

# 暗黒物質の半対消滅から生じるシグナル

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阿蘇研究会

参考文献: Phys.Rev.D 105 (2022) 4, 043007,  
arXiv:2309.00395

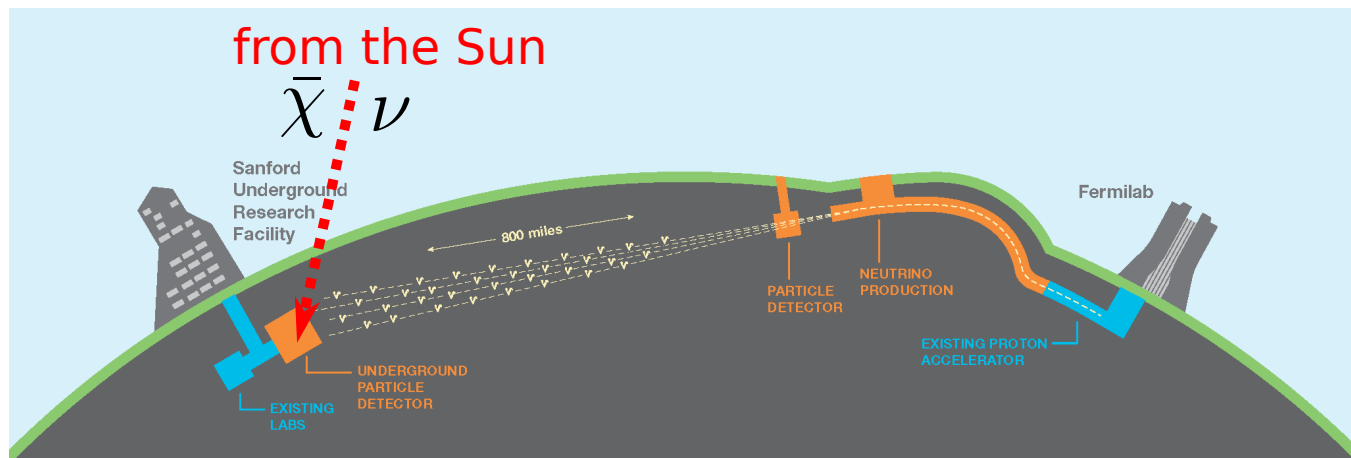
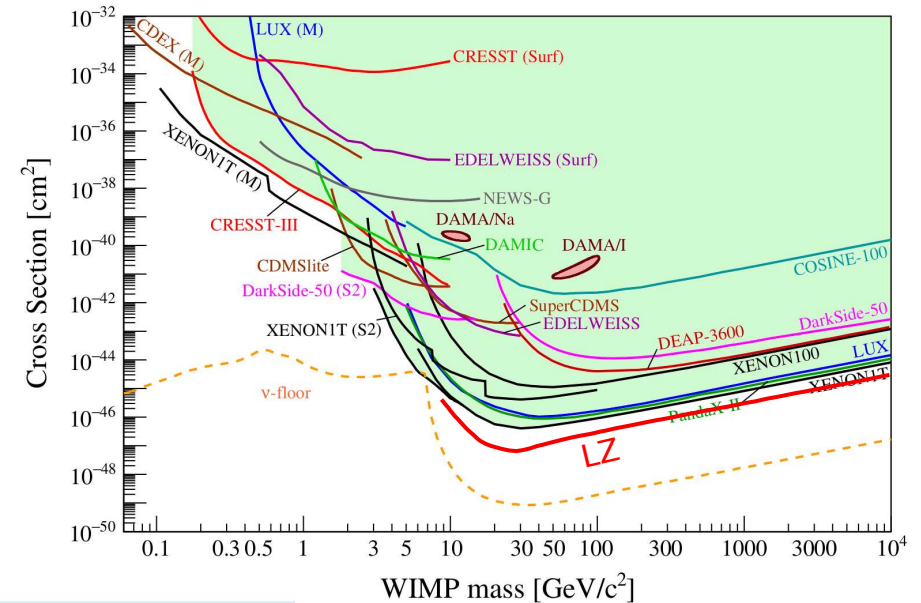
共同研究者：青木 真由美 氏



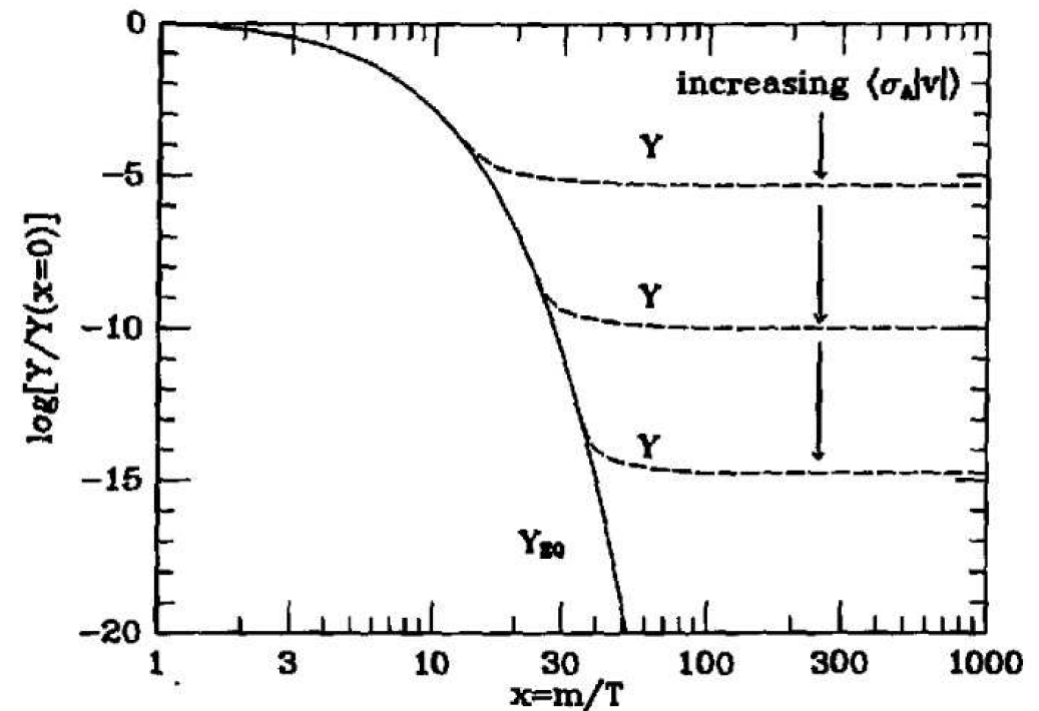
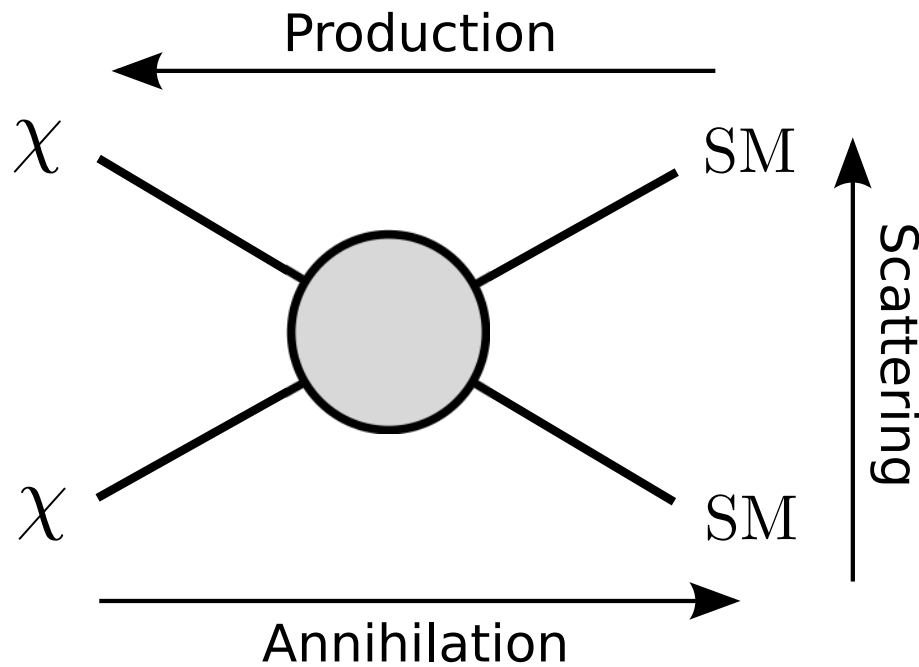
# 要約

- DM 直接検出実験の制限が強い  
 ⇒ 速度または運動量依存の散乱断面積 (ex. pNG DM)  
 ⇒ 速度の速いDMが生成  
 されれば検出できるかも
- DM 加速機構の一つ  
 半対消滅 (semi-annihilation)  
 $\chi\chi \rightarrow \chi\phi$
- DUNEで検証できるかも

参照：日本物理学会誌 2023年6月号



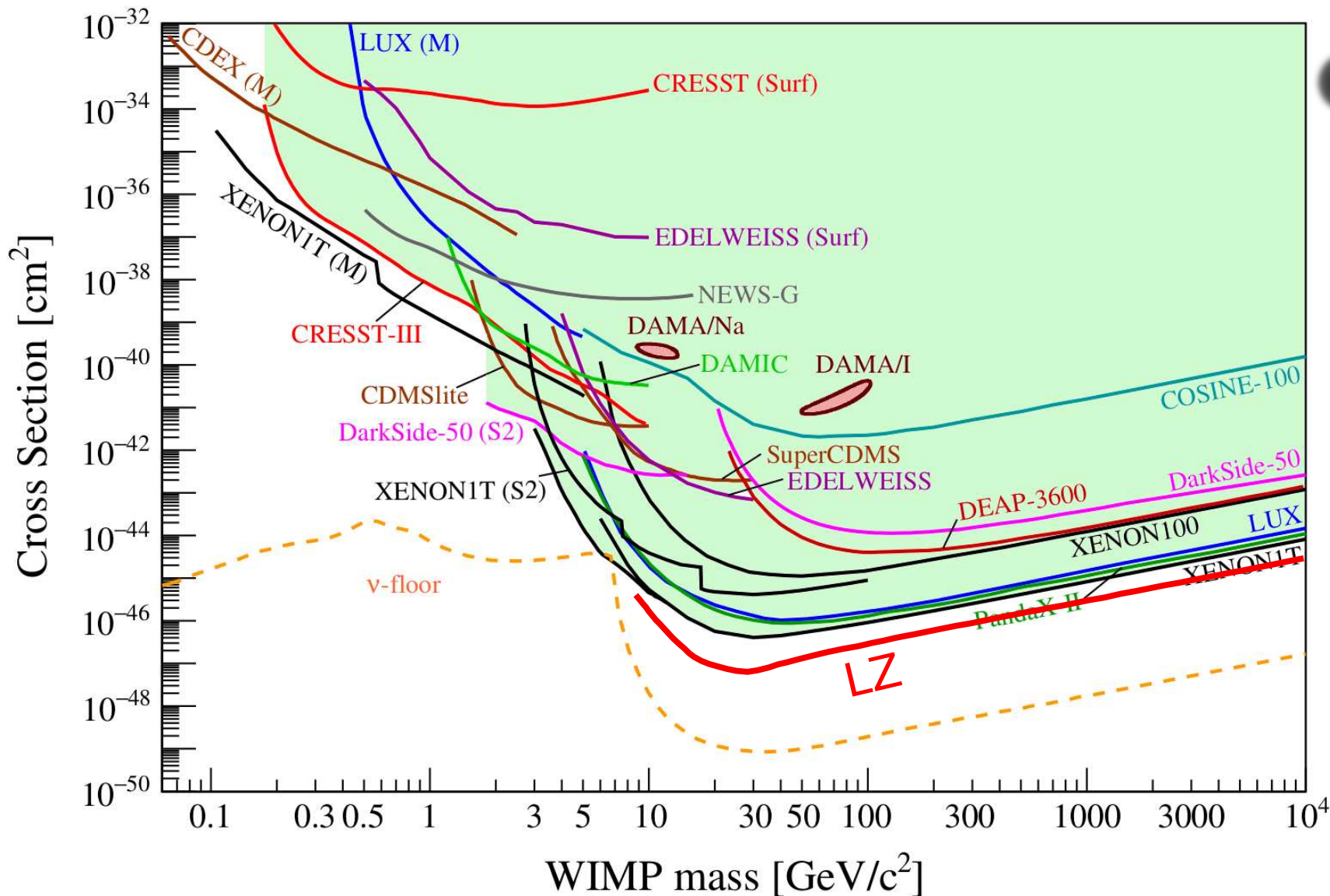
# WIMP (Weakly Interacting Massive Particle)



$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle (n_\chi^2 - n_\chi^{\text{eq}2})$$

- WIMP is thermalized with SM particles in early universe
- To get  $\Omega_\chi h^2 = 0.12$ , roughly  $\sigma \sim 1\text{pb} \sim 10^{-26}\text{cm}^3/\text{s} \sim 10^{-36}\text{cm}^2$
- Almost independent on DM mass
- Mass range: 10 MeV – 100 TeV

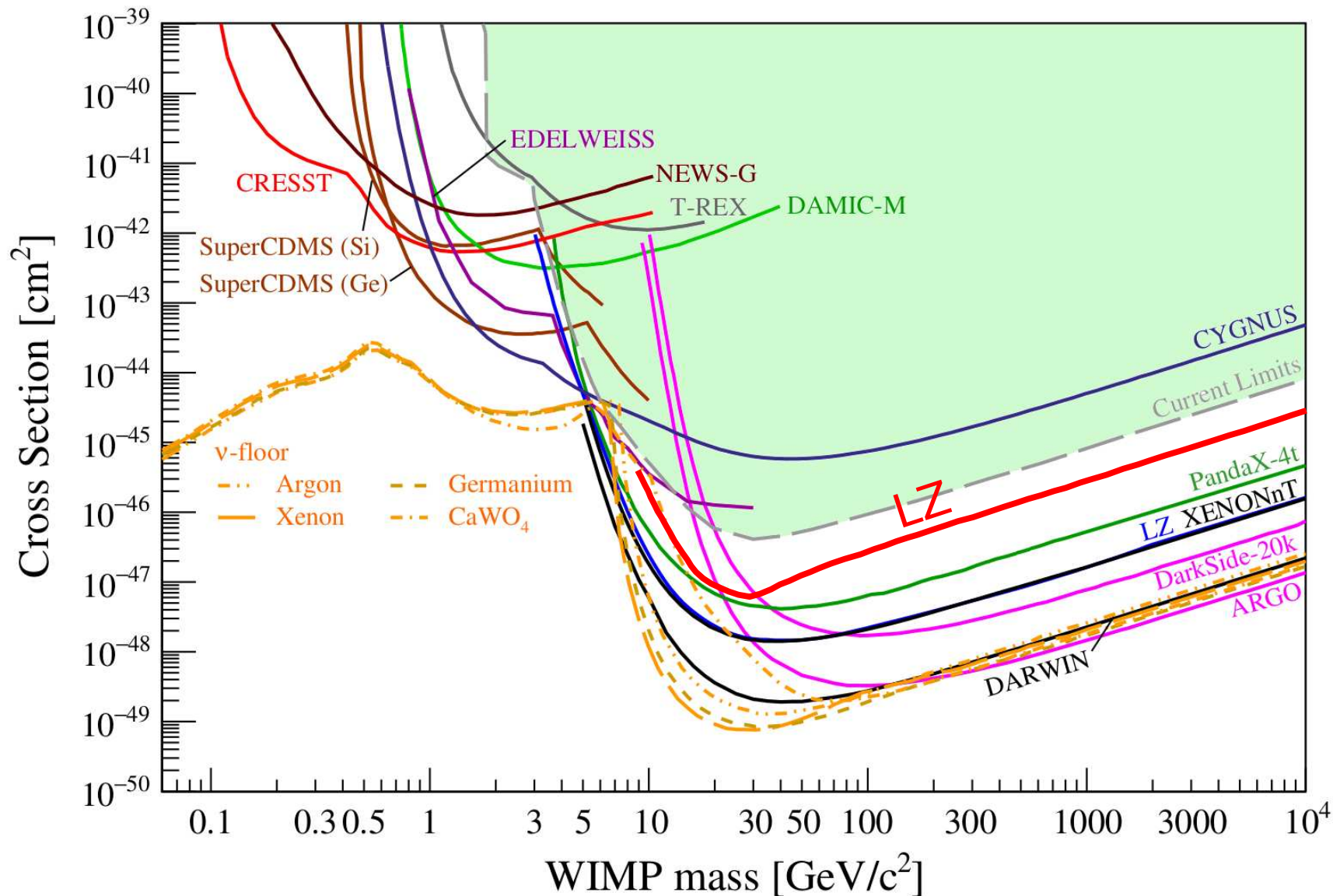
# Status of direct detection experiments



arXiv:2104.07634  
 LZ arXiv:2207.03764

- LZ gives the strongest bound above 10 GeV DM mass at present.

# Future sensitivity of direct detection experiments



Billard et al.,  
arXiv:2104.07634  
LZ arXiv:2207.03764

- Experiments will reach the neutrino floor in 20 years.

# Wayout

- $v_\chi$  dependent cross section ( $v_\chi \sim 10^{-3}$ )

Ex.1 pNGB DM ( $i\mathcal{M} \propto v_\chi^2$ )

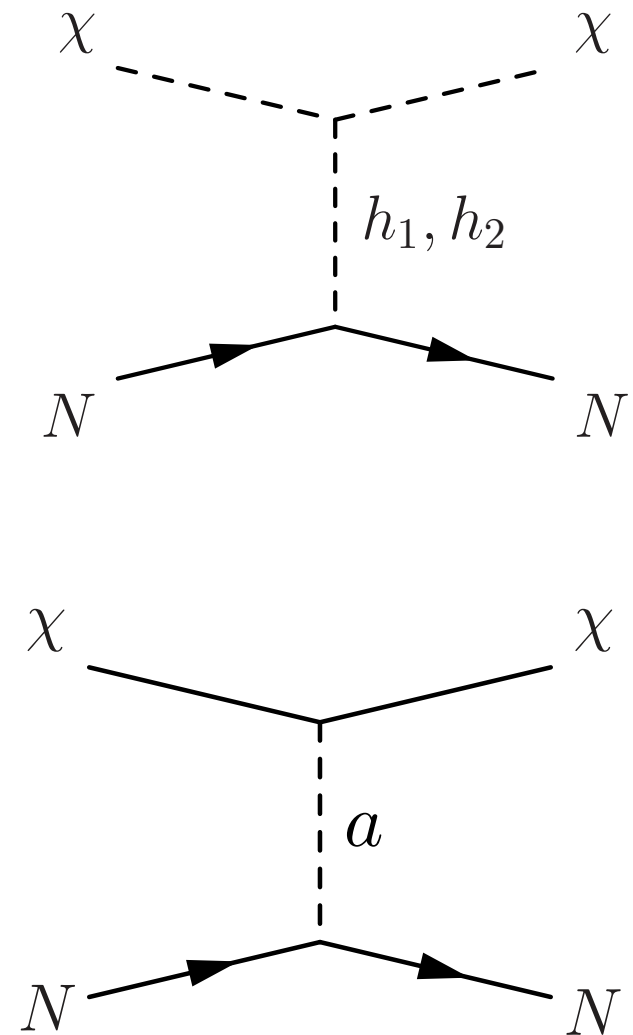
C. Gross, O. Lebedev, TT, PRL (2017) [arXiv:1708.02253]

Ex.2 Fermion DM with Pseudo-scalar int.

$$\mathcal{L} = a\bar{\chi}\gamma_5\chi$$

T. Abe, M. Fujiwara, J. Hisano, JHEP (2019) [arXiv:1810.01039]

⇒ These could be detected if boosted.





# Velocity-dependent scattering $\chi p \rightarrow \chi p$

$$\text{Anapole int.} \quad \mathcal{L} \supset \frac{1}{\Lambda^2} \bar{\chi} \gamma_\mu \gamma_5 \partial_\nu \chi F^{\mu\nu} \quad \rightarrow \quad \sigma \propto v^2$$

$$\text{SP int.} \quad \mathcal{L} \supset \frac{1}{\Lambda^2} (\bar{\chi} \chi) (\bar{p} \gamma_5 p) \quad \rightarrow \quad \sigma_{\text{SD}} \propto v^2$$

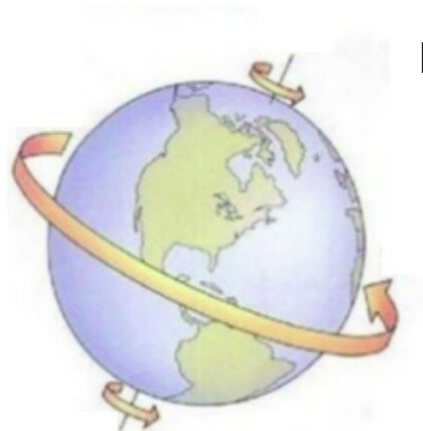
$$\text{PP int.} \quad \mathcal{L} \supset \frac{1}{\Lambda^2} (\bar{\chi} \gamma_5 \chi) (\bar{p} \gamma_5 p) \quad \rightarrow \quad \sigma_{\text{SD}} \propto v^4$$

# Mechanisms to boost DM

- Semi-annihilations  $\chi\chi \rightarrow \bar{\chi}\phi$  ( $v_\chi = \mathcal{O}(0.1 - 1)$ )  
 $\Rightarrow$  Simple and small uncertainties

## Other processes to boost DM

- Decay or annihilations of heavier particles (non-minimal dark sector)  
 $\chi_2\chi_2 \rightarrow \chi_1\chi_1$  ( $m_{\chi_2} \gg m_{\chi_1}$ )
- Collision with high energy cosmic-rays



boosted DM



Bringmann and Pospelov, PRL (2019), arXiv:1810.10543

<https://phys.org>



# Semi-annihilations

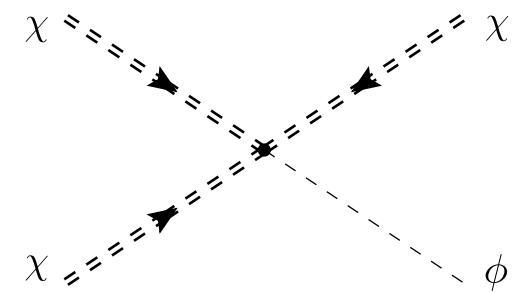
- $\chi_i \chi_j \rightarrow \chi_k \phi$       F. D'Eramo and J. Thaler, JHEP (2010) [arXiv:1003.5912]  
 $\chi_i$ : DM particles,       $\phi$ : SM or new unstable particle  
 One DM particle is in final state.
- Simplest case:  $\chi\chi \rightarrow \bar{\chi}\phi$   
 $\chi$ : DM,       $\phi$ : SM particle or new unstable particle
- Simple  $\mathbb{Z}_2$  parity does not work to stabilize DM.  
 $\Rightarrow$  DM is a non self-conjugate particle.
- Boltzmann equation

$$\frac{dn_\chi}{dt} + 3Hn_\chi = - \langle \sigma_{\chi\bar{\chi}} v \rangle (n_\chi^2 - n_\chi^{\text{eq}2}) - \langle \sigma_{\chi\chi} v \rangle (n_\chi^2 - n_\chi n_\chi^{\text{eq}})$$

1st term: normal ann.

2nd term: semi-ann.

Note: normal annihilations also exist.



# Example of model building

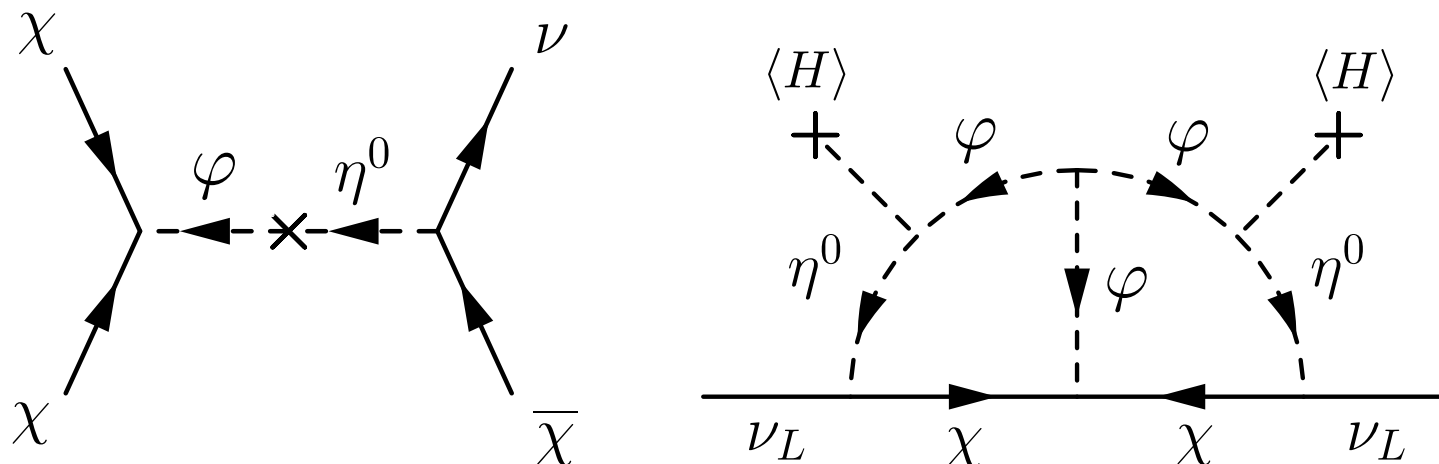
- Semi-annihilation  $\chi\chi \rightarrow \nu\bar{\chi}$

Ex.  $\mathbb{Z}_3$  symmetric model with radiative neutrino masses

M. Aoki and TT, JCAP (2014) [arXiv:1405.5870]

	$\chi_L$	$\chi_R$	$\eta$	$\varphi$
$SU(2)$	<b>1</b>	<b>1</b>	<b>2</b>	<b>1</b>
$U(1)_Y$	0	0	1/2	0
$\mathbb{Z}_3$	1	1	1	1
L number	1/3	1/3	-2/3	-2/3

New particles



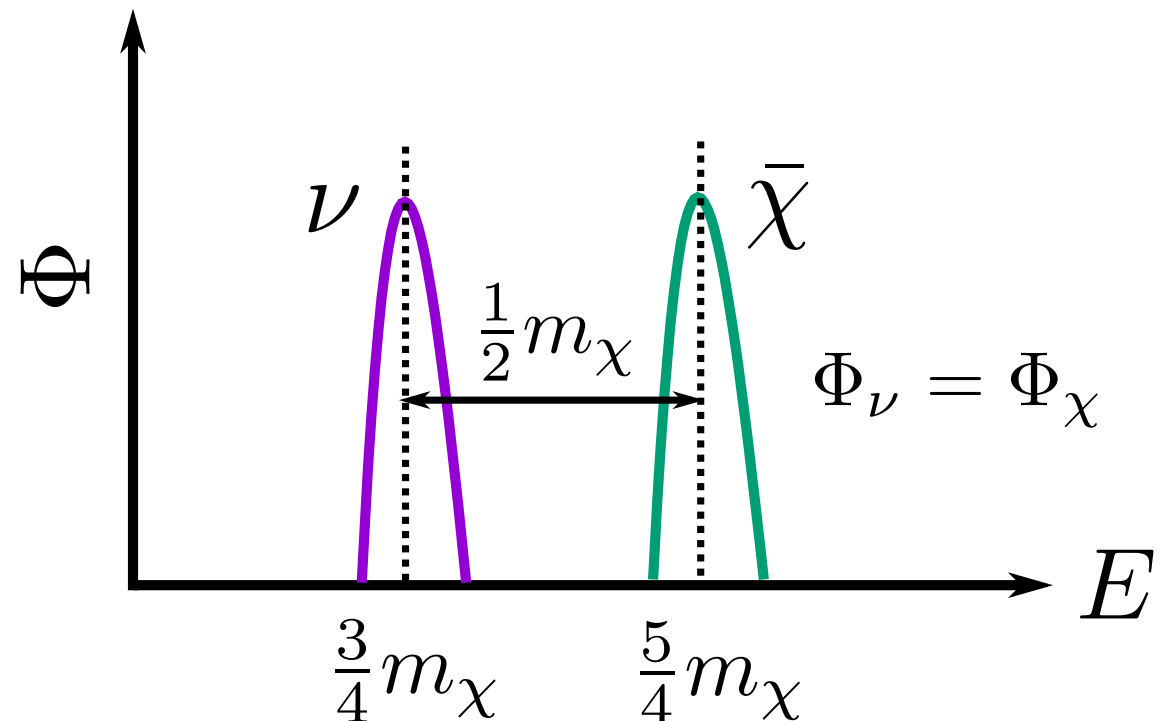
# Distinctive signals from semi-annihilations

# Specific semi-annihilation process

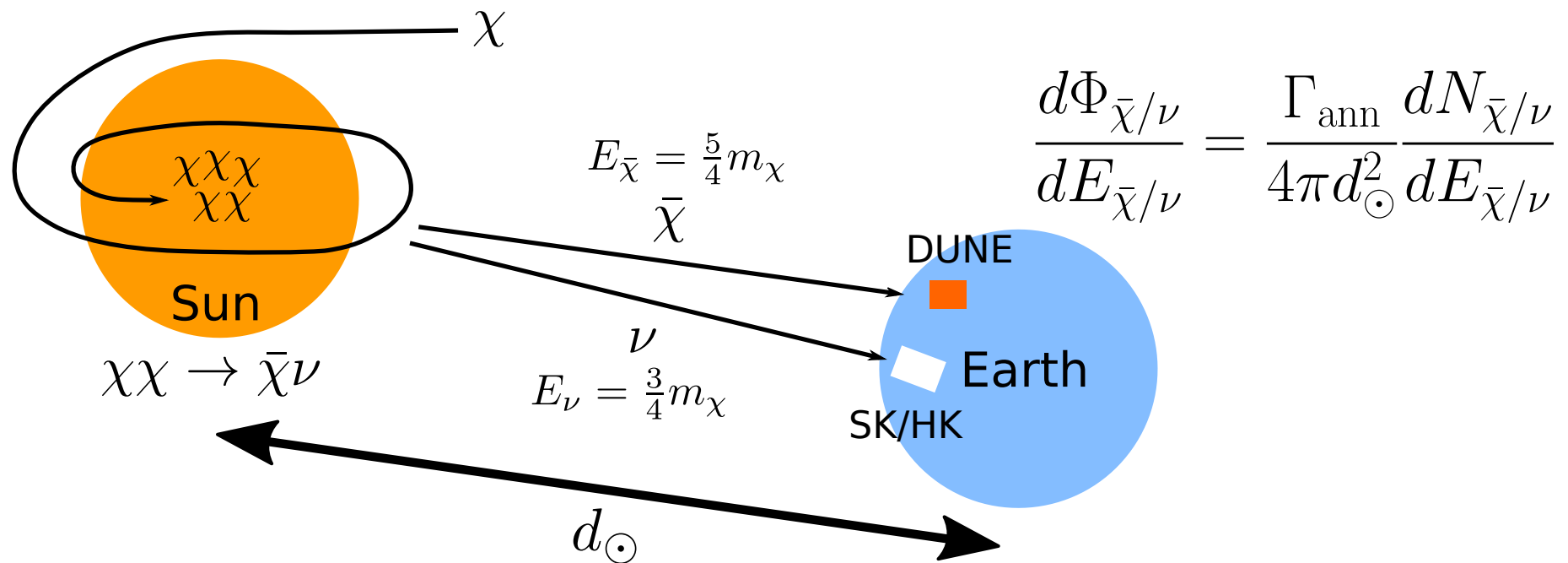
- We focus on  $\chi\chi \rightarrow \nu\bar{\chi}$ .
  - Both final state particles are monochromatic
  - May correlate with generation of small neutrino masses
- Energy of the produced particles

$$E_{\bar{\chi}} = \frac{5}{4}m_{\chi} \quad (v_{\chi} = 0.6), \quad E_{\nu} = \frac{3}{4}m_{\chi}$$

- Possible to detect both particles (monochromatic)
  - Energy difference:  $\frac{1}{2}m_{\chi}$
  - Same flux for  $\bar{\chi}$  and  $\nu$
- If detected, this strongly implies that DM is a Dirac fermion with spin 1/2.

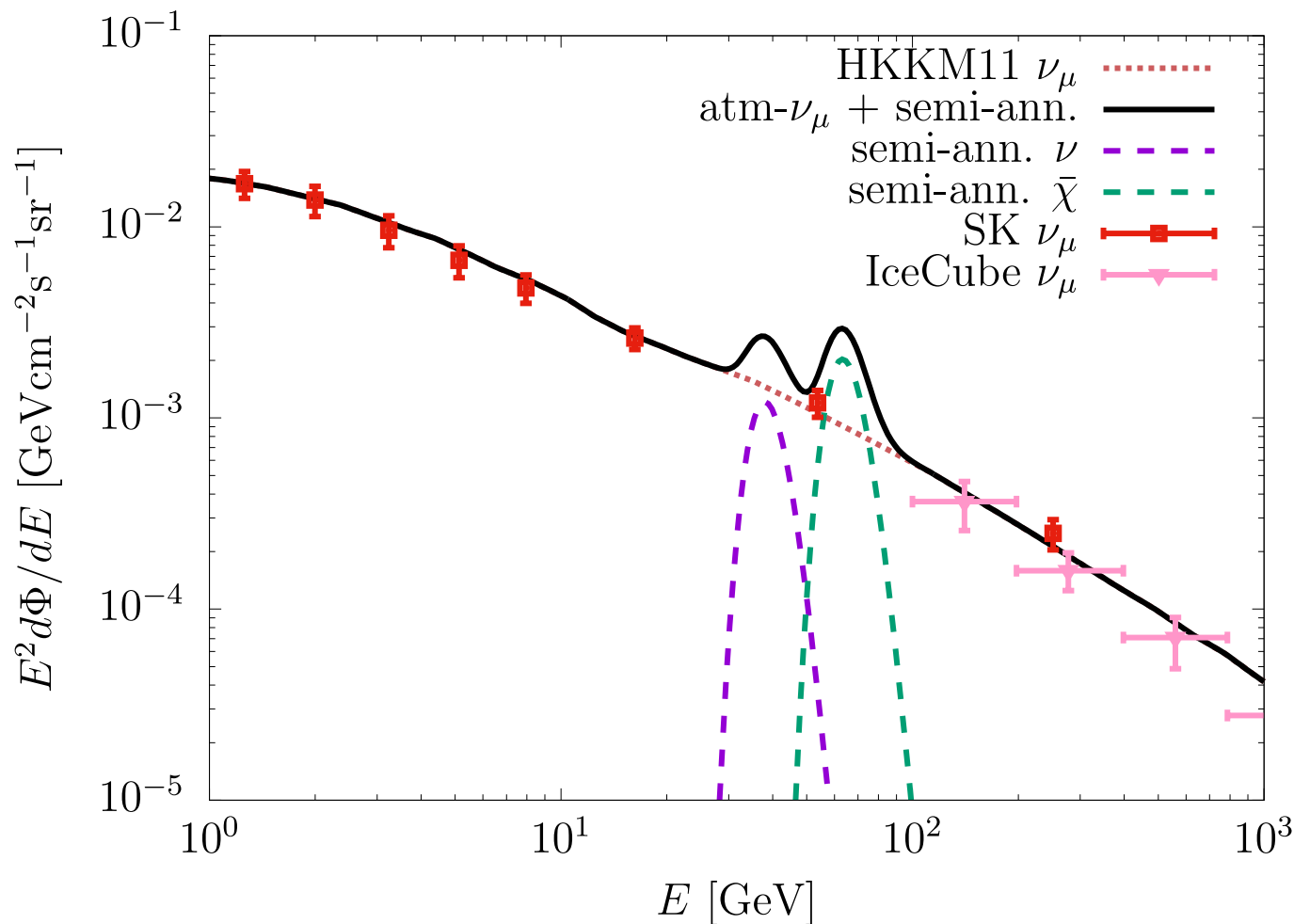


# Signals from the Sun

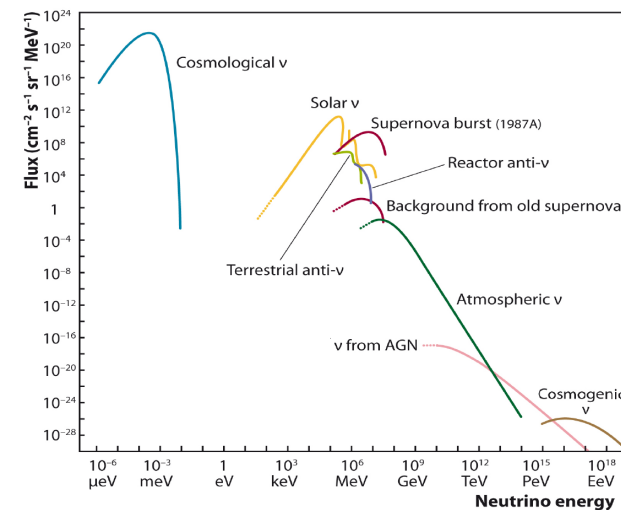


- A number of DM particles are accumulated in the centre of the Sun.
- Semi-annihilation occurs.
- Two kinds of signals can be searched at large volume neutrino detectors (SK, HK, DUNE etc).
- Signals produced at Galactic centre is smaller.

# $\nu + \bar{\chi}$ flux if it is nicely reconstructed



- $$E_{\bar{\chi}} = \frac{5}{4} m_\chi$$
- $$E_\nu = \frac{3}{4} m_\chi$$
- $$\Delta E = \frac{1}{2} m_\chi$$



- $m_\chi = 50 \text{ GeV}$  and  $\sigma_{\text{SD}} = 3 \times 10^{-41} \text{ cm}^2$  (non-relativistic)

- $\Delta E/E = 25\%$  is assumed

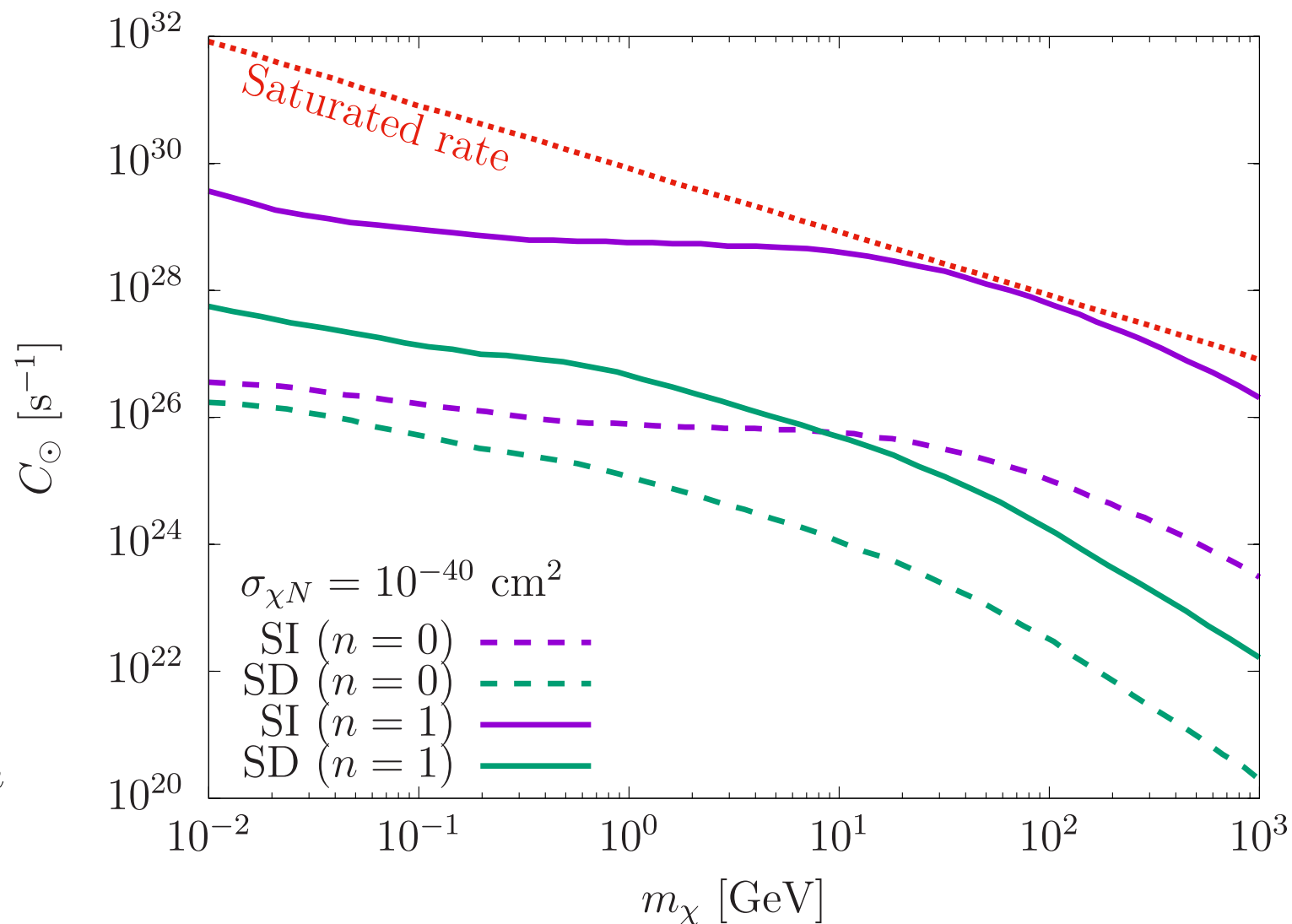
U. Katz and C. Spiering, Prog. Part. Nulc. Phys. (2012) [arXiv:1111.0507]



# Semi-annihilation at the Sun

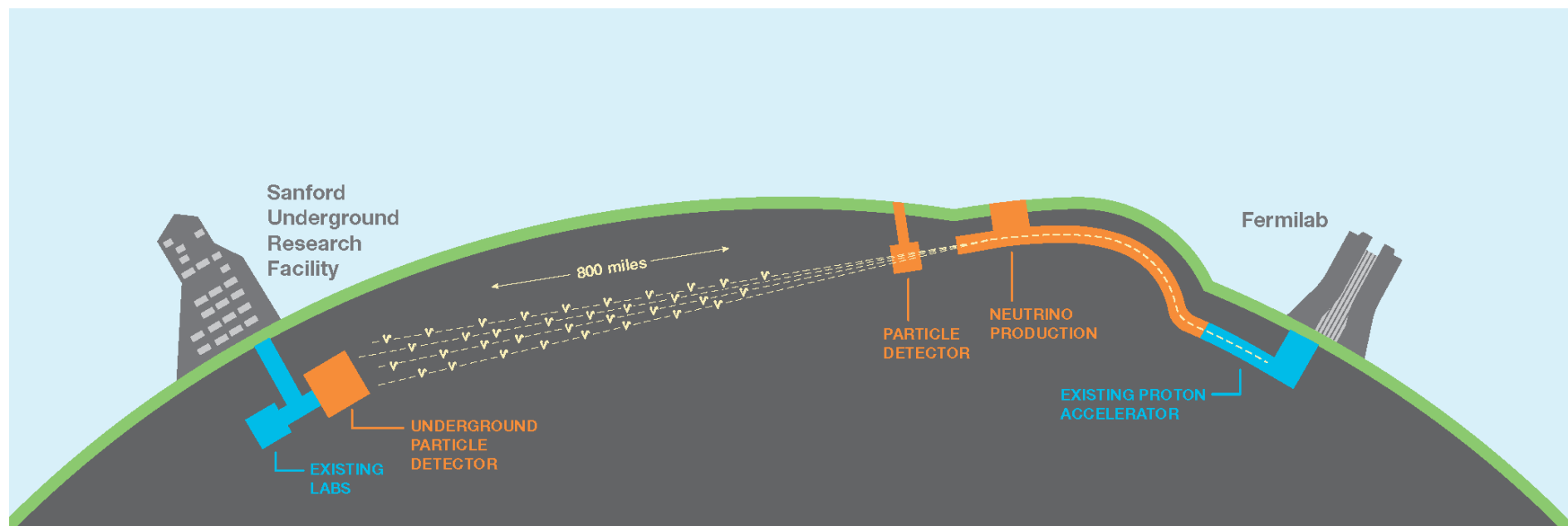
R. Garani et al., JCAP (2014) [arXiv:1702.02768]

- Capture rate for const. and  $Q^2$  (momentum transfer) dependent cases ( $C_{\odot} = \Gamma_{\text{capt}}$ )

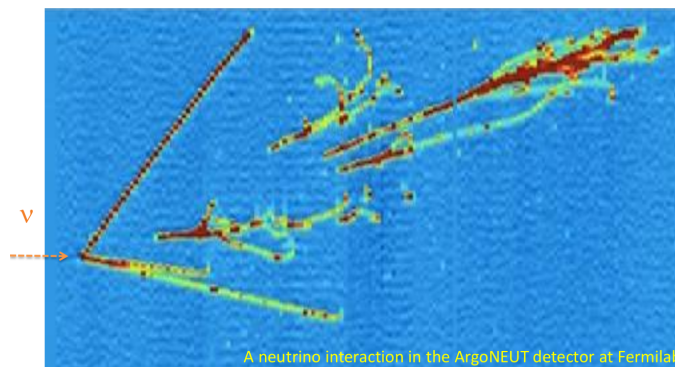


$$\sigma_{\chi N} \sim \sigma_0 (Q^2 / Q_0^2)^n$$

# DUNE (Deep Underground Neutrino Experiment)



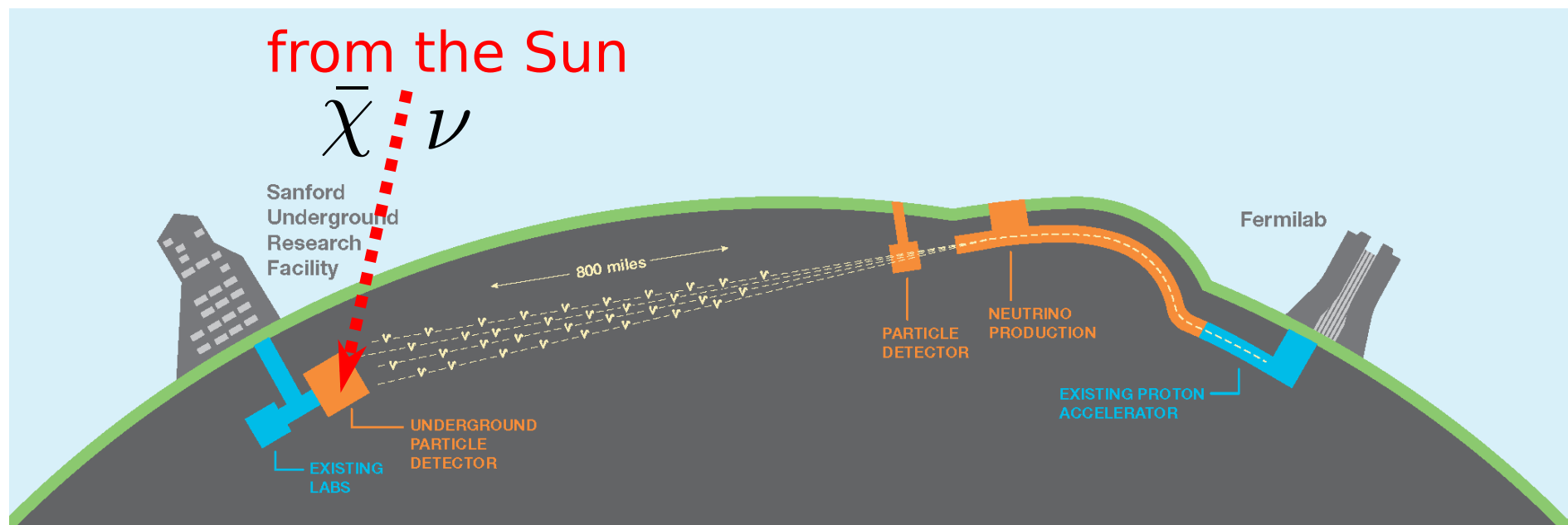
- Two detectors: near and **far** detectors.
- Massive liquid argon (fiducial volume: 40kt)
- Precise reconstruction of particle's trajectories with LArTPC



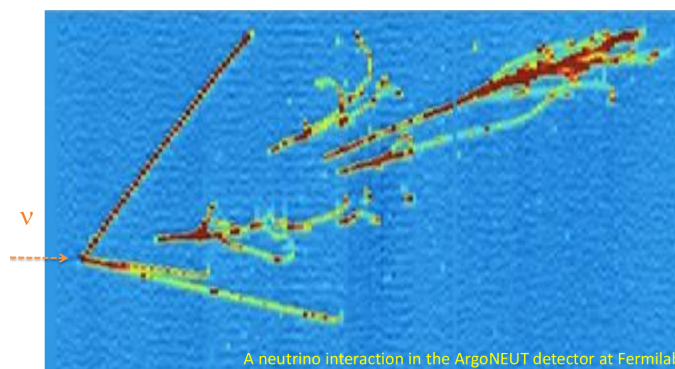
DUNE Coll., [arXiv:2002.03005]



# DUNE (Deep Underground Neutrino Experiment)



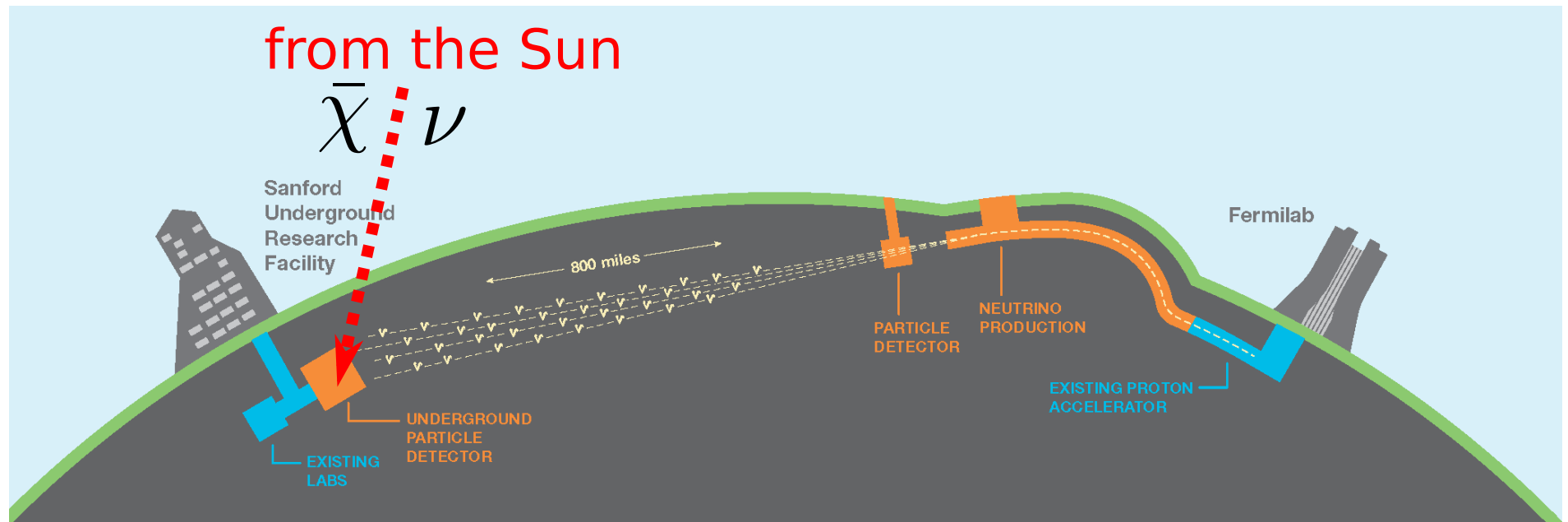
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DUNE Coll., [arXiv:2002.03005]



# DUNE (Deep Underground Neutrino Experiment)

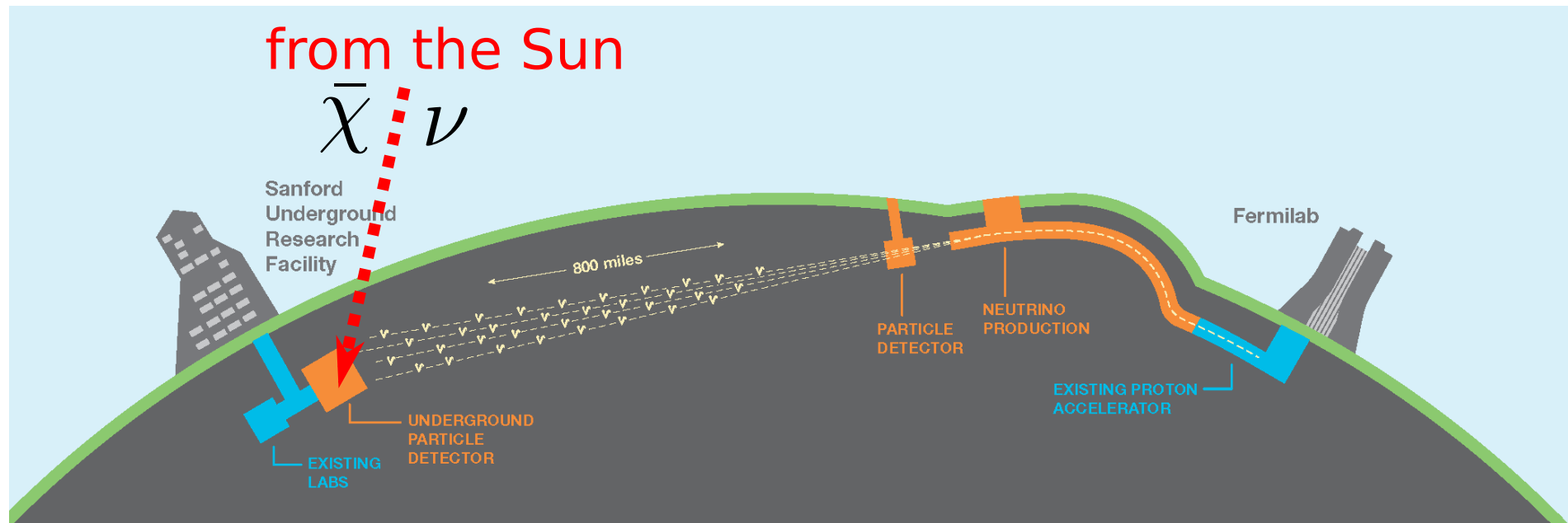


DUNE Coll., [arXiv:2002.03005]

## Timeline of far detector modules

- 2025: DUNE physics data taking with atmospheric neutrinos (fiducial mass 20kt)
- 2026: DUNE physics data taking with beam starts (fiducial mass 20kt)
- 2027: add third fiducial module (20kt + 10kt = 30kt)
- 2029: add fourth fiducial module (30kt + 10kt = 40kt)

# DUNE (Deep Underground Neutrino Experiment)



Timeline of far detector modules  $\Rightarrow$  **Delayed**

DUNE Coll., [arXiv:2002.03005]

More cost is needed than initially expected. (2 billion  $\Rightarrow$  3 billion dollars)

- 2029: slimmed version of DUNE will run
- 2035: DUNE full spec (40kt)
- 2027: Hyper-K

$\Rightarrow$  No advantage of DUNE for  $\nu$  mass ordering, CP violation etc.

# Simulation tool

## ■ GENIE (neutrino event generator)

<http://www.genie-mc.org/>

- Detailed experimental simulation (DUNE, SK etc) can be done.
- Boosted DM can also be implemented.



```

-----
GENIE GHEP Event Record [print level:  3]
-----
  Idx |      Name | Ist |      PDG |  Mother |  Daughter |  Px |  Py |  Pz |  E |  m
-----
  0 |   chi_dm |  0 | 2000010000 | -1 | -1 |  4 |  4 |  0.000 |  0.000 | 37.500 | 62.500 | **1.000 | M = 50.000
  1 |   Ar40  |  0 | 1000180400 | -1 | -1 |  2 |  3 |  0.000 |  0.000 |  0.000 | 37.216 | 37.216
  2 |  neutron | 11 |      2112 |  1 | -1 |  5 |  5 |  0.156 | -0.039 |  0.178 |  0.929 | **0.940 | M = 0.897
  3 |   Ar39  |  2 | 1000180390 |  1 | -1 |  7 |  7 | -0.156 |  0.039 | -0.178 | 36.287 | 36.286
  4 |   chi_dm |  1 | 2000010000 |  0 | -1 | -1 | -1 |  0.530 |  0.110 | 36.892 | 62.140 | **1.000 | M = 50.000 P = (0.014,0.003,1.000)
  5 |  neutron | 14 |      2112 |  2 | -1 |  6 |  6 | -0.374 | -0.149 |  0.786 |  1.289 |  0.940 | FSI = 3
  6 |  neutron |  1 |      2112 |  5 | -1 | -1 | -1 | -0.569 | -0.091 |  0.611 |  1.261 |  0.940
  7 | HadrBlob | 15 | 2000000002 |  3 | -1 | -1 | -1 |  0.069 | -0.015 | -0.035 | 36.286 | **0.000 | M = 36.286
  8 | NucBindE |  1 | 2000000101 | -1 | -1 | -1 | -1 | -0.030 | -0.005 |  0.032 |  0.029 | **0.000 | M = -0.032
-----
Fin-Init:                                     | -0.000 |  0.000 | -0.000 |  0.000 |
-----
Vertex:      chi_dm @ (x =  0.00000 m, y =  0.00000 m, z =  0.00000 m, t =  0.000000e+00 s)
-----
Err flag [bits:15->0] : 000000000000000000 | 1st set:                                     none
Err mask [bits:15->0] : 111111111111111111 | Is unphysical: NO | Accepted: YES
-----
sig(Ev) =      4.88517e-38 cm^2 | dsig(Q2;E)/dQ2 =      1.73521e-39 cm^2/GeV^2 | Weight =      1.00000
-----

```

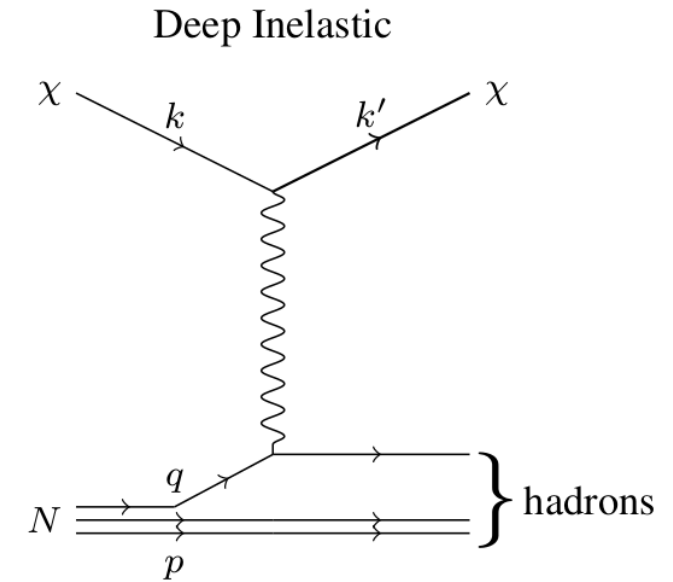
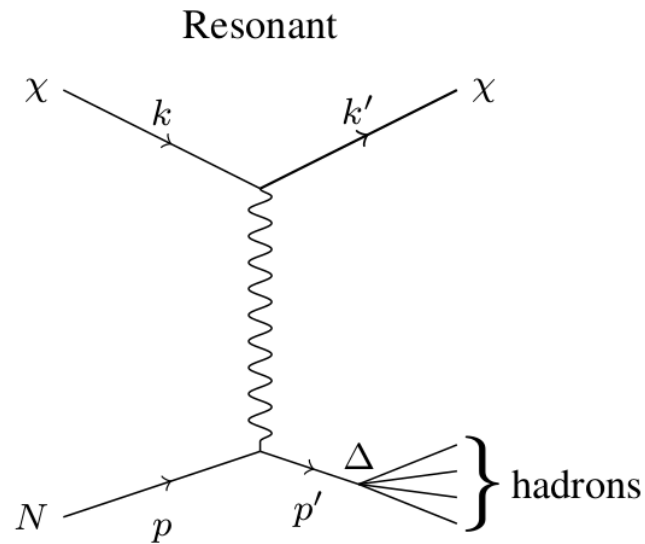
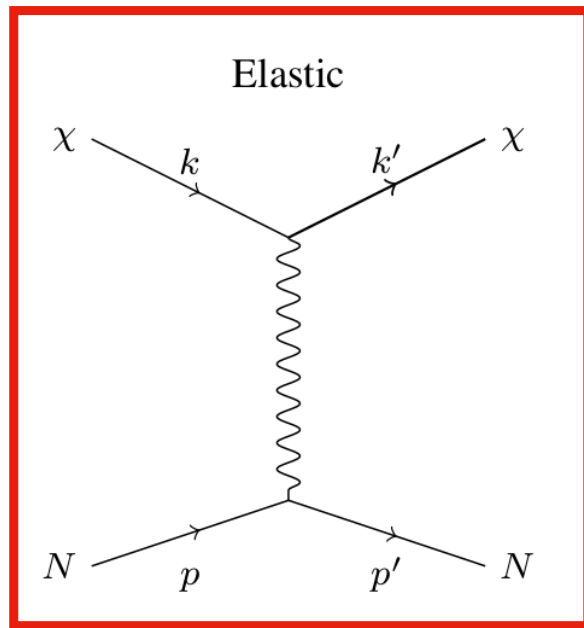


# Threshold and resolution for DUNE

	Detector threshold	Energy/momentum resolution	Angular resolution
$\mu^\pm$	30 MeV	5 %	1°
$\pi^\pm$	100 MeV	5 %	1°
$e^\pm/\gamma$	30 MeV	$2 + 15/\sqrt{E/\text{GeV}}$ %	1°
$p$	50 MeV	$p < 400 \text{ MeV: } 10 \%$ $p > 400 \text{ MeV: } 5 + 30/\sqrt{E/\text{GeV}}$ %	5°
$n$	50 MeV	$40/\sqrt{E/\text{GeV}}$ %	5°

- Precise angular resolution  
cf: 3° at SK and HK, 30° at IceCube
- These are taken into account in simulation.

# Setup for boosted dark matter



arXiv: 1912.05558, J. Berger et al.

- There are 3 processes.
- (Quasi)-elastic scattering is dominant for our case ( $\chi\chi \rightarrow \nu\bar{\chi}$ )  

$$0 \leq Q^2 \lesssim \frac{9}{4}m_N^2 \approx (2 \text{ GeV})^2$$

# Setup for boosted dark matter

We consider the following cross section (parametrization)

$$\frac{d\sigma_{\chi N}}{dQ^2} = \frac{\sigma_0 s}{4m_N^2 |\mathbf{p}_\chi|^2} \left( \frac{Q^2}{m_N^2 v_0^2} \right)^n |F(Q^2)|^2$$

■ Parameters:  $|\mathbf{p}_\chi| = \frac{5}{4}m_\chi$  and  $\sigma_0$  (reference cross section)

1  $n = 0$  (constant)

2  $n = 1$  ( $Q^2$  dependent)

3  $n = 2$  ( $Q^4$  dependent)

# Setup for boosted dark matter

Number of signal events ( $\bar{\chi} + N \rightarrow \bar{\chi} + N$ )

- $N_{\chi} = N_N T \int \sigma_{\chi N} \frac{d^2 \Phi_{\chi}}{dE_{\chi} d\Omega} dE_{\chi} d\Omega$
- Number of nucleons:  $N_N = 2.41 \times 10^{34}$

Exposure time:  $T = 10 \text{ yr}$

$$\text{DM flux: } \frac{d^2 \Phi_{\chi}}{dE_{\chi} d\Omega} = \frac{\Gamma_{\text{ann}}}{4\pi d_{\odot}^2} \sigma_{\chi N} \Bigg|_{E_{\chi}=5m_{\chi}/4} = \frac{C_{\odot}}{8\pi d_{\odot}^2} \sigma_{\chi N} \Bigg|_{E_{\chi}=5m_{\chi}/4}$$

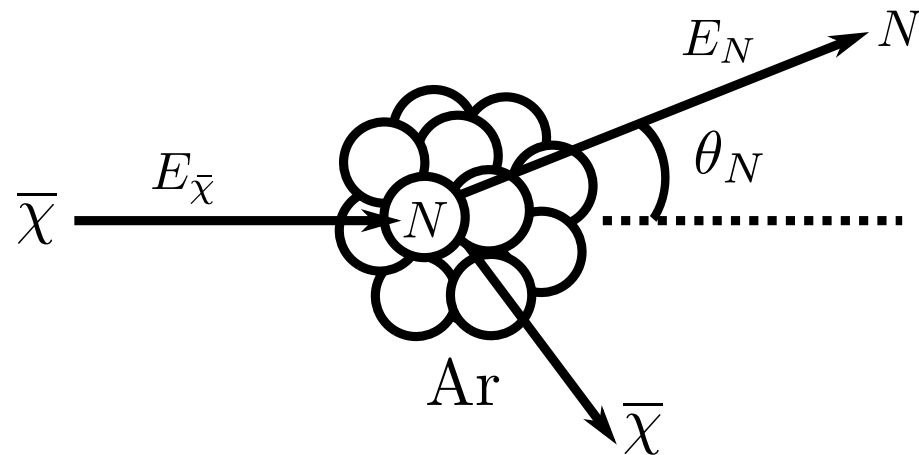
Distance between the Sun and Earth:  $d_{\odot} = 1.5 \times 10^{13} \text{ cm}$

# Boosted dark matter signal (energy reconstruction)

For elastic scattering  $\chi N \rightarrow \chi N$ , energy and angle are kinematically fixed.

- $$\cos \theta_N = \frac{E_\chi + m_N}{|\mathbf{p}_\chi|} \sqrt{\frac{E_N - m_N}{E_N + m_N}}$$

- Energy reconstruction from observed  $\theta_N$  and  $E_N$

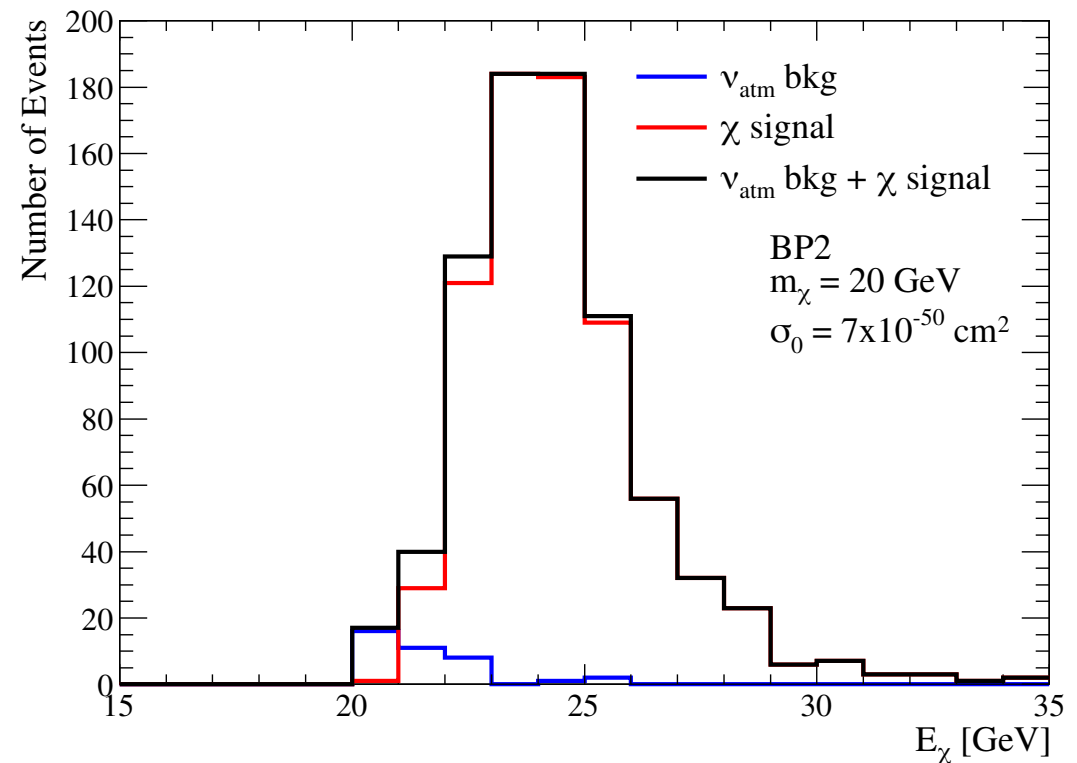


ex. benchmark point

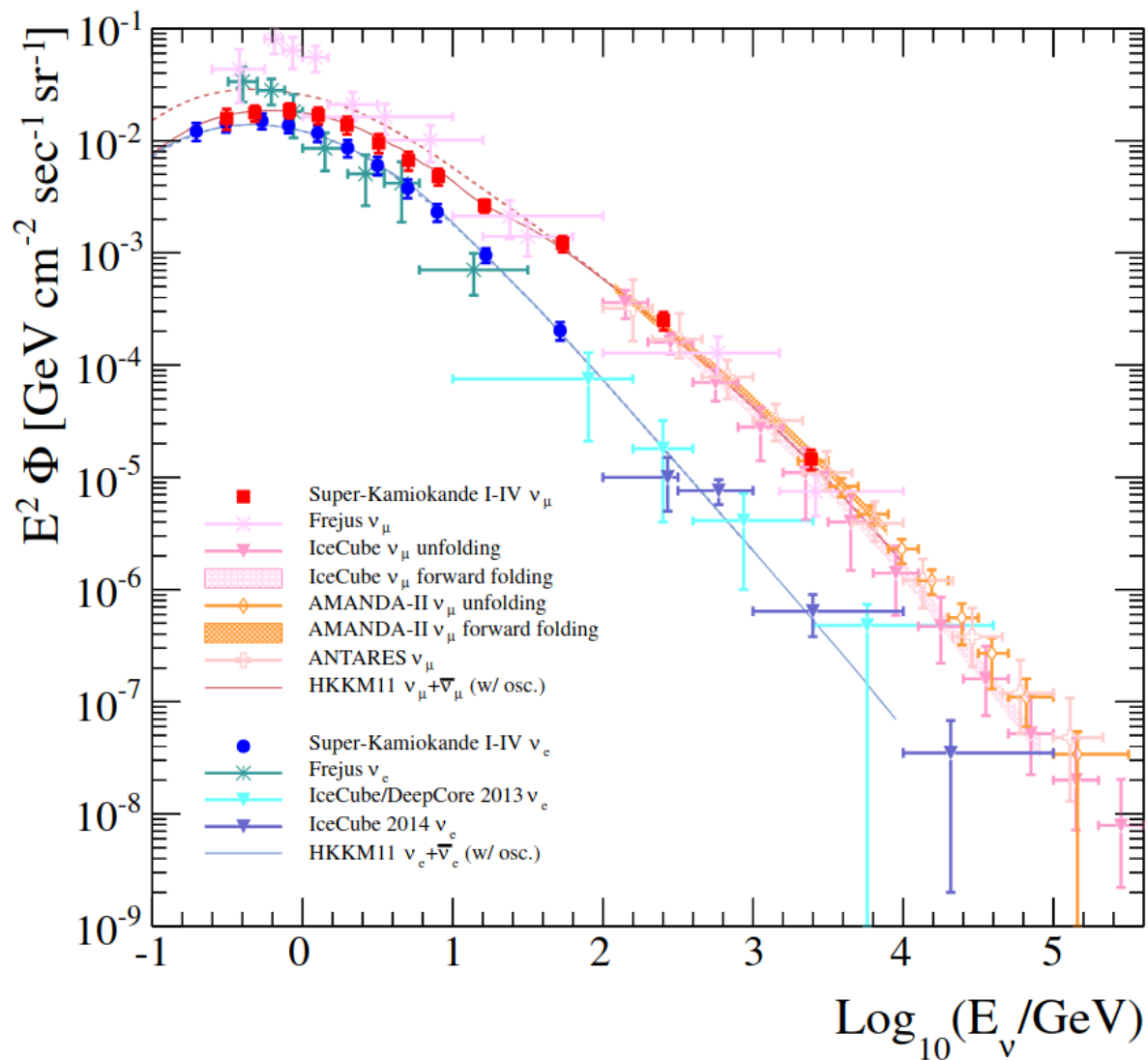
$$n = 2$$

$$m_\chi = 20 \text{ GeV},$$

$$\sigma_0 = 7 \times 10^{-50} \text{ cm}^2$$



# Background (atmospheric neutrinos)



$$N_{\text{atm } \nu} = N_N T \int \sigma_{\nu N} \frac{d^2 \Phi_{\nu}^{\text{atm}}}{dE_{\nu} d\Omega} dE_{\nu} d\Omega$$

Expected number of bkg events in 10 years

**245** via NC int. for  $\chi$  signal  
 $(\nu_{\text{atm}} + N \rightarrow \nu_{\text{atm}} + N)$

**510** via CC int. for  $\nu$  signal  
 $(\nu_{\text{atm}} + N \rightarrow e/\mu + j)$

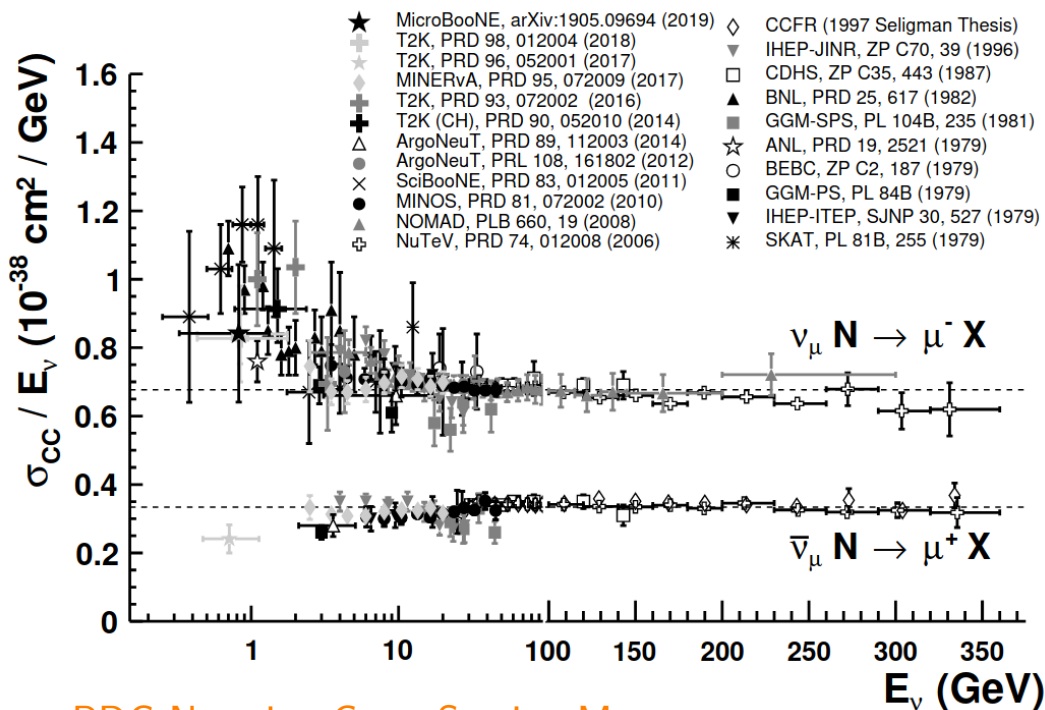
<http://www-rccn.icrr.u-tokyo.ac.jp/mhonda/public/>

■ We use  $\nu_{\text{atm}}$  HAKKM flux at Homestake (close to DUNE detector).

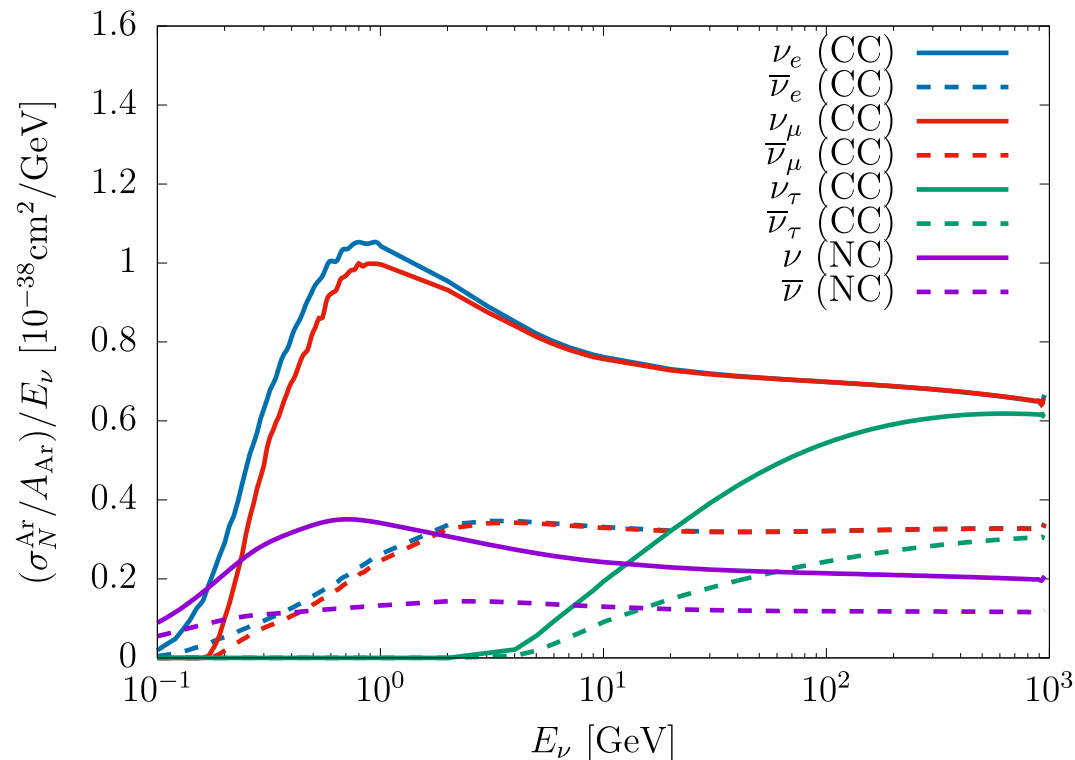


# Neutrino cross section

## ■ Default implementation in GENIE



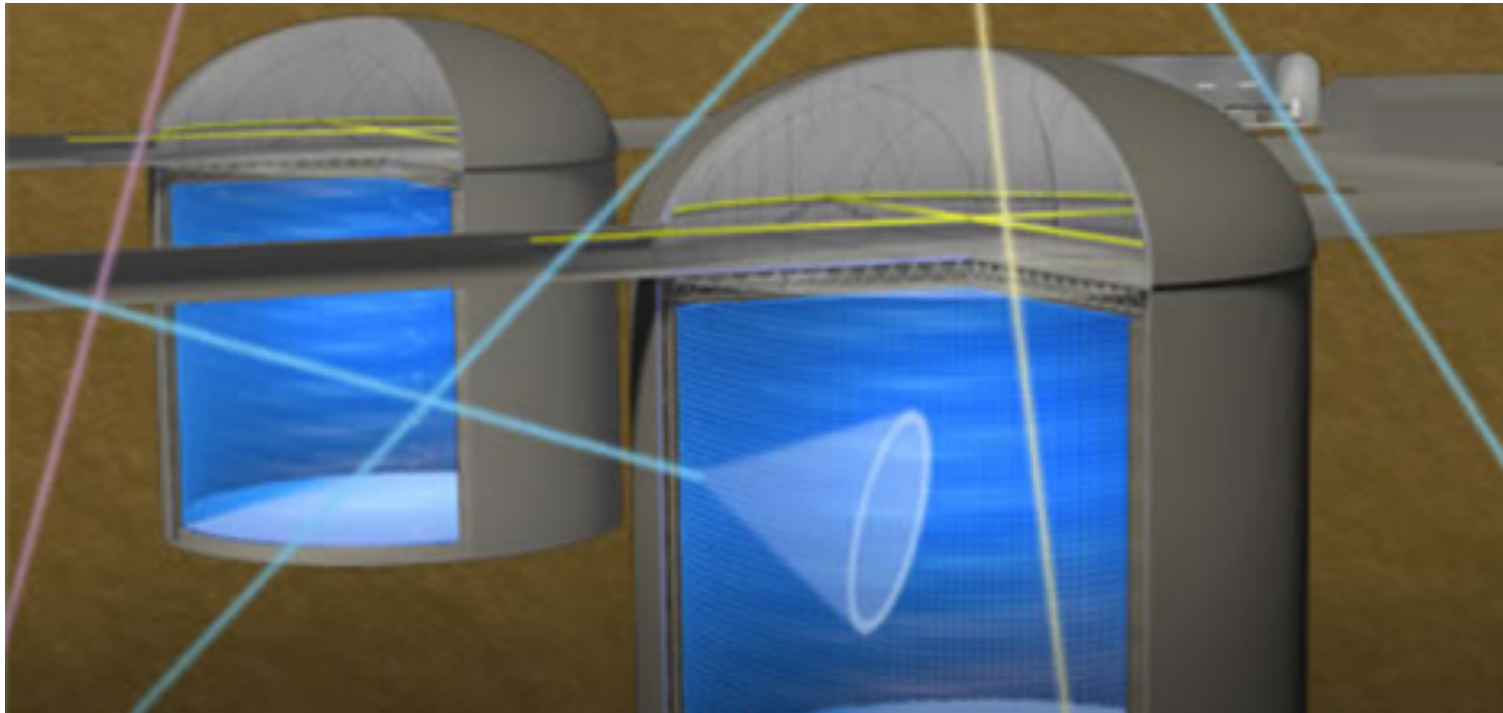
PDG Neutrino Cross Section Measurements



■ In the energy range from MeV to  $\mathcal{O}(100)$  GeV, many physical processes (non-perturbative QCD, nuclear models, hadronization etc) are important.

# Accompanied neutrinos

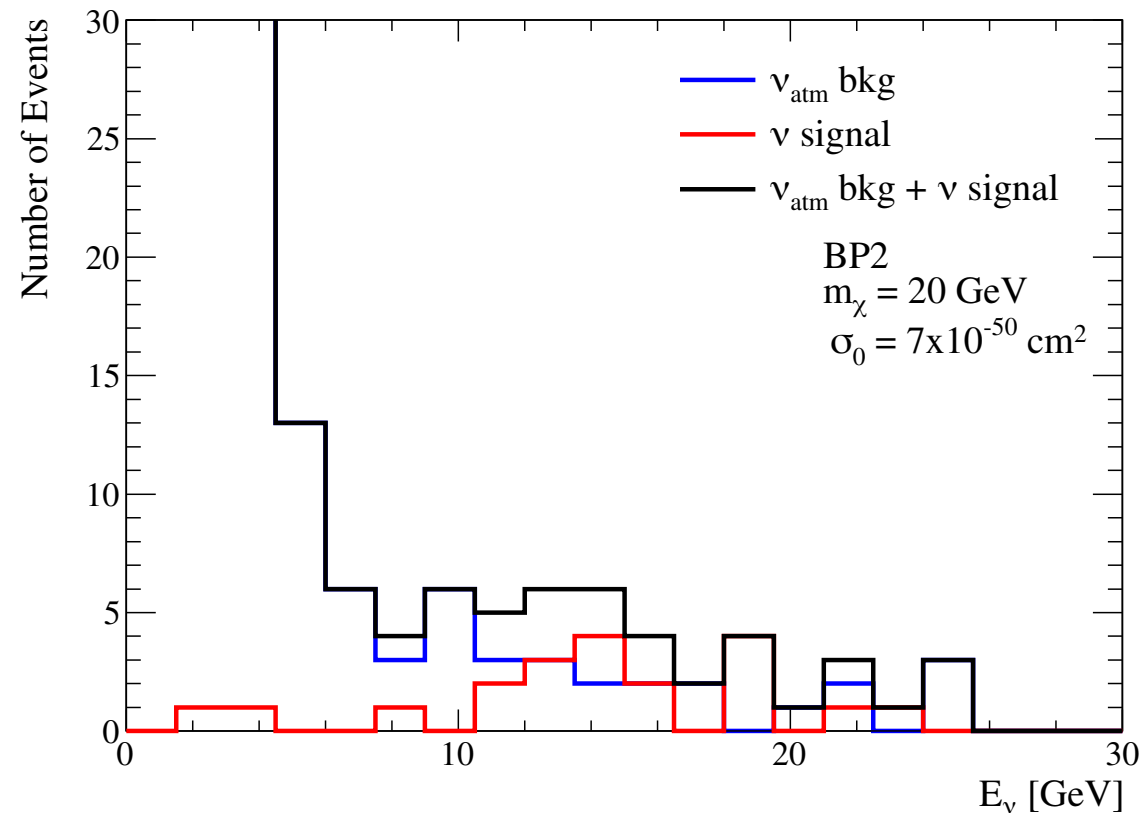
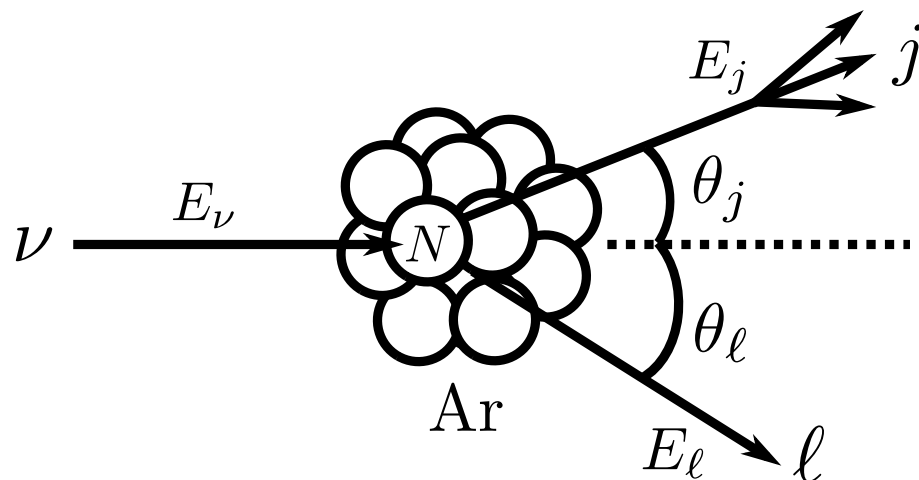
- Accompanied neutrinos can also be searched by DUNE, SK/HK and IceCube etc.



Hyper-Kamiokande Collaboration

- The boosted DM ( $v_\chi = 0.6$ ) is difficult to produce Cherenkov light.  
 $v_p > 0.75$  is required to produce Cherenkov radiation.

# Neutrino energy reconstruction arXiv: 1903.04175, C. Rott et al.



- $\nu + N \rightarrow e^-/\mu^- + \text{jet}$

- $$E_\nu = \frac{1 \sin \theta_j (1 + \cos \theta_\ell) + \sin \theta_\ell (1 + \cos \theta_j)}{2 \sin \theta_j} E_\ell$$

- Benchmark point:  $n = 2$ ,  $m_\chi = 20 \text{ GeV}$ ,  $\sigma_0 = 7 \times 10^{-50} \text{ cm}^2$

# Results

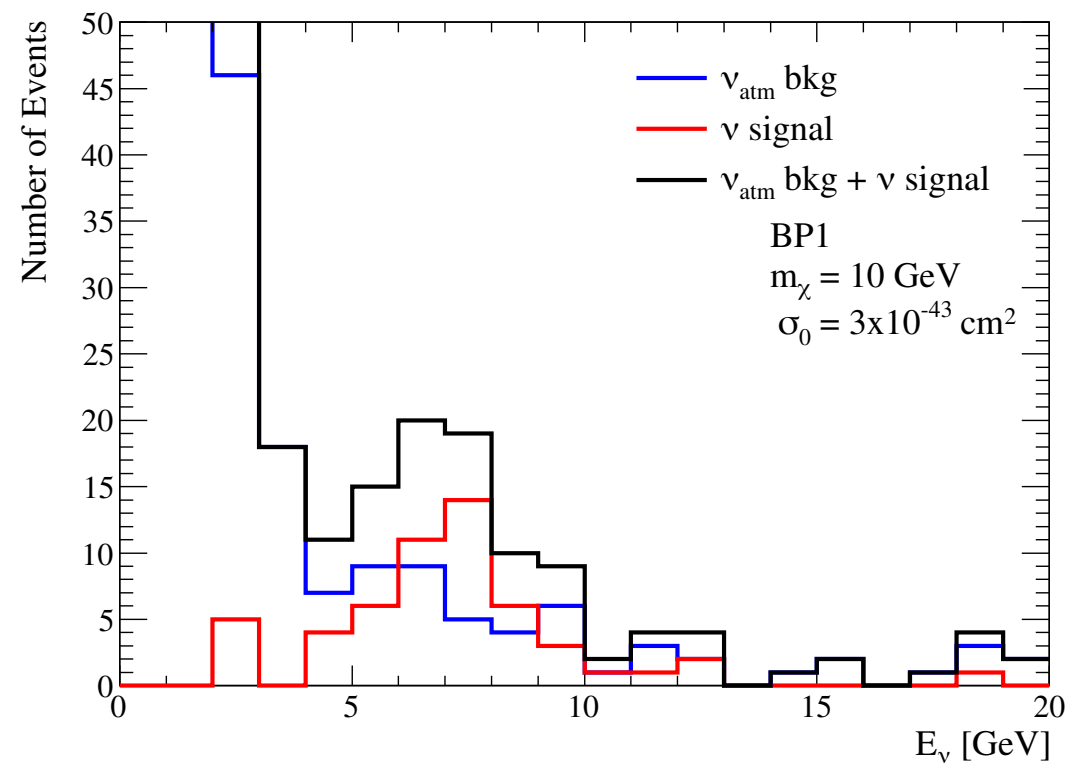
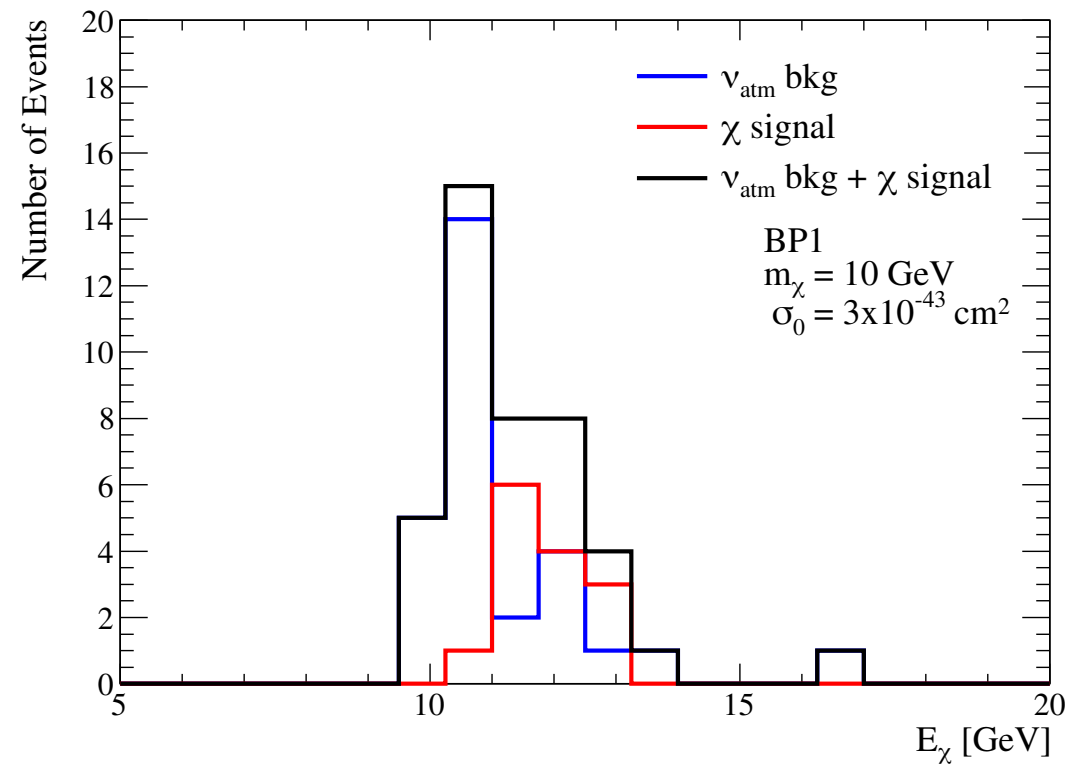
# Results

## Benchmark parameter sets

	model	$m_\chi$ [GeV]	$\sigma_0$ [cm <sup>2</sup> ]	# of $\nu$ events	# of $\chi$ events
BP1	SD ( $n = 1$ )	10	$3.0 \times 10^{-43}$	$N_{\text{atm}\nu}^{\text{CC}} = 510/510$ $N_\nu^{\text{CC}} = 56/56$	$N_{\text{atm}\nu}^{\text{NC}} = 35/245$ $N_\chi = 14/40$
BP2	SI ( $n = 2$ )	20	$7.0 \times 10^{-50}$	$N_{\text{atm}\nu}^{\text{CC}} = 510/510$ $N_\nu^{\text{CC}} = 20/20$	$N_{\text{atm}\nu}^{\text{NC}} = 46/245$ $N_\chi = 774/2396$

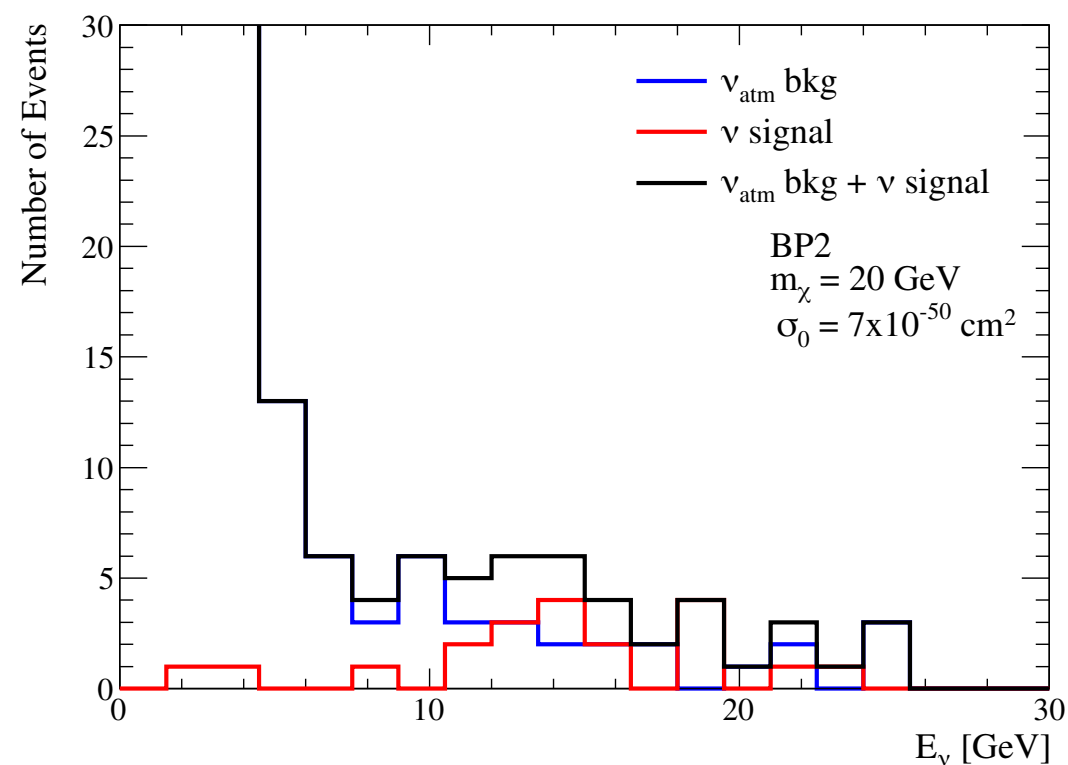
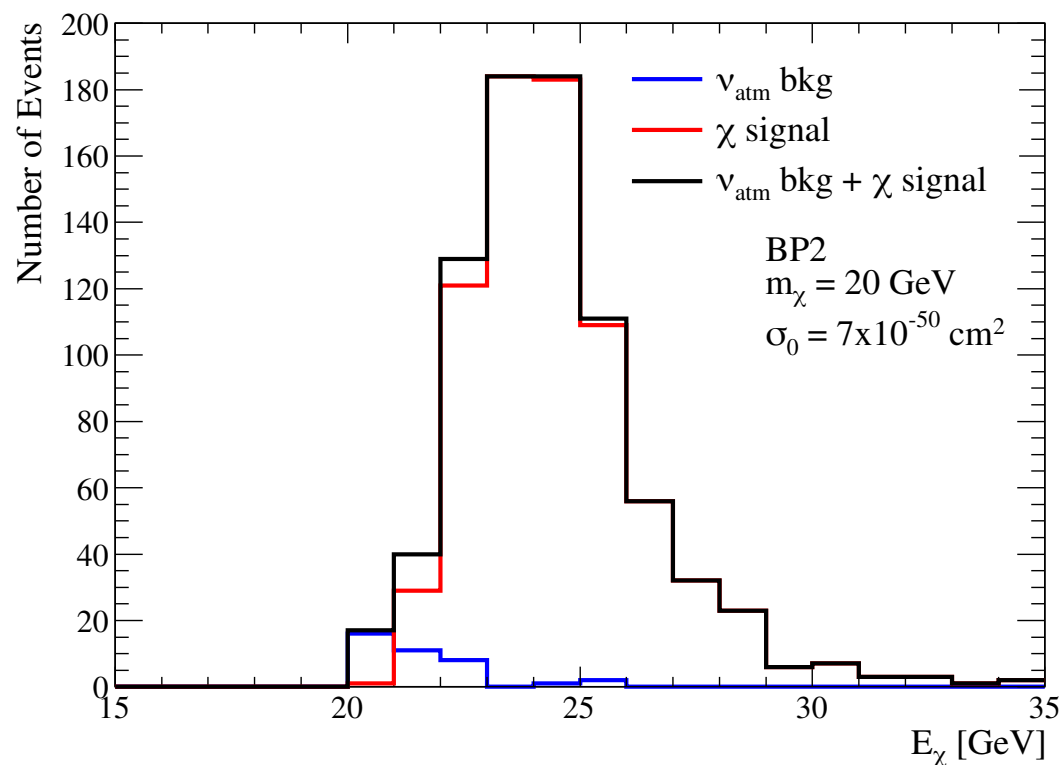
- Assumption: 40kton liquid argon, 10 years exposure
- 4th and 5th columns: Observed events / Expected events (detector threshold and resolutions)
- A large number of BDM signal events for BP2

# Energy distribution 1



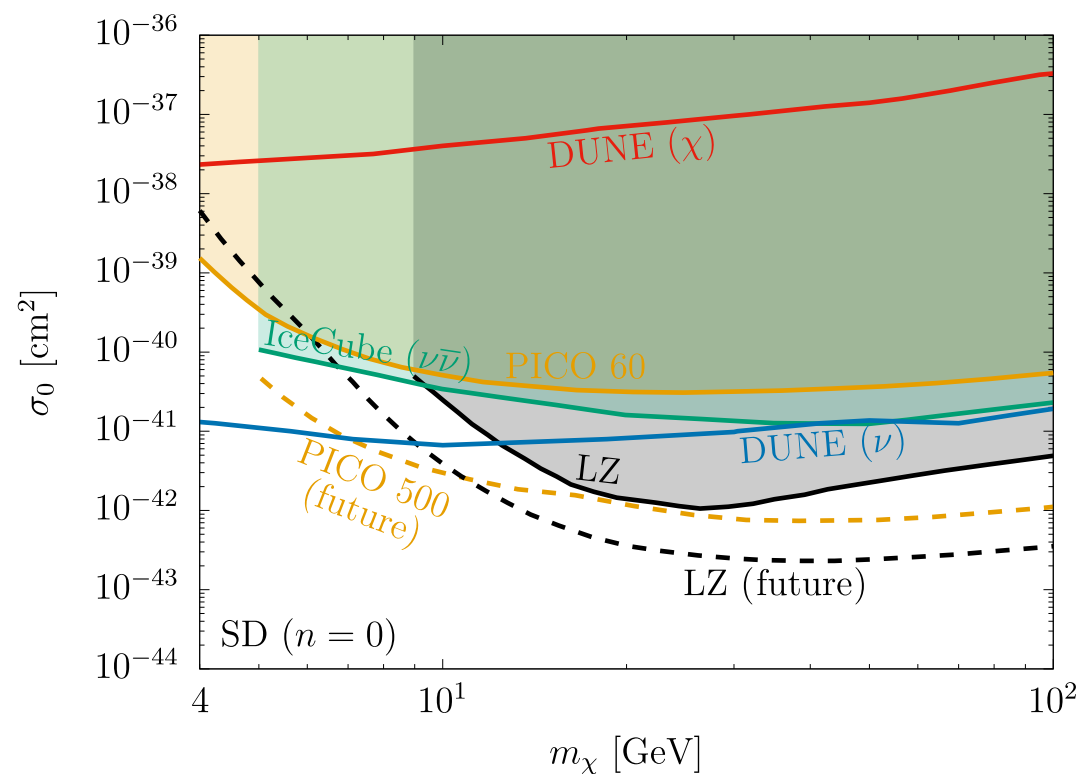
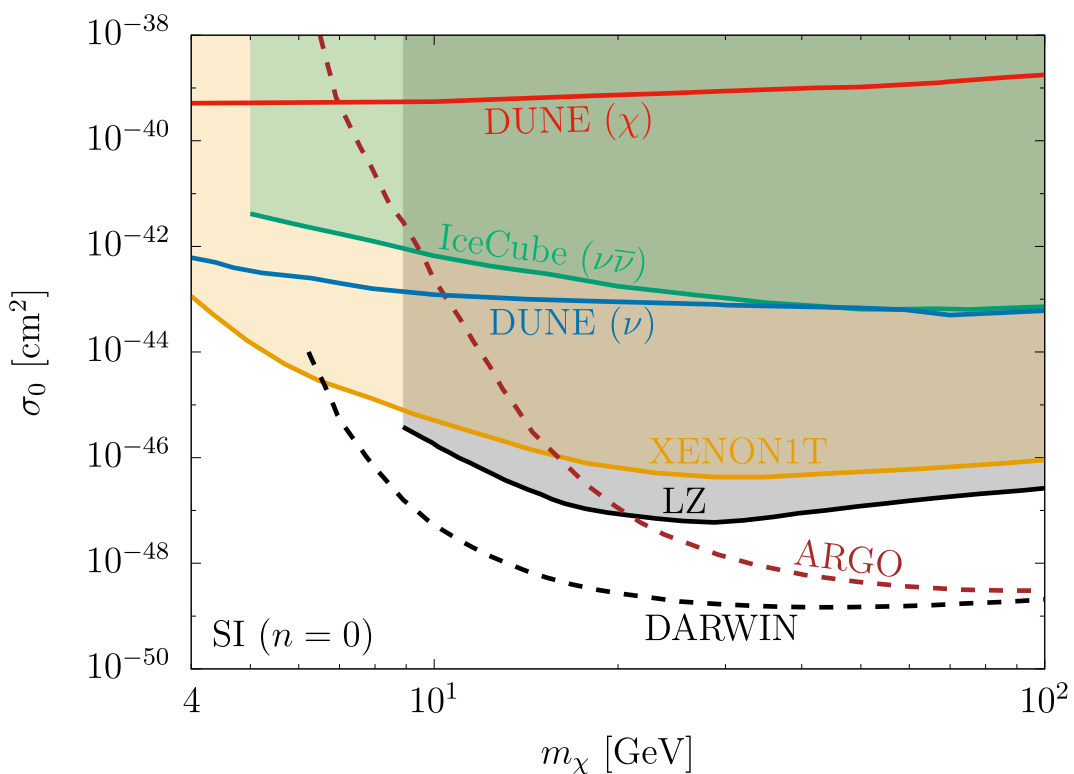
- Energy reconstruction for BP1
- Atmospheric neutrino bkg at low energy

# Energy distribution 2



- Energy reconstruction for BP2
- Atmospheric neutrino bkg at low energy
- A large number of BDM events on the left plot

# Parameter space 1



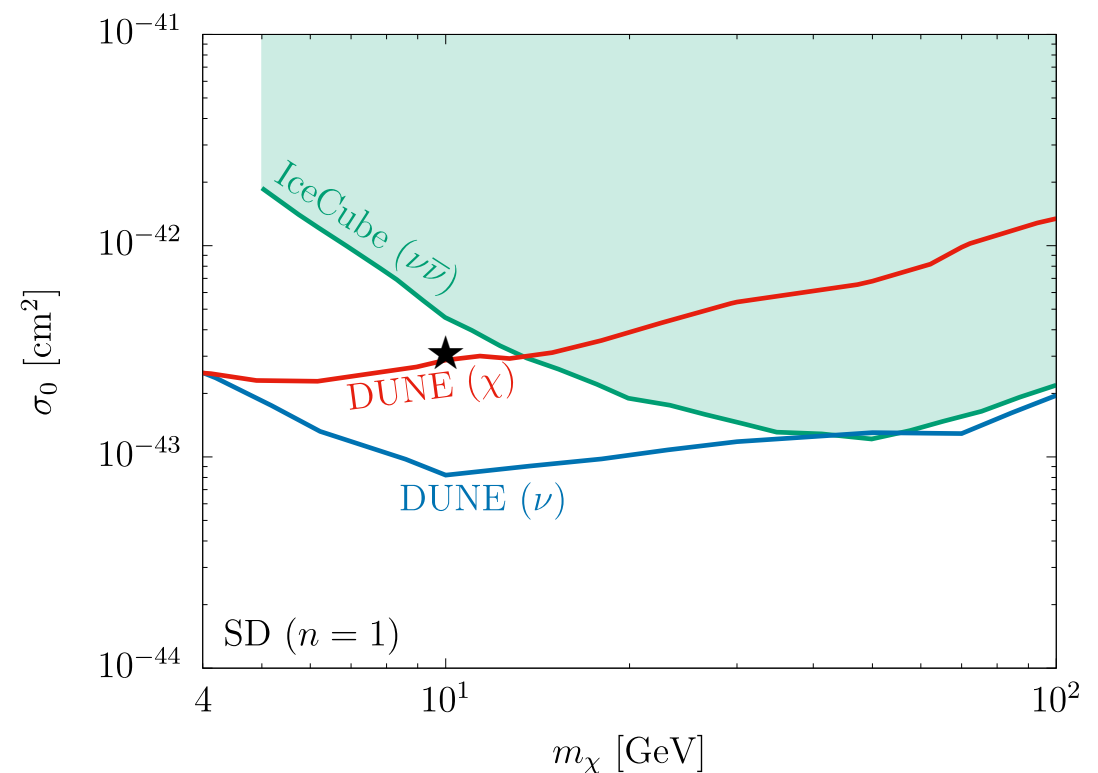
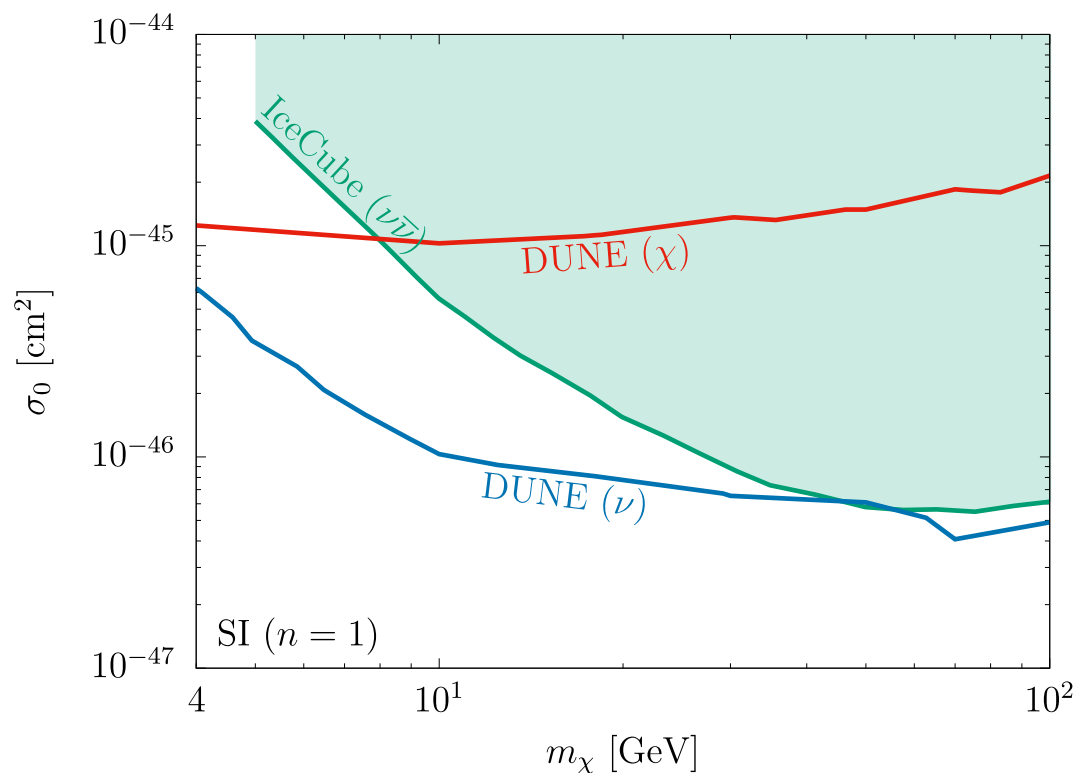
- DUNE sensitivity for constant  $\sigma_{\chi N}$  ( $n = 0$ )

- Significance: 
$$\mathcal{S} = \frac{N_{\text{sig}}}{\sqrt{N_{\text{bkg}} + N_{\text{sig}}}}$$

- Completely excluded by direct detection experiments **as expected**.

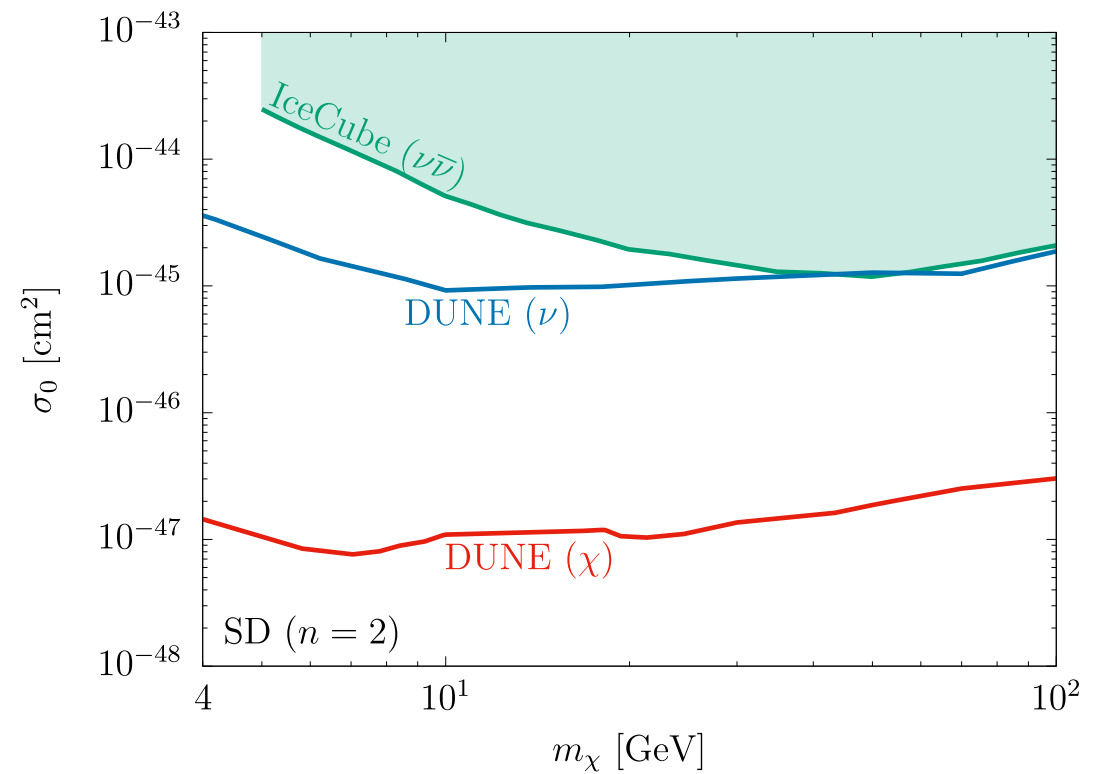
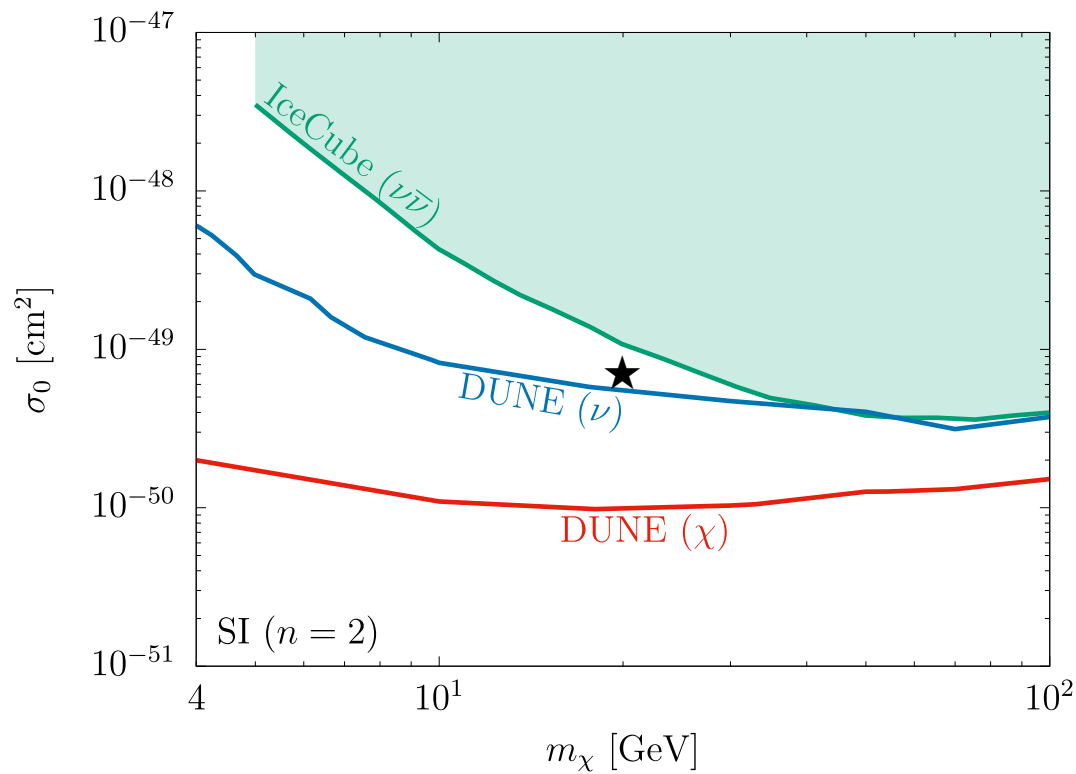


# Parameter space 2



- DUNE sensitivity for  $Q^2$  dependent  $\sigma_{\chi N}$  ( $n = 1$ )
- No substantial direct detection constraints.
- Sensitivities can be comparable if DM mass is lower.

# Parameter space 3



- DUNE sensitivity for  $Q^4$  dependent  $\sigma_{\chi N}$  ( $n = 2$ )
- Sensitivity for BDM can be much higher.

# Summary

- 1 Direct detection experiments impose the strong bound on (minimal) thermal dark matter scenarios.
- 2 Non-minimal extension of dark sector may induce semi-annihilations.
- 3  $\chi\chi \rightarrow \bar{\chi}\nu$  induces distinctive signals, which can be searched by DUNE, but not by SK/HK and IceCube.
- 4  $Q^2$  (or  $v_\chi^2$ ) suppressed cross sections are needed for BDM detection.

# Future works

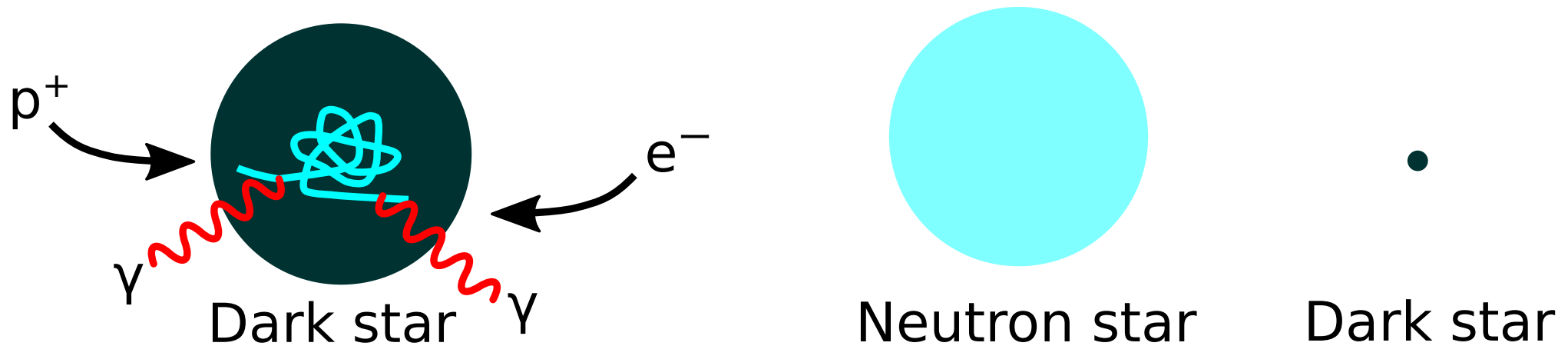
- 1 Concrete model building
- 2 Application to multi-component DM,  $3 \rightarrow 2$  or  $4 \rightarrow 2$  processes  
Dark matter particles are boosted:  $E_\chi = \frac{3}{2}m_\chi$ , or  $2m_\chi$

# Future works 2

- Consider very dense compact object (dark star)

B. Kamenetskaia, A. Brenner, A. Ibarra and C. Kouvaris, arXiv:2211.05845

⇒ enhancement of point source of boosted dark matter



cf: neutron stars:  $M \sim M_{\odot}$ ,  $r \sim 20\text{km}$

$M \sim 0.1M_{\odot}$ ,  $r \sim 1\text{km}$

- This can be signal of boosted dark matter from  $3 \rightarrow 2$  or  $4 \rightarrow 2$  processes, or maybe from semi-ann. too.

# Backup

# Semi-annihilation at the Sun

- Number of DM particles accumulated in the Sun

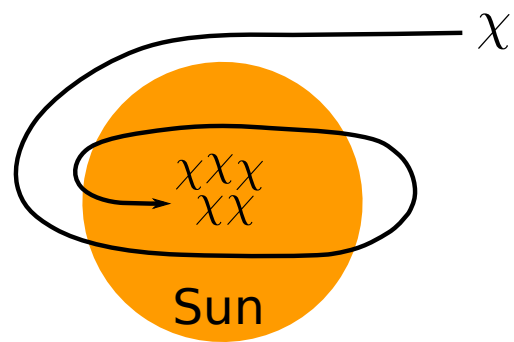
$$\frac{dN_\chi}{dt} = \Gamma_{\text{capt}} - 2\Gamma_{\text{ann}} - \Gamma_{\text{evap}}$$

- Capture rate

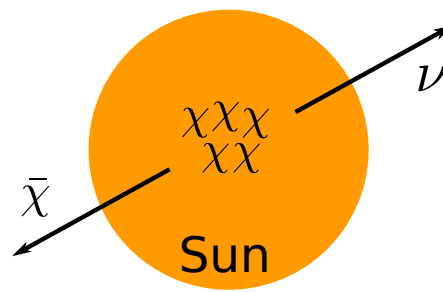
$$\Gamma_{\text{capt}} = \frac{\rho_\odot}{m_\chi} \sum_i \sigma_i \int_0^{R_\odot} dr 4\pi r^2 n_i(r) \int_0^\infty dv 4\pi v^2 f_\odot(v) \frac{v^2 + v_{\text{esc}}^2}{v} P(v, v_{\text{esc}})$$

where  $i =$  all the elements in the Sun

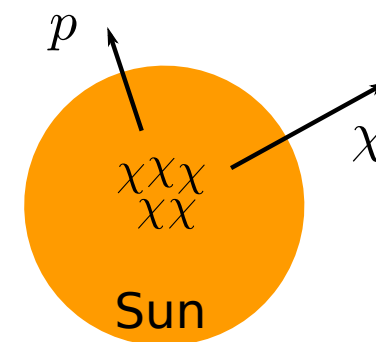
For  $m_\chi \gg m_i$ ,  $\Gamma_{\text{capt}} \approx \frac{\rho_\odot}{m_\chi^2} 4\pi f_\odot(0) \sum_i m_i \sigma_i I_i \quad \left( I_i \sim \int_0^{R_\odot} dr 4\pi r^2 n_i(r) v_{\text{esc}}^4 \right)$



Capture



Annihilation



Evaporation

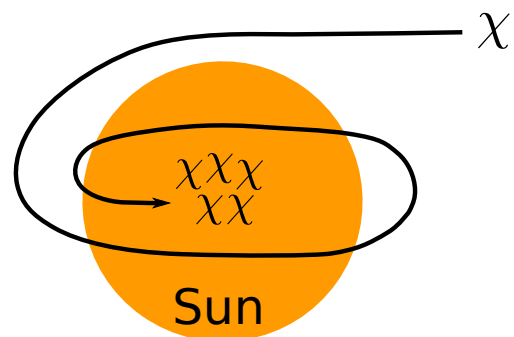
# Semi-annihilation at the Sun

- Number of DM particles accumulated in the Sun

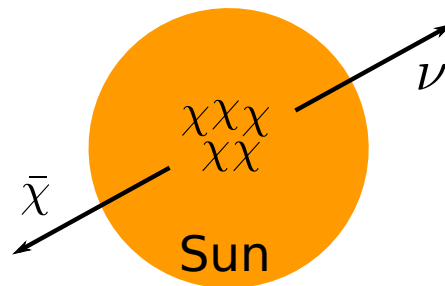
$$\frac{dN_\chi}{dt} = \Gamma_{\text{capt}} - 2\Gamma_{\text{ann}} - \Gamma_{\text{evap}}$$

- Annihilation rate:  $\Gamma_{\text{ann}} = \frac{C_{\text{ann}}}{2} N_\chi^2$

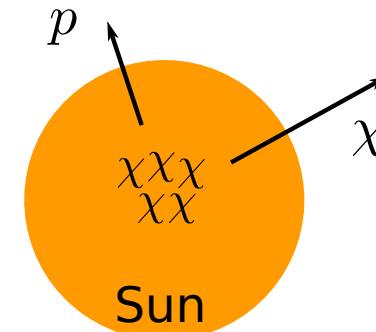
where  $C_{\text{ann}} = \left( \frac{\langle \sigma_{\chi\chi} v \rangle}{10^{-9} \text{ GeV}^{-2}} \right) \left( \frac{m_\chi}{100 \text{ GeV}} \right)^{3/2} 1.7 \times 10^{-54} \text{ s}^{-1}$



Capture



Annihilation



Evaporation

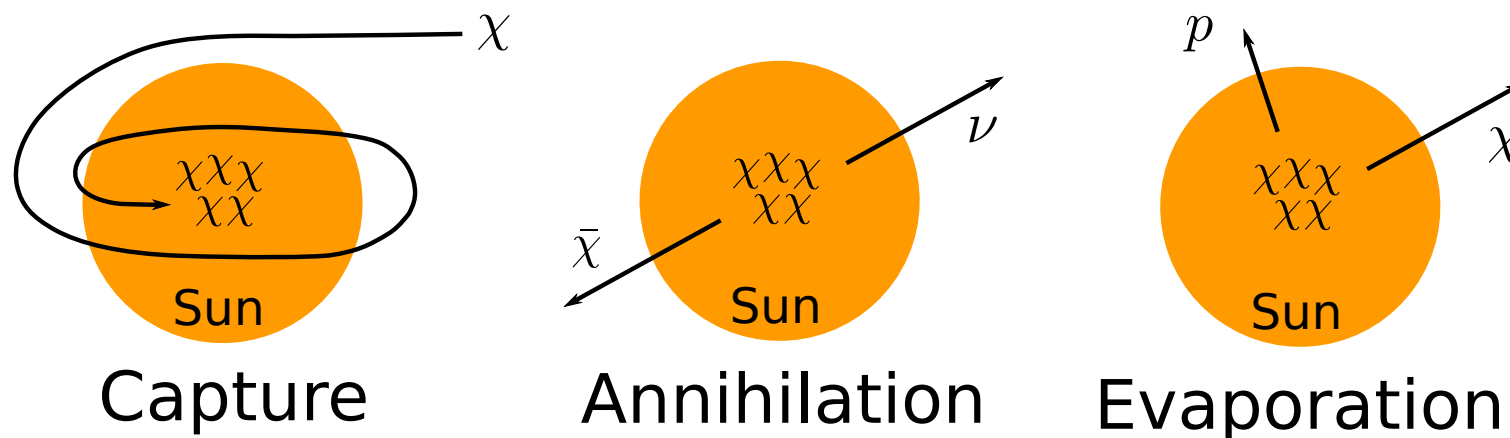
# Semi-annihilation at the Sun

- Evaporation rate: Some DM particles scatter with nuclei in the Sun and get enough energy to escape from the Sun.
- Neglecting  $\Gamma_{\text{evap}}$  ( $m_\chi \gtrsim 4 \text{ GeV}$ ), the solution is

$$\Gamma_{\text{ann}} = \frac{\Gamma_{\text{capt}}}{2} \tanh^2 \left( \frac{t}{\tau} \right) \xrightarrow{t \gg \tau} \frac{\Gamma_{\text{capt}}}{2}$$

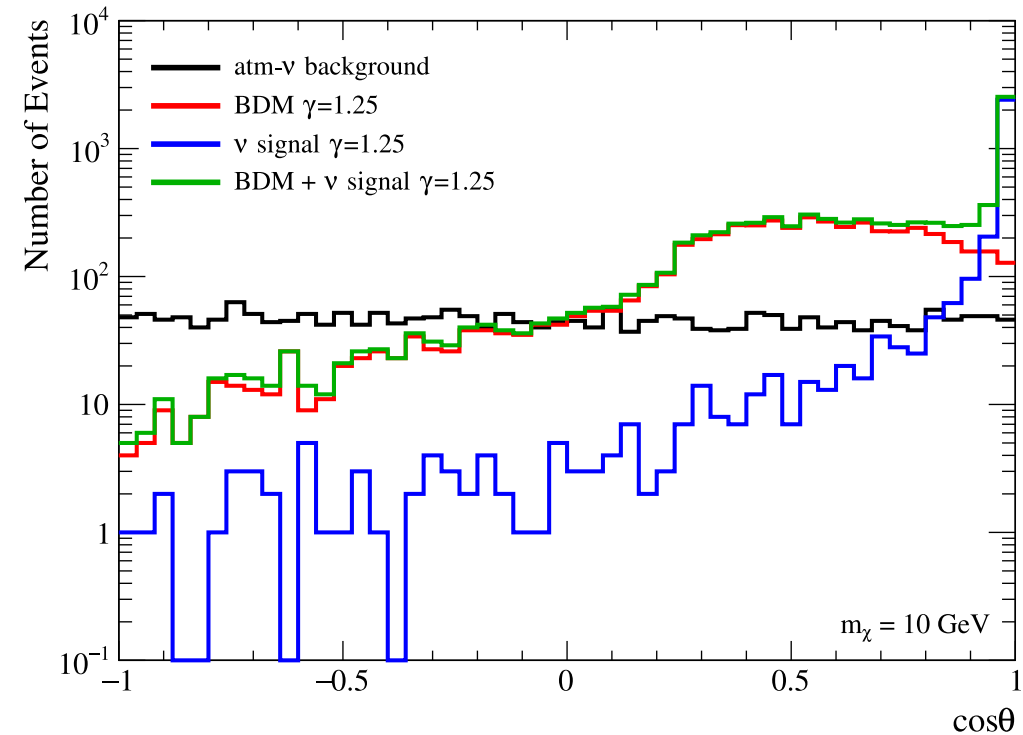
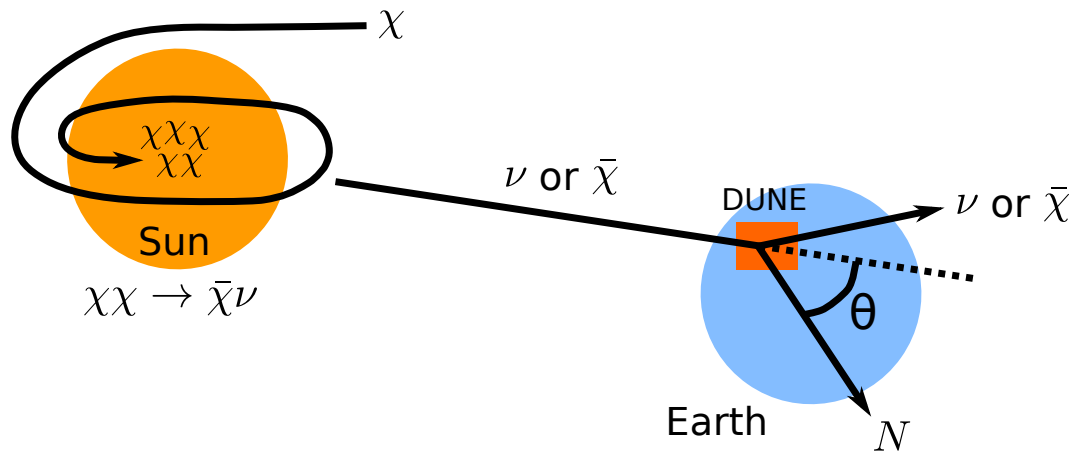
where  $\tau = (\Gamma_{\text{capt}} C_{\text{ann}})^{-1/2}$ , Age of the Sun  $t \sim 4.5 \text{ Gyr}$

- Equilibrium can easily be reached.





# Angular distribution



- Atmospheric neutrinos (black line) are uniform.
- Easy to distinguish the signals and  $\nu_{\text{atm}}$  background.
- But we need to distinguish two signals.