data
- Parallelization of computations by GPUs
- Many available toolkits

Theoretical Basics





"Multi-layer Perceptron"



Perceptron



input output

Perceptron



The math



input weights sum non-linearity output

Perceptron



input weights sum non-linearity output

The math...

$$egin{aligned} & [w_1 \quad w_2 \quad w_3] \cdot egin{bmatrix} x_1 \ x_2 \ x_3 \end{bmatrix} = w^T x \ & ext{linear combination} \ & ext{activation} \quad ext{of input} \quad ext{bias} \ & \hat{y} = \sigmaigg(\sum_{i=1}^3 w_i \cdot x_i + bigg) \ & \hat{y} = \sigmaigg(w^T x + bigg) \end{aligned}$$

Single Layer Network

input



layer

The math...

$$z_j = \sigma igg(\sum_{i=1}^3 w_{j,i}^{(1)} \cdot x_i + b_j^{(1)} igg), \, j = 1, \dots, 5$$

Single Layer Network



The math...



input layer

Single Layer Network



 $\begin{bmatrix} w_{1,1}^{(1)} & w_{1,2}^{(1)} & w_{1,3}^{(1)} \\ w_{2,1}^{(1)} & w_{2,2}^{(1)} & w_{2,3}^{(1)} \\ w_{3,1}^{(1)} & w_{3,2}^{(1)} & w_{3,3}^{(1)} \\ w_{4,1}^{(1)} & w_{4,2}^{(1)} & w_{4,3}^{(1)} \\ w_{5,1}^{(1)} & w_{5,2}^{(1)} & w_{5,3}^{(1)} \end{bmatrix} \cdot \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ x_3 \end{bmatrix} = W^{(1)}x + b^{(1)}$ The math... $z_j = \sigma igg(\sum_{i=1}^3 w_{j,i}^{(1)} \cdot x_i + b_j^{(1)} igg), \ j = 1, \dots, 5$ $z=\sigma\Big(W^{(1)}x+b^{(1)}\Big)$ ${\hat y}_j = \sigma igg({\sum\limits_{i = 1}^5 {w_{j,i}^{(2)} \cdot z_i + b_j^{(2)} } } igg), \, j = 1,2$ $\hat{y}=\sigma\Big(W^{(2)}z+b^{(2)}\Big)$

input

output

Multi-layer Network



 $\hat{y} =$

$$\sigma\Bigl(W^{(1)}x+b^{(1)}\Bigr)$$

Multi-layer Network



$$\hat{y} =$$

$$\sigma\Big(W^{(2)}\sigma\Big(W^{(1)}x+b^{(1)}\Big)+b^{(2)}\Big)$$

Multi-layer Network







Non-Linearities: Activation Functions



Biological motivation:

activate neuron if threshold b is exceeded



Non-Linearities: Activation Functions





Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

output within [0,1]

Supervised Learning Tasks









 $\hat{y}_i \in [0,1] o$ probability distribution (soft-max)

predict the value directly



What can a neural network learn?



What can a neural network learn?

anything


What can a neural network learn?

"anything"

Universal Approximation Theorem

"Neural networks with a non-polynomial activation function can approximate any continuous function arbitrary well"

 $\text{For any continuous } f \text{ there is } \theta^\# \text{st. } \left\| \Phi \big(x; \theta^\# \big) - f(x) \right\| < \varepsilon$





What is a dataset?

- An organized collection of data
 - One "unit" of data = an instance / data point
 - Information about a data point = *Features*
 - Labels or other annotations often included
 - \rightarrow Required for supervised tasks but not (necessarily) for unsupervised
 - \circ Normalize it: $[0,1], [-1,1], [0,256], ig(x_{(k)}-\muig)/\sigma$



Properties of a (good) dataset

- What about dataset size...?
 - Defined entirely by the task (from dozens/hundreds to millions)
 - Only certainty is that "the more the merrier", but also "the more representative the merrier"
- <u>Do not forget:</u> the **data split** (~80/20%)







Supervised learning:

Given samples of training data with corresponding labels (x,y)



Iabel y0catIabel y(binary vector with a 1 at
the correct class)1

Goal: Optimize the weights such that

buch that $\Phi(\mathbf{M}) = \mathsf{cat}$ for all of the samples in the training data. but also $\Phi(\mathbf{M}) = \mathsf{cat}$ for samples outside!

How to achieve this goal?

Loss function (*error, cost*) $\mathcal{L}(\hat{y}, y)$: how good is prediction \hat{y} compared to the true label y

- Zero-one loss: $\mathcal{L}_{0-1}(\hat{y}, y) = 1$ if $\hat{y} = y$ and 0 else Is it exactly the same or not?
- Square loss (L2): $\mathcal{L}_{sq}(\hat{y},y) = \left\|\hat{y} y\right\|^2$ Euclidean distance
- Cross entropy loss: $\mathcal{L}_{ce}(\hat{y},y) = -(y\log(\hat{y}) + (1-y)\log(1-\hat{y}))$ maximize likelihood

 \rightarrow minimizing the loss function will improve the prediction!

Idea: Start with random weights

- 1) Take a sample and measure good bad the prediction is:
- 2) Update the weights to improve the prediction (i.e., loss decreases):

Repeat the process for every sample in the training data set.



GOAL: find a weight update rule that produces a sequence that gradually decreases the loss.

$$\left(heta^{(0)}, heta^{(1)}, heta^{(2)},\dots, heta^{(k)}
ight)$$
 such that $\mathcal{L}iggl(\Phiiggl(x; heta^{(0)}iggr),yiggr) \geq \mathcal{L}iggl(\Phiiggl(x; heta^{(1)}iggr),yiggr) \geq \dots \geq \mathcal{L}iggl(\Phiiggl(x; heta^{(k)}iggr),yiggr) \geq \dots \geq \mathcal{L}iggl(\Phiiggl(x; heta^{(k)}iggr),yiggr)$

As training progresses, later weights should result in smaller losses.

And do it over the whole training set:

$$heta^{\#} := rgmin_{ heta}rac{1}{K}\sum_{k=1}^{K}\mathcal{L}ig(\Phiig(x_{(k)}; hetaig),y_{(k)}ig)$$

Find the weights which result in minimal loss over the whole training set.



 \rightarrow non-linear, non-convex optimization problem!

Special Case: Linear Perceptron



Loss
$$\mathcal{L}_{sq}(\hat{y},y) = \left\|\hat{y}-y
ight\|^2$$

Least squares problem!





Gradient Descent

Gradient of the loss: "how does the loss change, if a weight changes?"

$$abla L\left(w_1,\ldots,w_n
ight) = egin{bmatrix}rac{\partial L}{w_1}\dots\ rac{\partial L}{w_n}\end{pmatrix}$$

 \rightarrow points to **steepest ascent** (i.e., the direction to change the weights, so that there is maximal change in the loss)

Gradient Descent



Gradient Descent



go opposite direction of steepest ascent

Gradient Descent



go opposite direction of steepest ascent

Gradient Descent



go opposite direction of steepest ascent

$$w_1^{new} \gets w_1^{old} - \eta \cdot
abla \mathcal{L}ig(w_1^{old}ig)$$

Gradient Descent

Gradient of the loss:

 \rightarrow points to steepest ascent



Gradient Descent

Gradient of the loss:

 \rightarrow points to steepest ascent

Algorithm

Initialize $heta^{(0)}, \eta > 0$ Until convergence: Compute gradient $\nabla \mathcal{L}(\theta^{(n)})$ Update weights $\theta^{n+1} \leftarrow \theta^n - \eta \cdot
abla \mathcal{L}\left(heta^{(n)}
ight)$ Return weights "learning rate"

Training on Batches

Gradient descent is very expensive...

Example: A single step of gradient descent for AlexNet (neural network ~160M parameters) on ImageNet (dataset ~1.2M images) requires ~2*10^14 flops!

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Train on small batches of the dataset!

"Training with large minibatches is bad for your health. More importantly, it's bad for your test error. Friends don't let friends use minibatches larger that 32."

-Yann LeCun

Evaluation







Training-Test



Over- and underfitting

Example: Learn a second-degree polynomial from noisy observations



ground truth deg = 2

Over- and underfitting

Example: Learn a second-degree polynomial from noisy observations



ground truth deg = 2



underfitting deg too low

Simple model:

high bias, good capturing of essentials, bad fit

Over- and underfitting

Example: Learn a second-degree polynomial from noisy observations



ground truth deg = 2



12m

underfitting deg too low

overfitting deg too high

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Complex model:

high variance, good fit to data, too specific

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ground truth deg = 2



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high variance, good fit to data, too exact



Trade-off between model assumptions (bias) and model complexity (variance)

Training-Validation-Test



Training-Validation-Test



Training-Validation-Test



Metrics of performance

• Defined by the task: MSE, accuracy, mAP, etc...

 $accuracy = rac{number\,of\,correct\,predictions}{total\,number\,of\,predictions}$

• In case of **classification**:







Interpretability

- XAI: steering away from the black box
- Crucial in high-responsibility decision making, e.g. medicine
- **TOOLS:** explainable architecture, post-hoc analysis, etc.



Wu et al., 2023: Discover and Cure - Concept-aware Mitigation of Spurious Correlation

• Mitigating bias

- Especially important in decision making with a social effect (e.g., granting parole [1])
- **TOOLS:** metrics to assess group fairness (demographic parity, equalized odds, etc.), transparency about biases in the data collection process...

	WHITE	AFRICAN AMERICAN
Labeled Higher Risk, But Didn't Re-Offend	23.5%	44.9%
Labeled Lower Risk, Yet Did Re-Offend	47.7%	28.0%

Design and Techniques



Common Techniques

Regularizing:

Dropout:

$$\min_{ heta}\mathcal{L}\left(heta
ight)+\lambda\cdot r\left(heta
ight)$$

regularization term of the network weights

..often
$$r(heta) = \| heta\|^p$$

set weights to zero at random



Stochastic Gradient Descent (SGD):

use the gradient of a randomly selected subset

Batch normalization:

normalize the samples w.r.t. to the other samples in the batch

Popular architectures

Convolutional neural networks: apply "filters" to extract spatial features, textures, patterns, etc.

- Popular choice in image processing.
- Examples: VGG-16, VGG-19, AlexNet, etc.

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- Example: Variational Autoencoders (VAE)
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- Useful in applications requiring large networks: image segmentation, object detection, etc.
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- Example: ResNet

Transformers: capture relationships in sequential data by considering the whole context.

- Useful in applications with sequential data (e.g., text), but also otherwise (vision transformers).
- Examples: GPTs, BERT, ViT, DINOv2

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Using Google Colab and PyTorch.

Open the notebook Intro_WS_2025.ipynb.

Follow the instructions in the notebook.

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