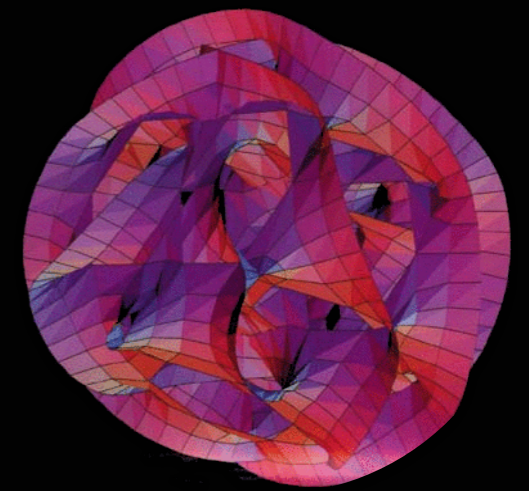
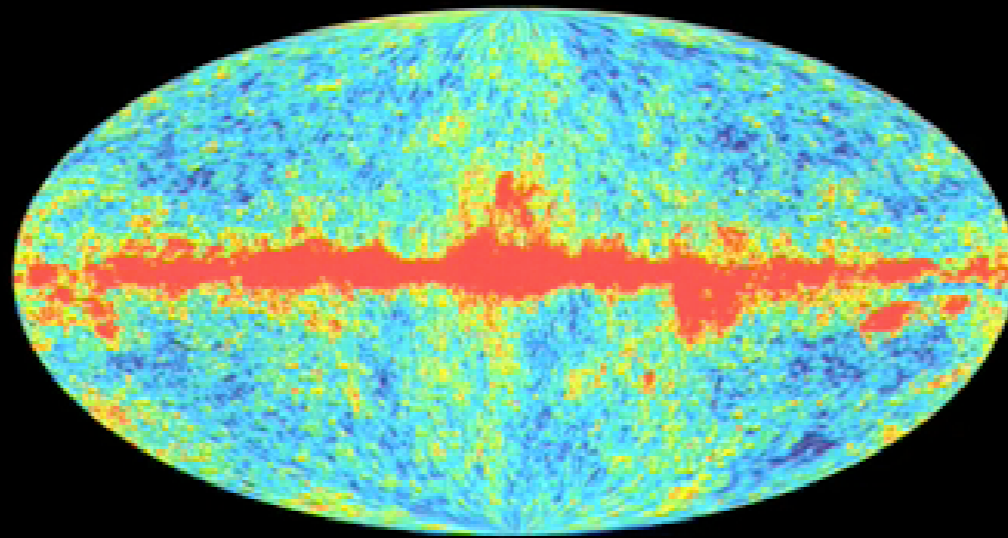
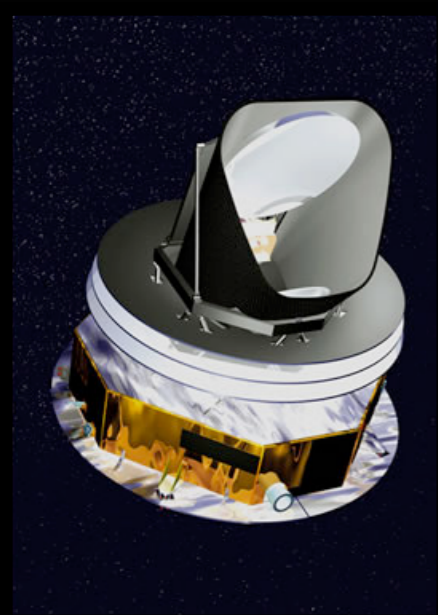


# Ultra-light particles & the cosmic microwave background

Daniel Grin  
Haverford College  
Copernicus Webinar  
*3/3/2023*



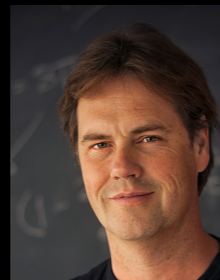
# Ultra-light particles & the cosmic microwave background

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# COLLABORATORS

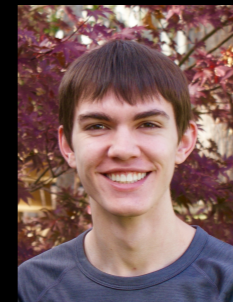
R.Hložek, D.J. E. Marsh, P.Ferreira, J. Dunkley, E. Calabrese, R.Allison, A. Jaffe, G. Farren



T. L. Smith, V. Poulin, M. Kamionkowski H. Tohfa, J. Crump, E. Baker



E. Trott, D. Zegeye, T. Cookmeyer



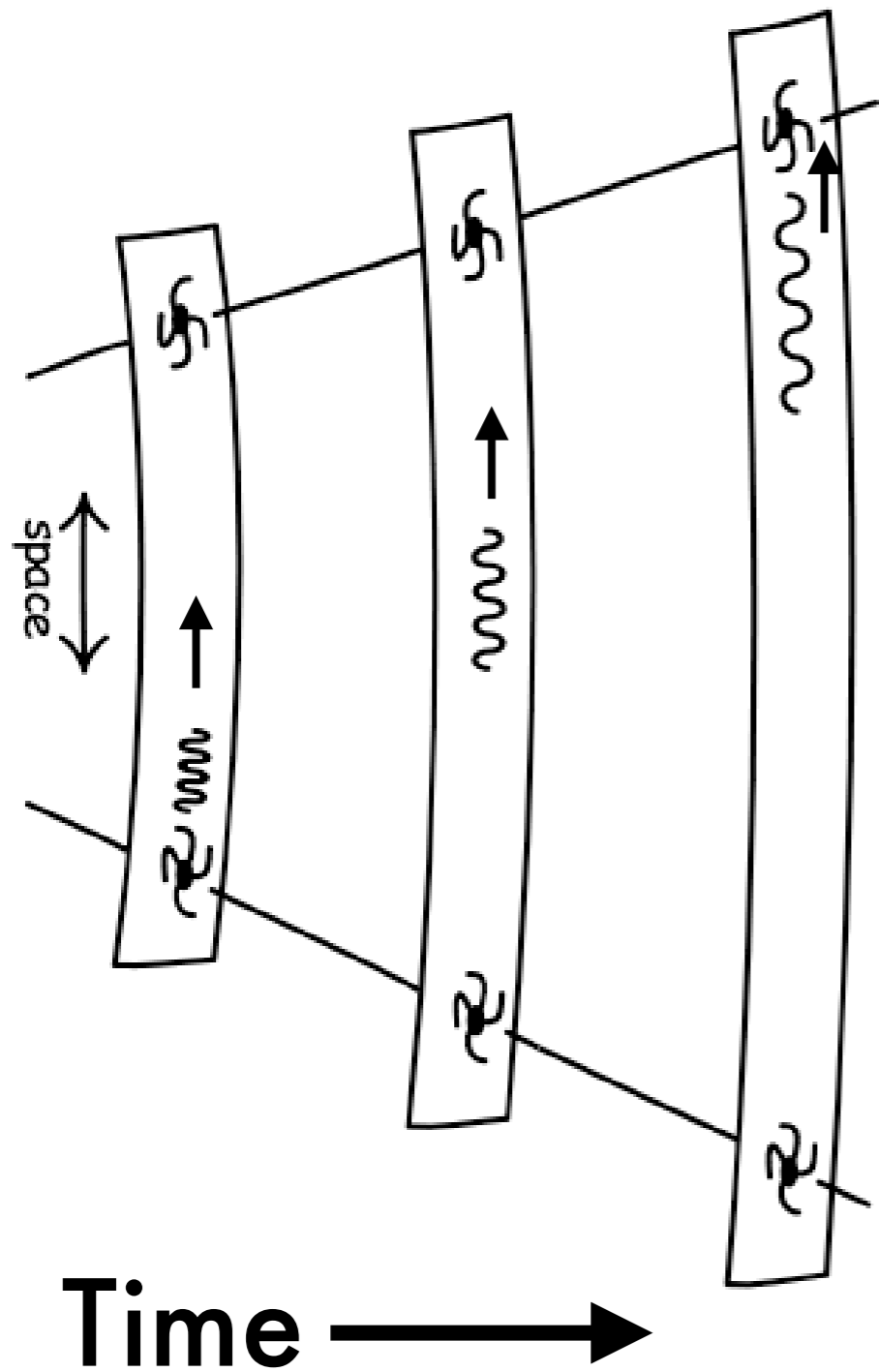
S. Singh, D. Wilson, J. Manley, J. Betz, M. Chowdhury



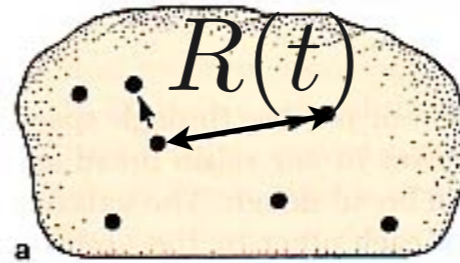
# Outline

- \* Quick intro to CMB, ULA, etc review
- \* Microwave tests of ultra-light axion dark matter
  - \* Primary CMB anisotropies
  - \* Lensing & Large-scale structure
  - \* Bulk flows
- \* Light scalars and varying fundamental constants

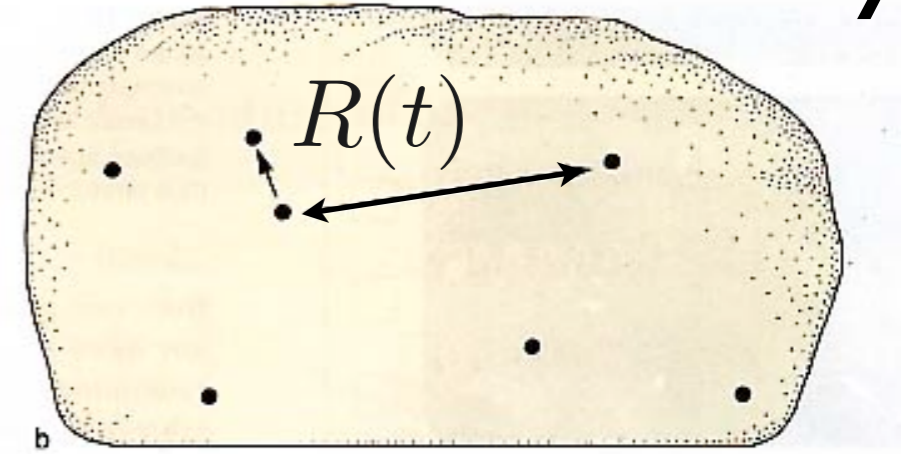
# The expanding universe



Past



Today



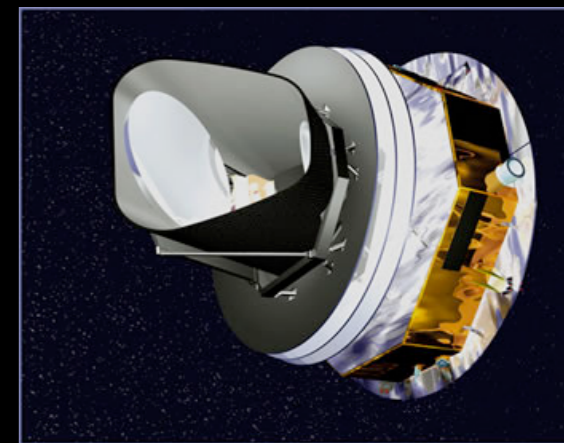
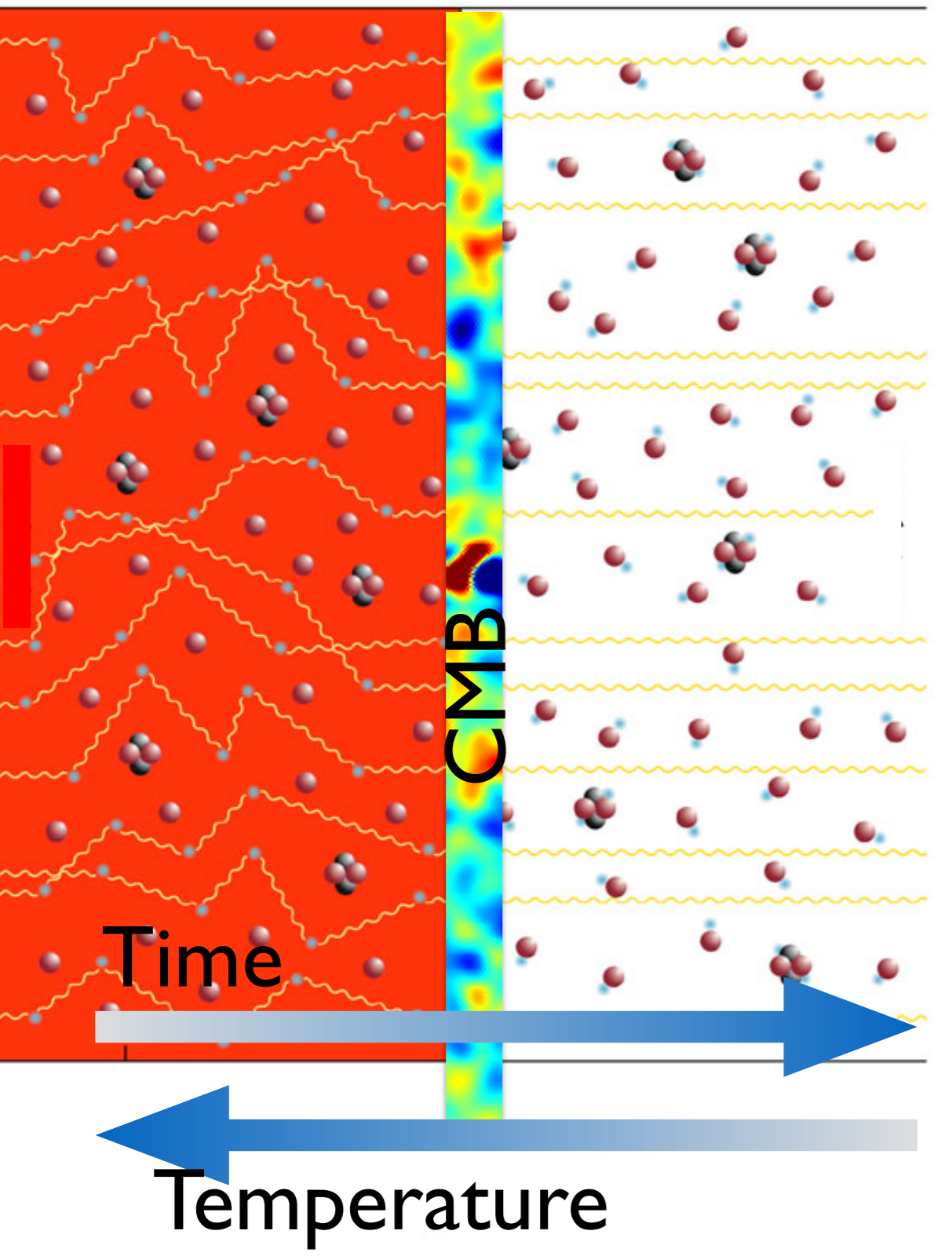
With expansion

$$z = \frac{\lambda_{\text{observed}}}{\lambda_{\text{emitted}}} - 1$$



# What are we looking at?

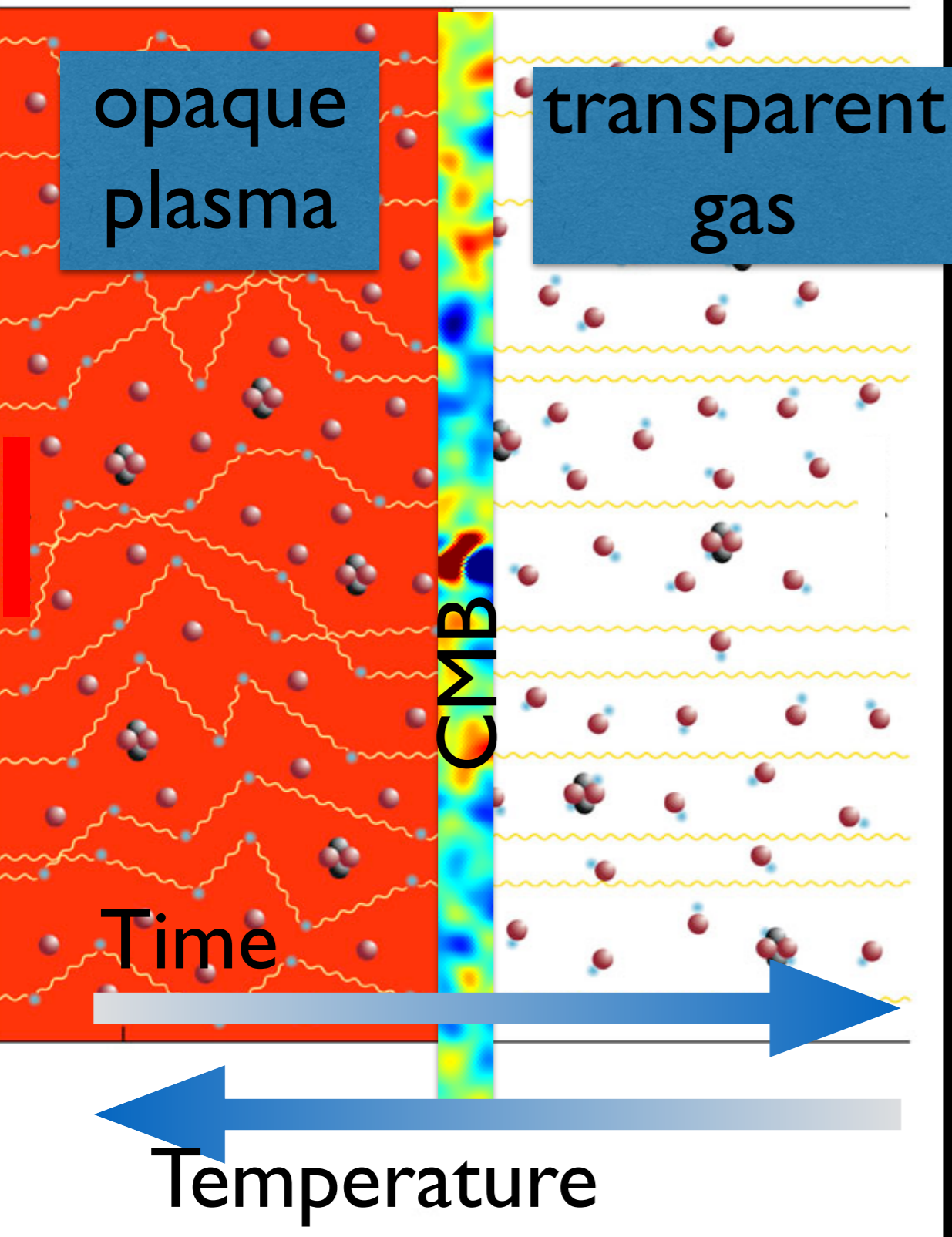
Image credit (Addison Wesley 2004)





# What are we looking at?

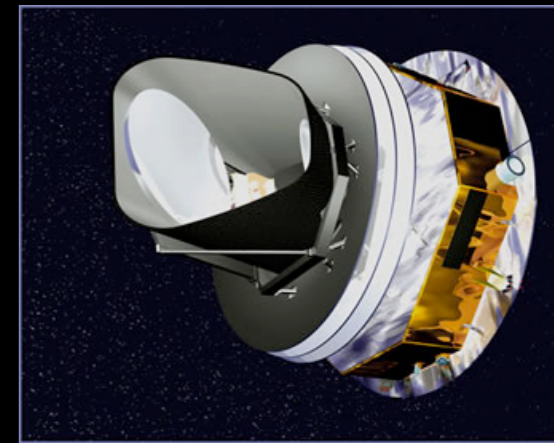
Image credit (Addison Wesley 2004)



**'RECOMBINATION':**

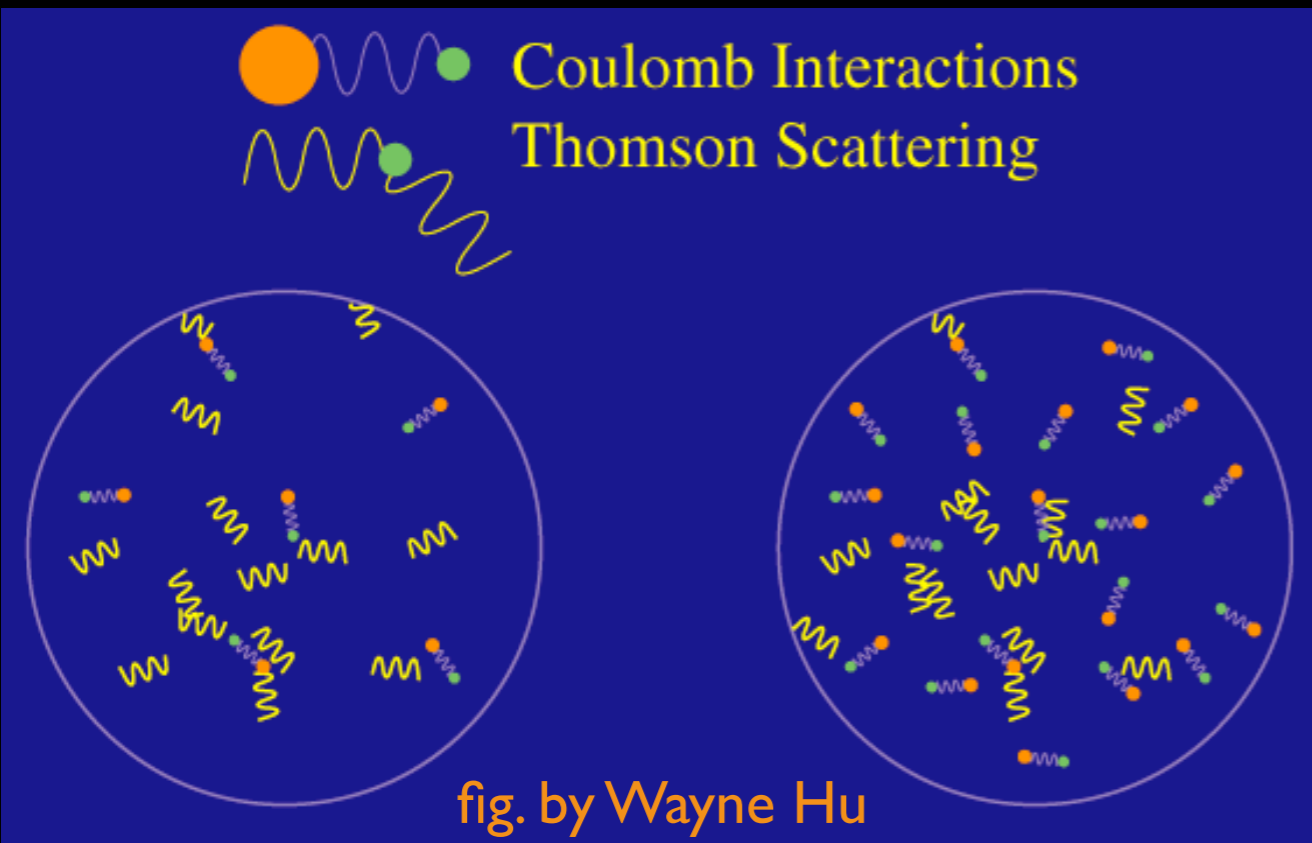
**FIRST H ATOMS**

**$z \sim 1100$ ,  $t \sim 380,000$  years**

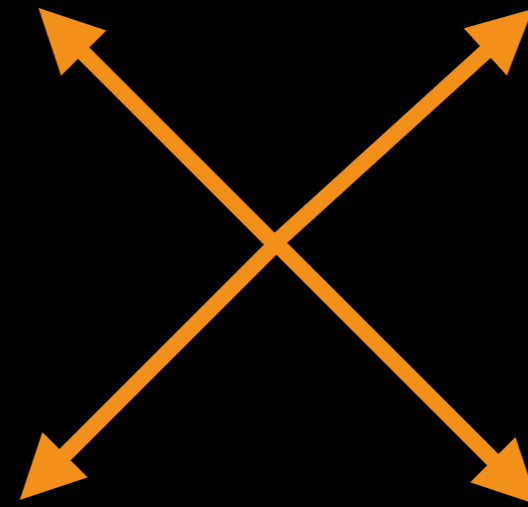


# Sound waves!

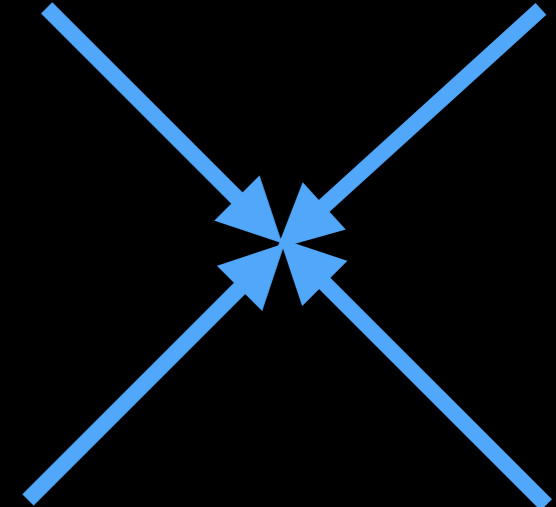
\* Photons, protons, electrons move together



Radiation pressure

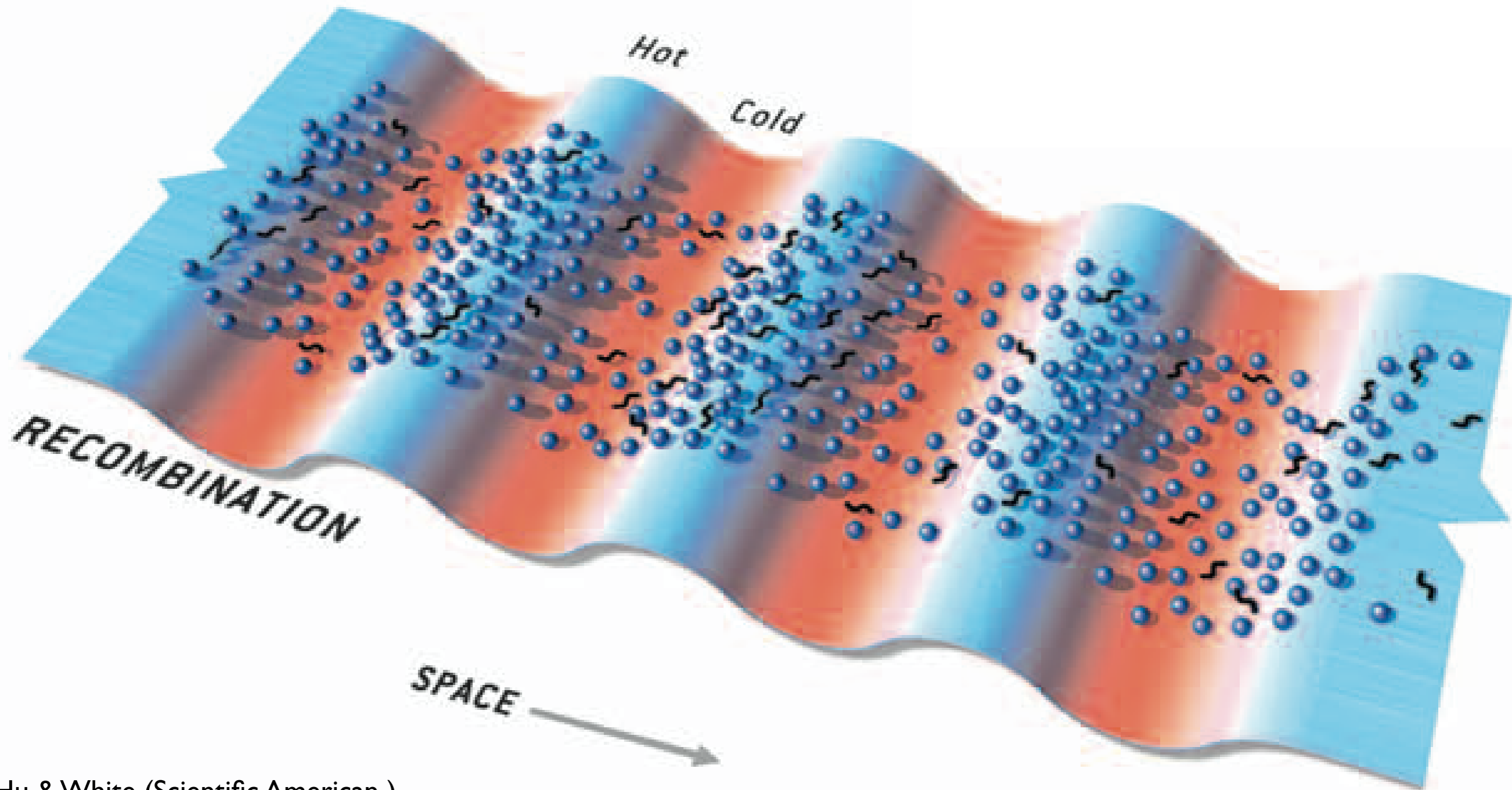


Gravity



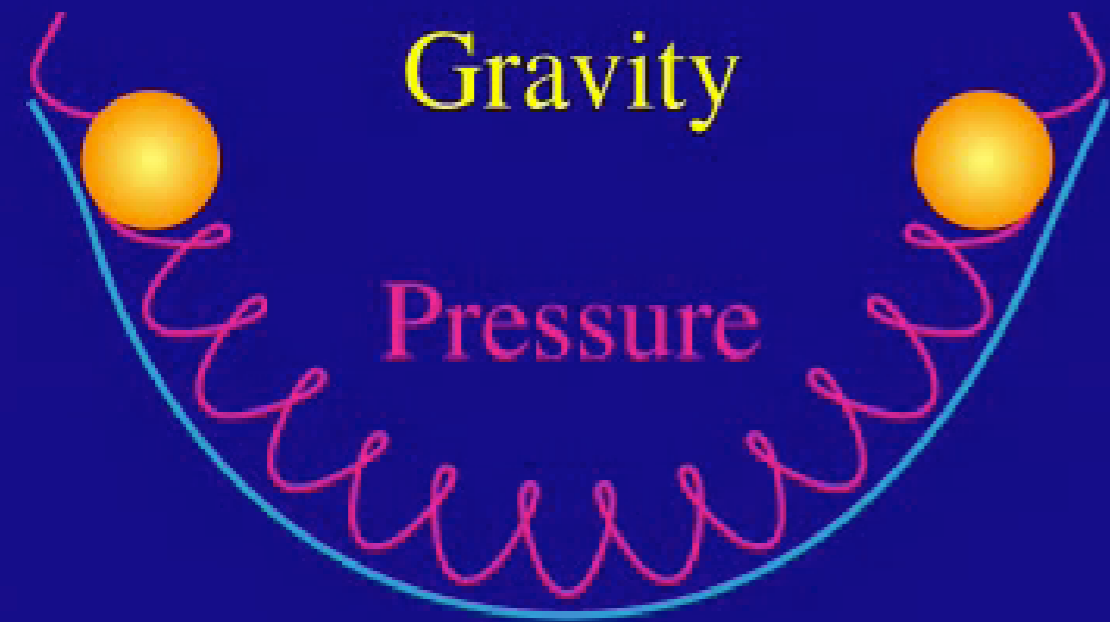
# Sound waves!

✦ Photons, protons, electrons move together



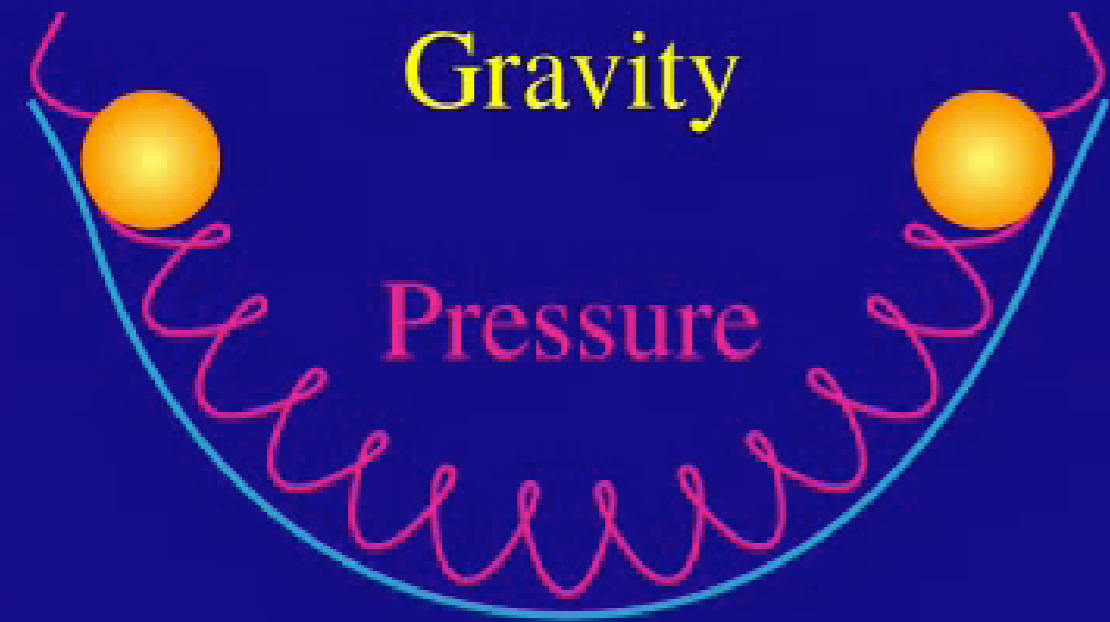
Hu & White (Scientific American )

# Snapshot and geometry

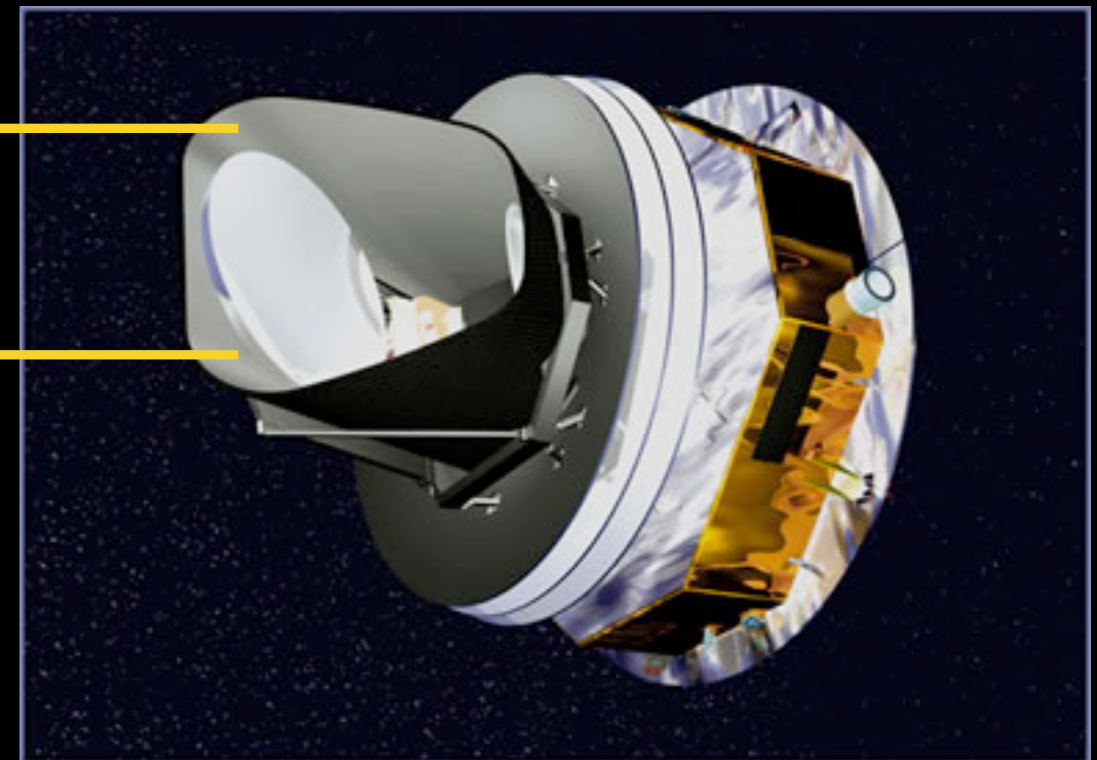
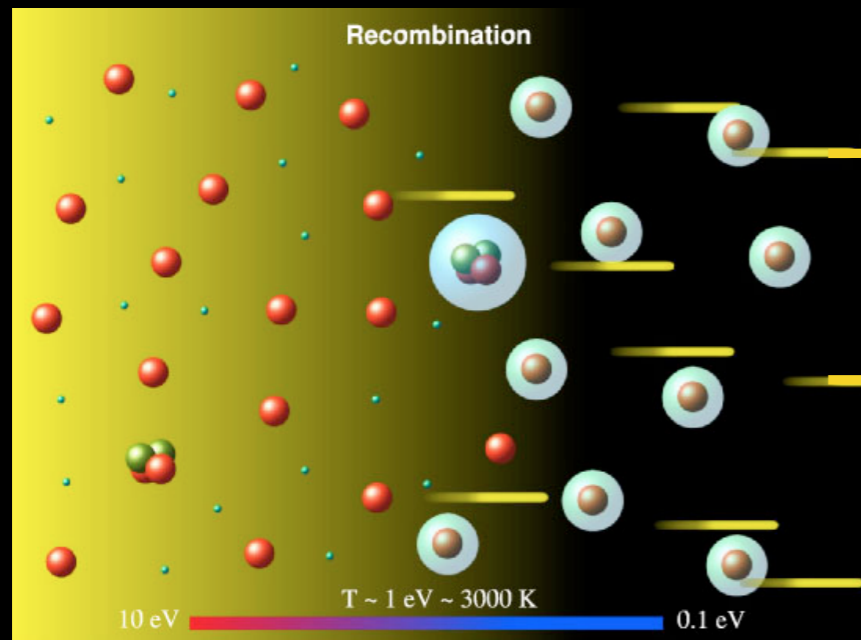
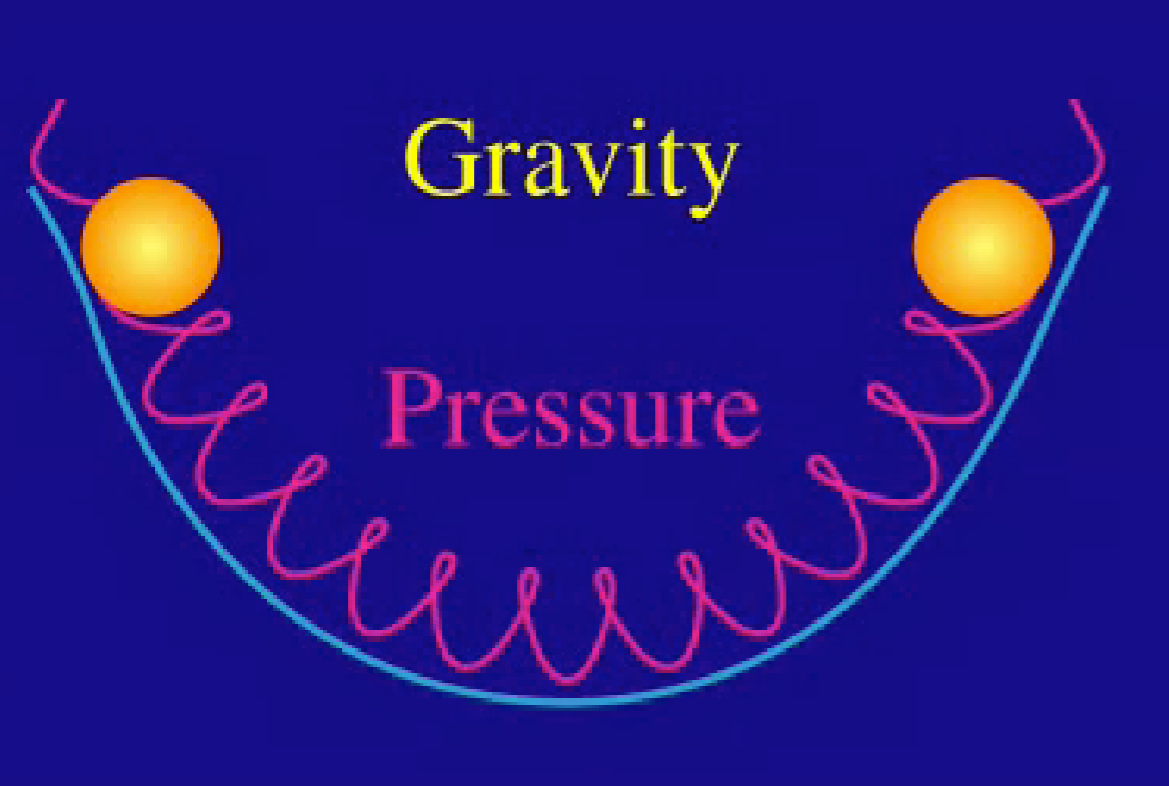




# Snapshot and geometry

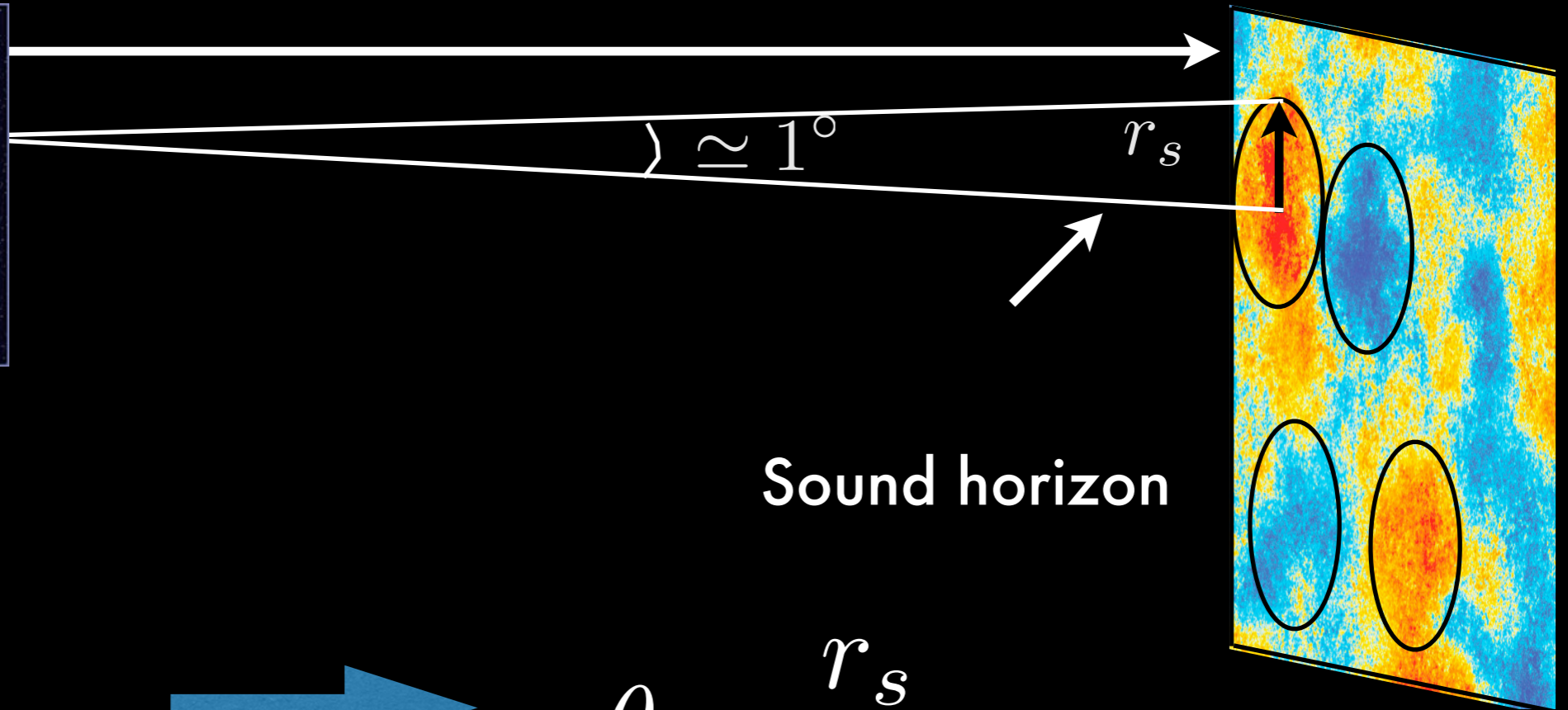
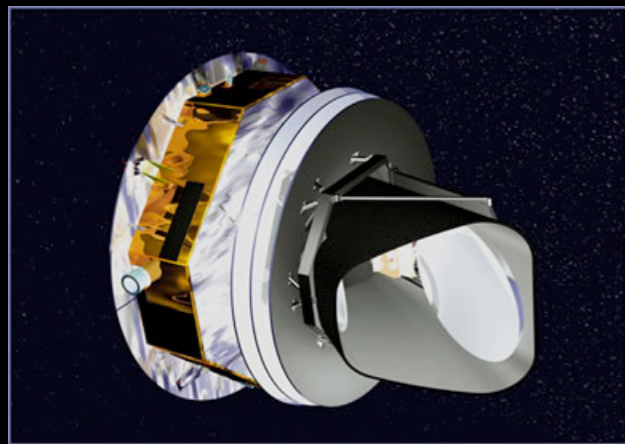


# Snapshot and geometry



# Snapshot and geometry

$D$  ( sensitive to any energy source)



Sound horizon

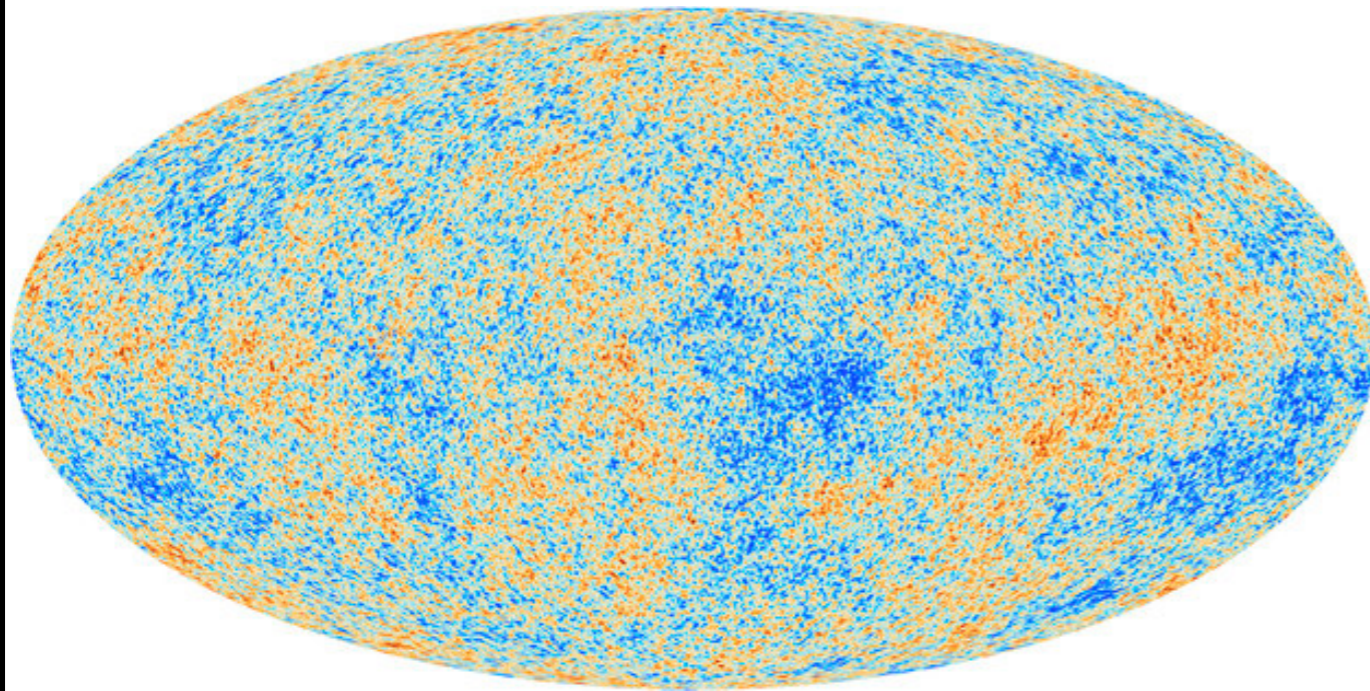
$$\theta = \frac{r_s}{D}$$

*Modified figure from T. Smith  
used with permission*

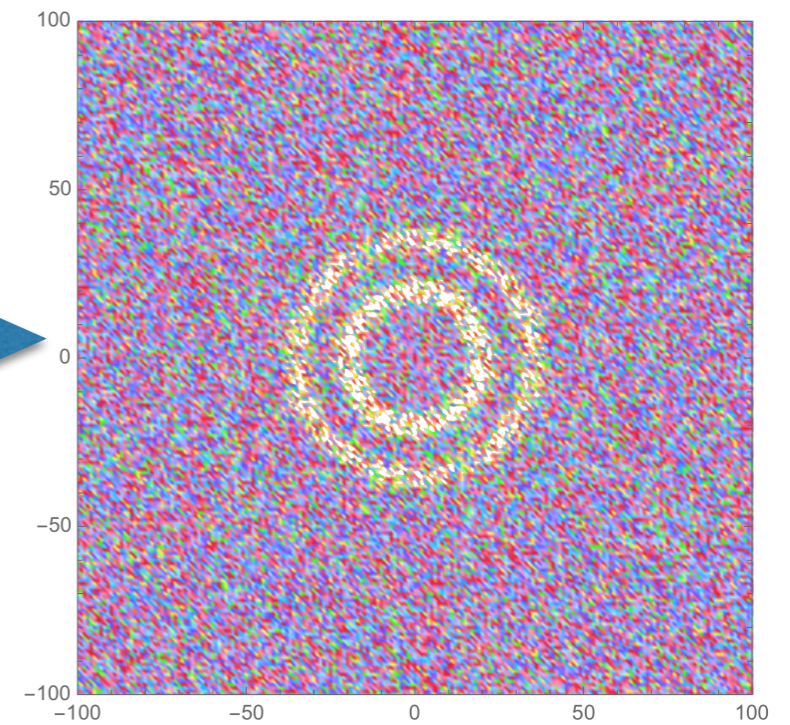
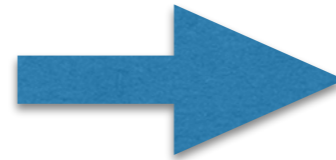


# Fourier analysis of primordial sound

$$T(\vec{\theta})$$



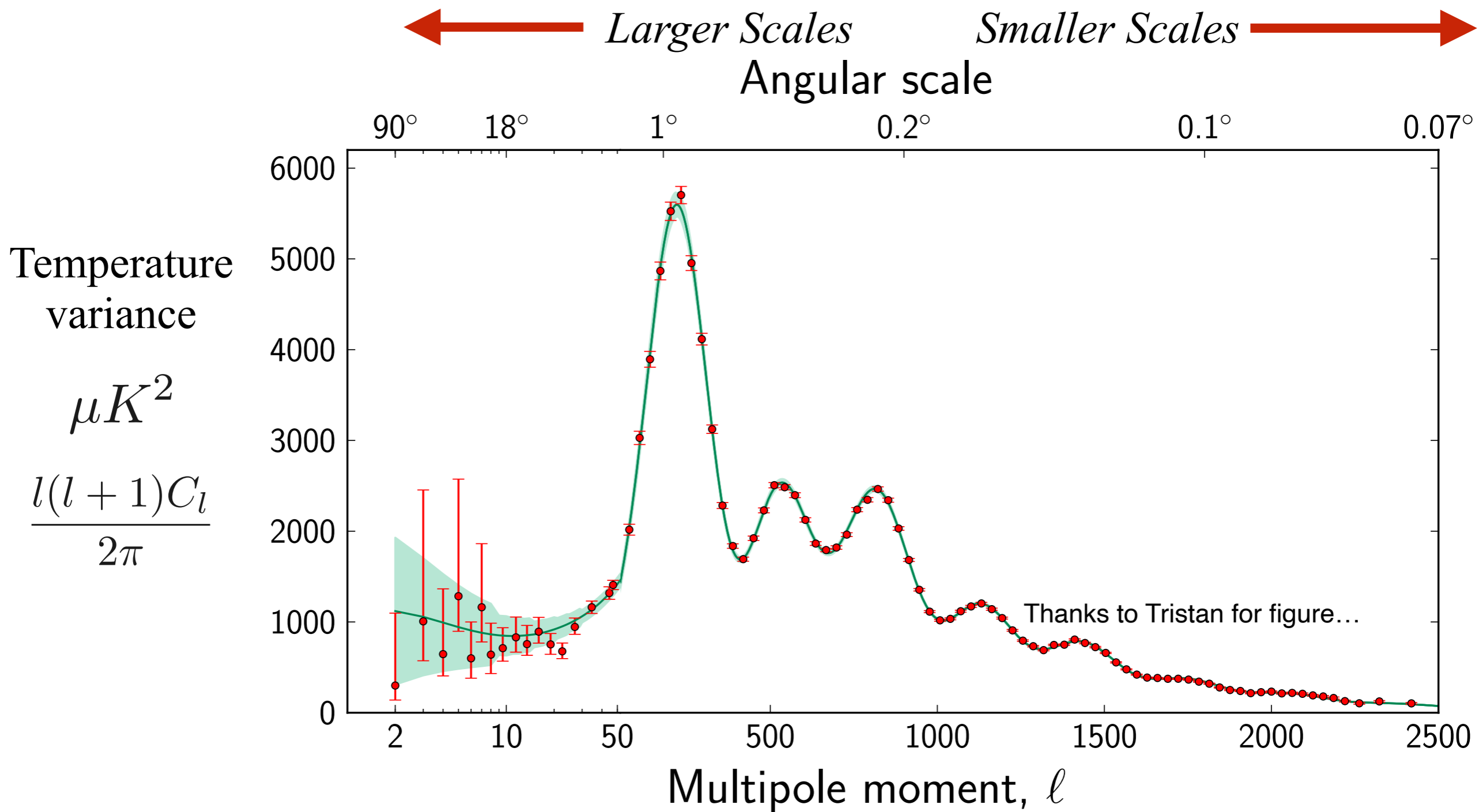
$$a(\vec{k}) = \int T(\vec{\theta}) e^{i\vec{\theta} \cdot \vec{k}} d^2\theta$$



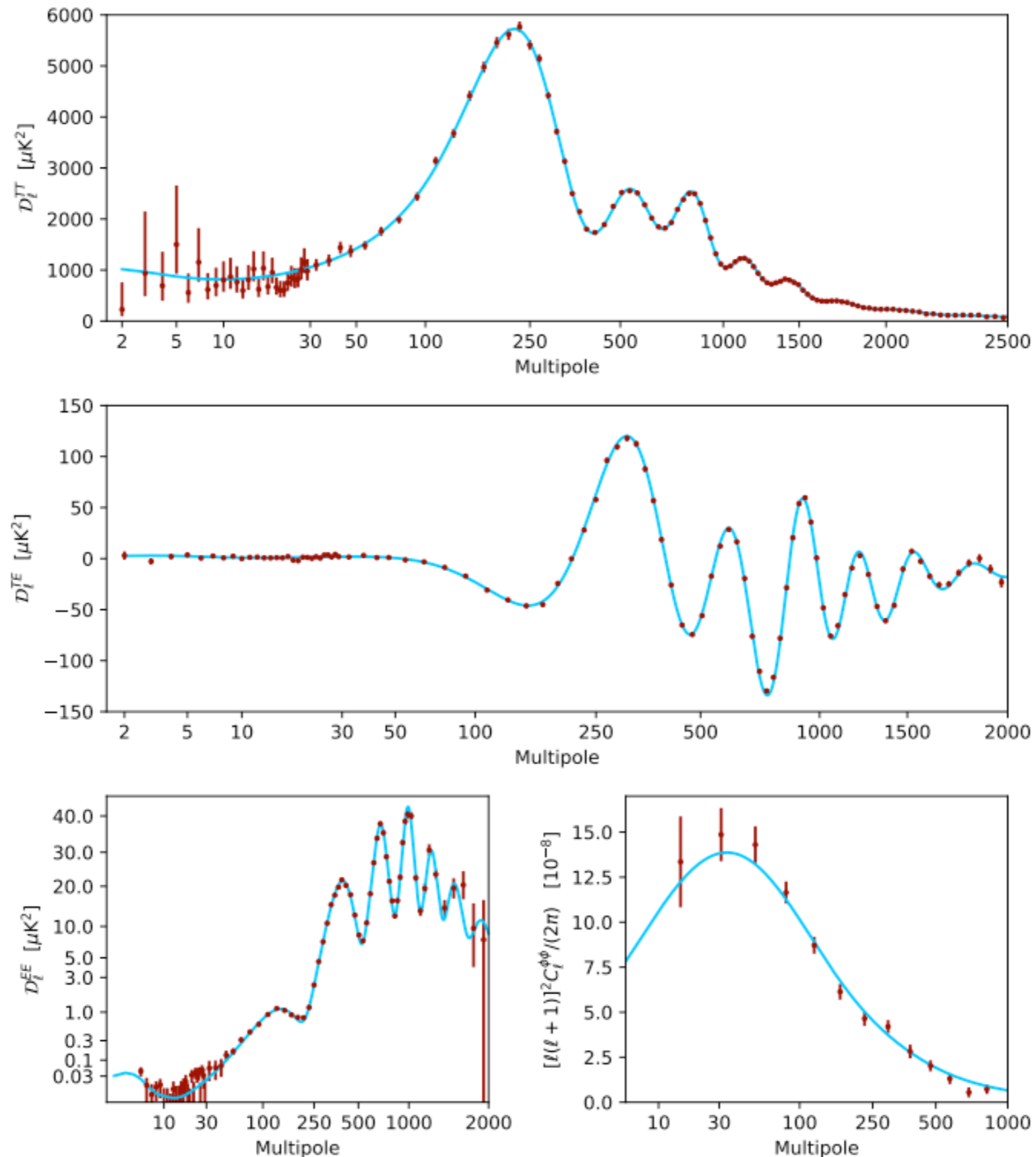
Thanks to Tristan for figure...



# Fourier analysis of primordial sound

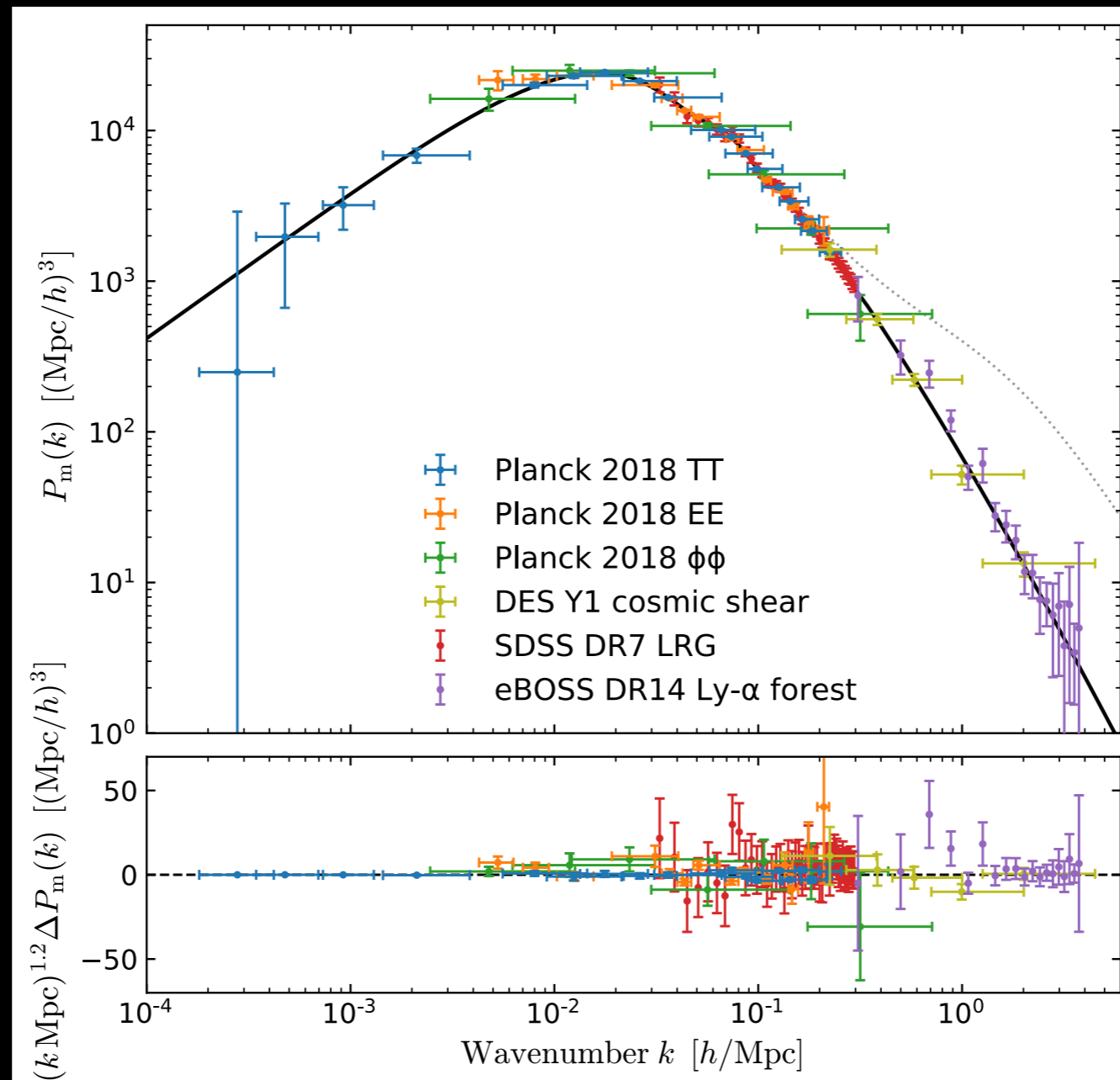


# Era of precision cosmology!



*A&A 641, A1 (2020), Planck 2018 data*

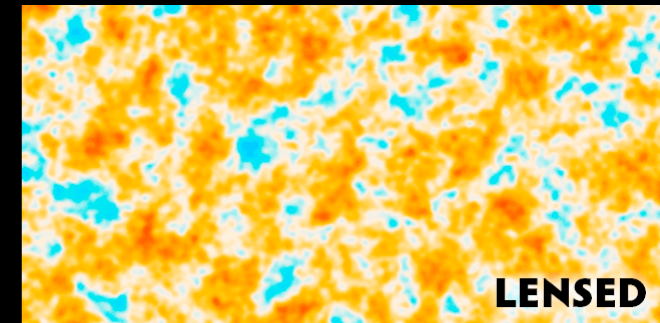
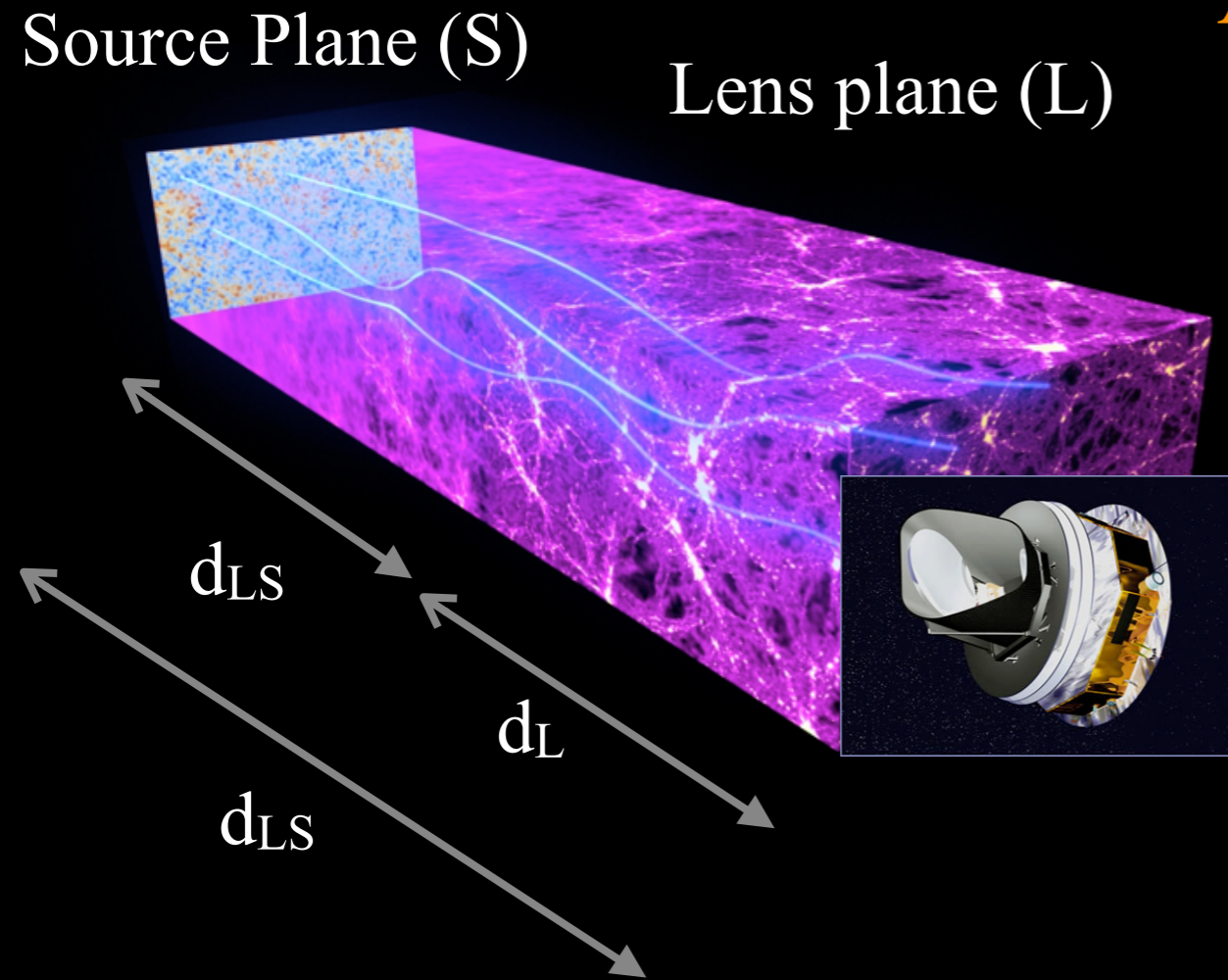
# Galaxy clustering observations



*Chabanier et al. 2019, MNRAS 489, p2247*

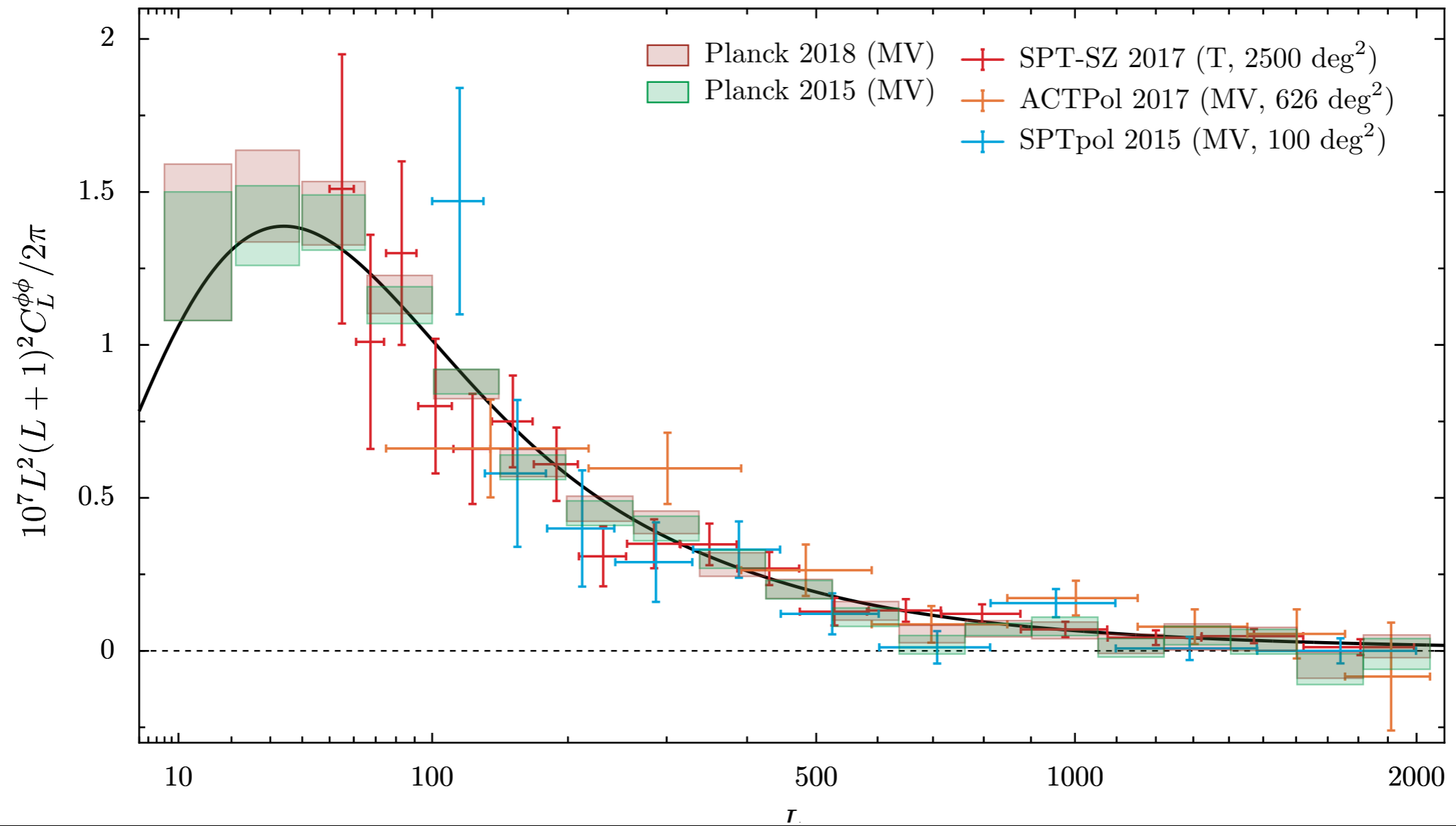
# LENSING

A slice of (dark matter) life at  $z \sim 1$





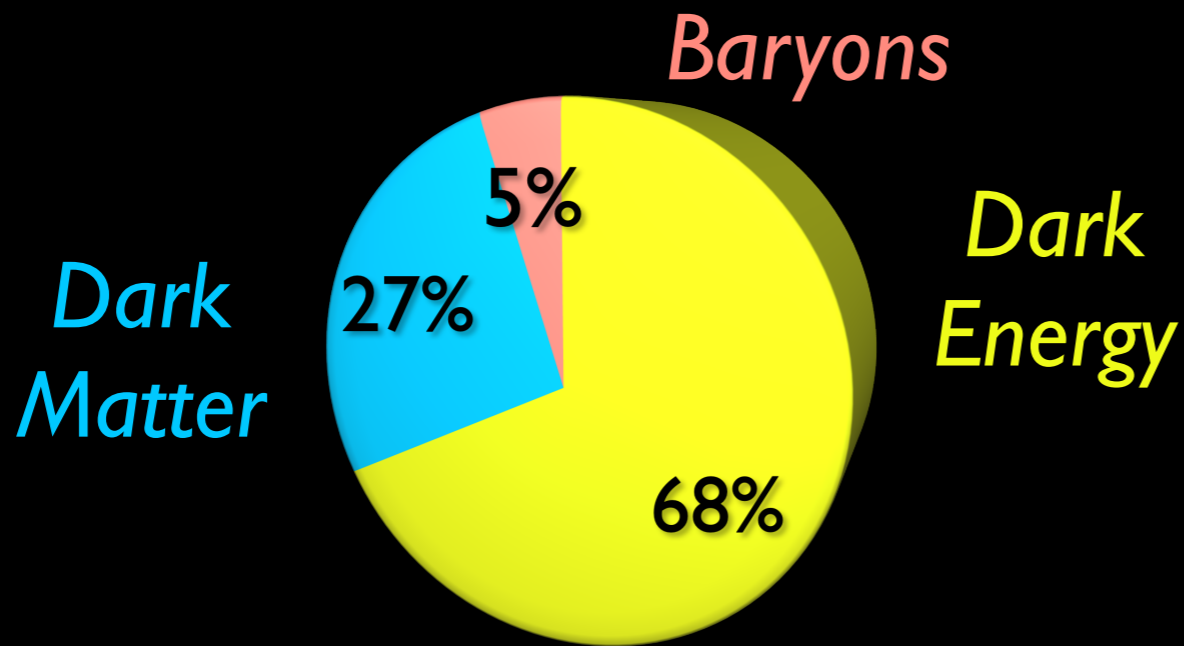
# LENSING



arXiv: 1807.06210

40 $\sigma$  detection!

# Cosmic energy budget



$\Omega_b h^2$	$.02237 \pm 0.00015$
$\Omega_c h^2$	$.1200 \pm 0.0012$
$\Omega_\Lambda$	$0.6847 \pm 0.0073$

5% baryonic matter: protons, electrons, atoms

\*“stuff we know”

27% cold dark matter (CDM)

\*Primordially non-relativistic non-interacting ‘gas’

\*Assume no scattering/interaction with standard model particles

68% dark energy

# Cosmic energy budget

$\Omega_b h^2$	$.02237 \pm 0.00015$
$\Omega_c h^2$	$.1200 \pm 0.0012$
$\Omega_\Lambda$	$0.6847 \pm 0.0073$

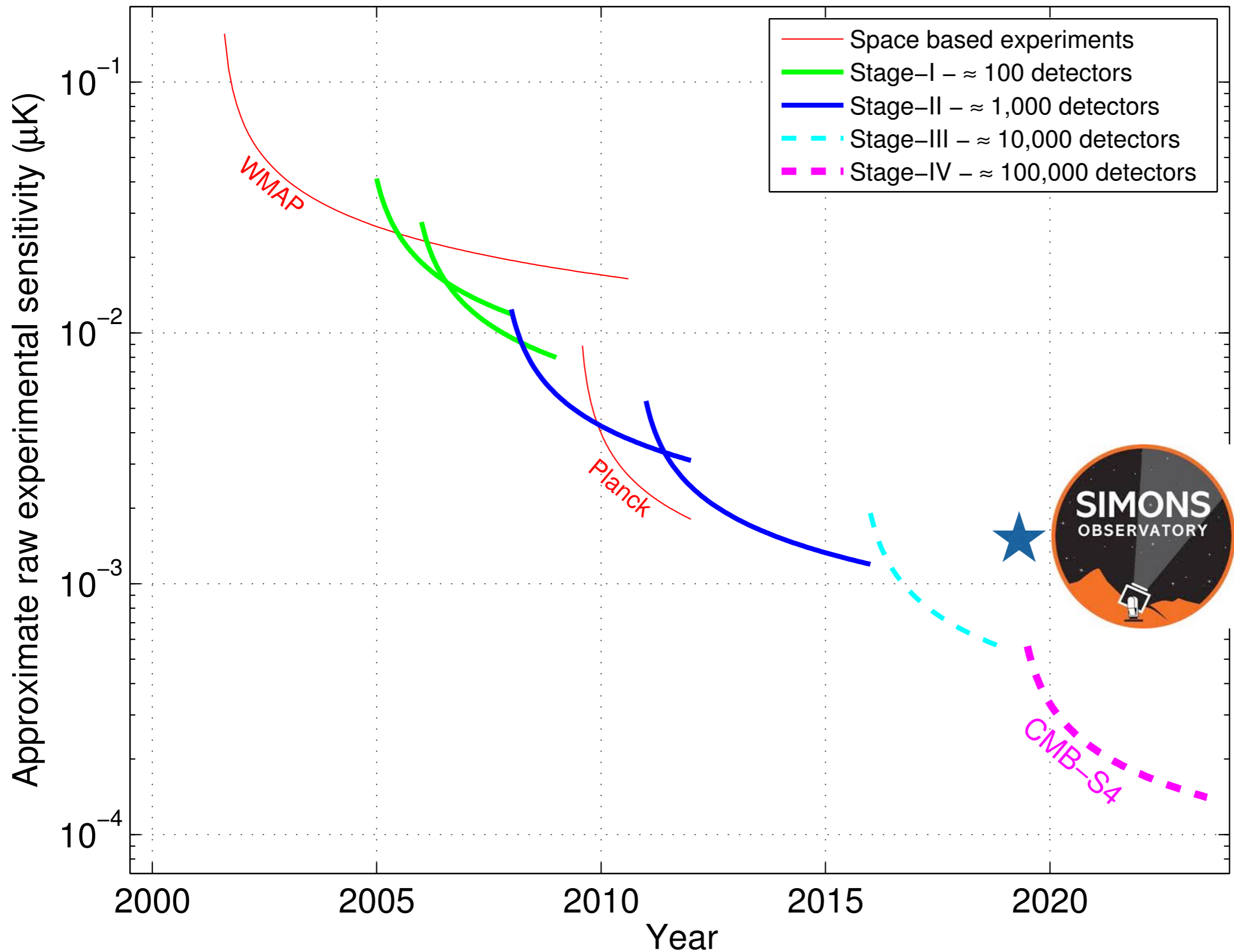


- \* Next gen. CMB ground-based expt. concept
  - \*  $\sim 1$  arcmin beam
  - \*  $1 \mu\text{K}$  arcmin noise level
  - \*  $\sim 500,000$  detectors
  - \* Location, sky coverage TBD

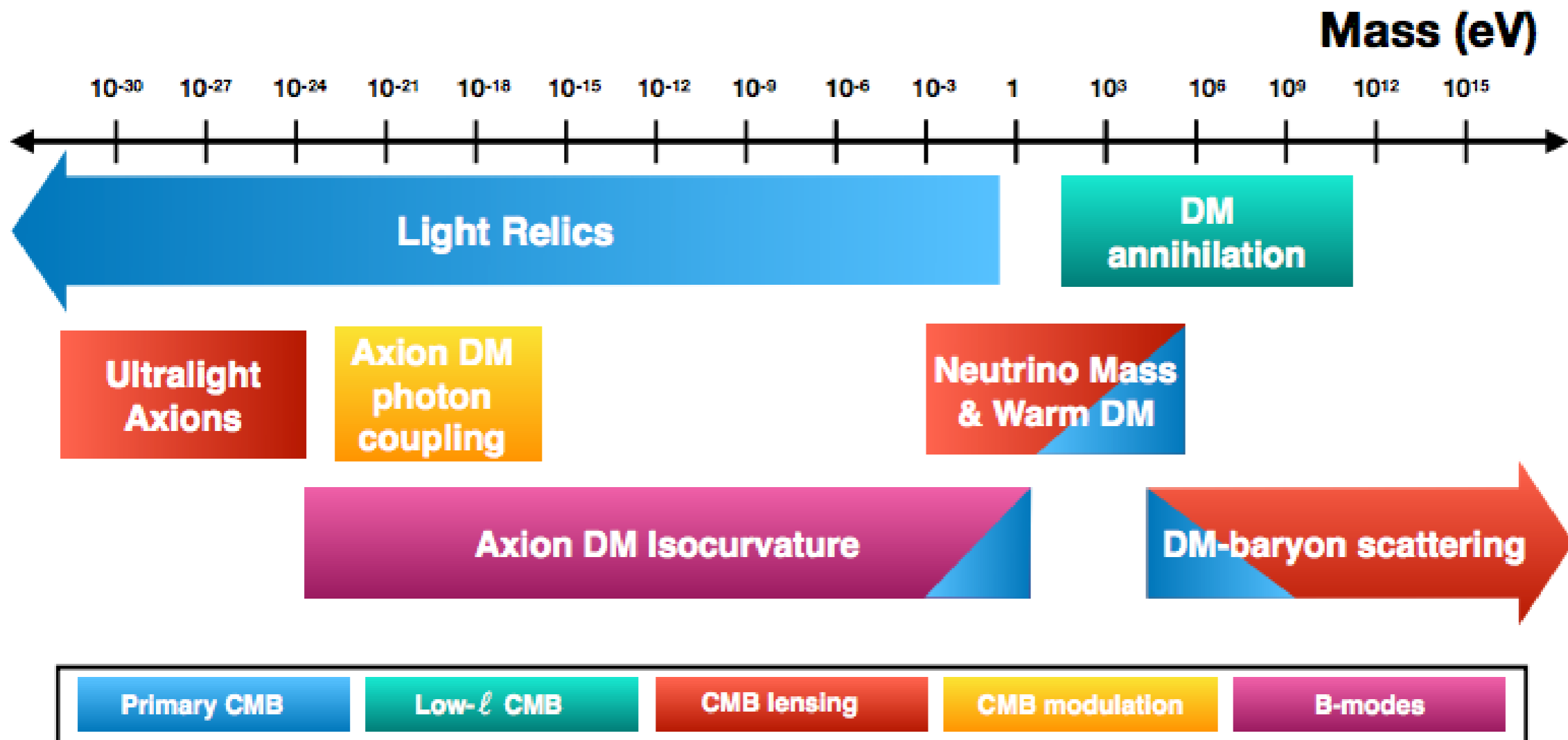
From CMB-S4 Science book... [arXiv: 1610.02743](https://arxiv.org/abs/1610.02743)



# FUTURE CMB EXPERIMENTS

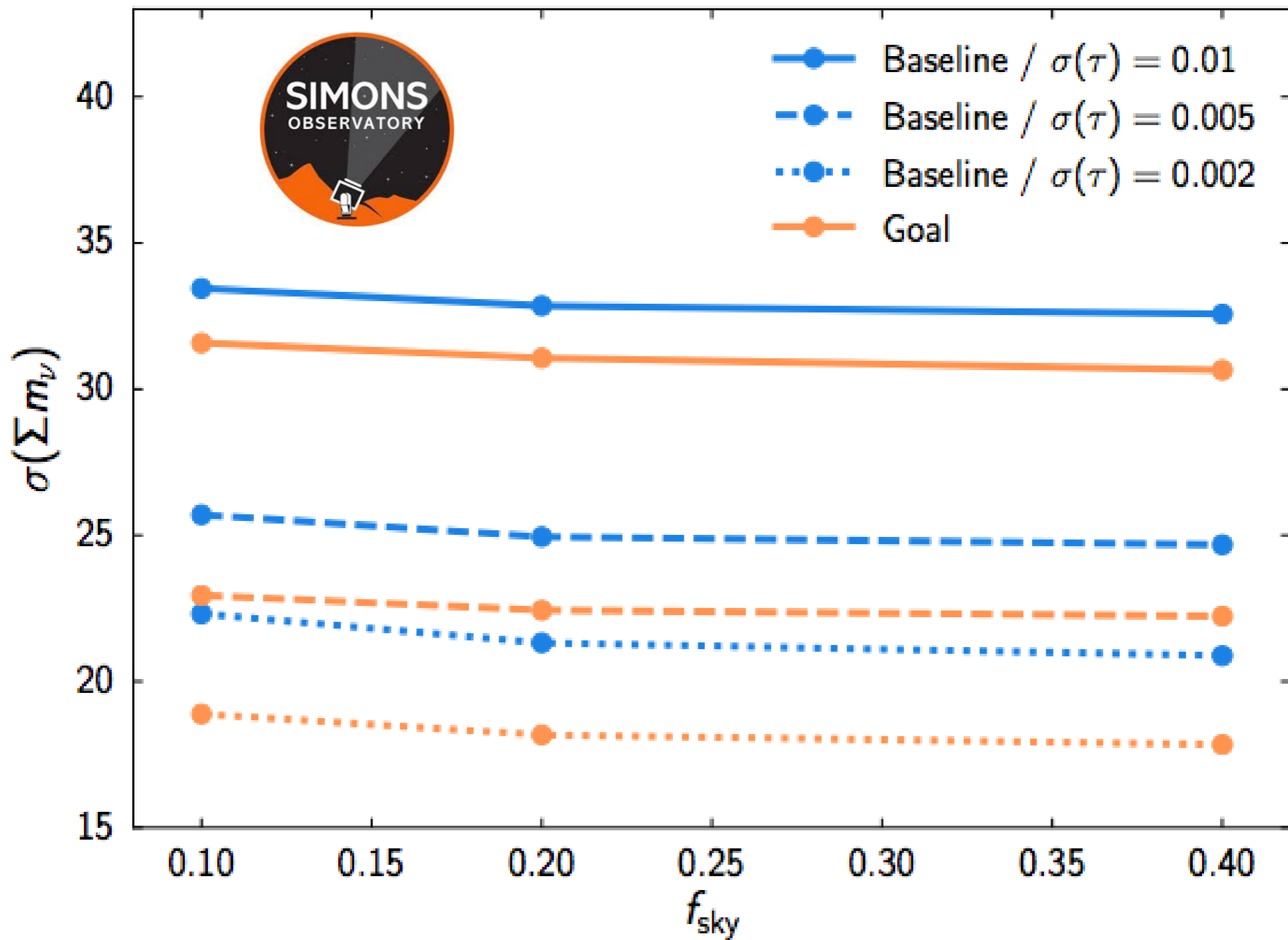


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From CMB-S4 Science book... arXiv: 1610.02743

# FUTURE CMB EXPERIMENTS



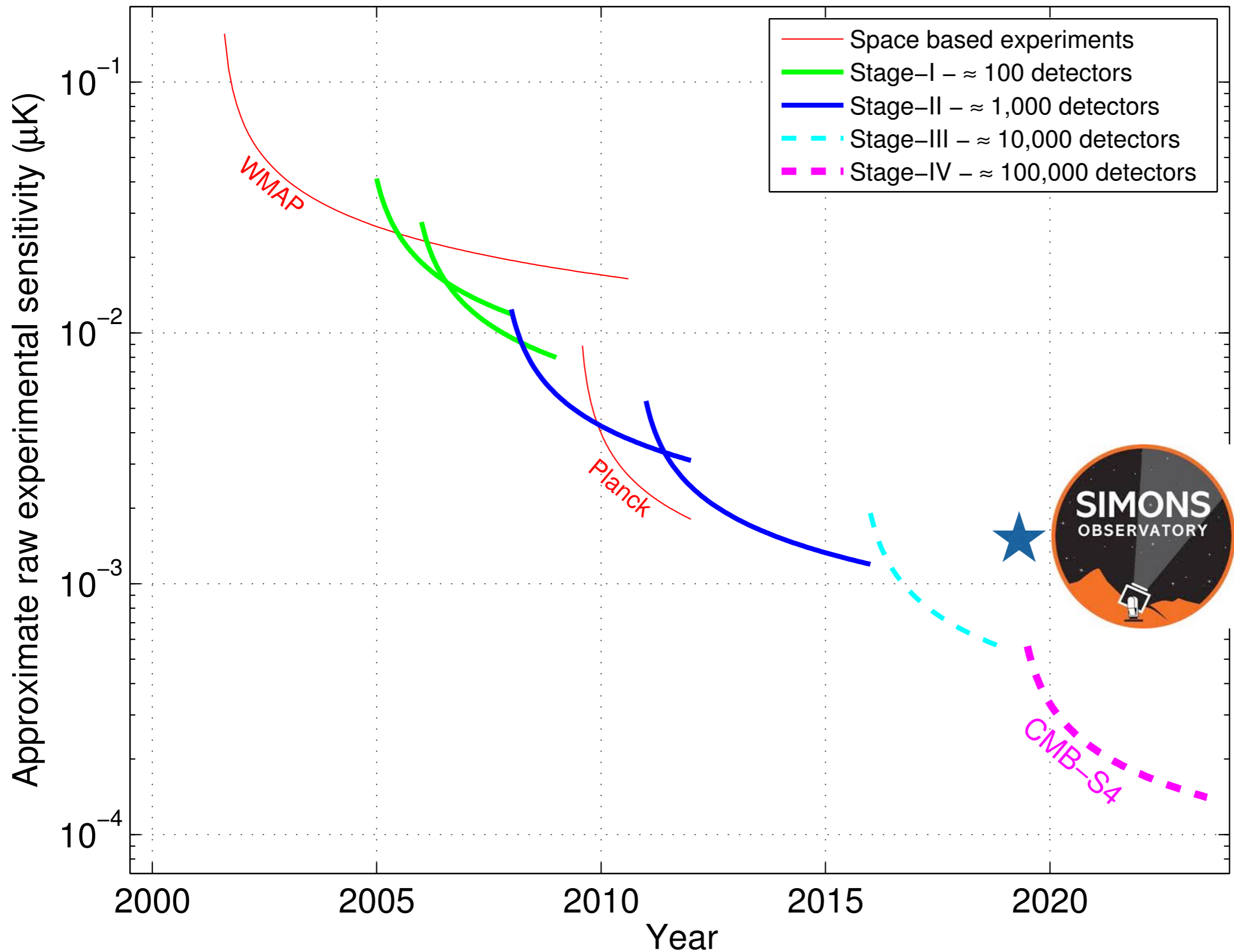


- \* Next gen. CMB ground-based expt. concept
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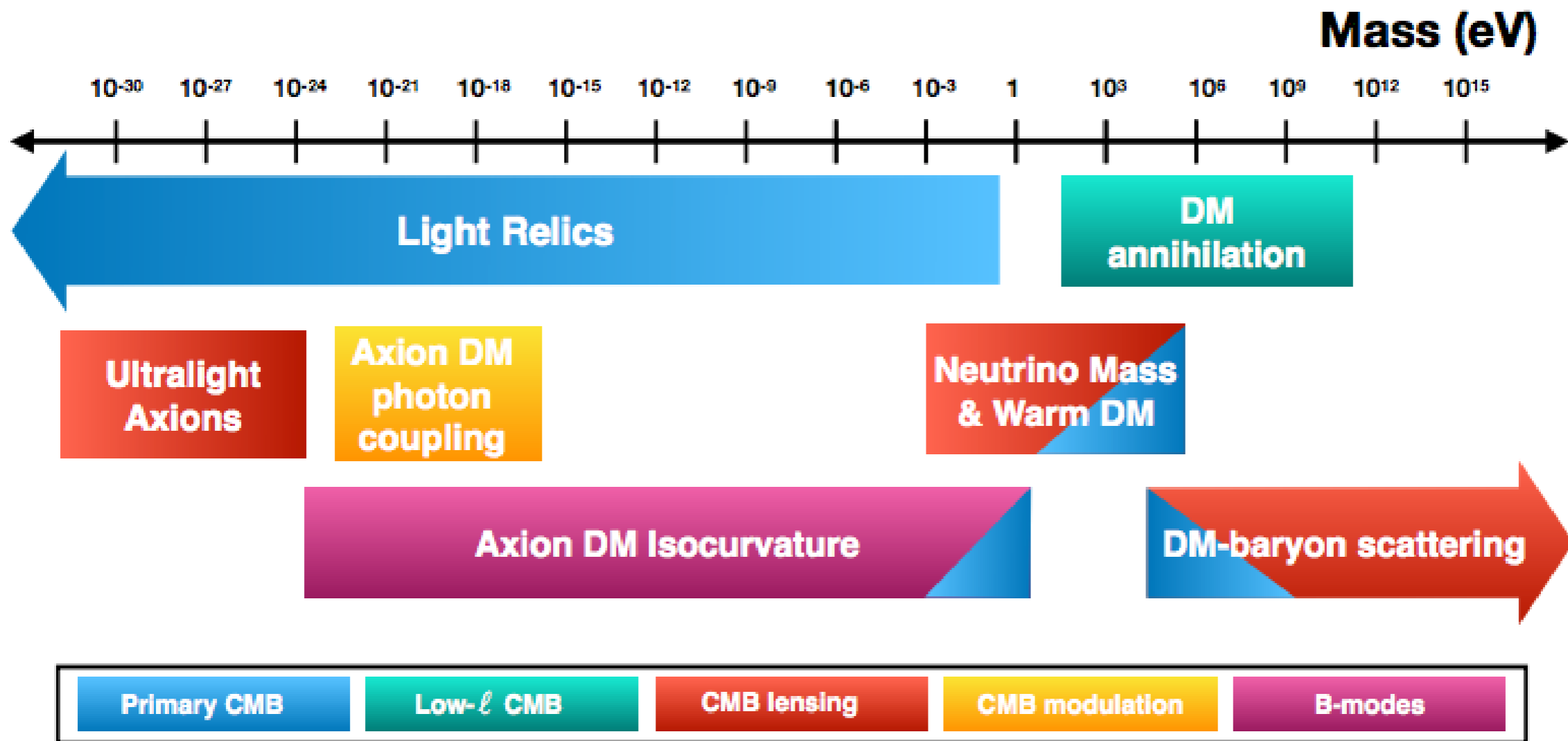
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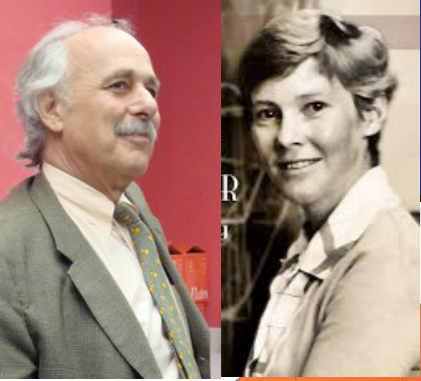


# FUTURE CMB EXPERIMENTS

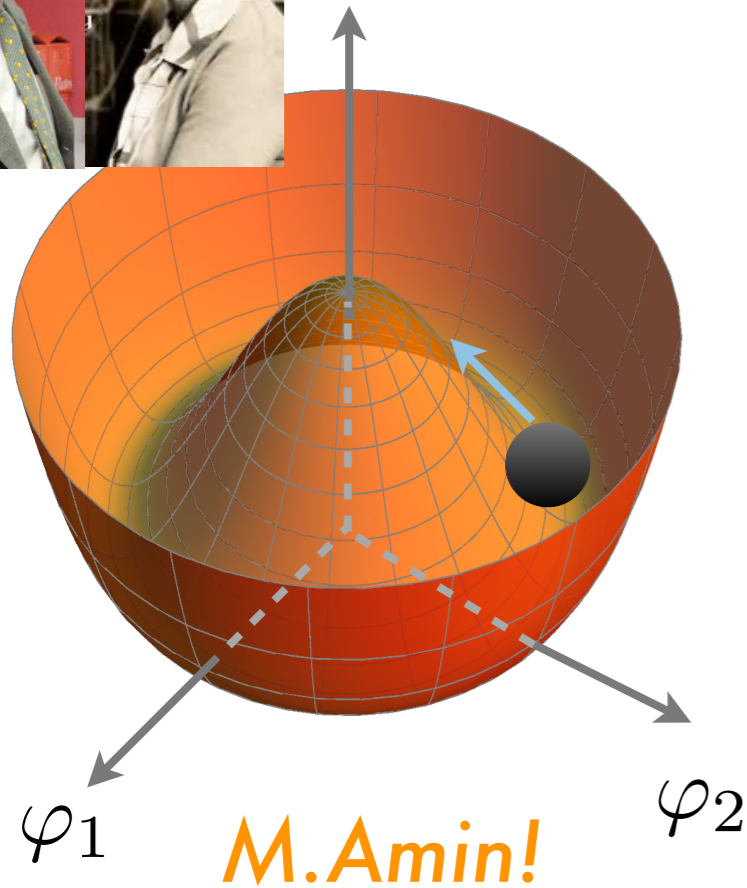


From CMB-S4 Science book... arXiv: 1610.02743

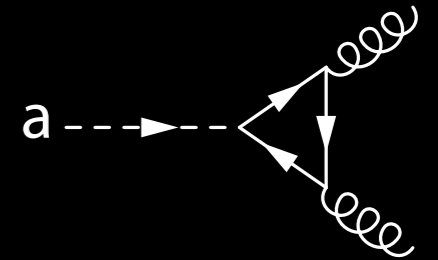
# What are axions?



*New scalar field with global U(1) symmetry!*



$$\mathcal{L}_{\text{CPV}} = \frac{\theta g^2}{32\pi^2} G\tilde{G} - \frac{a}{f_a} g^2 G\tilde{G}$$



\* Weakly couples to SM gauge fields (via fermions)

$$\mathcal{L} \propto \frac{1}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

\* Axion gets mass through non-perturbative QCD effects

$$m_a \sim \frac{\Lambda_{\text{QCD}}^2}{f_a}$$

*Peccei + Quinn (1977), Weinberg +Wilczek (1978), Kim (1979), Shifman et. al (1980), Zhitnitsky (1980), Dine et al. (1981), D.B. Kaplan (1985), A.E Nelson (1985,1990)*

# Axions

## \*Maxwell's equations

$$\nabla \cdot \vec{E} = 4\pi\rho_e$$

Gauss's Law

$$\vec{\nabla} \times \vec{B} - \partial_t \vec{E} = 4\pi\vec{J}_e$$

Ampere's Law



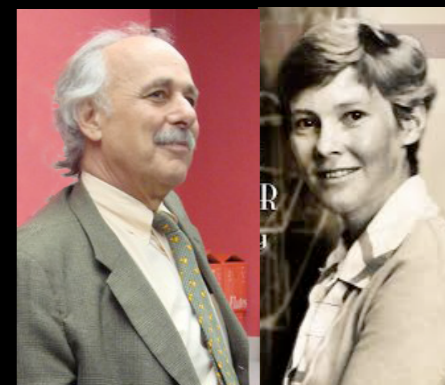
# Axions

\*Maxwell's equations

+New physics

(Peccei/Quinn 1977)

$$\nabla \cdot \vec{E} = 4\pi\rho_e + \frac{\vec{\nabla} a(\vec{x}) \cdot \vec{B}(\vec{x})}{f_a}$$



$$\vec{\nabla} \times \vec{B} - \partial_t \vec{E} = 4\pi \vec{J}_e - \frac{1}{f_a} \left( \vec{B} \partial_t a(\vec{x}) + \vec{\nabla} a(\vec{x}) \times \vec{E} \right)$$

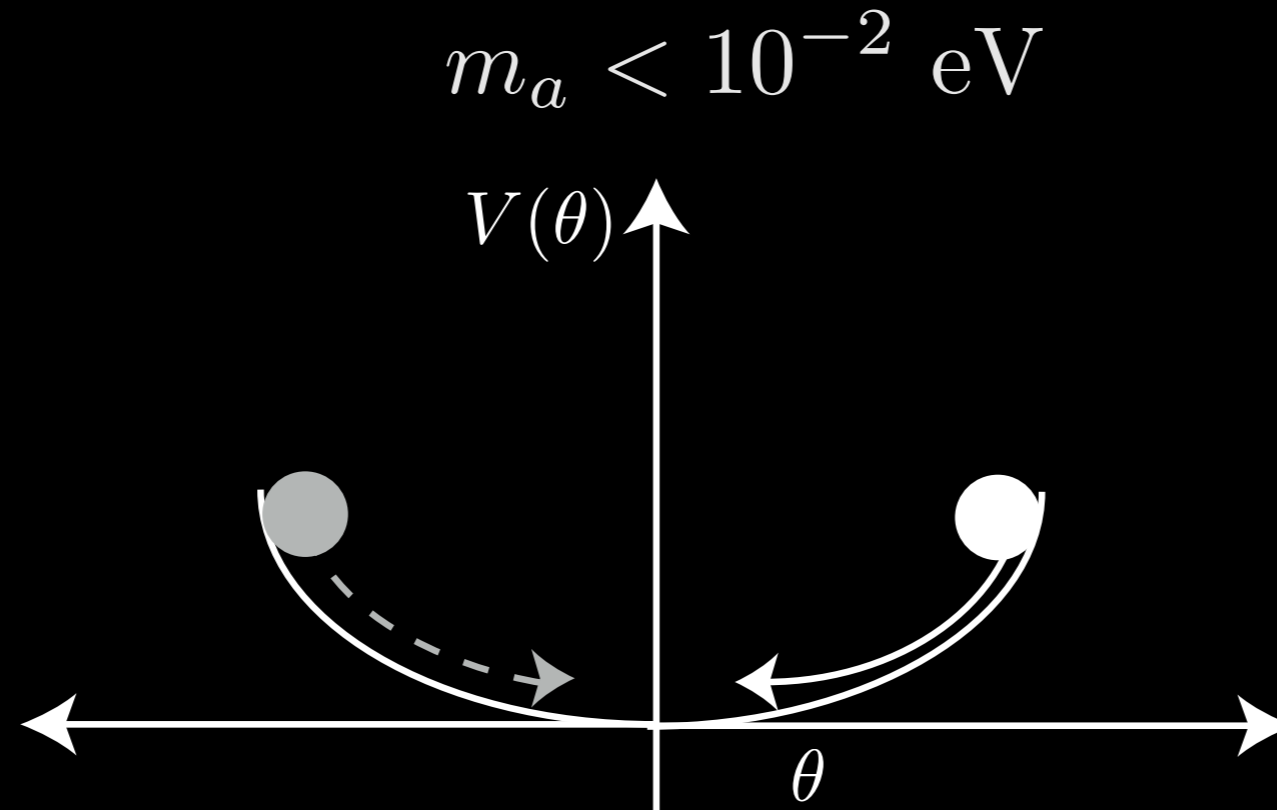
\*A new fundamental field

$$a(\vec{x})$$

$$\partial_t^2 a(\vec{x}) - \nabla^2 a(\vec{x}) = -\frac{1}{f_a} \vec{E} \cdot \vec{B} - m^2 a(\vec{x})$$

\*Shields neutron dipole moment

# relic abundance

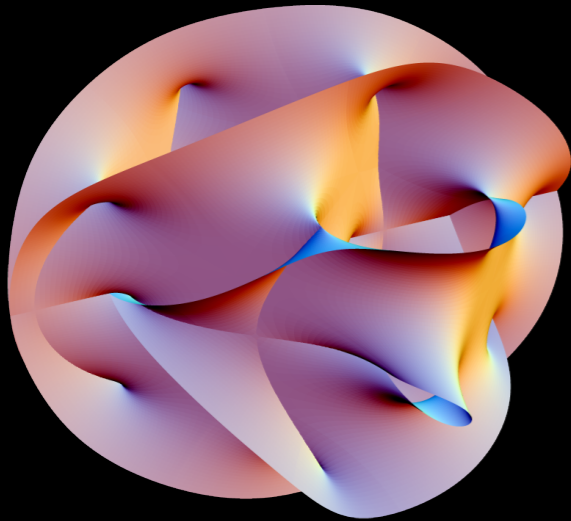


- \* Before PQ symmetry breaking,  $\theta$  is generically displaced from vacuum value
- \* EOM:  $\ddot{\bar{\theta}} + 3H\dot{\bar{\theta}} + m_a^2(T)\bar{\theta} = 0$
- \* After  $m_a(T) \gtrsim 3H(T)$ , coherent oscillations begin, leading to  $n_a \propto a^{-3}$

$$\Omega_{\text{mis}} h^2 = 0.236 \langle \theta_i^2 f(\theta_i) \rangle \left( \frac{m_a}{6.2 \mu\text{eV}} \right)^{-7/6}$$

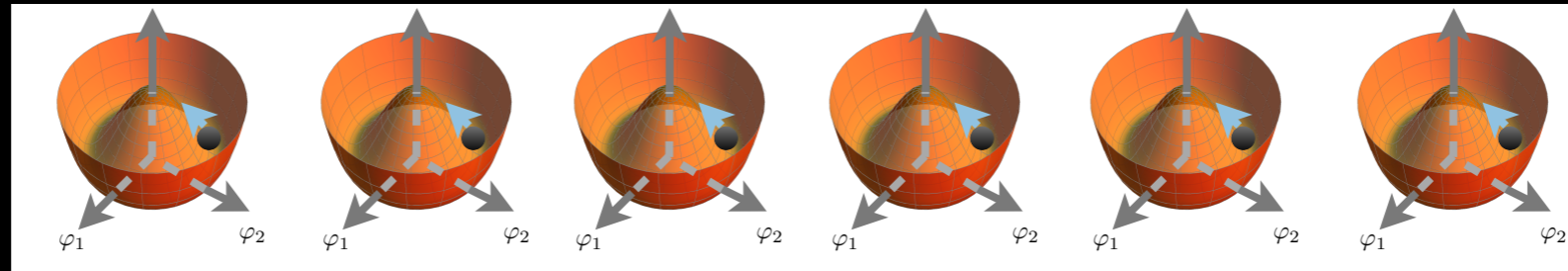
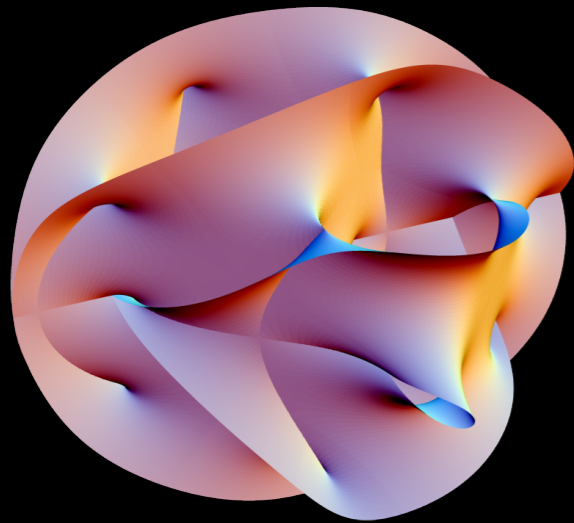
# Ultra-light axions (ULAS) in string theory

\* In string theory, extra dimensions compactified: Calabi-Yau manifolds



# Ultra-light axions (ULAS) in string theory

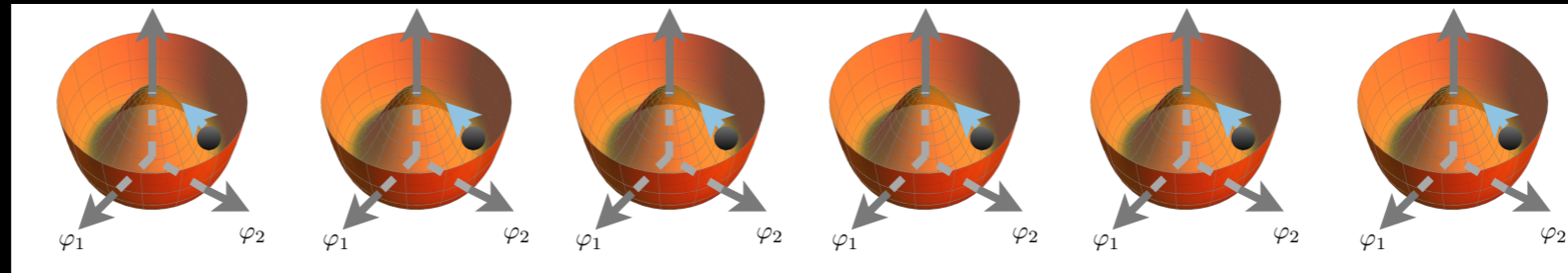
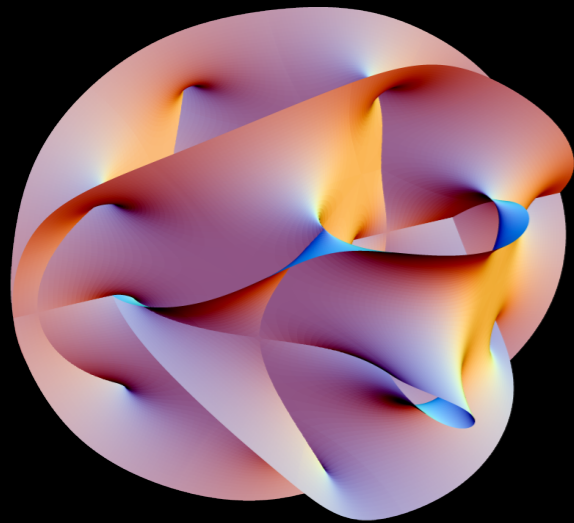
\* In string theory, extra dimensions compactified: Calabi-Yau manifolds



*Hundreds of scalars  
with approx shift symmetry*

# Ultra-light axions (ULAS) in string theory

\* In string theory, extra dimensions compactified: Calabi-Yau manifolds



+ ...

*Hundreds of scalars  
with approx shift symmetry*

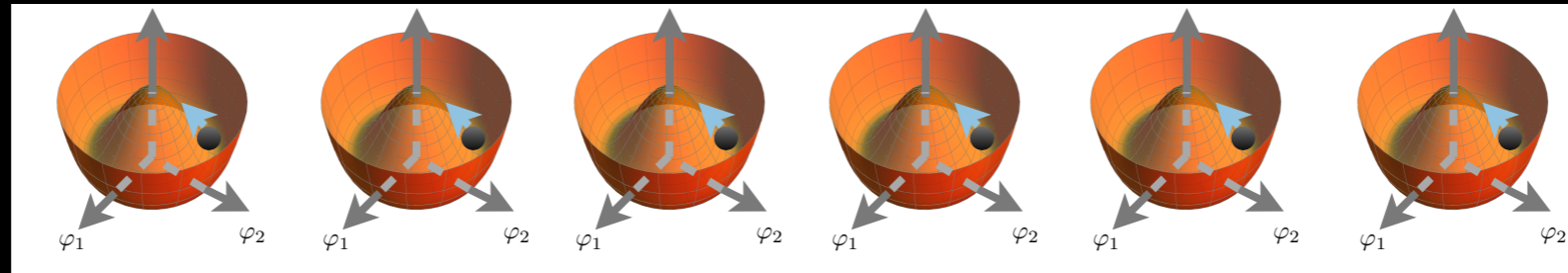
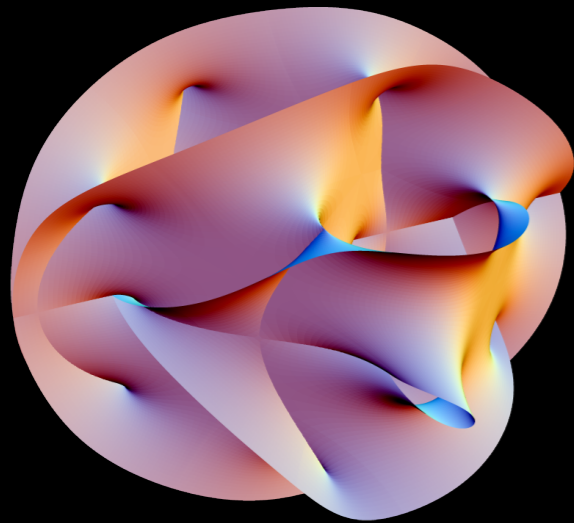


**Many axions**



# Ultra-light axions (ULAS) in string theory

- \* In string theory, extra dimensions compactified: Calabi-Yau manifolds



+ ...

*Hundreds of scalars  
with approx shift symmetry*



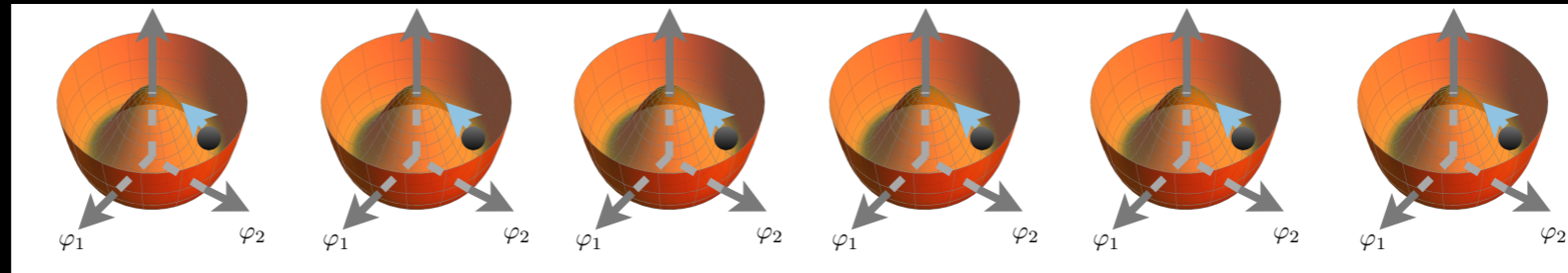
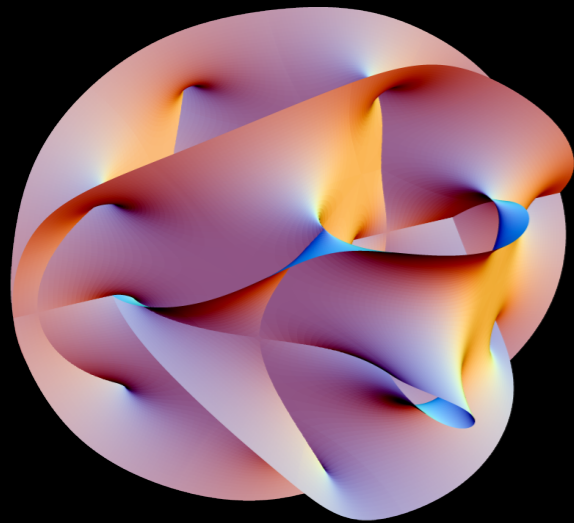
**Many axions**

- \* Mass acquired non-perturbatively (instantons, D-Branes)

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$

# Ultra-light axions (ULAS) in string theory

- \* In string theory, extra dimensions compactified: Calabi-Yau manifolds



+ ...

*Hundreds of scalars  
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**Many axions**

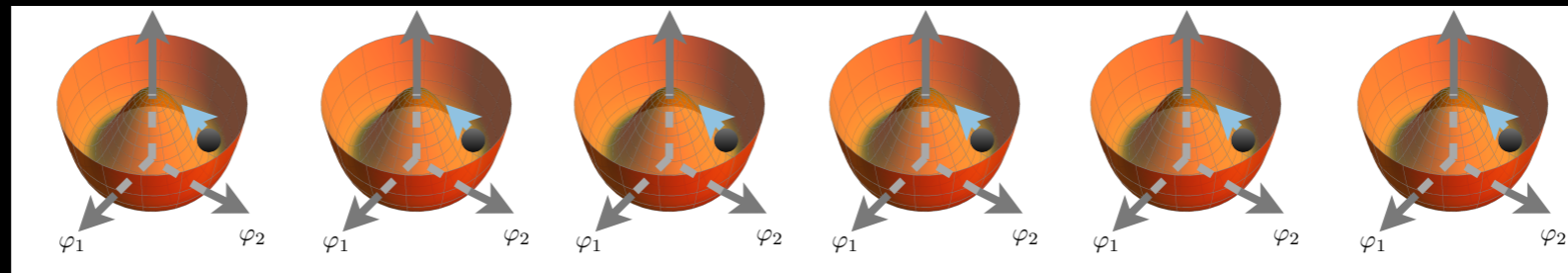
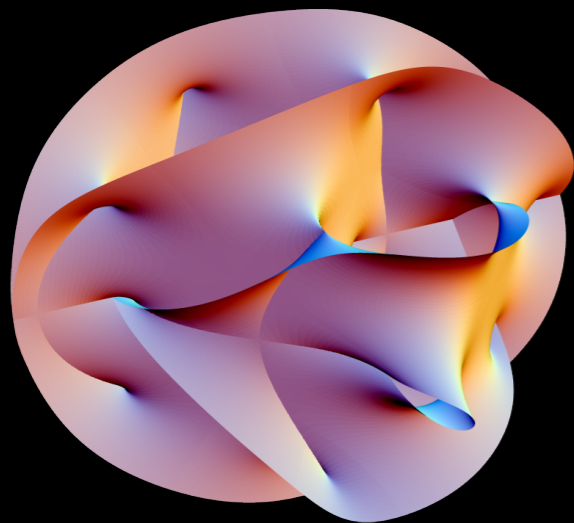
- \* Mass acquired non-perturbatively (instantons, D-Branes)

**Scale of new  
ultra-violet physics**

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$

# Ultra-light axions (ULAS) in string theory

- \* In string theory, extra dimensions compactified: Calabi-Yau manifolds



+ ...

*Hundreds of scalars  
with approx shift symmetry*



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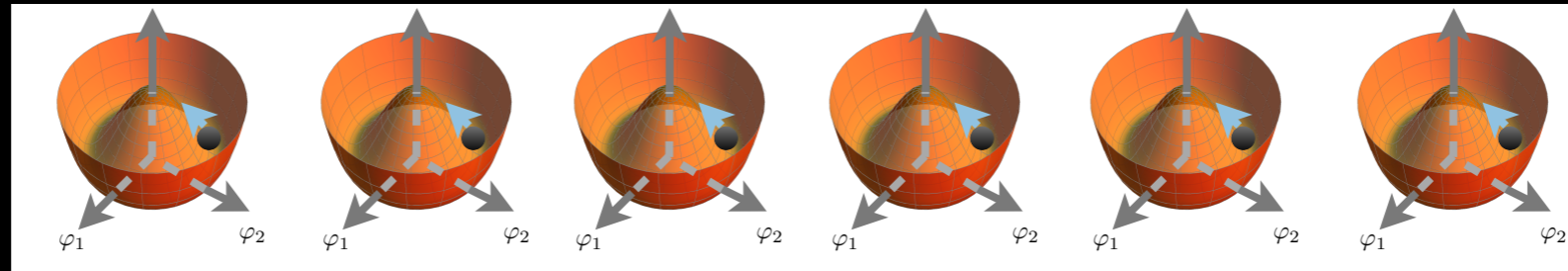
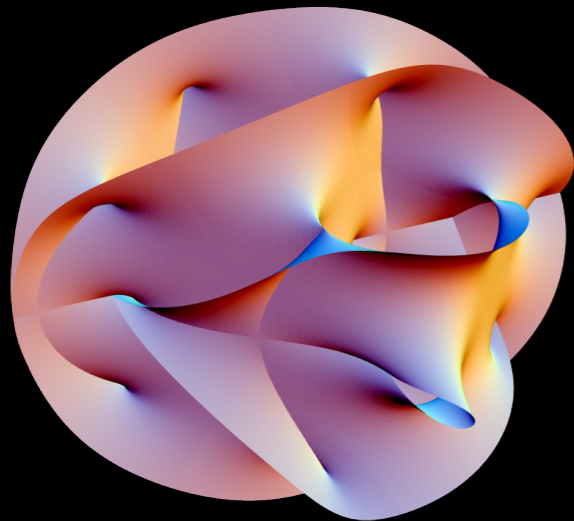
**Scale of extra dimensions  
in Planck units**

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$



# Ultra-light axions (ULAS) in string theory

\* In string theory, extra dimensions compactified: Calabi-Yau manifolds

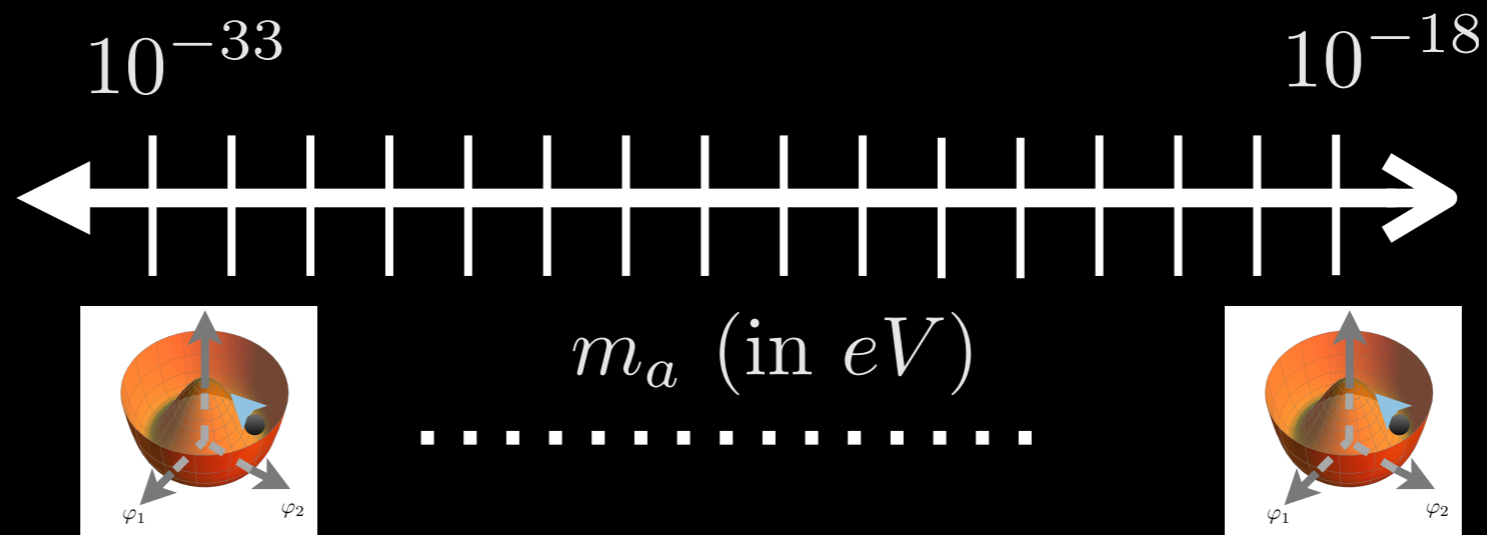


+ ...

*Axiverse! Arvanitaki+ 2009*

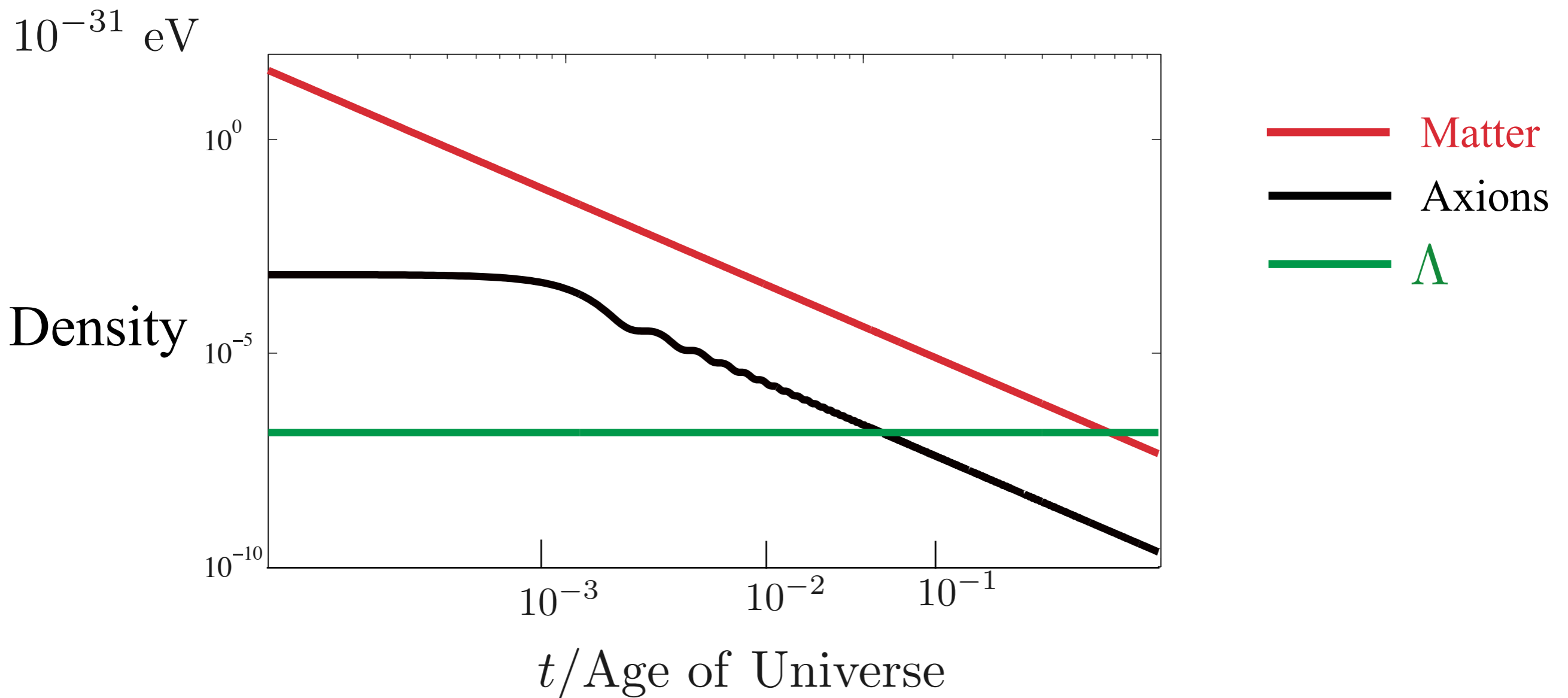
Witten and Srivceek (2006), Acharya et al. (2010),

Cicoli (2012), Hui (+ Witten, Ostriker, Tremaine) 2016



# ULA cosmology

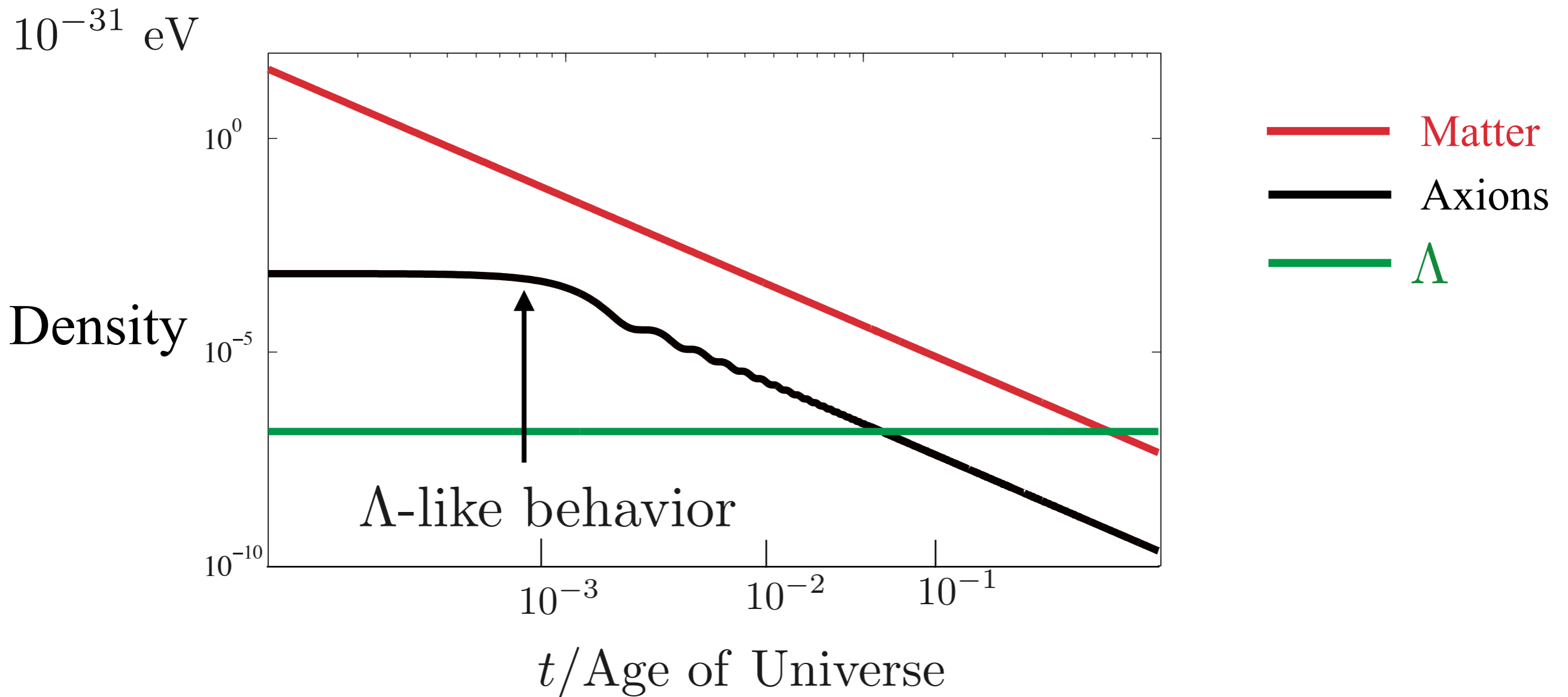
# Cosmology of axions: dark matter and dark energy candidates



Time

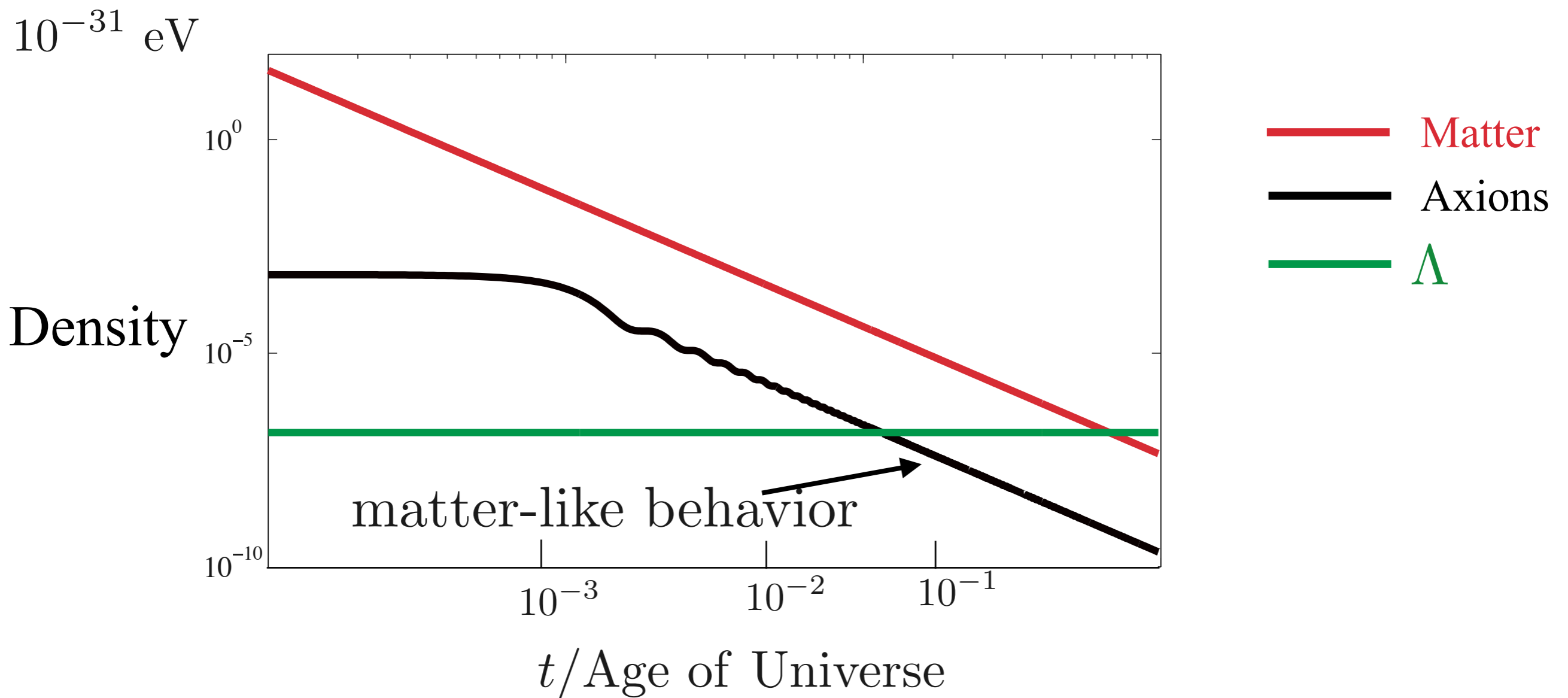


# Cosmology of axions: dark matter and dark energy candidates



Time

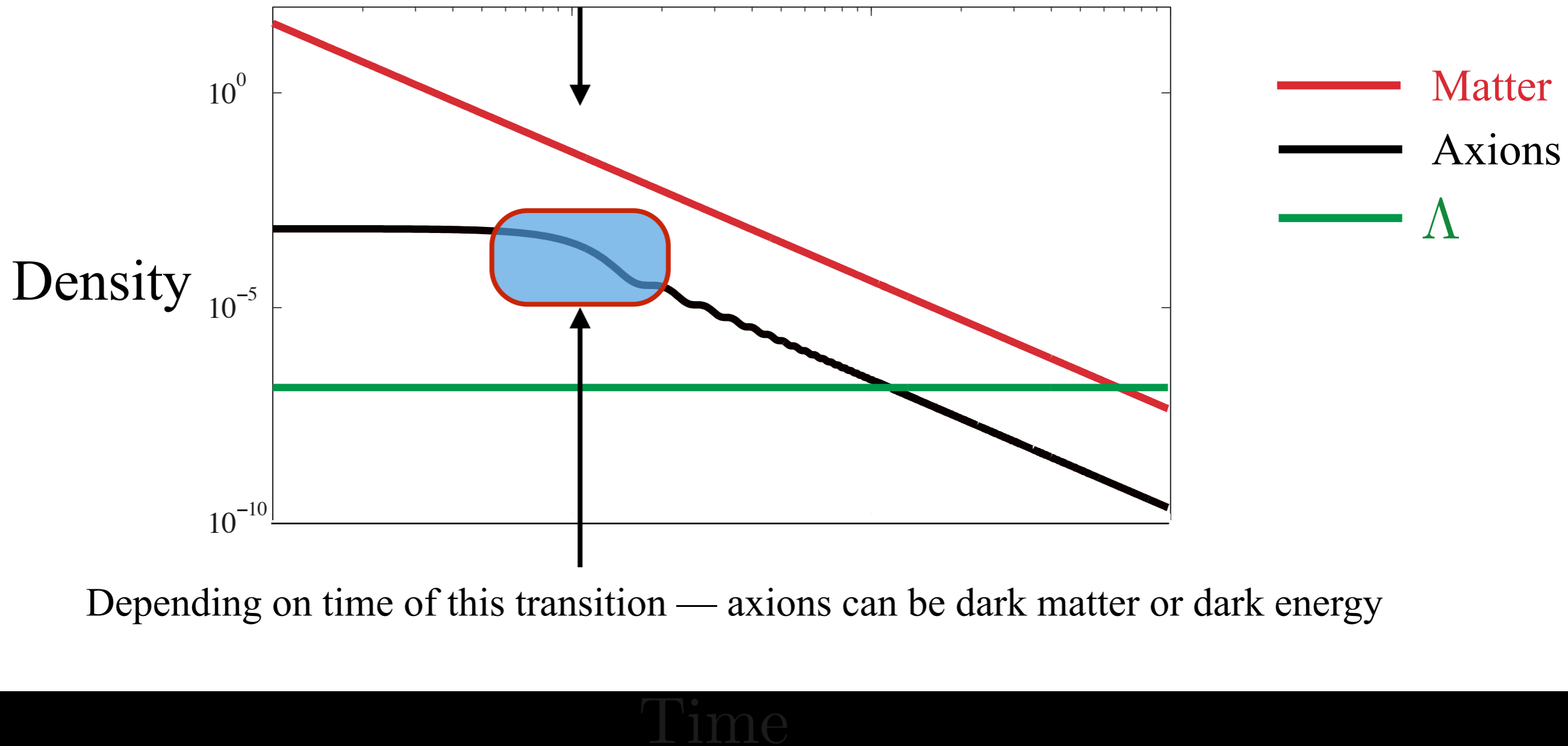
# Cosmology of axions: dark matter and dark energy candidates



Time

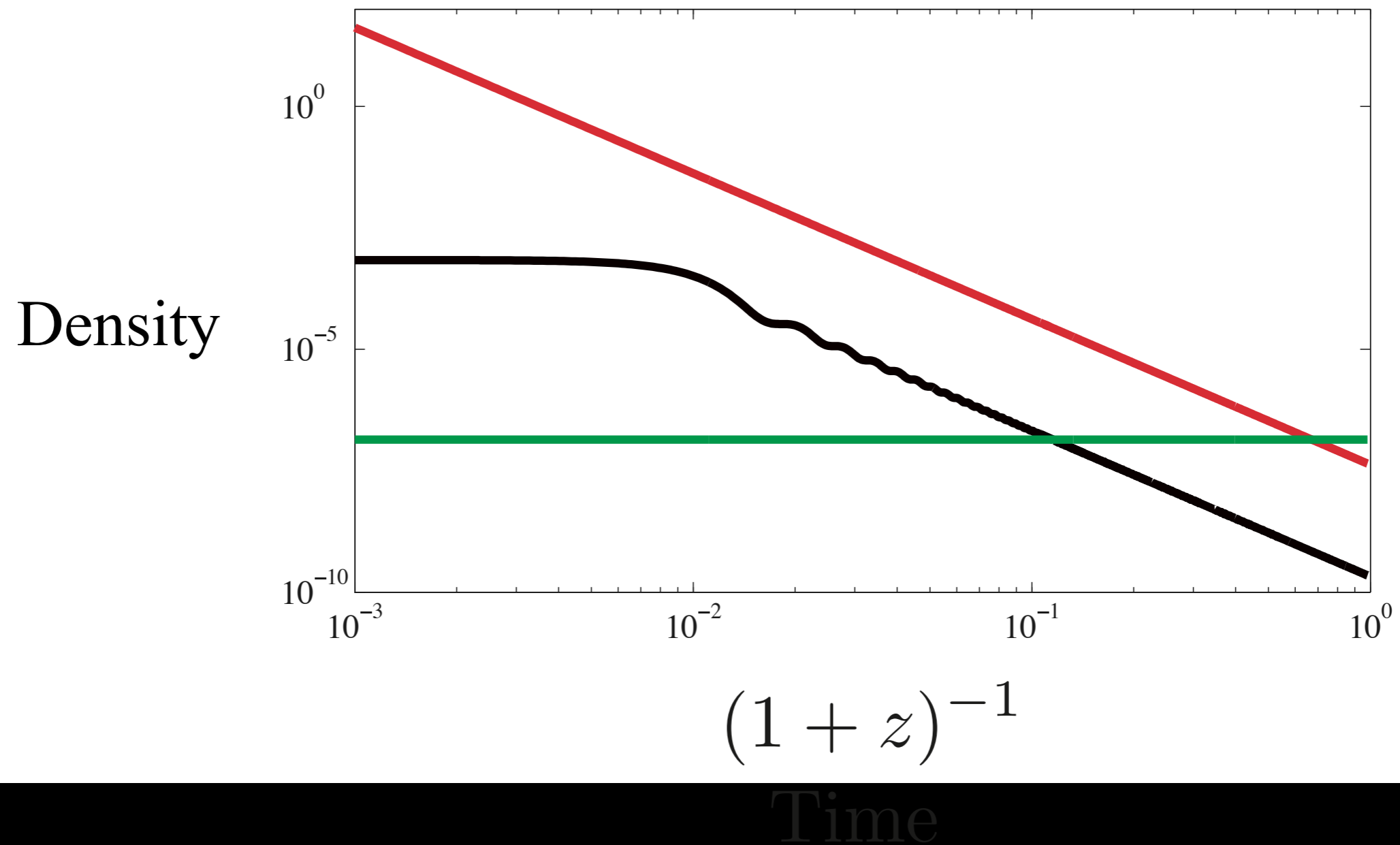
# Cosmology of axions: dark matter and dark energy candidates

Axion mass  $m_a$  sets time of this transition



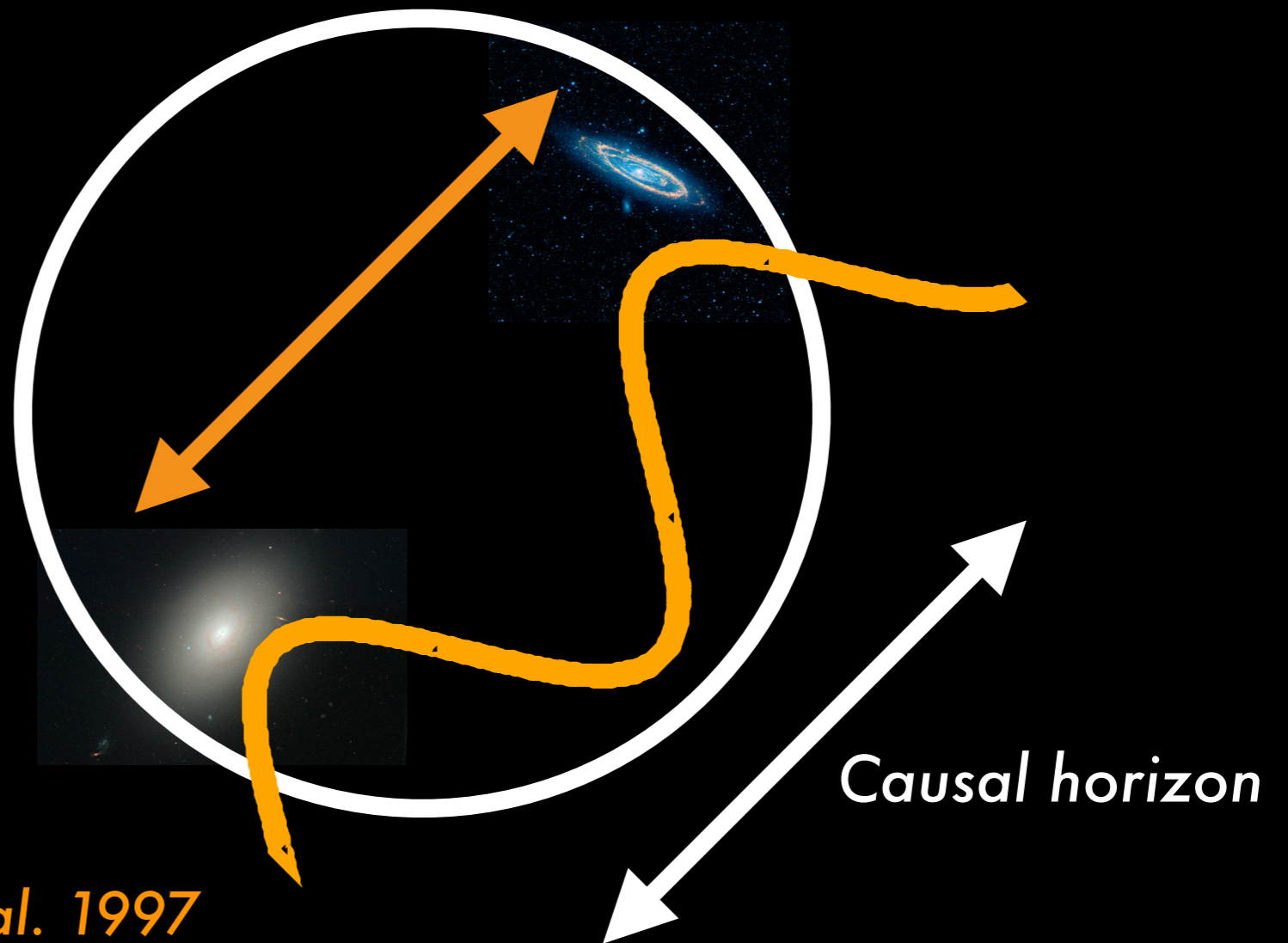
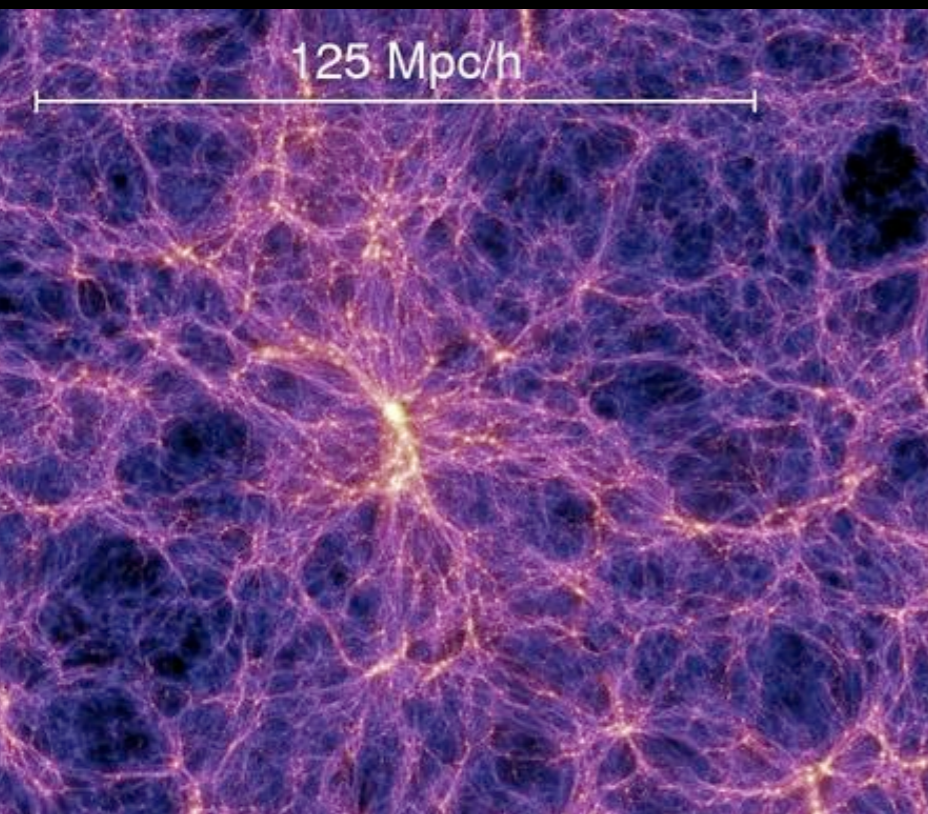
Depending on time of this transition — axions can be dark matter or dark energy

# Cosmology of ultra-light axions: dark matter and dark energy candidates



# Cosmology of ultra-light axions: dark matter and dark energy candidates

Scale corresponding to  
typical galaxy separation today



*Frieman et al 1995, Coble et al. 1997*

ULA as dark energy with specific  $w(z)$

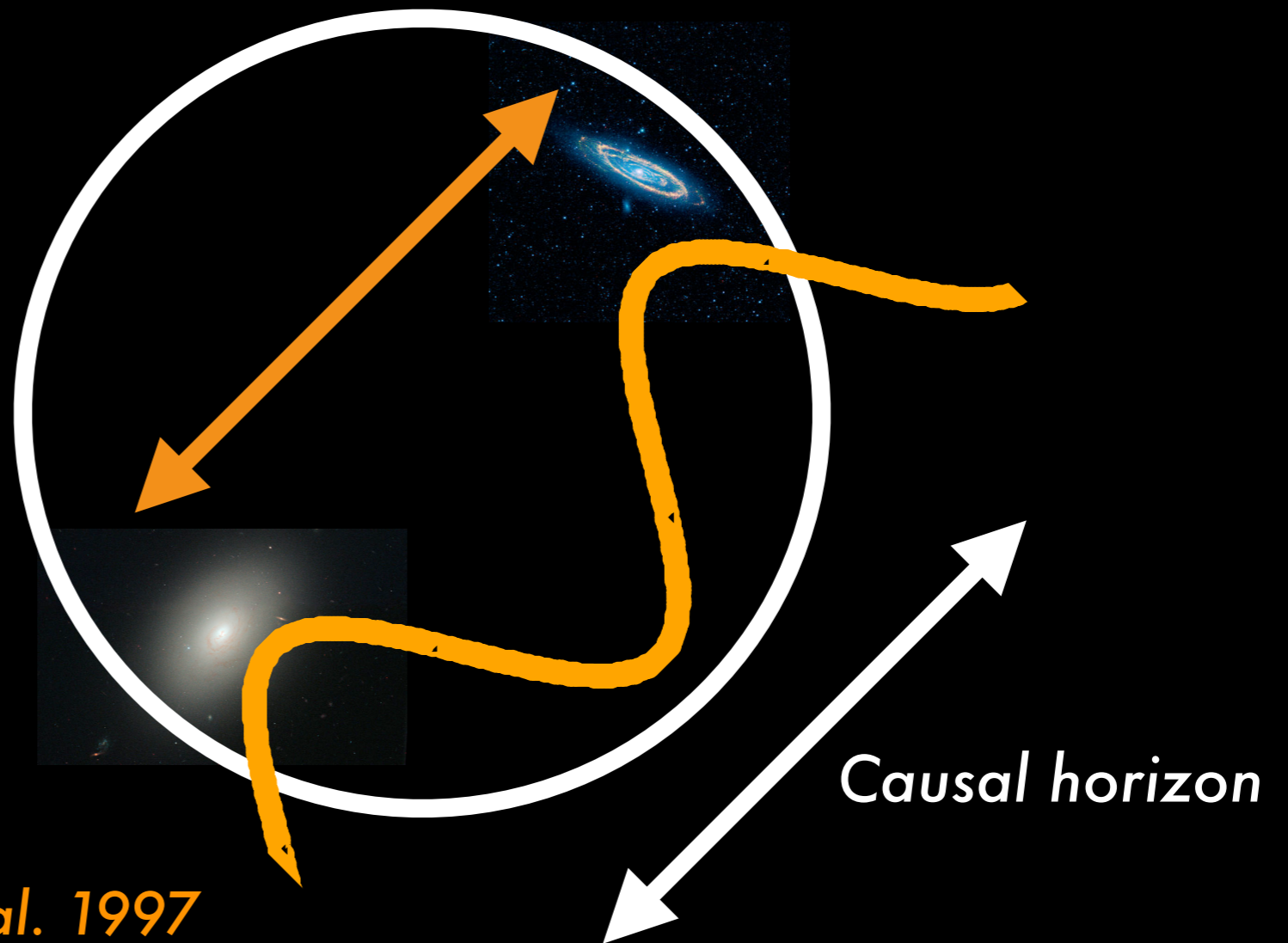
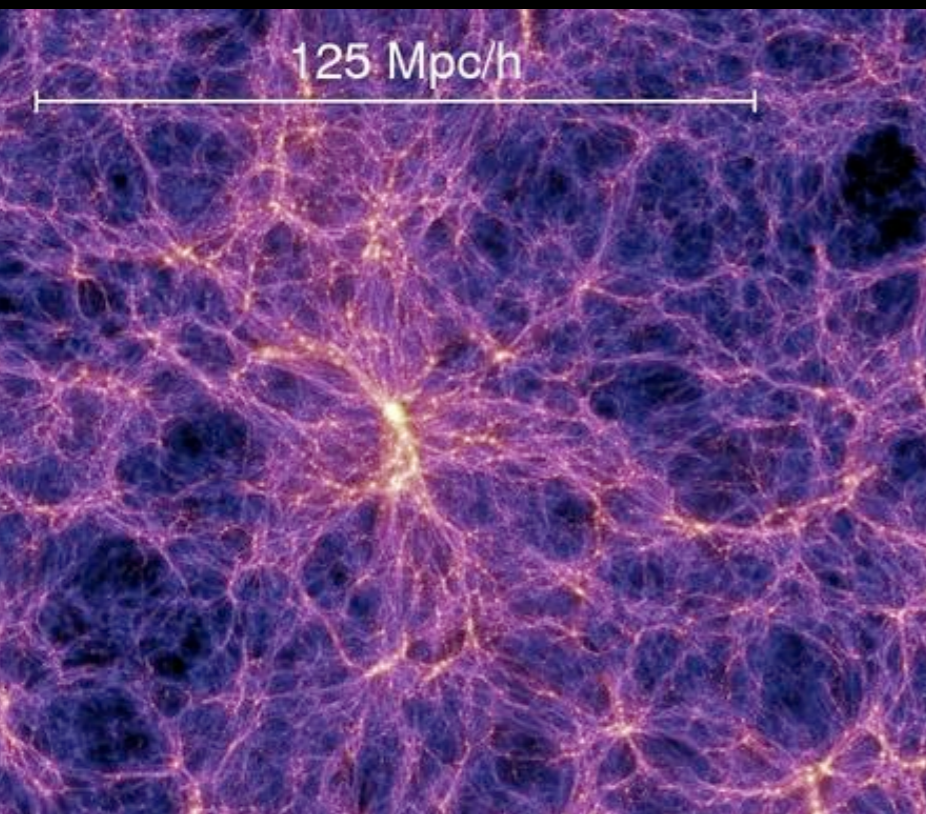
$$m_a \lesssim 10^{-27} \text{ eV}$$

ULA matter behavior starts too late for struct. formation



# Cosmology of ultra-light axions: dark matter and dark energy candidates

Scale corresponding to  
typical galaxy separation today



*Frieman et al 1995, Coble et al. 1997*

ULA as dark matter

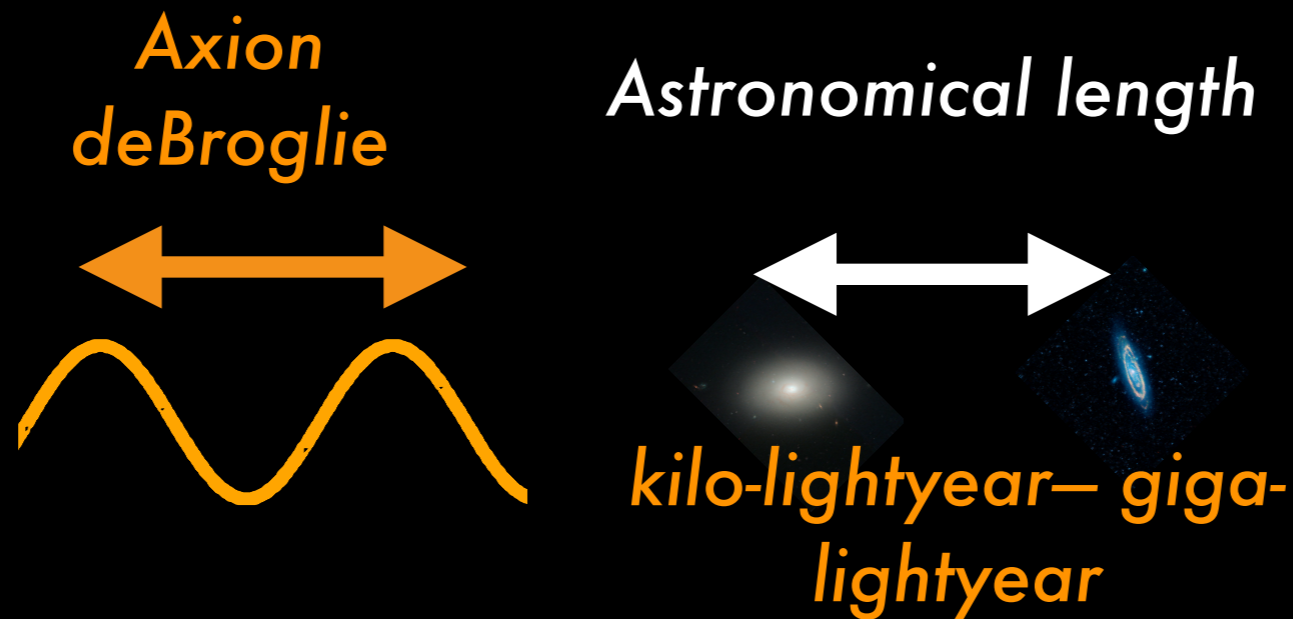
$$m_a \gtrsim 10^{-27} \text{ eV}$$

ULA matter behavior starts in time for struct. formation



# structure growth suppressed on small scales

\*Perturbed KG equation  $\delta\ddot{\phi} + 3H\delta\dot{\phi} + \left[ m^2 + \frac{k^2}{R^2} \right] \delta\phi \propto \Psi$

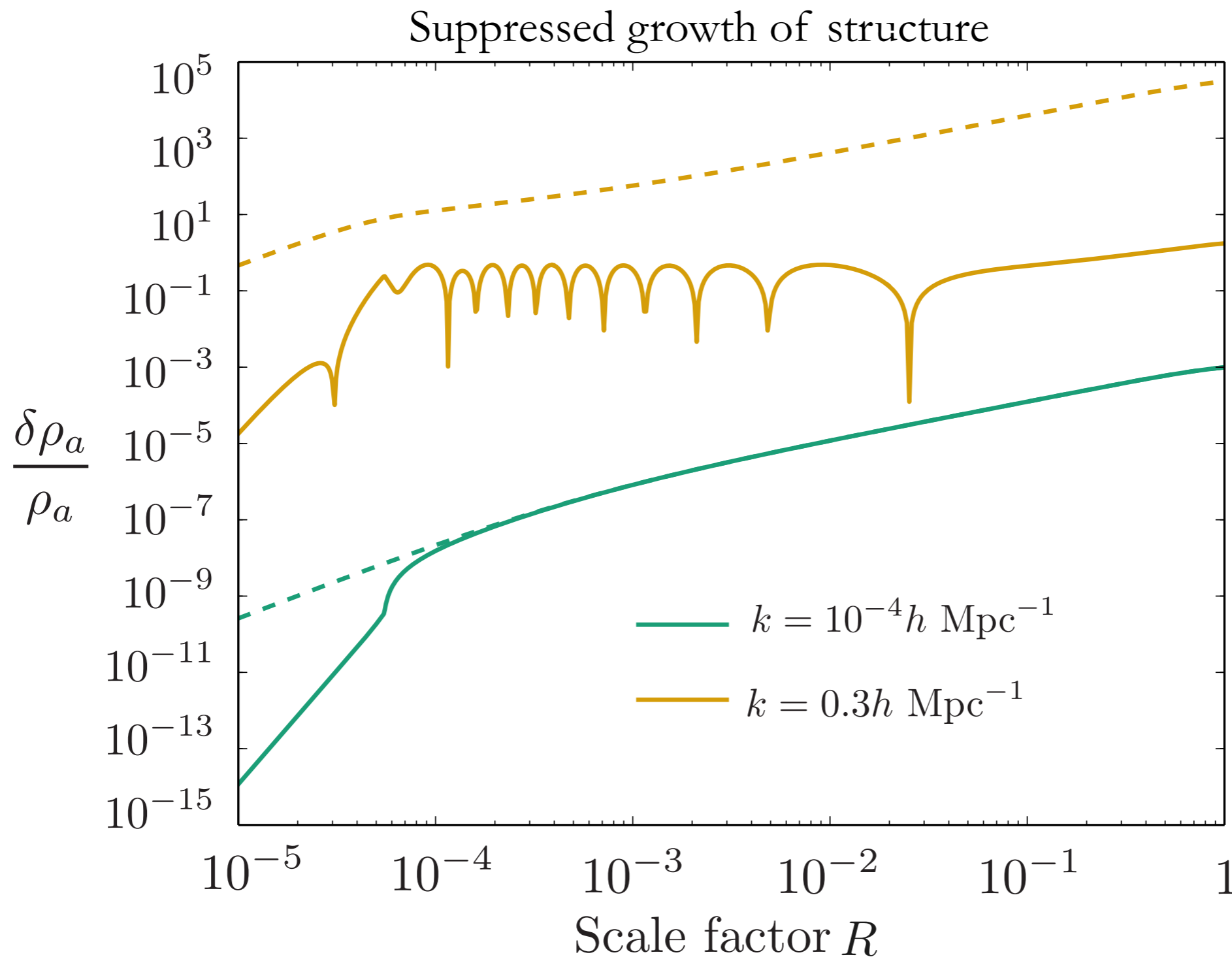


\*WKB fluid description  $c_s^2 \propto k^2 / (4m_a^2 R^2)$  *Hu, Barkana, Gruzinov 2000, Hwang & Noh 2009*

\*Small-scale suppression

$$\lambda_J \sim 3 \left( \frac{m_a}{10^{-25} \text{ eV}} \right)^{-1/2} \text{ Mpc} (1+z)^{1/4}$$

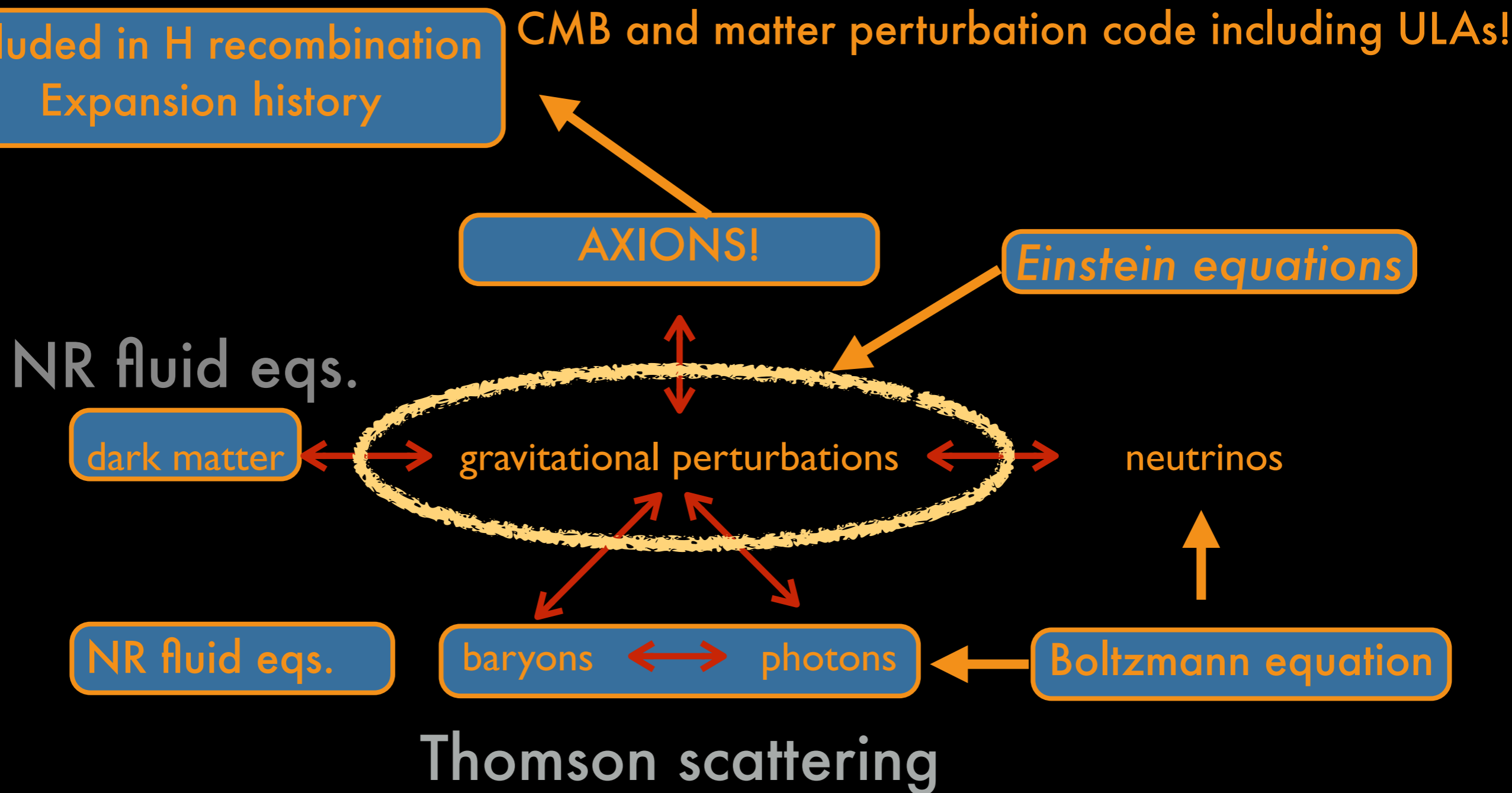
# structure growth suppressed on small scales



# AxionCAMB

Code by Grin et al. 2013, based on CAMB (A. Lewis)

<http://github.com/dgrin1/axionCAMB>



ULA of any mass is self-consistently followed from DE to DM regime

# Effective Fluid approximation (EFA)

	Background	Perturbations
early times	$\ddot{\phi}_0 + 2\mathcal{H}\dot{\phi}_0 + m_{\text{ax}}^2 a^2 \phi_0 = 0$	$\delta\ddot{\phi} + 2\mathcal{H}\delta\dot{\phi} + (m_{\text{ax}}^2 a^2 + k^2) \delta\phi =$ $(\Psi, \Phi) \times \mathcal{O}(\dot{\phi}_0) + (\dot{\Psi}, \dot{\Phi}) \phi_0$
late times	$\rho_{\text{ax}} = \rho_{\text{osc}} \left( \frac{a_{\text{osc}}}{a} \right)^3$	$\dot{\delta}_{\text{ax}} = -k u_{\text{ax}} - \frac{\dot{h}}{2}, \quad \dot{u}_{\text{ax}} = -\frac{\dot{a}}{a} u_{\text{ax}} + k c_s^2 \delta_{\text{ax}}$

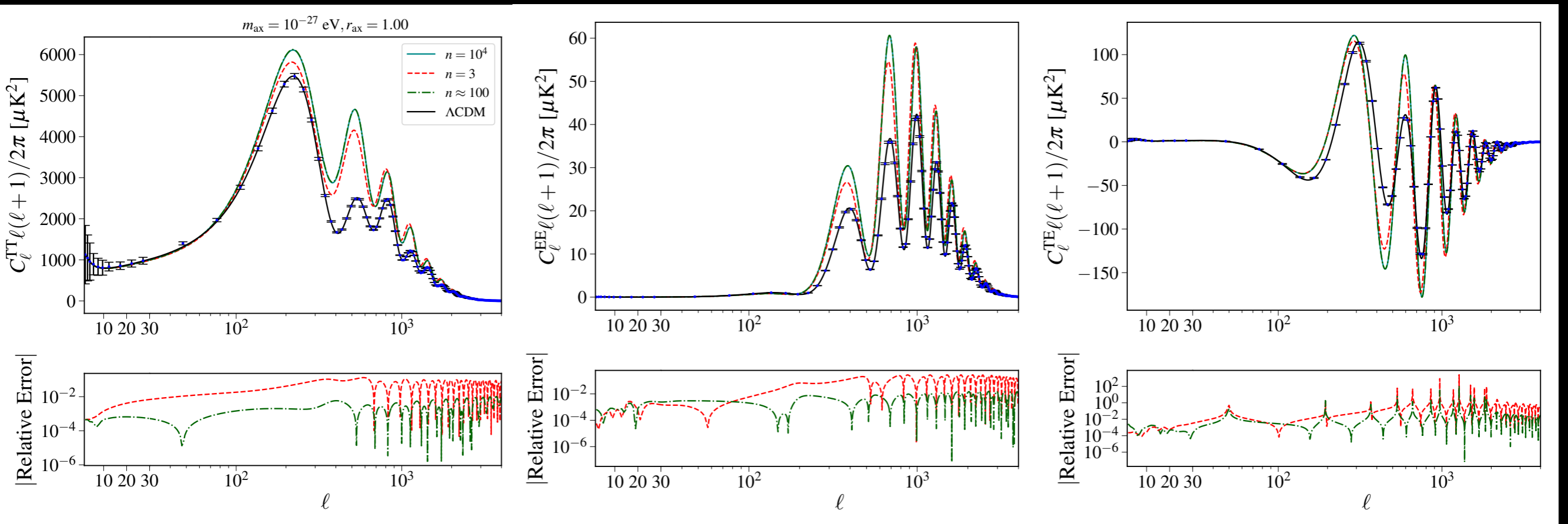
$$c_s^2 \equiv \frac{\frac{k^2}{4m_{\text{ax}}^2 a^2}}{1 + \frac{k^2}{4m_{\text{ax}}^2 a^2}}$$

Particle number and momentum conserved at transition  $m = n\mathcal{H}/a$

$$a = a_{\text{osc}}$$

# CMB power spectra

Worst-case scenario, from Cookmeyer, Grin, Smith, Phys. Rev. D 101, 023501 (2020), arXiv: 1909.11094  
 Uses separate Boltzmann code

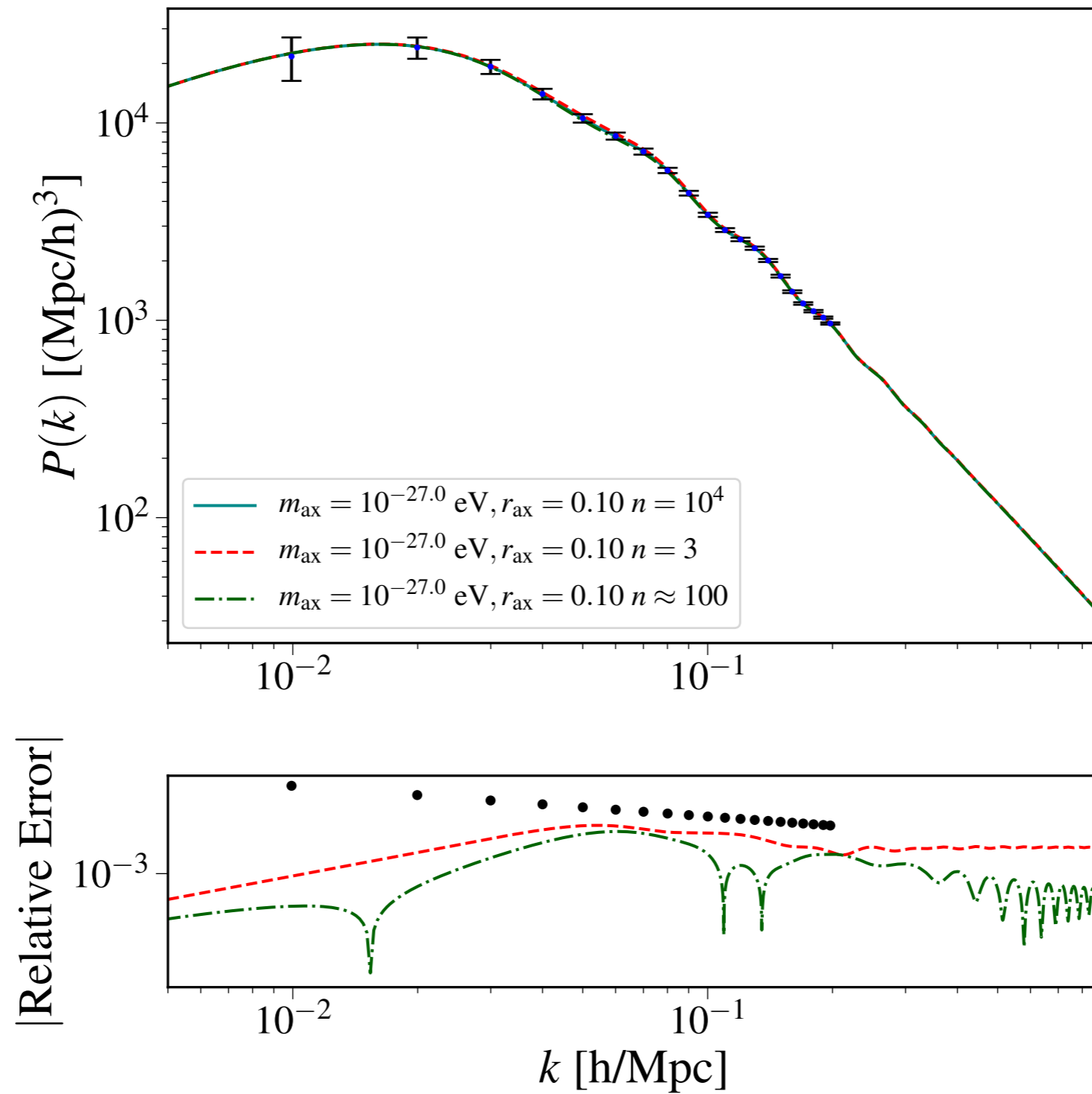


✦ Error ordering of prescription depends on axion mass

✦ Rough benchmark (Seljak Phys.Rev.D68:083507,2003) for CV-limited parameter estimates violated in some cases:

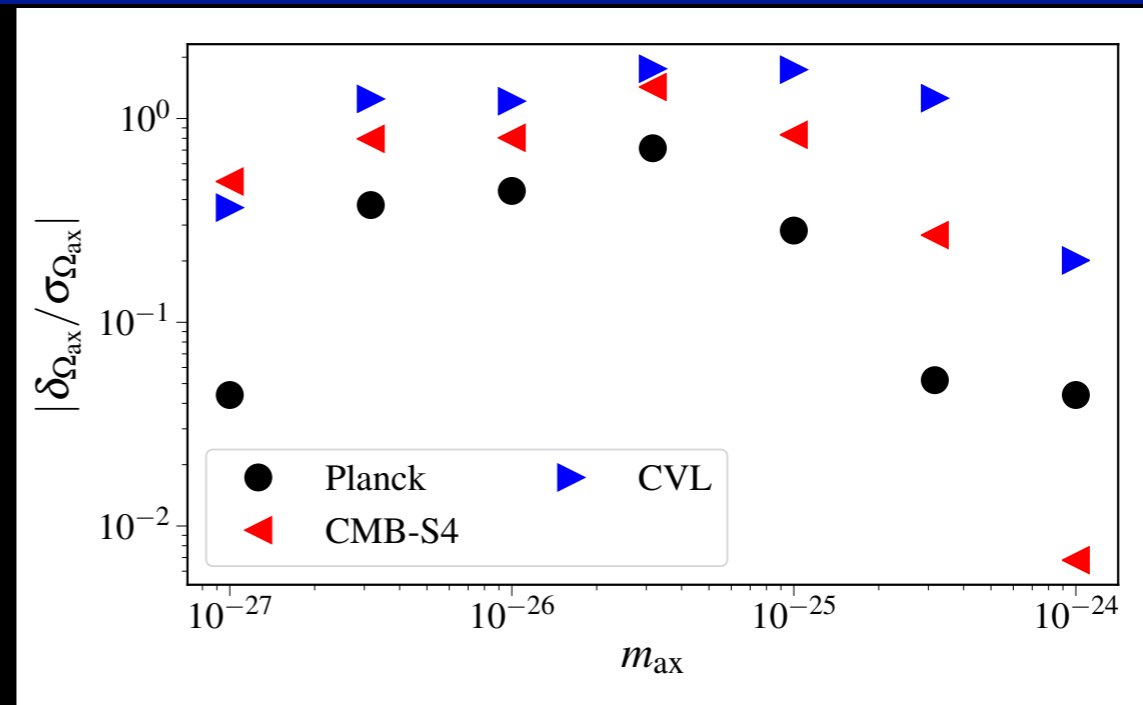
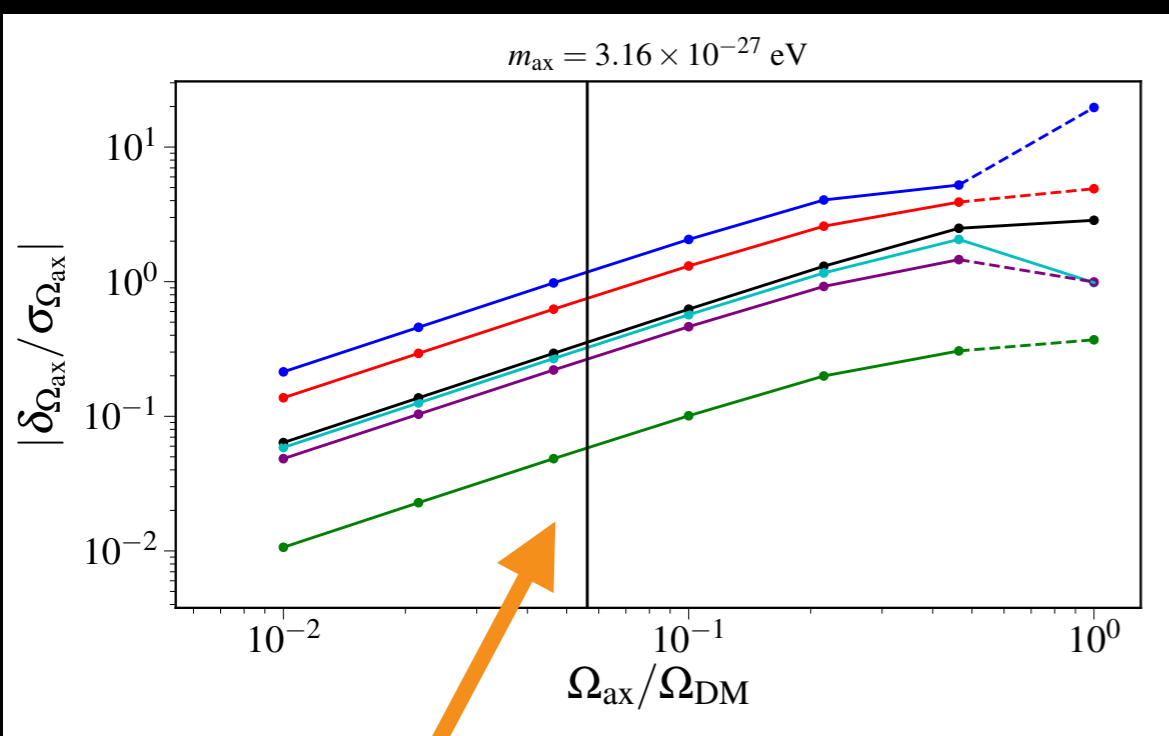
$$\frac{\Delta C_\ell}{C_\ell} \gtrsim \frac{3}{\ell} \text{ if } \ell \gtrsim \mathcal{O}(10^2) \text{ for } r_{\text{ax}} \sim 10^{-1} \text{ and } m_{\text{ax}} = 10^{-27} \text{ eV}$$

# Matter power spectrum (safe WiggleZ)





# Bias results



Saturate old limits

$3\sigma$  limit from Planck 2013

- \* Negligible bias for Planck and S4 (usually)
- \* Modest bias for S4 (some cases) and CVL (but likely only need to worry if claiming detection)

# Improving the Effective Fluid approximation (EFA)

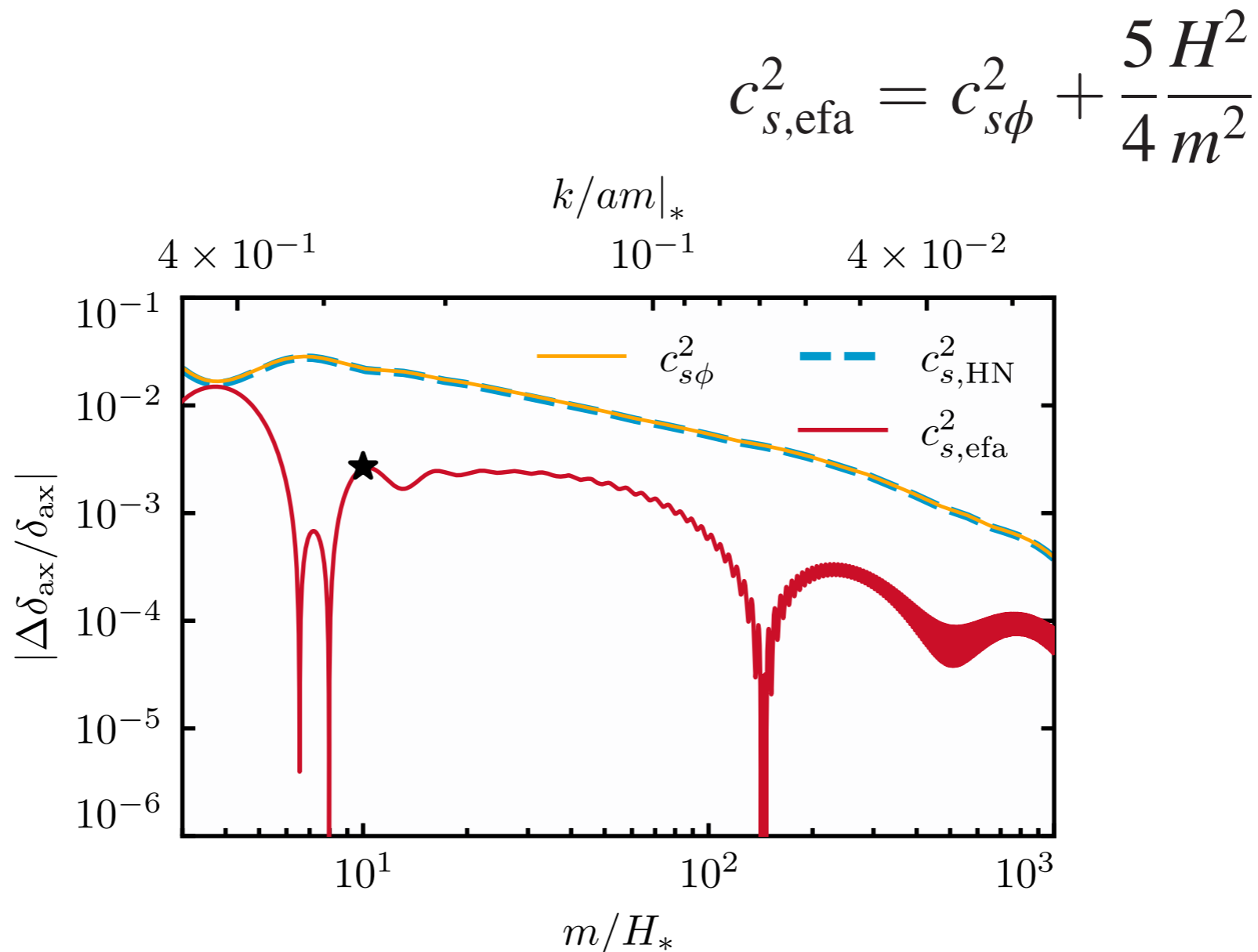
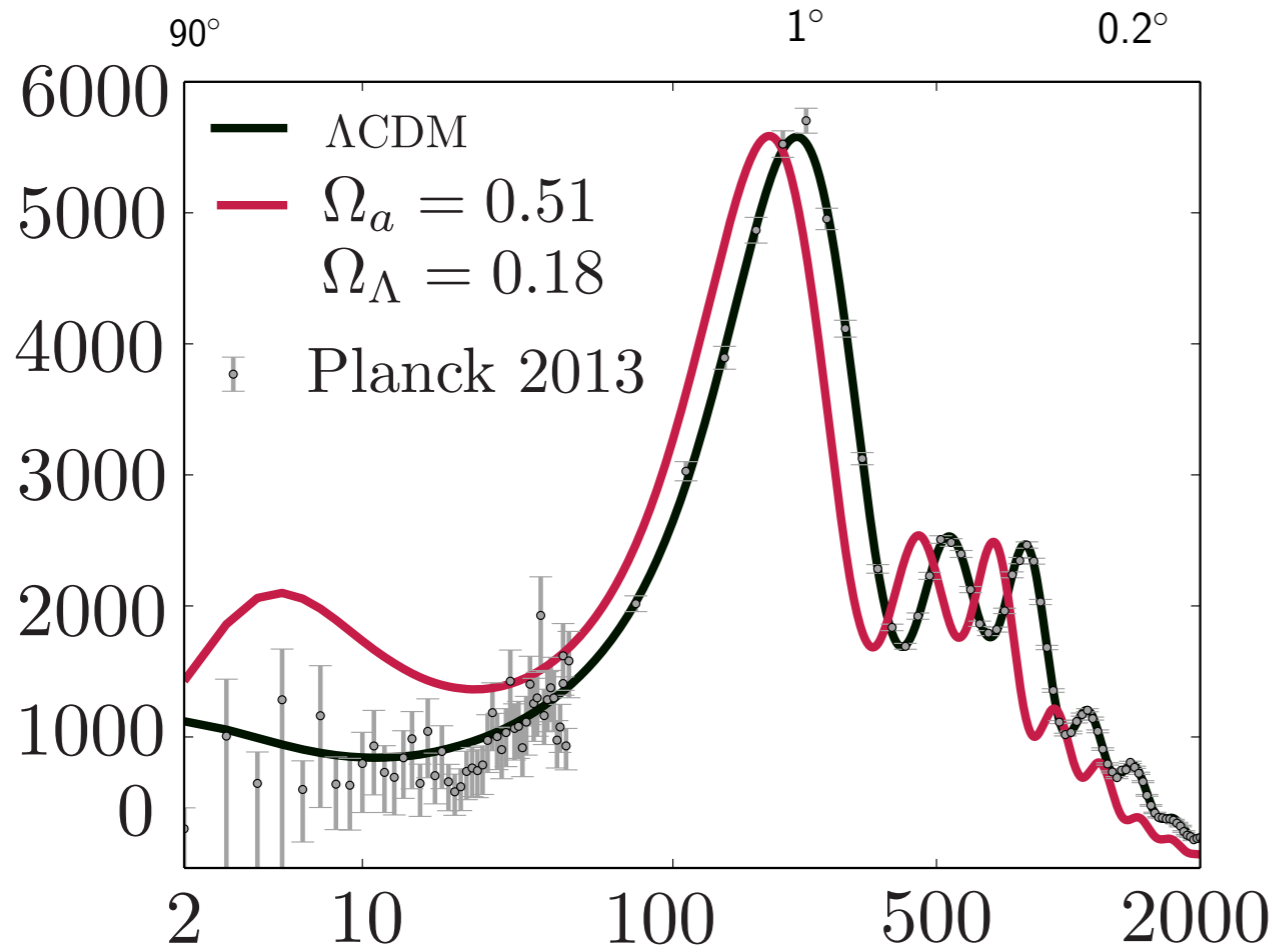


FIG. 9. For a mode  $k_{1/2}$  where the matter power spectrum yields half its CDM value, we show our technique's total error as a function of our switch time parameter  $m/H_*$  for various choices of the EFA equation of state  $c_s^2$ , computed by comparing to a late switch time  $m/H_* = 2 \times 10^3$ . Using the field sound speed  $c_{s\phi}$

# constraints

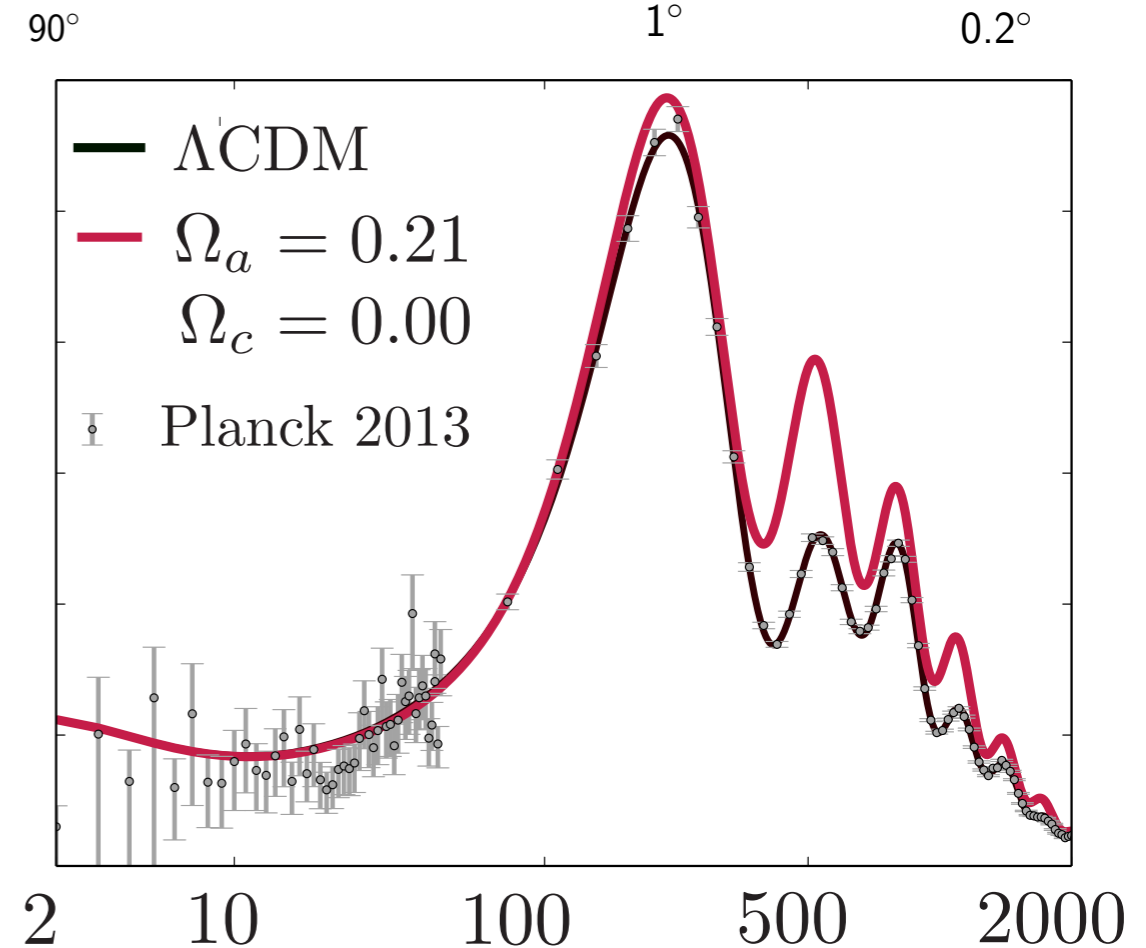
$$m_a = 10^{-32} \text{ eV}$$

Angular scale



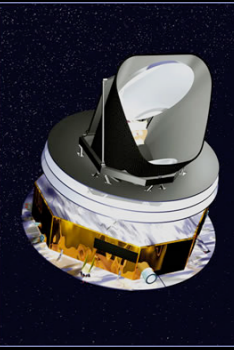
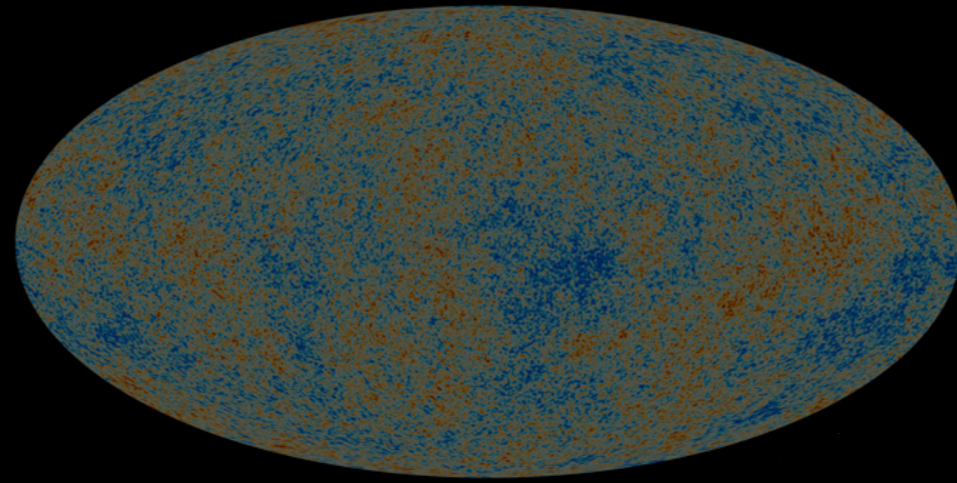
$$m_a = 10^{-27} \text{ eV}$$

Angular scale



Dramatic changes to observables can result

# Data + Analysis



\* Planck 2013 temperature anisotropy power spectra (+SPT+ACT)

\* Cosmic variance limited to  $\ell \sim 1500$

\* WiggleZ galaxy survey (linear scales only  $k \lesssim 0.2h \text{ Mpc}^{-1}$  )

\* 240,000 emission line galaxies at  $z < 1$

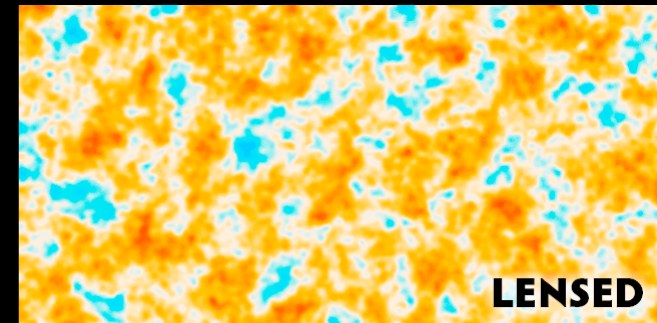
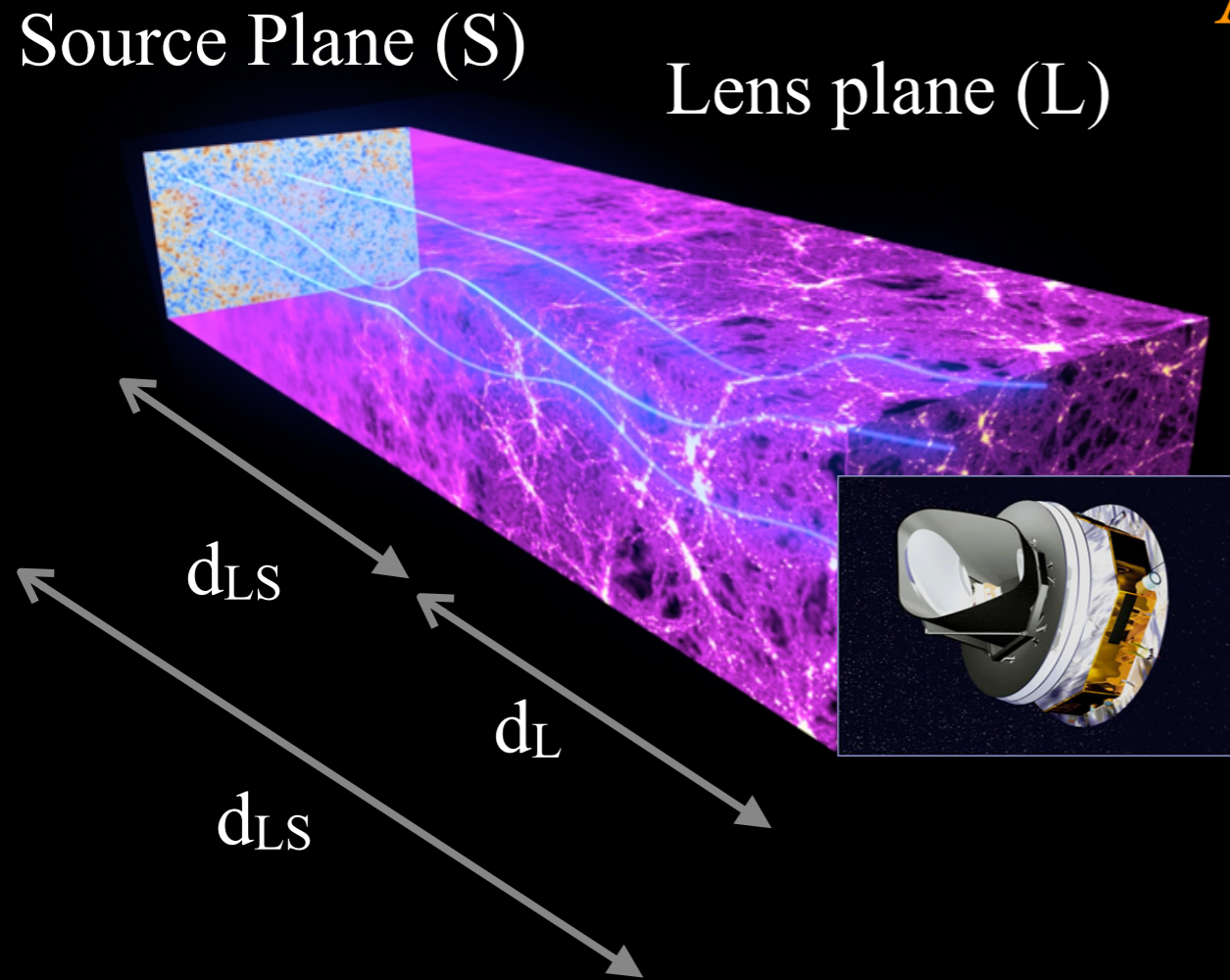
\* 3.9 m Anglo-Australian Telescope (AAT)

\* Nested sampling, MCMC, vary  $m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$



# CMB LENSING

A slice of (dark matter) life at  $z \sim 1$

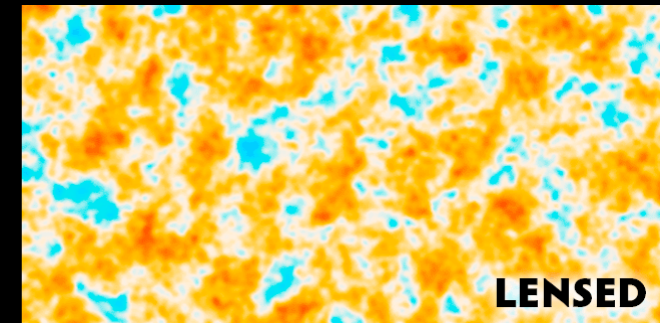
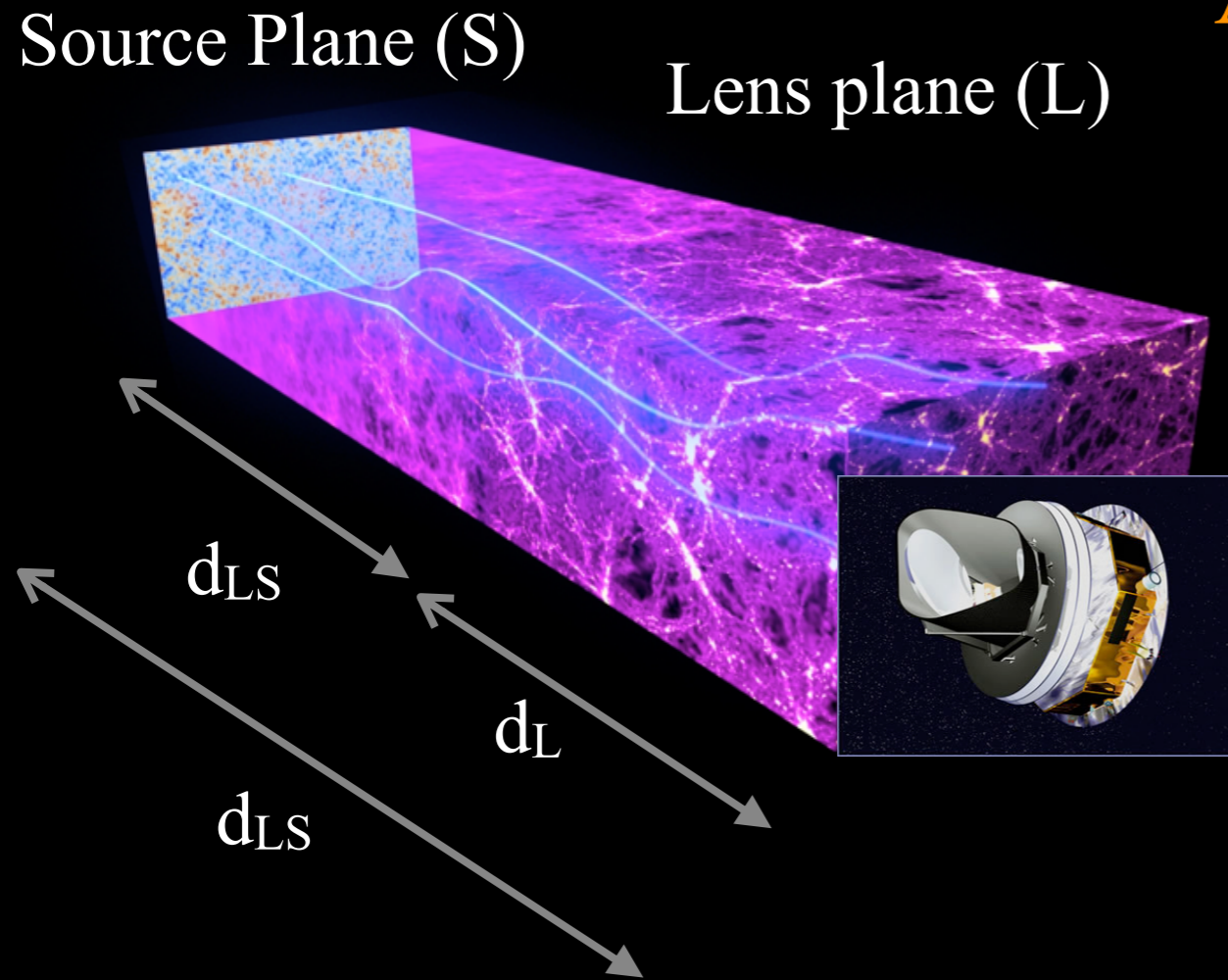


$$\vec{\alpha} = \nabla_{\vec{\theta}} \left\{ \int \left( \frac{d_{LS}}{d_L d_S} \right) \Phi \left[ d(\eta) \vec{\theta}, \eta \right] d\eta \right\}$$



# CMB LENSING

A slice of (dark matter) life at  $z \sim 1$

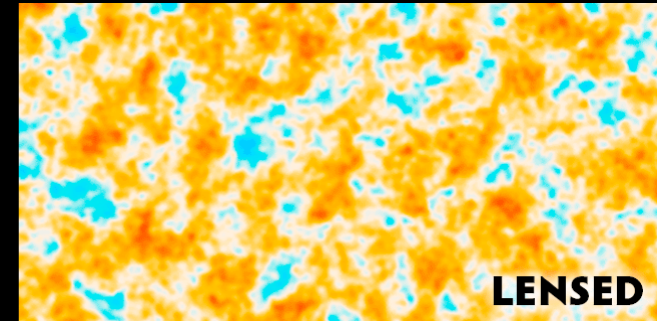
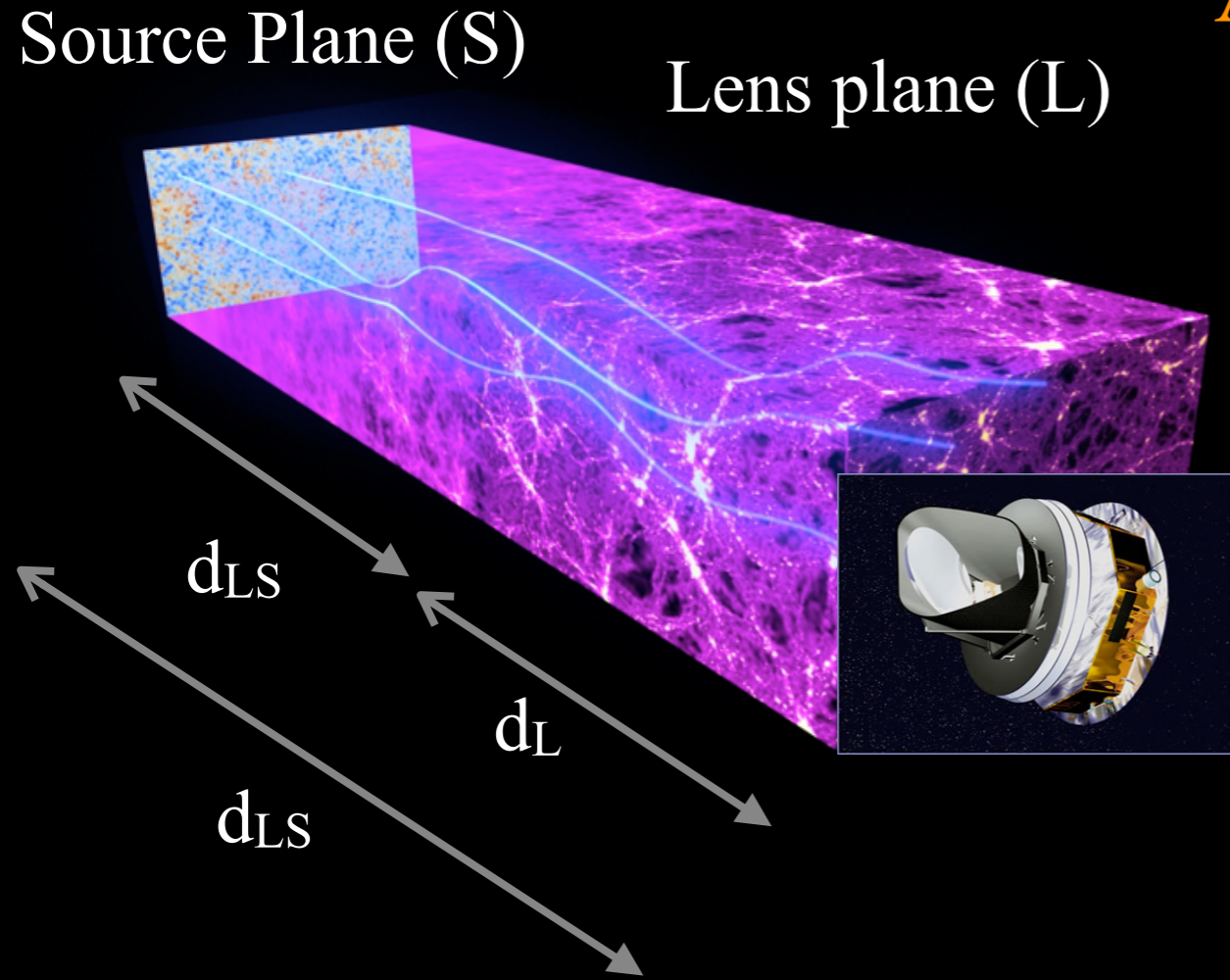


$$\vec{\alpha} = \nabla_{\vec{\theta}} \left\{ \int \left( \frac{d_{LS}}{d_L d_S} \right) \Phi \left[ d(\eta) \vec{\theta}, \eta \right] d\eta \right\}$$



# CMB LENSING

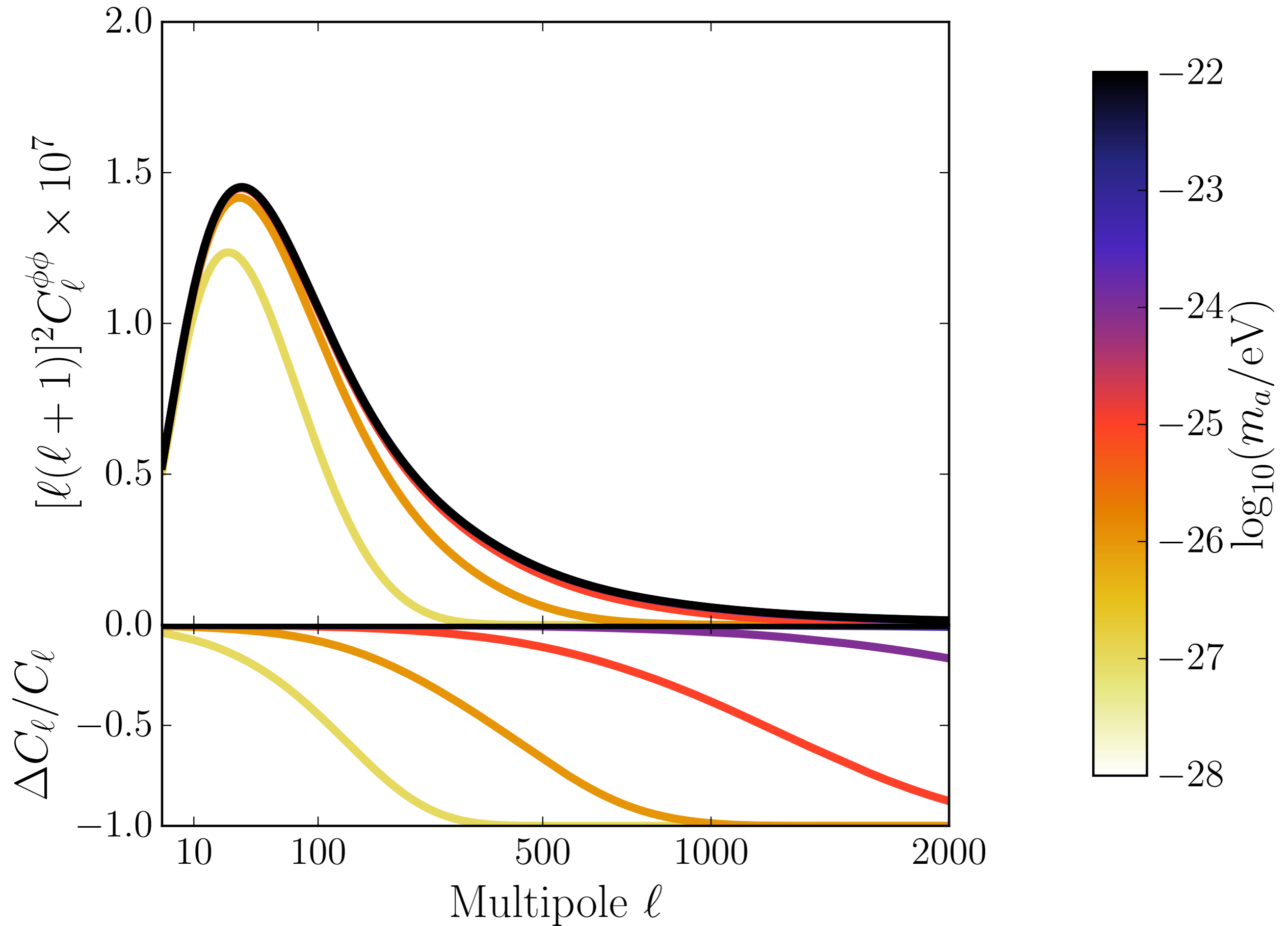
A slice of (dark matter) life at  $z \sim 1$



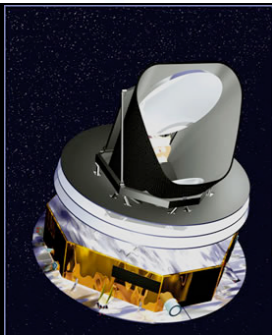
$$\vec{\alpha} = \nabla_{\vec{\theta}} \left\{ \int \left( \frac{d_{LS}}{d_L d_S} \right) \Phi \left[ d(\eta) \vec{\theta}, \eta \right] d\eta \right\}$$

ULAs change

# CMB LENSING

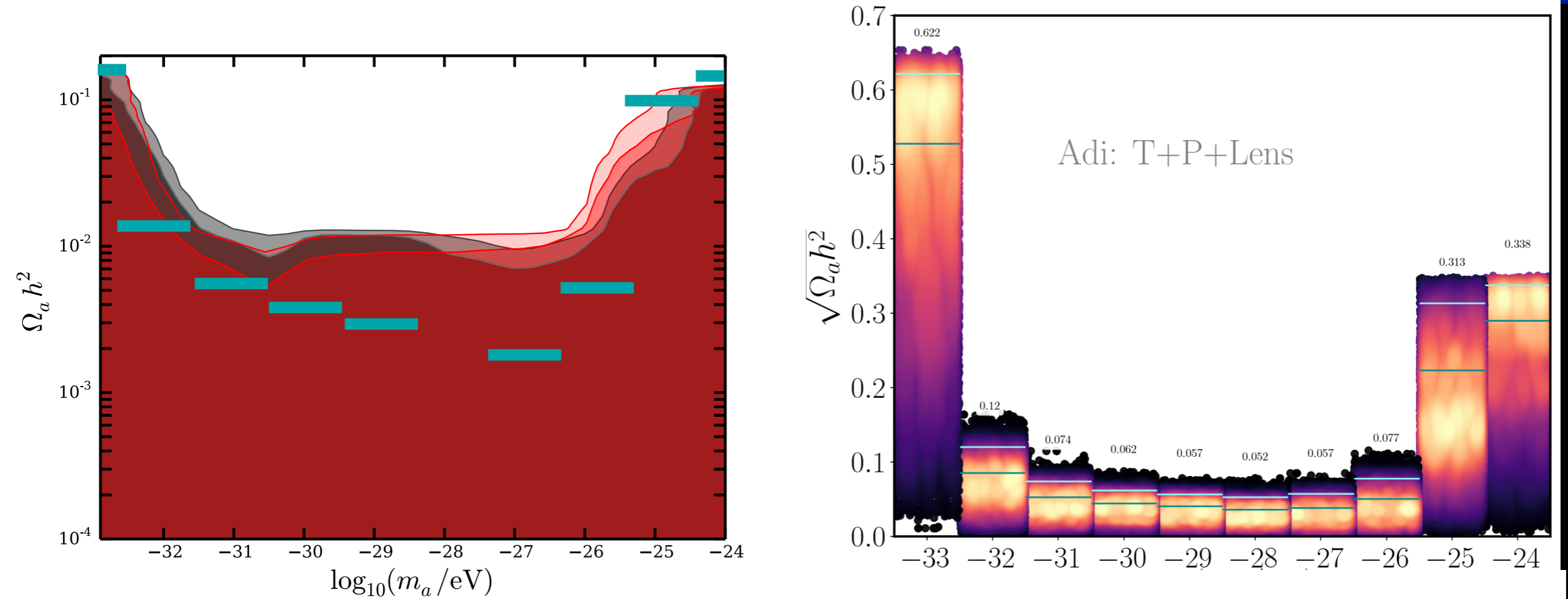


# Constraints



- 
- arXiv: 1708.05681, MNRAS 476, Volume 3*  
*arXiv: 1607.08208, Phys. Rev. D 95, 123511 (2017).*  
*arXiv:1410.2896, Phys. Rev. D 91, 103512 (2015)*  
*arXiv:1403.4216, Phys. Rev. Lett. 113, 011801 (2014)*  
*arXiv:1303.3008, Phys. Rev. D 87, 121701(R) (2013)*

# Constraints



*arXiv: 1708.05681, MNRAS 476, Volume 3*

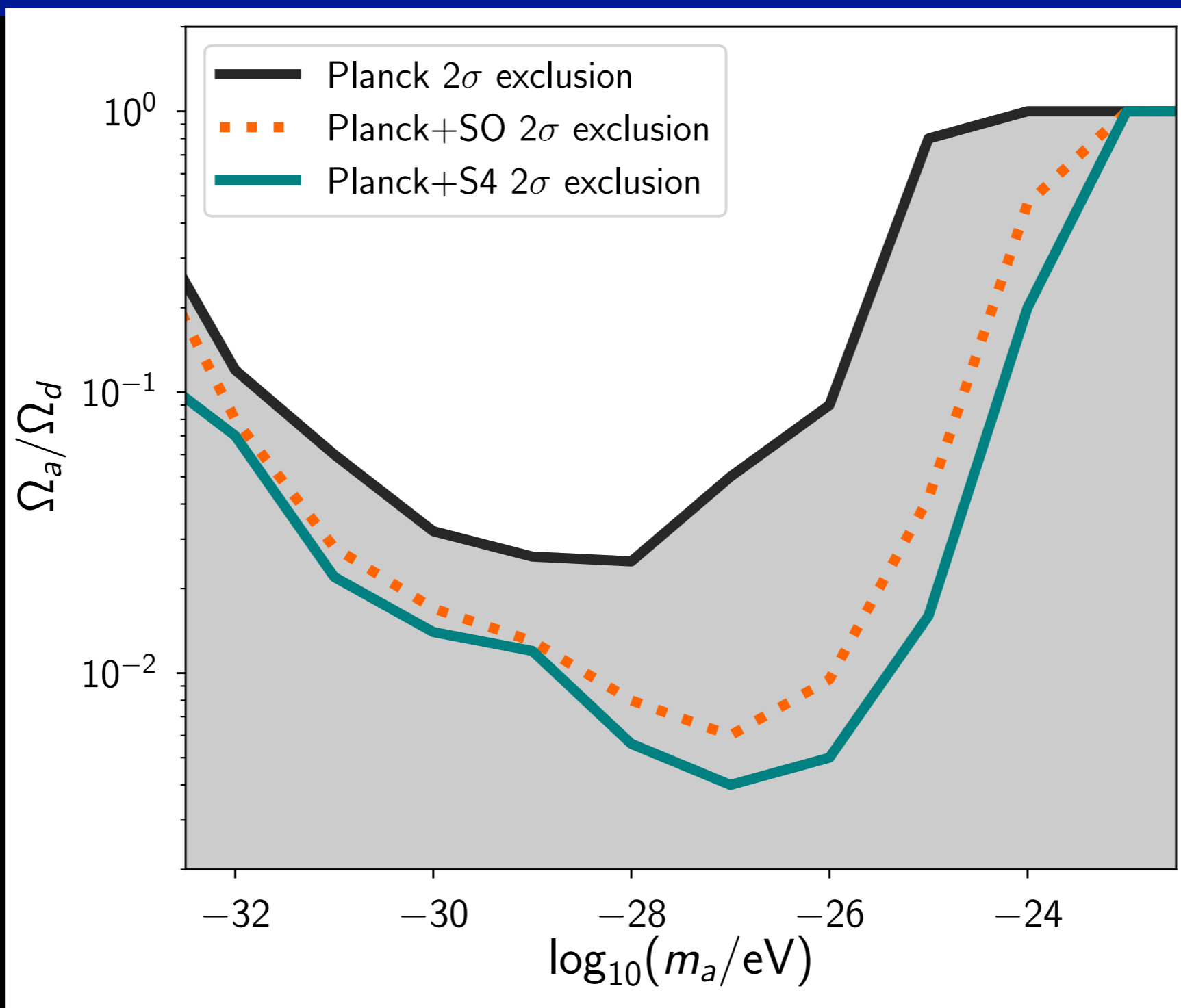
*arXiv: 1607.08208, Phys. Rev. D 95, 123511 (2017).*

*arXiv:1410.2896, Phys. Rev. D 91, 103512 (2015)*

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# Constraints

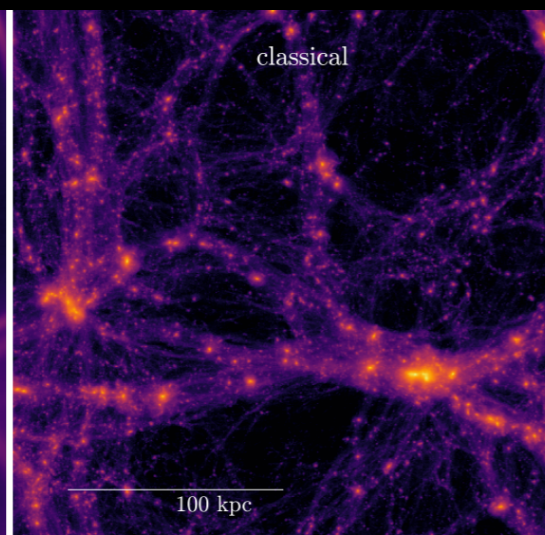
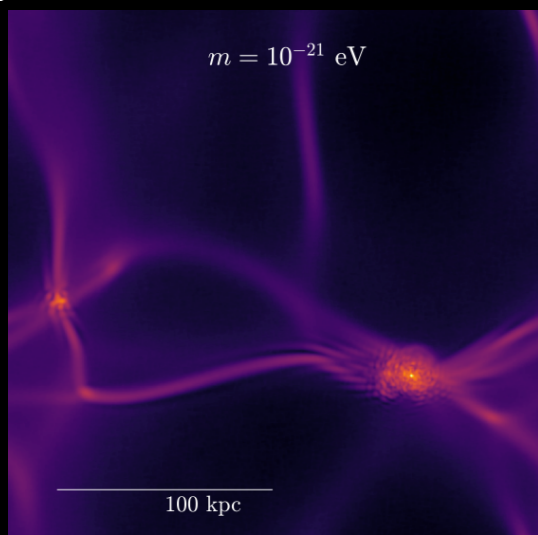
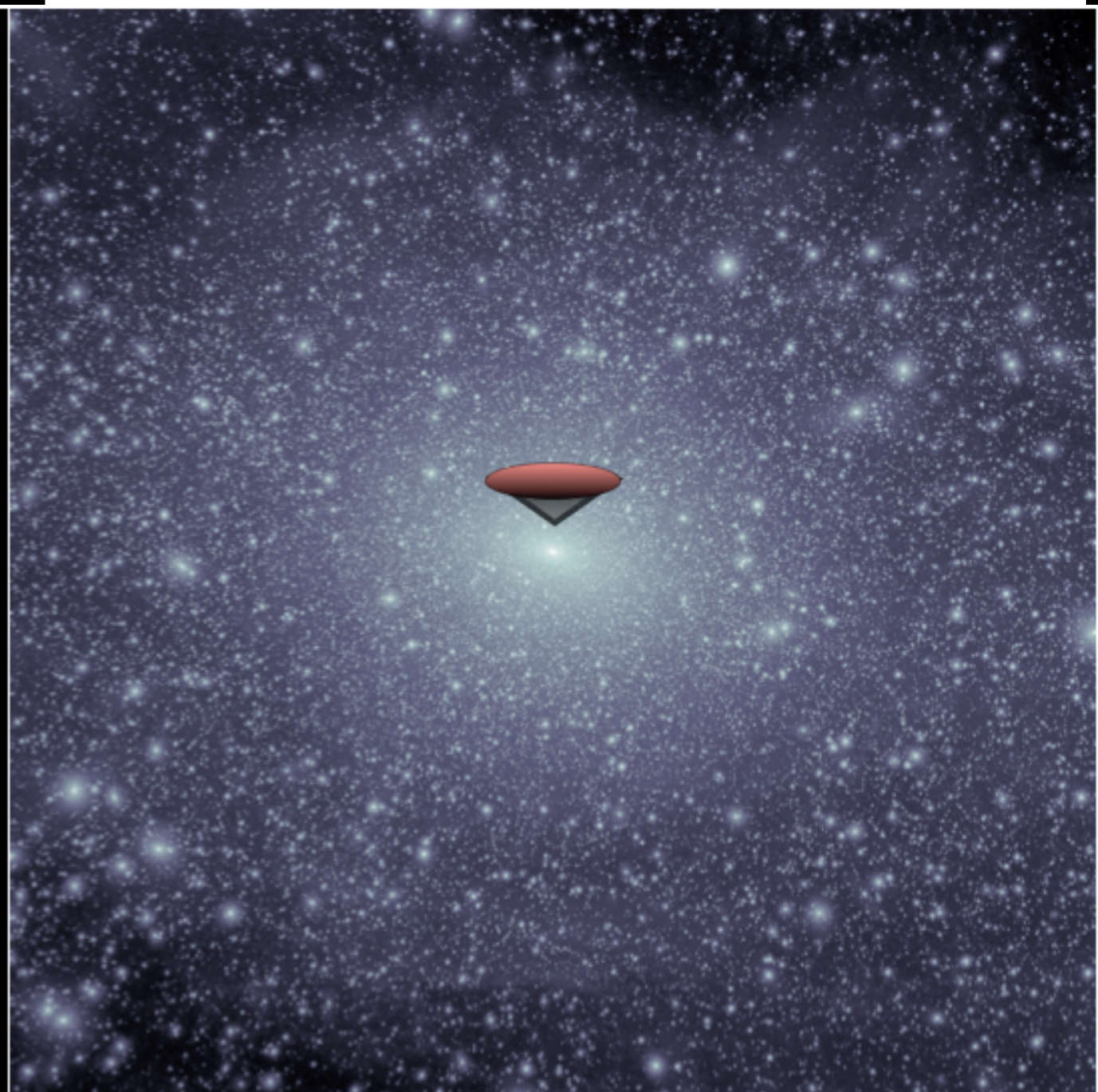
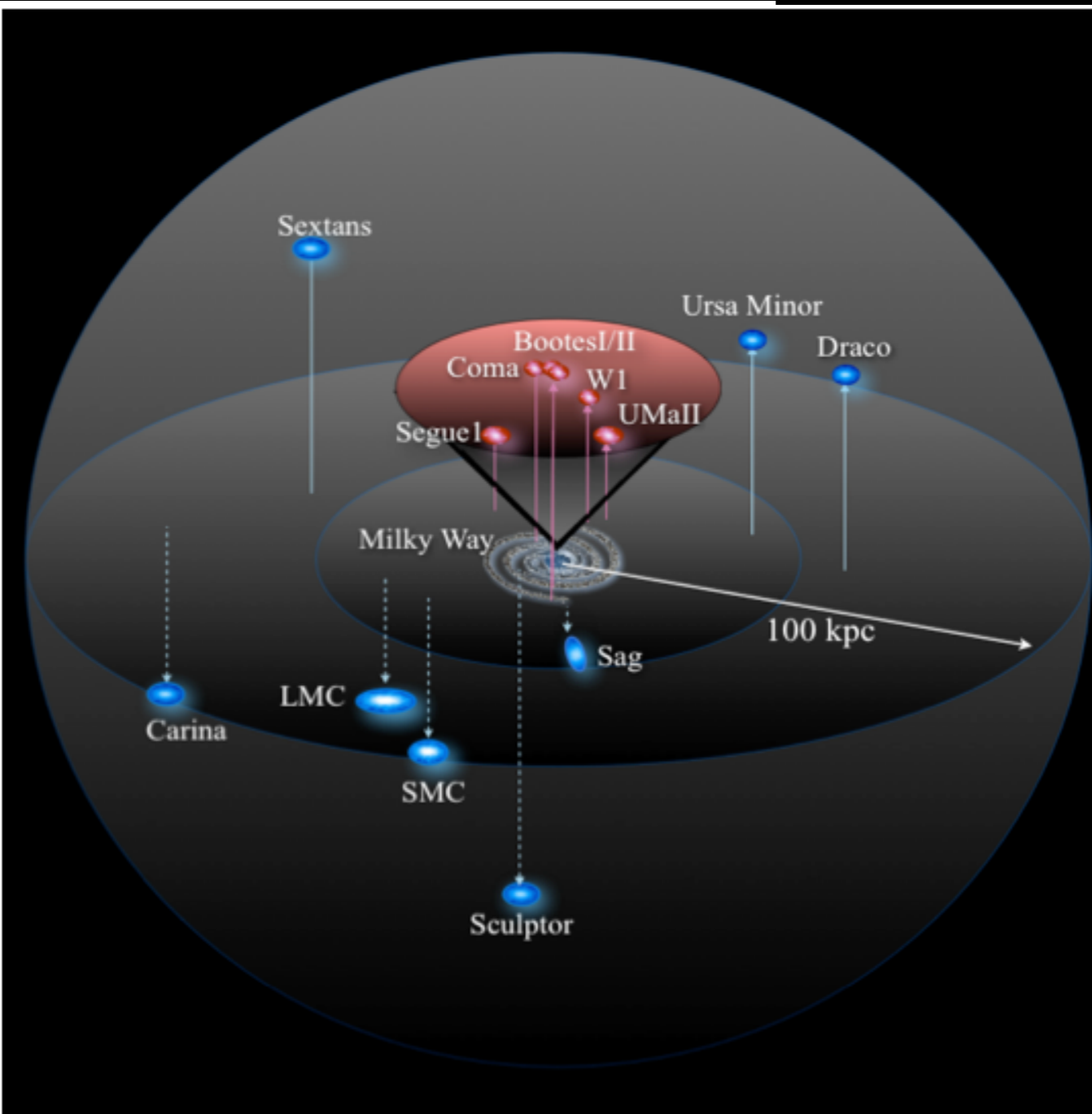


<https://arxiv.org/abs/1708.05681>

From CMB-S4 Science book/DSR report.... arXiv: 1610.02743, 1907.04473

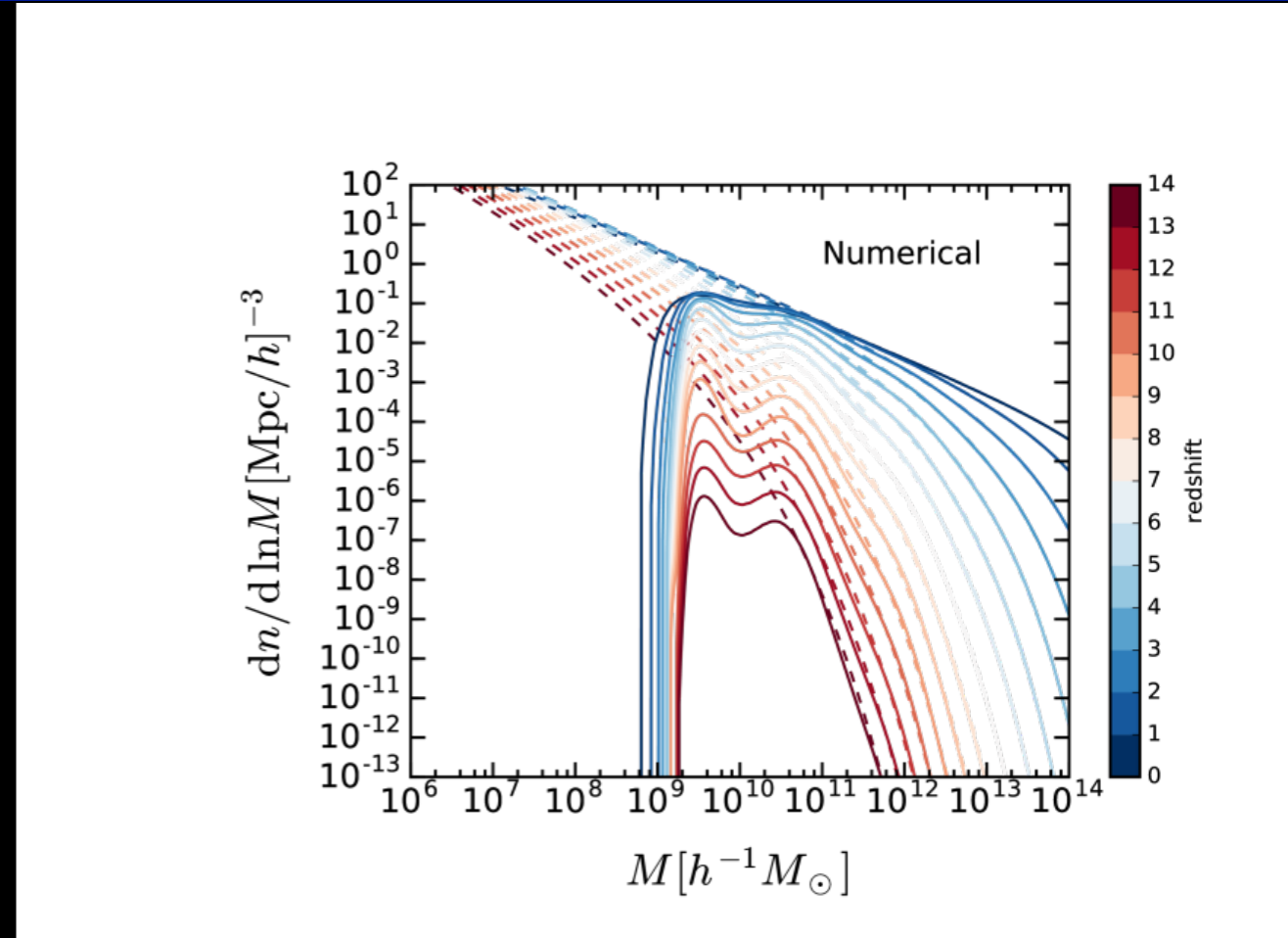
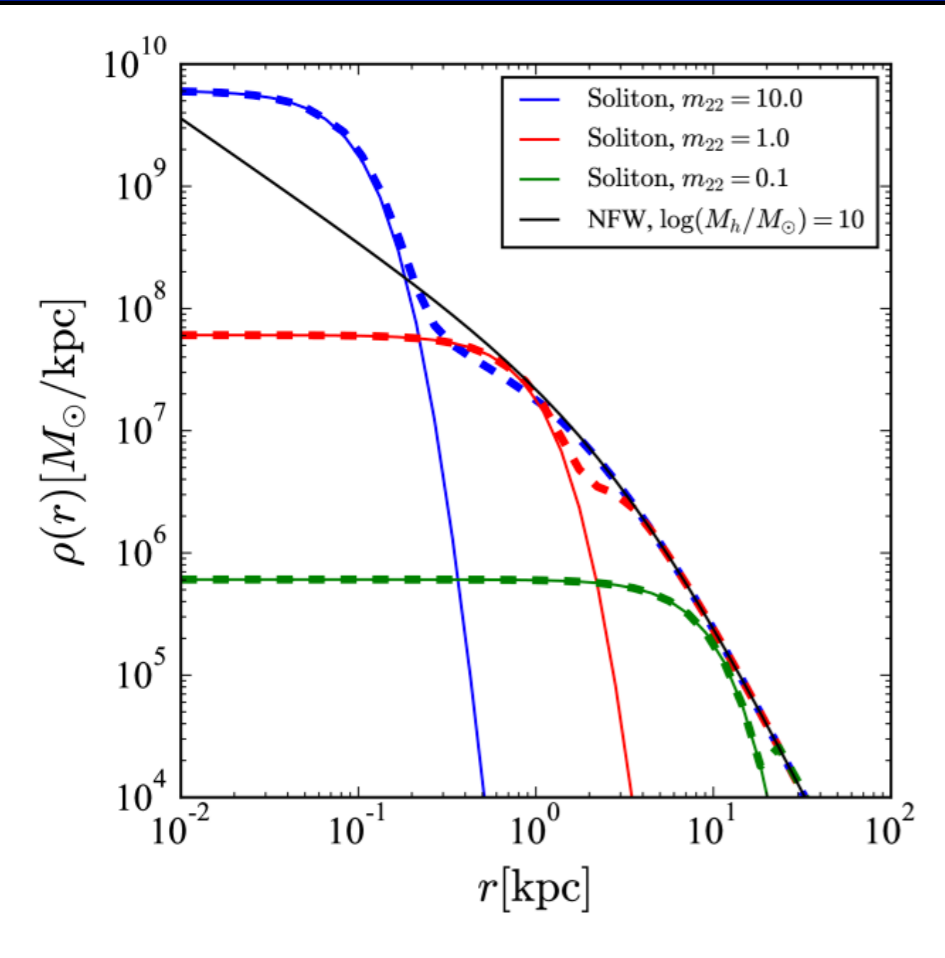


# ASTROPHYSICAL ATTRACTION (SMALL-SCALE CHALLENGES TO $\Lambda$ CDM)





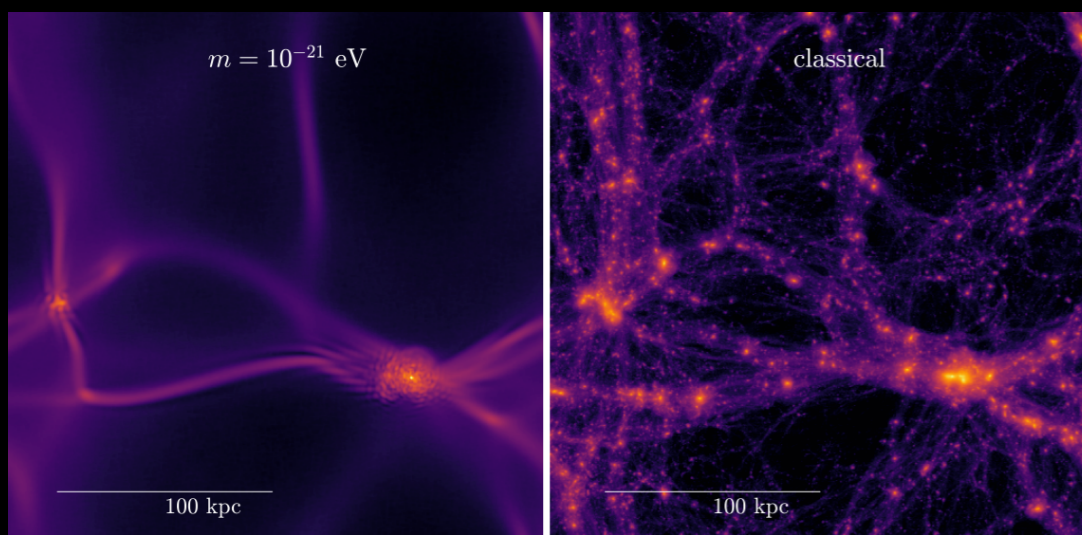
# ASTROPHYSICAL ATTRACTION (SMALL-SCALE CHALLENGES TO $\Lambda$ CDM)



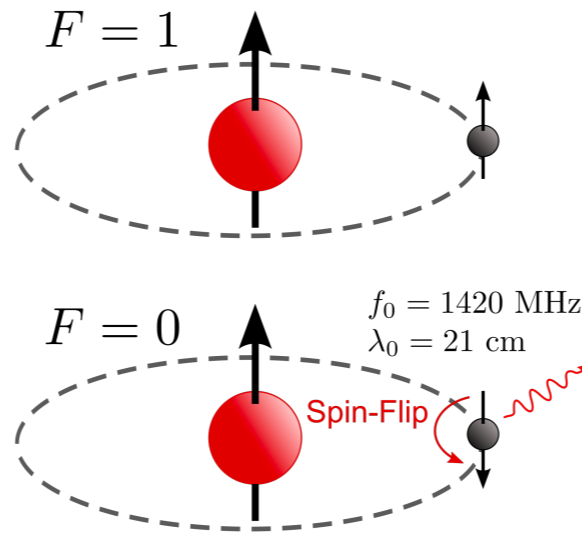
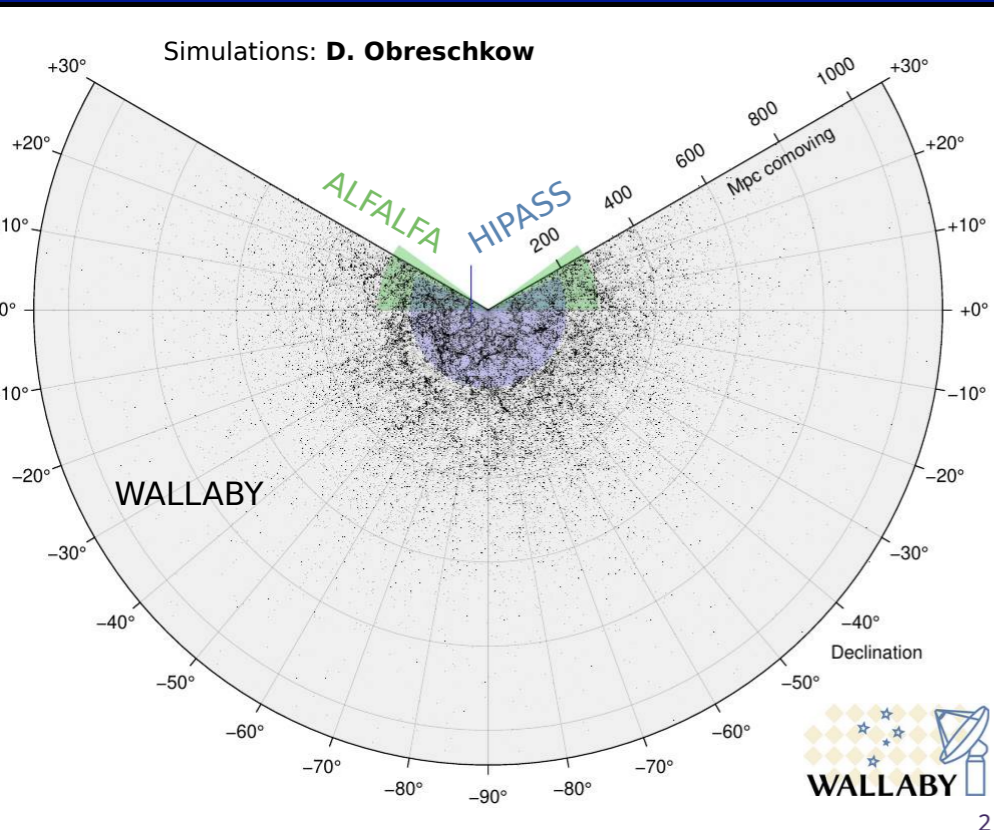
Safarzadeh & Spergel:  
The Astrophysical Journal, Volume 893, Number 1

Marsh, Physics Reports  
Volume 643, 1 July 2016, Pages 1-79

Mocz et al 2019.



# Extra-galactic HI surveys: $10^6 M_{\odot} \rightarrow 10^{11} M_{\odot}$



**CAUTION**  
**AREA UNDER**  
**CONSTRUCTION**

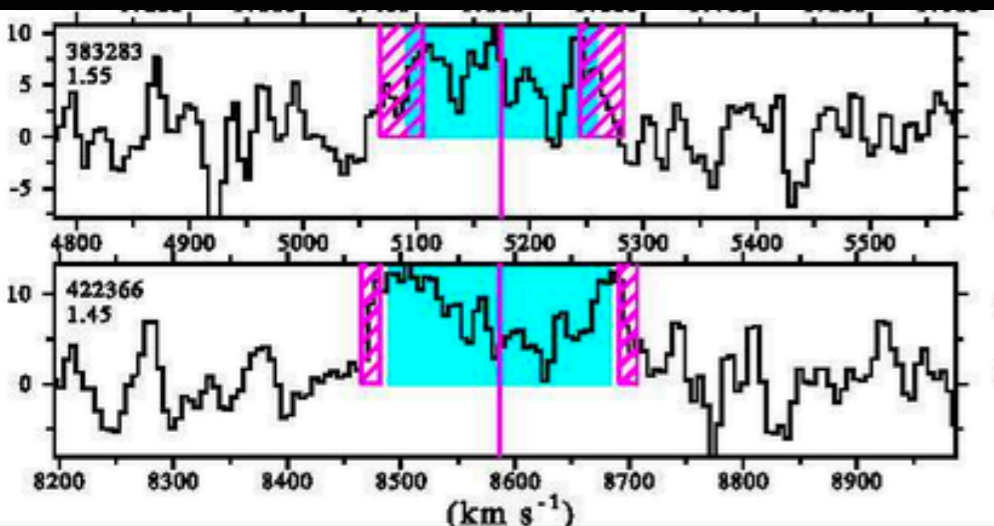
Figure/survey params from T. Westmeier

1. ALFALFA (Arecibo), done—

✦ 30,000 extragalactic HI line sources out to  $z \sim 0.06$ ,

2. Wallaby (SKA pathfinder, 36 X 12 m)

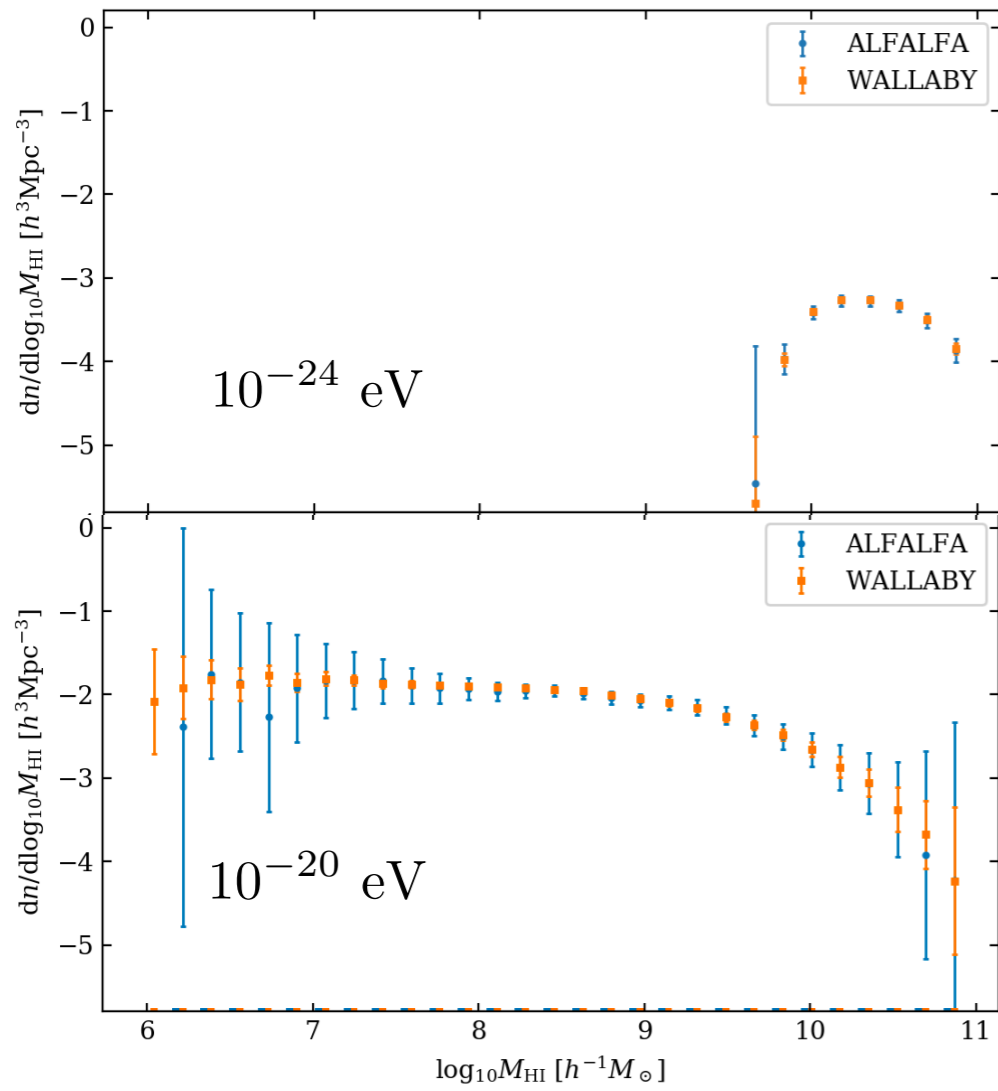
✦ 500,000 sources expected



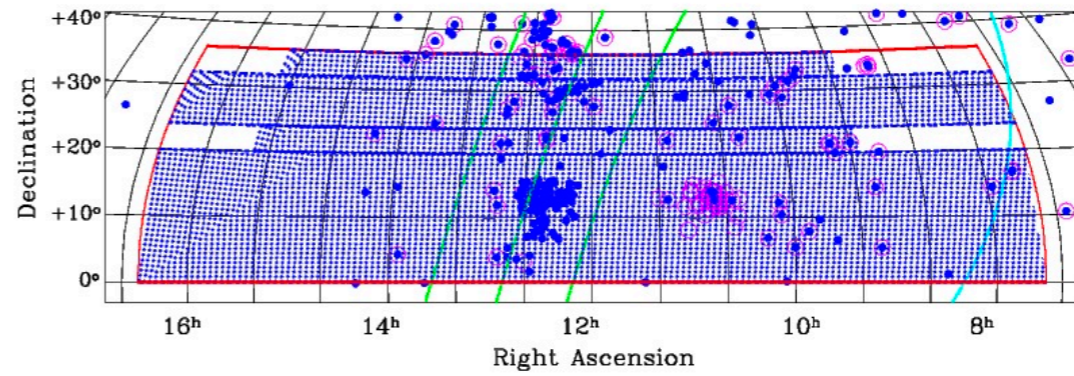
Simulations:

- 1) Specify survey volume — draw from mass function
- 2) Use semi-analytic  $M_{\text{halo}} \rightarrow M_{\text{HI}}$  conversion
- 3) Random LOS, geometric, realization
- 4) Mock observation

# Extra-galactic HI surveys

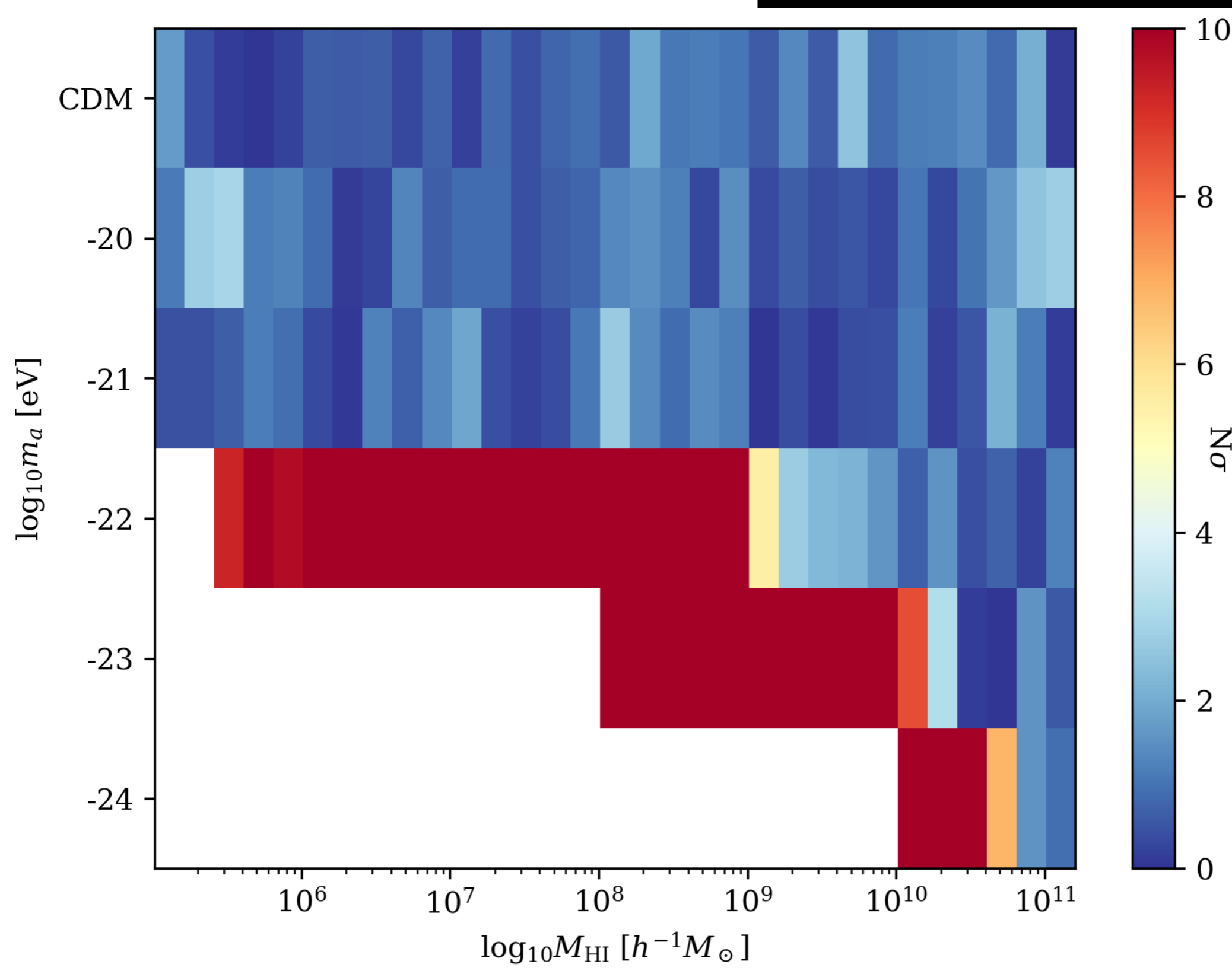


Haynes et al. 2013



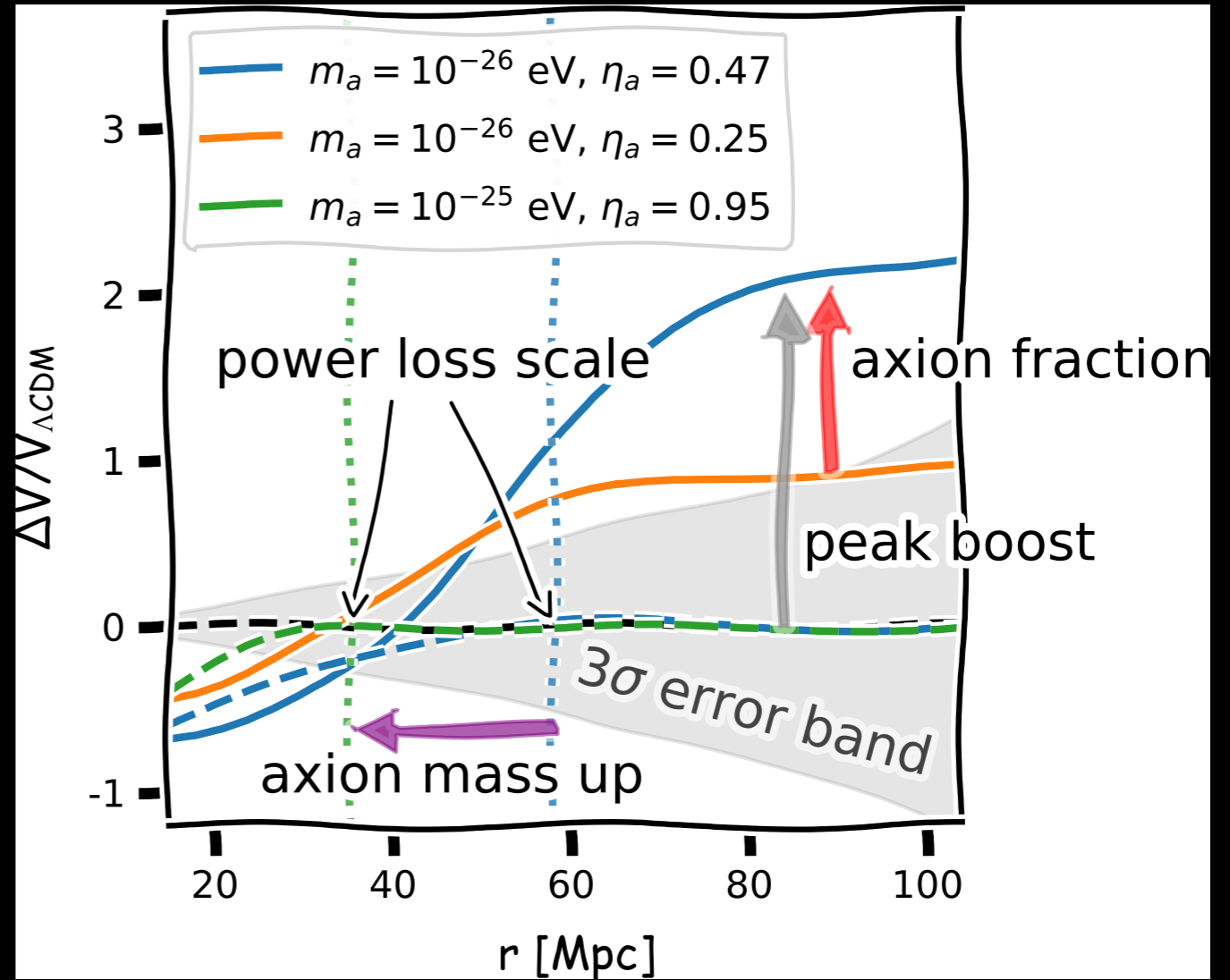
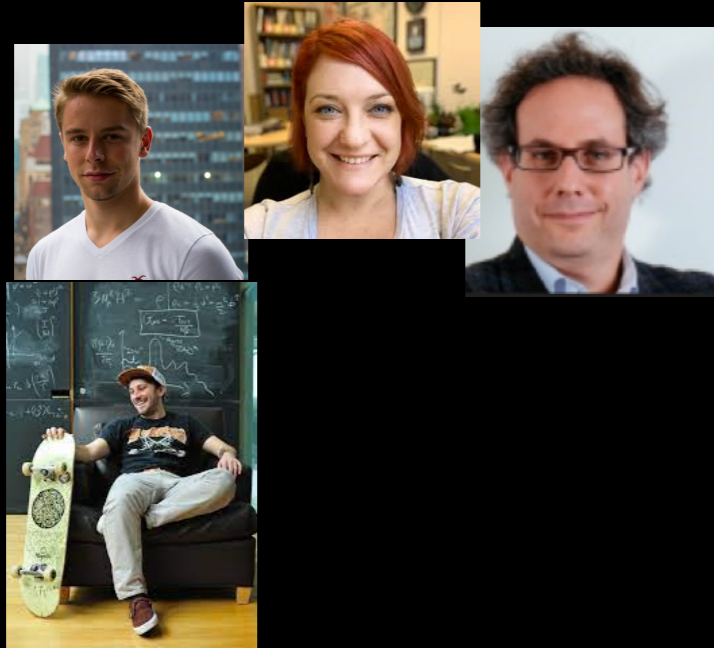
**CAUTION**  
**AREA UNDER**  
**CONSTRUCTION**

# Extra-galactic HI surveys



**CAUTION**  
**AREA UNDER**  
**CONSTRUCTION**



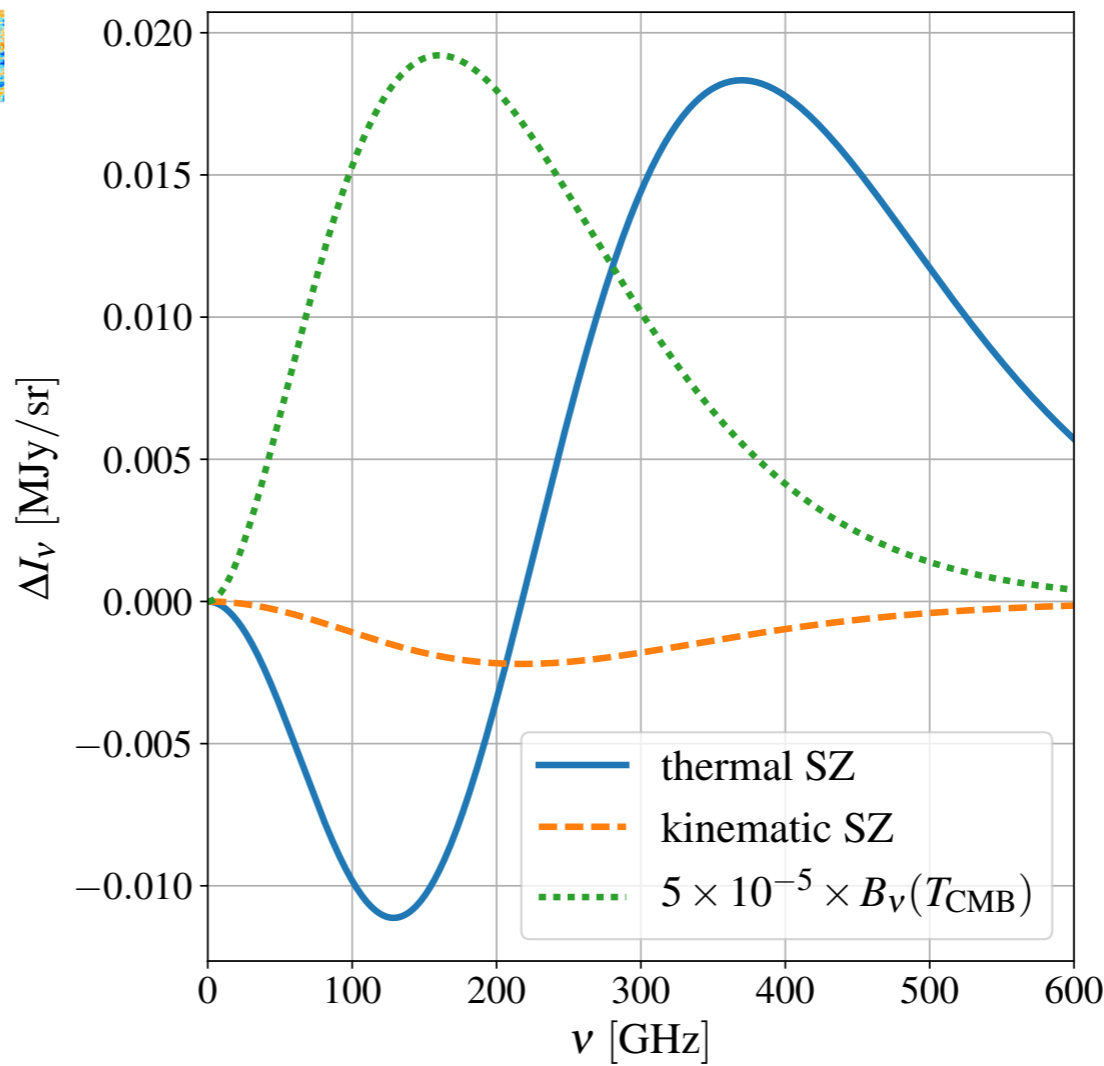
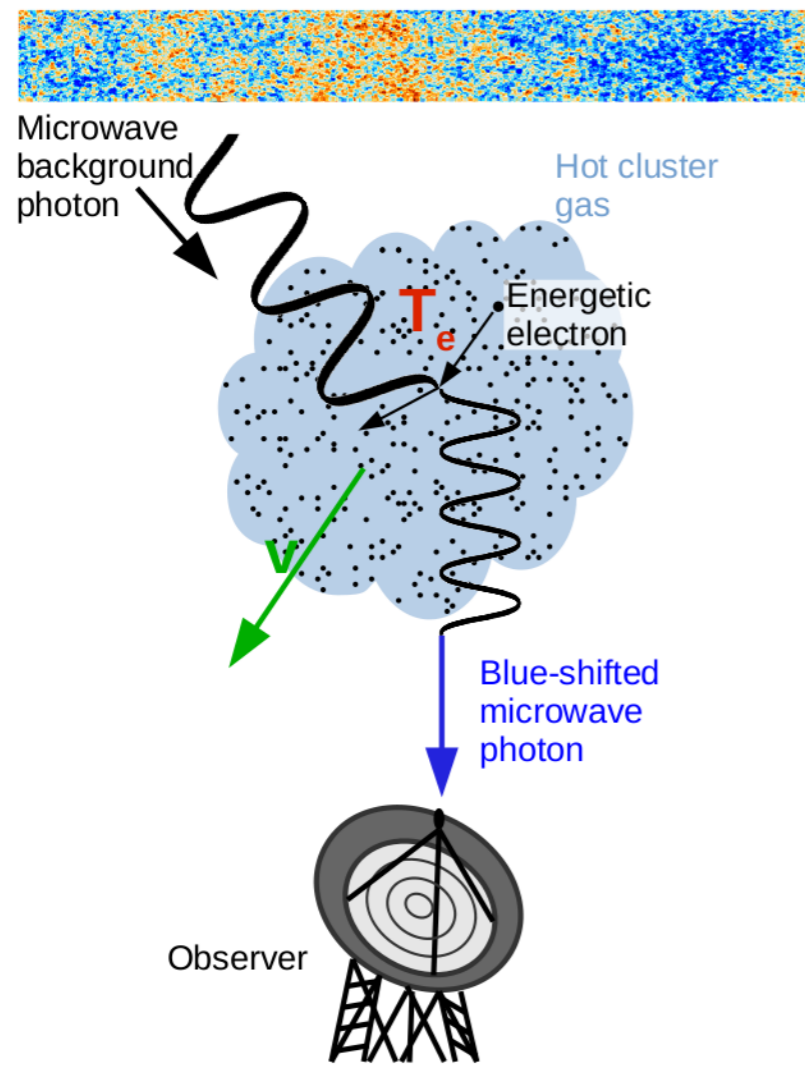


## ULAs and the kinetic SZ effect

arXiv:2109.13268

G. Farren, D. Grin, et al.....

# SUNYAEV ZEL'DOVICH EFFECT



*Soergel (2017)*

- Bulk flow contribution is kinetic (or kinematic) SZ effect:

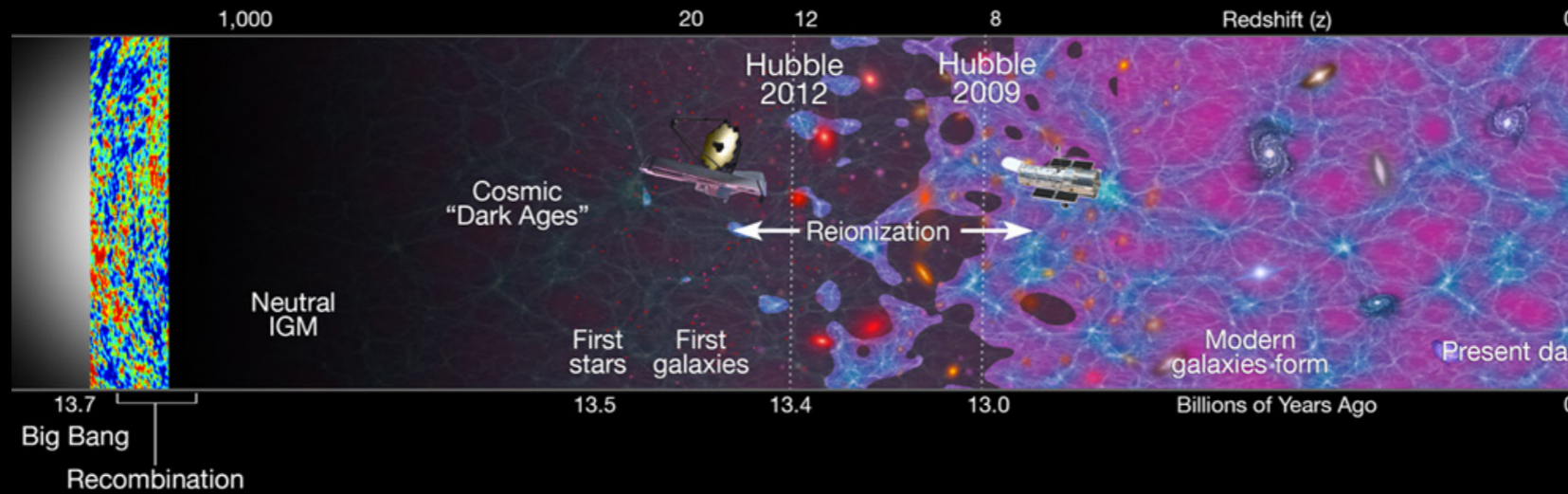
$$\frac{\Delta T_{\text{kSZ}}}{T_{\text{CMB}}} = -\sigma_T \int dl n_e \frac{\hat{\mathbf{r}} \cdot \mathbf{v}_e}{c} \simeq -\tau \frac{v_{\text{los}}}{c}$$

$$\Delta T_{\text{kSZ}} \approx 10 \mu\text{K}$$

Sunyaev ++ (1980)



# OSTRIKER-VISHNIAC EFFECT (SPECIAL CASE OF KSZ)



- Second-order contributions to power spectra from reionization

$$T \propto \bar{n}_e v \delta$$

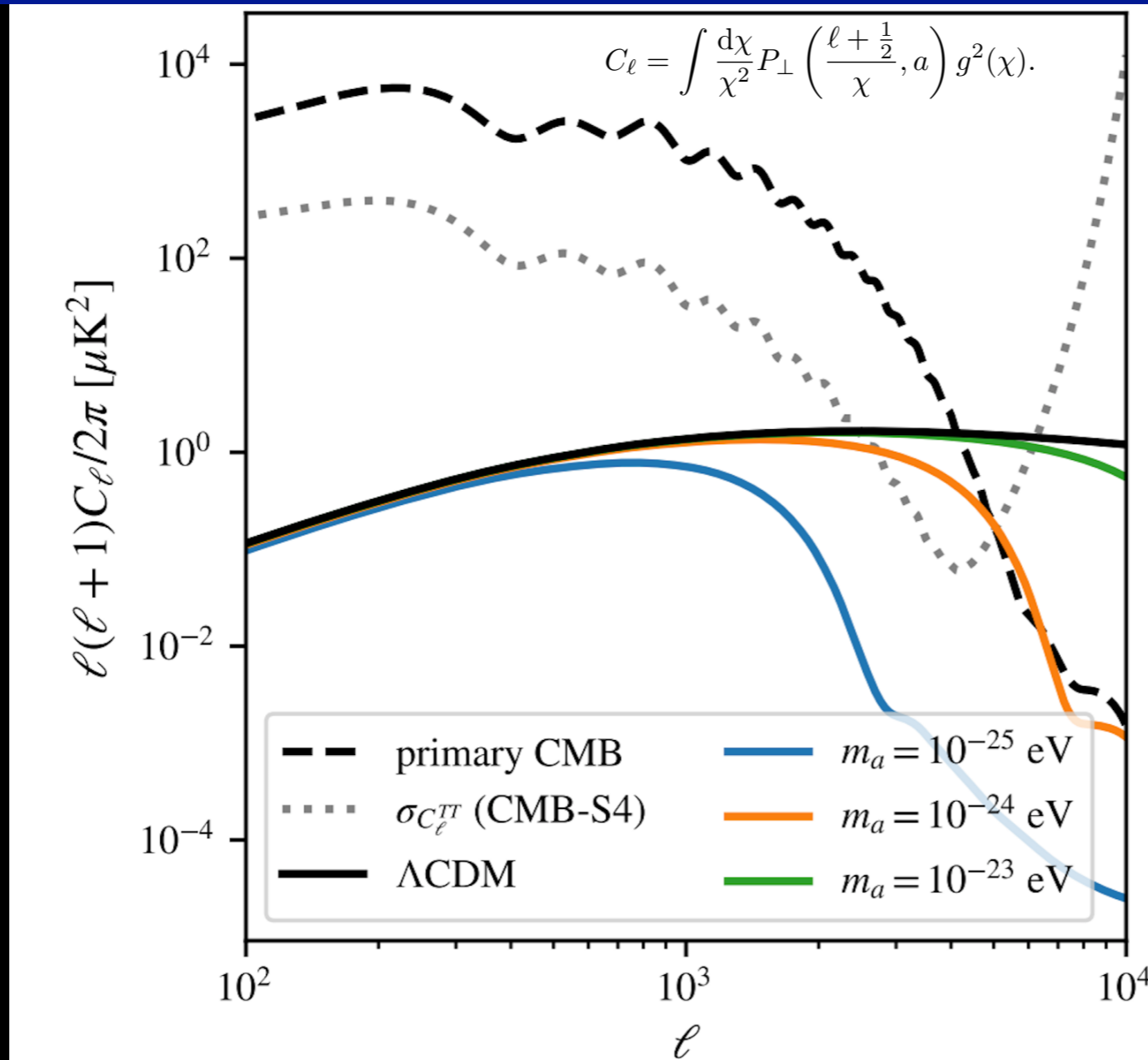
$$\frac{dv}{dt} \propto -\nabla\Phi \propto \delta \rightarrow v \propto \delta$$

$$T \propto \bar{n}_e \delta^2$$

$$C_l^{\text{TT}} \propto P^2(k)$$

# OSTRIKER-VISHNIAC EFFECT (SPECIAL CASE OF KSZ)

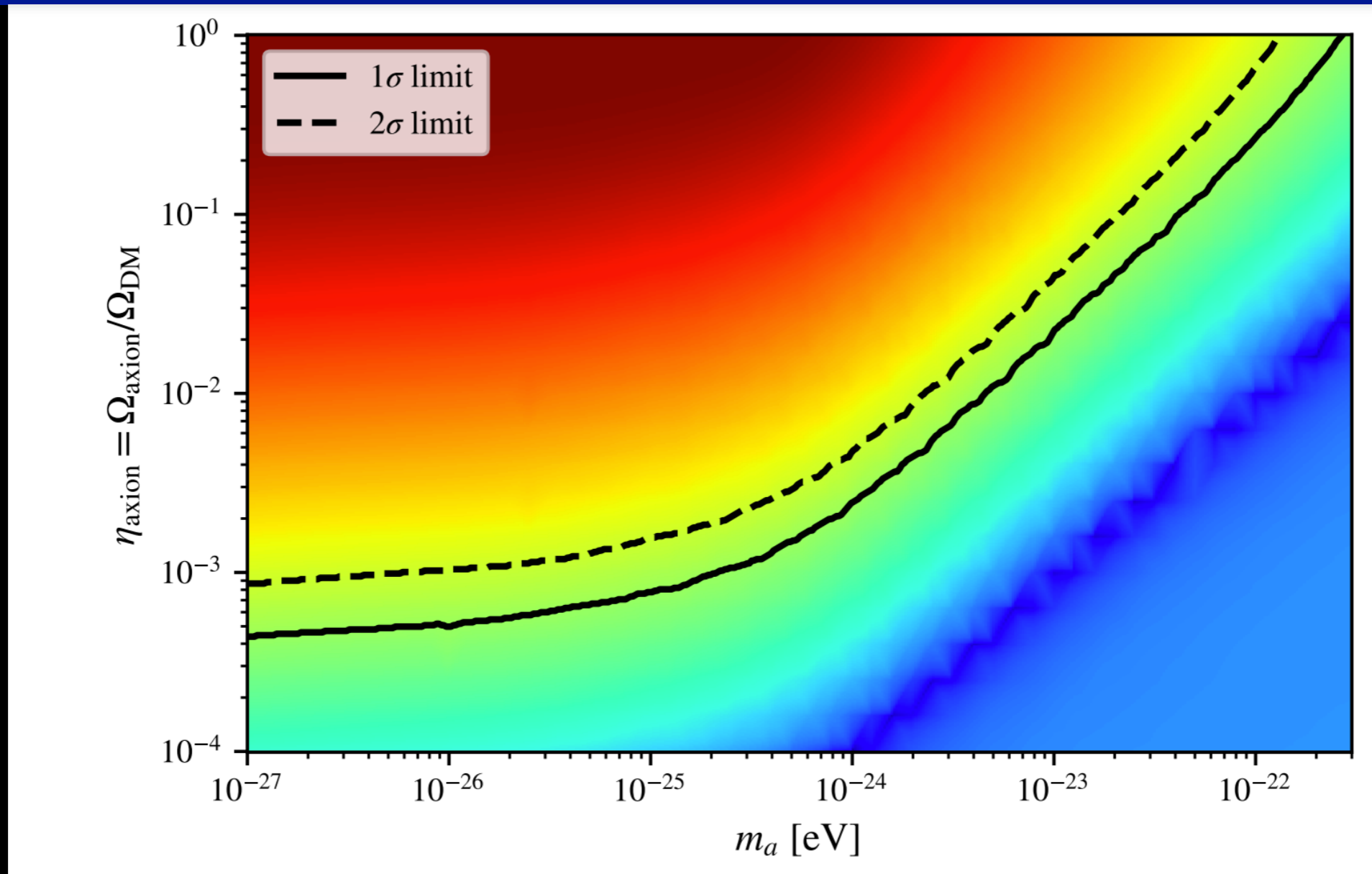
Ostriker+ (1986),  
Jaffe+ (1997)



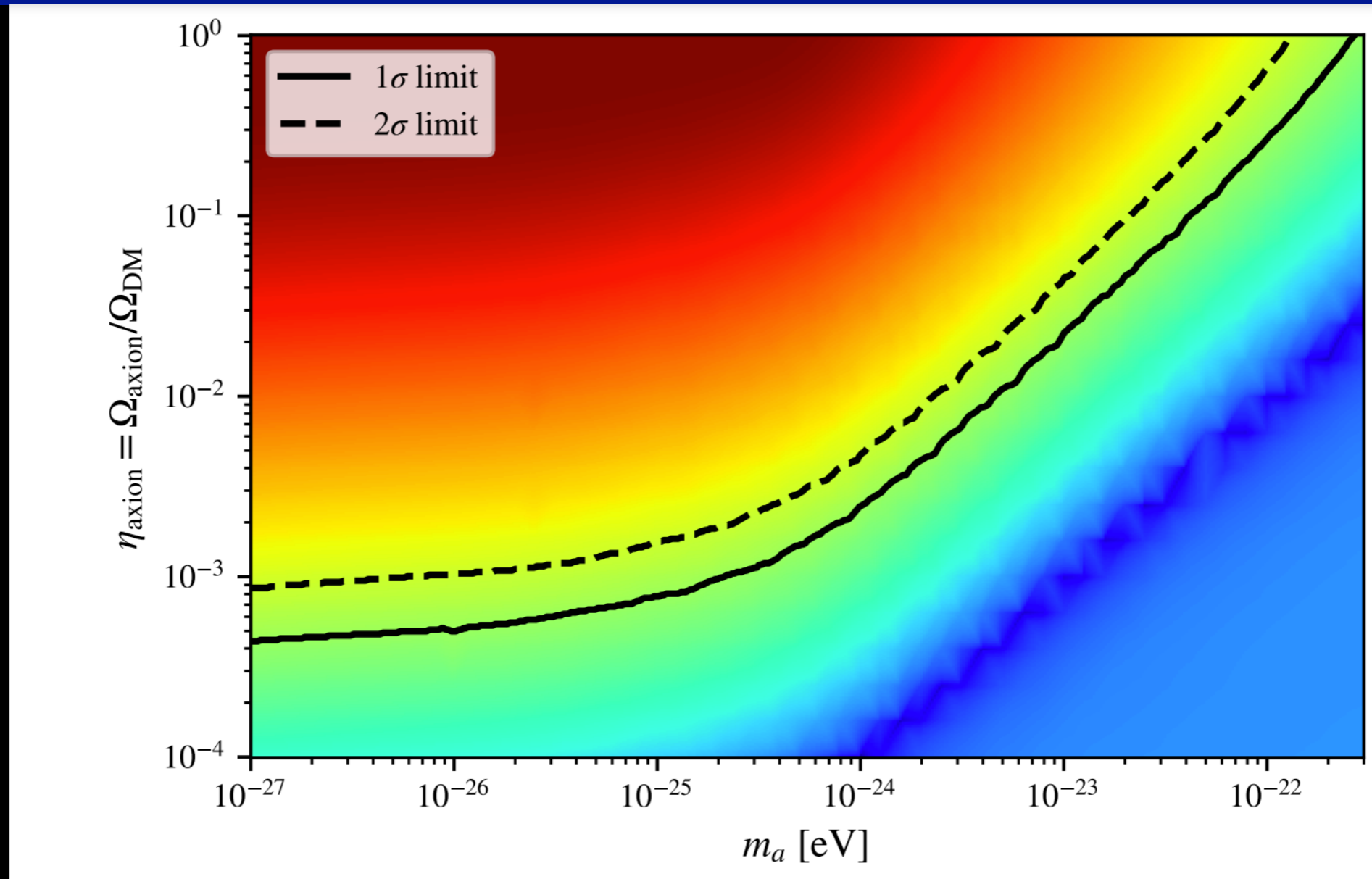
$$P_\perp(k, a) = \frac{a^2 H^2(a)}{8\pi^2} \int_0^\infty dy \int_{-1}^1 dx P_0(k\sqrt{1-2xy+y^2}) P_0(ky) \frac{\mathcal{G}^2(k\sqrt{1-2xy+y^2}, a)}{\mathcal{G}_0^2(k\sqrt{1-2xy+y^2})} \frac{\mathcal{G}^2(ky, a)}{\mathcal{G}_0^2(ky)}$$

$$\mathcal{G} = \frac{\delta_m(k, a)}{\delta_m(k, a=1)}$$

# OSTRIKER-VISHNIAC EFFECT (SPECIAL CASE OF KSZ)



# OSTRIKER-VISHNIAC EFFECT (SPECIAL CASE OF KSZ)



- Challenging to robustly detect ULA effect, even with future generation experiments
- **SOLUTION —LOOK NEAR HEAVIEST COSMIC STRUCTURES**



# KSZ — CLUSTER PAIRWISE VELOCITY DISPERSIONS

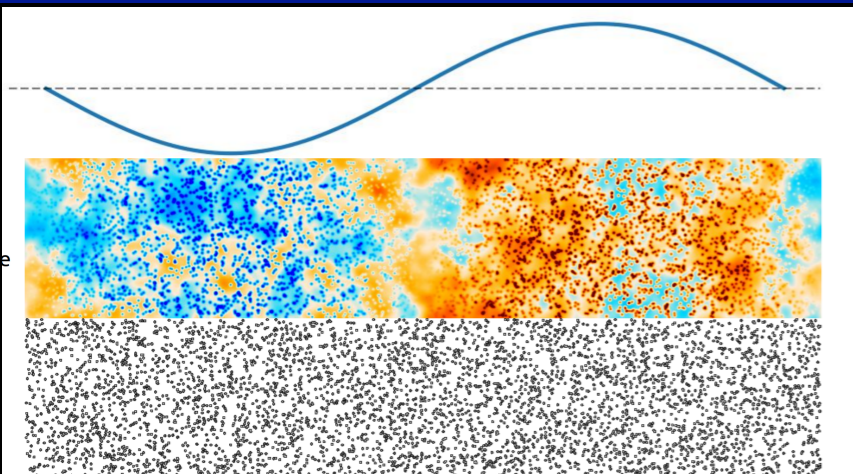
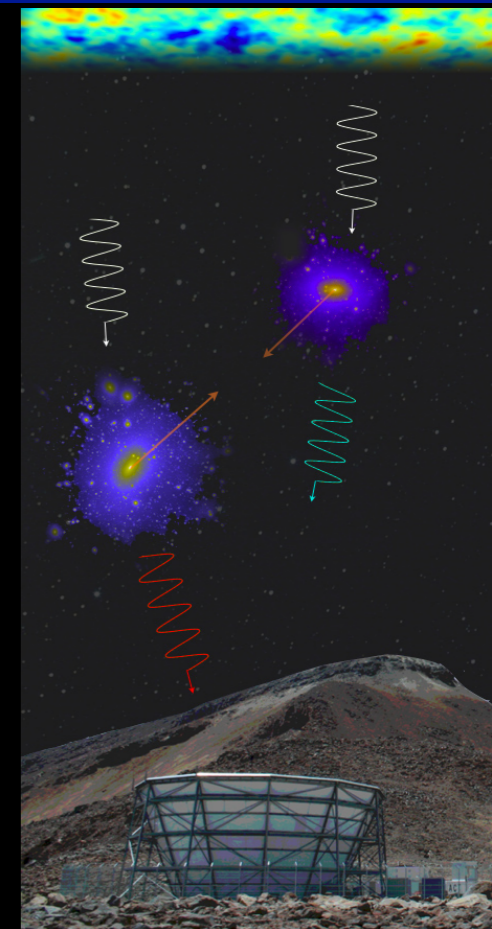


Figure from Madhavacheril...

Sunyaev ++ (1980)  
 Ostriker+ (1986), Jaffe+ (1997),  
 Sheth ++ (2001), Bhattacharya +  
 + (2007), Hand ++ (2012),  
 Mueller + (2014)



- Temperature change towards cluster due to local flow:

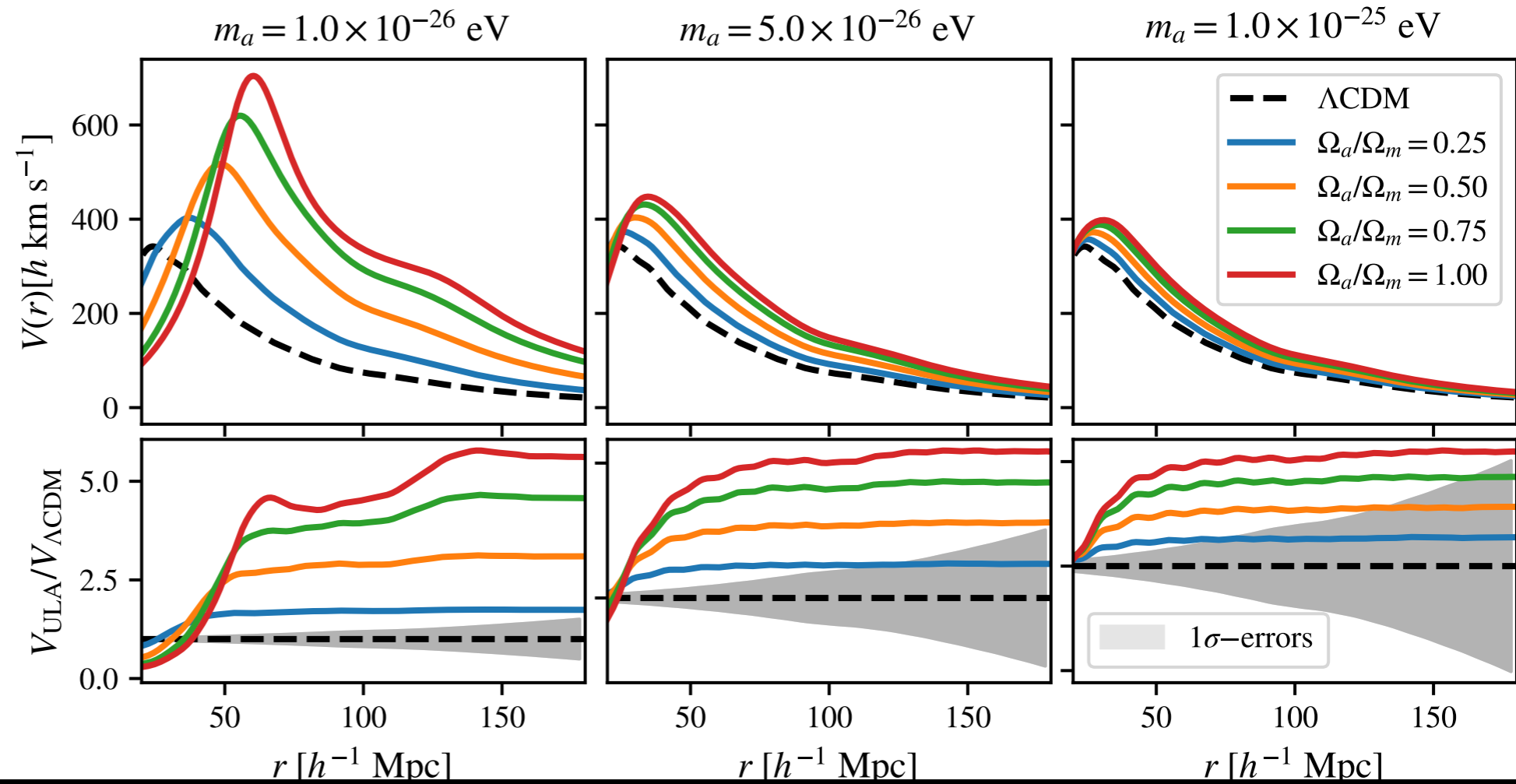
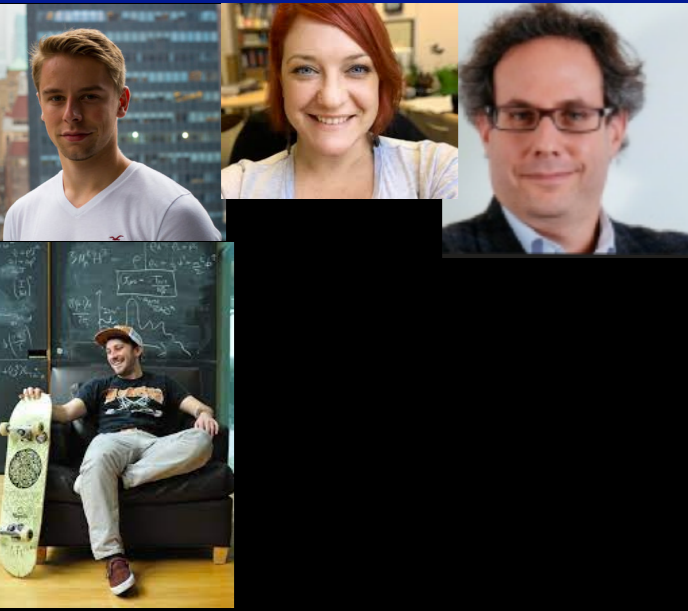
$$\frac{\Delta T}{T_{\text{CMB}}}(\hat{\mathbf{n}}_i) = -\tau_{e,i} \frac{\hat{\mathbf{r}}_i \cdot \mathbf{v}_i}{c}.$$

$$\Delta T_{\text{ksz}} \approx 10 \mu\text{K}$$

- Estimate assuming homogeneous optical depth:

$$\hat{T}_{\text{pkSZ}}(r) = -\frac{\sum_{i<j,r} [T(\hat{\mathbf{n}}_i) - T(\hat{\mathbf{n}}_j)] c_{ij}}{\sum_{i<j,r} c_{ij}^2} = \bar{\tau}_e \frac{v_{12}(r)}{c} T_{\text{CMB}}$$

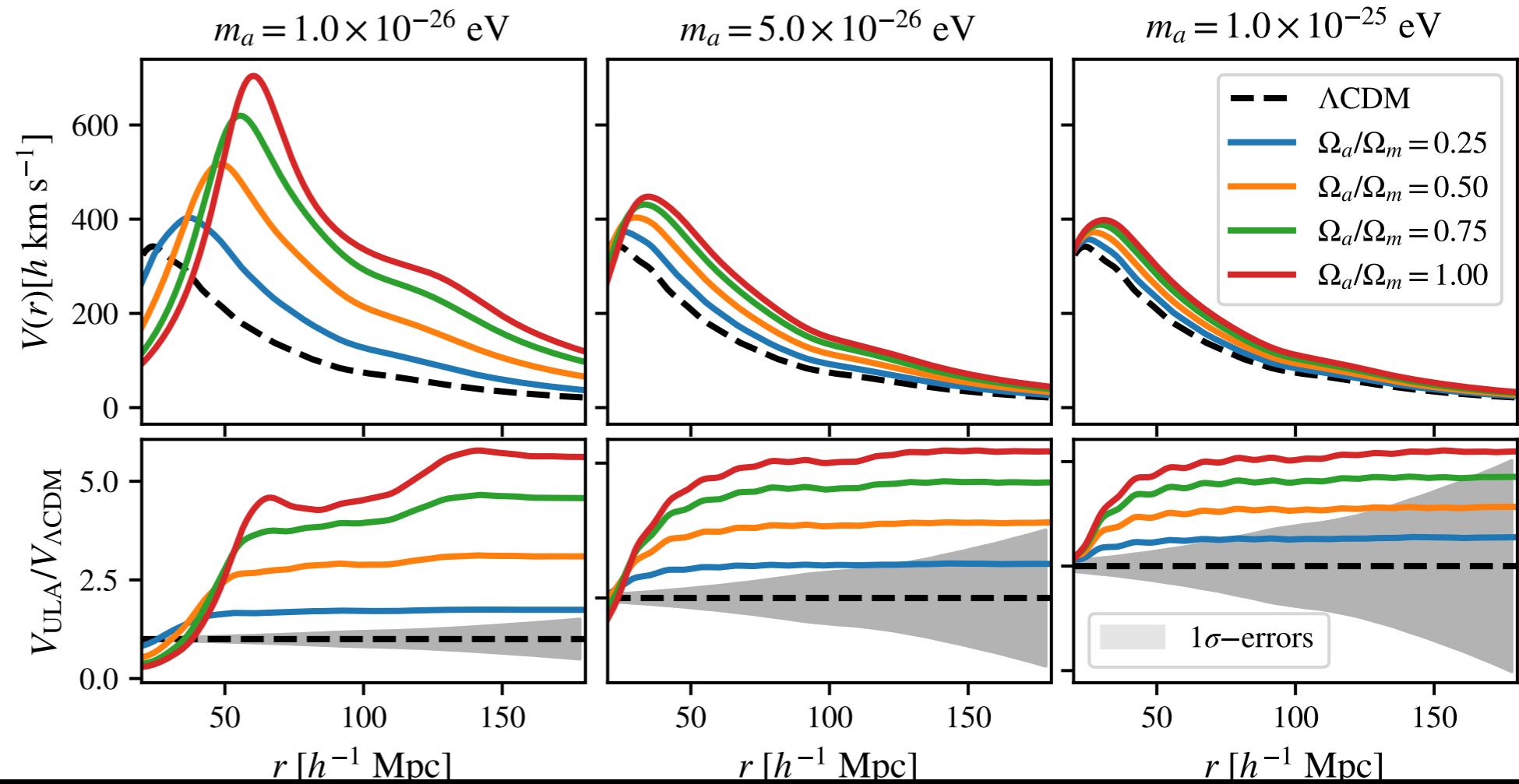
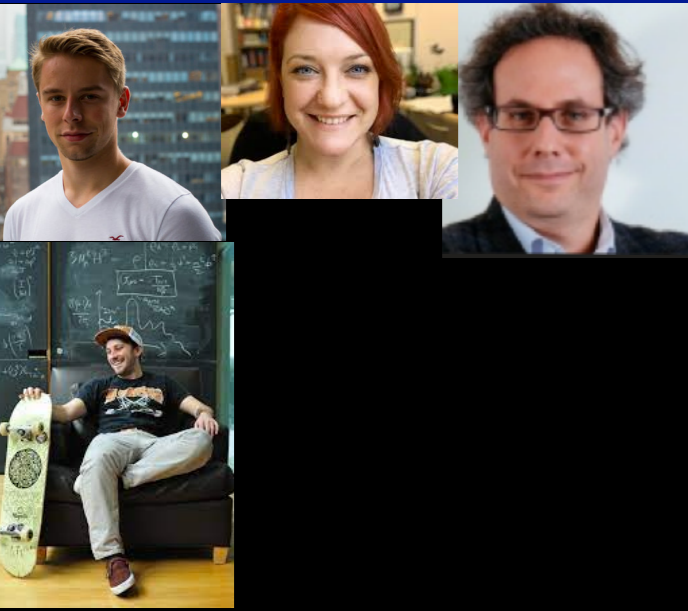
# KSZ — EFFECT OF ULAS



$$v_{12}(r) \propto \int d \ln k \langle b(k, M, a) \rangle \Delta^2(k, a) \frac{d \ln \delta(k, a)}{dt} W(kr)$$



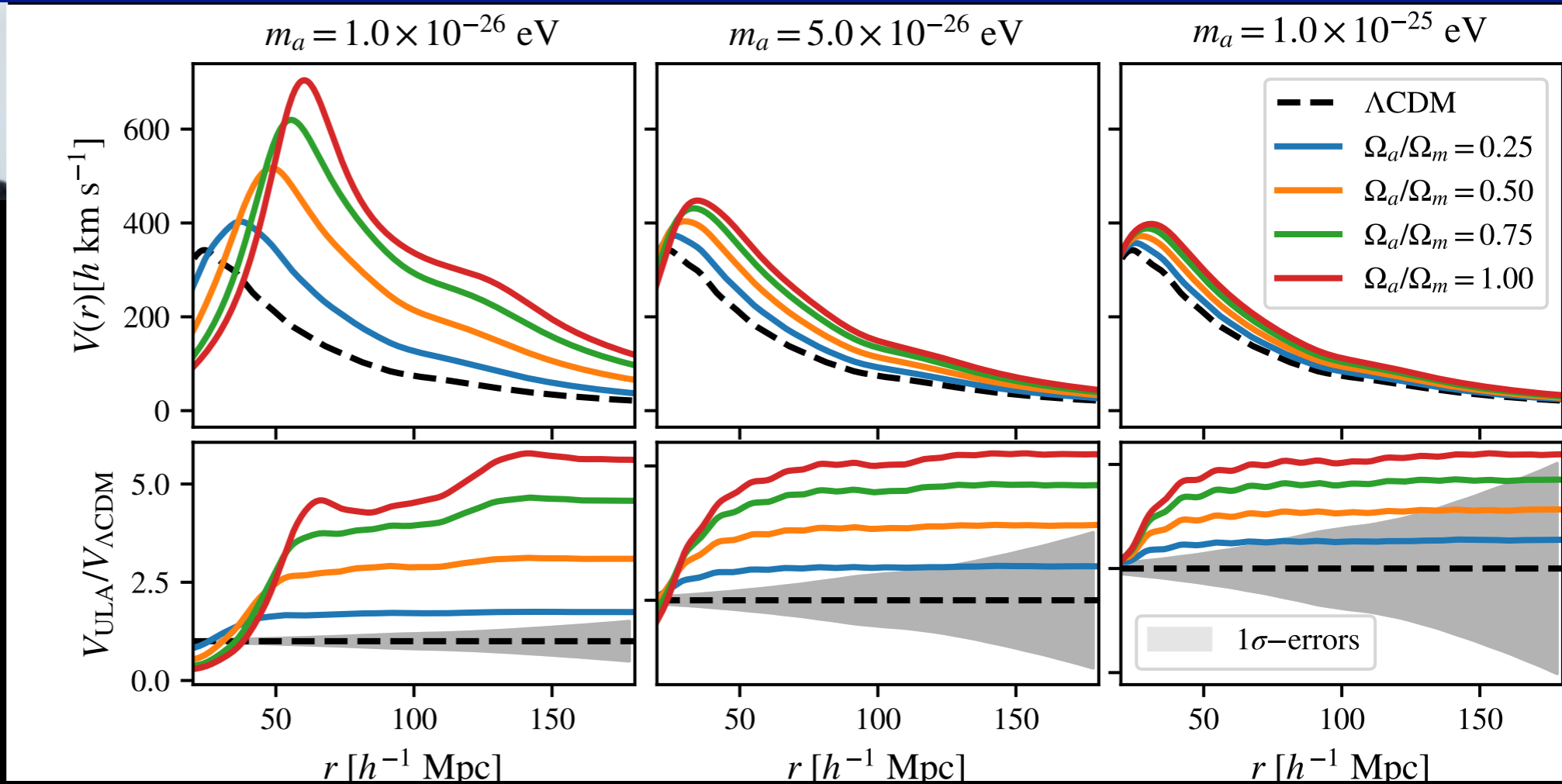
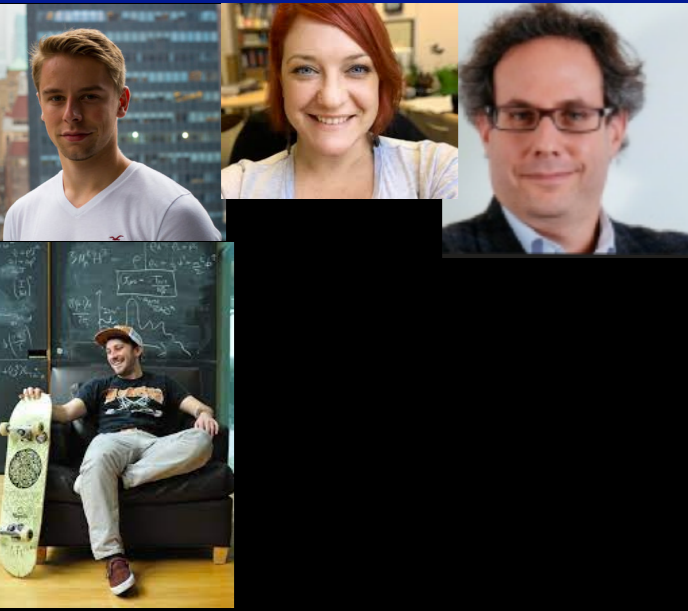
# KSZ — EFFECT OF ULAS



Halo bias

$$v_{12}(r) \propto \int d \ln k \langle b(k, M, a) \rangle \Delta^2(k, a) \frac{d \ln \delta(k, a)}{dt} W(kr)$$

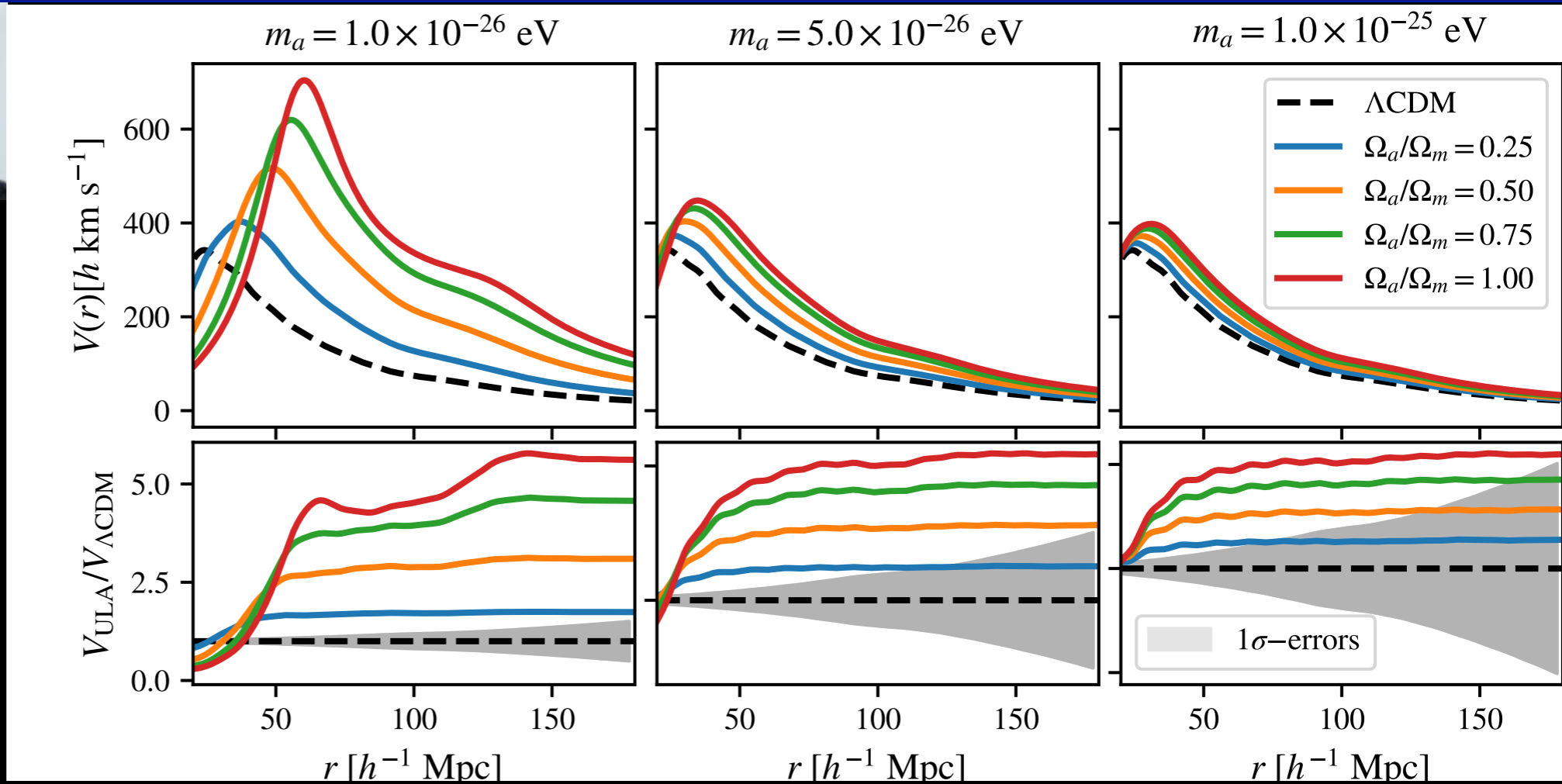
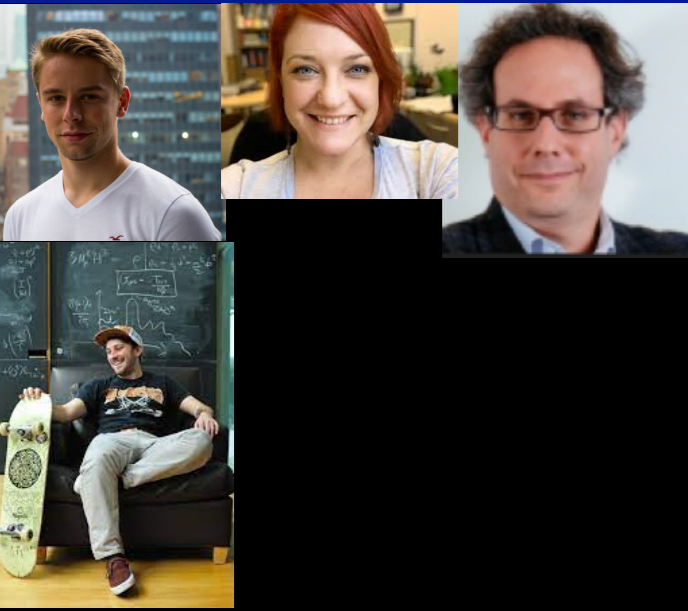
# KSZ — EFFECT OF ULAS



Typical fluct. on scale k

$$v_{12}(r) \propto \int d \ln k \langle b(k, M, a) \rangle \Delta^2(k, a) \frac{d \ln \delta(k, a)}{dt} W(kr)$$

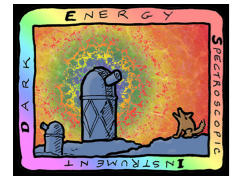
# KSZ — EFFECT OF ULAS



Geometric window

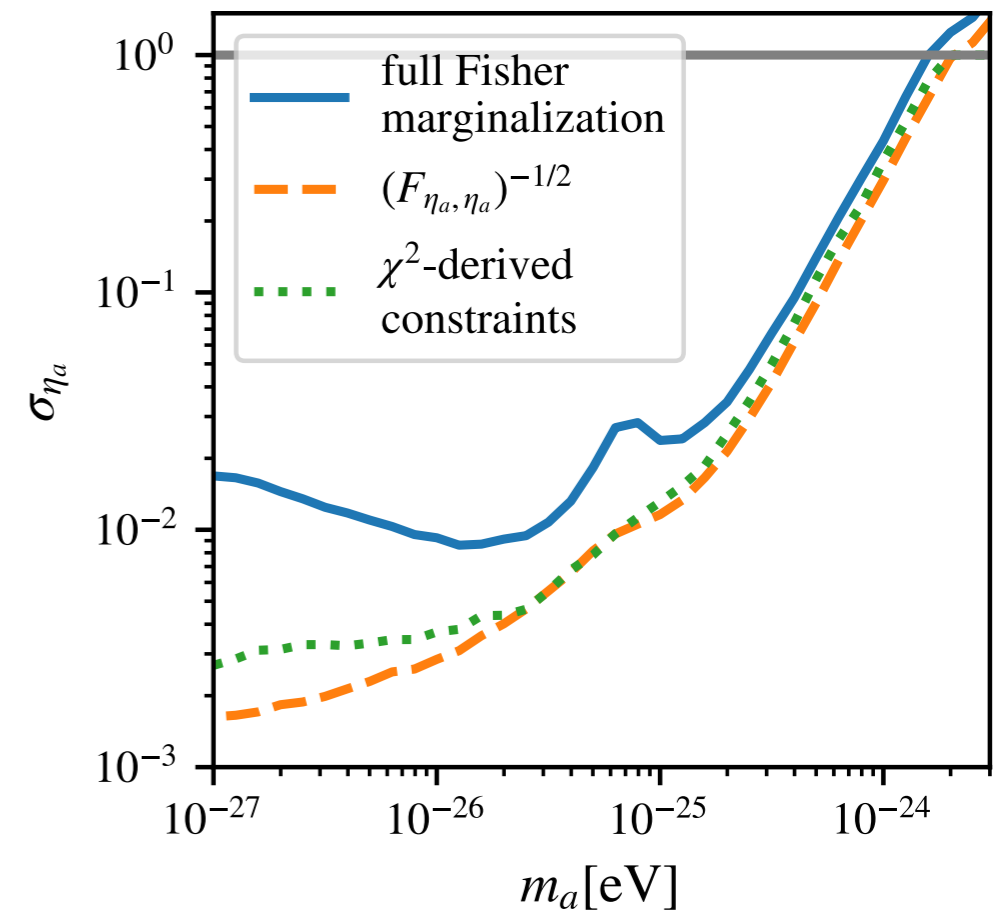
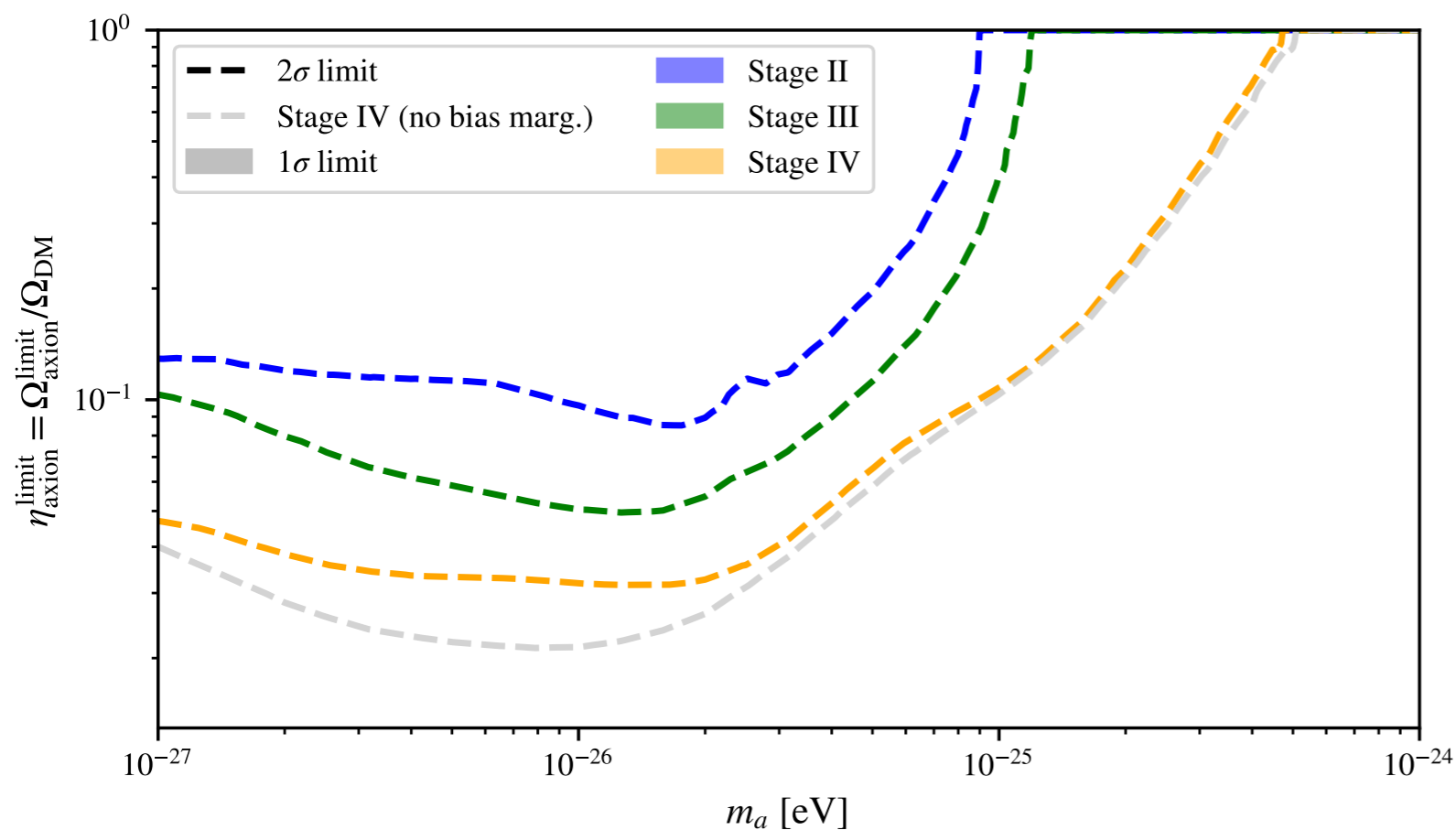
$$v_{12}(r) \propto \int d \ln k \langle b(k, M, a) \rangle \Delta^2(k, a) \frac{d \ln \delta(k, a)}{dt} W(kr)$$

# COVARIANCE, NOISE, AND FORECASTING

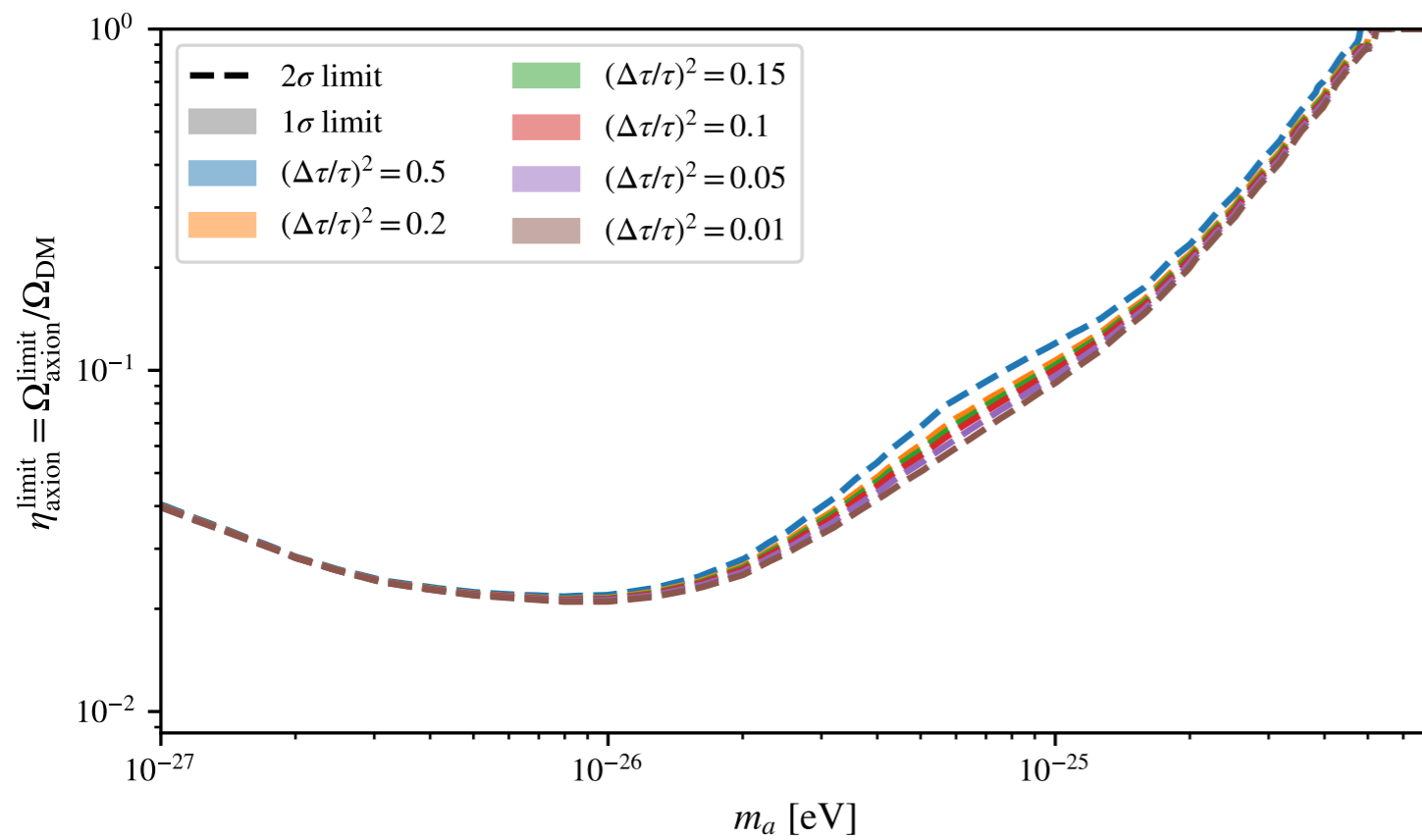


$$F_{\mu\nu} = \sum_i^{N_z} \sum_{j,k}^{N_r} \frac{\partial v(r_j, z_i)}{\partial p_\mu} C^{-1}(r_j, r_k, z_i) \frac{\partial v(r_k, z_i)}{\partial p_\nu}$$

Survey	Parameters	Survey Stage		
		II	III	IV
CMB	$\Delta T_{\text{instr}}$ ( $\mu\text{K arcmin}$ )	20	7	1
Galaxy	$z_{\text{min}}$	0.1	0.1	0.1
	$z_{\text{max}}$	0.4	0.4	0.6
	No. of $z$ bins, $N_z$	3	3	5
	$M_{\text{min}}$ ( $10^{14} M_\odot$ )	1	1	0.6
Overlap	Area (1000 sq. deg.)	4	6	10



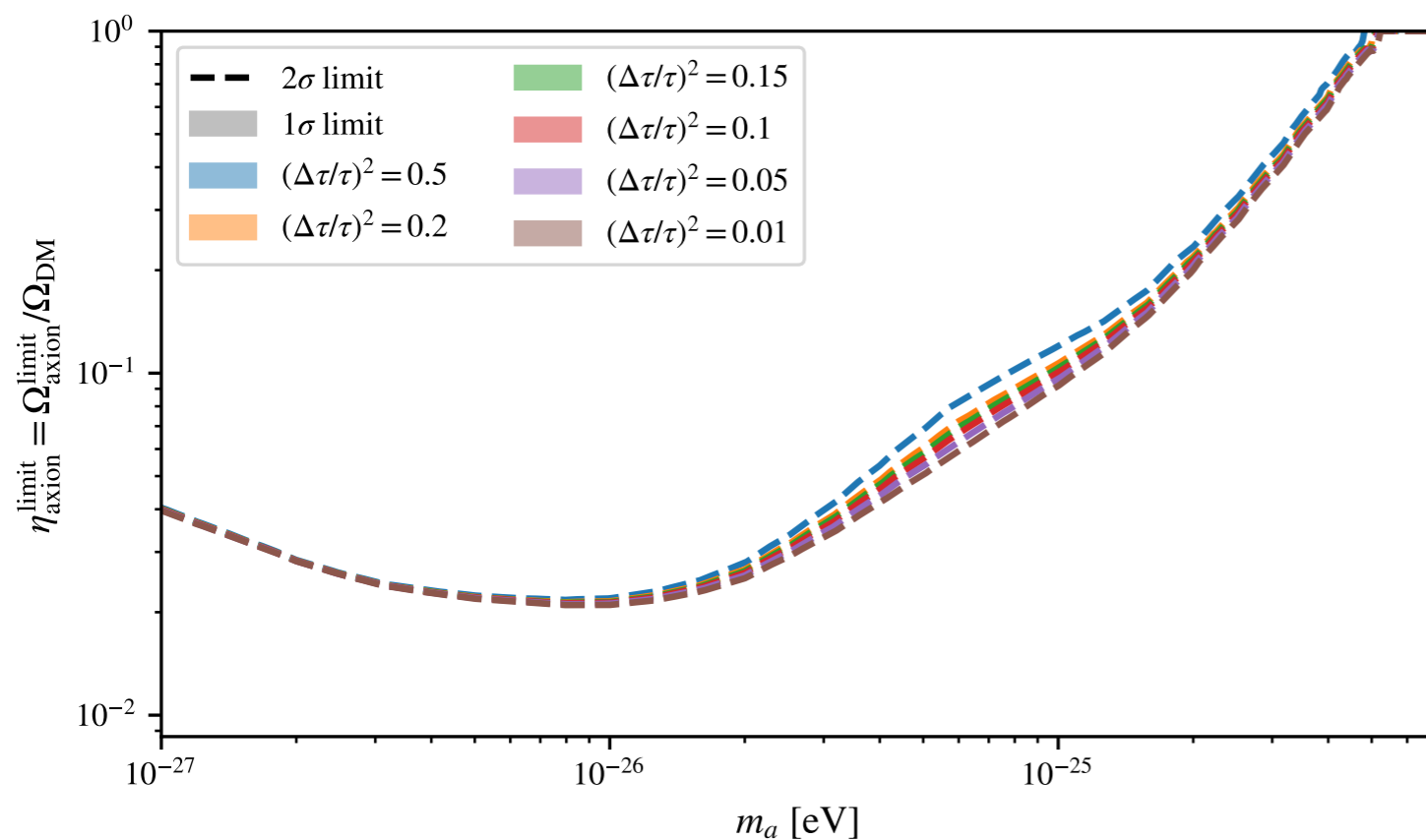
# SYSTEMATIC UNCERTAINTIES



$$\frac{\Delta T}{T_{\text{CMB}}}(\hat{\mathbf{n}}_i) = -\tau_{e,i} \frac{\hat{\mathbf{r}}_i \cdot \mathbf{v}_i}{c}.$$

$$\mathcal{B} \rightarrow b(z)\mathcal{B}$$

# SYSTEMATIC UNCERTAINTIES



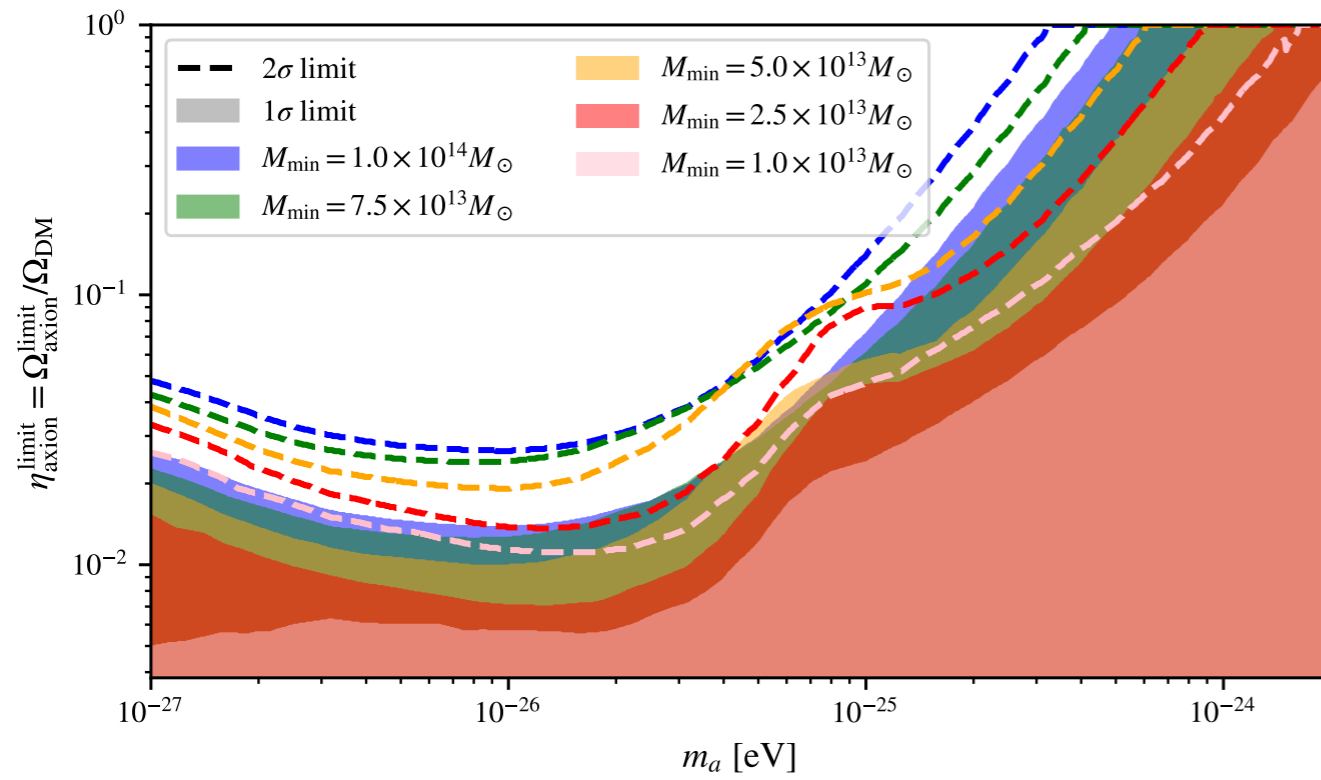
## Cluster astrophysics

$$\frac{\Delta T}{T_{\text{CMB}}}(\hat{\mathbf{n}}_i) = -\tau_{e,i} \frac{\hat{\mathbf{r}}_i \cdot \mathbf{v}_i}{c}.$$

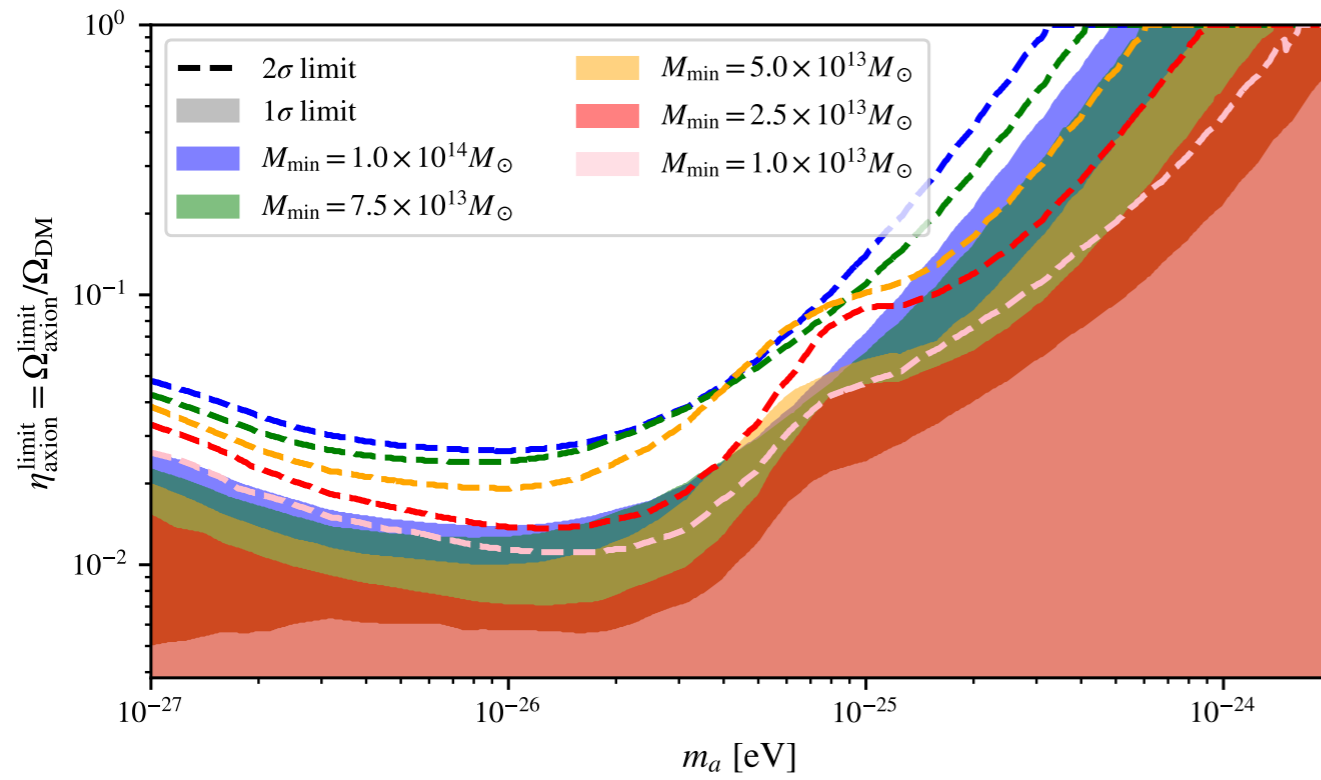
Galaxy bias:  $\mathcal{B} \rightarrow b(z)\mathcal{B}$



# SYSTEMATIC UNCERTAINTIES



# SYSTEMATIC UNCERTAINTIES



Halo Mass

# Take-home ULA cosmology message

0.5% level fractional ULA abundances accessible to next generation of observations, maybe better!

# Numerology of fundamental constants

Dirac, Teller, Gamow, Dicke, and others ....

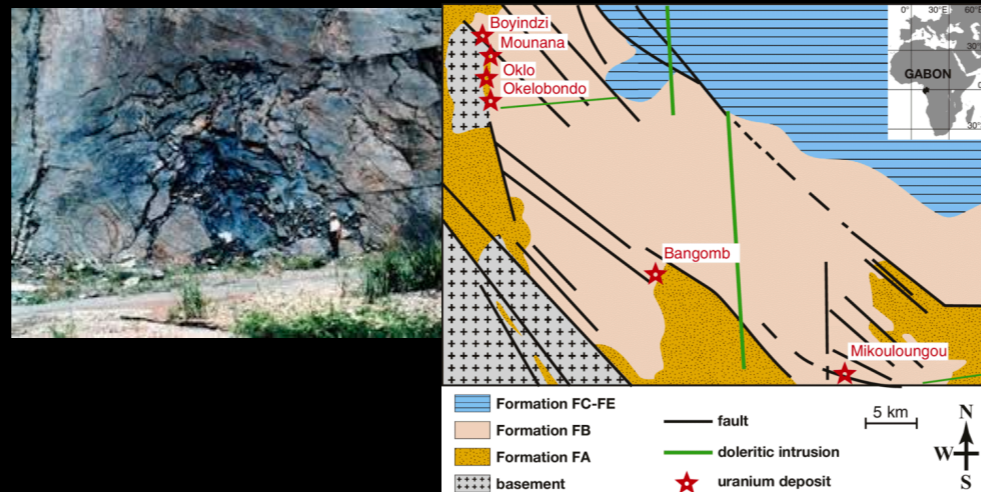
$$\frac{3e^4}{Gm_p m_e^2 c^3} = T_{\text{universe}}$$

What if always true?

$$G \propto 1/t \text{ or } e \propto t^{1/4} \text{ or } c \propto t^{-1/3} \text{ or } m_e \propto t^{-1/2} \text{ or } m_p \propto t^{-1}$$



Plants seed of interesting idea....



# The simplest theory of varying $\alpha$

- \* Simplest theory with varying  $\alpha = \frac{e^2}{\hbar c} \simeq \frac{1}{137}$  but otherwise behaves like EM, charge conserved

$\zeta$  is a plasma fudge factor,  $M$ , energy scale of new physics

$$\ddot{\varphi} + K\dot{\varphi} + m^2\varphi = \frac{e^{-\varphi} \left( |\vec{E}|^2 - |\vec{B}|^2 \right)}{8\pi\omega} = \frac{e^{-\varphi}\zeta\rho_m}{8\pi\omega}$$

$$\omega \equiv \frac{M^2}{M_{\text{pl}}^2}$$

## Modified Maxwell Equations

$$\begin{aligned} \nabla \cdot \left( e^{-2\varphi} \vec{E} \right) &= 4\pi e_0 n_e(\vec{x}) & \nabla \cdot \left( e^{-2\varphi} \vec{E} \right) &= 4\pi e_0 n_e(\vec{x}) & \nabla \cdot \mathbf{B} &= 0 \\ \nabla \times \mathbf{E} &= -\frac{1}{c} \frac{d\mathbf{B}}{dt} & \nabla \times \left( e^{-2\varphi} \mathbf{B} \right) &+ \frac{1}{c} \frac{d}{dt} \left( e^{-2\varphi} \mathbf{E} \right) &= \frac{4\pi \vec{J}}{c} \end{aligned}$$

- \* Bekenstein, Sandvik, Barrow, Magueijio, and much followup by Mota, Martins, Vucetich, Kraiselburd, Livio, and others....



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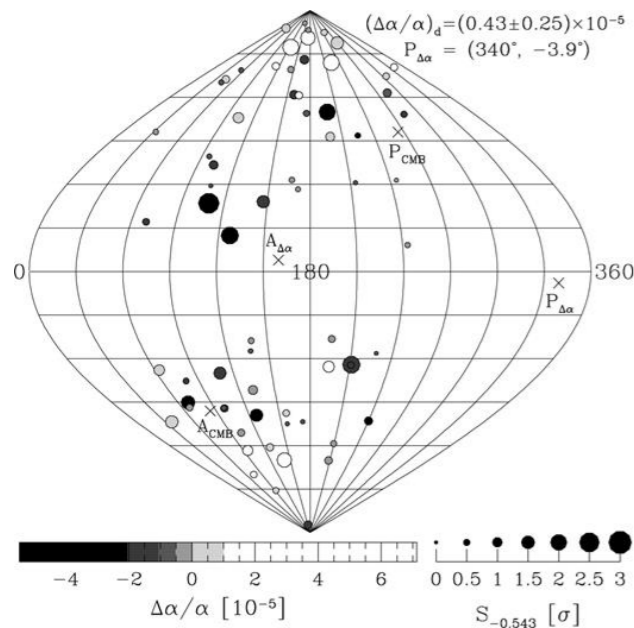
# String-inspired models (runaway dilation)



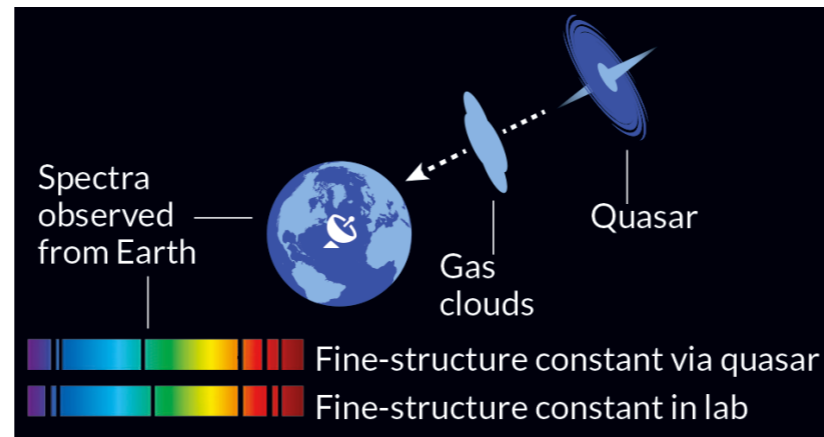
Extra-dimensions (Kaluza-Klein theories)

$$\ddot{\psi} + 3H\dot{\psi} + \frac{dV}{d\psi} + \frac{\omega'(\psi)\dot{\psi}^2}{2\omega(\psi)} = -\frac{B'_f(\psi)}{\omega(\psi)} e^{-B_f(\psi)} \zeta_m G \rho_m,$$

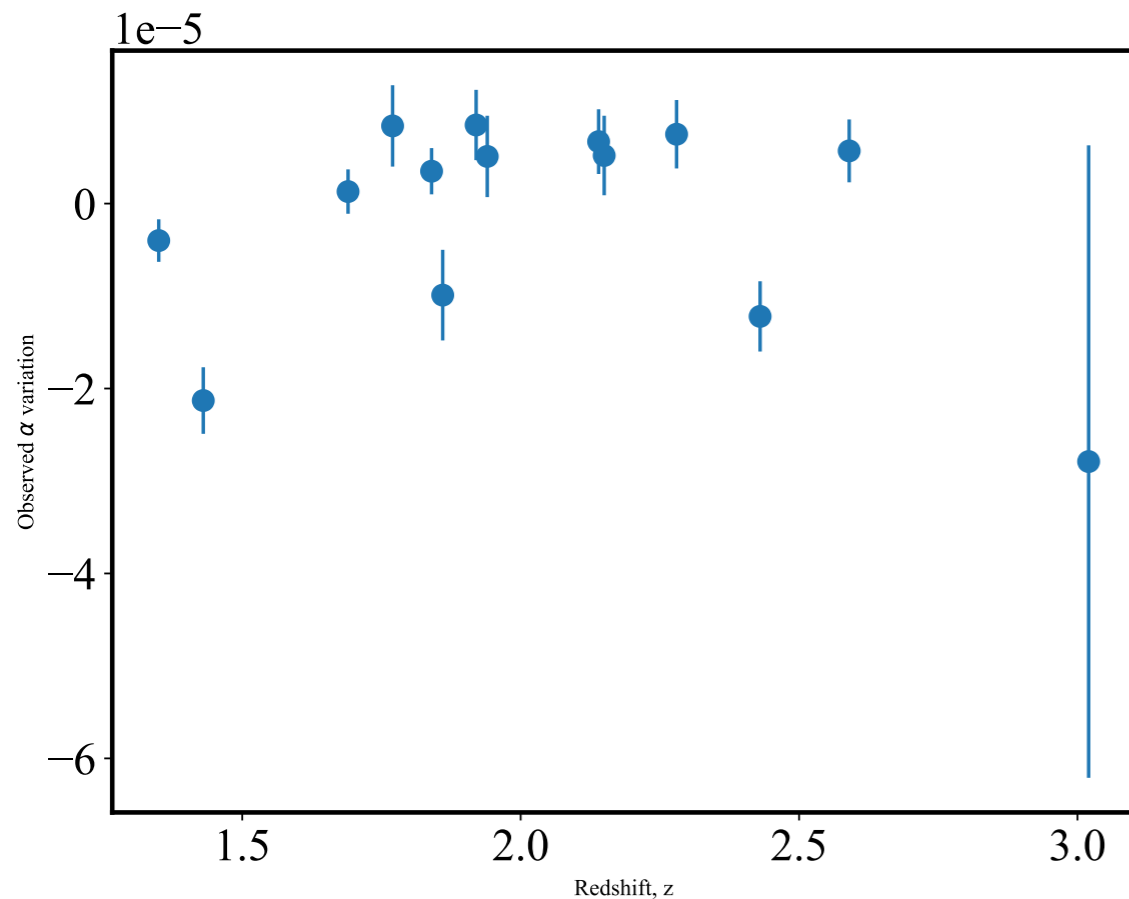
# QSO hints and constraints



$$\Delta\lambda \propto \Delta\alpha^2$$



✳ Webb, Martins, Murphy, Flambaum, Barrow, and others....



✳ Hints of  $\alpha$  variation from distant accreting black holes in galaxies

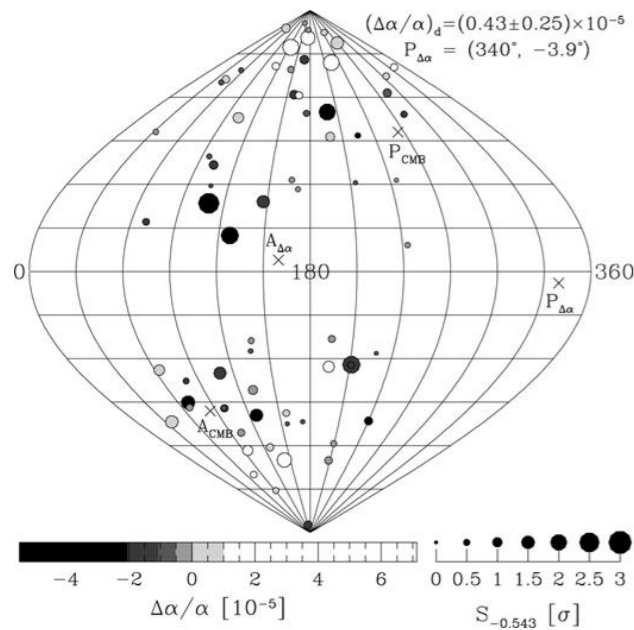
*Mon.Not.Roy.Astron.Soc.* 327 (2001) 1223. astro-ph/0012420

*Mon.Not.Roy.Astron.Soc.* 461 (2016) 3, 2461-2479  
1606.06293

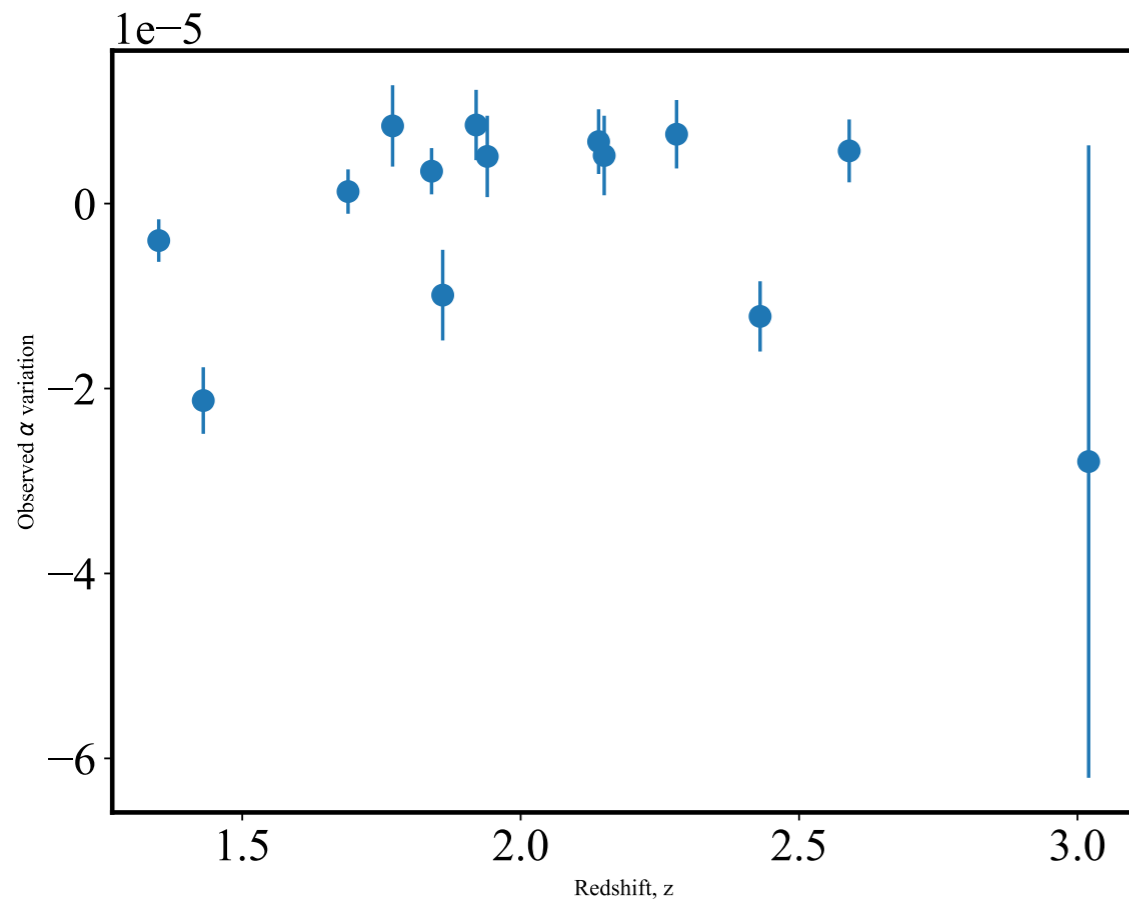
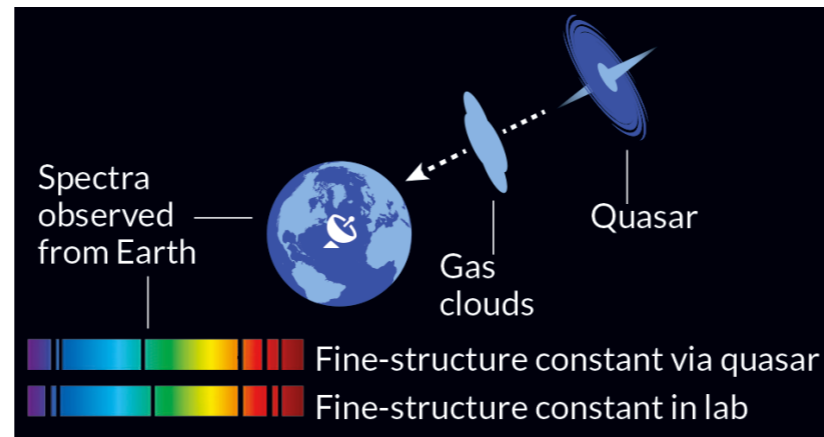
*Reports on Progress in Physics*, arXiv: 1709.02923

*Phys.Rev.Lett.* 107 (2011) 191101, arXiv: 1008.3907

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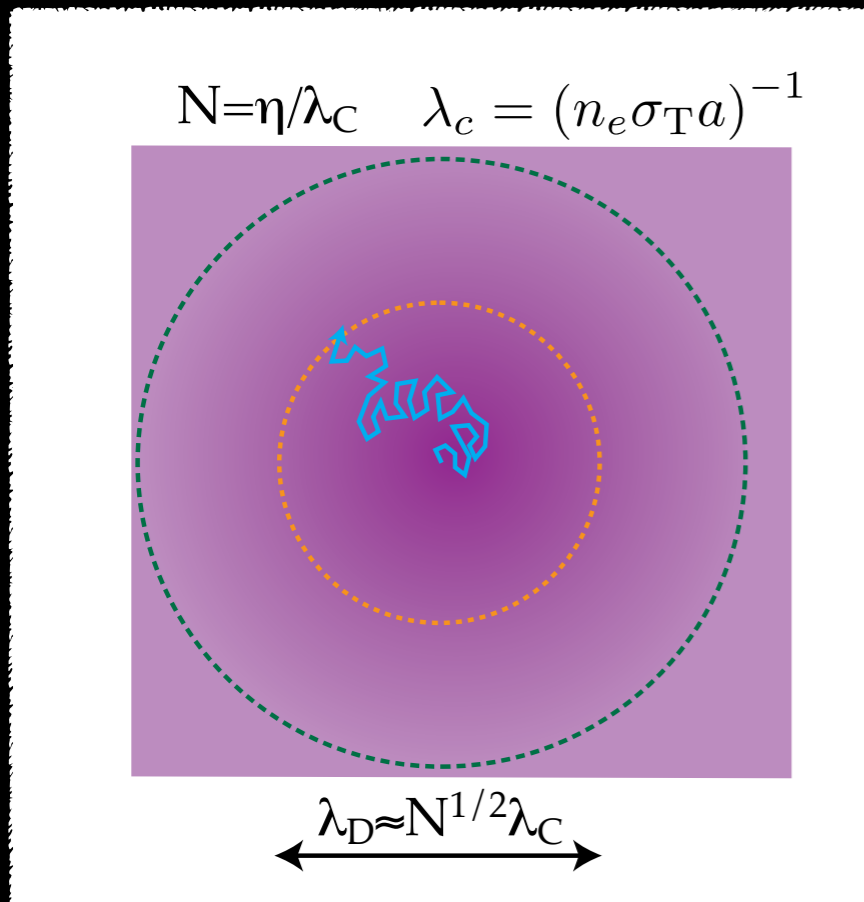
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# Effects on CMB

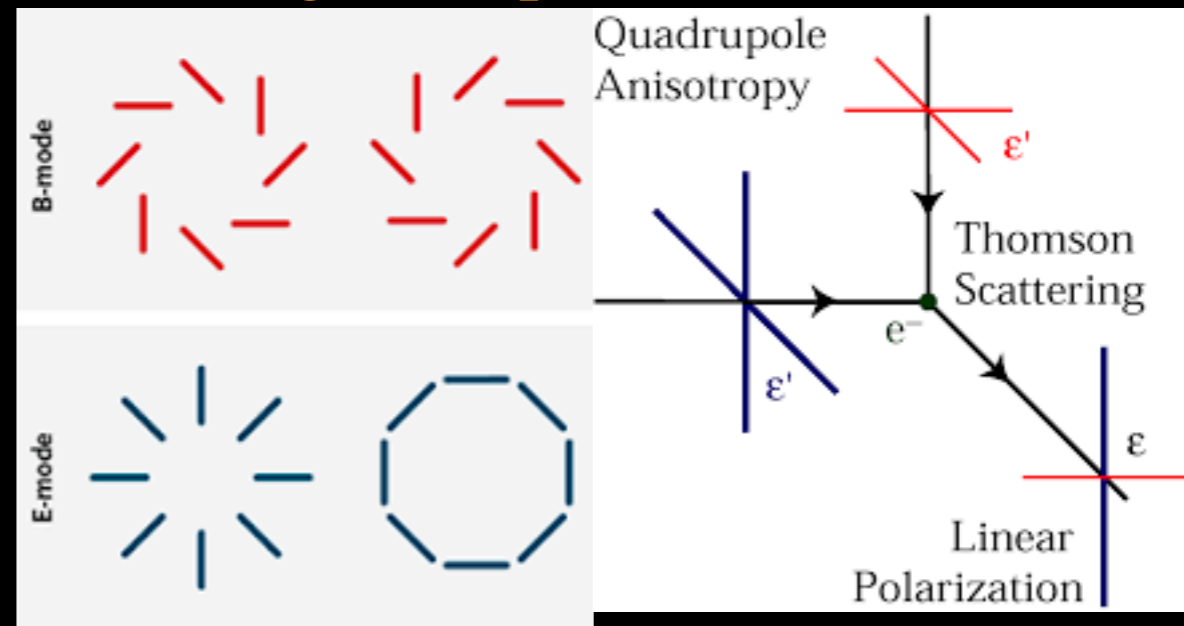
Images courtesy of Wayne Hu's website and Yacine Ali-Haïmoud

## Diffusion



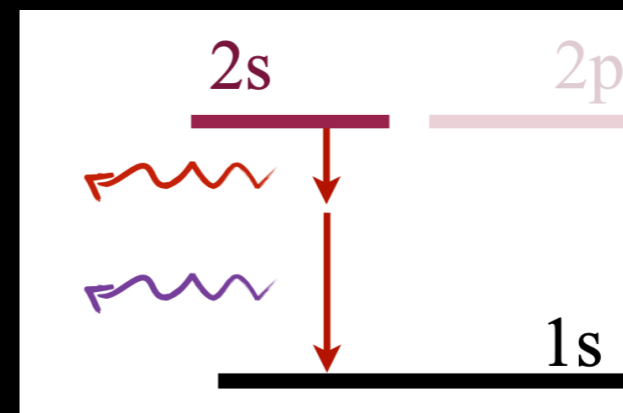
$$\sigma_T \propto \frac{8\pi}{3} \left( \frac{\alpha \hbar c}{mc^2} \right)^2$$

## Scattering from polarization modulated



## Recombination modulated

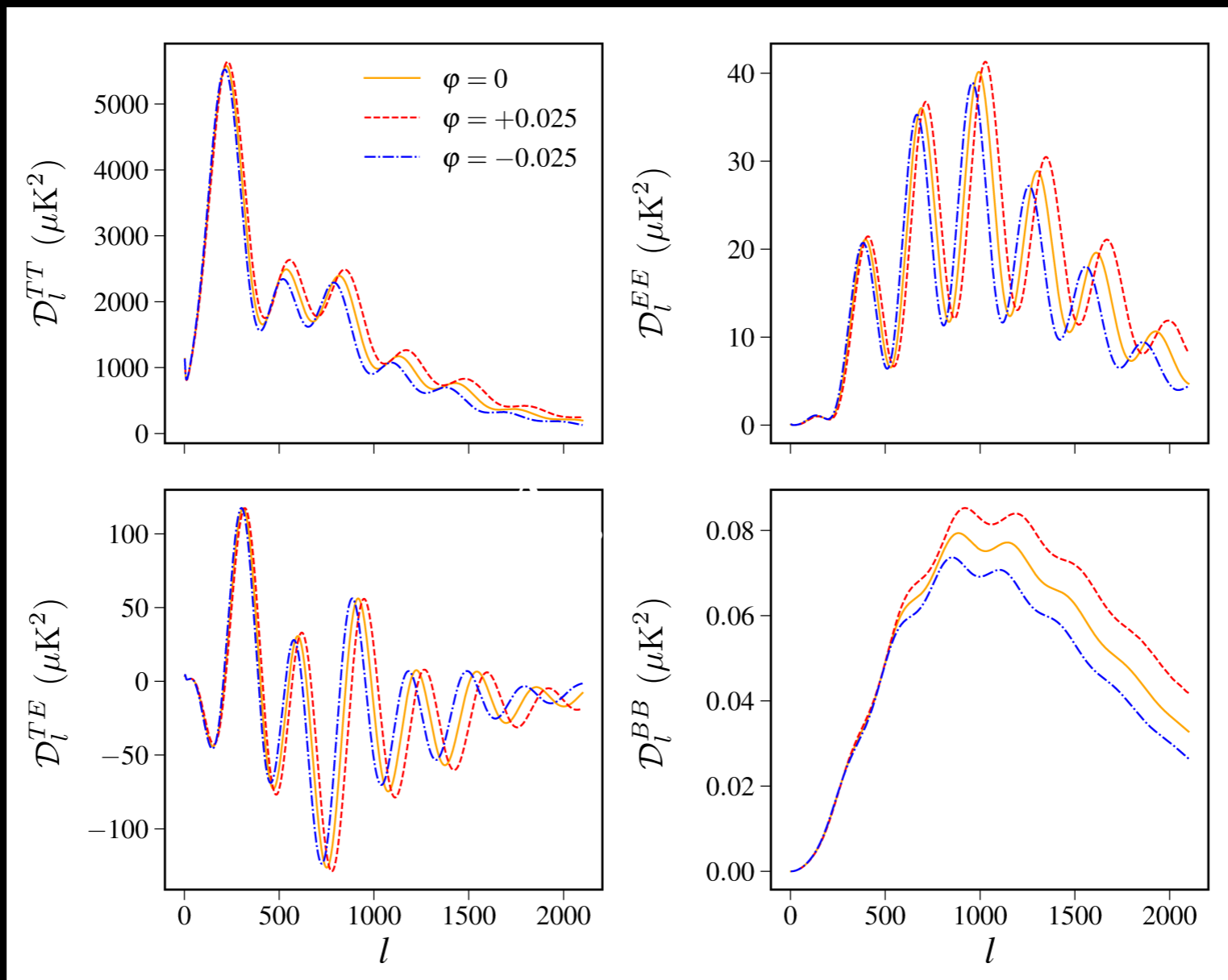
$$\Lambda_{2s \rightarrow 1s} \propto \alpha^8$$





# Effects on CMB

*Image from Phys. Rev. D 99, 043531 (2019)*



$$\alpha = \alpha_0 (1 + \varphi)$$

# Constraints so far

$\alpha_{\text{rec}} \neq \alpha_0$  SingleValues **OR**

$$\frac{\Delta\alpha}{\alpha_0} = A(1+z)^p \text{ very simple models}$$

Menegoni, Galli, Chluba, Hart, Martins, Rocha, and others— Planck 2018 data

$$\frac{\Delta\alpha}{\alpha} \leq 0.005 \text{ at } 1\sigma$$

$$\Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}, \omega$$

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**CAMB OR OTHER BOLTZMAN CODE**



**Compare with data**  
**Explore posterior using Monte Carlo**  
**Markov Chain (MCMC)**

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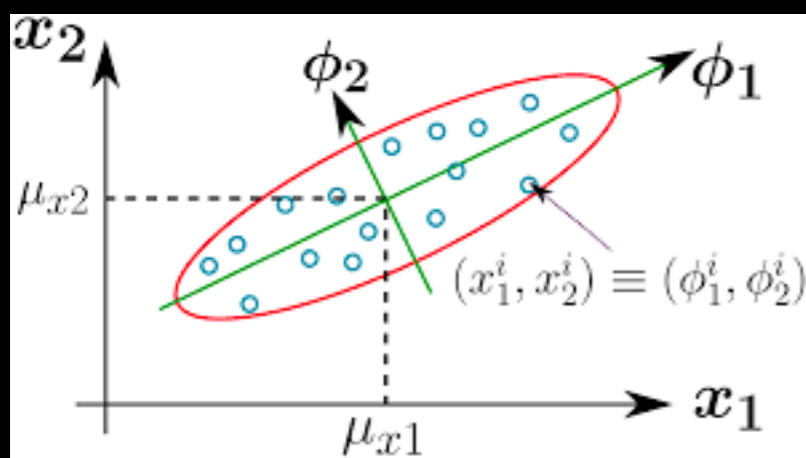
$$\Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}, \omega$$

# PCA — Principal Component analysis

\*Expand fine-structure parameter in some basis to discretize

$$\alpha = \sum_i a_i f_i(z)$$

\*Find principal axes of iso-likelihood contours in parameters space



$$\mathcal{L} \propto \exp\left[-\sum_{ij} a_i \mathbf{F}_{ij} a_j\right]$$

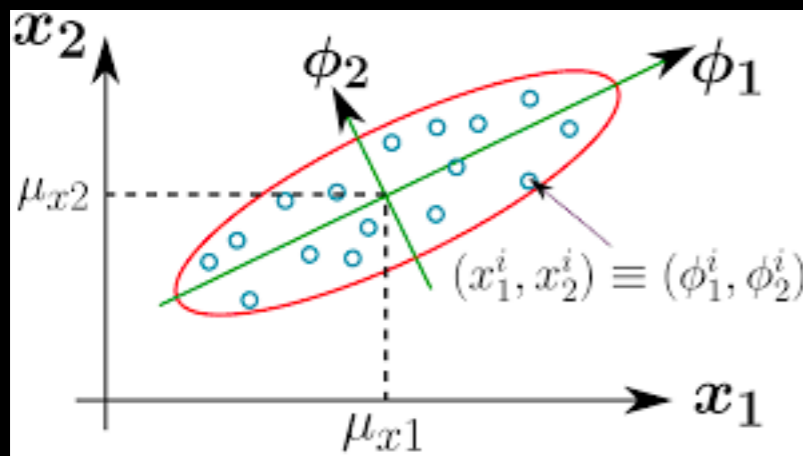
$$\mathbf{F}_{ij} = \sum_{\ell} \frac{f_{\text{sky}} \times (2\ell + 1)}{2} \left(\frac{dC_{\ell}}{da_i}\right)^2$$

\*These “vectors” are the best constrained models  $\alpha(z)$



# PCA — Principal Component analysis

$$\alpha = \sum_i a_i f_i(z)$$



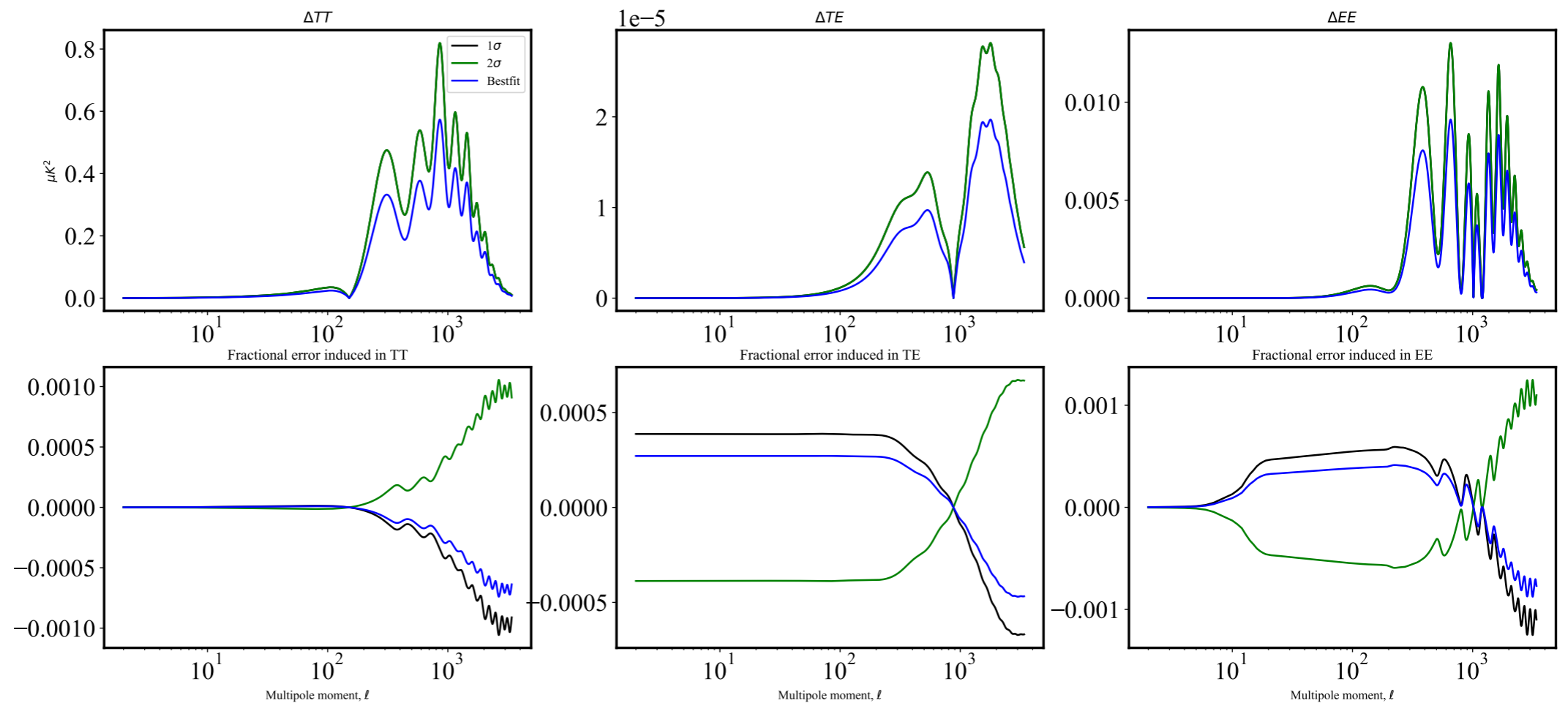
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# Projecting BSBM onto PCs — observables

**CAUTION**  
AREA UNDER  
CONSTRUCTION

H. Tohfa

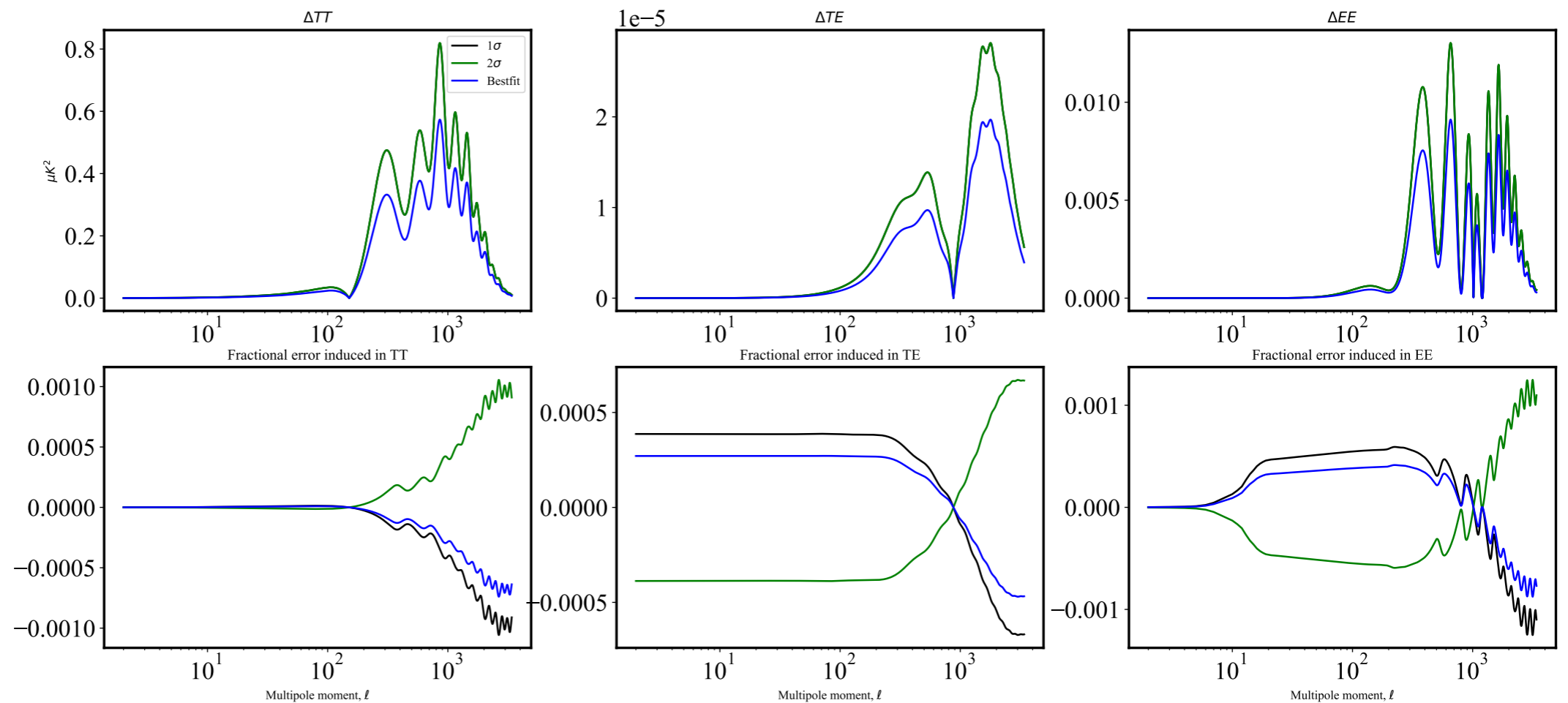


$$\frac{\Delta C}{C}(z) = \sum_i \rho_i E_i(z), \quad \rho_i = \int \frac{\Delta C}{C}(z) \cdot E_i(z) dz.$$

# Projecting BSBM onto PCs — observables

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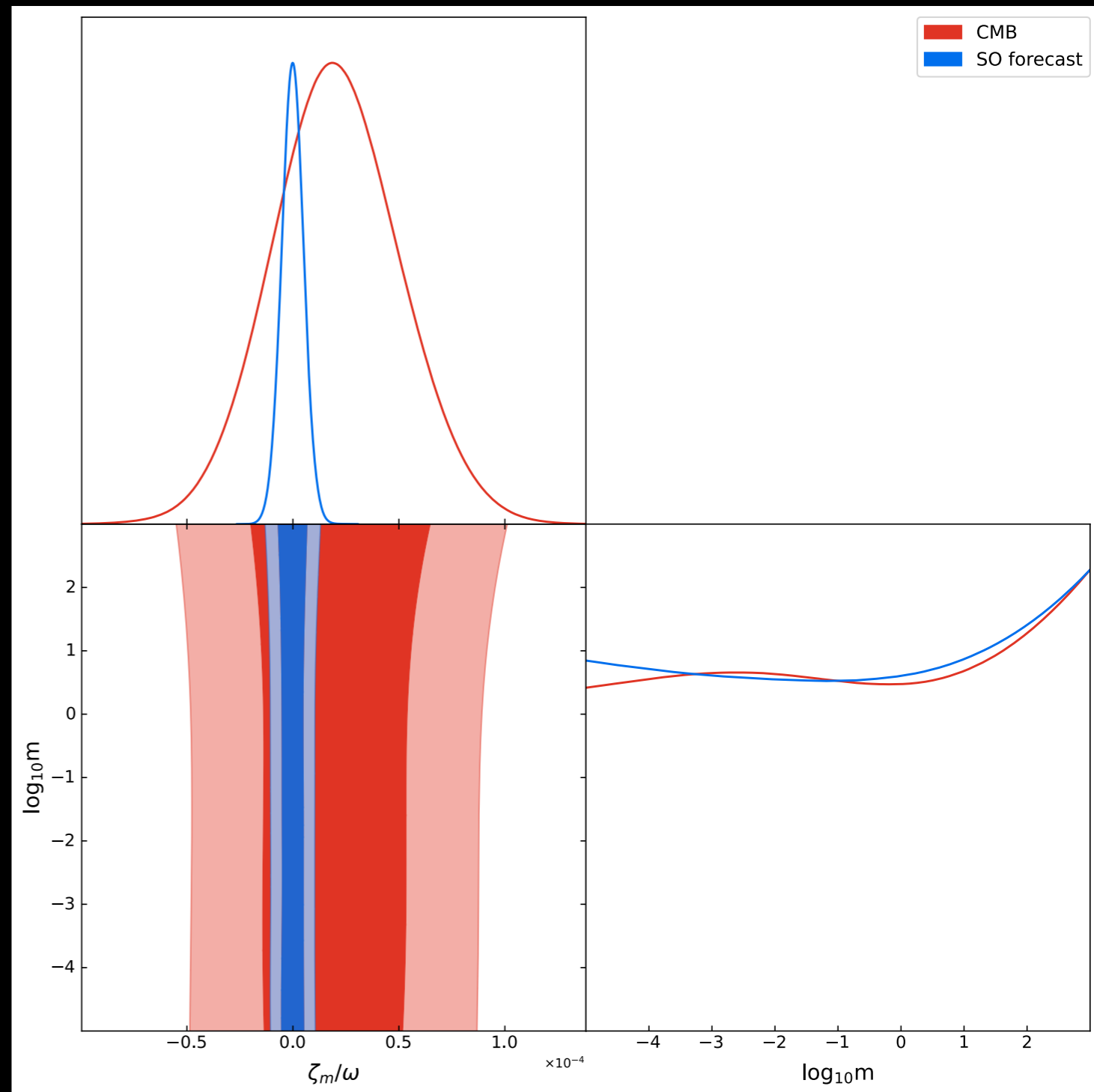
$$\frac{\Delta C}{C}(z) = \sum_i \rho_i E_i(z), \quad \rho_i = \int \frac{\Delta C}{C}(z) \cdot E_i(z) dz.$$

# Projecting BSBM onto PCs — constraints and forecasts

**CAUTION**  
**AREA UNDER**  
**CONSTRUCTION**

Constraints from Planck 2018  
data analysis

H. Tohfa (UCR, U. Washington)



# Future work

- \* Spatial variation in BSBM models + effect on CMB
- \* Full set of model family (e.g. dilaton models)
- \* Full covariance analysis with other cosmological parameters
- \* Understood poorly understand plasma physics of this work