

Quantum sensing of proton spins with a single NV center

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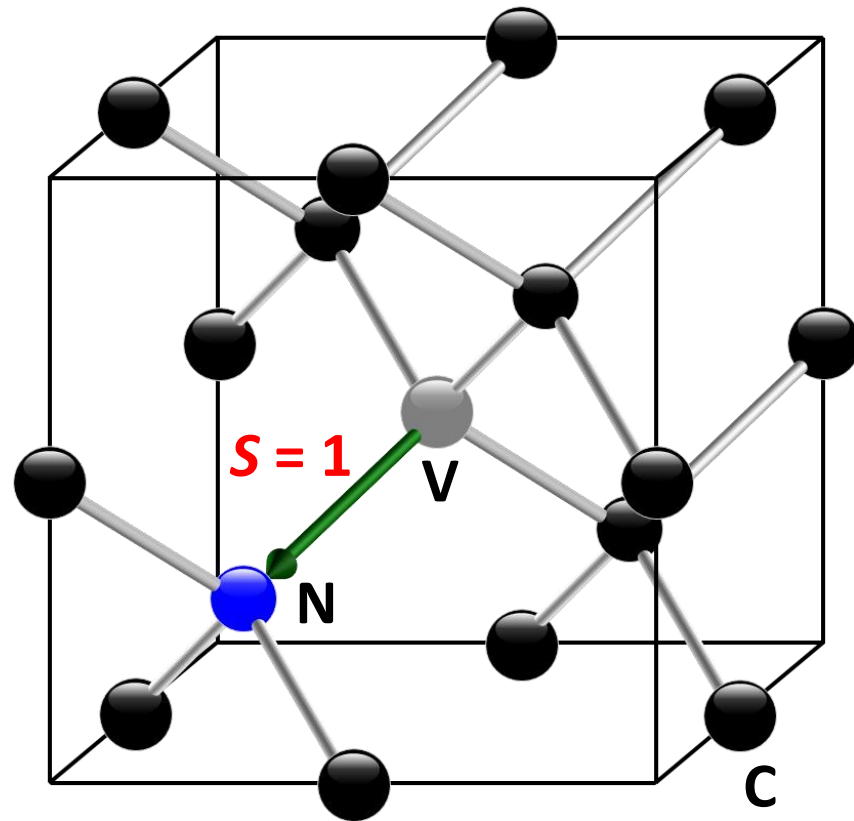
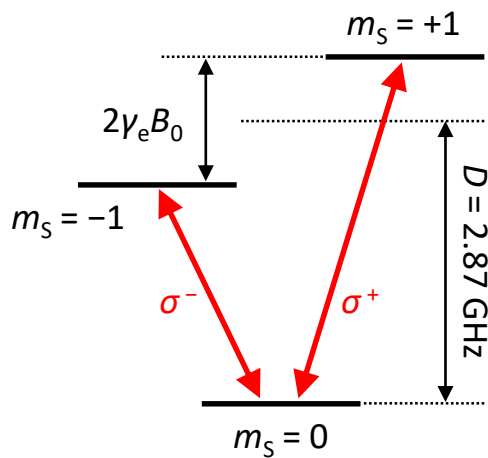
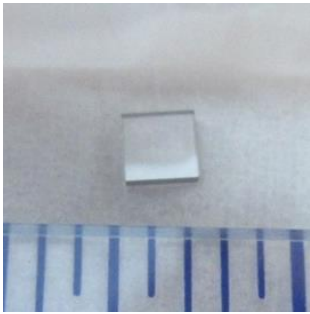
2022.3.9

Physics Frontiers with Quantum Science and Technology

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NV center in diamond

Synthetic (CVD) diamond
[N] < 5 ppb, [NV] < 0.03 ppb

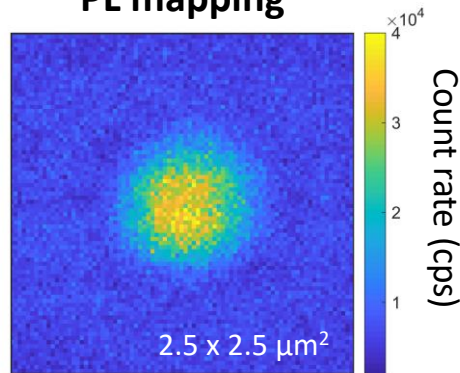


$$\rho_C = 1.77 \times 10^{23} \text{ cm}^{-3}$$

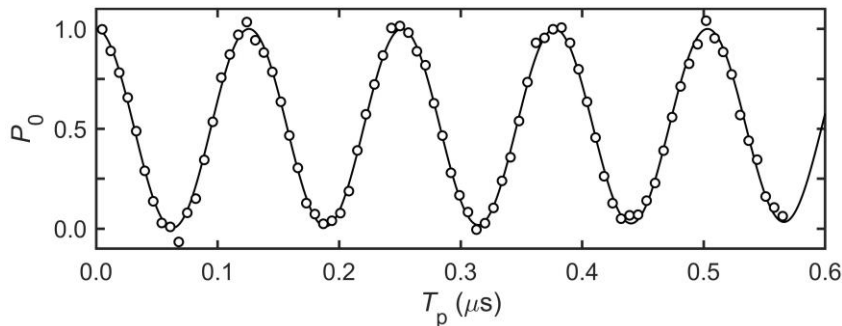
NV center in diamond

- Optical detection & initialization of single spins
- Microwave control of single spins
- Room temperature operation

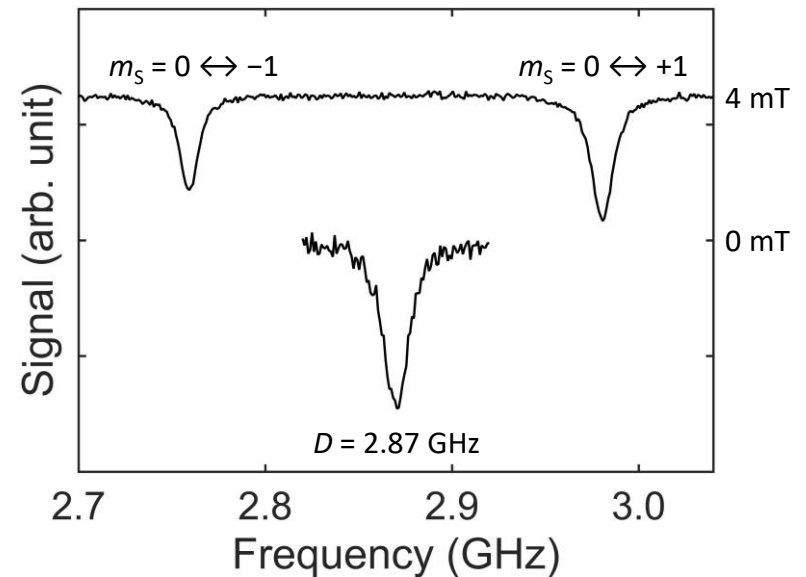
PL mapping



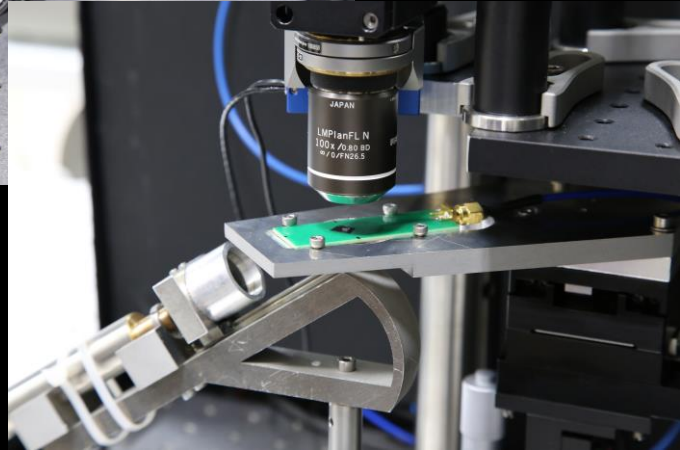
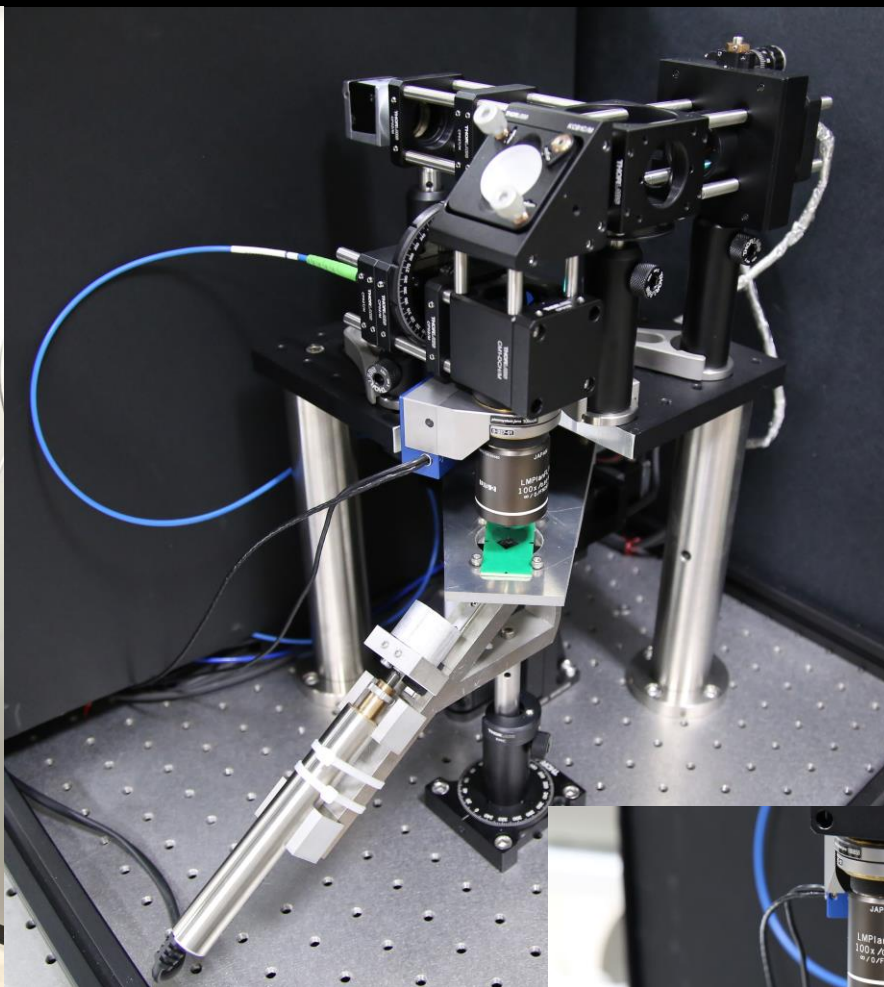
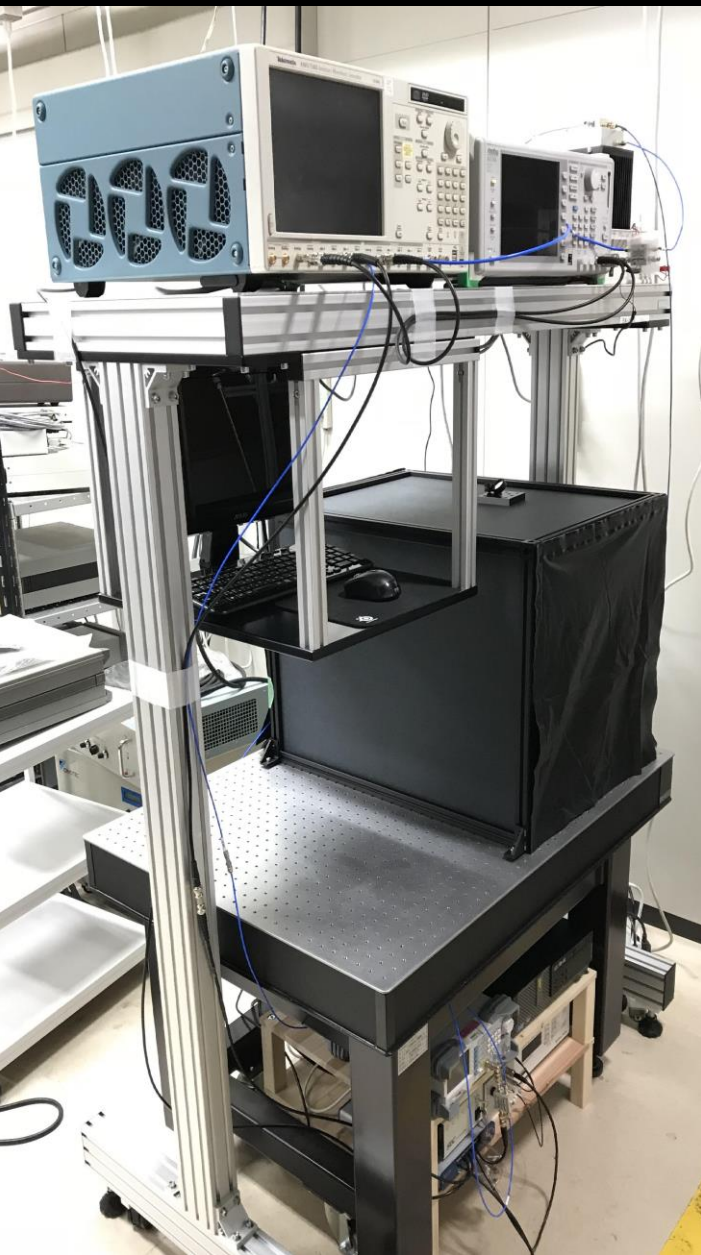
Rabi oscillation



Optically detected magnetic resonance



Experimental setup

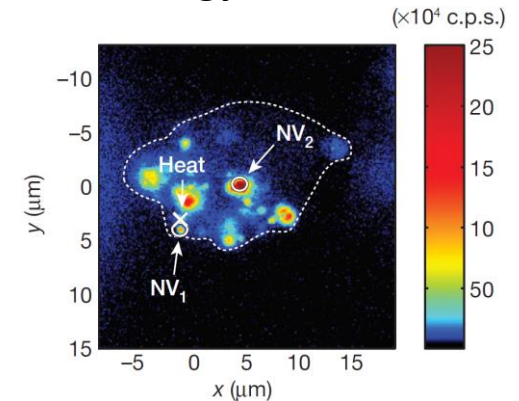
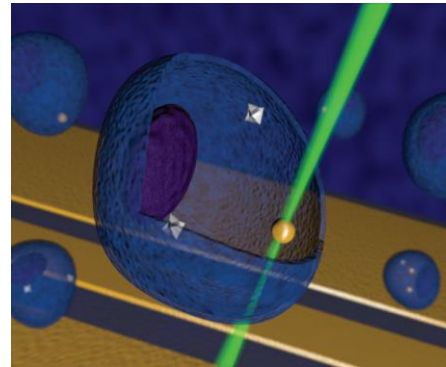


AIP Adv. **10**, 025206 (2020)
Misonou *et al.*

Quantum sensing with NV centers

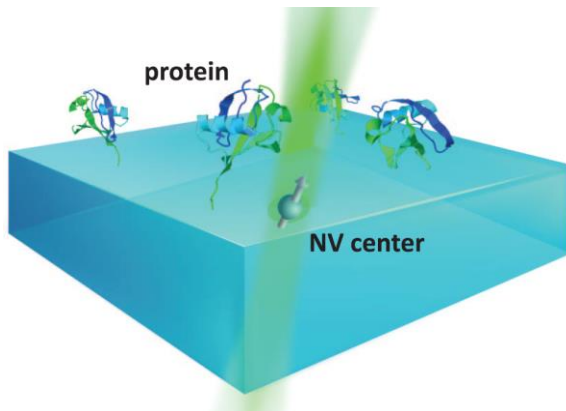
- *B, E, T, S...*
- DC & AC modes
- Wide temperature range
- Nondestructive
- High spatial resolution
- Various modalities

Nanodiamond & biology



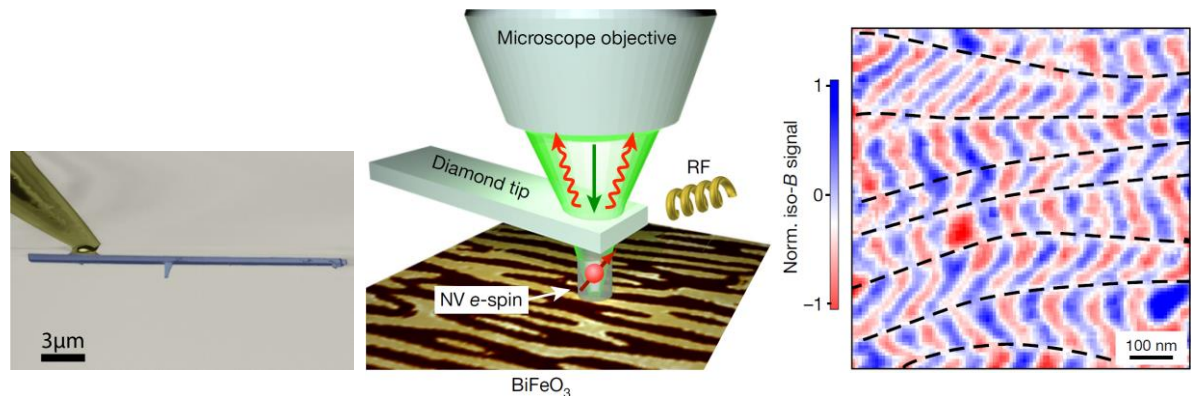
Nature **500**, 54 (2013)

Near-surface NV center & NMR



Science **351**, 836 (2016)

Scanning probe & condensed matter



Rev. Sci. Instrum. **87**, 063703 (2016); Nature **549**, 252 (2017)

Quantum sensing with NV centers

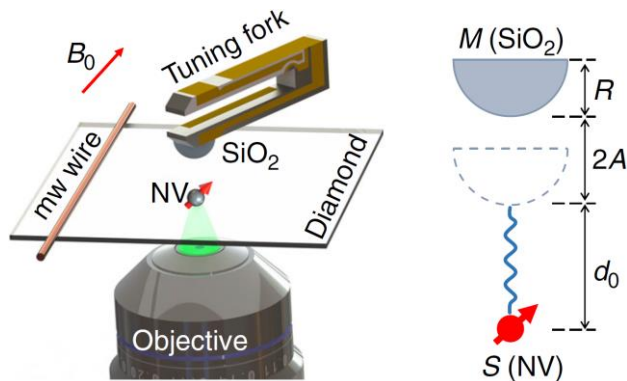
Fundamental physics: search for exotic interactions & dark matter candidates

DOI: 10.1038/s41467-018-03152-9

OPEN

Searching for an exotic spin-dependent interaction with a single electron-spin quantum sensor

Xing Rong^{1,2,3}, Mengqi Wang^{1,2,3}, Jianpei Geng^{1,2}, Xi Qin^{1,2,3}, Maosen Guo^{1,3}, Man Jiao^{1,3}, Yijin Xie^{1,3}, Pengfei Wang^{1,2,3}, Pu Huang^{1,2,3}, Fazhan Shi^{1,2,3}, Yi-Fu Cai^{4,5}, Chongwen Zou⁶ & Jiangfeng Du^{1,2,3}



Nature Commun. **9**, 739 (2018) Rong *et al.*

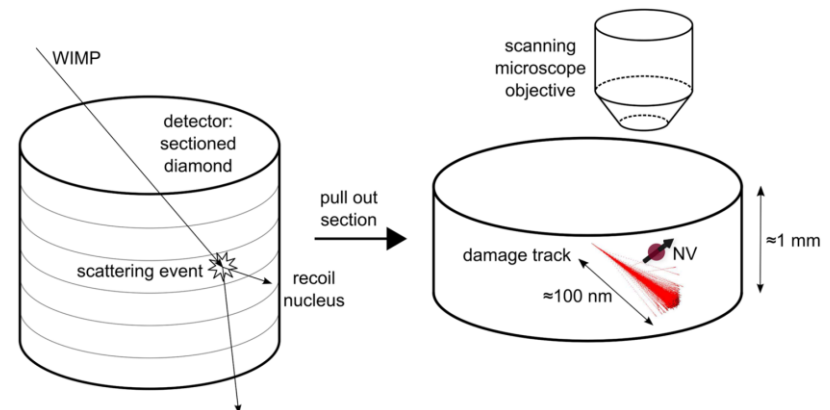
Related works from Jiangfeng Du's group at USTC:

- Phys. Rev. Lett. **121**, 080402 (2018) Rong *et al.*
- Phys. Rev. Lett. **127**, 010501 (2021) Jiao *et al.*
- arXiv: 2201.04408 Liang *et al.*

PHYSICAL REVIEW D **96**, 035009 (2017)

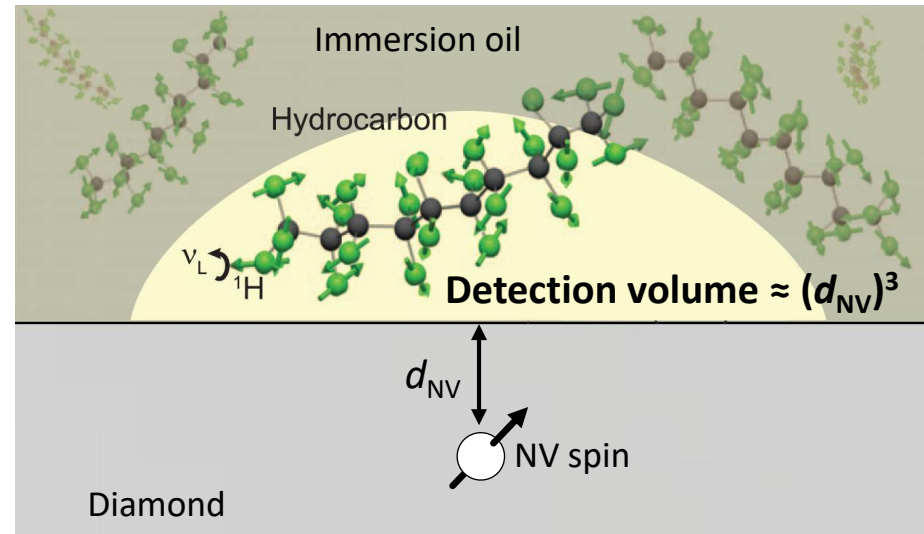
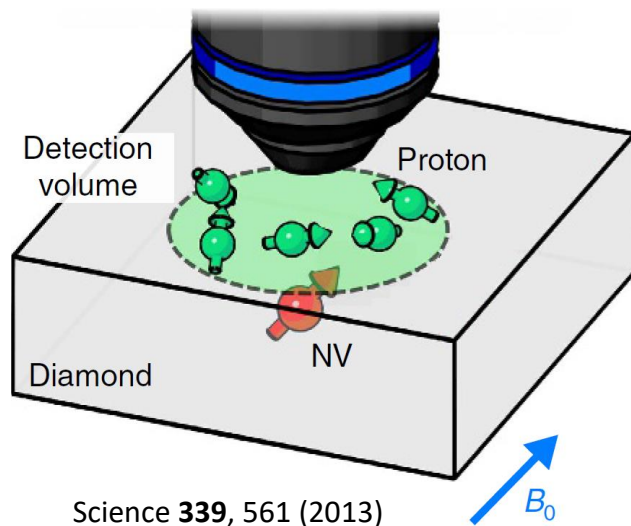
A method for directional detection of dark matter using spectroscopy of crystal defects

Surjeet Rajendran,¹ Nicholas Zobrist,² Alexander O. Sushkov,^{3,4} Ronald Walsworth,⁵ and Mikhail Lukin⁶

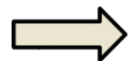


Phys. Rev. D **96**, 035009 (2017) Rajendran *et al.*

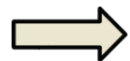
Quantum sensing of nuclear spins



Nuclear spins **precess** at $f_{ac} =$ a few kHz–MHz under B_0

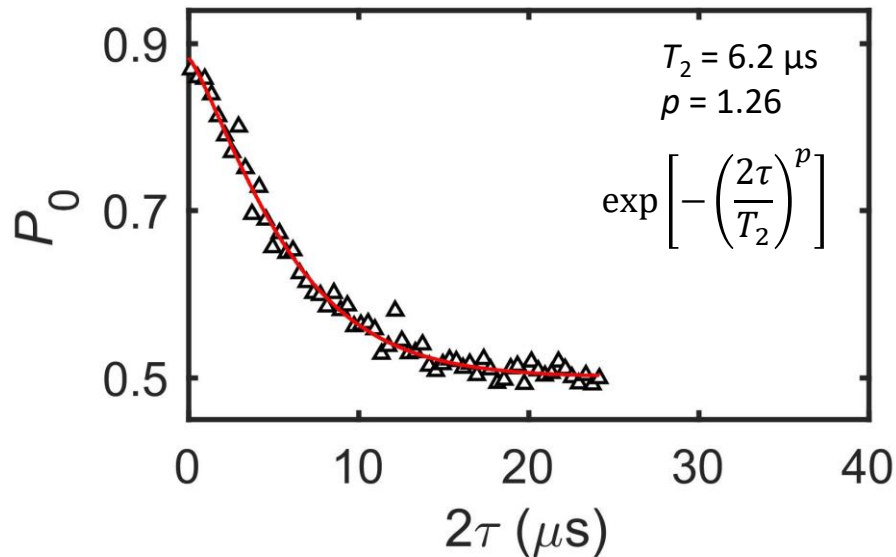
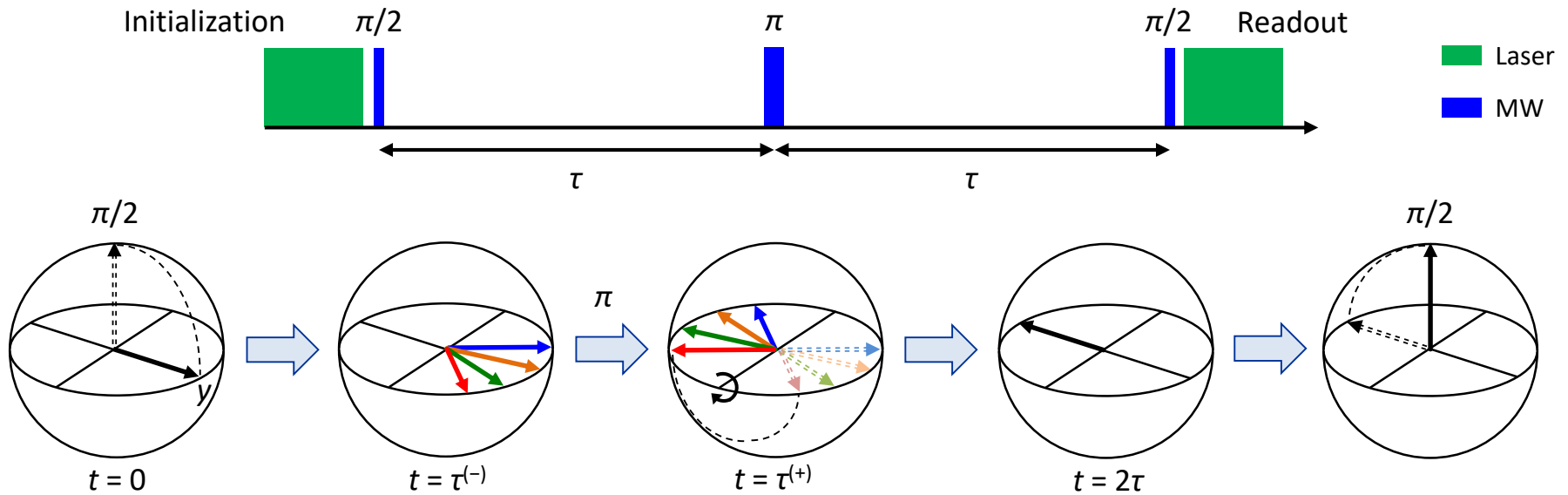


Weak AC magnetic field on the NV spin

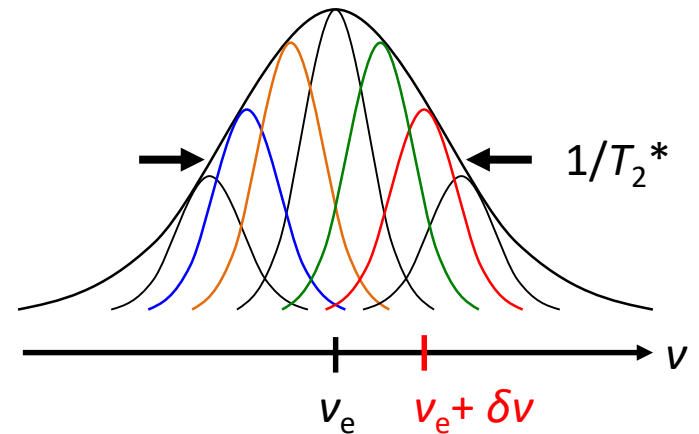


Detect using **quantum coherence** of the NV spin

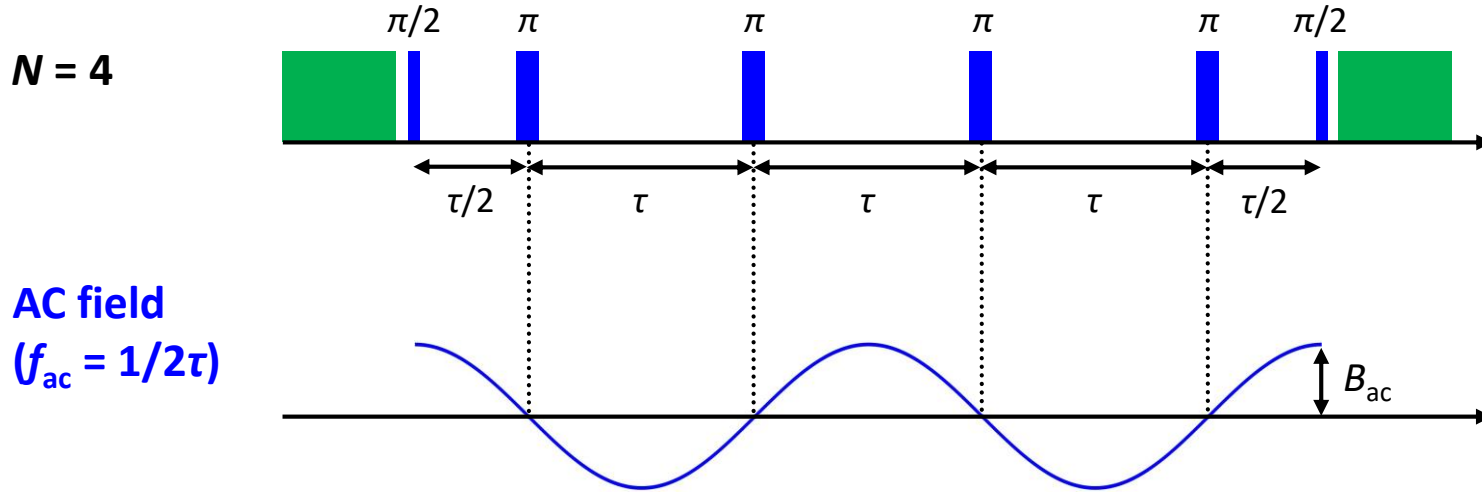
Coherence time of NV spin: T_2



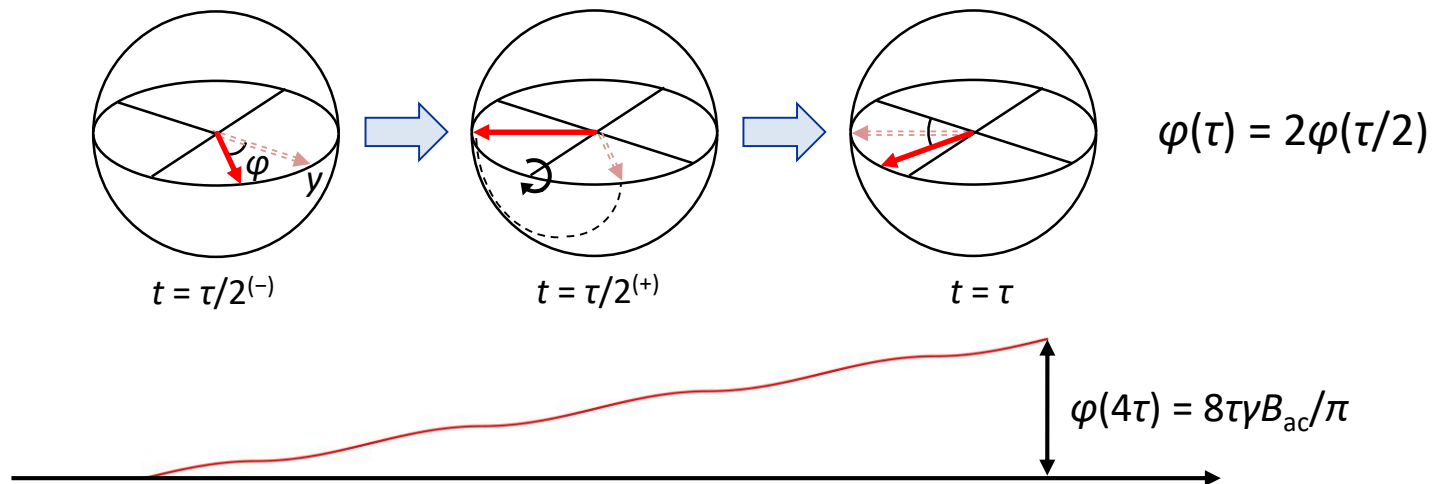
Static DC shifts cancelled
(refocusing)



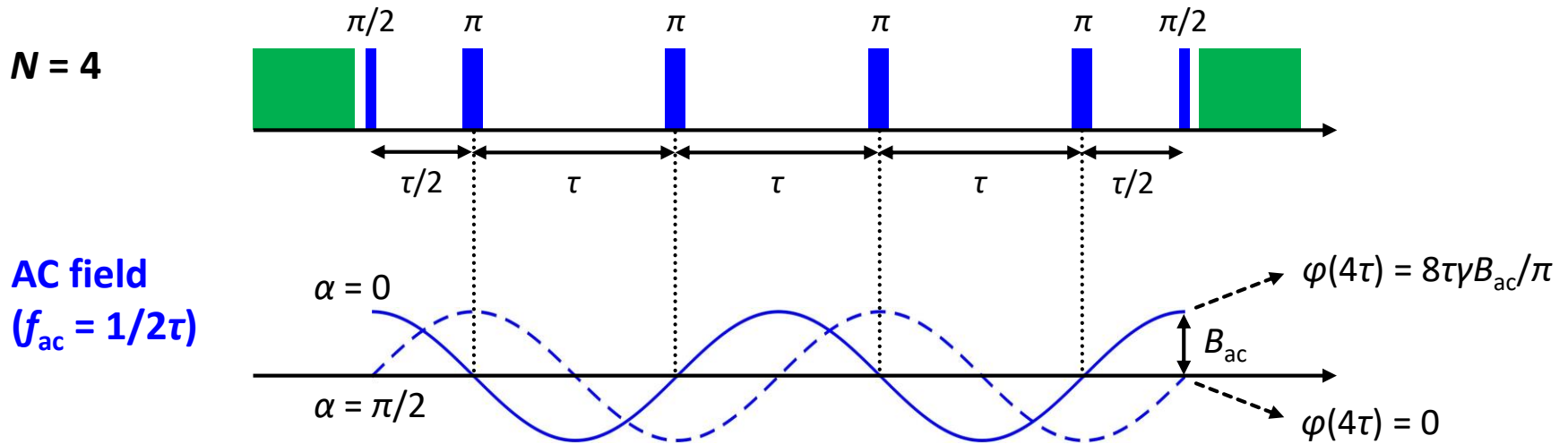
AC magnetometry



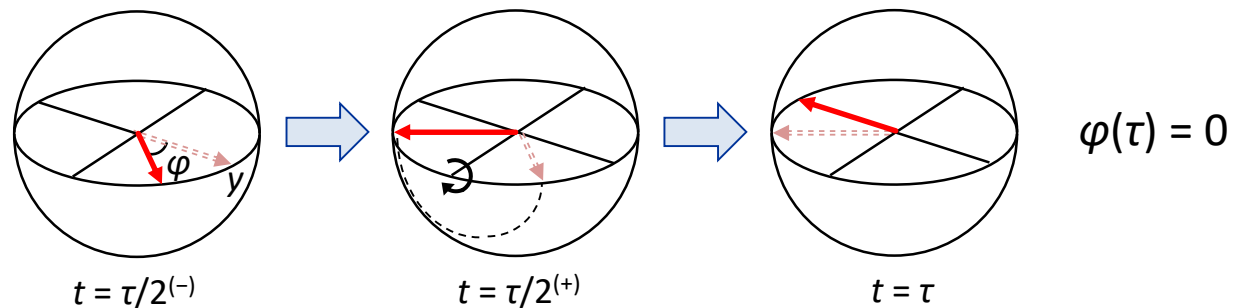
Sensor phase buildup (deviation from y axis): **loss of coherence**



AC magnetometry

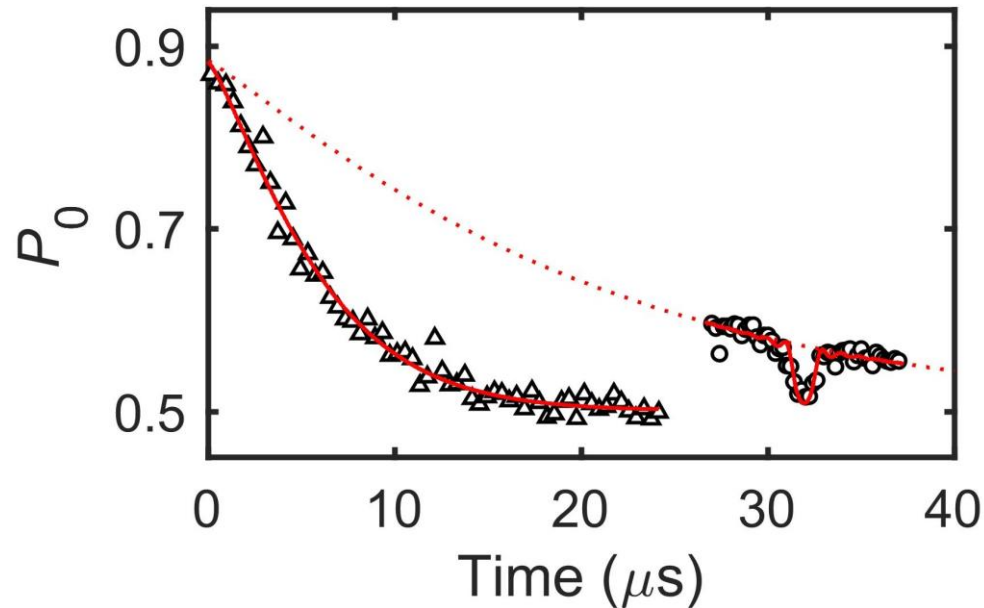


Sensor phase buildup (deviation from y axis): ***the initial phase α matters***

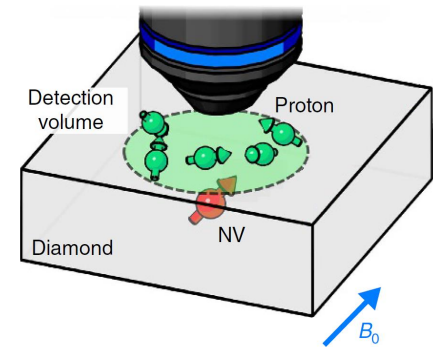


- $\varphi \propto \cos \alpha$
- Usually, we average over **random α**

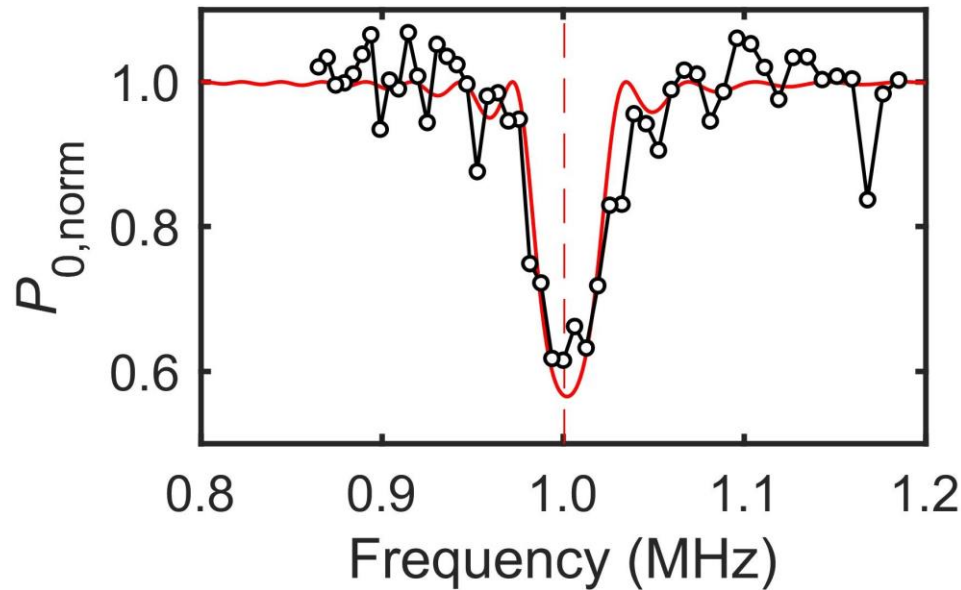
Sensing of ensemble n -spins



- $T_2 = 6.2 \mu\text{s} @ B_0 = 23.5 \text{ mT}$
- $N = 64$
- $2\tau = 2 \times 32 \mu\text{s}/64 = 1 \mu\text{s}$
→ $\gamma_{\text{H}} B_0 = (42.577 \text{ kHz/mT}) \times B_0 = 1.00 \text{ MHz}$



Sensing of ensemble n -spins

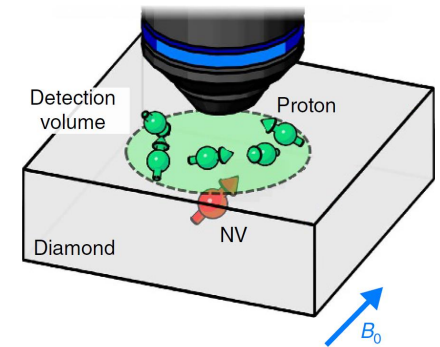


$$C(\tau) = f(B_{\text{rms}})$$

$$B_{\text{rms}} = \frac{\mu_0}{4\pi} h\gamma_{\text{H}} \sqrt{\frac{5\pi\rho}{96d_{\text{NV}}^3}}$$

Phys. Rev. B **93**, 045425 (2016)

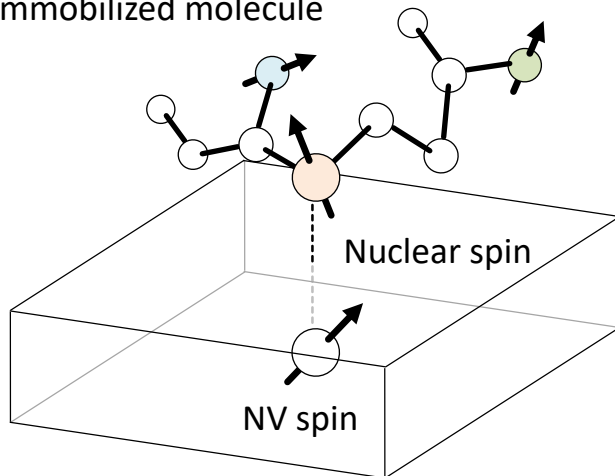
- Proton density $\rho = 6 \times 10^{28} \text{ m}^{-3}$ (known)
- $d_{\text{NV}} = 6.26 \text{ nm}$
- $B_{\text{rms}} \approx 560 \text{ nT}$
- Detection volume $(d_{\text{NV}})^3 \approx \mathbf{0.25 \text{ zL}}$ (zepto = 10^{-21})
- # of protons $\rho(d_{\text{NV}})^3 \approx 1500$
- Thermal polarization (10^{-7}) vs. statistical fluctuation $(1500)^{0.5} \approx \mathbf{39}$



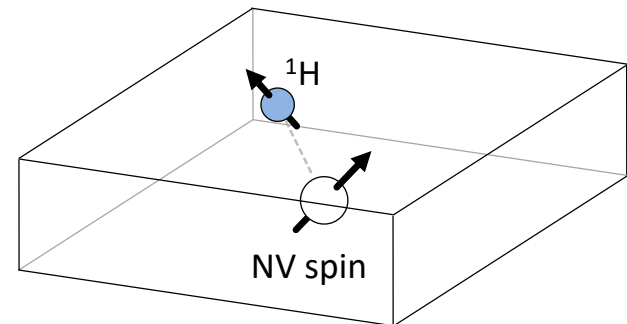
Toward single-molecular imaging

- **High spatial resolution**
 - Special about *single-nuclear-spin-level* NMR
 - **Measure the positions of individual nuclear spins** in a single molecule
- **High spectral resolution**
 - Routine in conventional ensemble NMR spectroscopy
 - Measure nuclear species (^1H , ^{13}C , ^{19}F ...)
 - Measure J -couplings & chemical shifts with ppm accuracy

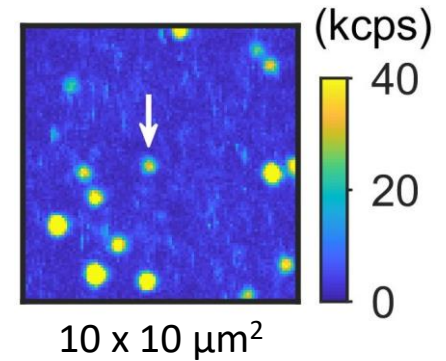
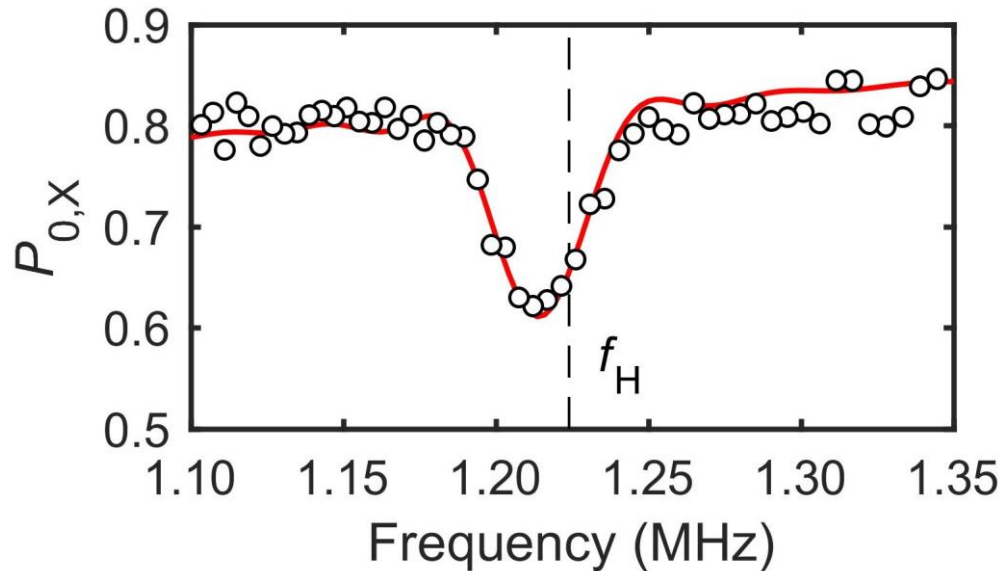
Immobilized molecule



Detection of single protons in CVD diamond
(as a testbed)

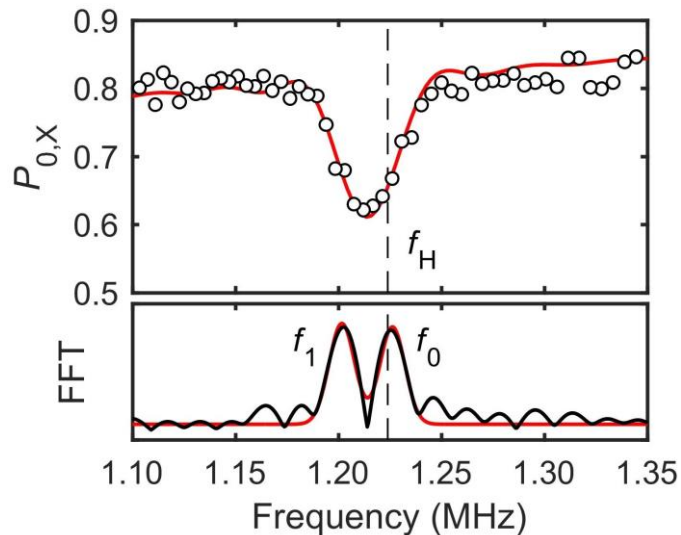
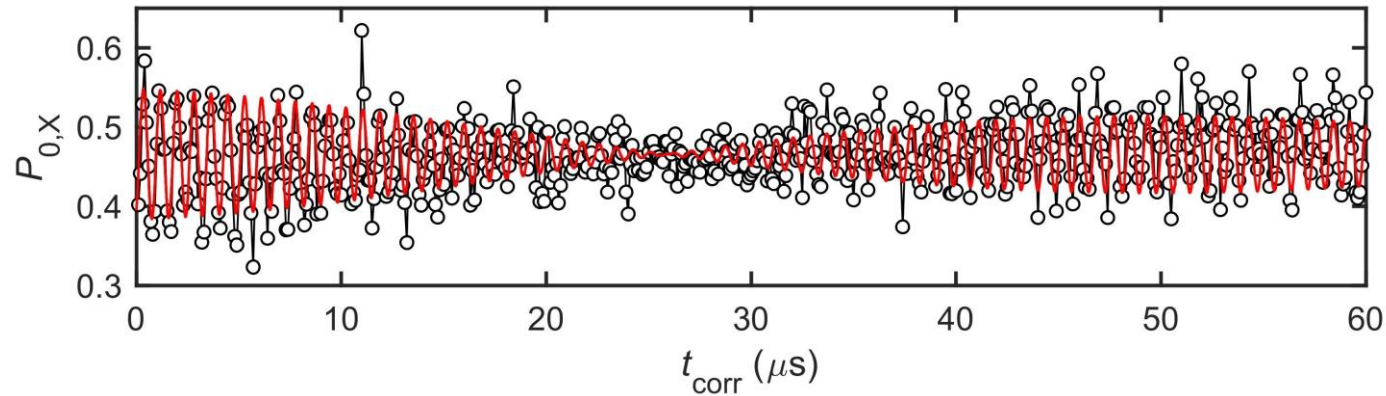


Sensing of single n -spin



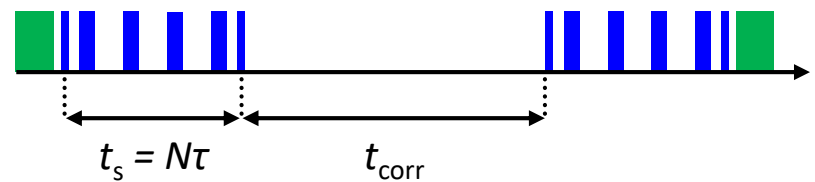
- Single NV in a N-doped CVD film ($[^{12}\text{C}] = 99.999\%$)
- $N = 64$
- $f_H = \gamma_H B_0 = 42.577 \text{ kHz/mT} \times 28.7 \text{ mT} = 1.2239 \text{ MHz}$

Correlation spectroscopy of single n -spin

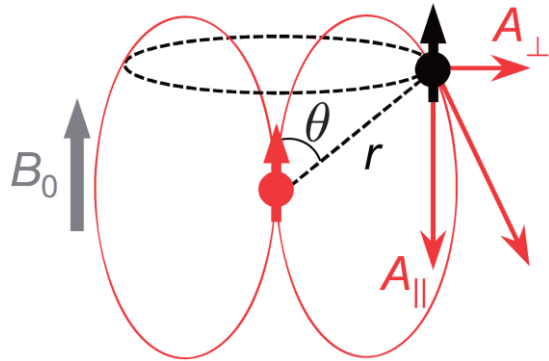


- $f_0 = 1.2234$ MHz
- $f_1 = 1.2046$ MHz

T_1 -limited spectroscopy



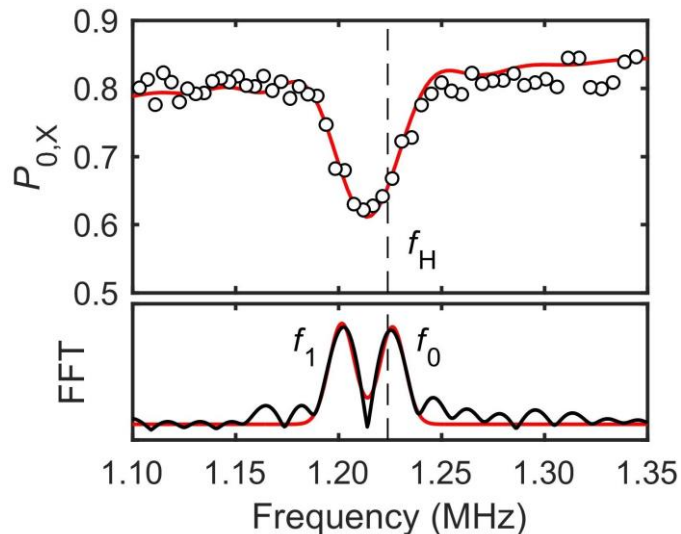
Correlation spectroscopy of single n -spin



Hamiltonian of ^1H n -spin coupled with NV e -spin

$$H_n = f_H I_z + |m_s = -1\rangle\langle -1| (A_{\parallel} I_z + A_{\perp} I_x)$$

→ No hyperfine field when $|m_s = 0\rangle$

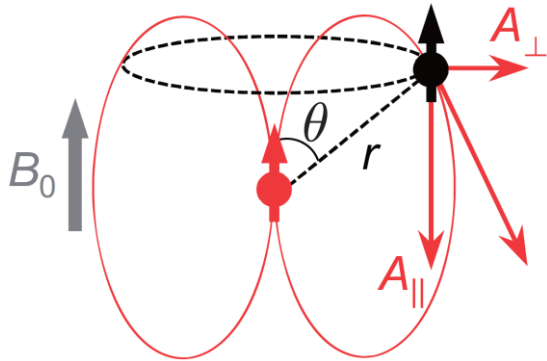


- $f_0 = 1.2234 \text{ MHz} = f_H (m_s = 0)$
- $f_1 = 1.2046 \text{ MHz} = f_H + A'_{\parallel} (m_s = -1)$

$$A'_{\parallel} = -18.8 \text{ kHz}$$

$$(f_0 + f_1)/2 = 1.2140 \text{ MHz} \rightarrow \text{dip}$$

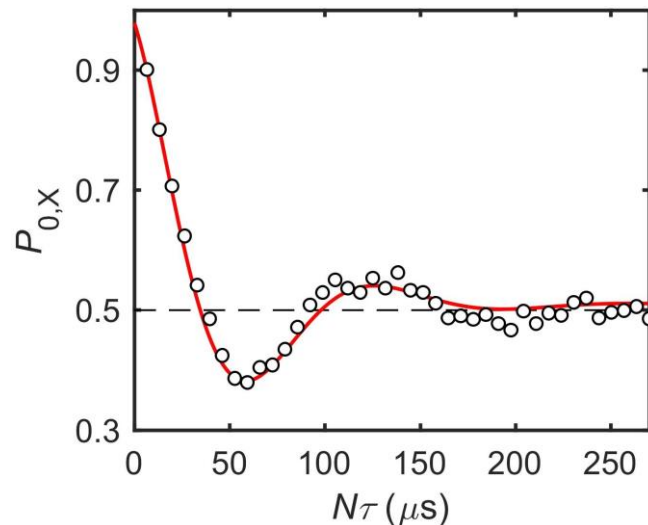
Coherent control of single n -spin



Hamiltonian of ^1H n -spin coupled with NV e -spin

$$H_n = f_{\text{H}} I_z + |m_s = -1\rangle\langle -1| (A_{\parallel} I_z + A_{\perp} I_x)$$

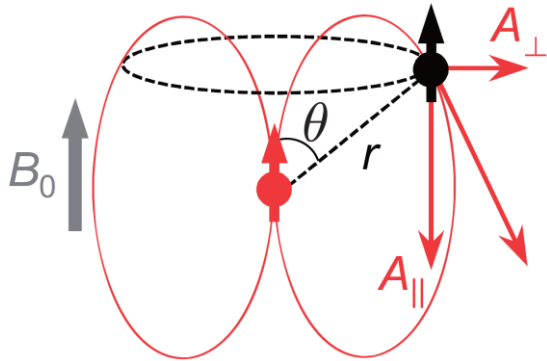
→ The single ^1H n -spin rotates about the A_{\perp} axis



- $N \rightarrow 656$ ($\tau = 411.5$ ns, fixed)
- $f_{\text{osc}} = 7.414$ kHz = $A'_{\perp}/2$

$P_{0,x} < 0.5$ (coherent rotation)
→ Single proton

Determination of hyperfine constants

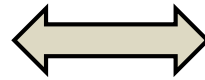


Magnetic dipole interaction

$$A_{\parallel} = h\gamma_e\gamma_H \frac{3 \cos^2 \theta - 1}{r^3}$$

$$A_{\perp} = h\gamma_e\gamma_H \frac{3 \cos \theta \sin \theta}{r^3}$$

$$\begin{aligned} A_{\parallel} &= -19.0 \text{ kHz} \\ A_{\perp} &= 22.9 \text{ kHz} \end{aligned}$$



$$\begin{aligned} r &= 1.44 \text{ nm} \\ \theta &= 72.3^\circ \end{aligned}$$

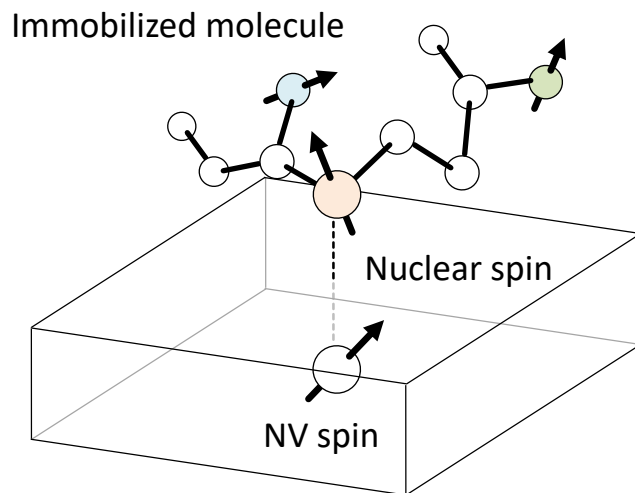
The position of the nucleus can be determined
→ Basis for single-molecular structure analysis

[Azimuthal angle ϕ can be determined by RF control] Phys. Rev. B **98**, 121405 (2018) Sasaki *et al.*

Appl. Phys. Lett. **117**, 114002 (2020) Sasaki *et al.*

Toward single-molecular imaging

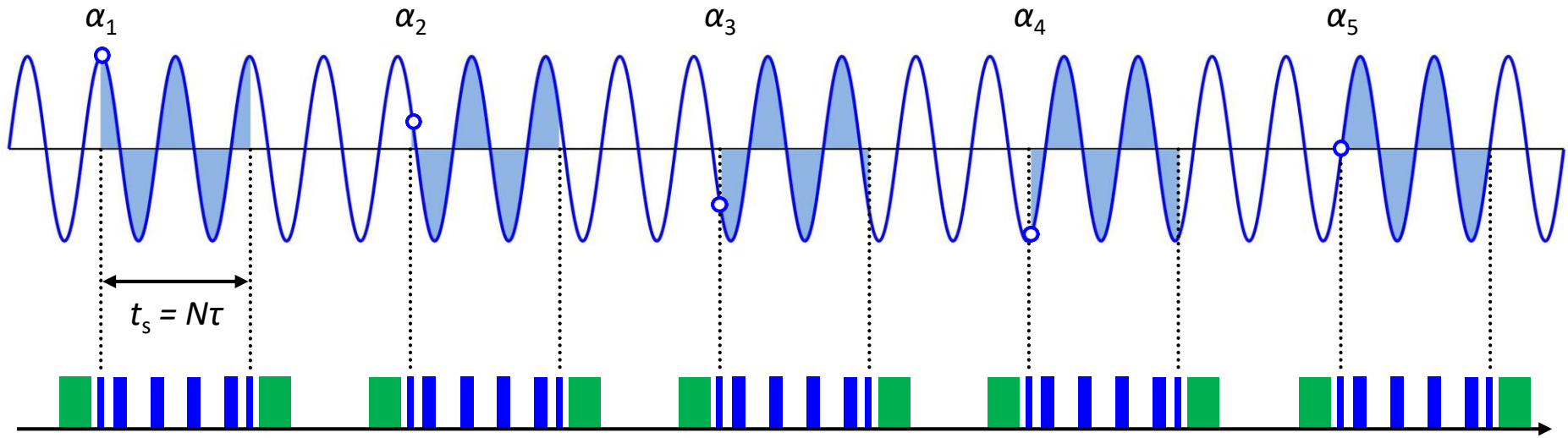
- **High spatial resolution**
 - Accurate measurement of $e-n$ int. const's (A_{\parallel}, A_{\perp}) $\approx (r, \theta)$
 - ϕ can be determined by RF control
- **High spectral resolution**
 - Routine in conventional ensemble NMR spectroscopy
 - Measure nuclear species (^1H , ^{13}C , ^{19}F ...)
 - Measure J -couplings & chemical shifts with **ppm accuracy**



Not so easy with NV centers
Limited by sensor/memory
spin lifetimes ($T_{2e/n}$, $T_{1e/n}$)

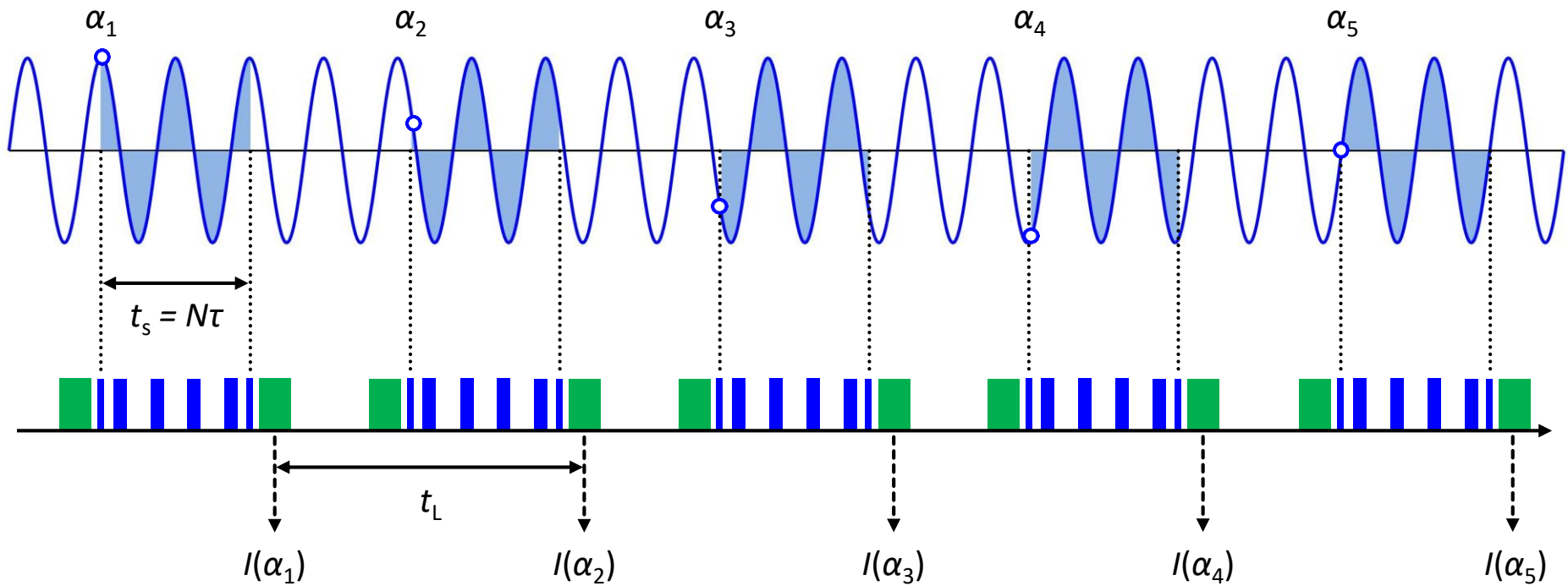
T_{2e} tends to be shorter for
near-surface NV centers

AC magnetometry revisited



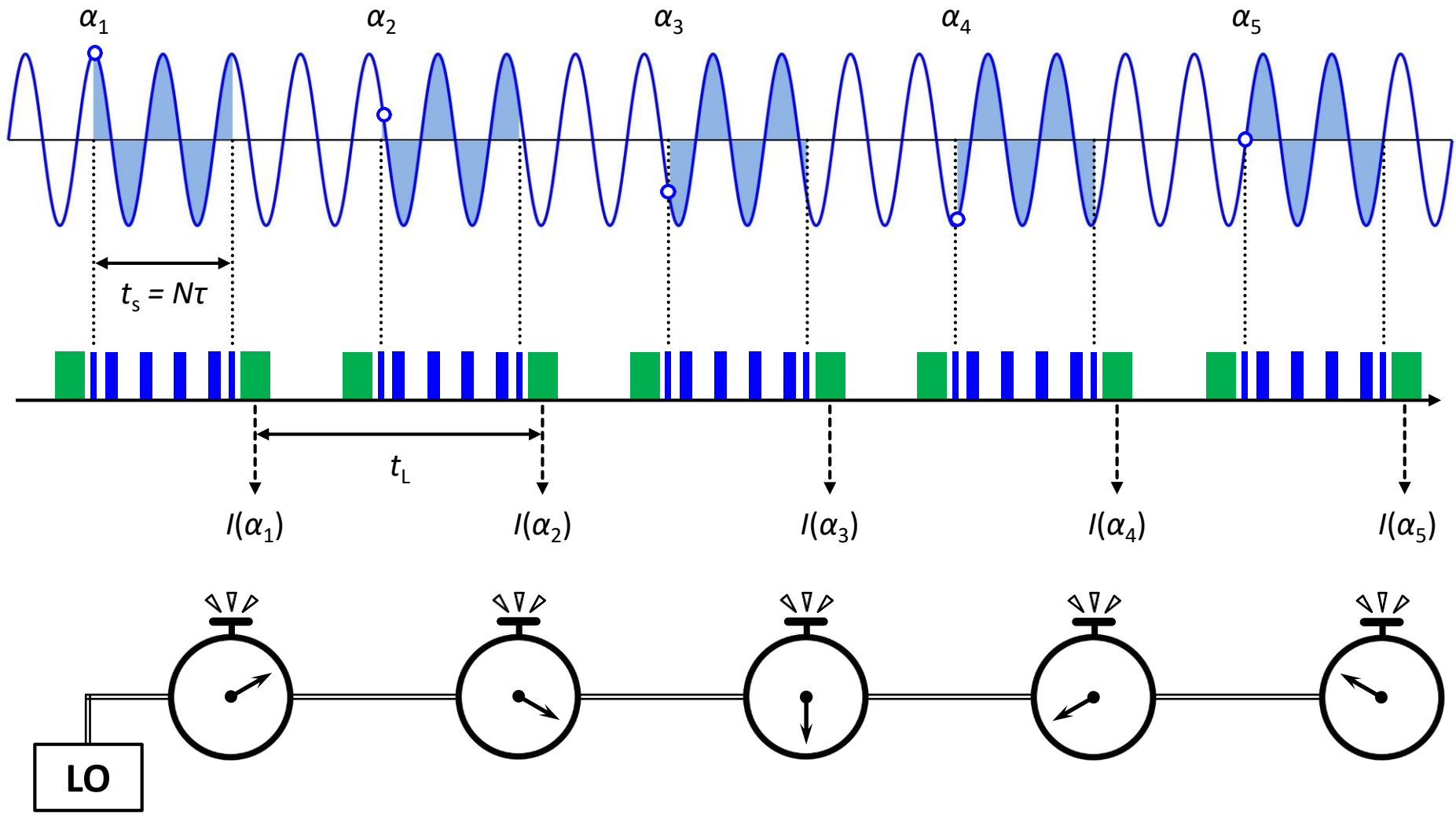
- $\varphi \propto \cos \alpha$
- Usually, we average over **random α**

AC magnetometry revisited



- $\varphi \propto \cos \alpha$
- Usually, we average over **random α**
- **If the data acq. is periodic**, adjacent α 's are related by $\alpha_{k+1} = 2\pi f_{ac} t_L + \alpha_k$

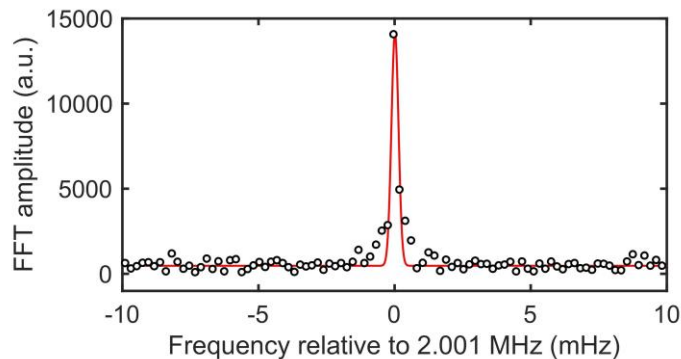
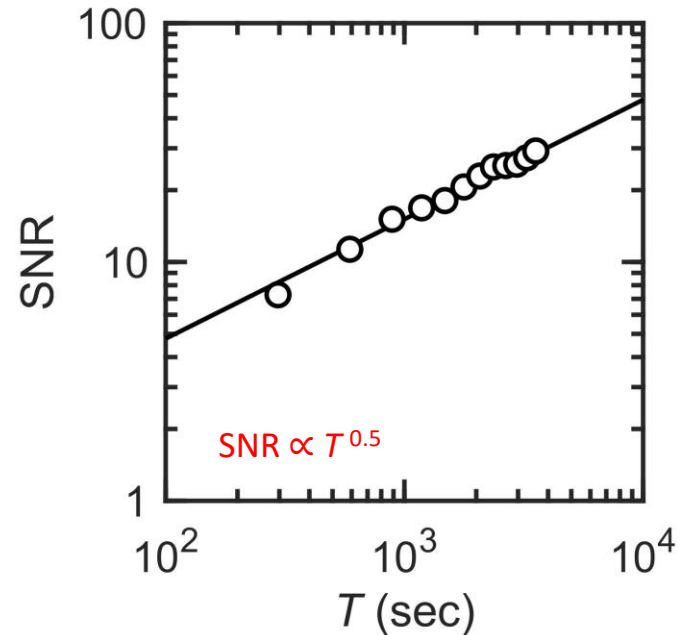
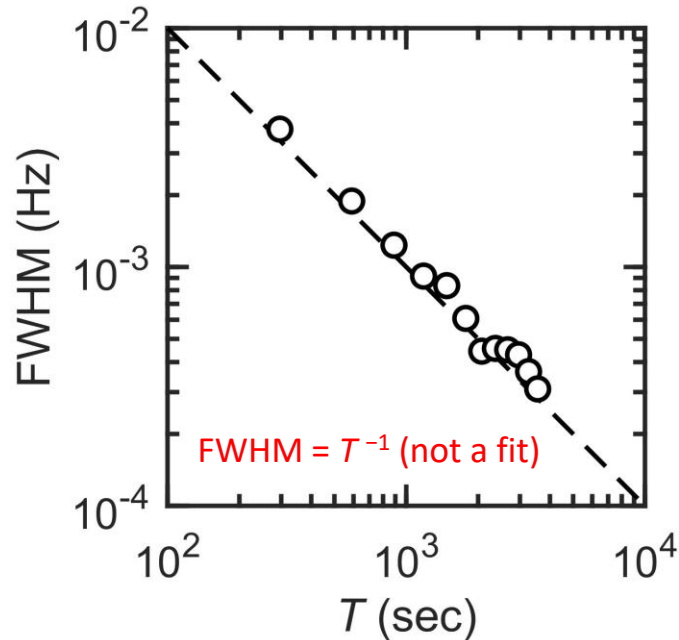
Ultrahigh resolution sensing



Undersampled, sensor-lifetime-unlimited signal

Ultrahigh resolution sensing

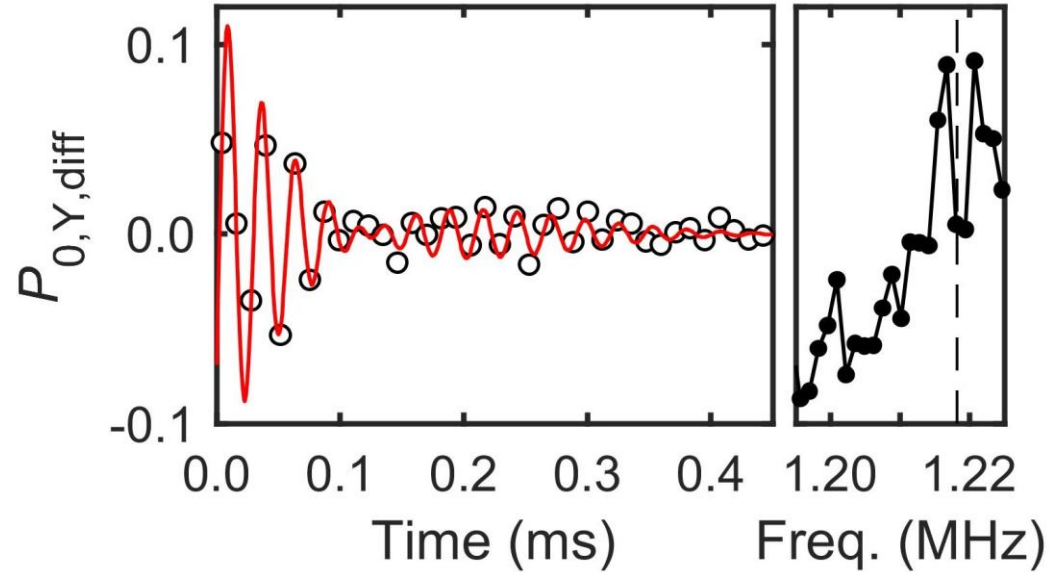
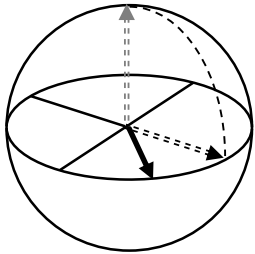
$B_{ac} = 96.5$ nT & $f_{ac} = 2.001$ MHz applied from a coil, detected by a single NV center



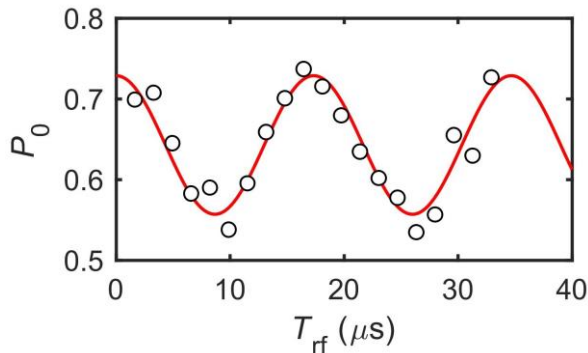
- $T = 3600$ sec
- $FWHM = 0.304$ mHz

Free induction decay of single n -spin

RF control & free precession of n -spin



Nuclear Rabi oscillation



- $T_{\text{rf}, \pi/2} = 4.115 \mu\text{s}$
- $[\text{PulsePol}] - T_{\text{rf}, \pi/2} - [\text{X}/2 - (\text{XY16}) - \text{Y}/2 - \text{L}_{\text{RO}}]^{50}$
- $f_{\text{sample}} = 1/t_L = 84.46 \text{ kHz}$
- $f_p = (f_0 + f_1)(t_s/t_L)/2 + f_0(t_s - t_L)/t_L = 1.2182 \text{ MHz}$
 \rightarrow Split (analogous to chemical shifts)

Summary

- **Tools for single-molecule imaging/structural analysis are being developed**
 - Ultrahigh resolution sensing^[1,2,3], resolving chemical shifts^[3,4] & suppression of back action from n -spins^[5,6]
 - Determination of the positions of individual n -spins via RF control^[7,8,9,10]
 - Detection and control of single proton spins^[11,12]
- **Also useful for fundamental physics? I hope so.**

[1] Science **356**, 832 (2017) Schmitt *et al.* (Ulm)

[2] Science **356**, 837 (2017) Boss *et al.* (ETH)

[3] Nature **555**, 351 (2018) Glenn *et al.* (Harvard)

[4] Science **357**, 67 (2017) Aslam *et al.* (Stuttgart)

[5] Nature Commun. **10**, 594 (2019) Pfender *et al.* (Stuttgart)

[6] Nature **571**, 230 (2019) Cujia *et al.* (ETH)

[7] Phys. Rev. B **98**, 121405 (2018) Sasaki *et al.* (Keio)

[8] Phys. Rev. Lett. **121**, 170801 (2018) Zopes *et al.* (ETH)

[9] Nature **576**, 411 (2019) Abobeih *et al.* (Delft)

[10] arXiv:2103.10669 Cujia *et al.* (ETH)

[11] Phys. Rev. Lett. **113**, 197601 (2014) Sushkov *et al.* (Harvard)

[12] Appl. Phys. Lett. **117**, 114002 (2020) Sasaki *et al.* (Keio)