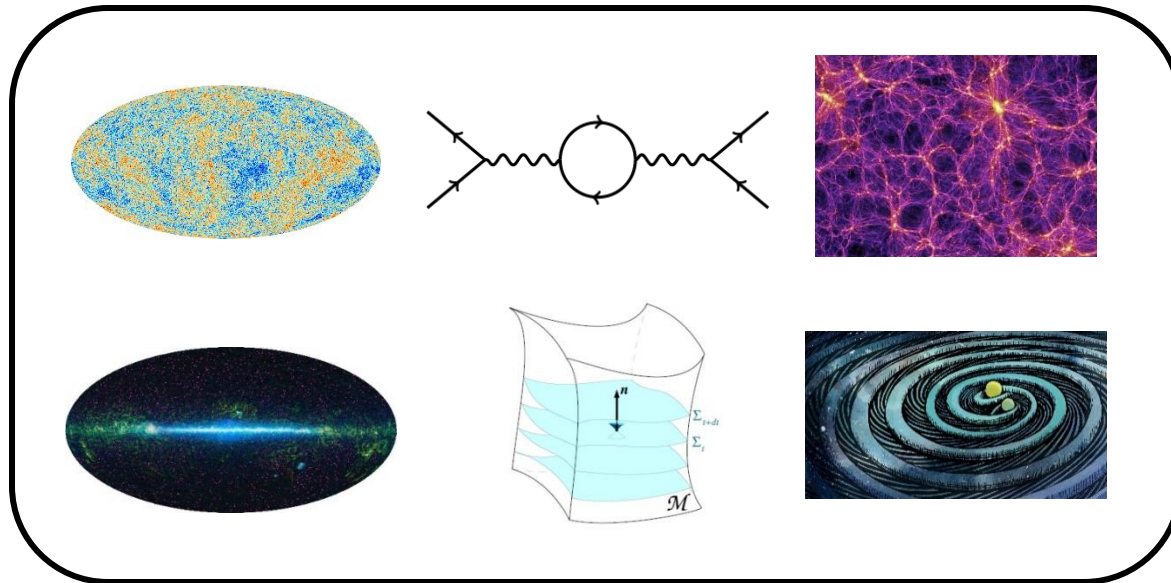


Testing gravity on all scales



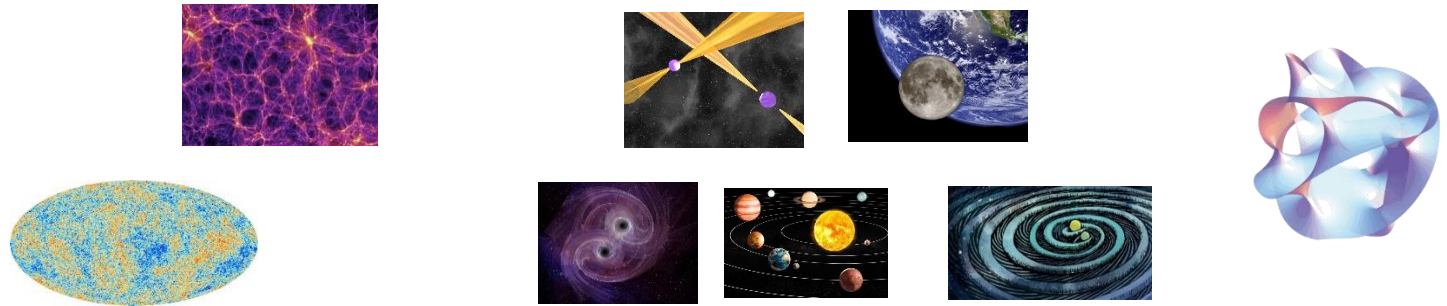
Johannes Noller

ICG, University of Portsmouth
DAMTP, University of Cambridge



Science & Technology
Facilities Council

Gravity across scales



Frequency (Hz):

10^{-18}

10^{-13}

10^{-8}

10^{-2}

10^2

10^{43}

Distance (km):

10^{23} km

10^{18} km

10^{13} km

10^7 km

10^3 km

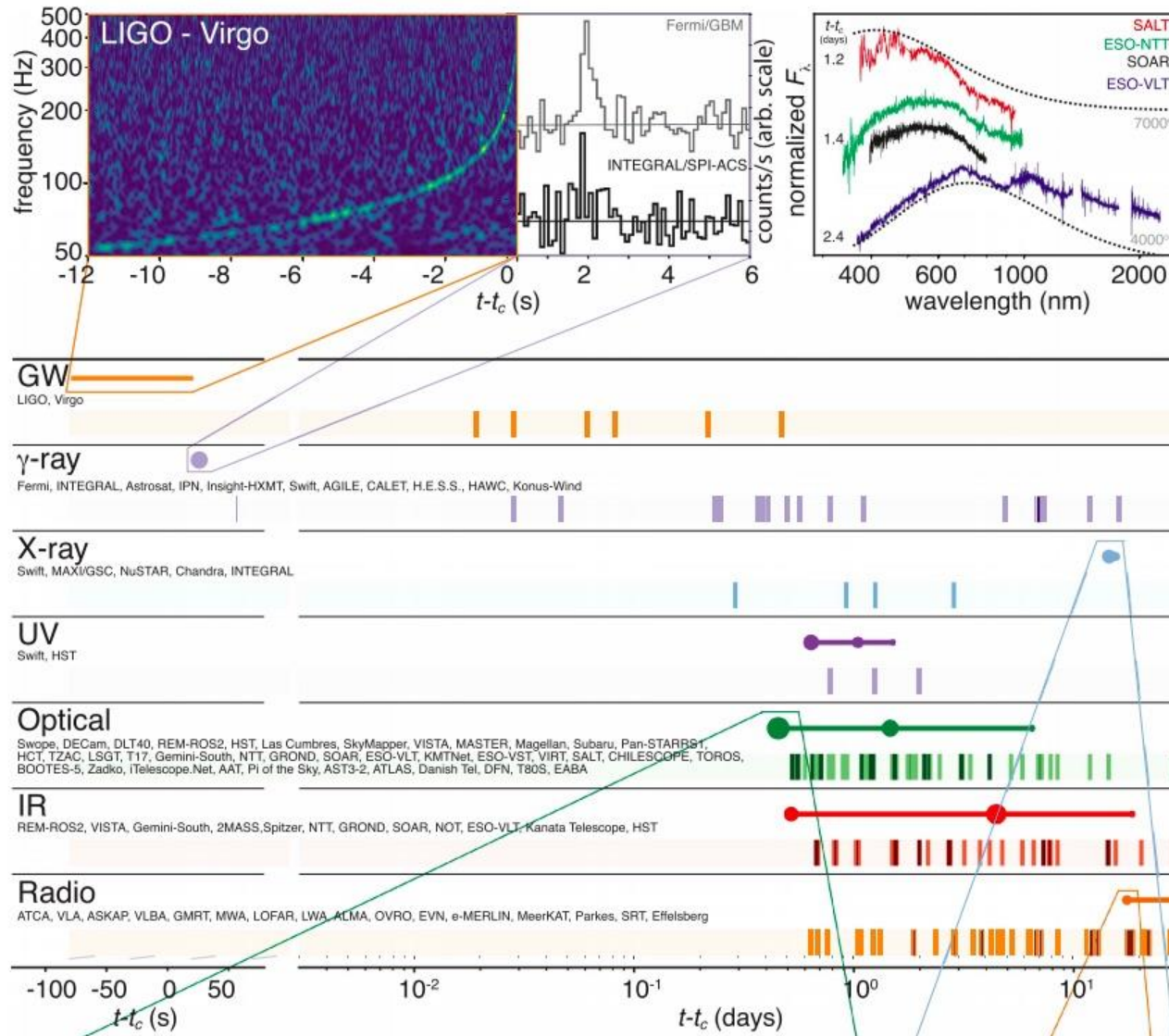
10^{-38} km

Gravity across scales

“The elegant logic of general relativity theory, and its precision tests, recommend GR as the first choice for a working model for cosmology. But the Hubble length is fifteen orders of magnitude larger than the length scale of the precision tests, at the astronomical unit and smaller, a spectacular extrapolation.”

Jim Peebles, IAU 2000

GW170817

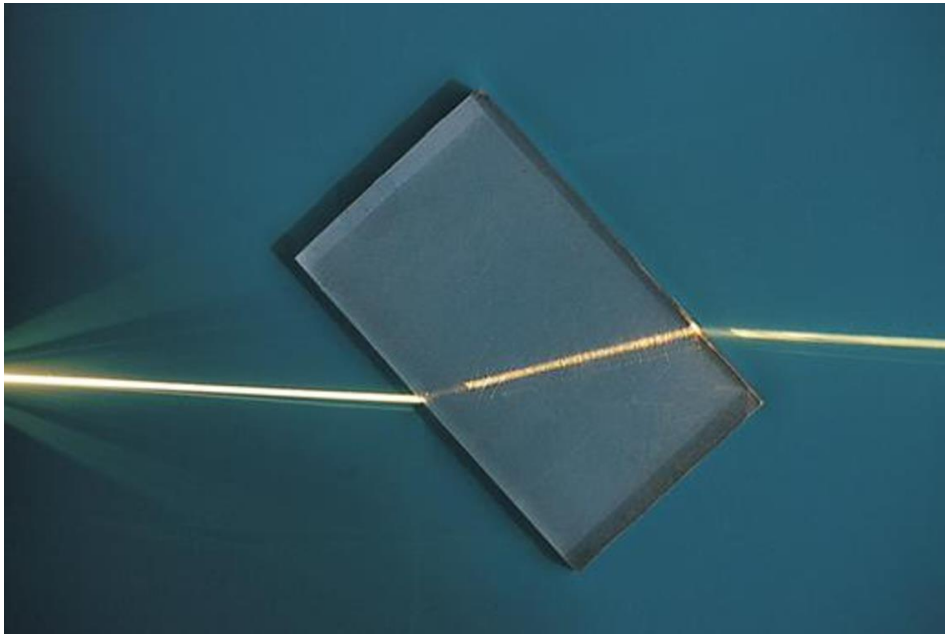


The speed of gravitational waves

$$ds^2 = -dt^2 + a^2(t) [\delta_{ij} + \gamma_{ij}] dx^i dx^j$$



$$\ddot{\gamma}_{ij} + 3H\dot{\gamma}_{ij} + c_{\text{GW}}^2 k^2 \gamma_{ij} = 0$$



Constraints on speed of GWs: $|c_{\text{GW}}^2 - 1| \lesssim 10^{-15}$.

The speed of gravitational waves

$$\ddot{\gamma}_{ij} + 3H\dot{\gamma}_{ij} + c_{\text{GW}}^2 k^2 \gamma_{ij} = 0$$

$$\mathcal{L} = G_2 + G_3 \square\phi + G_4 R + G_{4,X} \{(\square\phi)^2 - \nabla_\mu \nabla_\nu \phi \nabla^\mu \nabla^\nu \phi\} + G_5 G_{\mu\nu} \nabla^\mu \nabla^\nu \phi - \frac{1}{6} G_{5,X} \{(\square\phi)^3 - 3\nabla^\mu \nabla^\nu \phi \nabla_\mu \nabla_\nu \phi \square\phi + 2\nabla^\nu \nabla_\mu \phi \nabla^\alpha \nabla_\nu \phi \nabla^\mu \nabla_\alpha \phi\}.$$

where $G_i \equiv G_i(\phi, X)$ and $X \equiv -\frac{1}{2} \nabla^\mu \phi \nabla_\mu \phi$

Horndeski '74, Deffayet et al. '11



$$\mathcal{L} = G_4(\phi)R + G_2(\phi, X) - G_3(\phi, X)\square\phi$$

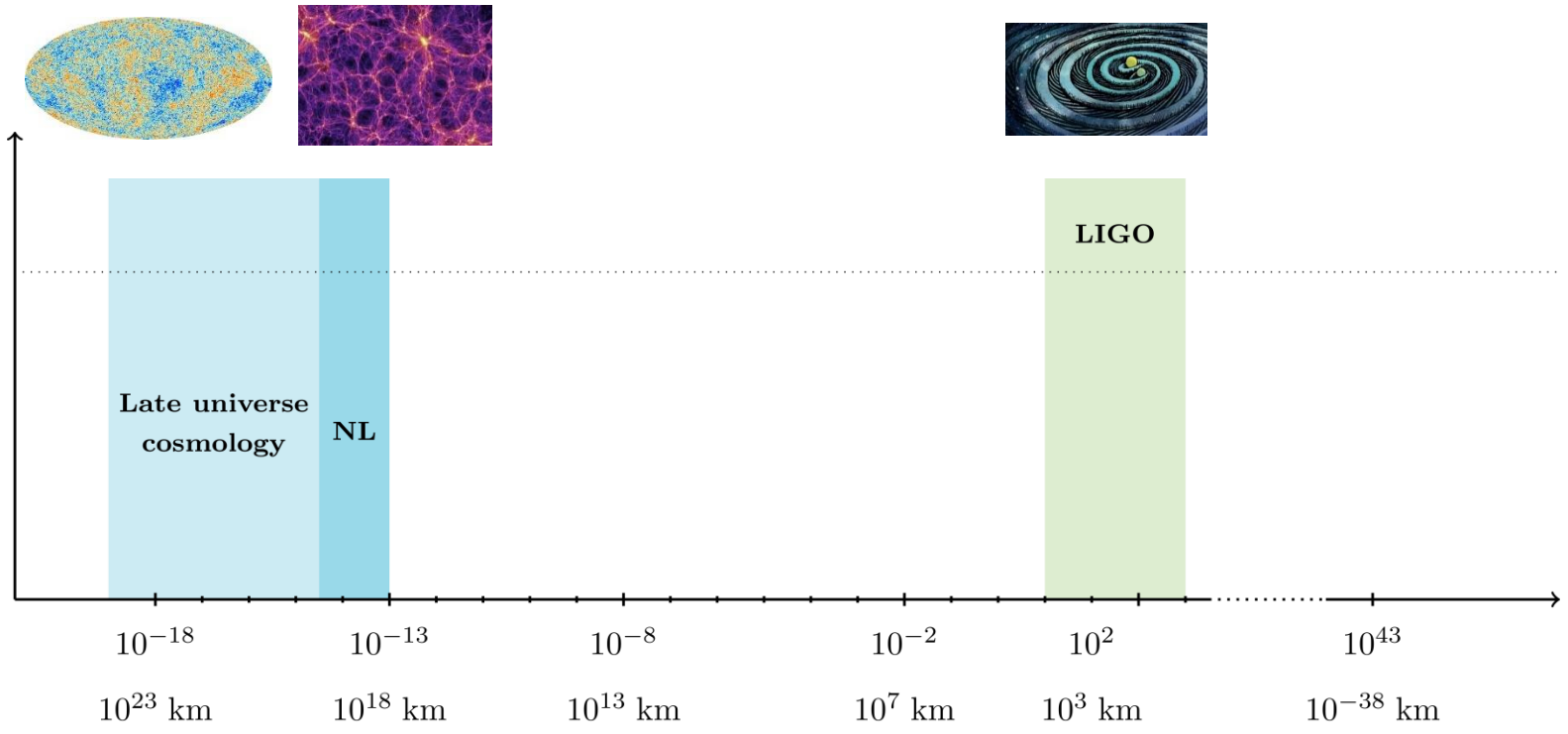
Baker, Bellini, Ferreira, Lagos, JN, Sawicki '17, Creminelli, Vernizzi '17, Ezquiaga, Zumalacarregui '17, Sakstein, Jain '17

Also see: Deffayet, Pujolas, Sawicki, Vikman '10, Amendola et al. '12, Linder '14, Saltas et al. '14, Beltran Jimenez et al. '15, Sawicki et al. '16, Bettoni et al. '16, Lombriser, Lima '16, Cornish et al. '17, ...

Constraints on speed of GWs: $|c_{\text{GW}}^2 - 1| \lesssim 10^{-15}$.

LIGO & Virgo Collaborations '17, Fermi, IGAL '17

Gravity across scales



Frequency (Hz):

Distance (km):

10^{-18}

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10^{-2}

10^2

10^{43}

10^{23} km

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10^3 km

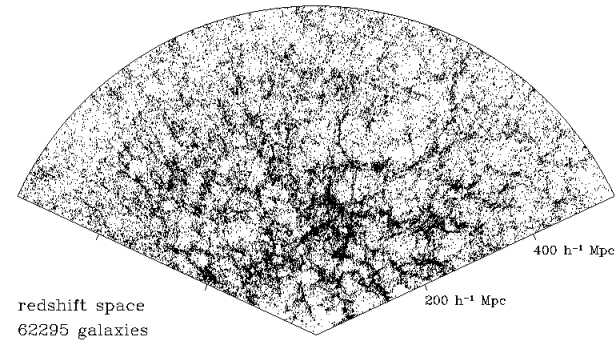
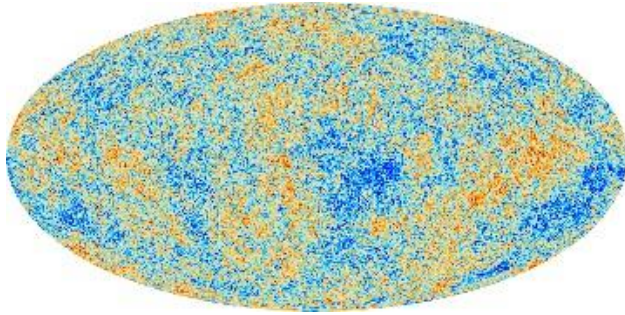
10^{-38} km

Late universe
cosmology

NL

LIGO

Probing Dark Energy: CMB + LSS



Metric fluctuations:

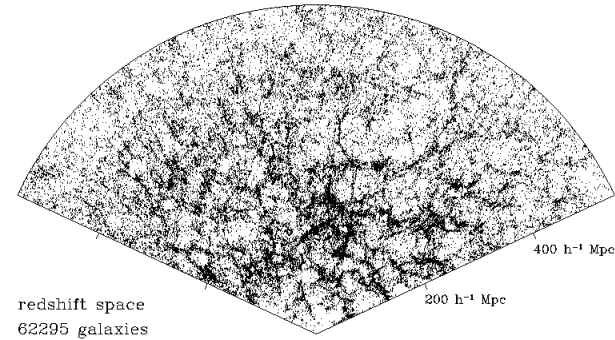
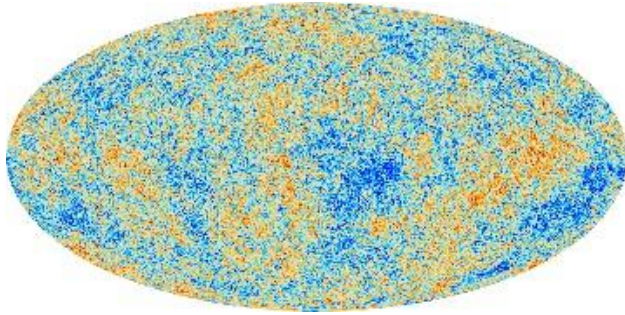
$$ds^2 = a^2(\tau) \left[-(1 + 2\Phi)d\tau^2 + (1 - 2\Psi)dx_i dx^i \right]$$

Free-falling particles:

$$\frac{1}{a} \frac{d(av)}{d\tau} = \nabla \Phi \quad (\text{CDM})$$

$$\frac{d(\mathbf{v})}{d\tau} = \nabla_{\perp}(\Phi + \Psi) \quad (\text{photons})$$

Probing Dark Energy: CMB + LSS



Metric fluctuations:

$$ds^2 = a^2(\tau) [-(1 + 2\Phi)d\tau^2 + (1 - 2\Psi)dx_i dx^i]$$

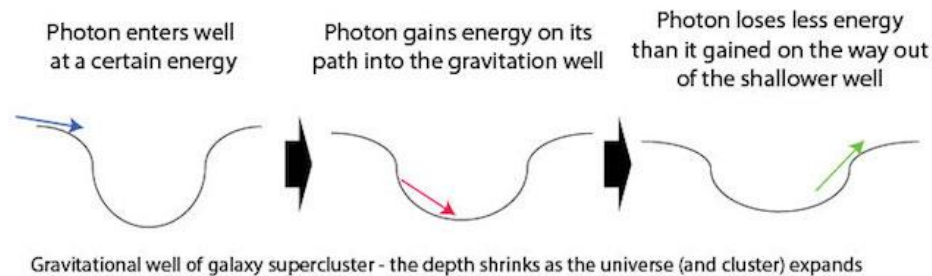
Free-falling particles:

$$\frac{1}{a} \frac{d(av)}{d\tau} = \nabla\Phi \quad (\text{CDM})$$

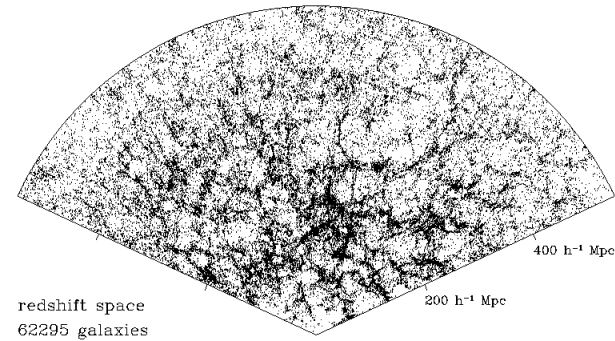
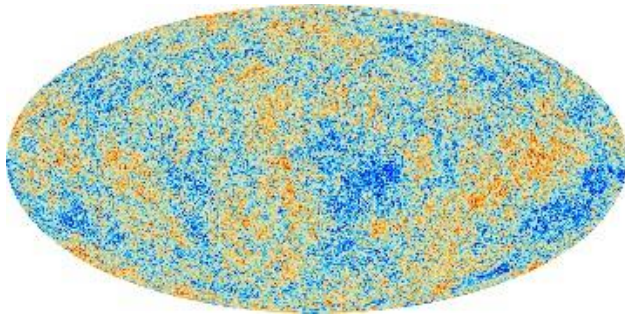
$$\frac{d(\mathbf{v})}{d\tau} = \nabla_{\perp}(\Phi + \Psi) \quad (\text{photons})$$

ISW effect:

$$\frac{\delta T}{T} = \text{initial conditions} + \int_{\tau_{*}}^{\tau_0} d\tau (\dot{\Phi} + \dot{\Psi})$$



Probing Dark Energy: CMB + LSS



Metric fluctuations:

$$ds^2 = a^2(\tau) \left[-(1 + 2\Phi)d\tau^2 + (1 - 2\Psi)dx_i dx^i \right]$$

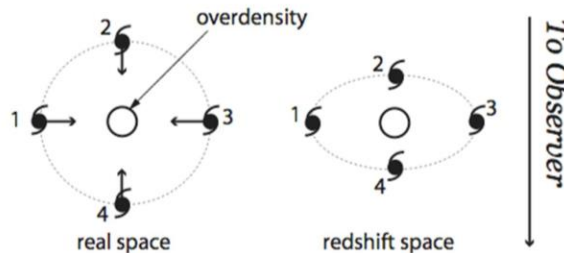
Free-falling particles:

$$\frac{1}{a} \frac{d(av)}{d\tau} = \nabla\Phi \quad (\text{CDM})$$

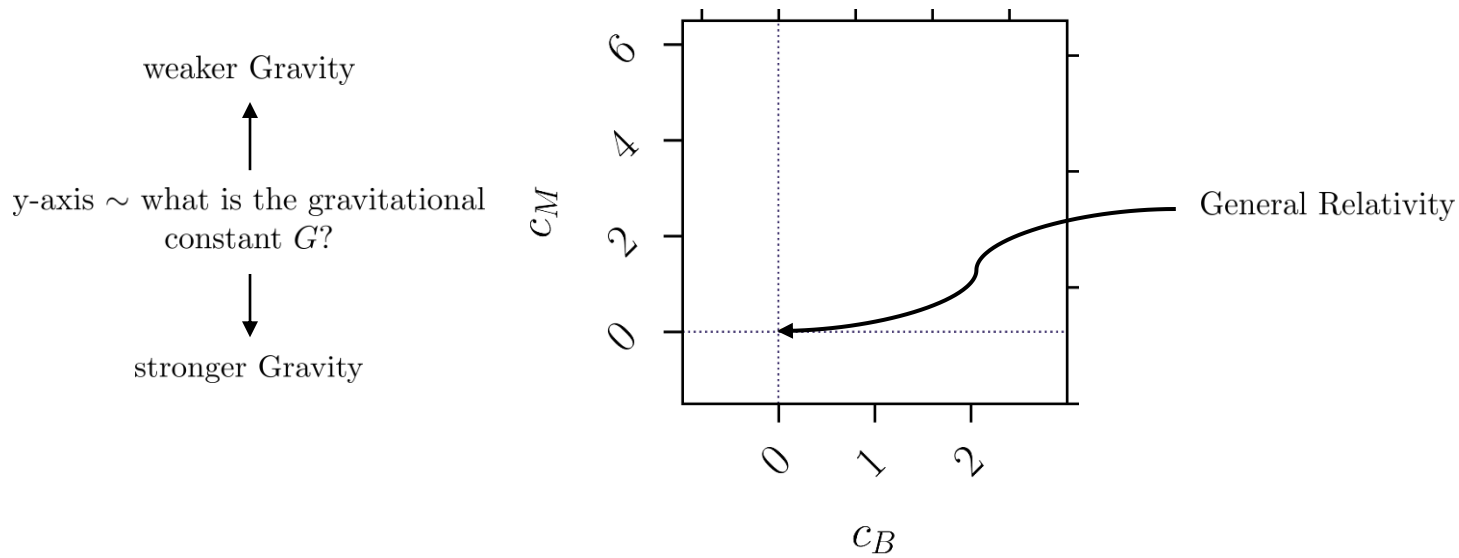
$$\frac{d(\mathbf{v})}{d\tau} = \nabla_{\perp}(\Phi + \Psi) \quad (\text{photons})$$

Poisson equation:

$$\nabla^2\Phi = 8\pi G_N(t)\delta\rho$$



Probing Dark Energy: CMB + LSS



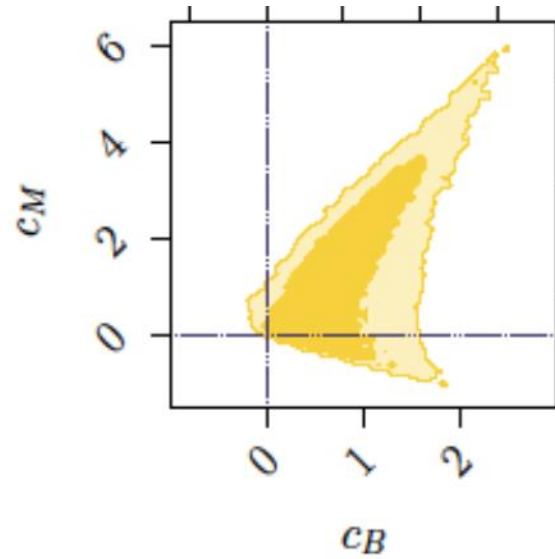
x-axis ~ how much does the graviton interact with DE scalar?

Parametrisation: $\alpha_{M,B} = c_{M,B} \Omega_{DE}$ \Rightarrow α_i framework *Bellini, Sawicki, '14*
 improved param. *Traykova, Bellini, Ferreira, Garcia-Garcia, JN, Zumalacarregui '21*

Probing Dark Energy: CMB + LSS

JN, Nicola '18a, 18b

weaker Gravity
↑
y-axis ~ what is the gravitational constant G ?
↓
stronger Gravity

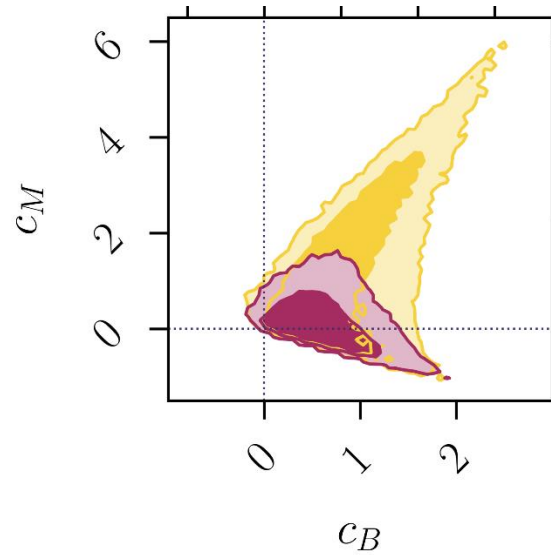


x-axis ~ how much does the graviton interact with DE scalar?

Probing Dark Energy: CMB + LSS

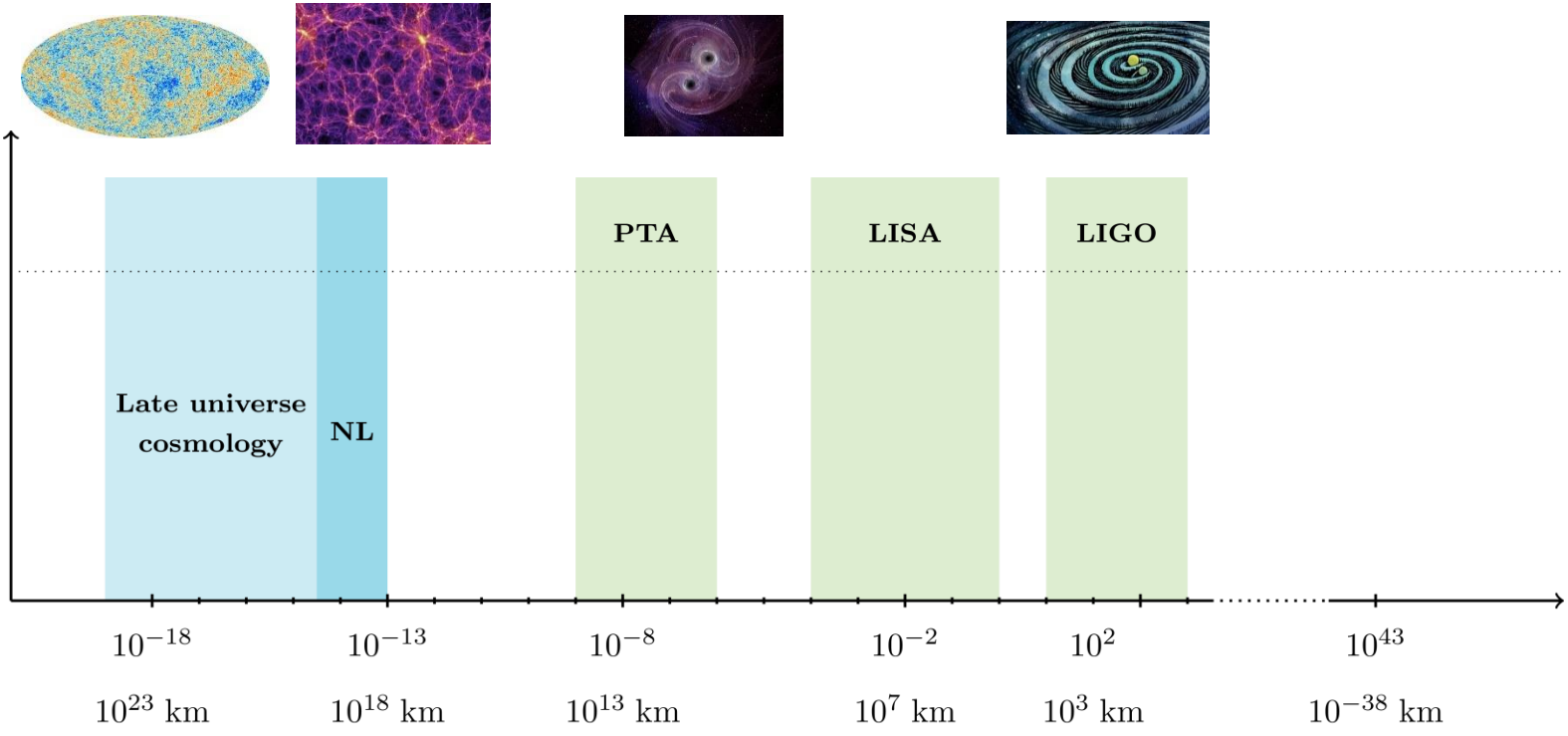
JN, Nicola '18a, 18b

weaker Gravity
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y-axis ~ what is the gravitational constant G ?
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stronger Gravity



x-axis ~ how much does the graviton interact with DE scalar?

Gravity across scales



Frequency (Hz):

10^{-18}

10^{-13}

10^{-8}

10^{-2}

10^2

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Distance (km):

10^{23} km

10^{18} km

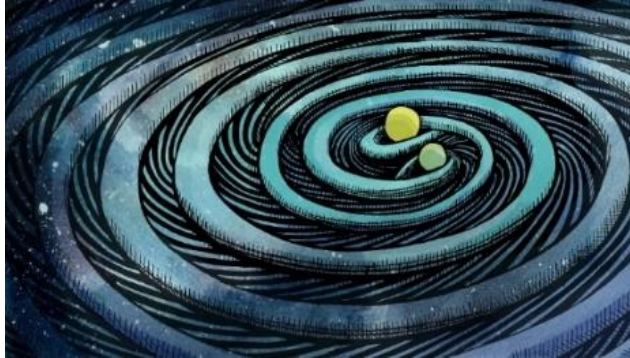
10^{13} km

10^7 km

10^3 km

10^{-38} km

Probing Dark Energy: CMB + LSS + GW



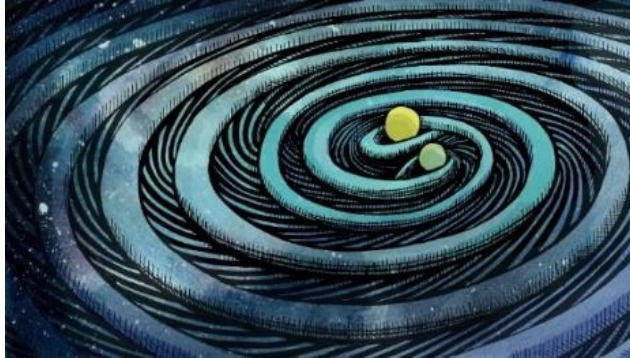
π fluctuations: $\ddot{\pi} + c_s^2 k^2 \pi = 0$

Background: $\gamma_{ij} = M_{\text{Pl}} h_0^+ \cos[\omega(t - z)] \epsilon_{ij}^+$

Amplitude: $h_0^+ \sim \frac{4}{r} (GM_c)^{5/3} (\pi f_{\text{gw}})^{2/3}$

DE fluctuations: $\ddot{\pi} + c_s^2 [k^2 + \beta(c_M, c_B, h_0^+) \cos[\omega(t - z)] \epsilon_{ij}^+ \partial^i \partial^j] \pi = 0$

Probing Dark Energy: CMB + LSS + GW



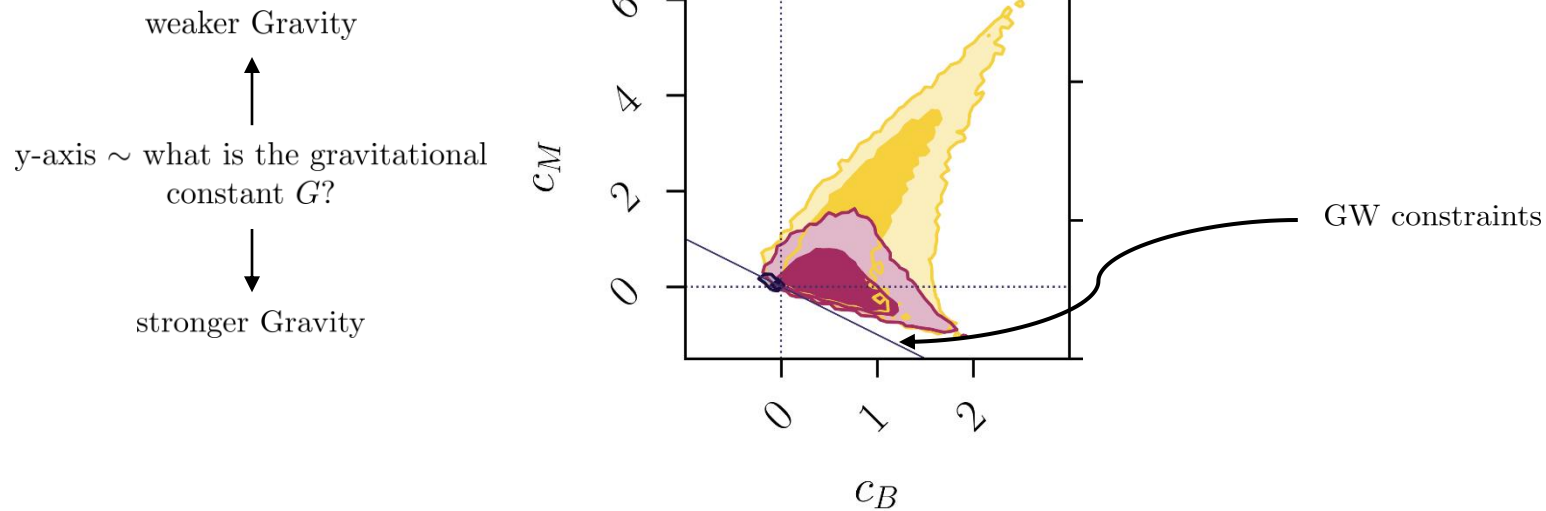
Instability triggered within $r \sim 10$ Mpc for SMBH & $|c_M + c_B| \gtrsim \mathcal{O}(10^{-1})$.

Background:
$$h_0^+ \sim \frac{4}{r} (GM_c)^{5/3} (\pi f_{\text{gw}})^{2/3} \quad \gamma_{ij} = M_{\text{Pl}} h_0^+ \cos[\omega(t - z)] \epsilon_{ij}^+$$

DE fluctuations:
$$\ddot{\pi} + c_s^2 [k^2 + \beta(c_M, c_B, h_0^+) \cos[\omega(t - z)] \epsilon_{ij}^+ \partial^i \partial^j] \pi = 0$$

Probing Dark Energy: CMB + LSS + GW

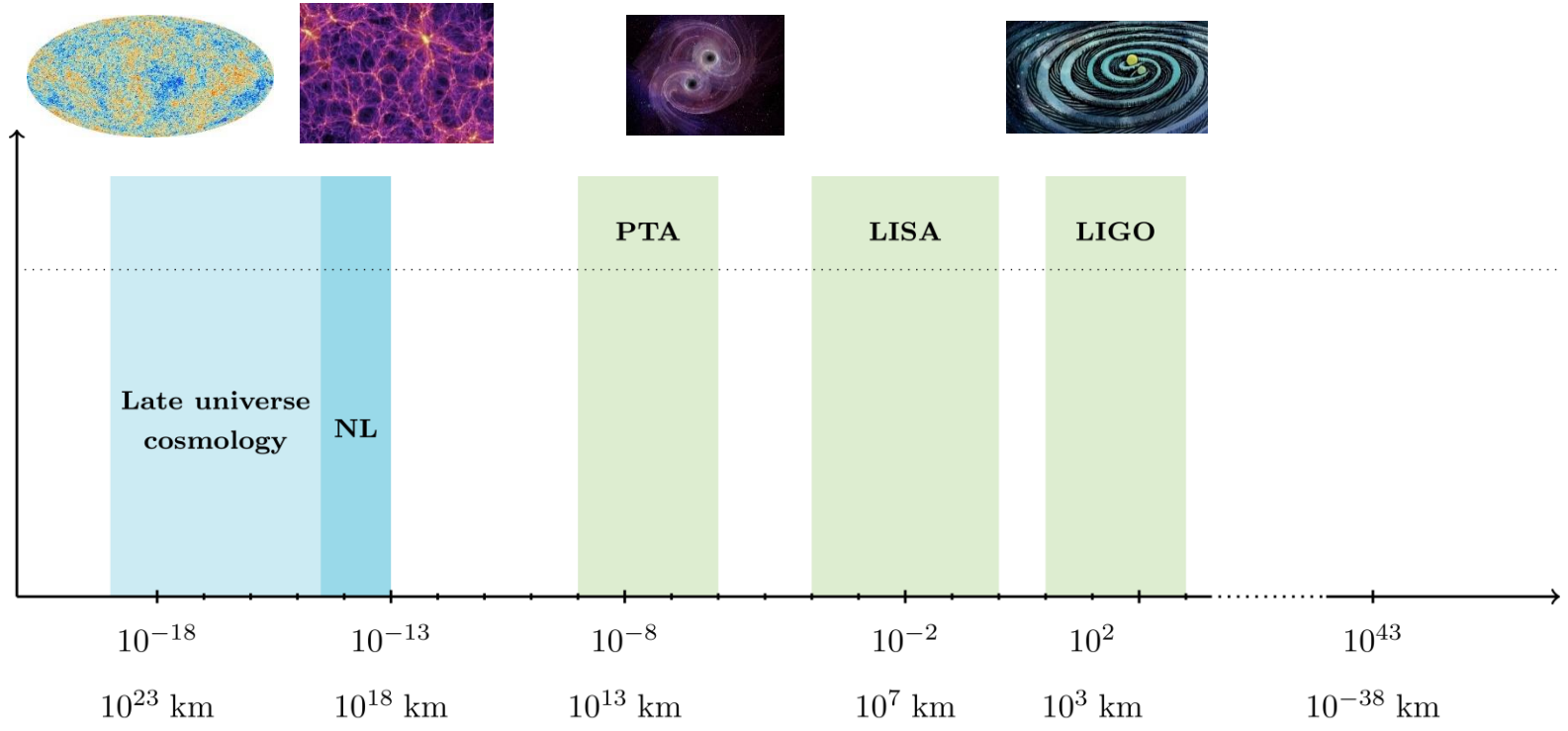
JN '20



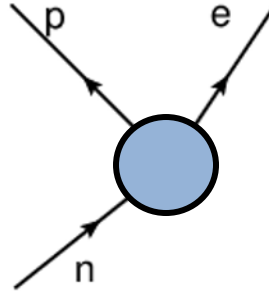
x-axis ~ how much does the graviton interact with DE scalar?

Demanding healthy GW-DE interactions can be used to constrain dark energy

Gravity across scales

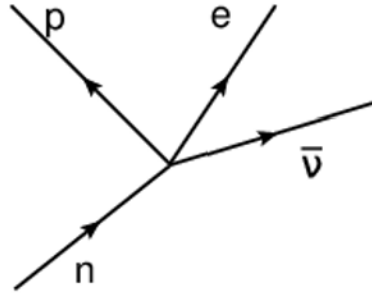


The reach of a theory



Neutron decay

The reach of a theory



Fermi theory

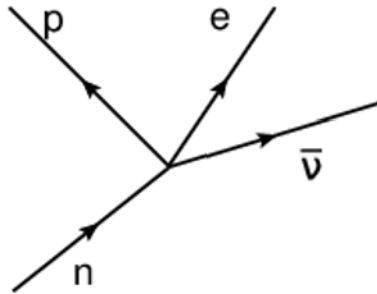
Scattering amplitude:

$$\mathcal{A} \sim \frac{d\sigma}{d\Omega} \sim \frac{\text{Scattered flux}}{\text{Incident flux}}$$

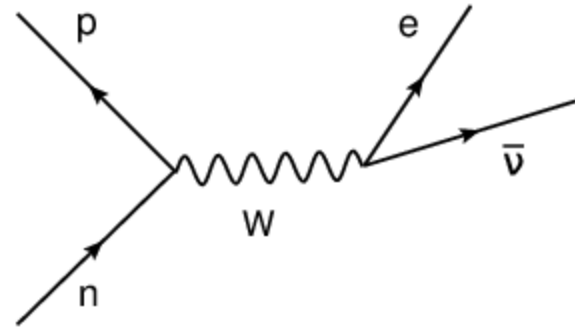
Energy scaling:

$$\mathcal{A} \sim \left(\frac{E}{\text{TeV}} \right)^4$$

The reach of a theory



Fermi theory



Electro-weak theory

Scattering amplitude:

$$\mathcal{A} \sim \frac{d\sigma}{d\Omega} \sim \frac{\text{Scattered flux}}{\text{Incident flux}}$$

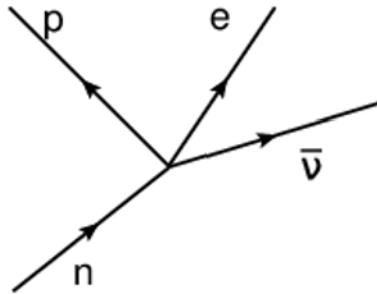
Energy scaling:

$$\mathcal{A} \sim \left(\frac{E}{\text{TeV}} \right)^4$$

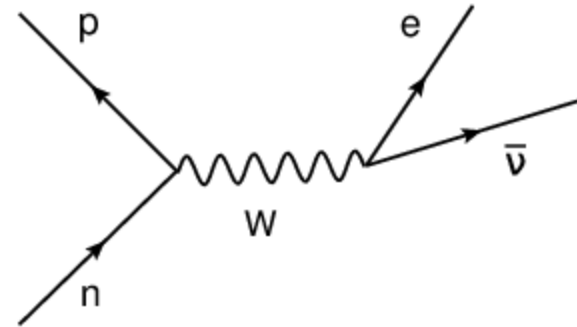
The scale of new physics:

$$m_W \sim 80 \text{ GeV}$$

The reach of a theory



Fermi theory



Electro-weak theory

Fermi theory:

$$\mathcal{A} \sim \left(\frac{E}{\text{TeV}} \right)^4$$

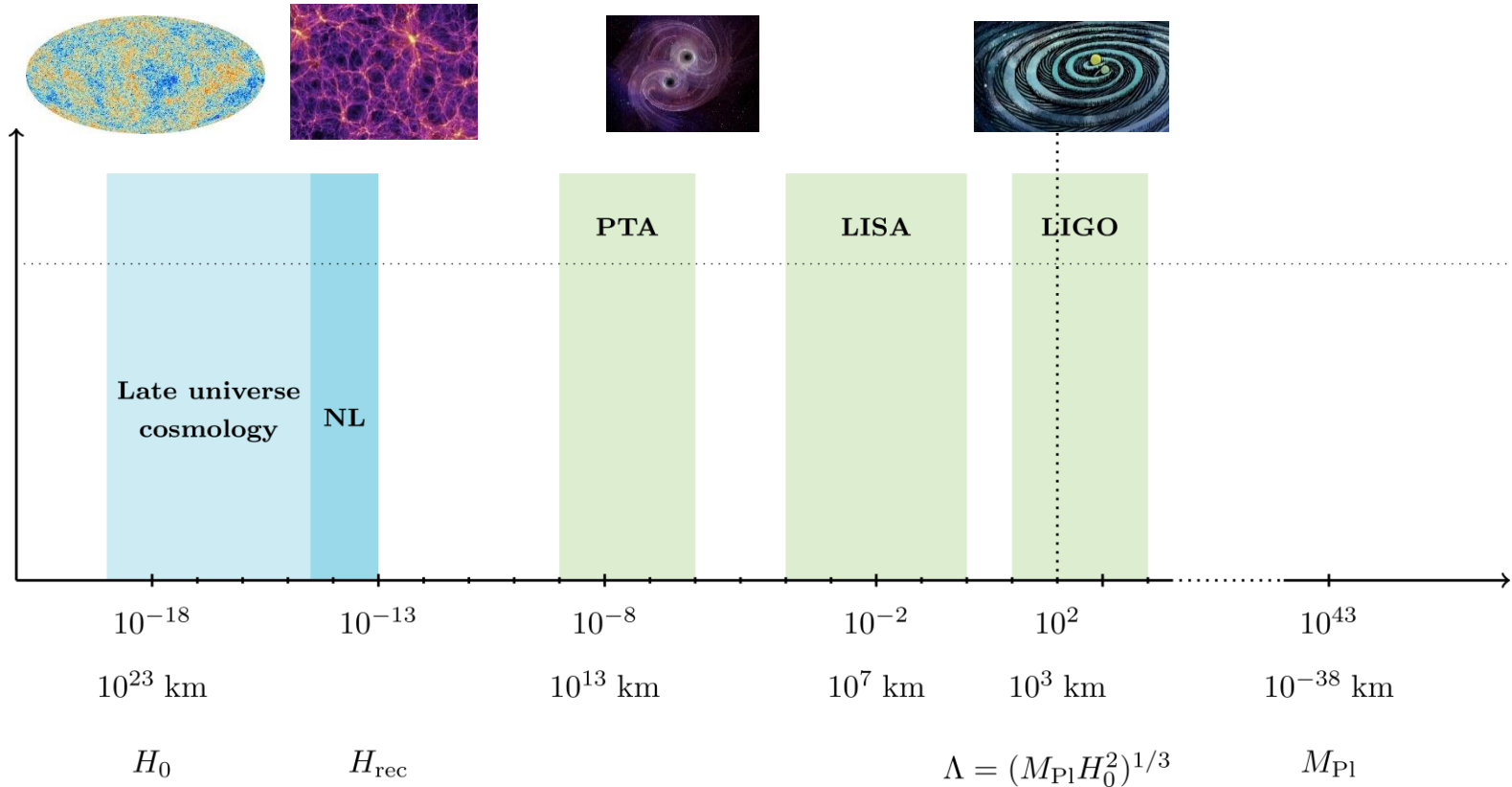
General Relativity:

$$\mathcal{A} \sim \left(\frac{E}{M_{\text{Pl}}} \right)^2 \sim \left(\frac{E}{10^{15} \text{ TeV}} \right)^2$$

Dark Energy EFT:

$$\mathcal{A} \sim \left(\frac{E}{10^{-12} \text{ eV}} \right)^6$$

Gravity across scales

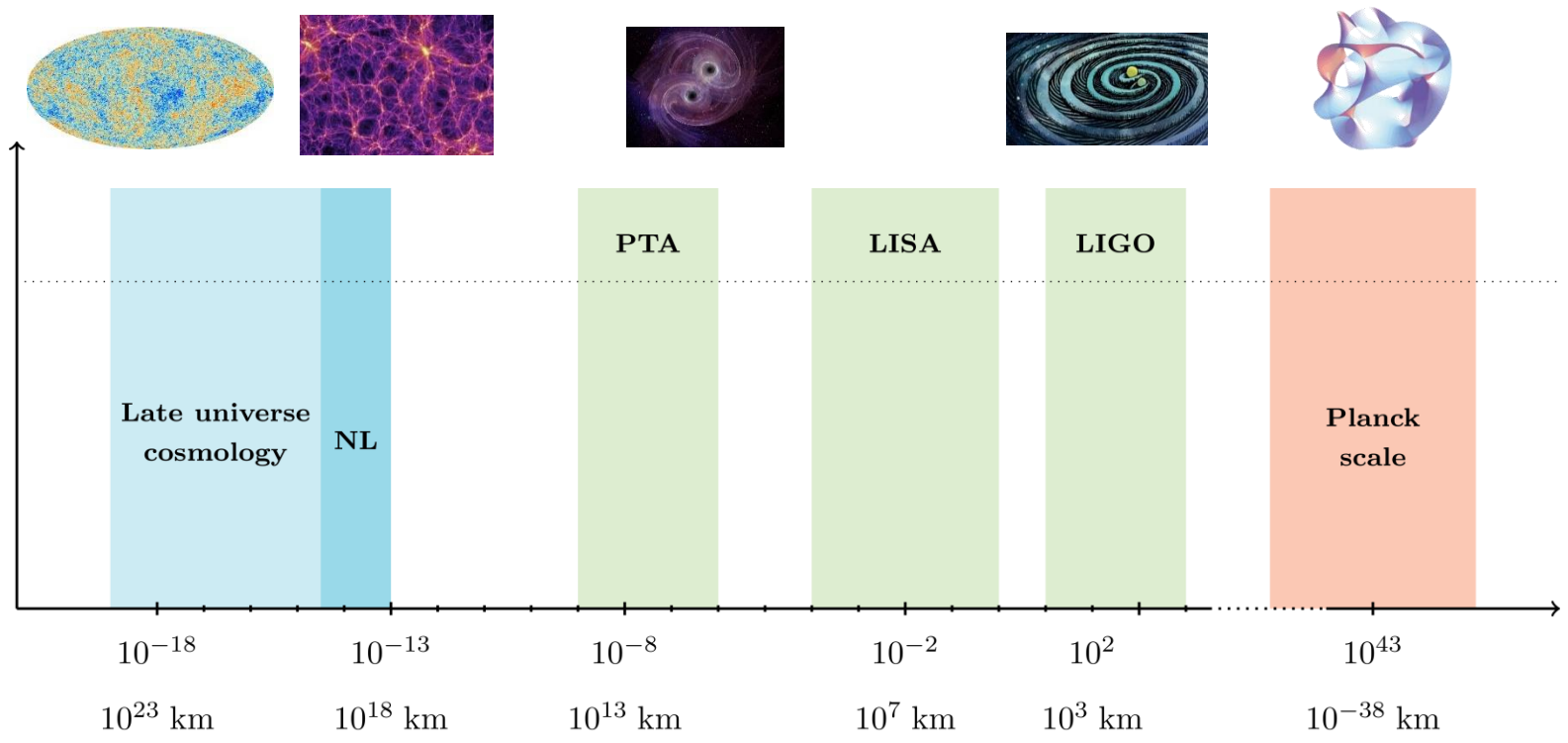


$$\mathcal{L} = -\frac{1}{2}(\nabla\phi)^2 + M_{\text{Pl}}^2 R + \frac{1}{\Lambda^6}(\nabla\phi)^2(\square\phi)^2 + \dots$$

Connecting LIGO and cosmological scales non-trivial

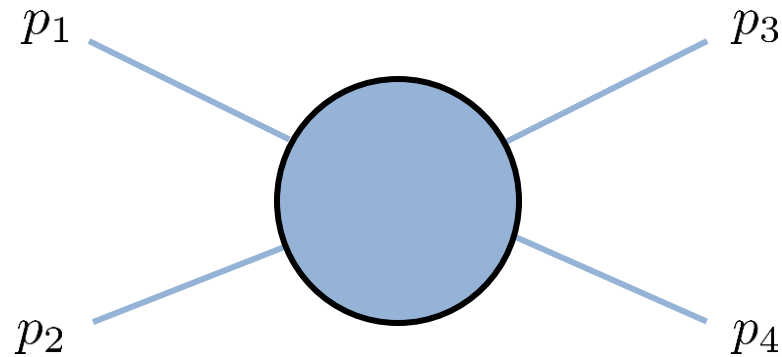
Raise cutoff + test dark energy with black holes

Gravity across scales



Positivity bounds

Theoretical bounds that any
unitary, local and causal
gravitational theory has to satisfy

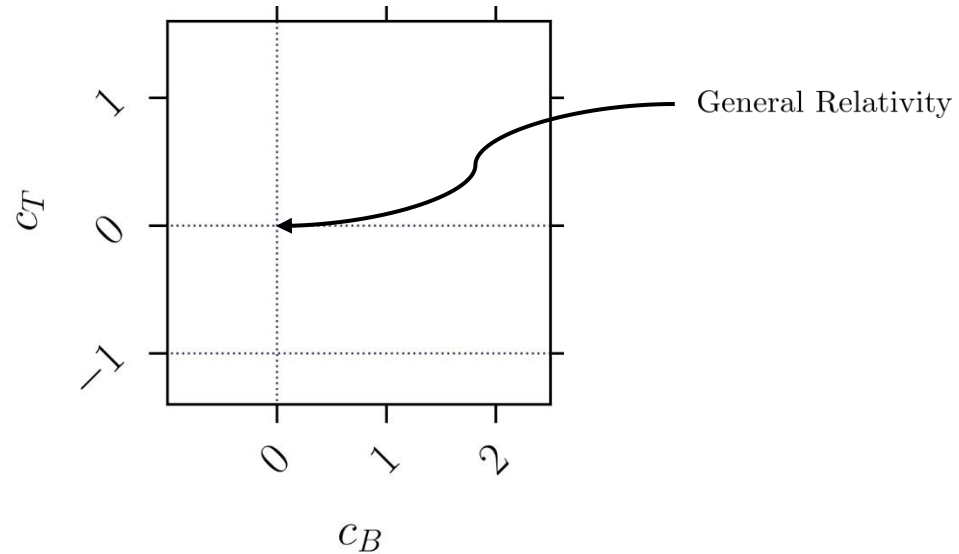


Scattering amplitude: $\mathcal{A} = c_{ss}s^2 + \dots$, where $s = -(p_1 + p_2)^2$

$$\underbrace{c_{ss}}_{\text{Cauchy's theorem}} = \frac{1}{2\pi i} \oint_{\mathcal{C}} ds \frac{\mathcal{A}(s)}{s^3} = \dots = \underbrace{\frac{4}{\pi} \int_0^\infty ds \frac{\sigma(s)}{s^2}}_{\text{positive(!)}}$$

A case study

GWs faster than photons
 ↑
 y-axis ~ what is the speed
 of gravitational waves?
 ↓
 Photons faster than GWs



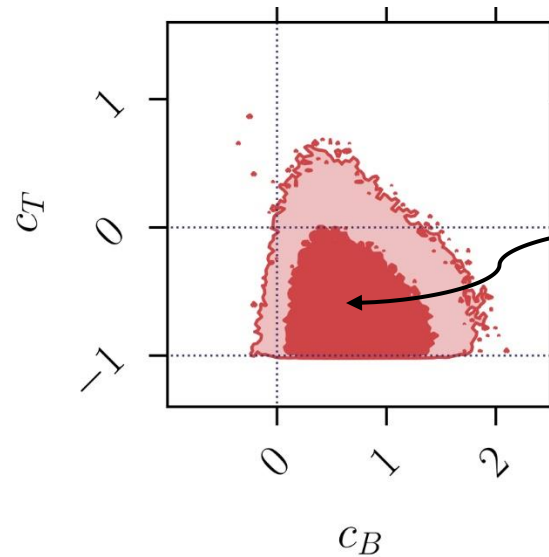
x-axis ~ how much does the graviton interact with DE scalar?

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where $G_i \equiv G_i(X)$ and $X \equiv -\frac{1}{2} \nabla^\mu \phi \nabla_\mu \phi$

A case study

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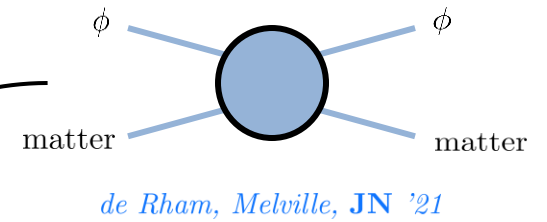
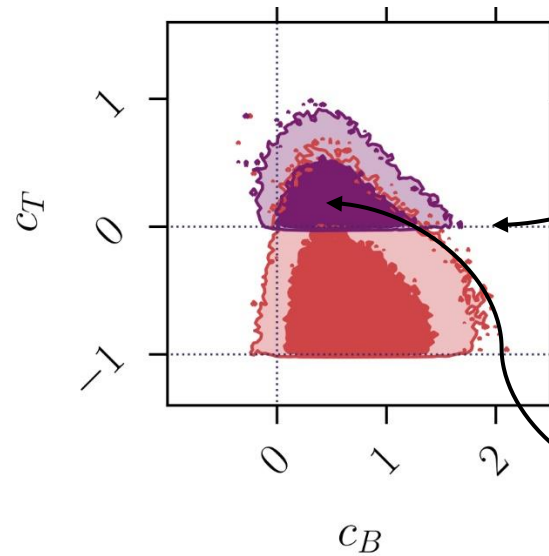


Data constraints from
CMB and LSS
JN, Nicola '18

x-axis ~ how much does the graviton interact with DE scalar?

A case study

GWs faster than photons
↑
y-axis ~ what is the speed
of gravitational waves?
↓
Photons faster than GWs

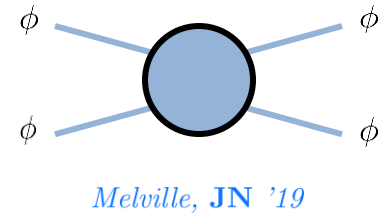
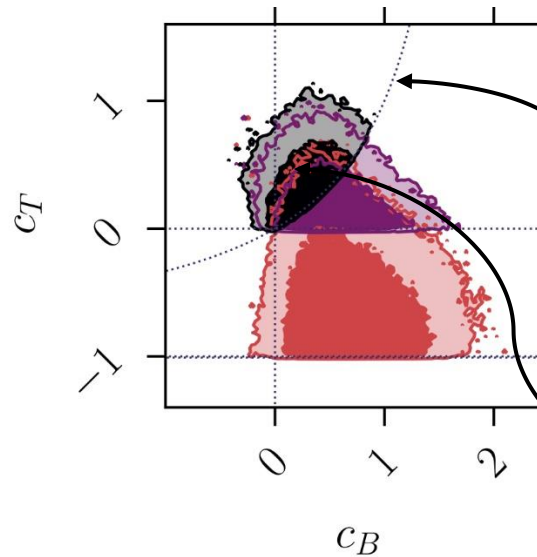


Data constraints with
this positivity prior

x-axis ~ how much does the graviton interact with DE scalar?

A case study

GWs faster than photons
↑
y-axis \sim what is the speed
of gravitational waves?
↓
Photons faster than GWs



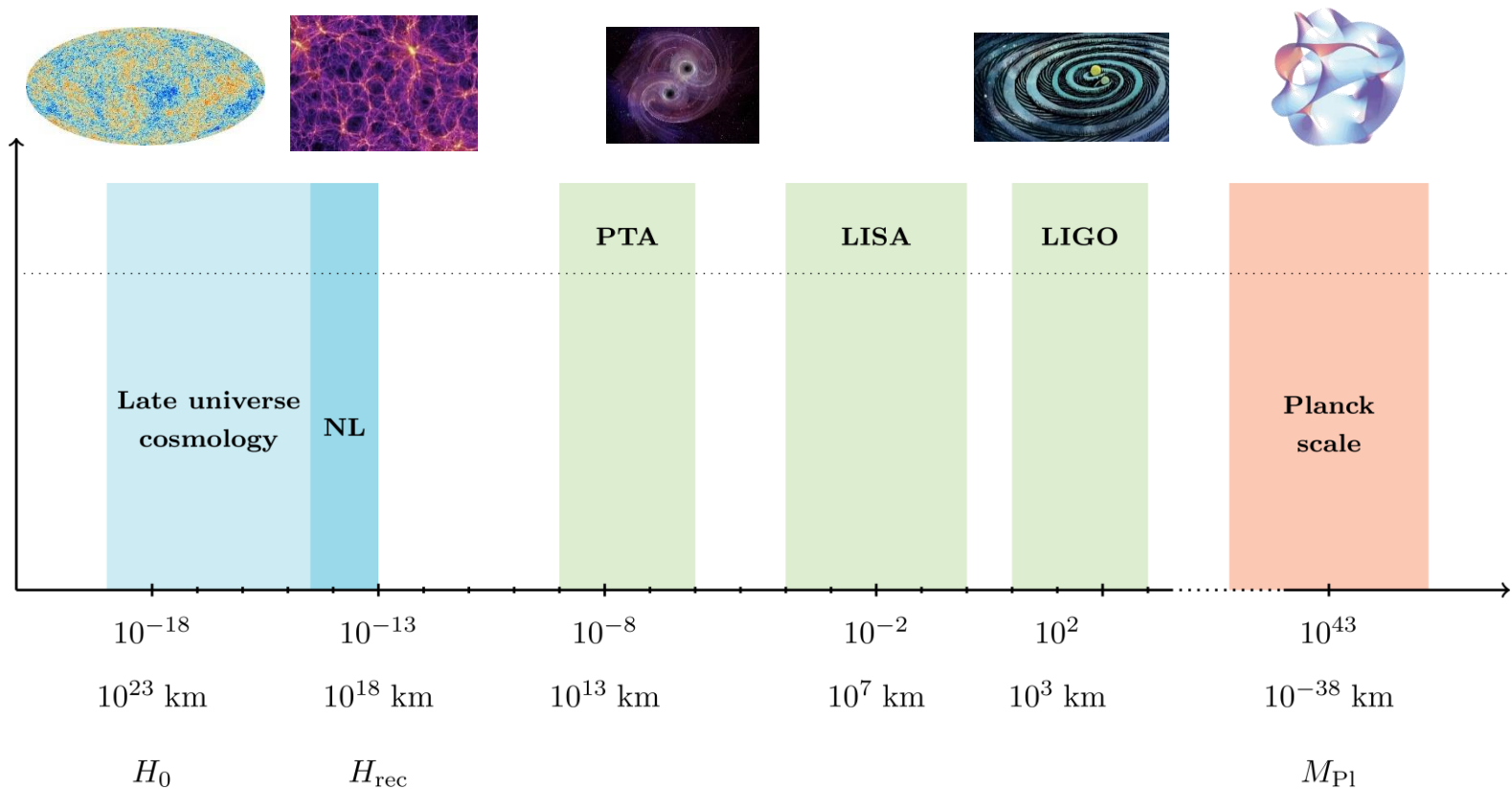
Data constraints with
both positivity priors

x-axis \sim how much does the graviton interact with DE scalar?

Key observations:

- Positivity priors tighten constraints.
- Physical vs. unphysical parameter space.
- Alternative perspective: IR test of UV physics.

Testing gravity on all scales



Thank you!