

Probing $\mu\tau$ flavor violating solutions for the muon $g-2$ anomaly at Belle II

IPA2022 Vienna
Sept. 5–9, 2022

Syuhei Iguro

• [Inspire](#)

• [Web page](#)



Based on

JHEP 09 (2020) 144 with Y. Omura, M. Takeuchi

See also for the relevant works

JHEP 1911 (2019) 130 with Y. Omura, M. Takeuchi,

Phys.Rev.D 101 (2020) 7, 075011 with C.-P. Yuan, A. Kirtmaan,

JHEP 06 (2020) 040 with M. Endo, T. Kitahara,

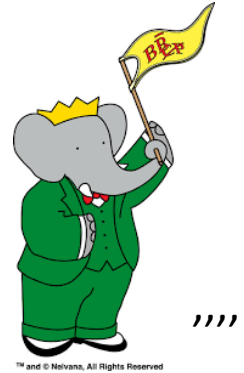
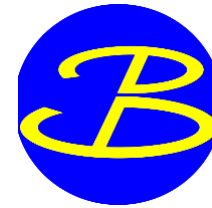
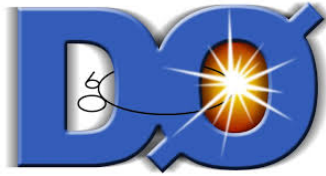
Thanks for the invitation

Key words: Flavor, collider experiment, lepton flavor violation

Menu

- Introduction of the muon $g-2$ and status
- Our simplified model
 - scalar with LFV interactions
- Collider signal
 - Belle II prospect
- Summary

Our SM is a very good theory to describe almost all measurements



However, large part of theorists is not satisfied with the SM.

Mysteries of the SM

Dark Matter, neutrino masses, matter vs antimatter asymmetry, strong CP problem, fine tuning of Higgs mass, Yukawa hierarchy,,,,,

Each problem has several New Physics (NP) solutions and we need further hints to specify the scenario!

Deviations in flavor physics may be a hint for NP?

muon g-2 anomaly

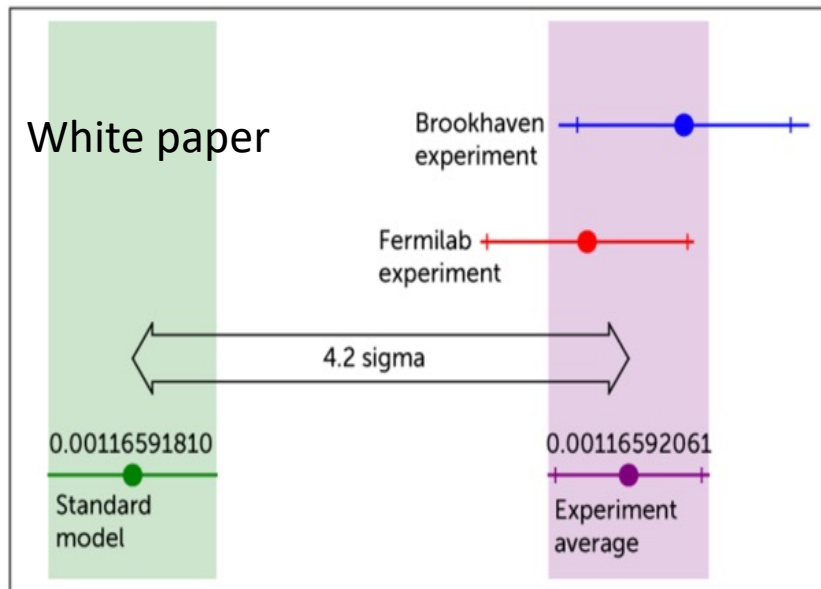
Overview: yesterday by Carlo Ferrari

$$\vec{\mu} = -g \frac{e}{2m} \vec{S}$$

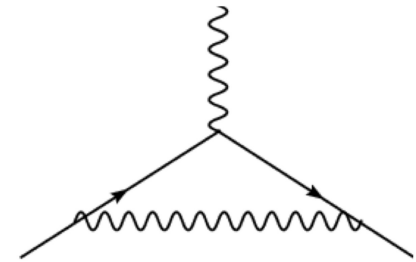
$\vec{\mu}$: Magnetic moment of the muon

$g=2$: tree level corresponds to 2 freedoms (spin up and down)

Anomalous magnetic moment: $\alpha_{\mu} = (g - 2)/2$



Muon magnetic anomaly



Many developments

Theoretical calculation:
5-loop QED, lattice calculation,
Hadronic Light-by-Light,
Hadronic Vacuum Polarization,,,

$$\Delta a_{\mu} = a_{\mu}^{\text{Exp}} - a_{\mu}^{\text{SM}} \sim 2.5 \times 10^{-9}$$

Hint for BSM?

Recent lattice favors smaller gap but
new problem arises in the EW fit, $e^+e^- \rightarrow 2\pi$

If this anomaly is true, we have a hint for new physics!

$g-2$



My criteria of the anomaly

- Long standing? -> yes. 20 years old
- Multiple experiments? -> yes but need J-PARC
- Statistical significance? -> yes, 4.2σ

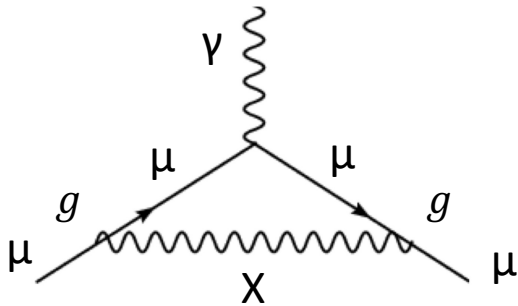
R_D, R_K



What kind of new physics you need?

Naïve new physics scale to explain muon g-2 anomaly.

$$L \sim \frac{e \Delta a_\mu}{m_\mu} \mu_L \sigma^{\mu\nu} \mu_R F_{\mu\nu}$$



If new particle X appear at 1-loop with a flavor conserving coupling

$$\Delta a_\mu \sim \frac{g^2}{16\pi^2} \frac{m_\mu^2}{m_X^2} \sim 3 \times 10^{-9} \left(\frac{100 \text{ GeV}}{m_X} \right)^2 \quad g \sim g_W = 0.66$$

EW scale !
No signal in LHC so far

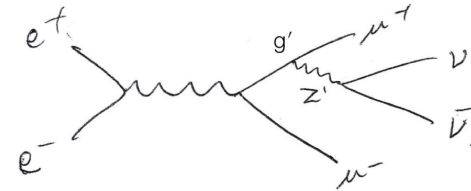
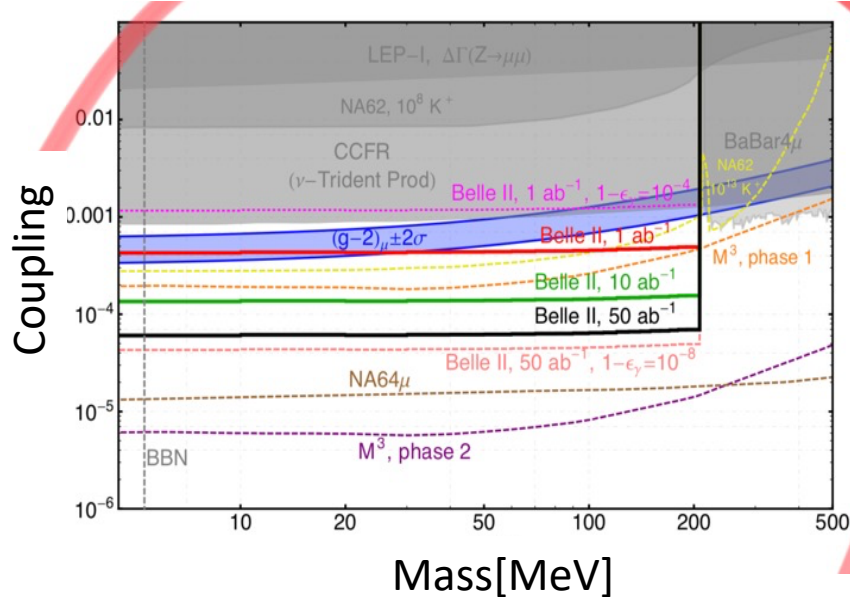
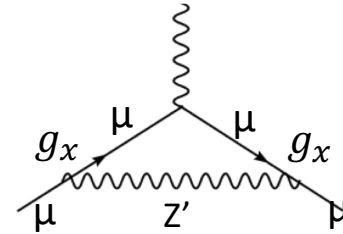
What kind of new physics scenarios are still allowed?

Light particle is available.

flavor conserving regime

e.g. Z' : $L_\mu - L_\tau$ (global $U(1)$).

particle	$L_2 = (\nu_{\mu L}, \mu_L)$	$L_3 = (\nu_{\tau L}, \tau_L)$	$(\mu_R)^c$	$(\tau_R)^c$	$(\nu_{\mu R})^c$	$(\nu_{\tau R})^c$	others
charge	+1	-1	-1	+1	-1	+1	0

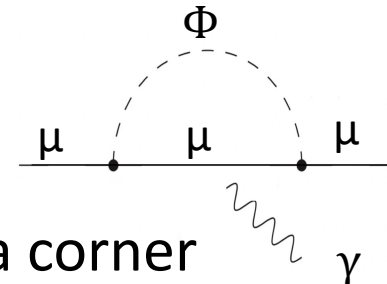


The scenario will be explored soon in Belle II!

1904.13053: $2\mu + \text{missing}$

also

Heavy scenario like muon specific 2HDM is driven into a corner and will be fully probed at LHC in near future.



What's else?

If there is some mechanism to enhance the contribution of Δa_μ , heavier mass and/or smaller coupling are enough for muon g-2. Then it is more easy to evade constraints.

$$\Delta a_\mu \sim \frac{g^2}{16\pi^2} \frac{m_\mu^2}{m_X^2} \sim 3 \times 10^{-9} \left(\frac{100 \text{ GeV}}{m_X} \right)^2$$



What's else?

If there is some mechanism to enhance the contribution of Δa_μ , heavier mass and/or smaller coupling are enough for muon g-2. Then it is more easy to evade constraints.

$$\Delta a_\mu \sim \frac{g^2}{16\pi^2} \frac{m_\mu^2}{m_X^2} \sim 3 \times 10^{-9} \left(\frac{100 \text{ GeV}}{m_X} \right)^2$$



One solution is

Chirality enhancement

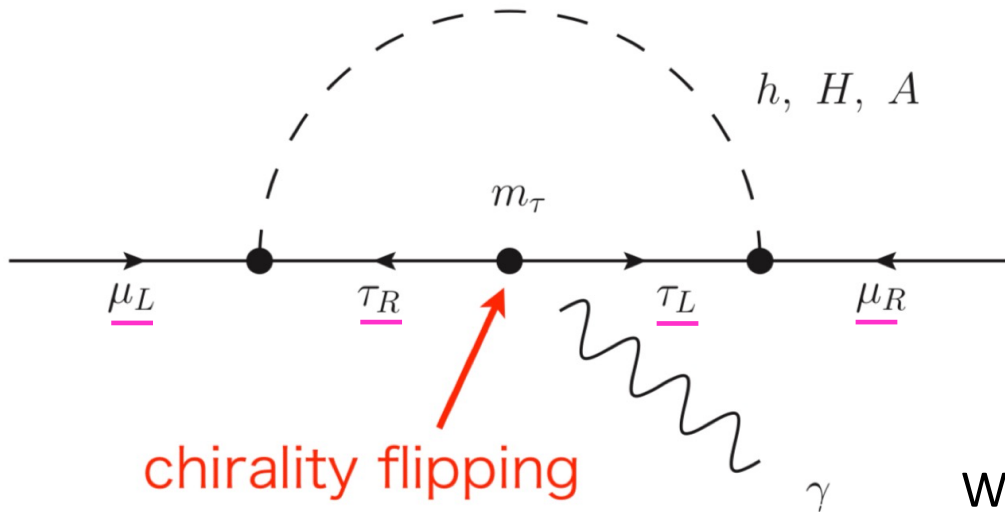
Chirality enhancement

$$\frac{e\Delta a_\mu}{m_\mu} \mu_L \sigma^{\mu\nu} \mu_R F_{\mu\nu}$$

$\Delta a_\mu \propto m_\mu^2$ for common scenarios

Chirality flip with a heavy internal fermion mass ($\gg m_\mu$)

e.g. flip with tau mass



$$\frac{m_\tau}{m_\mu} \sim 17$$

chirality flipping
with tau mass!

When $\Delta a_\mu \propto \text{coupling}^2$,
coupling can be smaller by $\sqrt{17}$

Such a particle can explain muon g-2 with smaller couplings

Model examples

- $\tau\mu$ flavor violating scalars S. Nie and M. Sher 9875376
- $\tau\mu$ flavor violating gauge boson,

Soni, et al 1607.06832

τ mass enhancement

$$m_\tau/m_\mu \sim 17$$

- Scalar leptoquark (LQ) is also discussed

Bauer, Neubert 1511.01900

Top mass enhancement

$$m_t/m_\mu \sim 1600$$

- Mixing with heavy vector like leptons

Czarnecki, Marciano 0102122

Heavy lepton mass enhancement

$$m_L/m_\mu \sim 10 \times m_L [\text{GeV}]$$

Menu

- Introduction
- **Simple Model**
- Belle II signal
- Summary

One realistic model

Tsumura, Abe, Toma 1904.10908

$(SU(3)_c, SU(2)_L)_{U(1)_Y}$

Discrete symm.

$$\Phi = \begin{pmatrix} H^+ \\ \frac{H+iA}{\sqrt{2}} \end{pmatrix}$$

Additional neutral scalars: H,A

Extra singlet scalar is needed for the neutrino masses

Particle	SM	Z_4
(L_e, L_μ, L_τ)	$(1, 2)_{-1/2}$	$(1, i, -i)$
(e_R, μ_R, τ_R)	$(1, 1)_{-1}$	$(1, i, -i)$
H	$(1, 2)_{1/2}$	1
New entry Φ	$(1, 2)_{1/2}$	-1

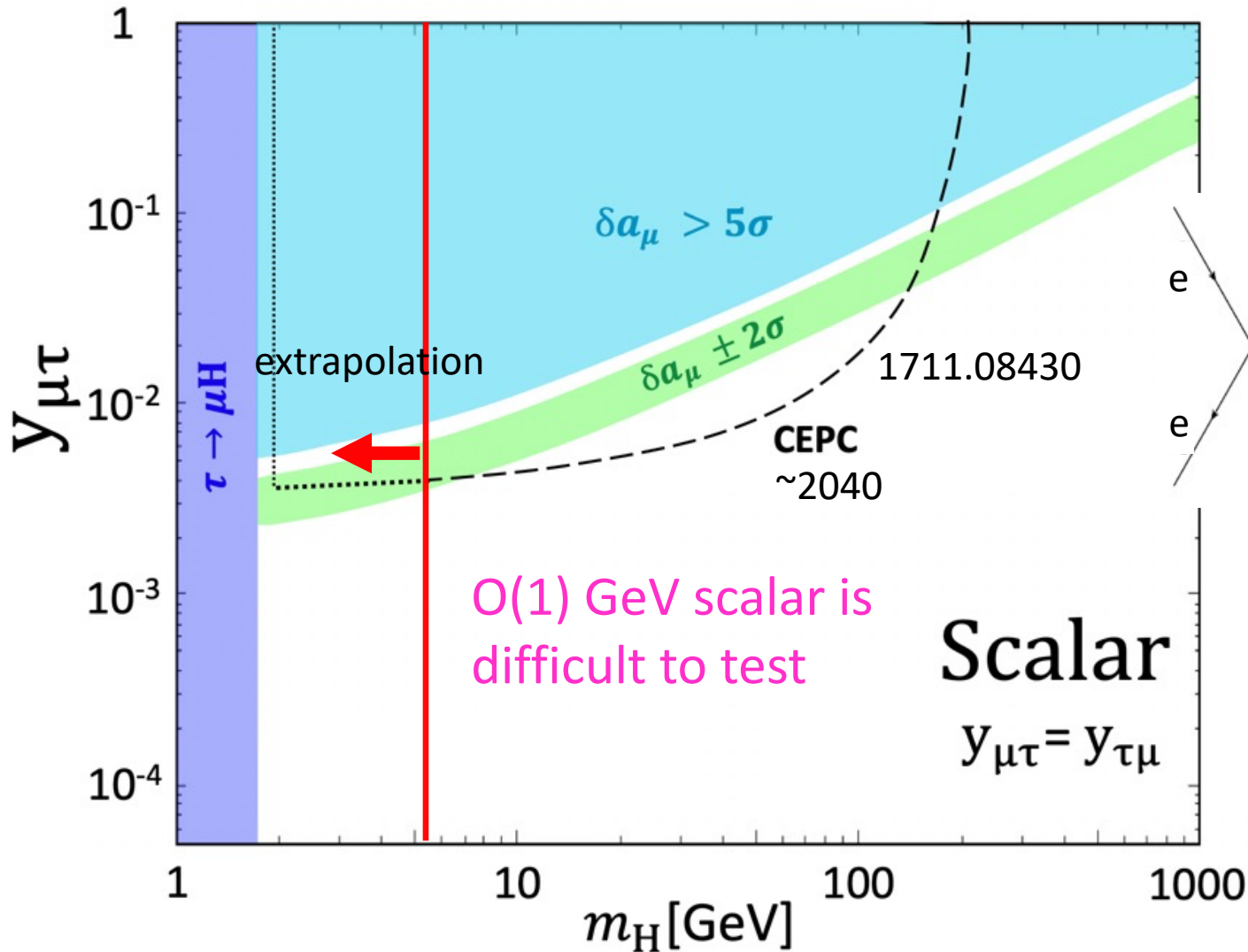
$$-\mathcal{L}_{Z_4}^{\text{yukawa}} = \bar{\ell}_R \begin{pmatrix} y_e H^\dagger & & \\ & y_\mu H^\dagger & \underline{y_{\mu\tau} \Phi^\dagger} \\ & \underline{y_{\tau\mu} \Phi^\dagger} & y_\tau H^\dagger \end{pmatrix} L + \text{H.c.}$$

Additional scalars in Φ can only couple to $\mu\tau$. $m_H \ll m_A = m_{H^\pm}$

We only consider a scalar (H) as a demonstration

muon $g - 2$ in $\mu\tau$ philic scalar model

2002.12728 S. Iguro et al



Other constraints?

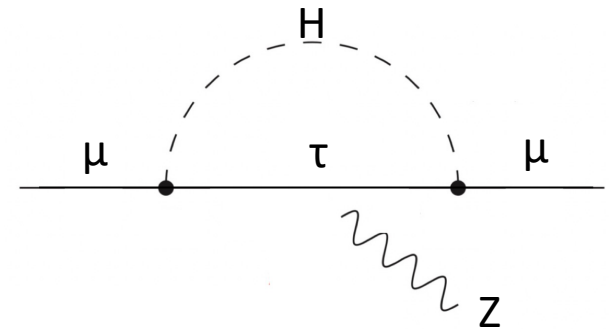
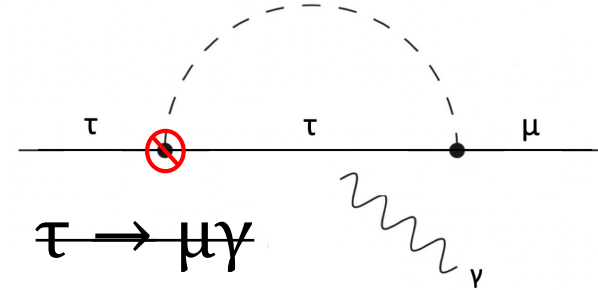
If only LFV couplings are sizable, it is difficult to test in flavor physics.

- 1-loop contribution to $Z \rightarrow \mu\mu$ is small.
 \Rightarrow the correction is 1-2 order smaller than LEP sensitivity.
- Additional scalar does not talk to quarks.
 \Rightarrow LHC production cross section is small and difficult for a GeV order scalar due to threshold (interesting for EW scale scenario (Discussed later)).

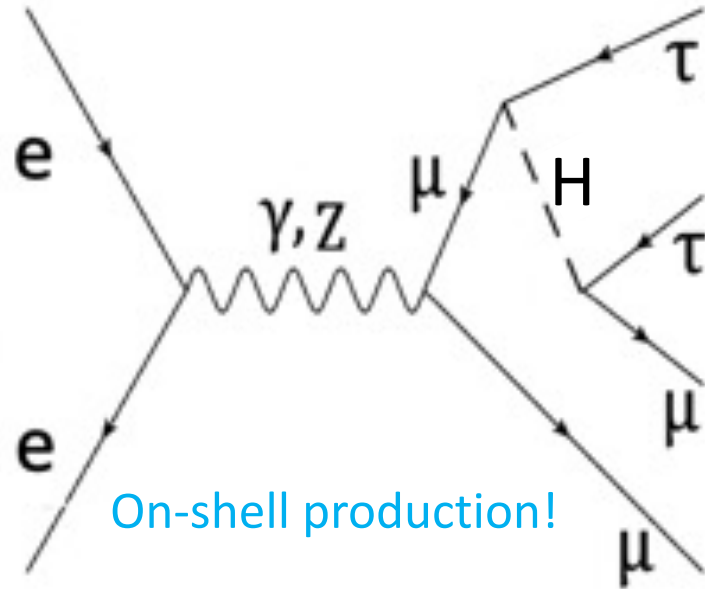


How we test the light scenario?

Diagonal coupling is prohibited by Z_4 symmetry



Proposal: $\mu^{\mp}\mu^{\mp}\tau^{\pm}\tau^{\pm}$ final state in Belle II



Distinctive features of our signal

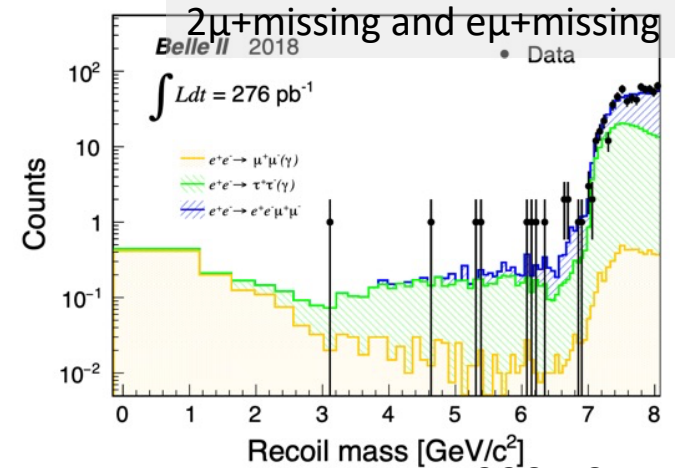
- $\mu\tau$ LFV resonance
- same sign lepton pairs

We required that all the visible particles are within the detector

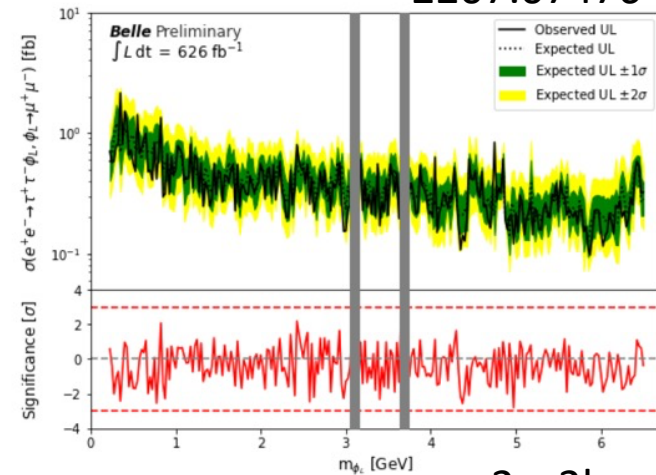
Madgraph + Pythia 8

Syuhei Iguro IPA_09/09/2022

Similar to Belle II 1912.11276



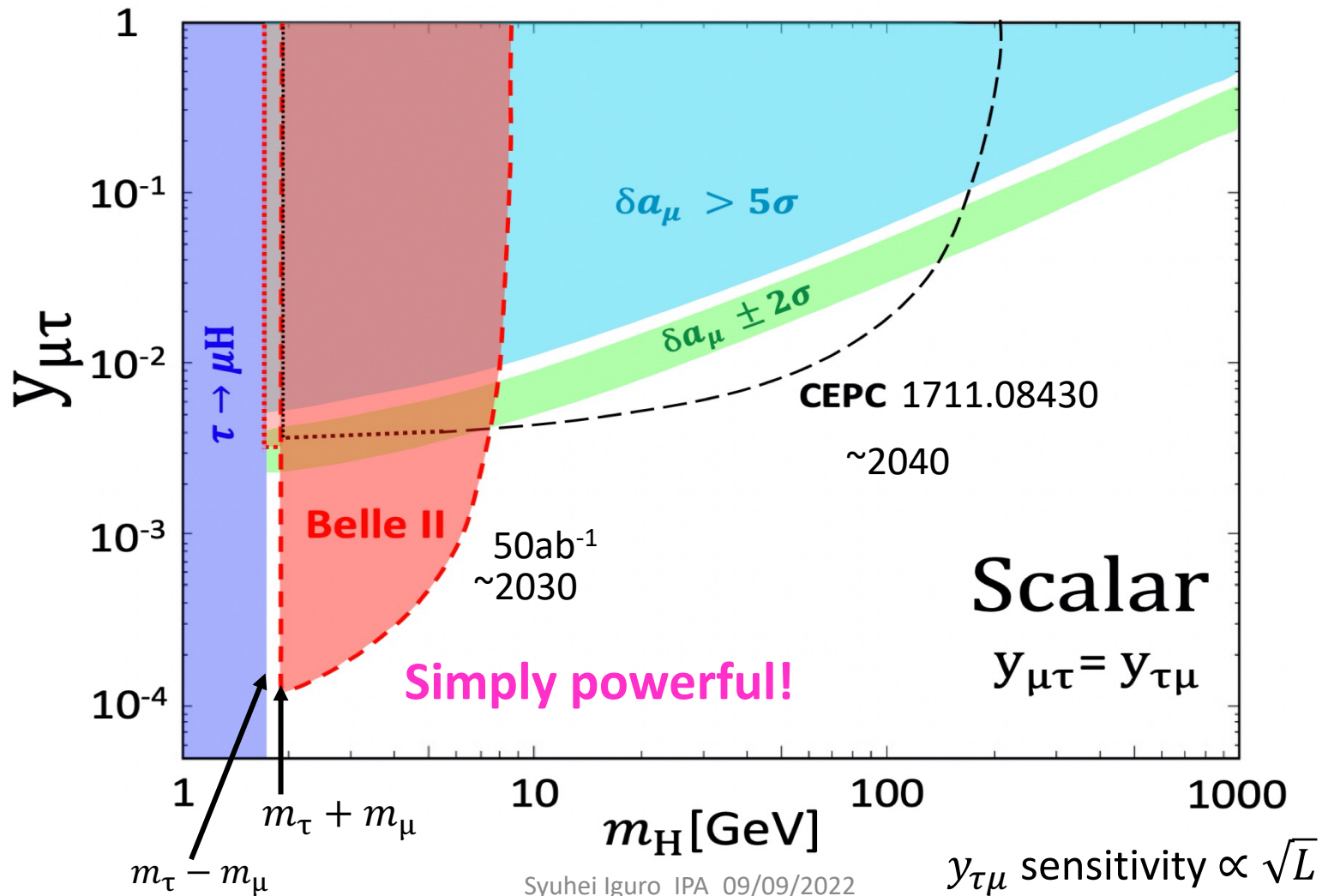
2207.07476



assuming BG free

$g - 2$ in $\mu\tau$ -philic scalar model at Belle II

2002.12728 S. Iguro et al

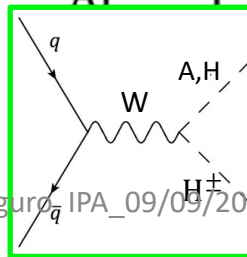
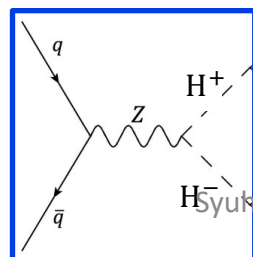
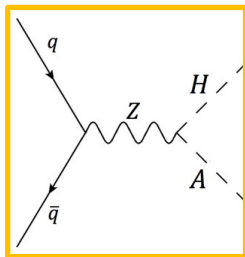
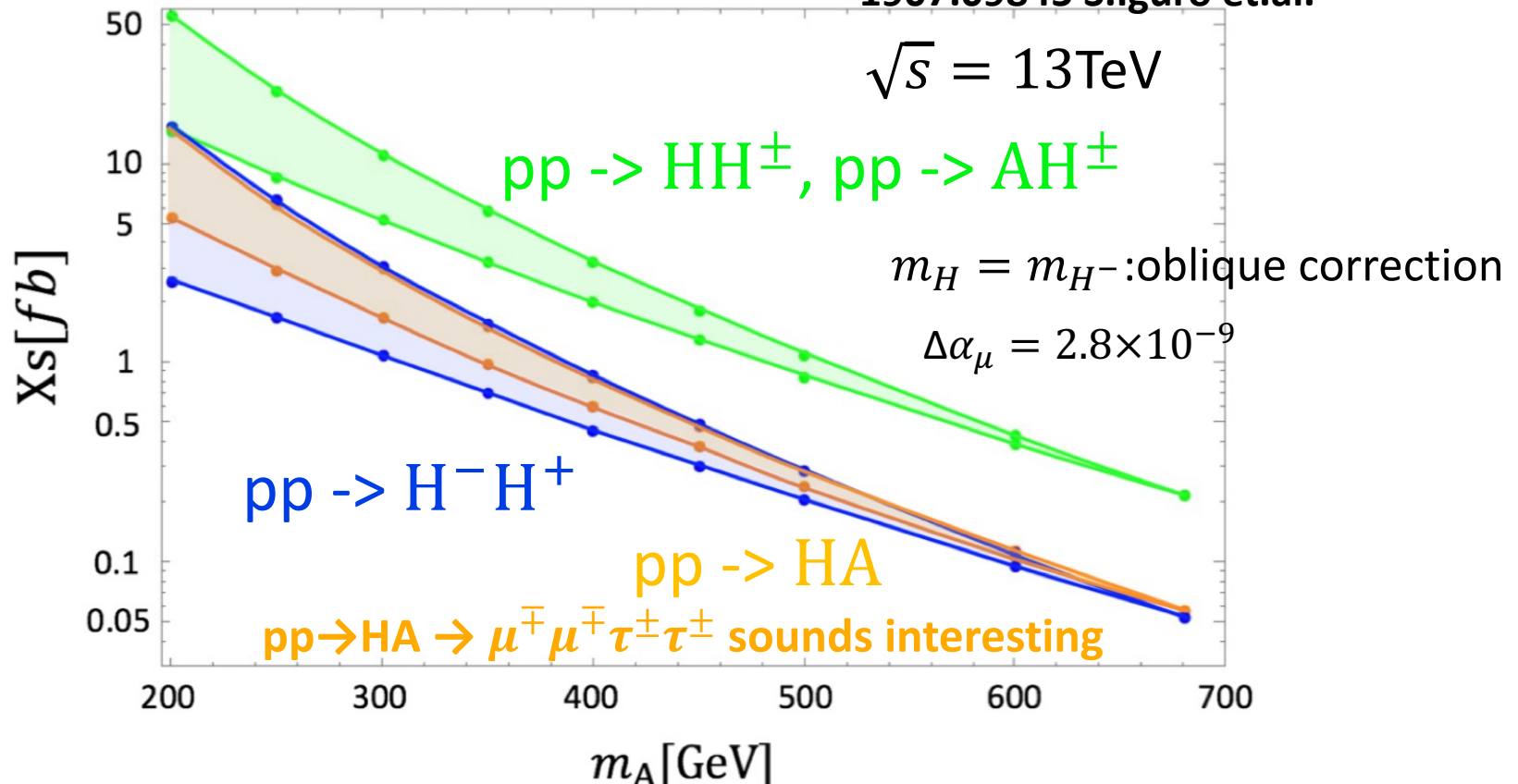


Heavy scalar scenario

Electroweak production in LHC

- Maximum mass gap in H and A is given as $m_H^2 = m_A^2 + \lambda_5 v^2 = m_A^2 + v^2$ (for $\lambda_5 < 1$)
- Minimum mass gap is given by $|y_e^{\mu\tau}|, |y_e^{\tau\mu}| < 1$.

1907.09845 S.Iguro et.al.

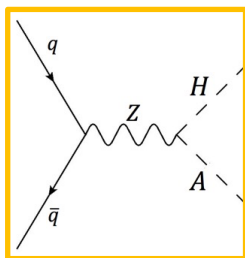
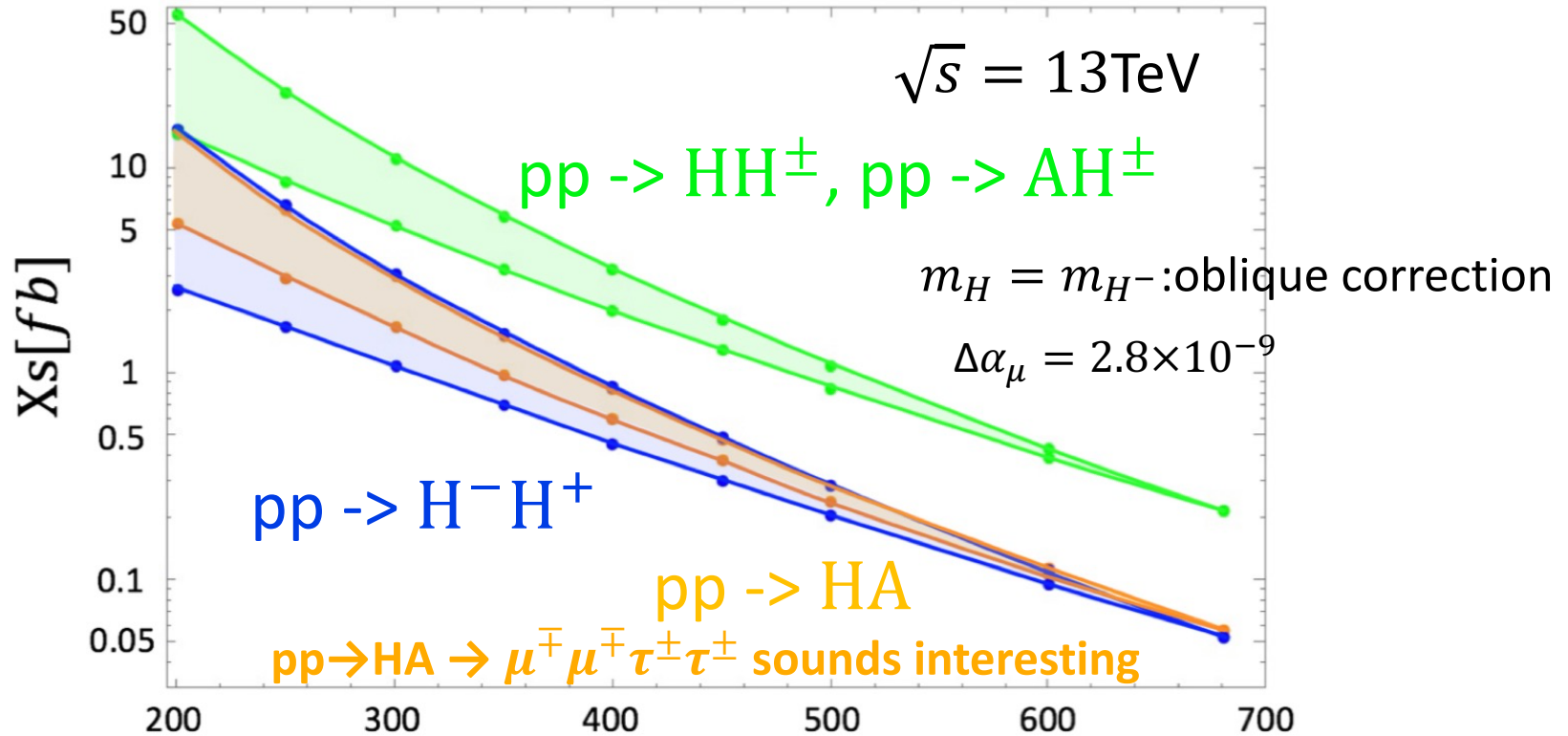


Syukei Iguro, IPA_09/09/2022

Heavy scalar scenario

Electroweak production in LHC

- Maximum mass gap in H and A is given as $m_H^2 = m_A^2 + \lambda_5 v^2 = m_A^2 + v^2$ (for $\lambda_5 < 1$)
- Minimum mass gap is given by $|y_e^{\mu\tau}|, |y_e^{\tau\mu}| < 1$.



Run 2 data is sensitive up to 500 GeV.
HL-LHC is sensitive up to 1150 GeV.

Summary

$\mu\tau$ lepton flavor violating scalars can explain the muon $g-2$ discrepancy.

The model predicts distinctive $\mu^{\mp}\mu^{\mp}\tau^{\pm}\tau^{\pm}$ final state in colliders.

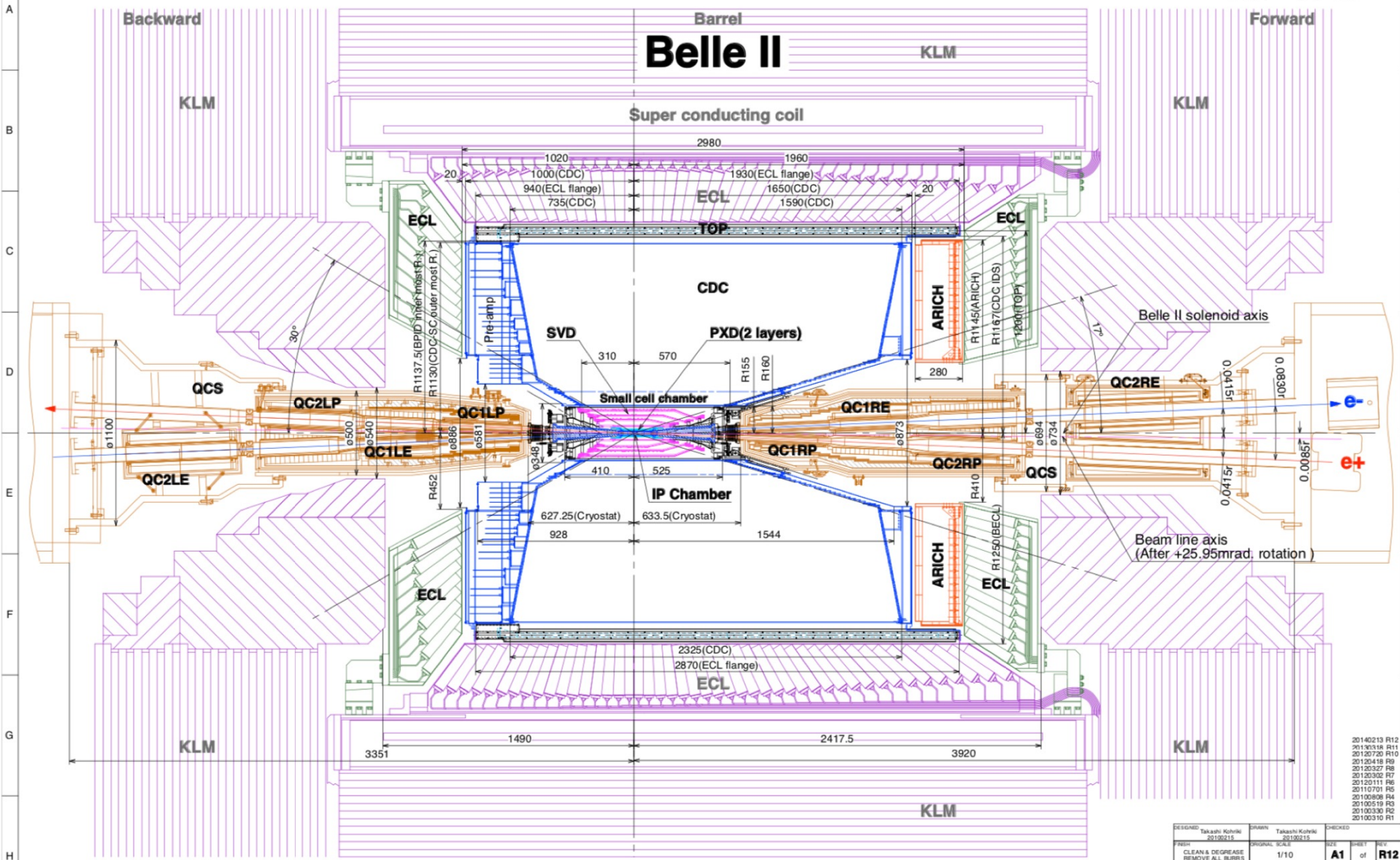
Belle II with 50ab^{-1} can test the scenario when the mass is $O(1)$ GeV.

LHC is also important for the heavy scenario.

Comment: However, I skipped in this talk, the $\mu\tau$ LFV scalar model can explain the dark matter and neutrino masses with singlet scalars in type-I seesaw. See, 2205.08998 for model setup.

Thank you!

TOP VIEW



- 20140213 R10
- 20130316 R11
- 20120720 R10
- 20120418 R9
- 20120327 R8
- 20120302 R7
- 20120111 R6
- 20111070 R5
- 20110606 R4
- 20100519 R3
- 20100330 R2
- 20100310 R1

DESIGNED	Takashi Kohno 20120215	DRAWN	Takashi Kohno 20120215	CHECKED	
FINISH	CLEAN & DEGREASE REMOVE ALL BURRS	ORIGINAL SCALE	1/10	SIZE	A1 of R12
FILE	Belle-II(Nano beam)		PROJECT	Belle-II-Topview41.5.vnx	
PROJECTION	Belle II				

20140213 R12
 -QCS20131203
 -CDC covers
 -B&FWD new pole pieces

Table 17: Summary of the detector components.

Purpose	Name	Component	Configuration	Readout channels	θ coverage
Beam pipe	Beryllium		Cylindrical, inner radius 10 mm, 10 μm Au, 0.6 mm Be, 1 mm paraffin, 0.4 mm Be		
Tracking	PXD	Silicon Pixel (DEPFET)	Sensor size: $15 \times (\text{L1 } 136, \text{ L2 } 170) \text{ mm}^2$, Pixel size: $50 \times (\text{L1a } 50, \text{ L1b } 60, \text{ L2a } 75, \text{ L2b } 85) \mu\text{m}^2$; two layers at radii: 14, 22 mm	10M	[17°;150°]
	SVD	Silicon Strip	Rectangular and trapezoidal, strip pitch: $50(\text{p})/160(\text{n}) - 75(\text{p})/240(\text{n}) \mu\text{m}$, with one floating intermediate strip; four layers at radii: 38, 80, 115, 140 mm	245k	[17°;150°]
	CDC	Drift Chamber with He-C ₂ H ₆ gas	14336 wires in 56 layers, inner radius of 160mm outer radius of 1130 mm	14k	[17°;150°]
<u>Particle ID</u>	TOP	RICH with quartz radiator	16 segments in ϕ at $r \sim 120 \text{ cm}$, 275 cm long, 2cm thick quartz bars with 4×4 channel MCP PMTs	8k	<u>[31°;128°]</u>
	ARICH	RICH with aerogel radiator	$2 \times 2 \text{ cm}$ thick focusing radiators with different n , HAPD photodetectors	78k	<u>[14°;30°]</u>
<u>Calorimetry</u>	ECL	CsI(Tl)	Barrel: $r = 125 - 162 \text{ cm}$, end-cap: $z = -102 - +196 \text{ cm}$	6624 (Barrel), 1152 (FWD), 960 (BWD)	<u>[12.4°;31.4°]</u> , [32.2°;128.7°], <u>[130.7°;155.1°]</u>
<u>Muon ID</u>	KLM	barrel:RPCs and scintillator strips	2 layers with scintillator strips and 12 layers with 2 RPCs	θ 16k, ϕ 16k	[40°;129°]
	KLM	end-cap: scintillator strips	12 layers of $(7-10) \times 40 \text{ mm}^2$ strips	17k	[25°;40°], <u>[129°;155°]</u>

Muon specific 2HDM is available.

flavor conserving

1705.01469, Abe et al.

Table I: Particle contents and the charge assignment.

	q_L^j	u_R^j	d_R^j	ℓ_L^e	ℓ_L^τ	ℓ_L^μ	e_R	τ_R	μ_R	H_1	H_2
$SU(3)_c$	3	3	3	1	1	1	1	1	1	1	1
$SU(2)_L$	2	1	1	2	2	2	1	1	1	2	2
$U(1)_Y$	1/6	2/3	-1/3	-1/2	-1/2	-1/2	-1	-1	-1	1/2	1/2
Z_4	1	1	1	1	1	<u>i</u>	1	1	<u>i</u>	<u>-1</u>	1

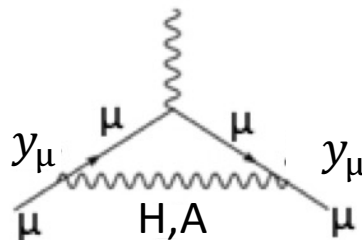
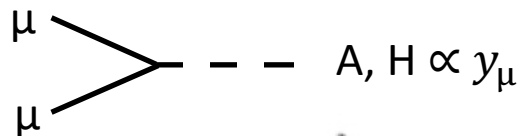
$$i = e^{i\frac{\pi}{2}}$$

H_1 only couples to $\mu\mu$

$$\mathcal{L}^{\text{Yukawa}} = -\bar{q}_L \tilde{H}_2 Y_u u_R - \bar{q}_L H_2 Y_d d_R - \bar{L}_L H_1 Y_{\ell 1} E_R - \bar{L}_L H_2 Y_{\ell 2} E_R + (h.c.),$$

$$Y_{\ell 1} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_\mu \end{pmatrix}$$

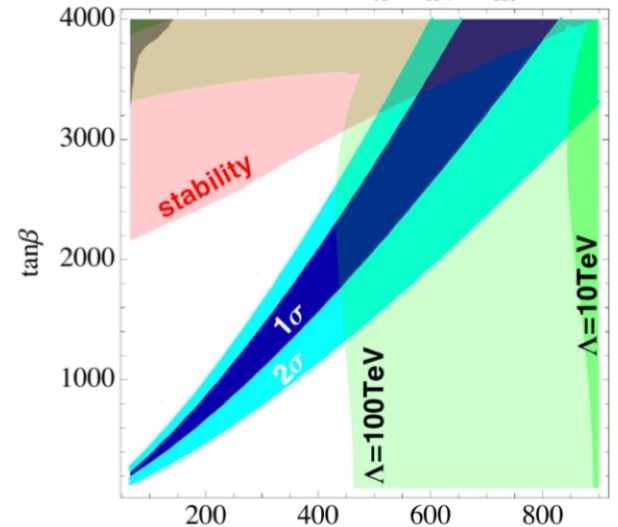
$$y_\mu = \frac{\sqrt{2}m_\mu}{v} \sqrt{1+t_\beta^2} \simeq 0.6 \left(\frac{t_\beta}{1000} \right)$$



$$H_1 = \begin{pmatrix} H^+ \\ \frac{H + iA + v'}{\sqrt{2}} \end{pmatrix} \quad H_2 = \begin{pmatrix} G^+ \\ \frac{v'' + h + iG}{\sqrt{2}} \end{pmatrix}$$

$$\tan\beta = v''/v' \quad v = \sqrt{v'^2 + v''^2}$$

$$m_A = m_{H^\pm} = m_{H_0} + 80 \text{ GeV}$$



$$m_\mu = \frac{v}{\sqrt{2}} \frac{y_\mu}{\sqrt{1+t_\beta^2}}, \quad m_f = \frac{v}{\sqrt{2}} \frac{y_f t_\beta}{\sqrt{1+t_\beta^2}} \quad \text{others}$$

Muon specific 2HDM is available.

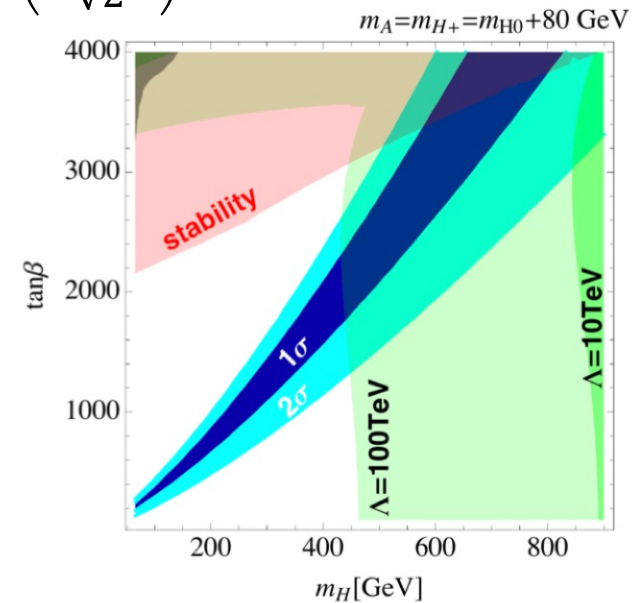
flavor conserving

1705.01469

Table I: Particle contents and the charge assignment.

	q_L^j	u_R^j	d_R^j	ℓ_L^e	ℓ_L^τ	ℓ_L^μ	e_R	τ_R	μ_R	H_1	H_2
$SU(3)_c$	3	3	3	1	1	1	1	1	1	1	1
$SU(2)_L$	2	1	1	2	2	2	1	1	1	2	2
$U(1)_Y$	1/6	2/3	-1/3	-1/2	-1/2	-1/2	-1	-1	-1	1/2	1/2
Z_4	1	1	1	1	1	i	1	1	i	-1	1

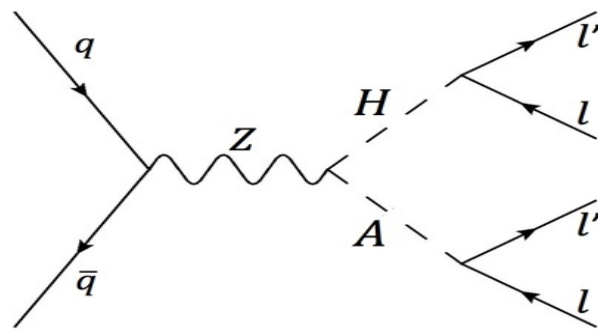
$$H_1 = \left(\frac{H^+}{\sqrt{2}} \right) \quad \text{in large } \tan\beta \text{ limit}$$



H_1 only couples to $\mu\mu$

$$\mathcal{L}^{\text{Yukawa}} = -\bar{q}_L \tilde{H}_2 Y_u u_R - \bar{q}_L H_2 Y_d d_R - \bar{L}_L H_1 Y_{\ell 1} E_R - \bar{L}_L H_2 Y_{\ell 2} E_R + (h.c.),$$

$$Y_{\ell 1} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_\mu \end{pmatrix}$$



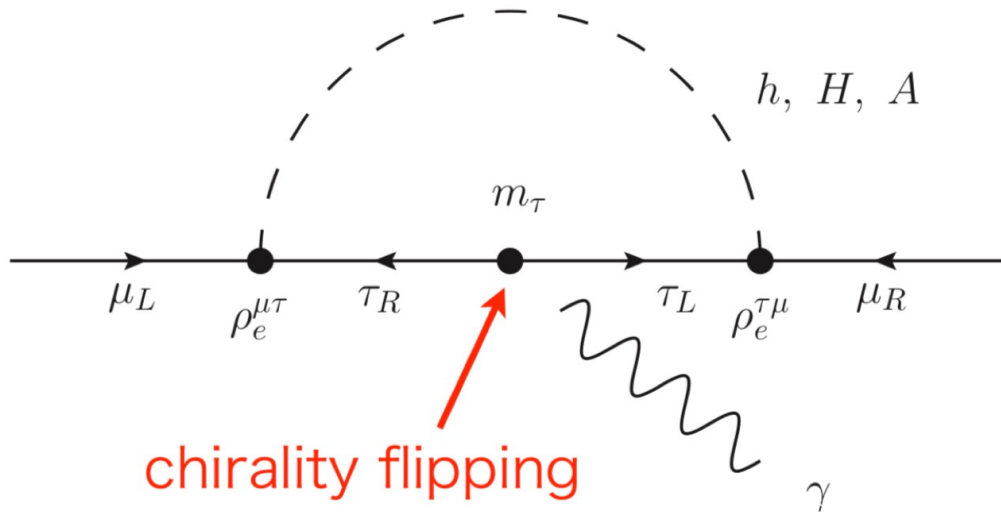
Multi lepton search in LHC(36fb⁻¹)

$m_H \lesssim 640 \text{ GeV}$ is excluded at 95% CL

The scenario will be explored in LHC!

Light pseudo scalar scenario in 2HDM is also available (Barr-Zee)

g-2 contribution

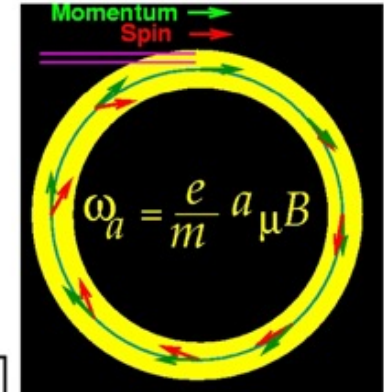


Notation: $y \leftrightarrow \rho$

$$\Delta a_\mu \simeq \frac{m_\mu m_\tau \rho_e^{\mu\tau} \rho_e^{\tau\mu}}{16\pi^2} \left(\frac{\ln \frac{m_H^2}{m_\tau^2} - \frac{3}{2}}{m_H^2} - \frac{\ln \frac{m_A^2}{m_\tau^2} - \frac{3}{2}}{m_A^2} \right)$$

muon g-2 and EDM measurements

In uniform magnetic field, muon spin rotates ahead of momentum due to $g-2 \neq 0$



general form of spin precession vector:

$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} + \frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

BNL E821 approach
 $\gamma=30$ ($P=3$ GeV/c)

$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} + \frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

FNAL E989

J-PARC approach
 $E = 0$ at any γ

$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} + \frac{\eta}{2} \left(\vec{\beta} \times \vec{B} \right) \right]$$

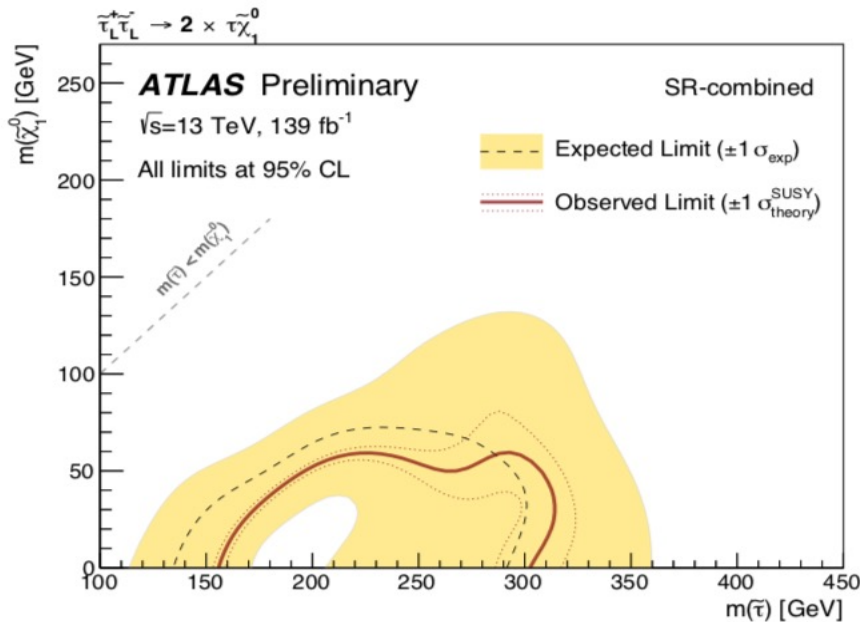
J-PARC E34

Slide by Mibe-san

Slepton search

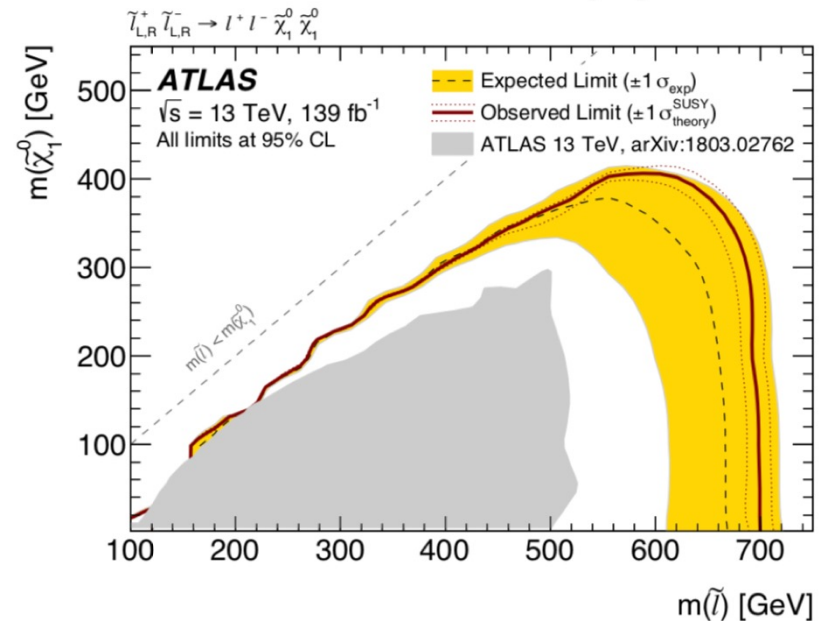
Left-handed slepton has the same quantum number as H^+ has.

stau



150-300 GeV with $BR(H^- \rightarrow \tau\nu)=1$
Is excluded

smuon



All $\tilde{e}_L, \tilde{e}_R, \tilde{\mu}_L$ and $\tilde{\mu}_R$ are combined

We still have room for $m_{H^+} = 120$ GeV

Concern

- SMBG from 4τ ?