Probing BSM effects through gravitational wave observations

Katsuya Hashino (KOSEN/Fukushima Coll.)

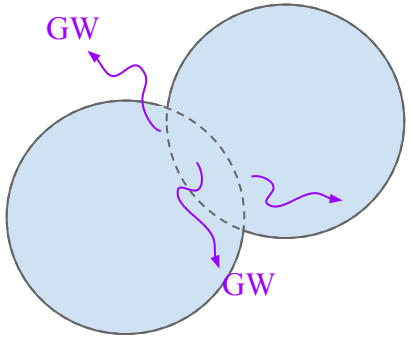
Collaborators: Daiki Ueda (Technion)

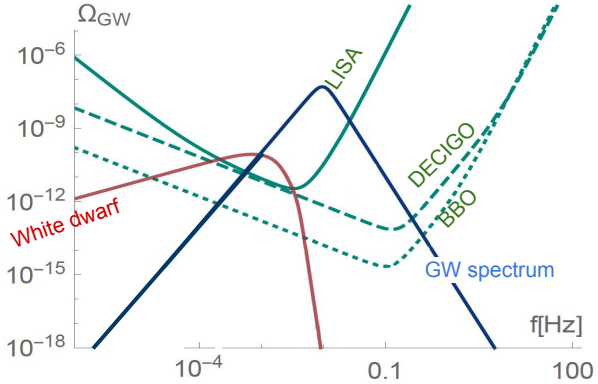
[K. H., Daiki Ueda, Phys.Rev.D 107 (2023) 9, 095022]
[K. H., Daiki Ueda, arXiv: 2505.13074]

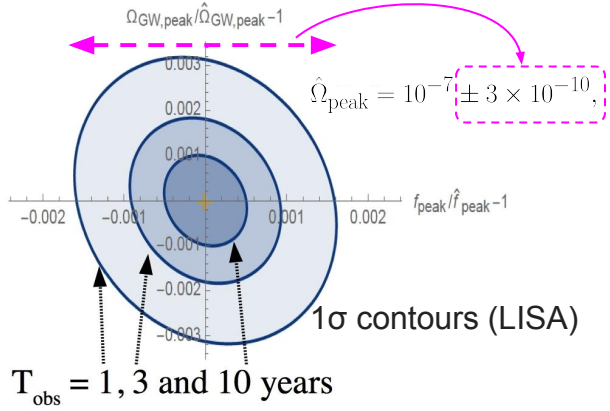
Introduction

★ The gravitational waves (GWs) are produced by the first-order phase transition (FOPT).

GW observations can be used to explore the new physics (NP) effects for the first-order phase transition.







We can quantitatively discuss how precisely obtain the NP parameter at the GW observation by the Fisher matrix analysis.

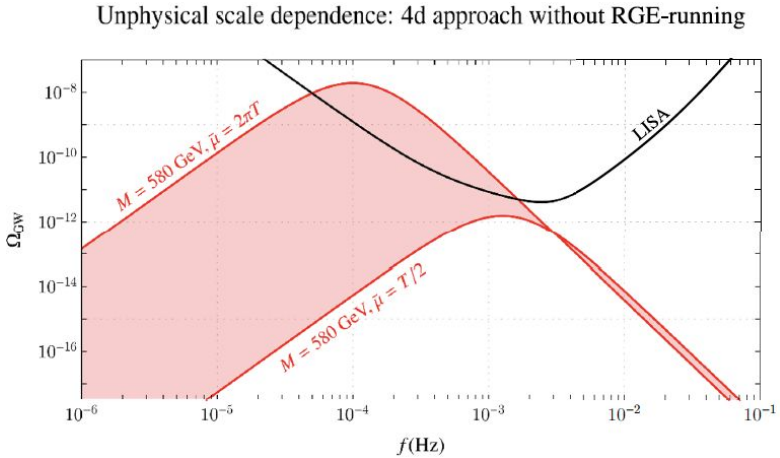
We can evaluate the width of confidence interval of the NP effects by GW observation.

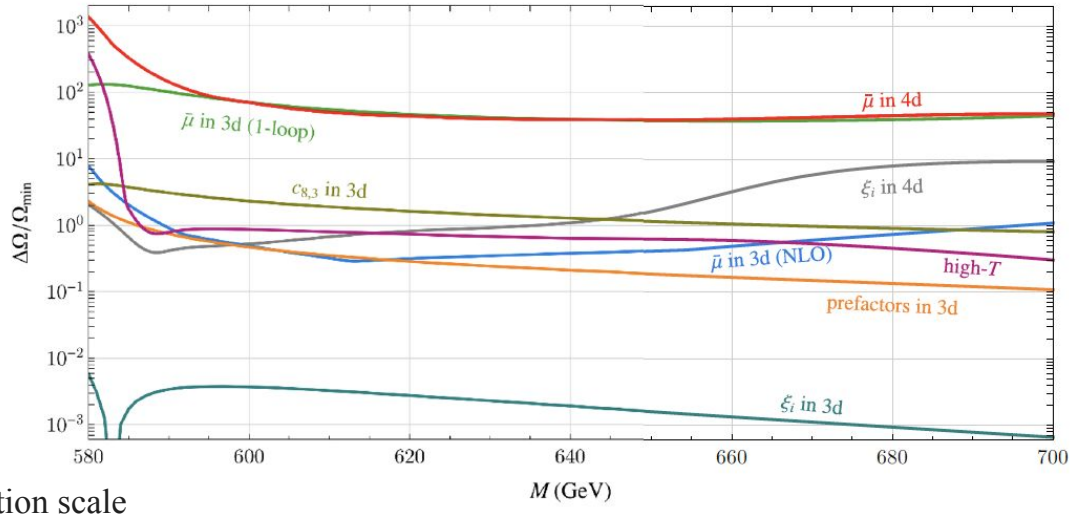
Theoretical uncertainties

★ However, the GW spectra have some theoretical uncertainties...

[D. Croon, O. Gould, P. Schicho, T. V. I. Tenkanen and G. White, JHEP 04 (2021), 055]

$\Delta\Omega_{\rm GW}/\Omega_{\rm GW}$	4d approach	3d approach
RG scale dependence	$\mathcal{O}(10^2 - 10^3)$	$\mathcal{O}(10^0 - 10^1)$
Gauge dependence	$\mathcal{O}(10^1)$	$\mathcal{O}(10^{-3})$
High-T approximation	$\mathcal{O}(10^{-1} - 10^0)$	$\mathcal{O}(10^0 - 10^2)$
Higher loop orders	unknown	$\mathcal{O}(10^0 - 10^1)$
Nucleation corrections	unknown	$\mathcal{O}(10^{-1} - 10^0)$
Nonperturbative corrections	unknown	unknown





$$V_{\rm tree}(\phi) = \mu_h^2\,\phi^\dagger\phi + \lambda\,(\phi^\dagger\phi)^2 + \frac{1}{M^2}(\phi^\dagger\phi)^3$$

$\bar{\mu}$: Renormalization scale

The uncertainties have been highlighted using the Standard Model Effective Field Theory (SMEFT) as a benchmark.

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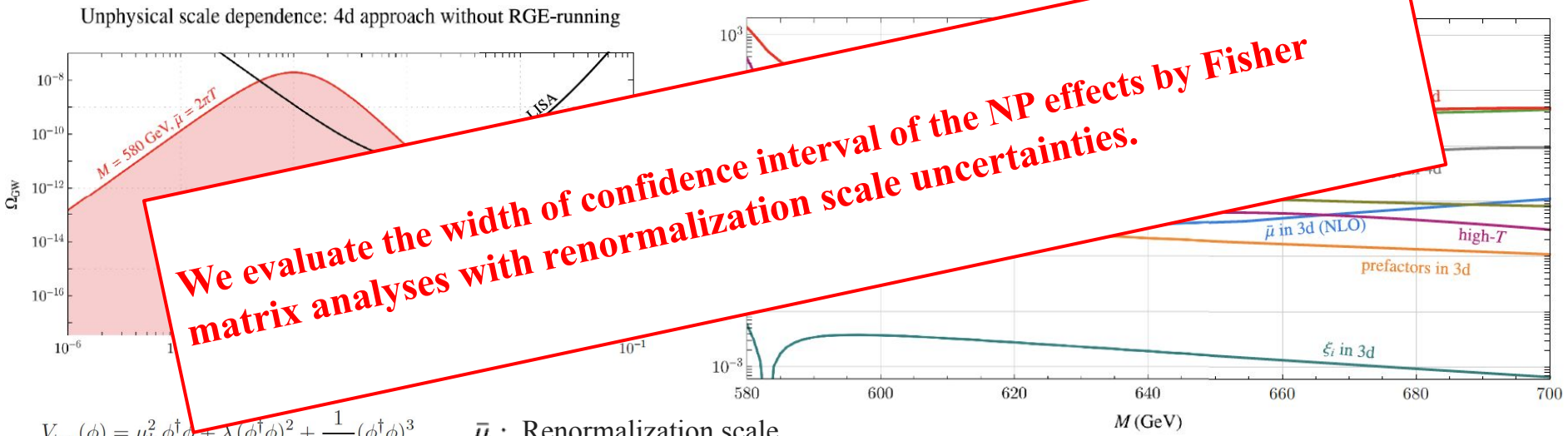


We evaluate the width of confidence interval of the NP effects by Fisher matrix analyses with renormalization scale uncertainties.

$$V_{\rm tree}(\phi) = \mu_h^2\,\phi^\dagger\phi + \lambda(\phi^\dagger\phi)^2 + \frac{1}{M^2}(\phi^\dagger\phi)^3$$

$\bar{\mu}$: Renormalization scale

The uncertainties have been highlighted using the Standard Model Effective Field Theory (SMEFT) as a benchmark.

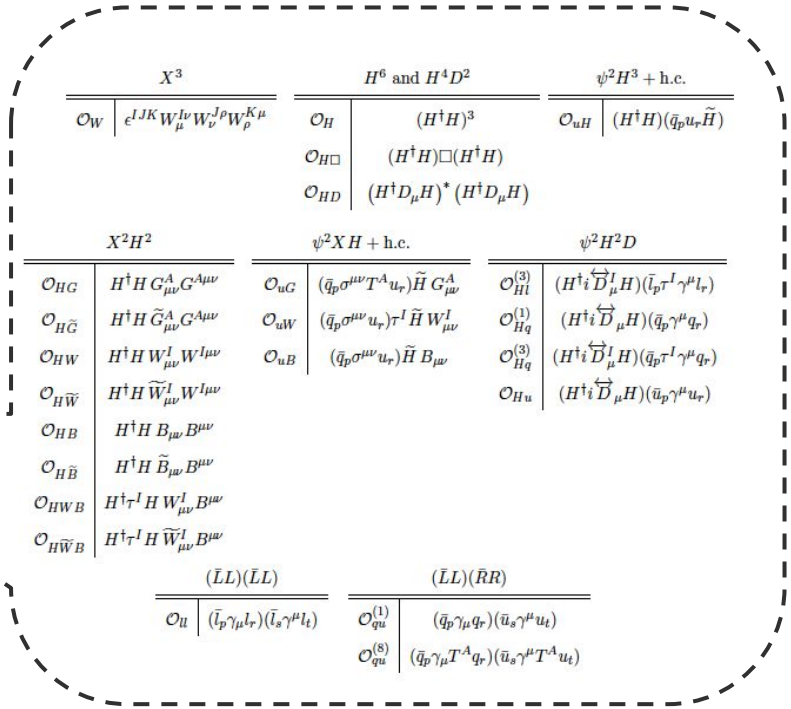
Benchmark model (SMEFT)

SMEFT

- The first-order phase transition
- Theoretical uncertainties

We adopt the SMEFT as a benchmark.

$$\mathcal{L}_{\rm SMEFT} = \mathcal{L}_{\rm SM} + \sum_i C_i \mathcal{O}_i$$



X^3

$\mathcal{O}_W$	$\epsilon^{IJK} W_\mu^{Iv} W_\nu^{J\rho} W_\rho^{K\mu}$

H^6 and H^4D^2

$\mathcal{O}_H$	$(H^\dagger H)^3$
$\mathcal{O}_{H\Box}$	$(H^\dagger H)\Box(H^\dagger H)$
$\mathcal{O}_{HD}$	$(H^\dagger D_\mu H)^*(H^\dagger D_\mu H)$

$\psi^2 H^3 + \text{h.c.}$

$\mathcal{O}_{uH}$	$(H^\dagger H)(\bar{q}_p u_r \tilde{H})$

X^2H^2

$\mathcal{O}_{HG}$	$H^\dagger H\, G^A_{\mu\nu} G^{A\mu\nu}$
$\mathcal{O}_{H\tilde{G}}$	$H^\dagger H\, \tilde{G}^A_{\mu\nu} G^{A\mu\nu}$
$\mathcal{O}_{HW}$	$H^\dagger H\, W^I_{\mu\nu} W^{I\mu\nu}$
$\mathcal{O}_{H\widetilde{W}}$	$H^\dagger H\, \widetilde{W}^I_{\mu\nu} W^{I\mu\nu}$
$\mathcal{O}_{HB}$	$H^\dagger H\, B_{\mu\nu} B^{\mu\nu}$
$\mathcal{O}_{H\tilde{B}}$	$H^\dagger H\, \tilde{B}_{\mu\nu} B^{\mu\nu}$
$\mathcal{O}_{HWB}$	$H^\dagger \tau^I H\, W^I_{\mu\nu} B^{\mu\nu}$
$\mathcal{O}_{H\widetilde{W}B}$	$H^\dagger \tau^I H\, \widetilde{W}^I_{\mu\nu} B^{\mu\nu}$

$\psi^2 X H + \text{h.c.}$

$\mathcal{O}_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{H}\, G^A_{\mu\nu}$
$\mathcal{O}_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{H}\, W^I_{\mu\nu}$
$\mathcal{O}_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{H}\, B_{\mu\nu}$

$\psi^2 H^2 D$

$\mathcal{O}_{Hl}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}^I_\mu H)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$\mathcal{O}_{Hq}^{(1)}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{q}_p \gamma^\mu q_r)$
$\mathcal{O}_{Hq}^{(3)}$	$(H^\dagger i \overleftrightarrow{D}^I_\mu H)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$\mathcal{O}_{Hu}$	$(H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{u}_p \gamma^\mu u_r)$

$(\bar{L}L)(\bar{L}L)$

$\mathcal{O}_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$

$(\bar{L}L)(\bar{R}R)$

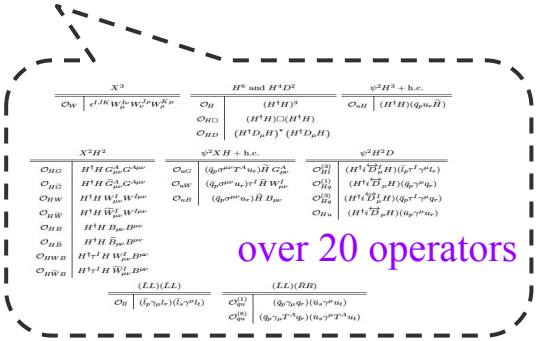
$\mathcal{O}_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
$\mathcal{O}_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$

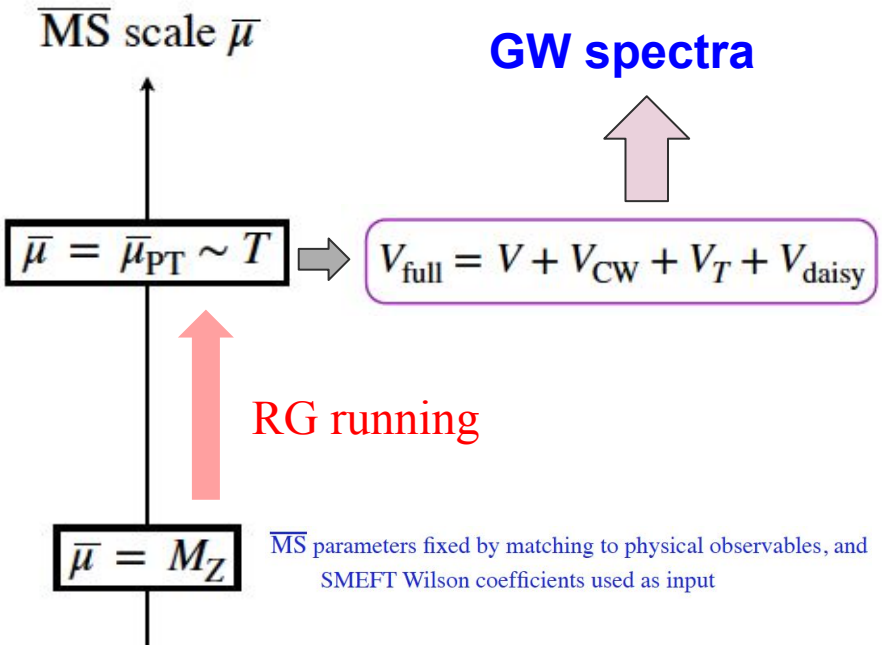
These operators can describe various NP effects in a model-independent manner.

Benchmark model (SMEFT)

★ The GW spectra is evaluated by the effective potential at typical scales of the FOPT.

The vast number of SMEFT operators affect the potential.





★ In this work, we compare the GW spectra predicted by the effective potential at two different renormalization scales:

$$\bar{\mu}_{PT} = 2\pi T_n \text{ and } T_n/2$$

It is the source of first-order PT

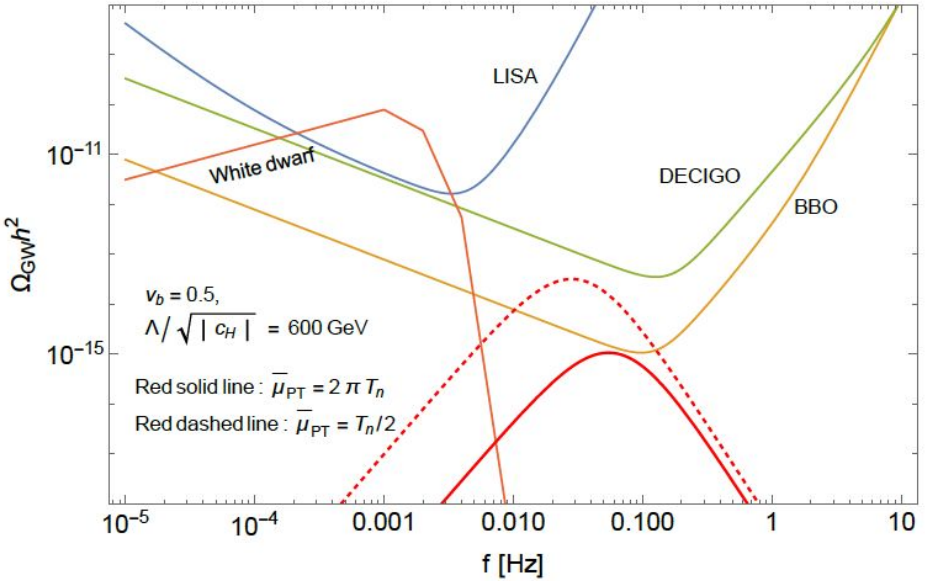
The GW spctra

★ If the value of $|C_H|$ is $1/\Lambda^2 = (600\ \text{GeV})^2$, the GW spectra are given by right figure.

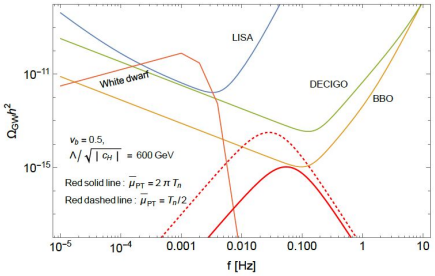
(All others are set to zero)

It is difficult to determine the value of C_H by only an observation of GW spectrum.

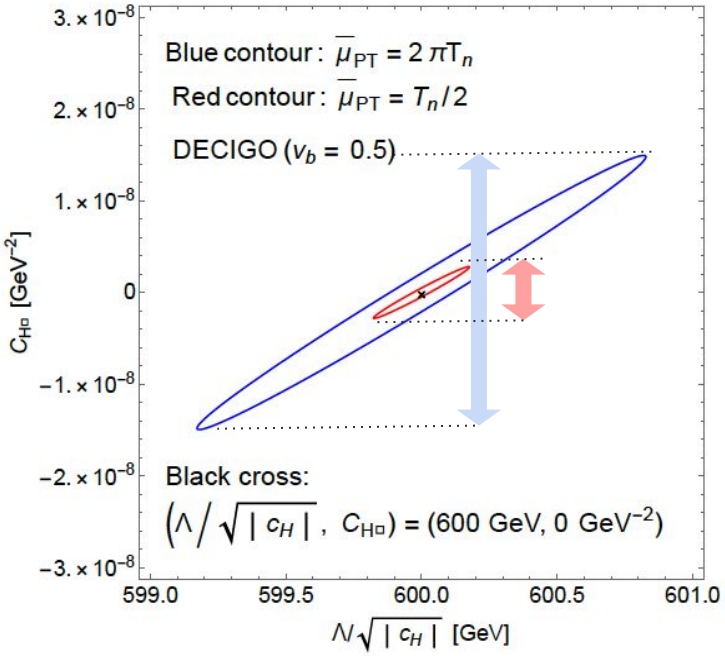
We assume that the value of C_H is determined by other experiments, e.g., collider experiment.

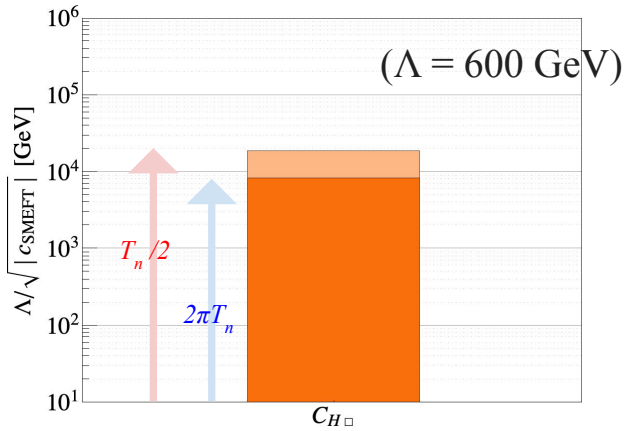


The results



★ $1/\Lambda^2 = (600\ \text{GeV})^2$, $C_{H\Box}$, $v_b = 0.5$, and DECIGO experiment case.

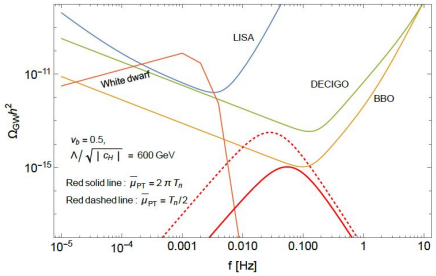




[K. H., Daiki Ueda, arXiv: 2505.13074]

We also performed the analysis for different values of Λ, operators, velocities, and experiments.

The results



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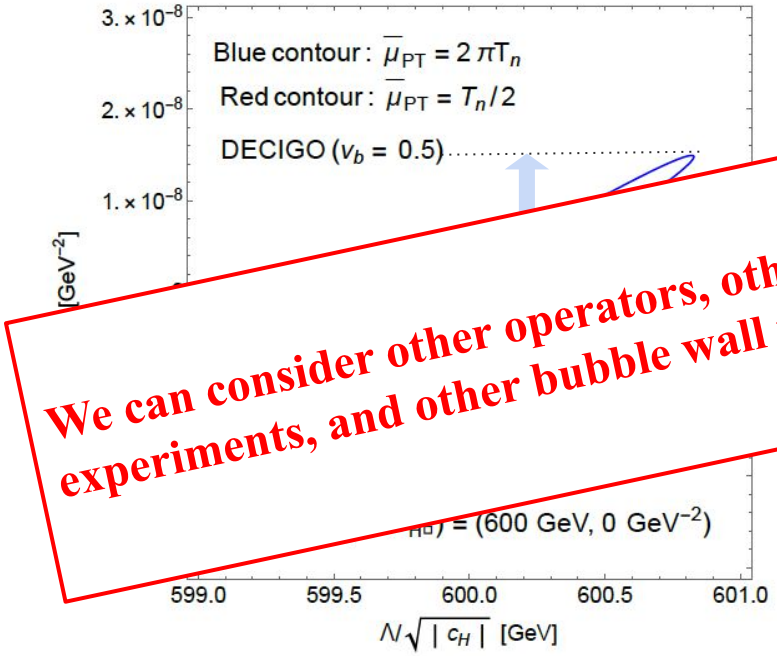
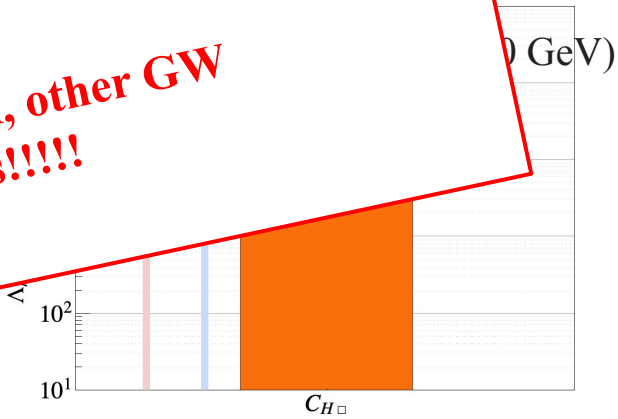


We can consider other operators, other value of Λ, other GW experiments, and other bubble wall velocity cases!!!!!



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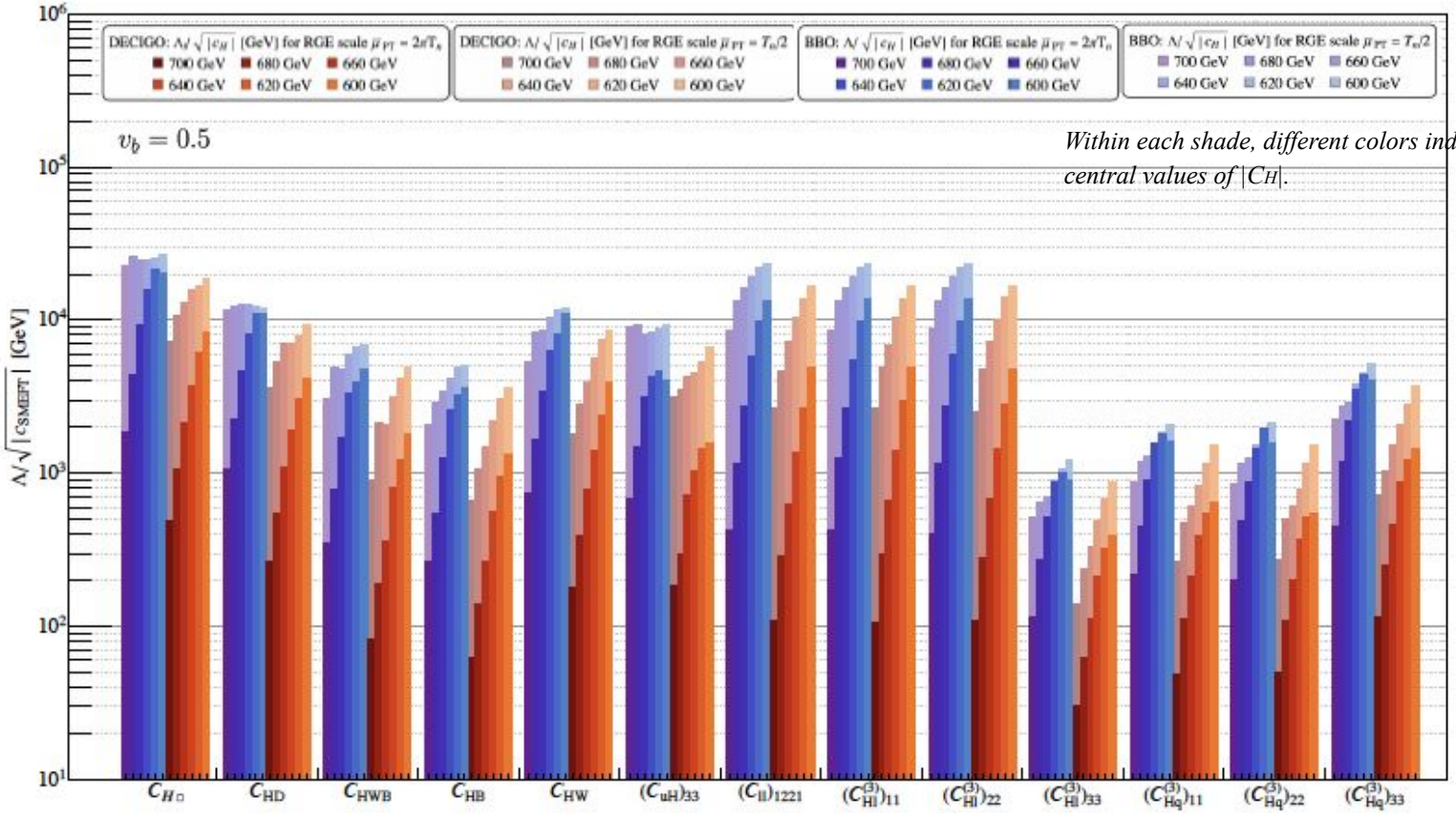
Results

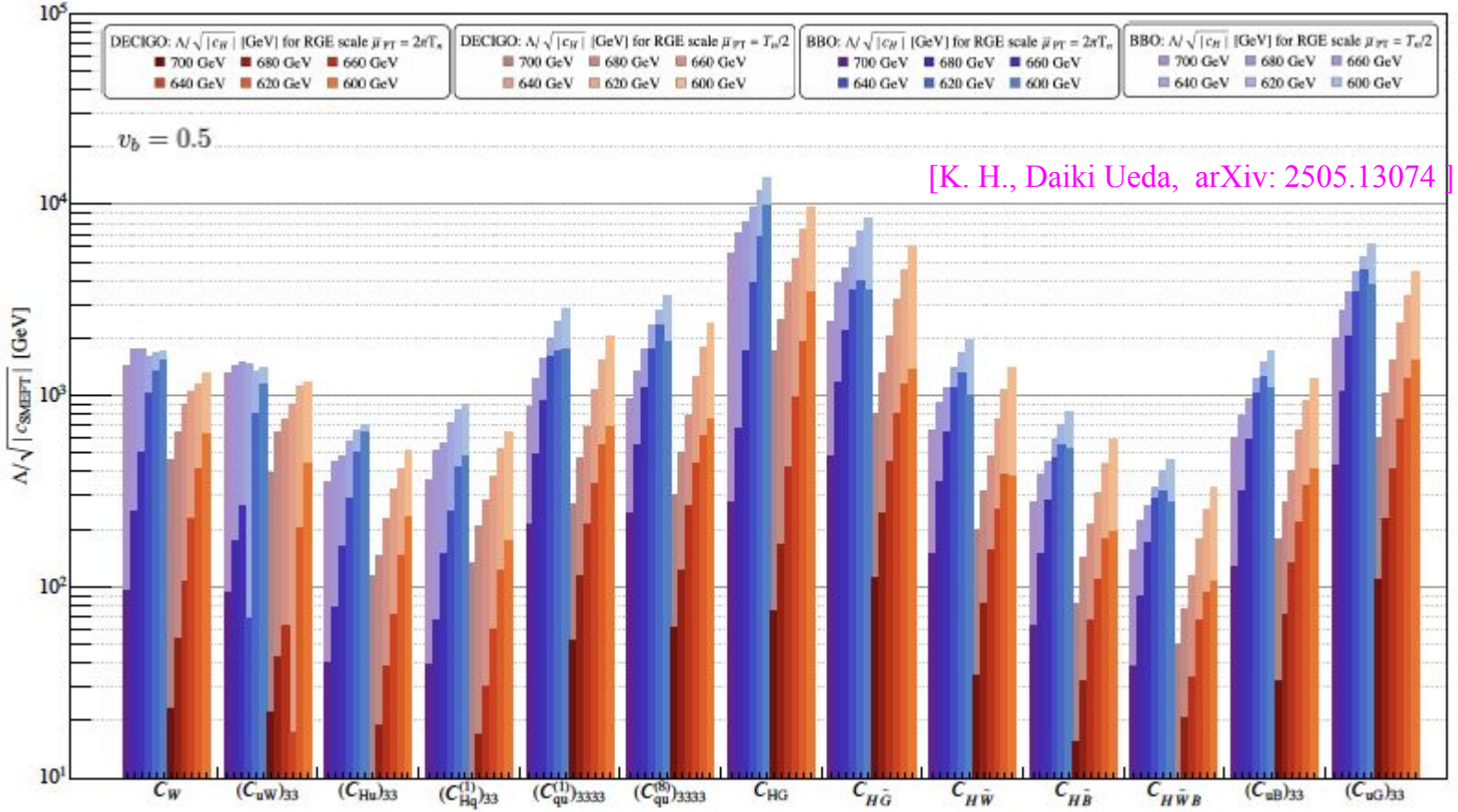
The dark- and light-colored bands represent the choices μPT = 2πTn and Tn/2, respectively,

BBO (bluish bands) and DECIGO (reddish bands)



Within each shade, different colors indicate different central values of |CH|.

Results



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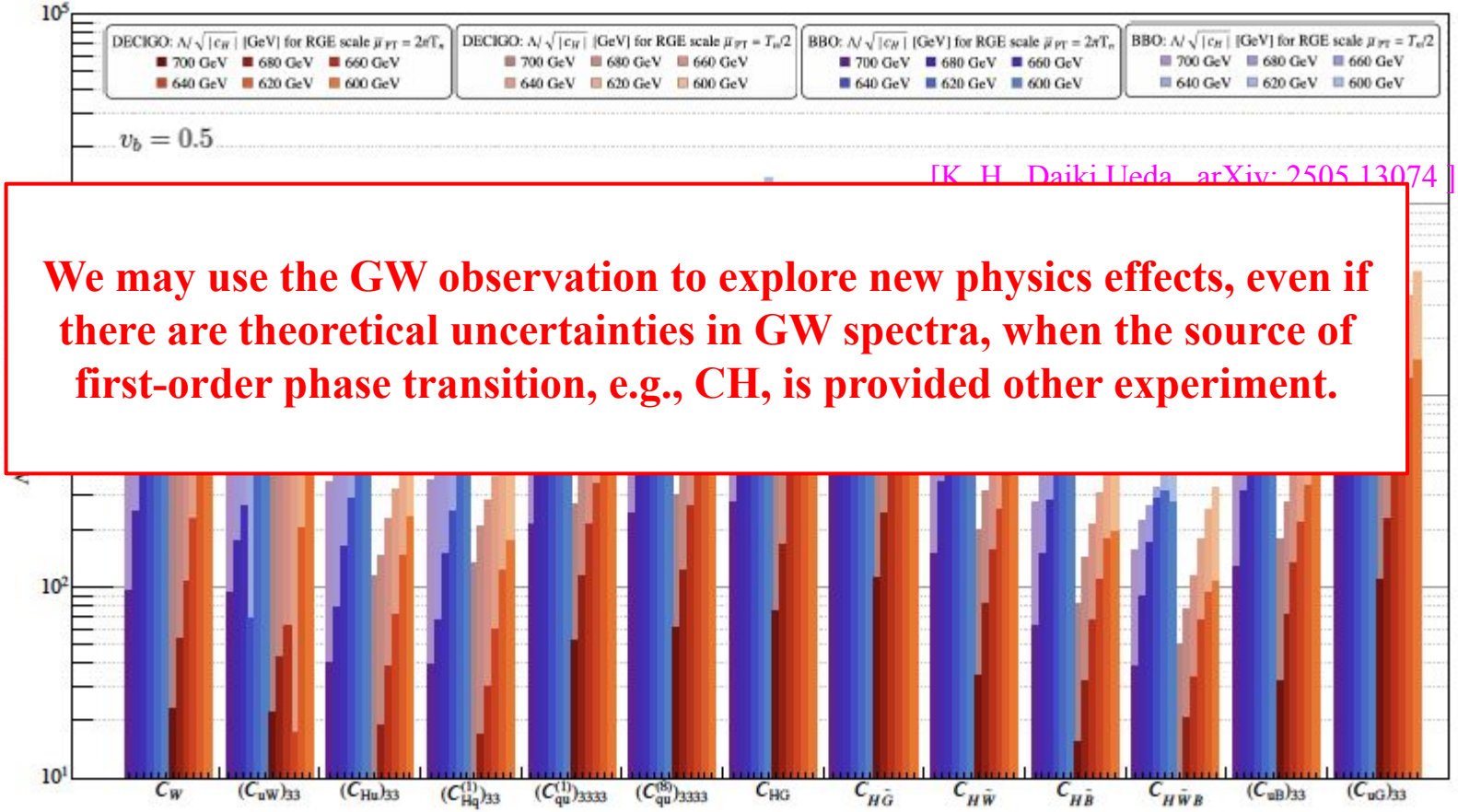

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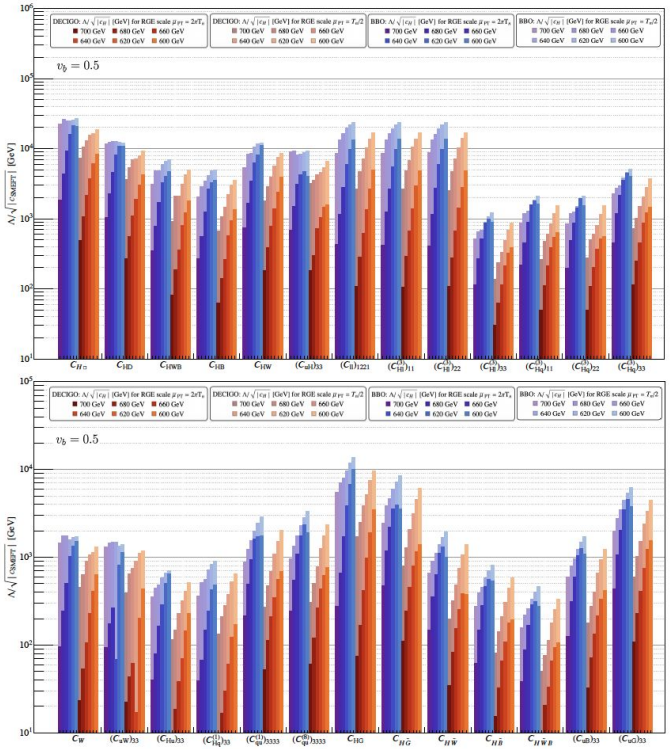
We may use the GW observation to explore new physics effects, even if there are theoretical uncertainties in GW spectra, when the source of first-order phase transition, e.g., CH, is provided other experiment.

Summary

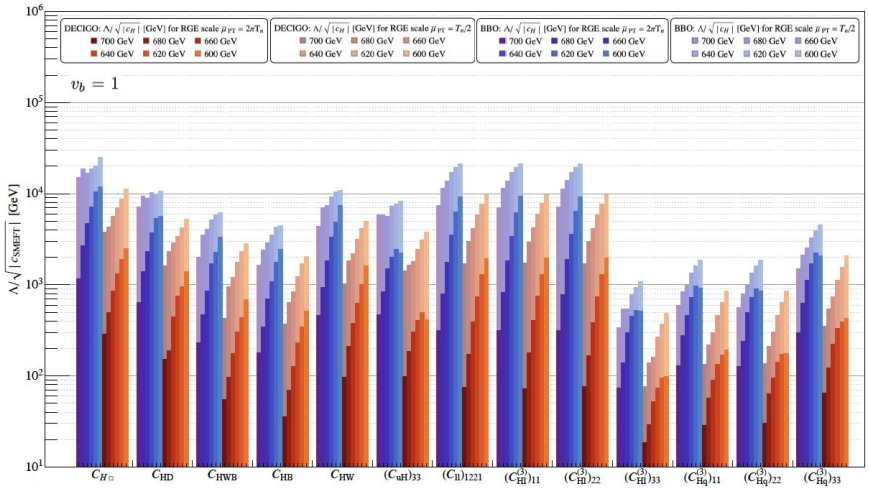
★ The spectra of GW from first-order phase transition depends on the NP effects.

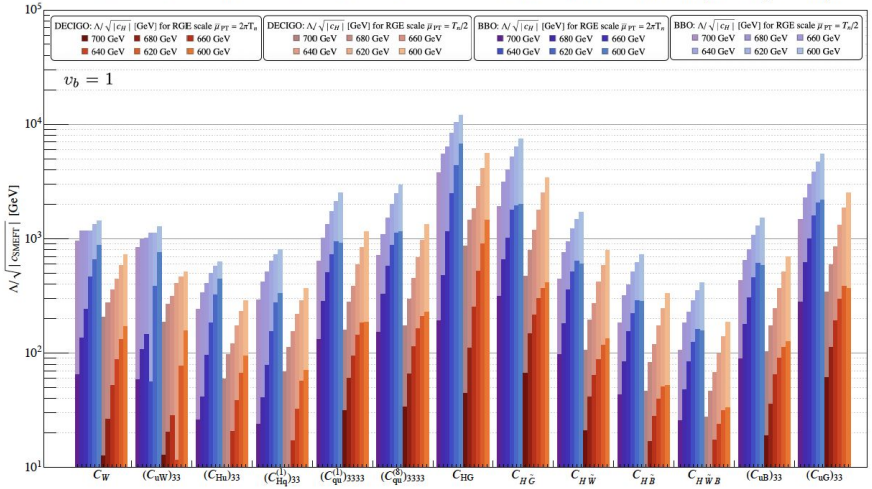
→ We can use the GW observation experiments to explore the NP effects.

★ The GW observations can remain sensitive to various new physics effects, even in the presence of renormalization scale uncertainties, provided that the source of first-order phase transition is precisely measured, e. g., by future collider experiments.



Backup


DECIGO: $\Lambda/\sqrt{|c_H|}$ [GeV] for RGE scale $\bar{\mu}_{PT} = 2\pi T_n$
DECIGO: $\Lambda/\sqrt{|c_H|}$ [GeV] for RGE scale $\bar{\mu}_{PT} = T_n/2$
BBO: $\Lambda/\sqrt{|c_H|}$ [GeV] for RGE scale $\bar{\mu}_{PT} = 2\pi T_n$
BBO: $\Lambda/\sqrt{|c_H|}$ [GeV] for RGE scale $\bar{\mu}_{PT} = T_n/2$
700 GeV 680 GeV 660 GeV
640 GeV 620 GeV 600 GeV
$v_b = 1$
$\Lambda/\sqrt{|c_{SMEFT}|}$ [GeV]
$C_{H\Box}$ C_{HD} C_{HWB} C_{HB} C_{HW} $(C_{uH})_{33}$ $(C_{ll})_{1221}$ $(C^{(3)}_{Hl})_{11}$ $(C^{(3)}_{Hl})_{22}$ $(C^{(3)}_{Hl})_{33}$ $(C^{(3)}_{Hq})_{11}$ $(C^{(3)}_{Hq})_{22}$ $(C^{(3)}_{Hq})_{33}$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700 GeV 680 GeV 660 GeV
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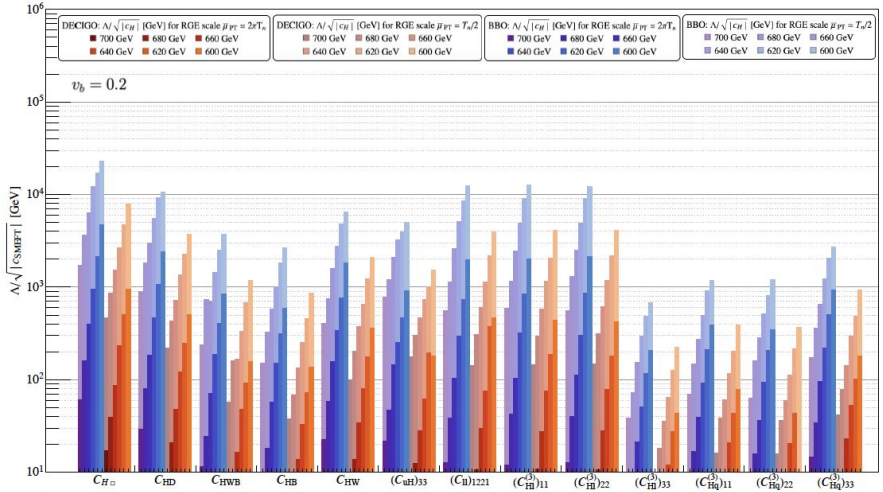
$v_b = 1$
$\Lambda/\sqrt{|c_{SMEFT}|}$ [GeV]
C_W $(C_{uW})_{33}$ $(C_{Hu})_{33}$ $(C^{(1)}_{Hq})_{33}$ $(C^{(1)}_{qu})_{3333}$ $(C^{(8)}_{qu})_{3333}$ C_{HG} $C_{H\tilde{G}}$ $C_{H\tilde{W}}$ $C_{H\tilde{B}}$ $C_{H\tilde{W}B}$ $(C_{uB})_{33}$ $(C_{uG})_{33}$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700 GeV 680 GeV 660 GeV
640 GeV 620 GeV 600 GeV
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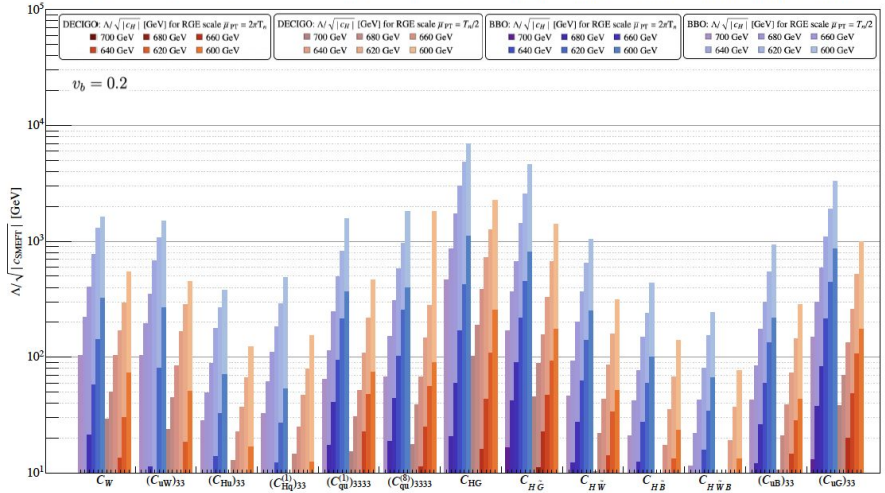
$\Lambda/\sqrt{|c_{SMEFT}|}$ [GeV]
$C_{H\Box}$ C_{HD} C_{HWB} C_{HB} C_{HW} $(C_{uH})_{33}$ $(C_{ll})_{1221}$ $(C^{(3)}_{Hl})_{11}$ $(C^{(3)}_{Hl})_{22}$ $(C^{(3)}_{Hl})_{33}$ $(C^{(3)}_{Hq})_{11}$ $(C^{(3)}_{Hq})_{22}$ $(C^{(3)}_{Hq})_{33}$


DECIGO: $\Lambda/\sqrt{|c_H|}$ [GeV] for RGE scale $\bar{\mu}_{PT} = 2\pi T_n$
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BBO: $\Lambda/\sqrt{|c_H|}$ [GeV] for RGE scale $\bar{\mu}_{PT} = 2\pi T_n$
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700 GeV 680 GeV 660 GeV
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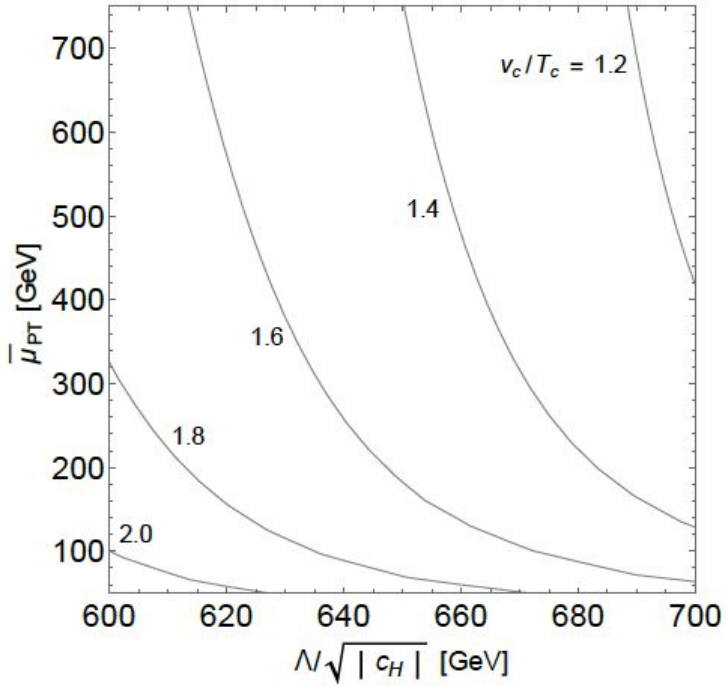
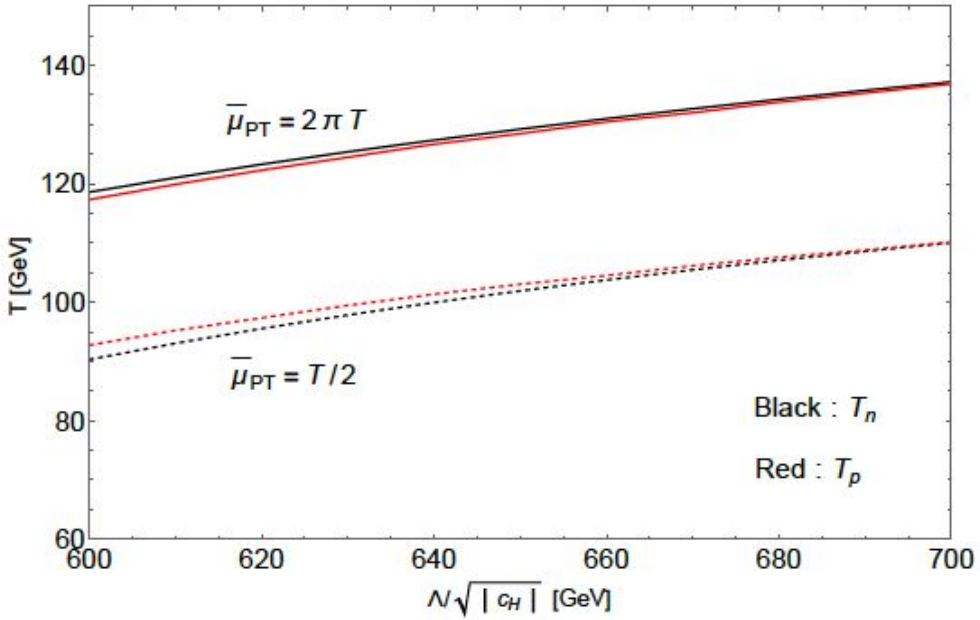
$v_b = 0.2$
$\Lambda/\sqrt{|c_{SMEFT}|}$ [GeV]
C_W $(C_{uW})_{33}$ $(C_{Hu})_{33}$ $(C^{(1)}_{Hq})_{33}$ $(C^{(1)}_{qu})_{3333}$ $(C^{(8)}_{qu})_{3333}$ C_{HG} $C_{H\tilde{G}}$ $C_{H\tilde{W}}$ $C_{H\tilde{B}}$ $C_{H\tilde{W}B}$ $(C_{uB})_{33}$ $(C_{uG})_{33}$

The results


v_c/T_c = 1.2
1.4
1.6
1.8
2.0
$\bar{\mu}_{PT}$ [GeV]
$\Lambda/\sqrt{|c_H|}$ [GeV]
700
600
500
400
300
200
100
600
620
640
660
680
700


$\bar{\mu}_{PT} = 2\pi T$
$\bar{\mu}_{PT} = T/2$
Black : T_n
Red : T_p
T [GeV]
$\Lambda/\sqrt{|c_H|}$ [GeV]
140
120
100
80
60
600
620
640
660
680
700