

First observation of the H₂ quadrupole in saturation (or any quadrupole at all)

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Why hydrogen?

Why a rovibrational transition?

- Simplest neutral molecule
 - 4 body problem
 - Rovibrational transitions are well calculable
- Excellent test for molecular QED theory^[1]
- Put bounds on a 'fifth' force^[2]
- Extract fundamental constants

$$F(\alpha, R_\infty, r_p, \mu_p)$$

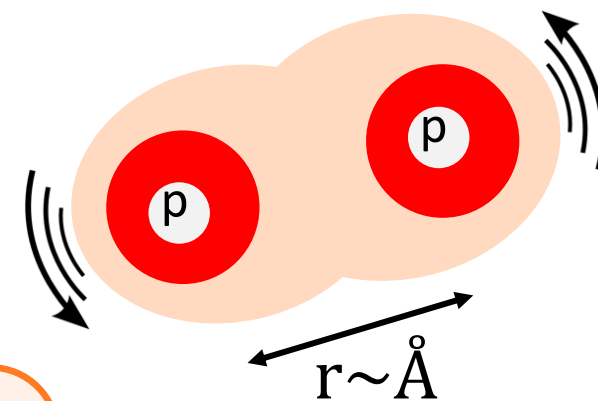
$$\downarrow$$

$$F^{-1}(\alpha, R_\infty, r_p, \nu, \dots)$$

≤ kHz level accuracy required to determine μ_p and compete with other experiments

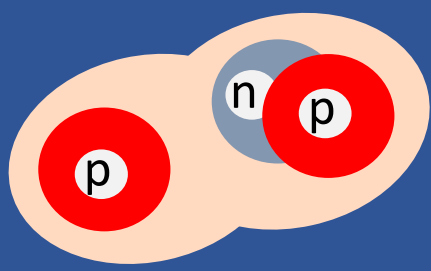
$$\frac{\delta\nu}{\nu} \leq 5 \times 10^{-12}$$

- Lifetimes exceed ...
 - 20 digit accuracy possible

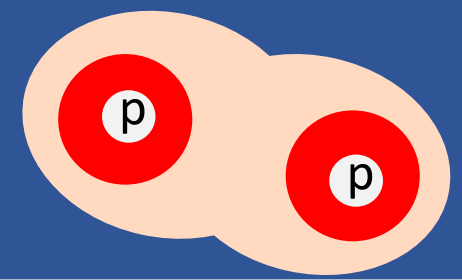


[1] Czachorowski *et al.*, Phys. Rev. A **98**, 052506 (2018)

[2] Salumbides *et al.*, Phys. Rev. D **87**, 112008 (2013)

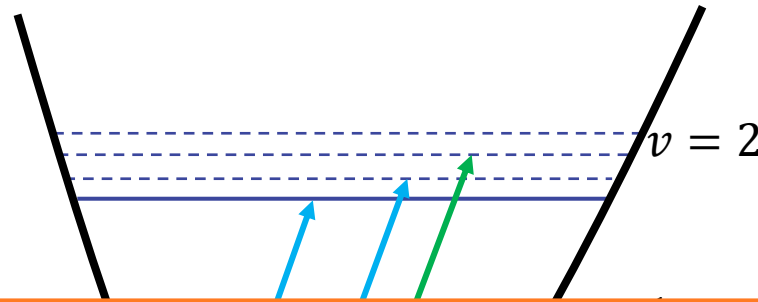


HD vs H₂



Dipole transitions

- $\Delta j = \pm 1$
- Weak dipole
 - First saturation signal in 2017
- Linestrength: $3.5 \times 10^{-25} \text{ cm mol}^{-1}$
- Einstein A-coefficient: $2.1 \times 10^{-7} \text{ s}^{-1}$
- Underlying hyperfine splitting
- Complex signal
 - No easy hyperfine target
 - Limits accuracy to $\sim 50 \text{ kHz}$



100 times weaker in detection
Probably 100 times more difficult to saturate

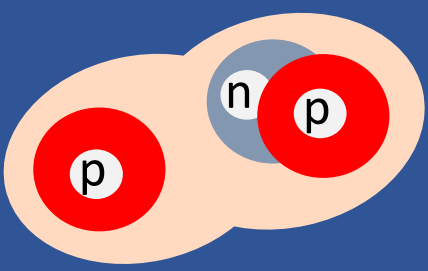
Quadrupole transitions

- $\Delta j = 0, \pm 2$
- Extremely weak
 - Transition moment over 100 times smaller
- Linestrength: $1.6 \times 10^{-27} \text{ cm mol}^{-1}$
- Einstein A-coefficient: 10^{-07} s^{-1}
- No hyperfine splitting (ortho has no hyperfine splitting)
- Q(1) is the most interesting target

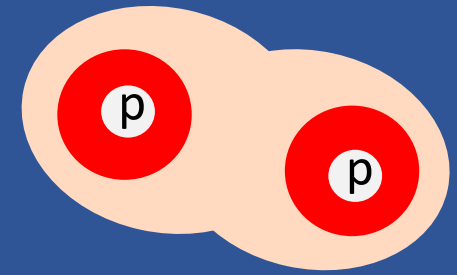
- Best determination at 310 kHz^[1]
 - Q(1) (ortho)

Cozijn *et al.*, Phys. Rev. Lett. **120**, 153002 (2018)
 Diouf *et al.*, Opt. Lett. **44**, 4733-4736 (2019)
 Diouf *et al.*, Phys. Rev. Research **2**, 023209 (2020)
 Cozijn *et. al.*, PRA **105**, 062823 (2022)
 Cozijn *et. al.*, Eur. Phys. J. D **76**, **220** (2022)

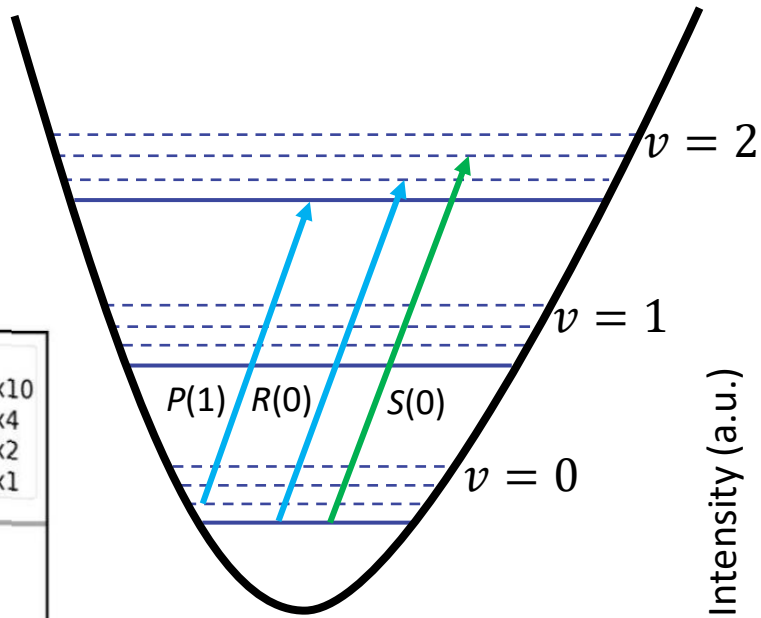
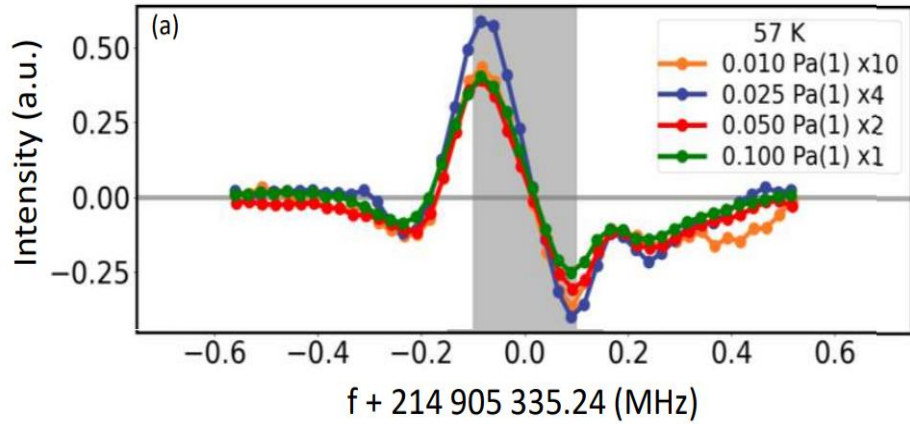
[1] M. Lamperti *et al.*, Nat. Comm. **6**, 67 (2023)



HD vs H2



Previous R(0) result:

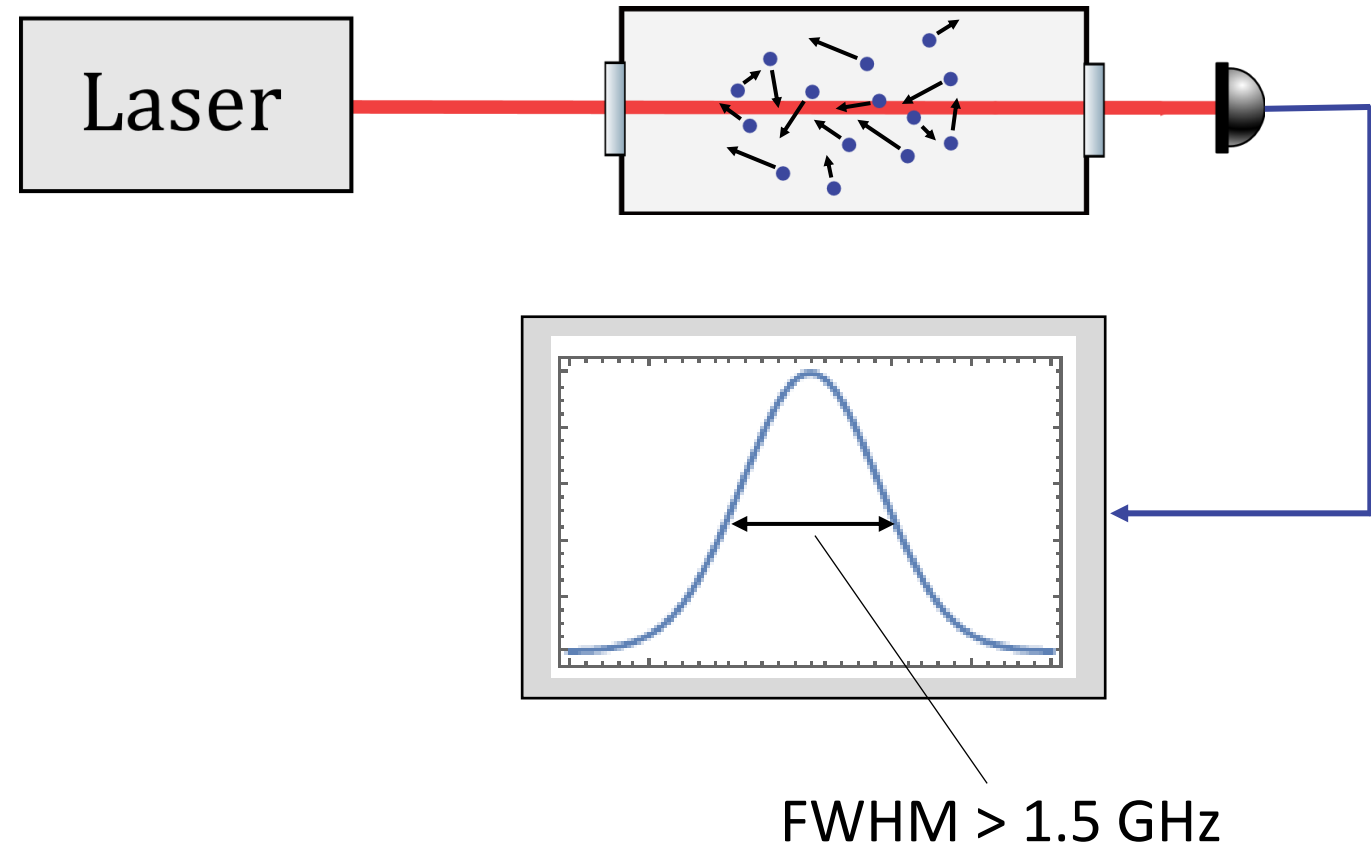


H2 S(0)

?

Rovibrational transitions of hydrogen: Absorption spectroscopy

- Doppler broadened absorption spectroscopy
 - Most recent measurement of S(0) in 1982 at 60 MHz accuracy^[1]
 - Other lines at around 30 MHz accuracy^[2]
- 33 kHz accuracy best result on HD R(1) transition by a Doppler broadened measurement^[3]

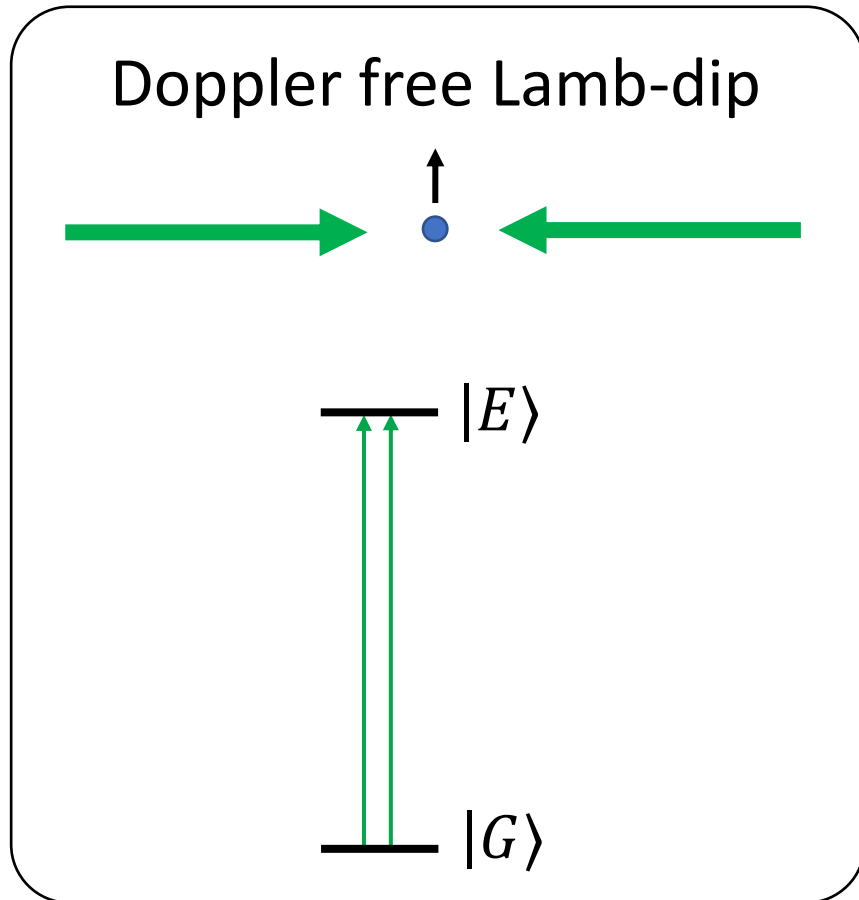


[1] S.L. Bragg, W.H. Smith, J. W. Brault, *Astroph. J.* **263**, 999 (1982)

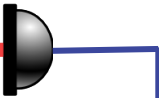
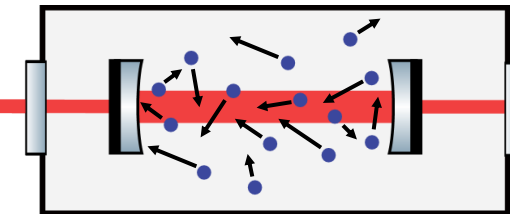
[2] S. Kassi, A. Campargue, *J. Mol. Spectr.* **300**, 55 (2014)

[3] Kassi *et. al.* *Phys. Chem. Chem. Phys.*, **24**, 23164-23172 (2022)

Saturation spectroscopy in H₂

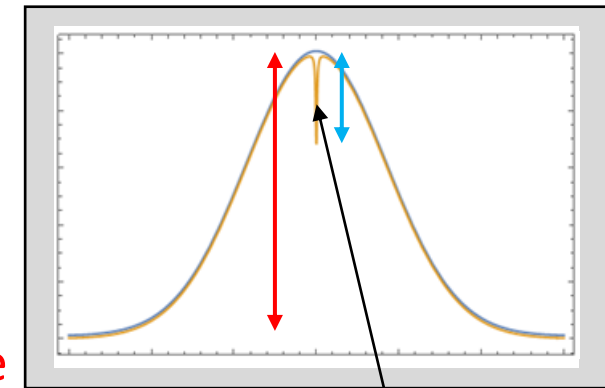


Laser



- Lamb-dip in Doppler broadened profile
- Factor 1000 reduction in linewidth

- Sensitivity to detect the profile
- Power to burn the hole



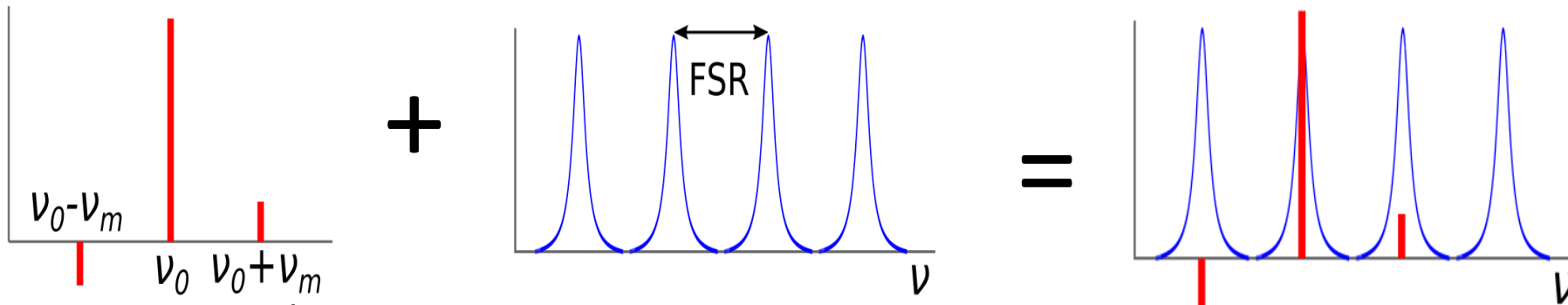
Only ~10 ppm
absorption for HD

NICE-OHMS:

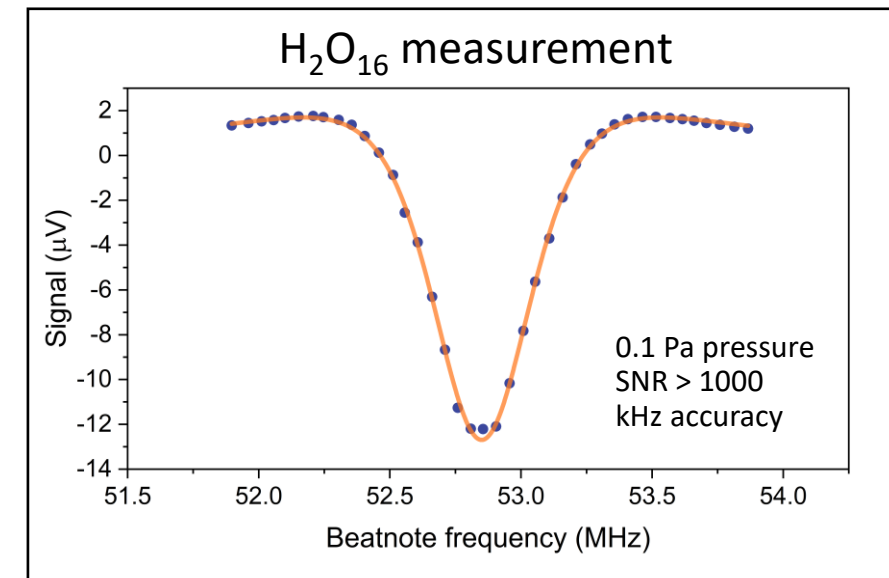
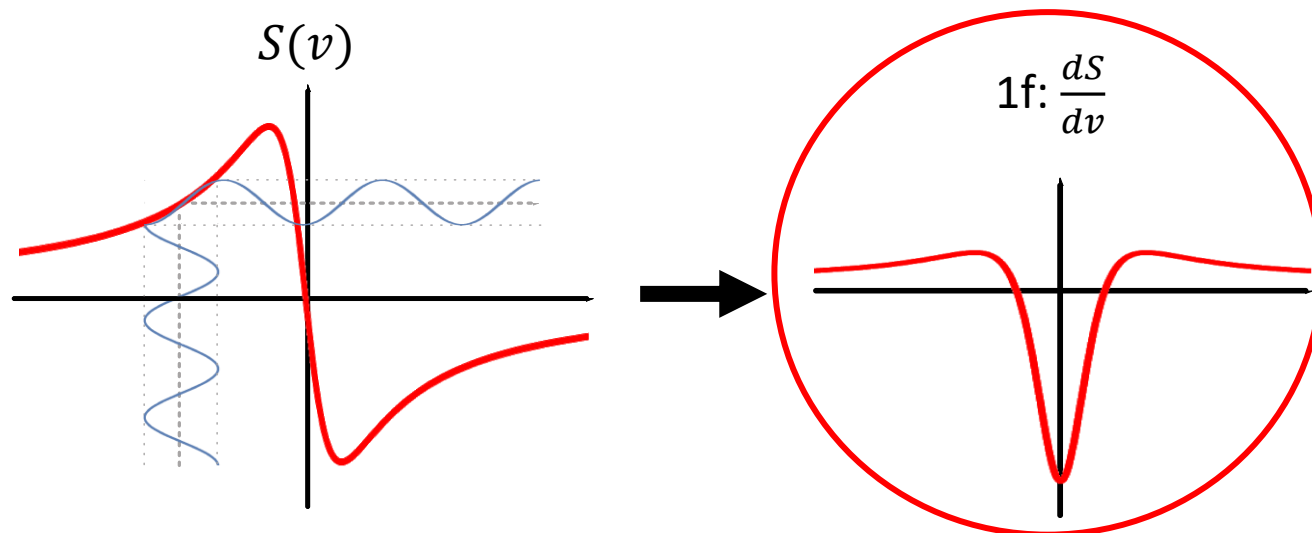
Noise-Immune Cavity-Enhanced Optical Heterodyne Molecular Spectroscopy

Frequency Modulation Spectroscopy in a cavity

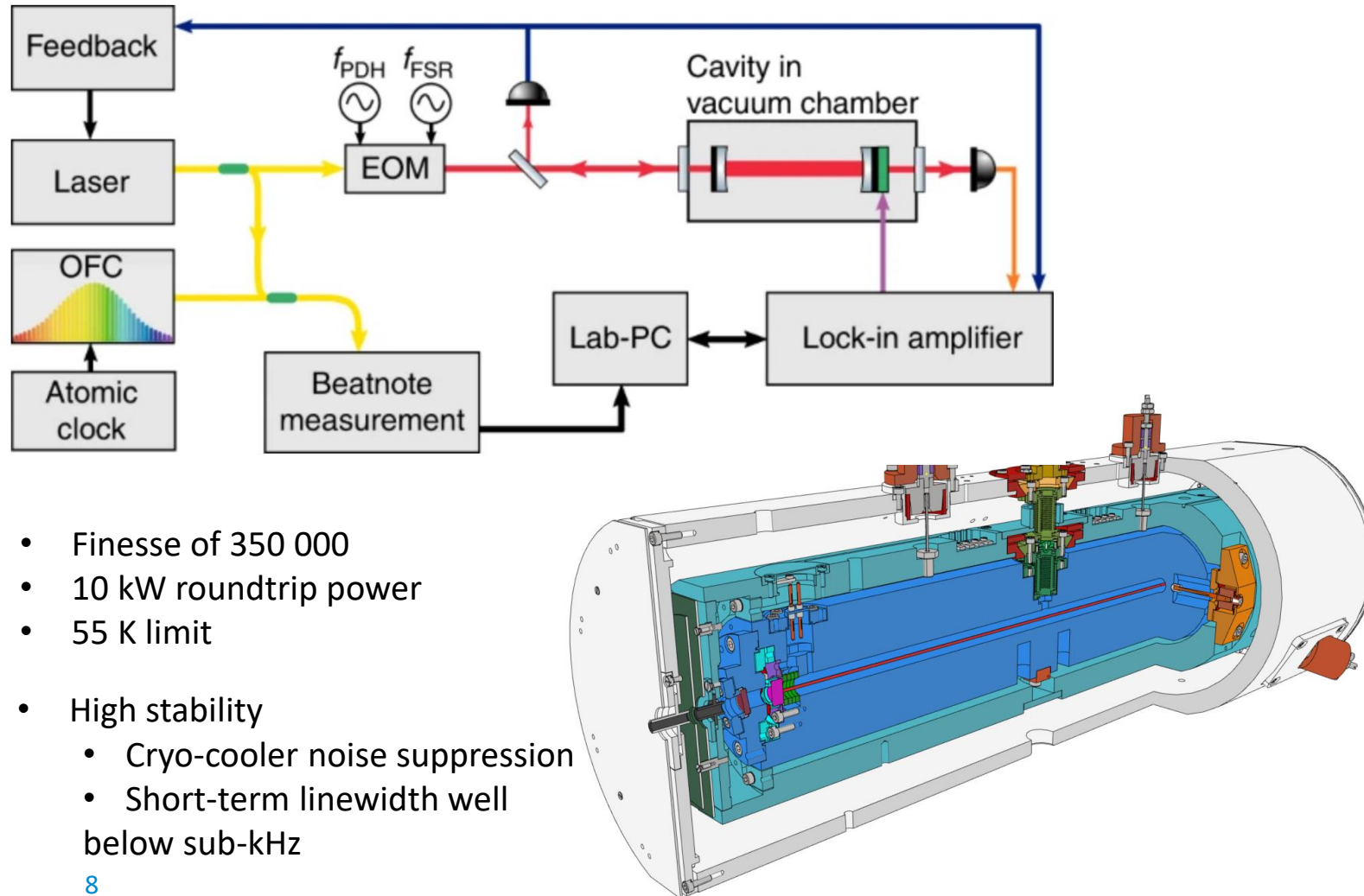
J. Ye, L.S. Ma, and J. Hall, *Opt. Lett.* **21**, 1000 (1996)



- Phase sensitive detection

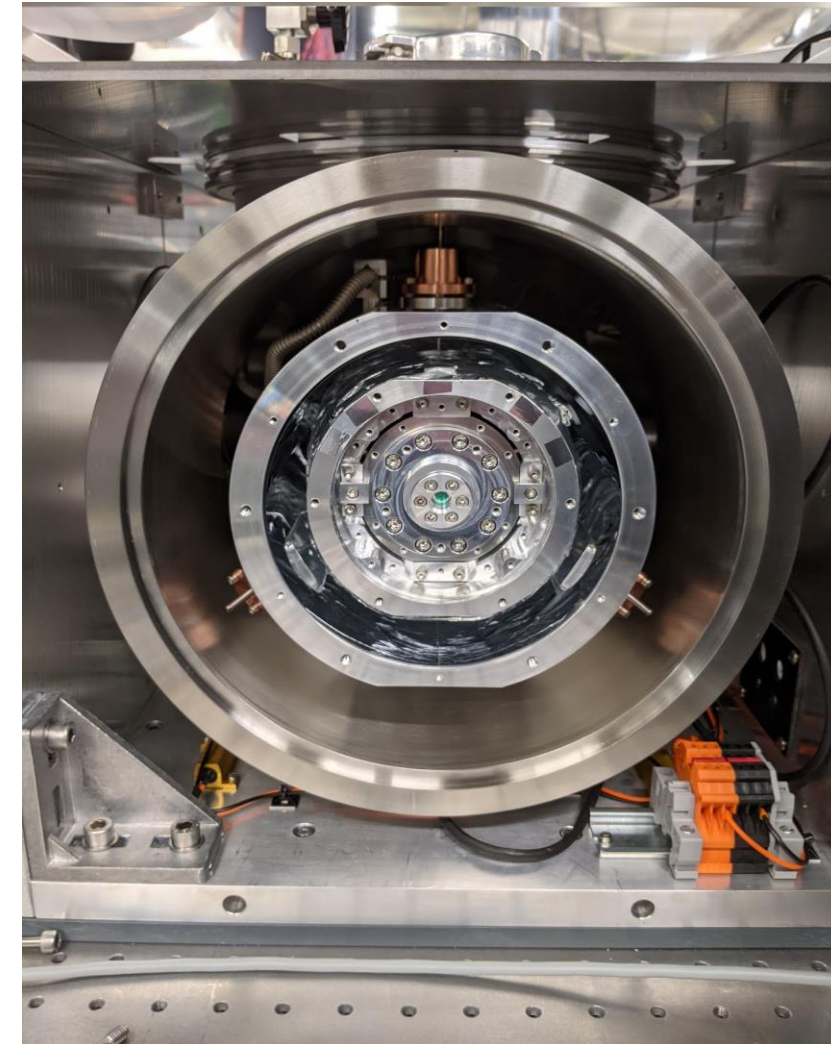


Cryogenic NICE-OHMS setup at VU

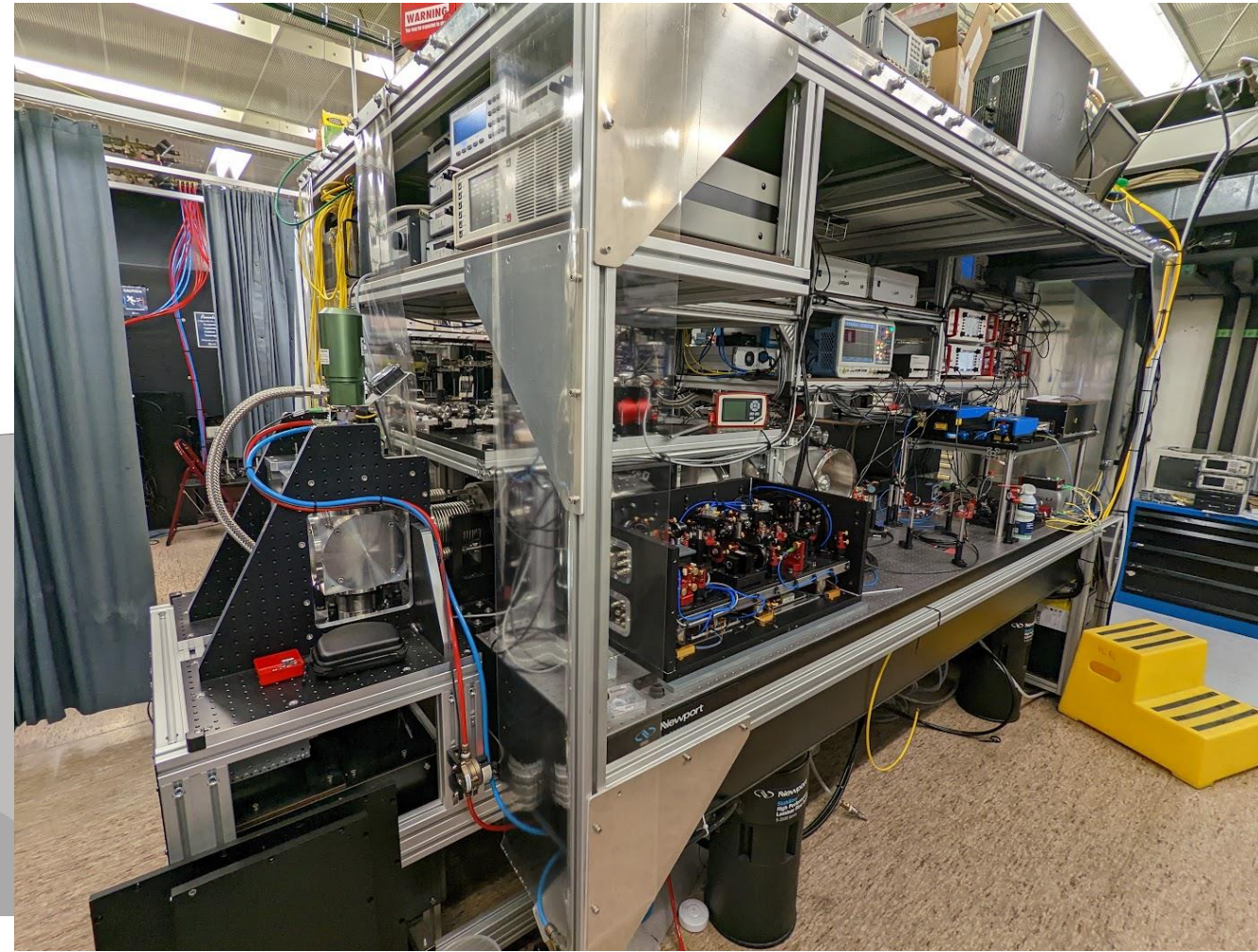
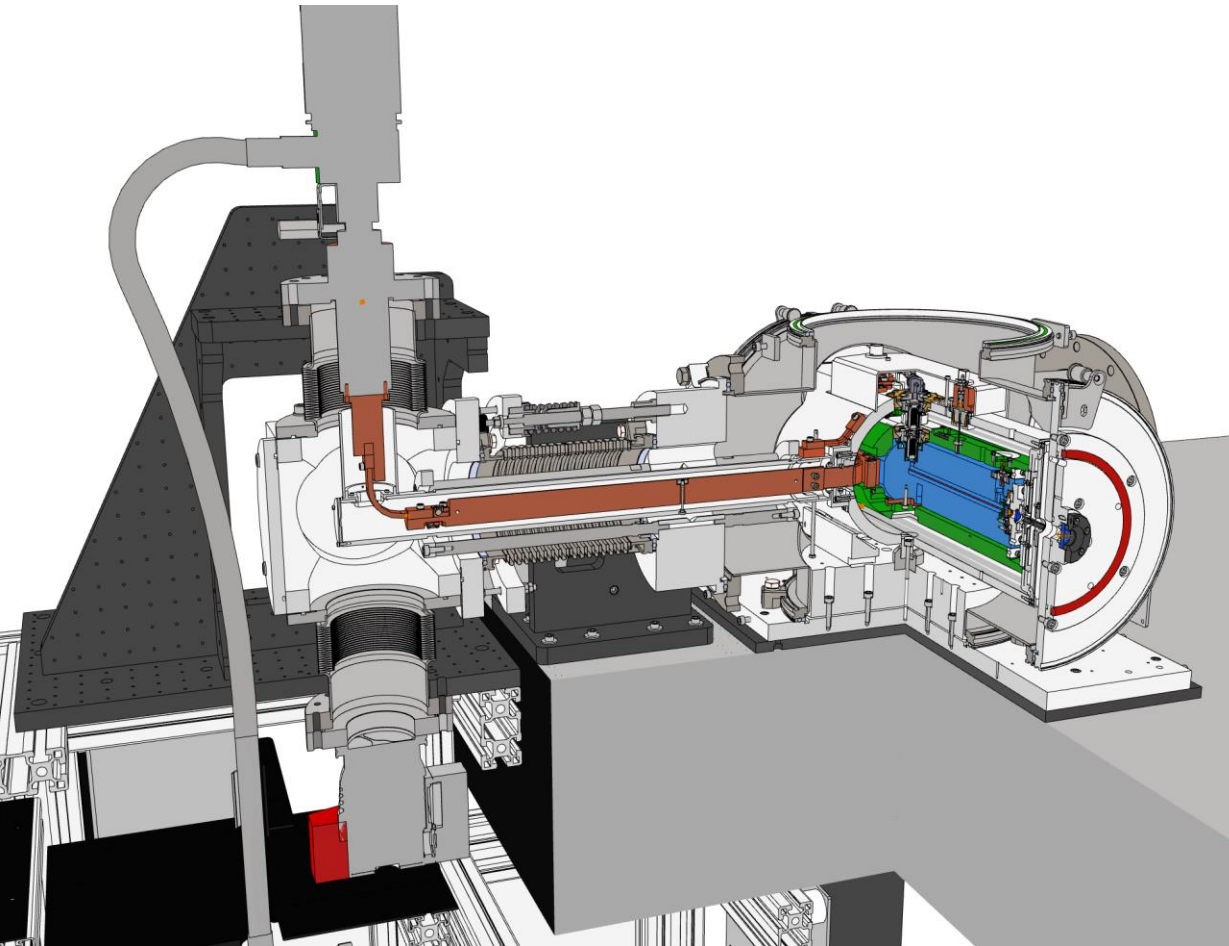


- Finesse of 350 000
- 10 kW roundtrip power
- 55 K limit
- High stability
 - Cryo-cooler noise suppression
 - Short-term linewidth well below sub-kHz

8

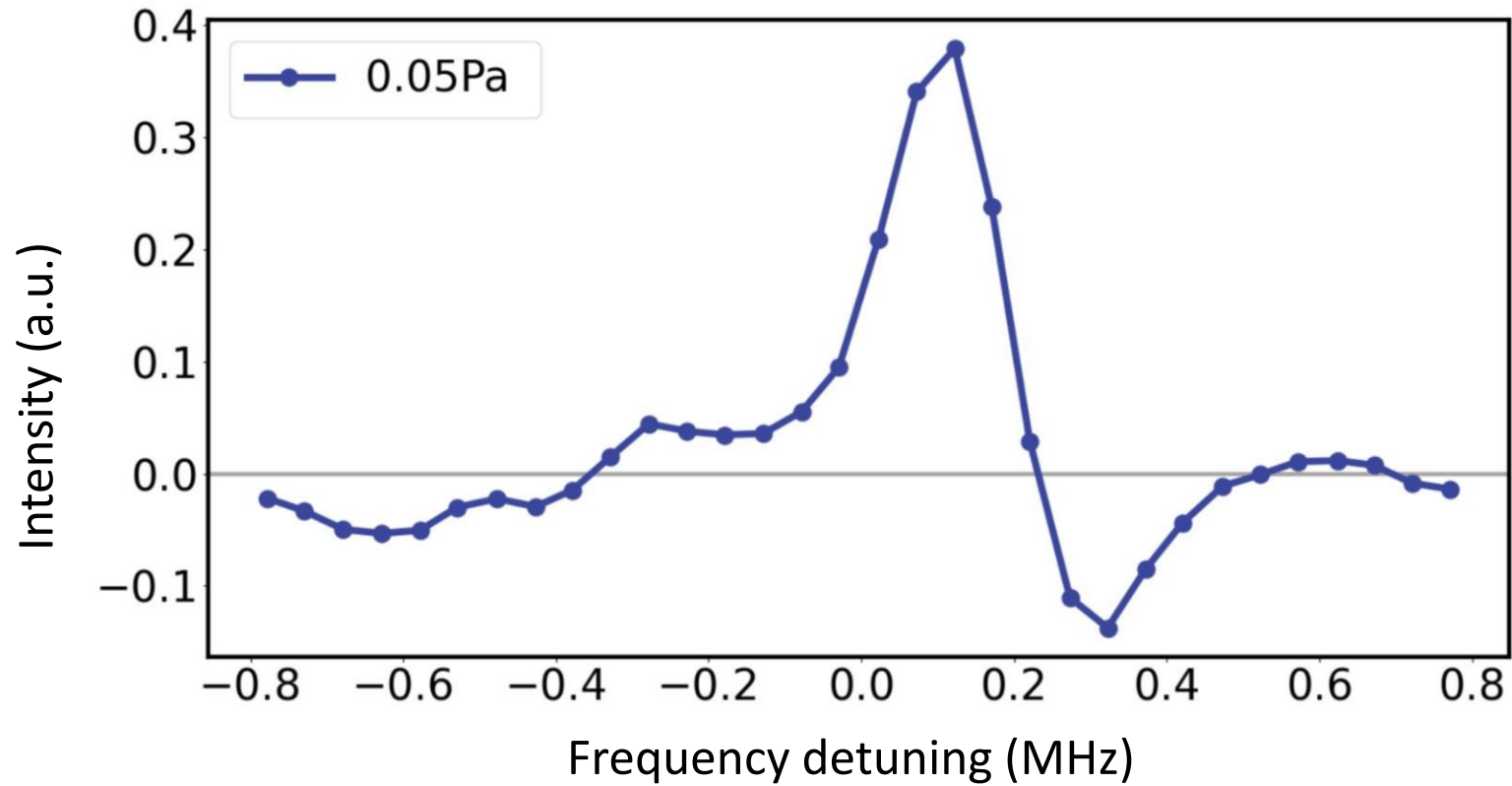


Cryogenic cavity design

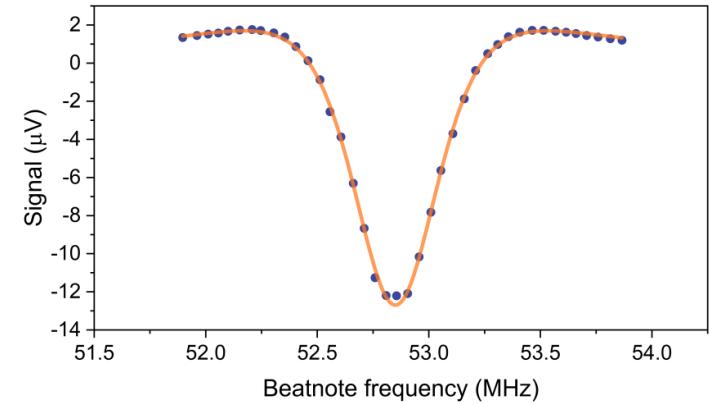


First Results in H2:

$S(0)$ at 8KW



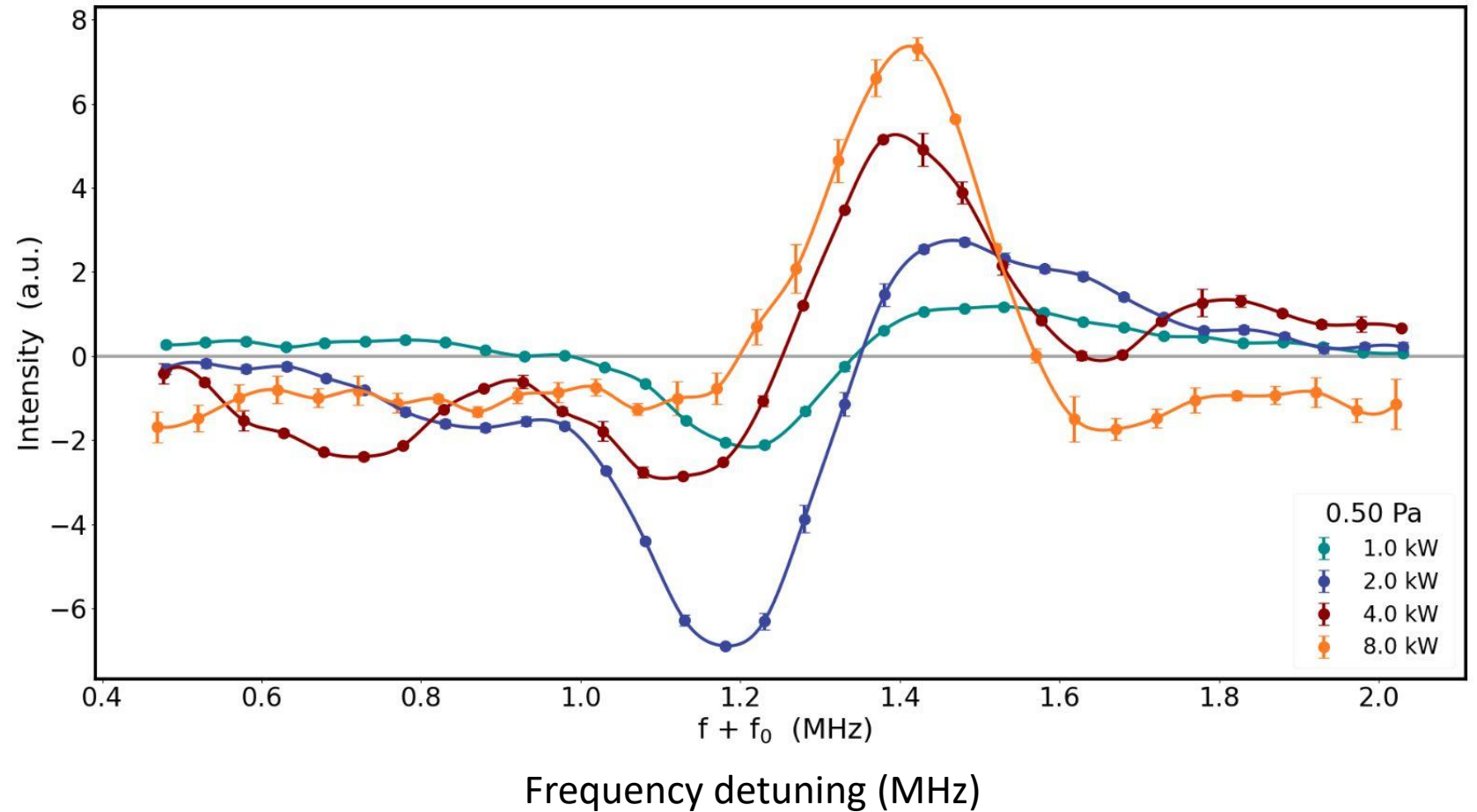
Saturation template



Lineshape puzzling:
Strong dependance with
power and pressure

Results in H2: What if we lower the power?

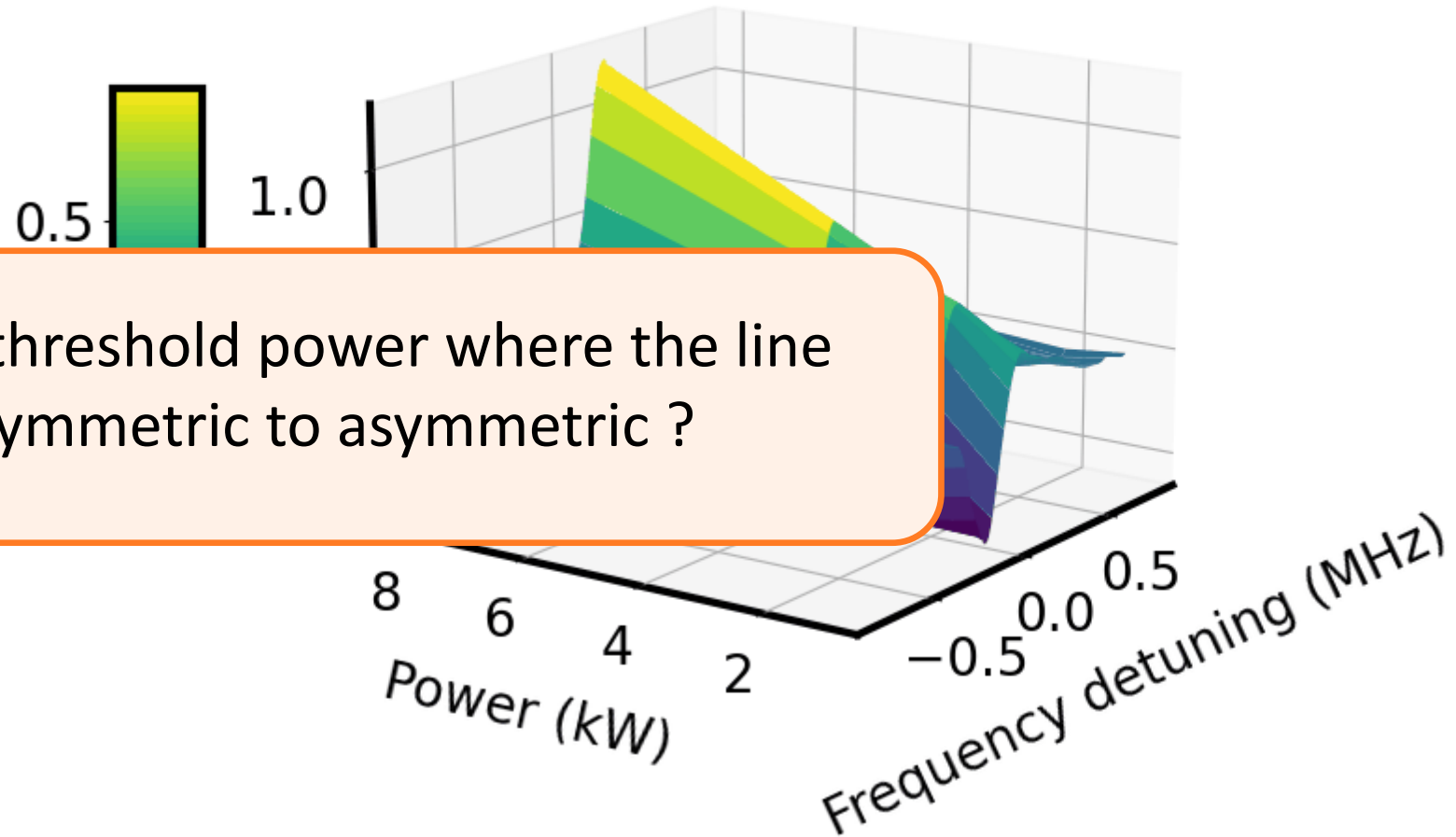
- Varying from 8 kW to 1 kW of power
- Signal transforms from peak to dip!
- Still plenty of signal



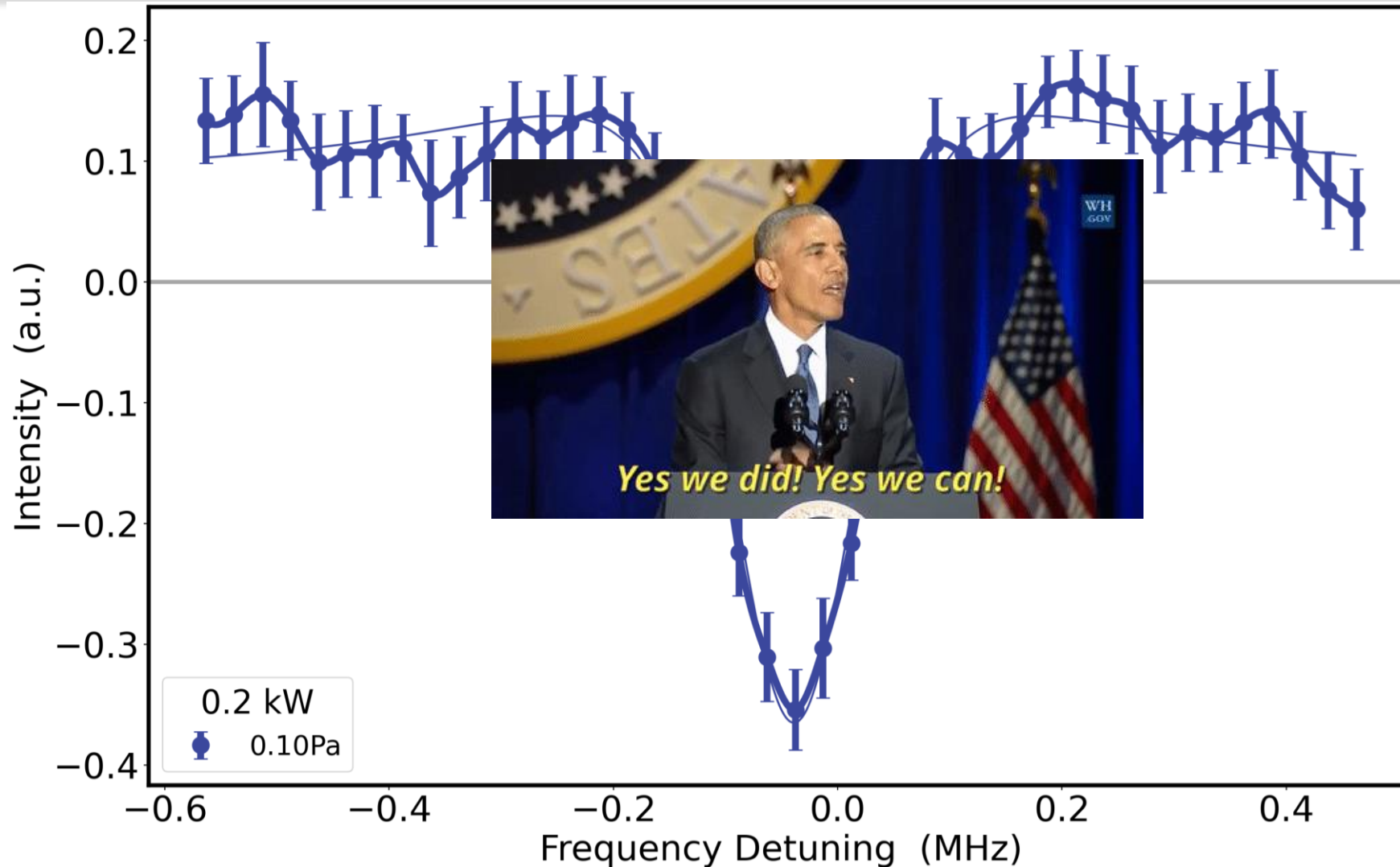
Results in H2: What if we lower the power?

- Do we form a Lamb-dip?
- If so, the trend is clear, we need to lower the power

Can we find the threshold power where the line goes from symmetric to asymmetric?



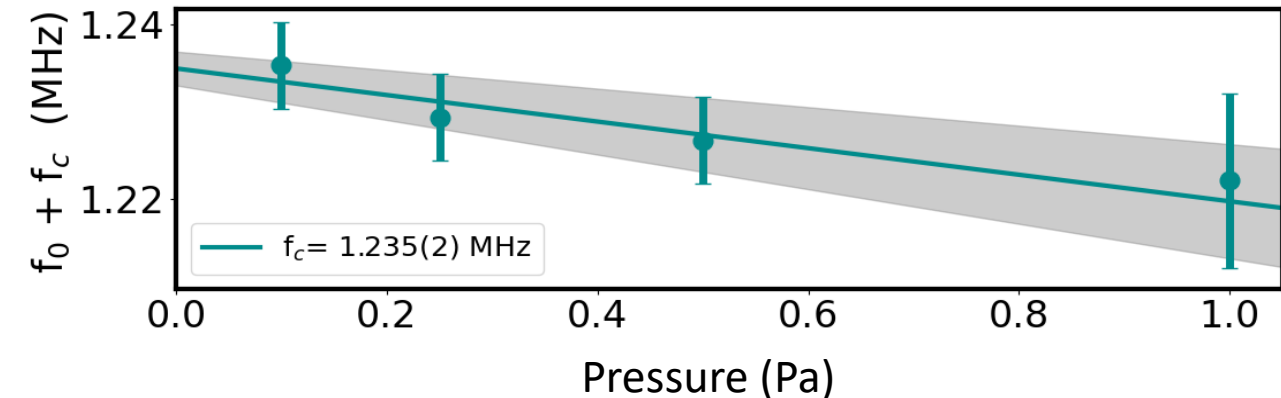
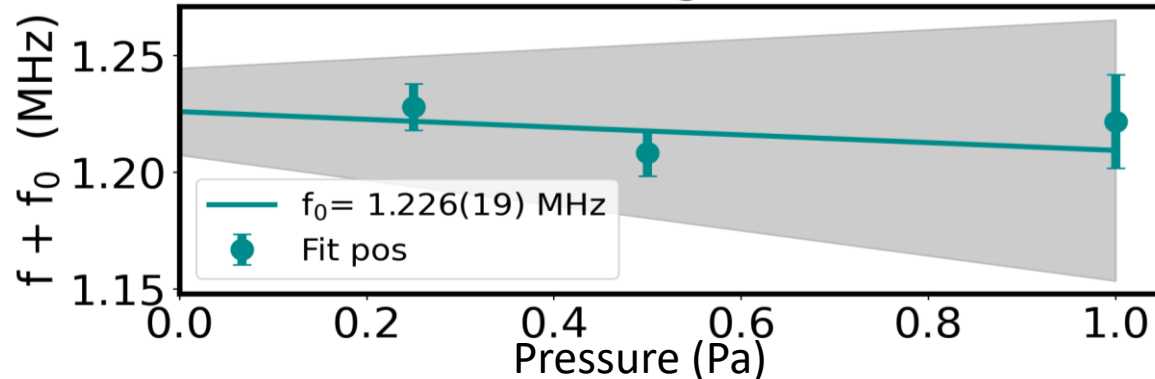
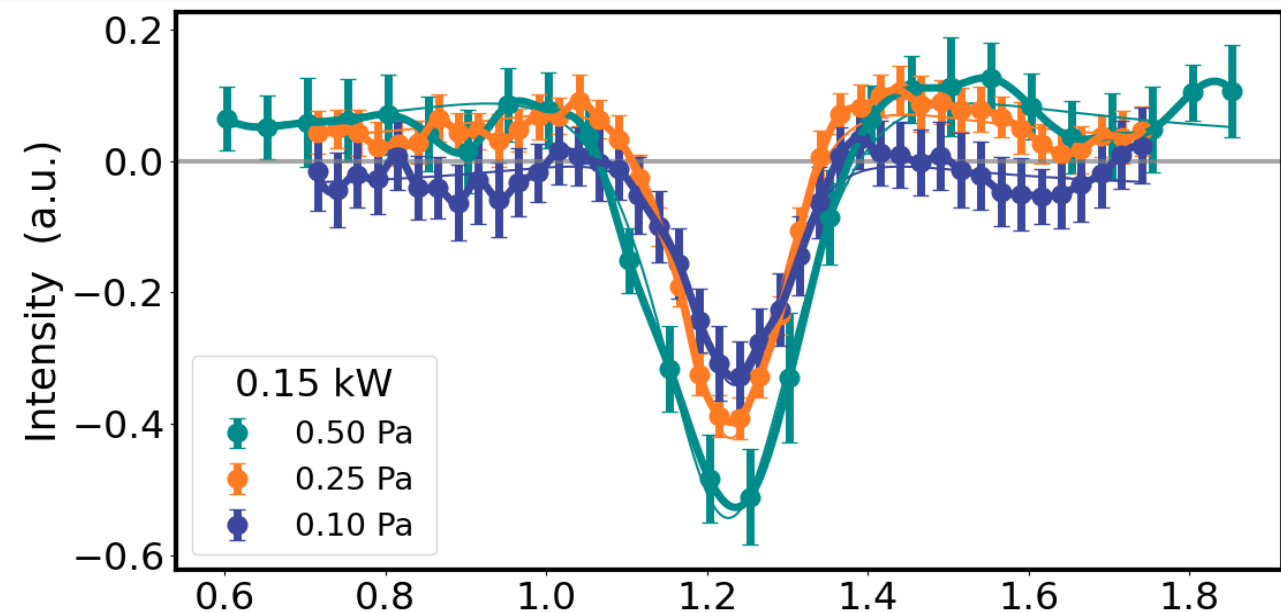
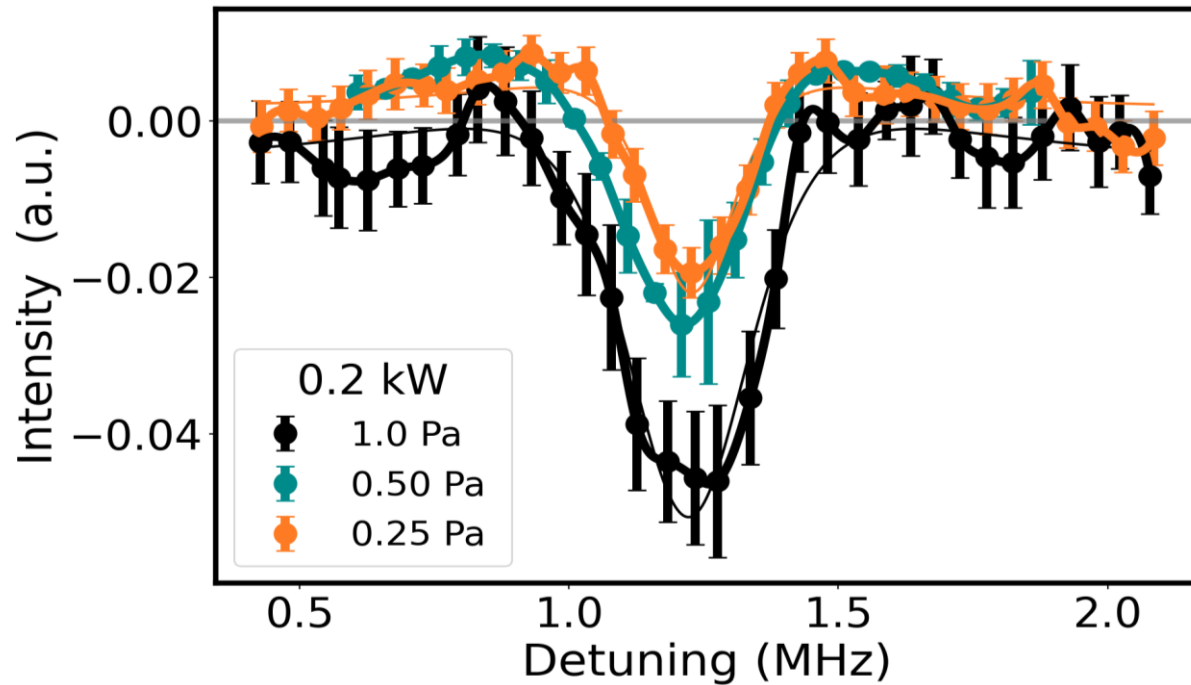
H₂ S(0) Low power



0.1 Pa @ 200 W

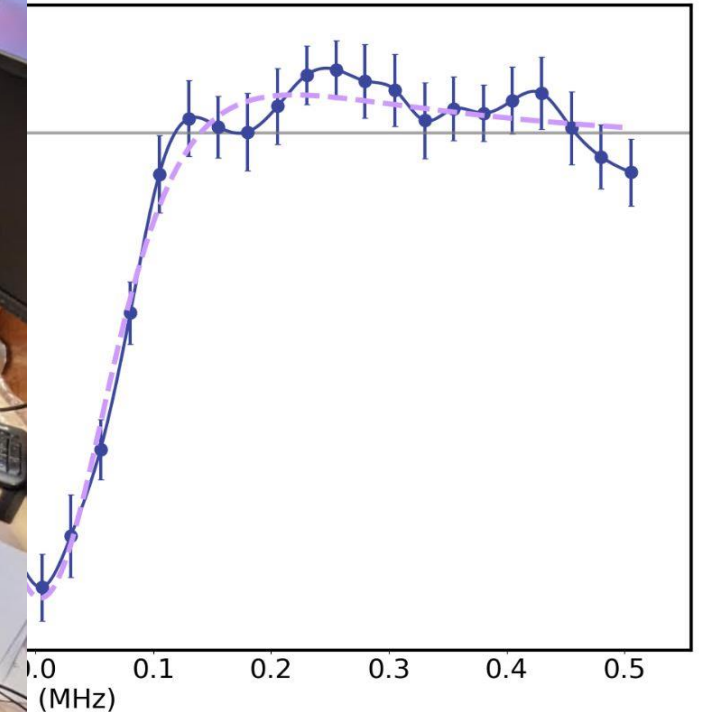
Symmetric lineshape

H₂S(0) position extraction



Results in H₂ : Low power measu

- **<300 W**
- Transformation to perfect
 - Fitting accuracy of a few
- Twice narrower than tra
predicts
 - Optical selection of cold
 - 13 K effective temperatu
- Zero pressure, zero pow
252 016 361 234.4 (7.3)
 - Blue line marker in f



Extracting the absolute transition frequency

$$E_{\text{photon}} = h\nu_0 \pm \cancel{\frac{h\vec{k}\cdot\vec{v}}{2\pi}} \pm \frac{(h\nu_0)^2}{2mc^2} - \frac{(h\nu_0)v^2}{2c^2}$$



Recoil shift:
70 kHz

What about the sign?

Absorption is +

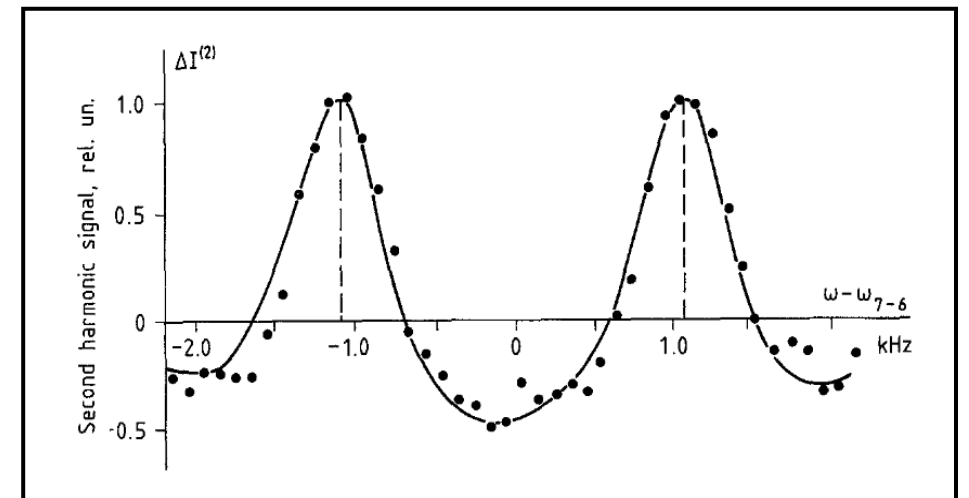
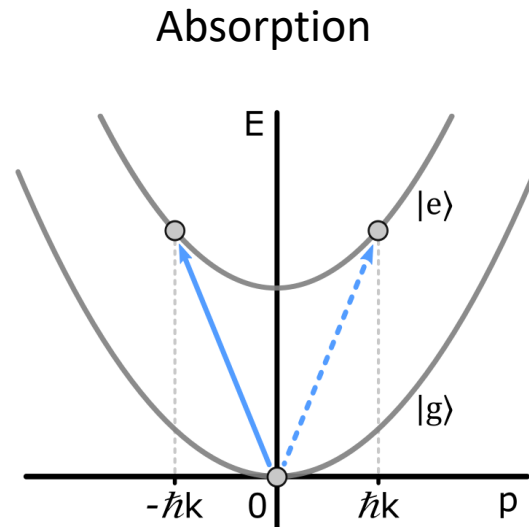
Emission is -



Relativistic Doppler shift:
< 200 Hz

(13 K effective temperature)

Recoil doublet when saturating



Doublet unresolvable in most experiments

- kHz splitting
- 100's kHz profile widths
- No shift applied

Recoil doublet resolved

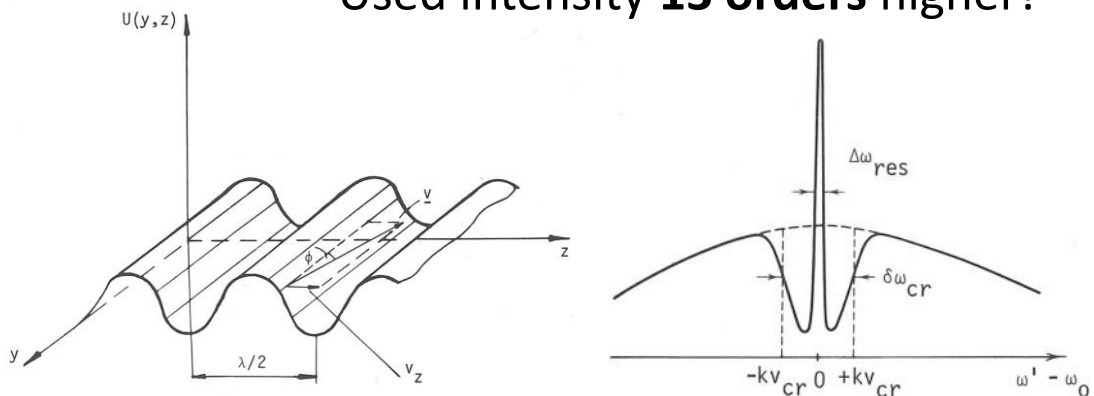
- Only 3 experiments so-far
- All in methane

A.P. Kol'chenko, S.G. Rautian, R.I. Sokolovskii, Zh. Eksp. Teor. Fiz. **55**, 1864-1873 (1968)

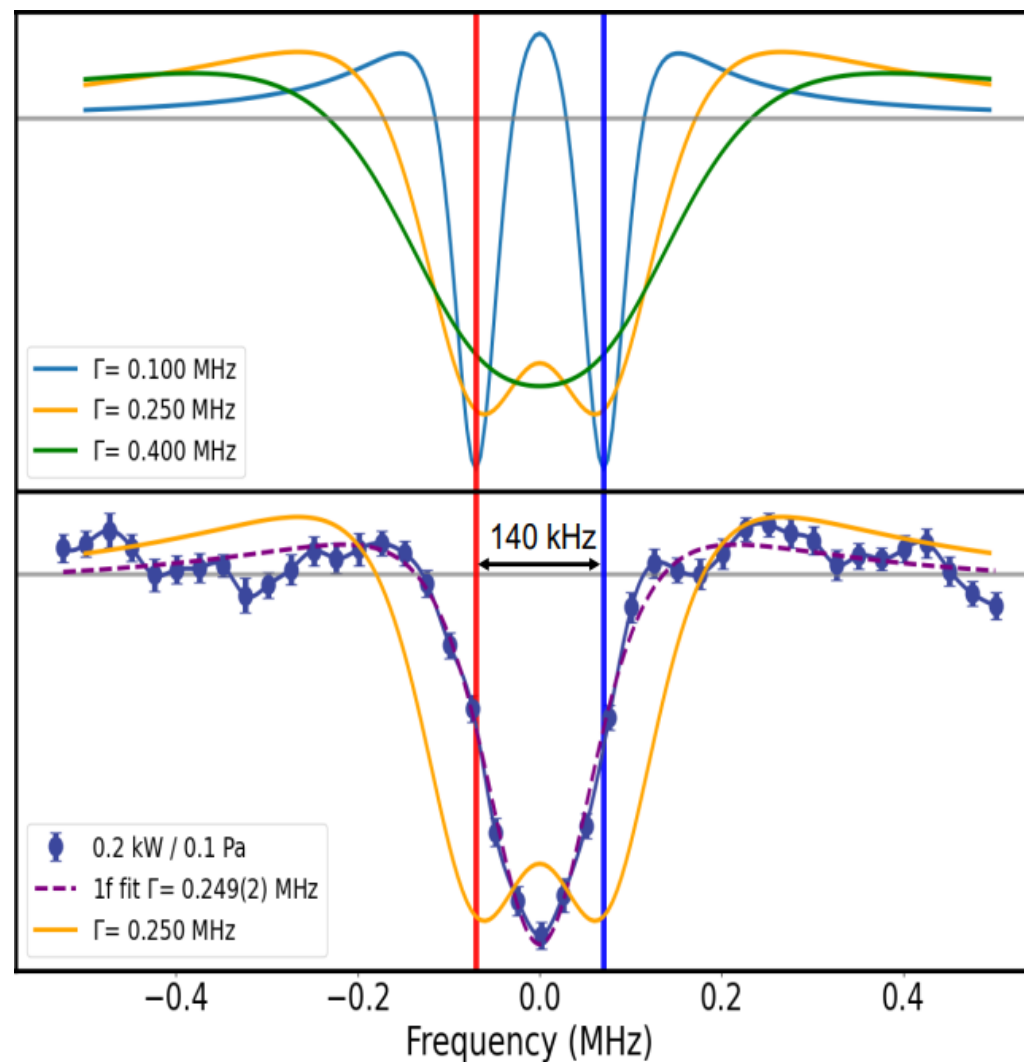
17 S.N. Bagayev, V.P. Chebotayev, A.K. Dmitriyev et. al., Appl. Phys. B **52**, 63-66 (1991)

Recoil in H₂

- H₂ is the lightest molecule
 - Recoil splitting of 140 kHz
 - Linewidth of 250 kHz
- Single Lorentzian fits perfectly
 - Model is significantly broader
 - One recoil component is suppressed
- Mechanisms of suppression
 - Pressure → collisions
 - Power → standing wave forces
 - Used intensity **13 orders** higher!



“Nonlinear Laser Spectroscopy”, V.S. Letokhov, V.P. Chebotayev (1977)



Possible 1D-lattice effects?

- Standing wave gives strong axial field gradient
 - Striction force on locally enhanced polarizability is significant
- Effect leads to altered velocity distribution

Could this effect explain the decoherence of a recoil component?

Could this effect explain our complex lineshapes?

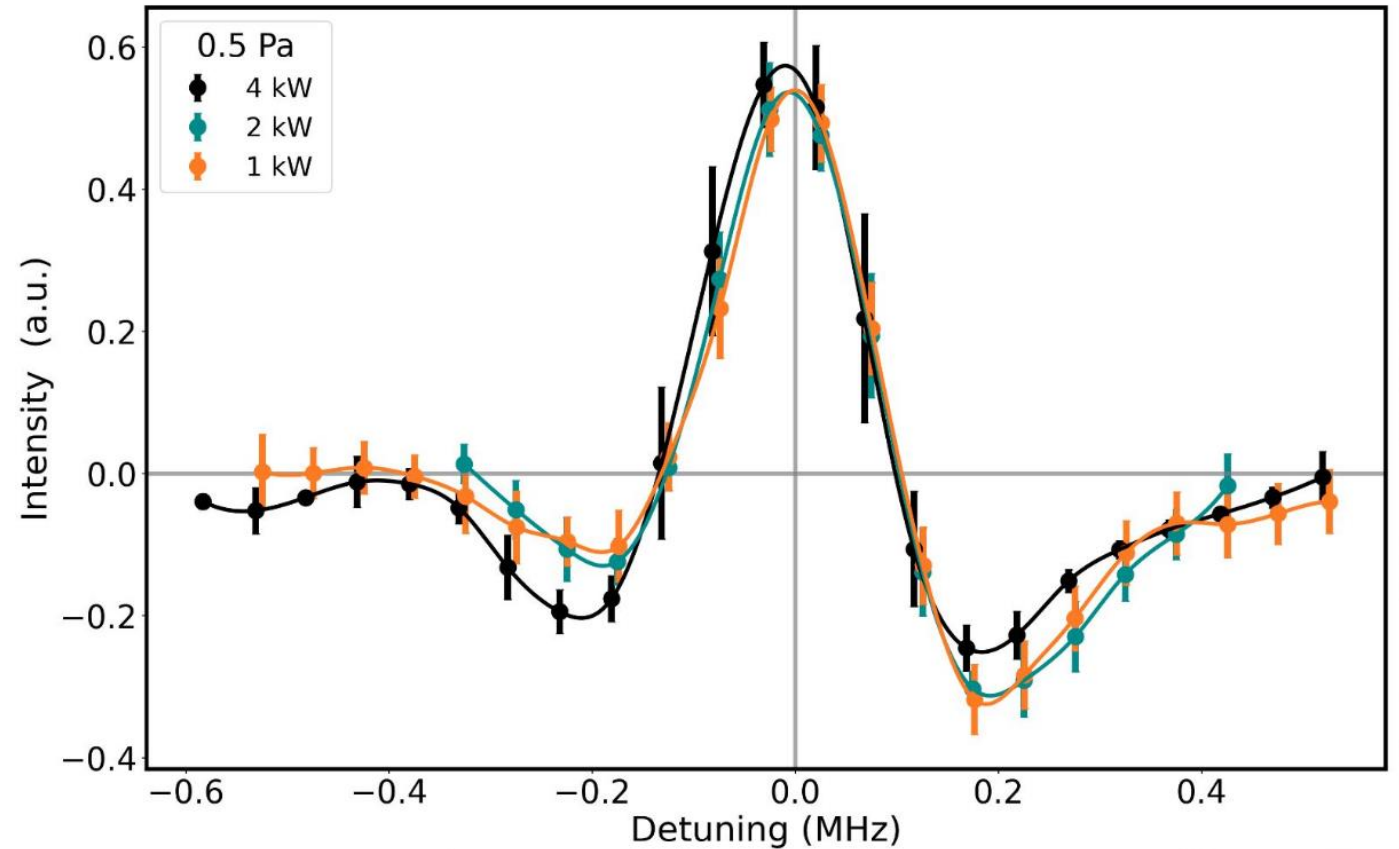
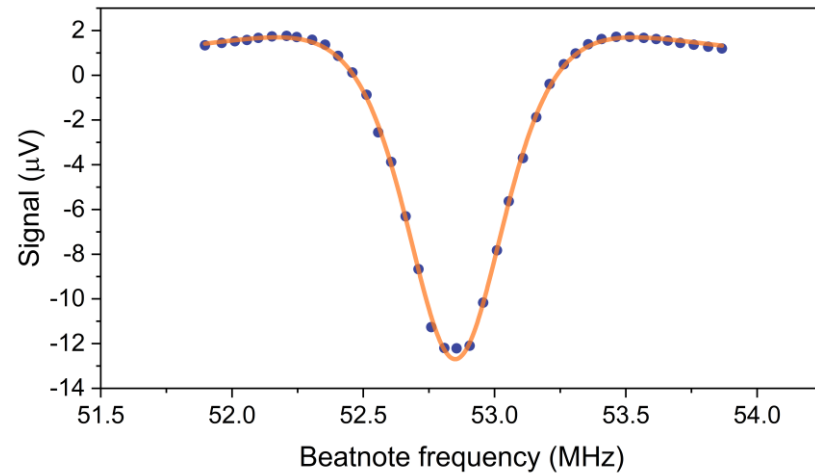
$\frac{\Omega^*}{z} \rho_{eg}$

$(\rho_{eg} + \rho_{ge})$

$b \quad -kv_{cr} \quad 0 \quad +kv_{cr} \quad \omega' - \omega_0$

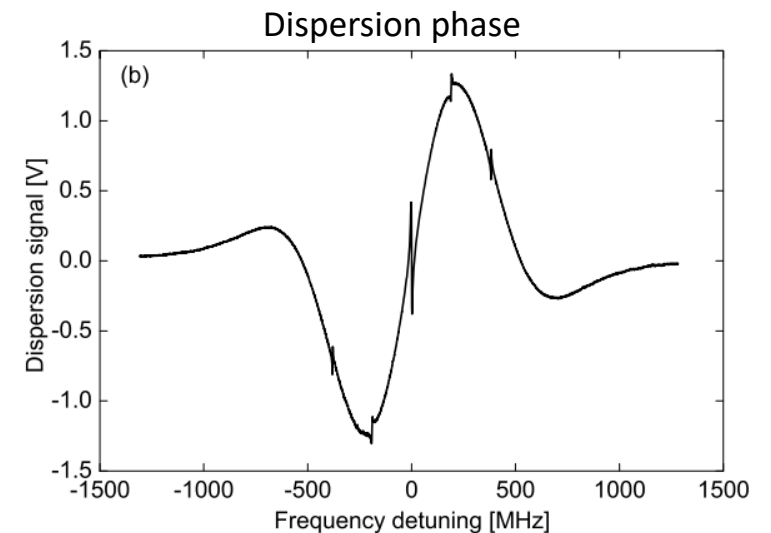
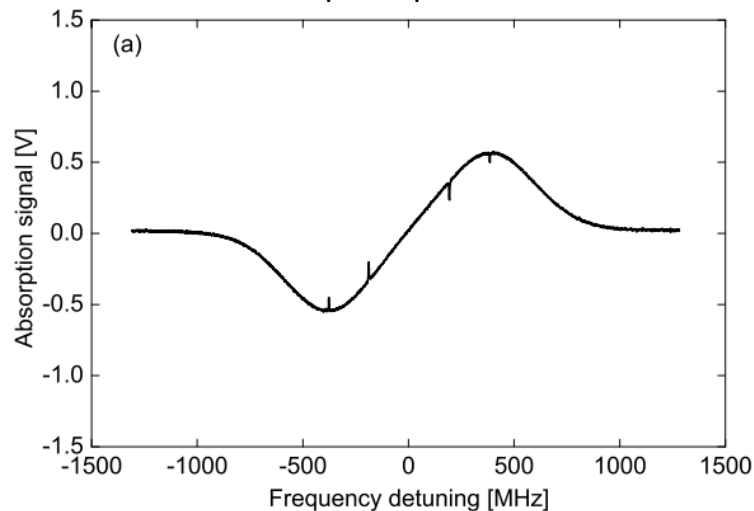
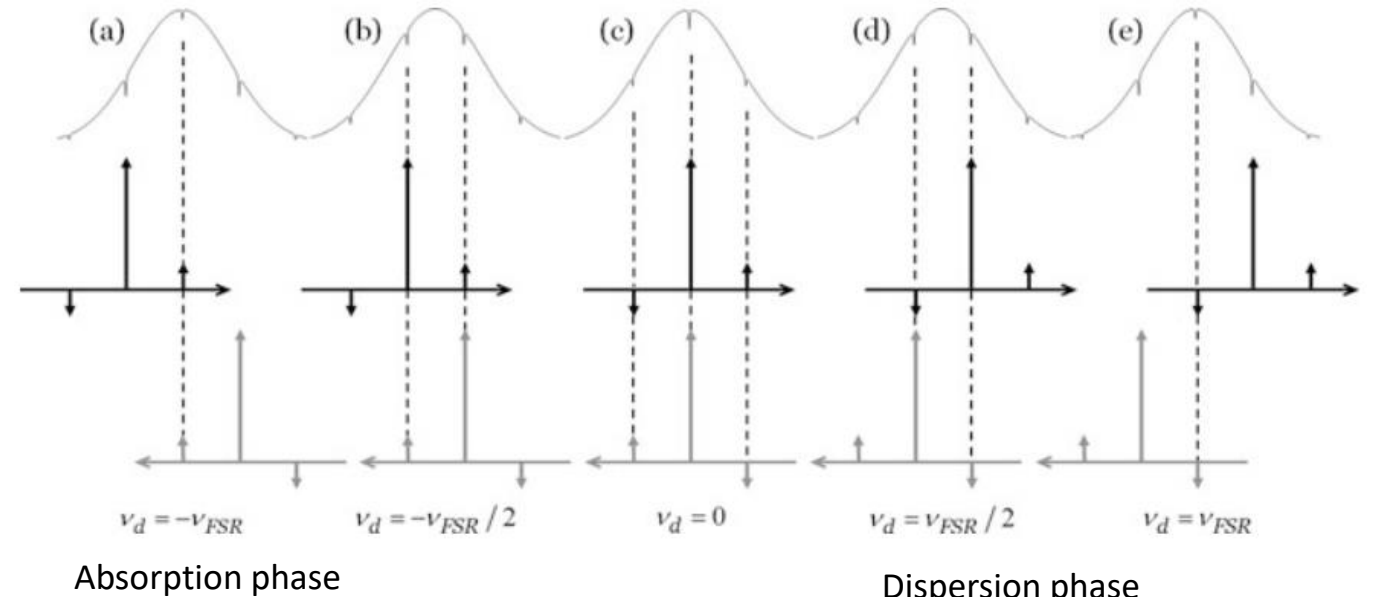
Peaked lineshape in CO₂

- Fully peaked signal for extremely weak CO₂ transition
 - Einstein-A: $1.56\text{E-}07\text{ s}^{-1}$
 - Linestrength of $1.25\text{E-}28\text{ cm mol}^{-1}$
 - R24e at $8247.420872\text{ cm}^{-1}$



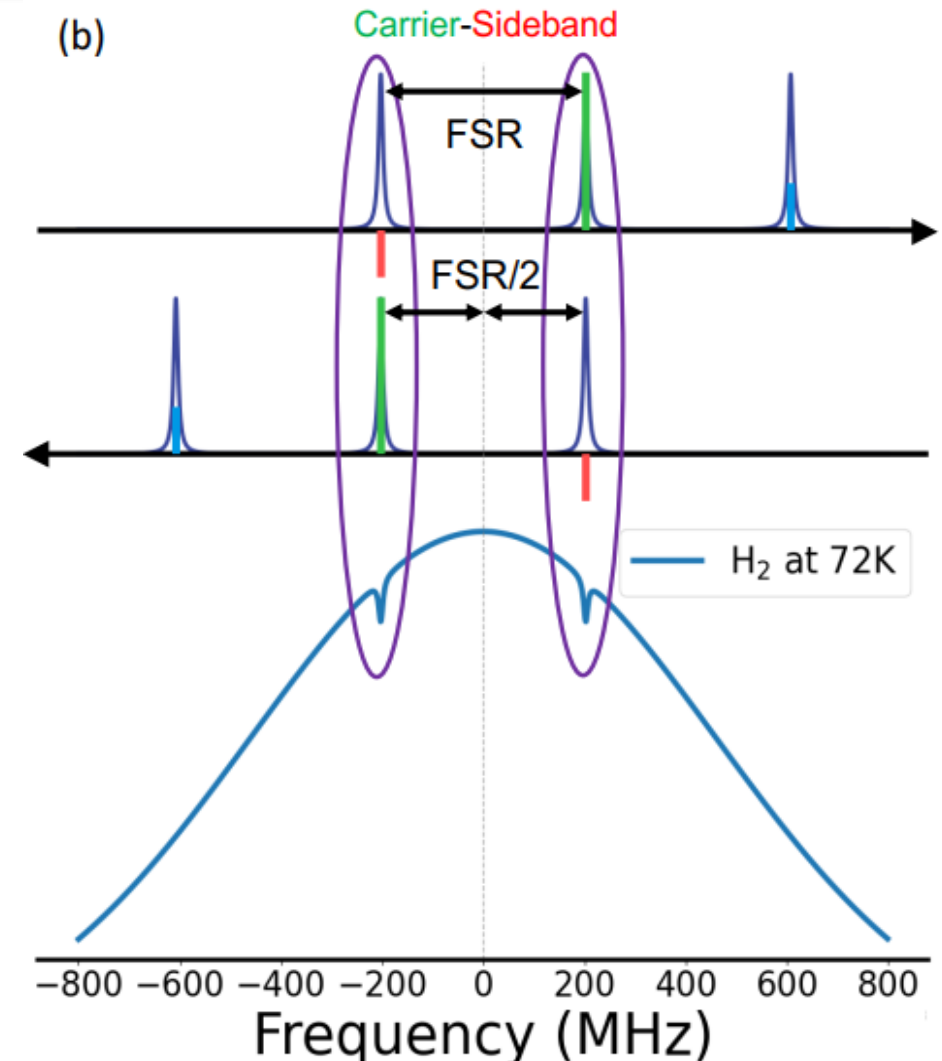
INTERMEZZO: Sub-Doppler signals in NICE-OHMS

- 3 distinctive saturation schemes
 - 5 signal positions
- Central position: Carrier-Carrier
- FSR/2 detuning: Carrier-Sideband
- FSR detuning: Sideband-Sideband



Carrier-Sideband saturation: (pump probe) Doppler-detuned saturation spectroscopy

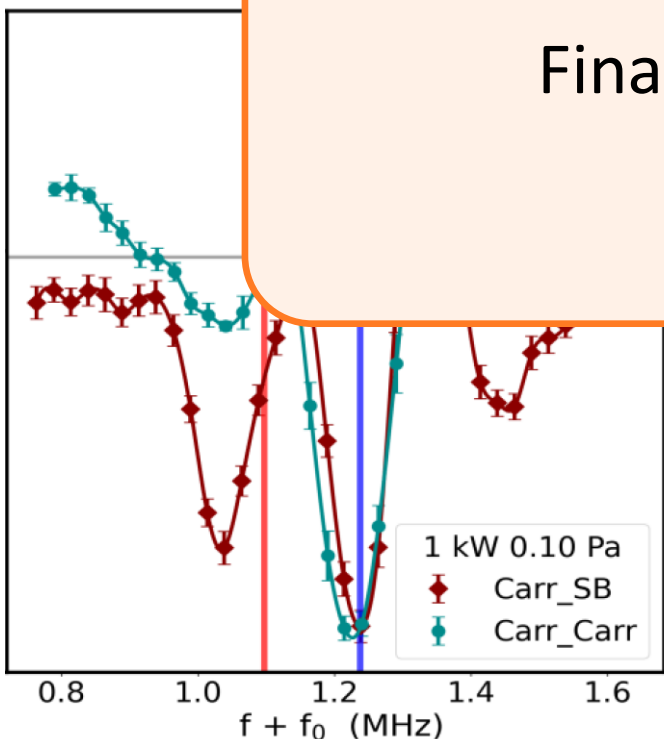
- Detuned by $\pm FSR/2$
 - Doppler shift cancels detuning
- Molecules fly along the beam
 - Part of velocity is projected radially
 - Reduced radial speed
 - Reduced 2nd order Doppler
 - Increased transit time
- On-resonance traveling wave
- Off-resonance standing wave



Doppler-detuned saturation spectroscopy (pump probe)

Results on H₂

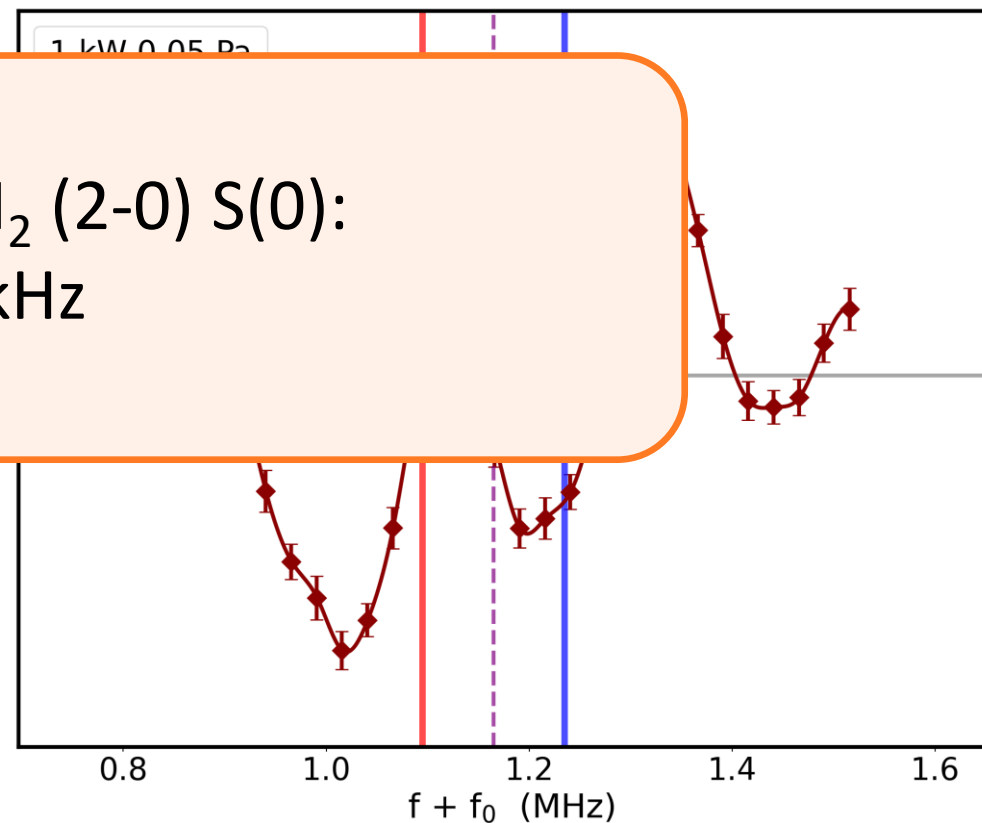
- Saturating molecules flying along the beam
- Doppler shift equal to detuning
- On-resonance standing wave → travelling wave
- S:



Final transition frequency of H₂ (2-0) S(0):
252 016 361 164 (8) kHz

Recoil doublet recovered

- Asymmetric lineshapes
- Red recoil is suppressed
- Recoil shift must be applied



Conclusion of H₂

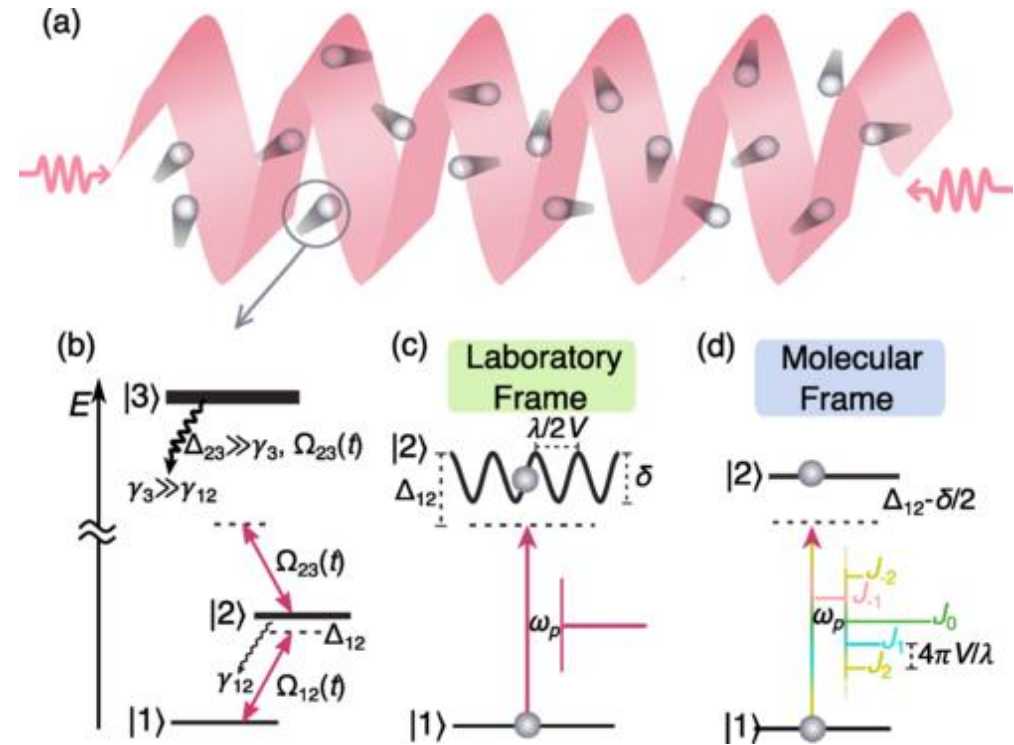
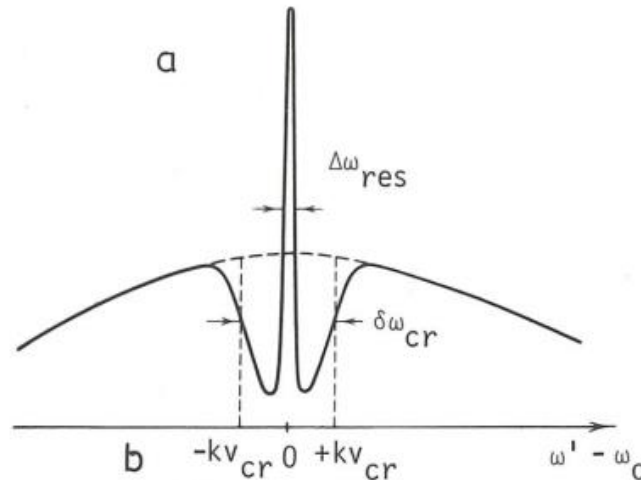
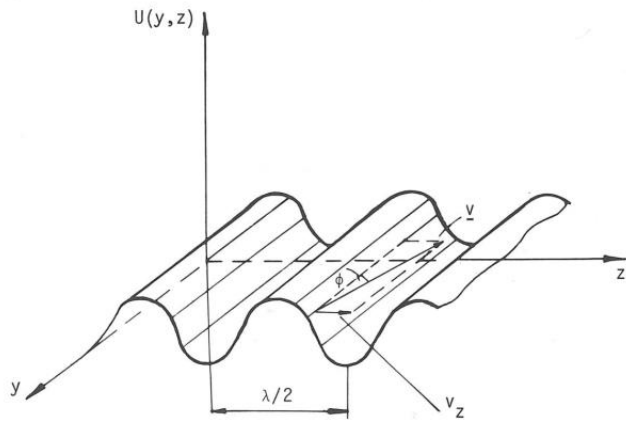
- Molecular quadrupole transition saturated for the first time
 - New-era in rovibrational saturation spectroscopy
- H₂ transition frequency of 252 016 361 164 (8) kHz ⁱ
 - 3×10^{-11} relative accuracy
 - Most accurate determination of any vibrational splitting within all isotopes of molecular hydrogen
 - Recent Doppler Broadened measurement is -65(60)kHz off ⁱⁱ
 - Theory is 2.6 MHz (1.6 σ) off (E⁽⁵⁾)
 - 1.6 MHz uncertainty
- Recoil splitting observed
 - 2nd molecule ever
 - Absence of red recoil under certain conditions

ⁱ <http://arxiv.org/abs/2303.17818>

ⁱⁱ H. Fleurbaey *et al*, PCCP accepted

Outlook

- HT (radioactive) measurements
- Last targets before the end
 - H₂ Q(1)
 - Understanding lineshapes finally ?
 - Transitions below 10^{-4} s^{-1}
 - Standing wave effects



Y.N. Lv *et. al.*, Phys. Rev. Lett. **129**, 163201 (2022)

Acknowledgements & questions



NICE-OHMS team:
Meissa Diouf
Frank Cozijn
Wim Ubachs

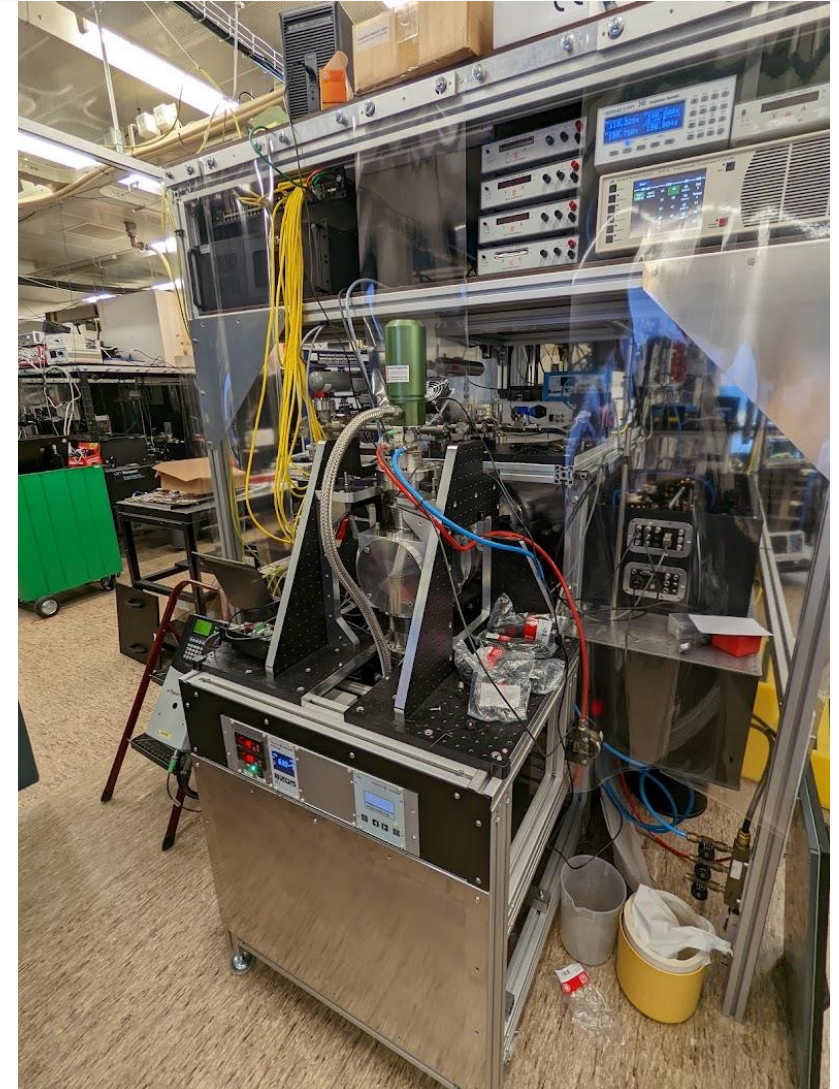
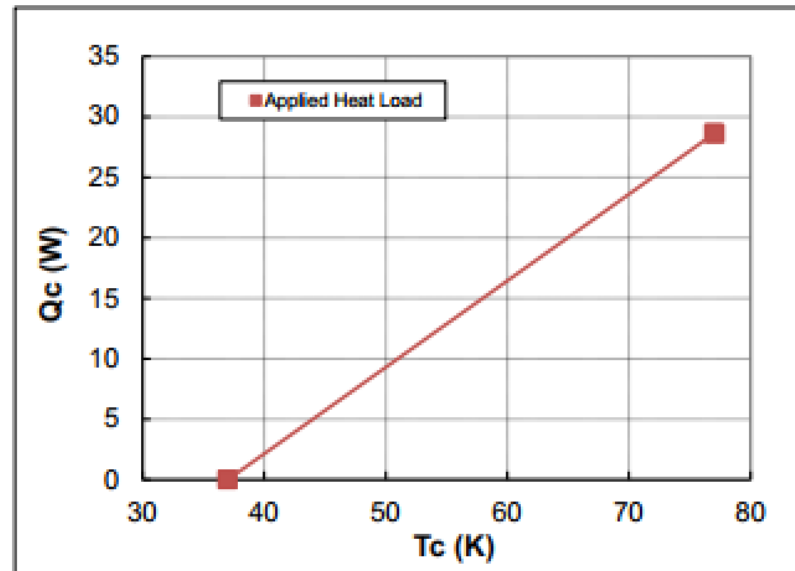


Cryo-cooler

- Thermo acoustic cryo-cooler
 - 60 Hz oscillation with low noise
- Vibration damping works excellent
 - 60 Hz vibration invisible in noise analysis

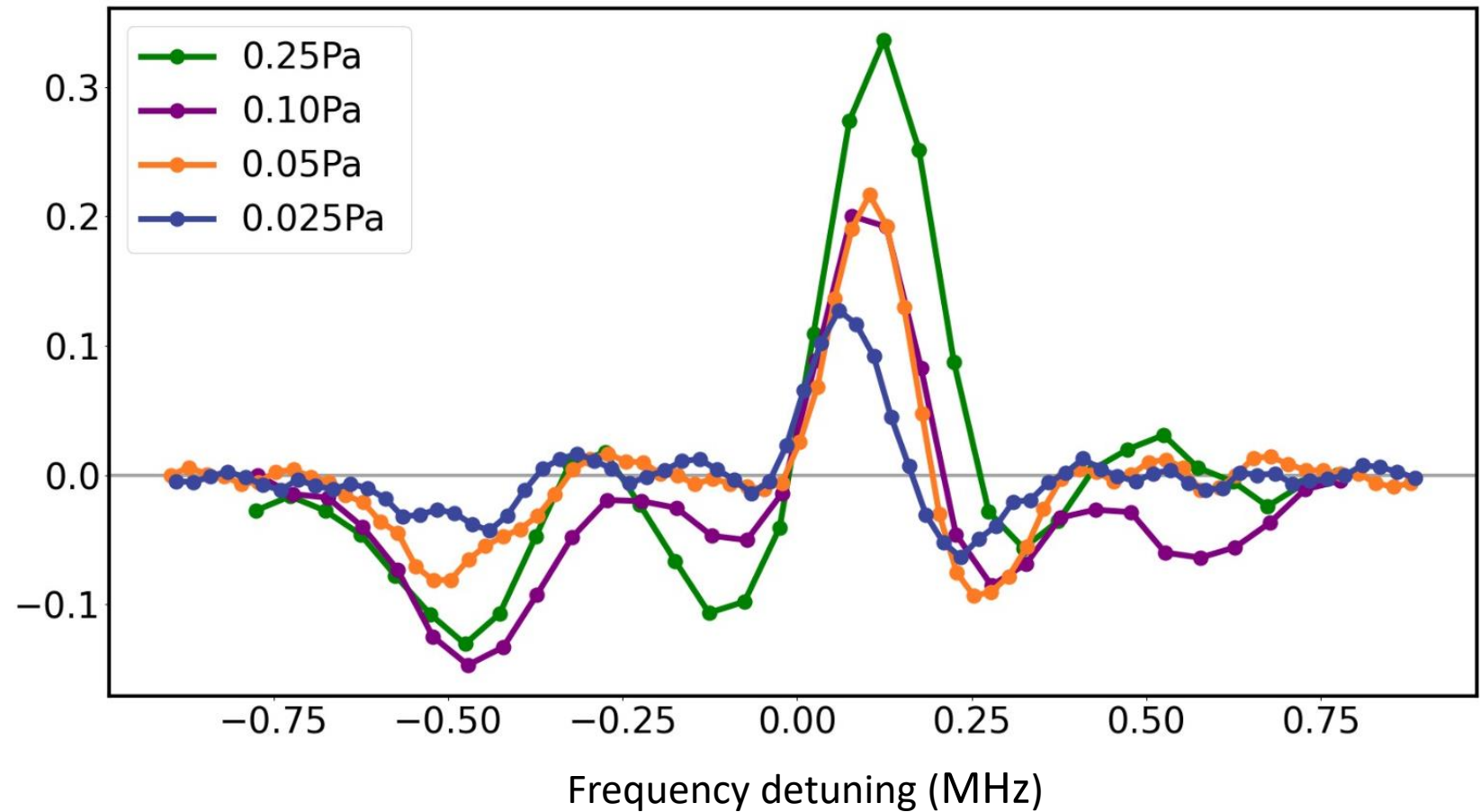


LOAD CURVE:

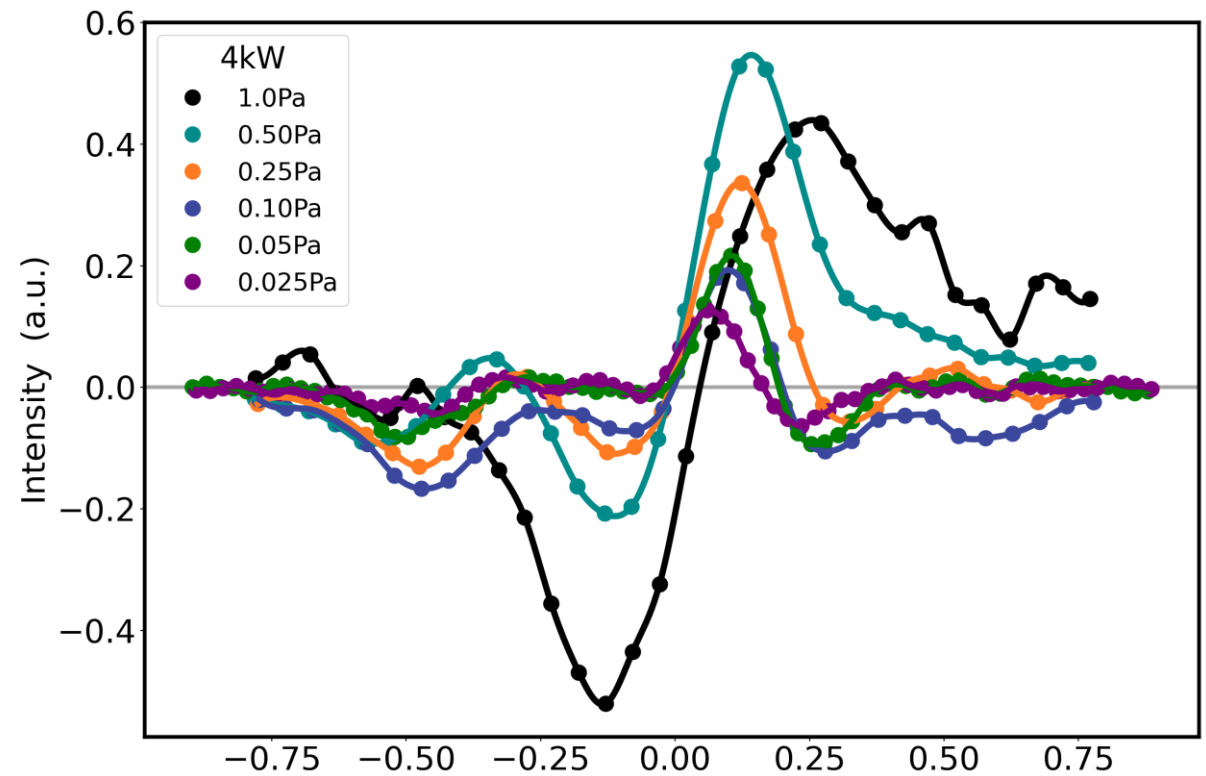
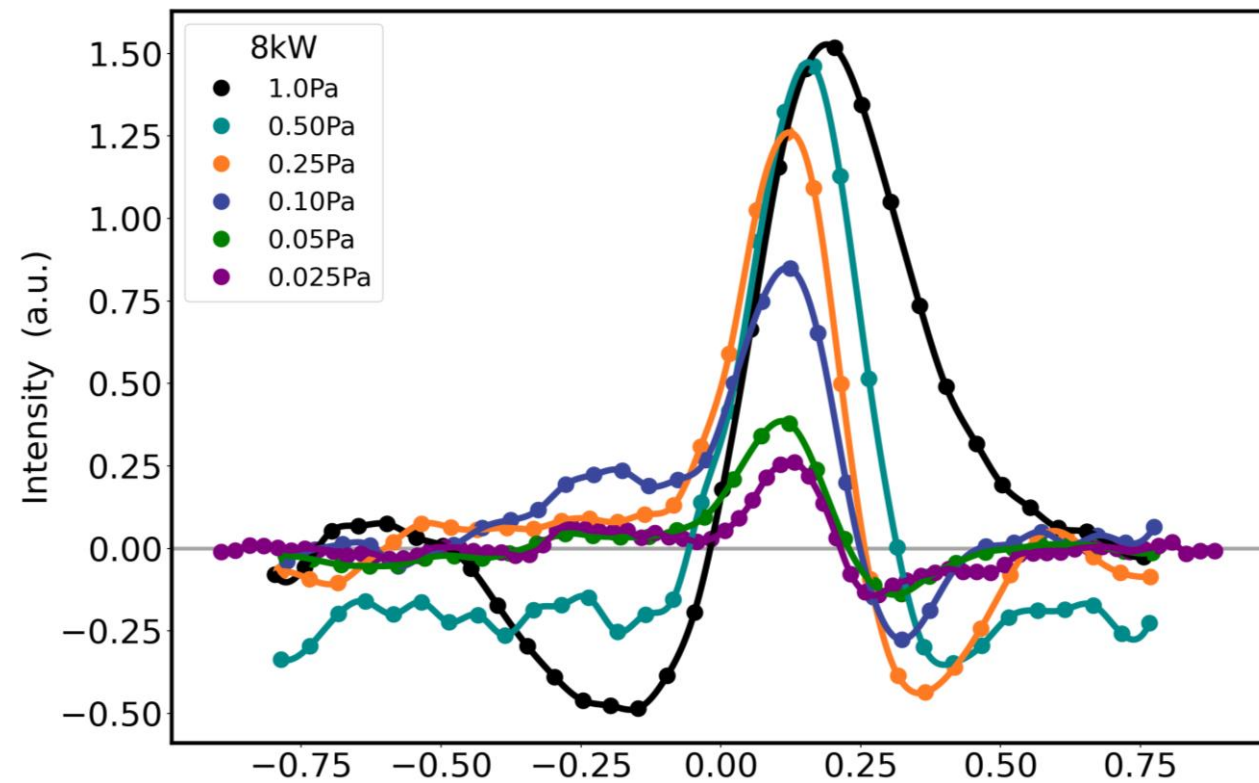


Results in H2: Pressure variation

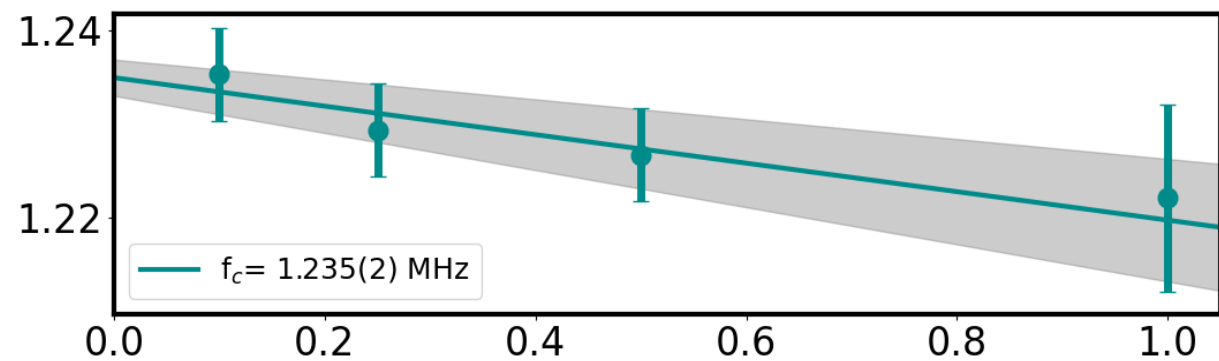
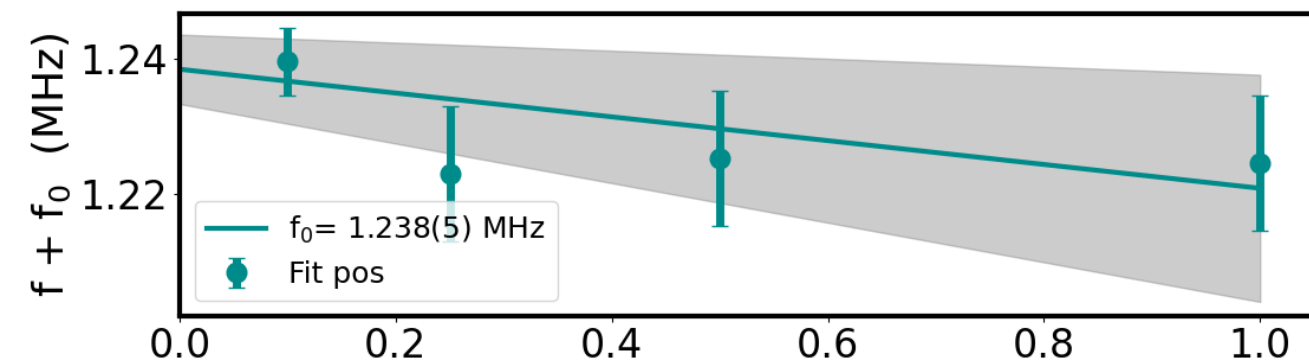
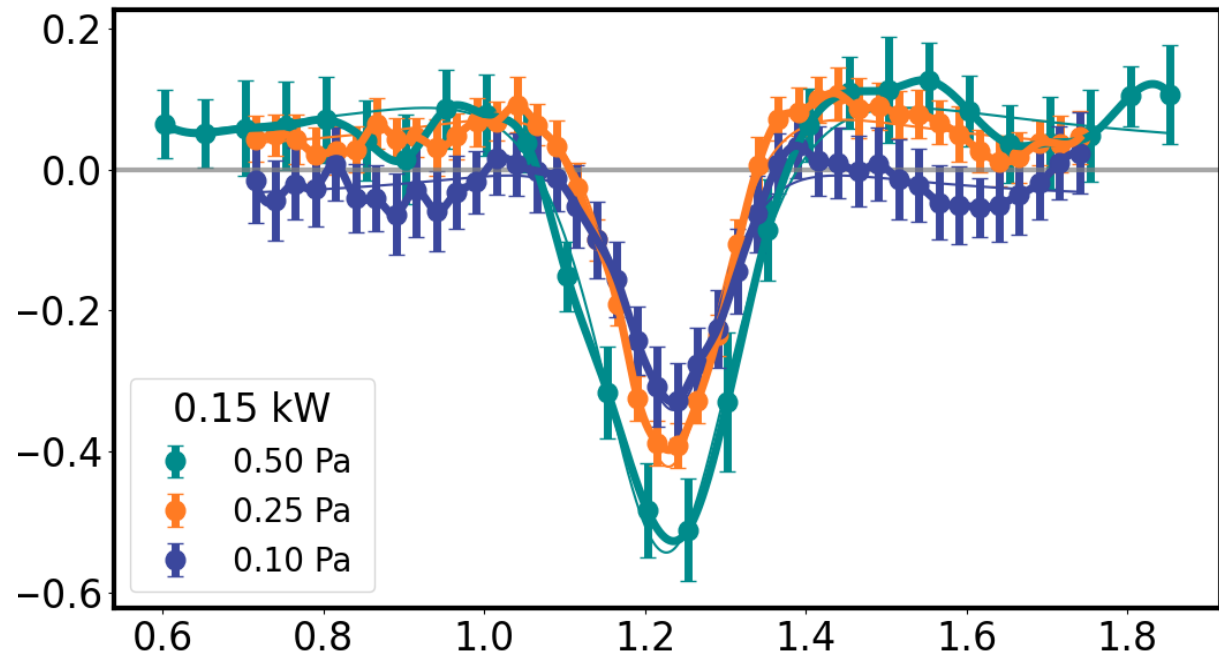
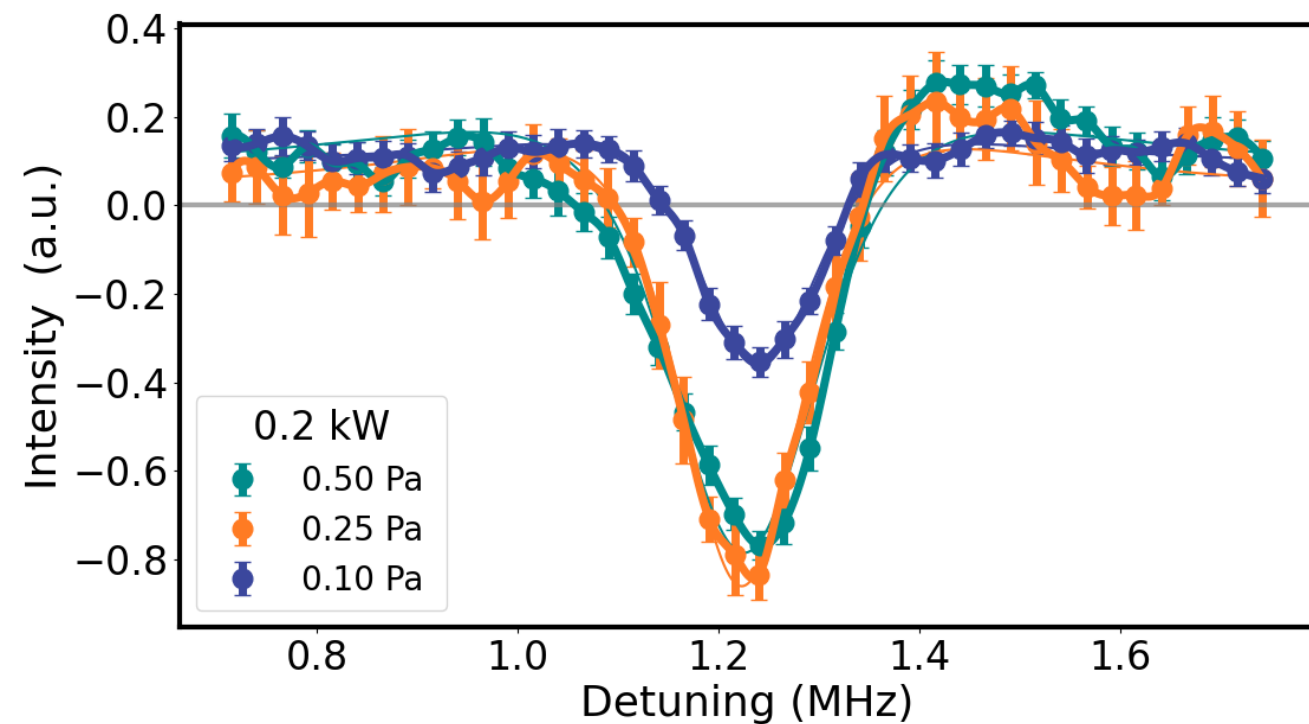
- 4 kW of power
- 55 K temperature
- Signal doesn't drop as expected



Niceohms = random lineshape simulator

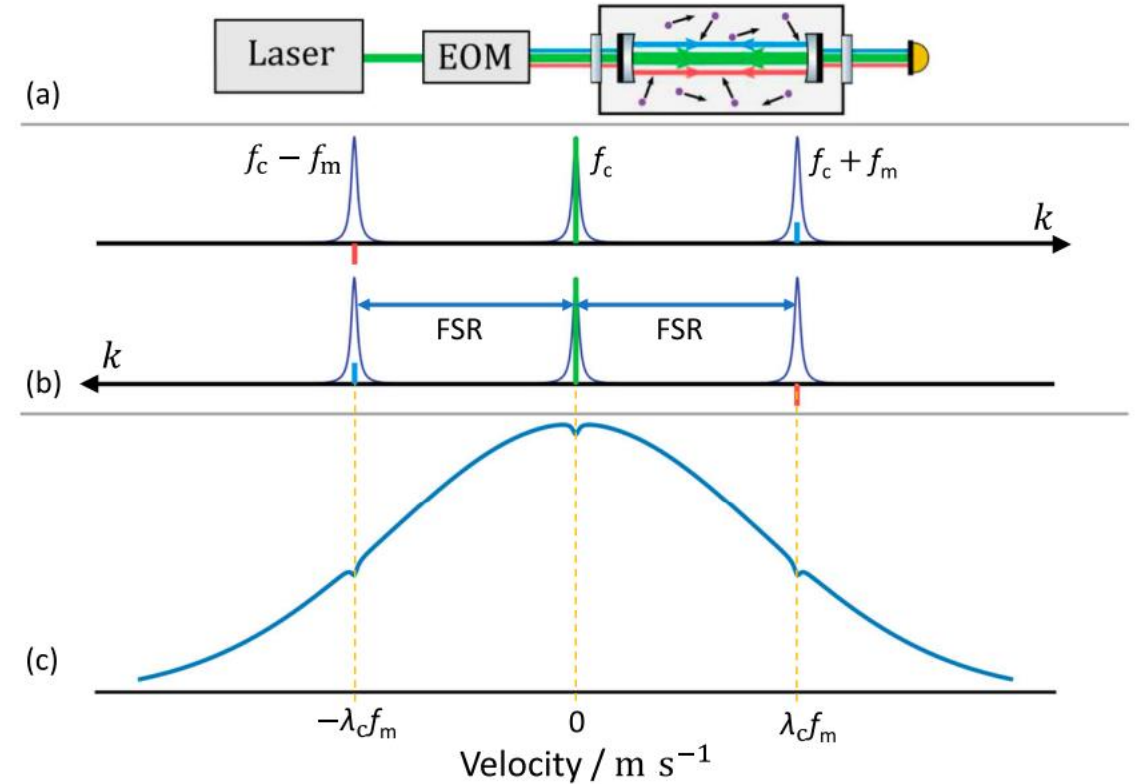
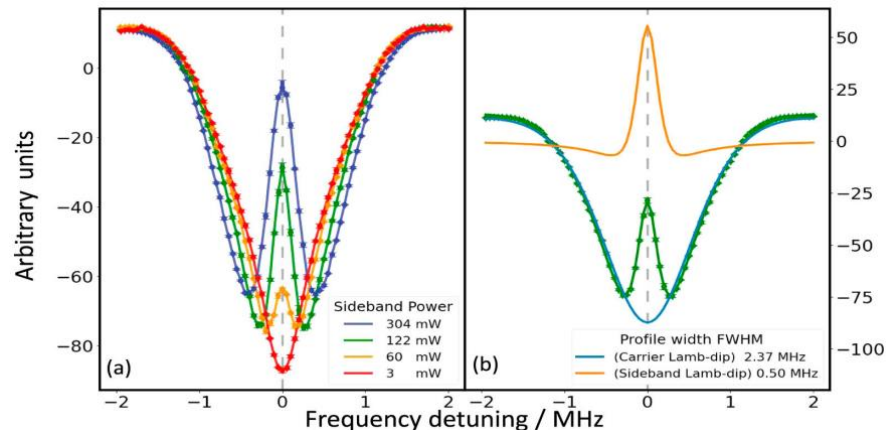


H₂S(0) position extraction



Carrier-Carrier saturation

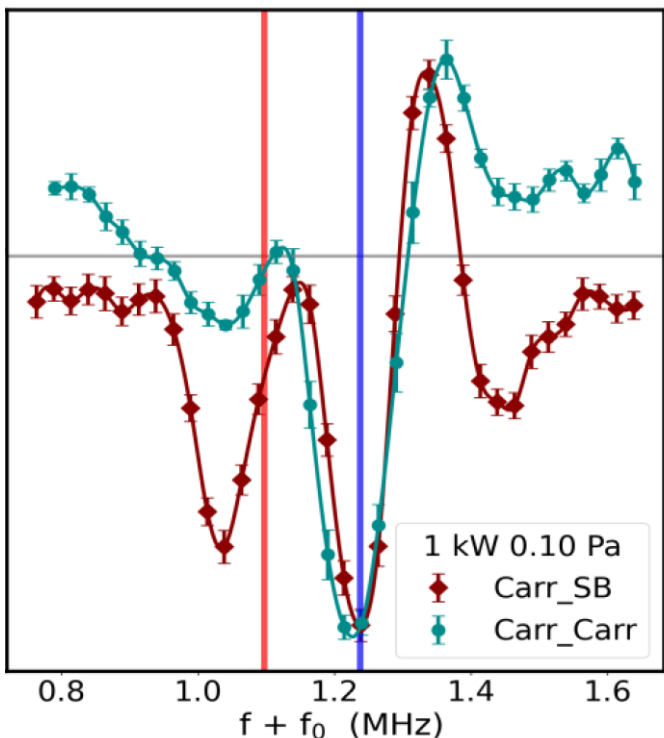
- ‘standard’ scheme
- Orthogonal flying molecules
- Strong on-resonance standing wave
- Only signal in dispersion phase
- Actually composition of two signals
 - Carrier-Carrier
 - Doppler detuned sidebands
- Typically invisible as summation of opposite sign
- Visible for strong transitions such as water



Doppler-detuned saturation spectroscopy (pump probe)

Results on H2

- Saturating molecules flying along the beam
- Doppler shift equal to detuning
- On-resonance standing wave \rightarrow travelling wave
 - Sideband only a few watt



Recoil doublet recovered

- Asymmetric lineshapes
- Red recoil is suppressed
- Recoil shift must be applied

Both dispersion and absorption channel

